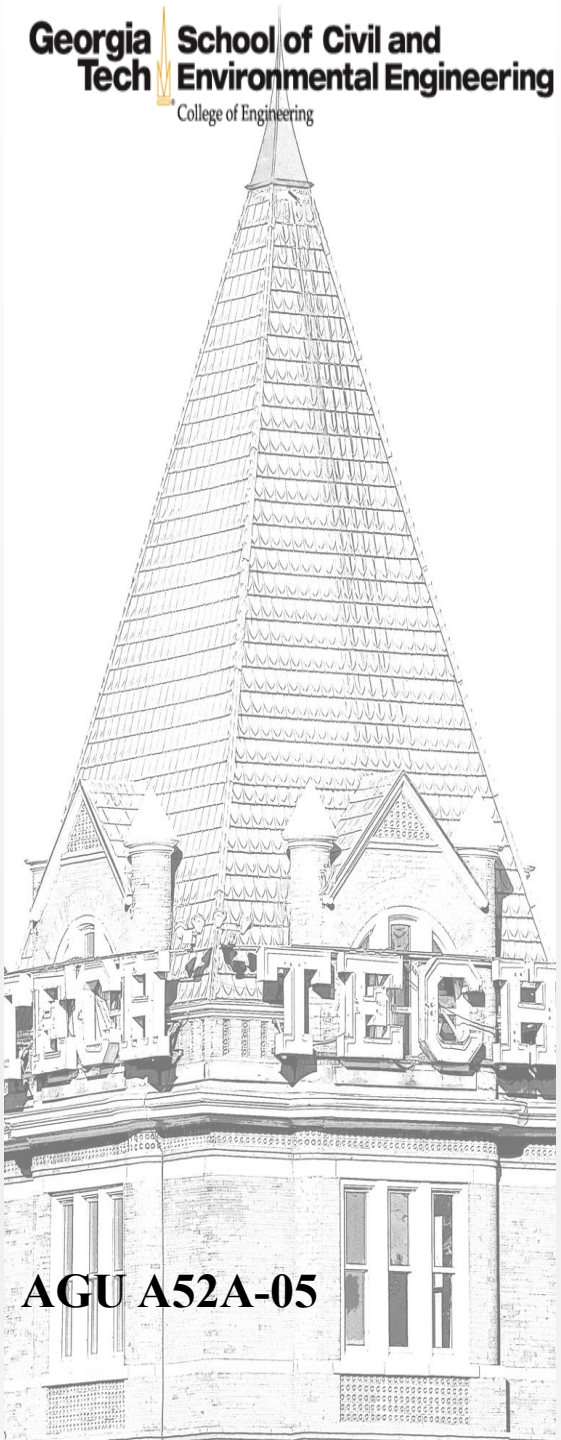




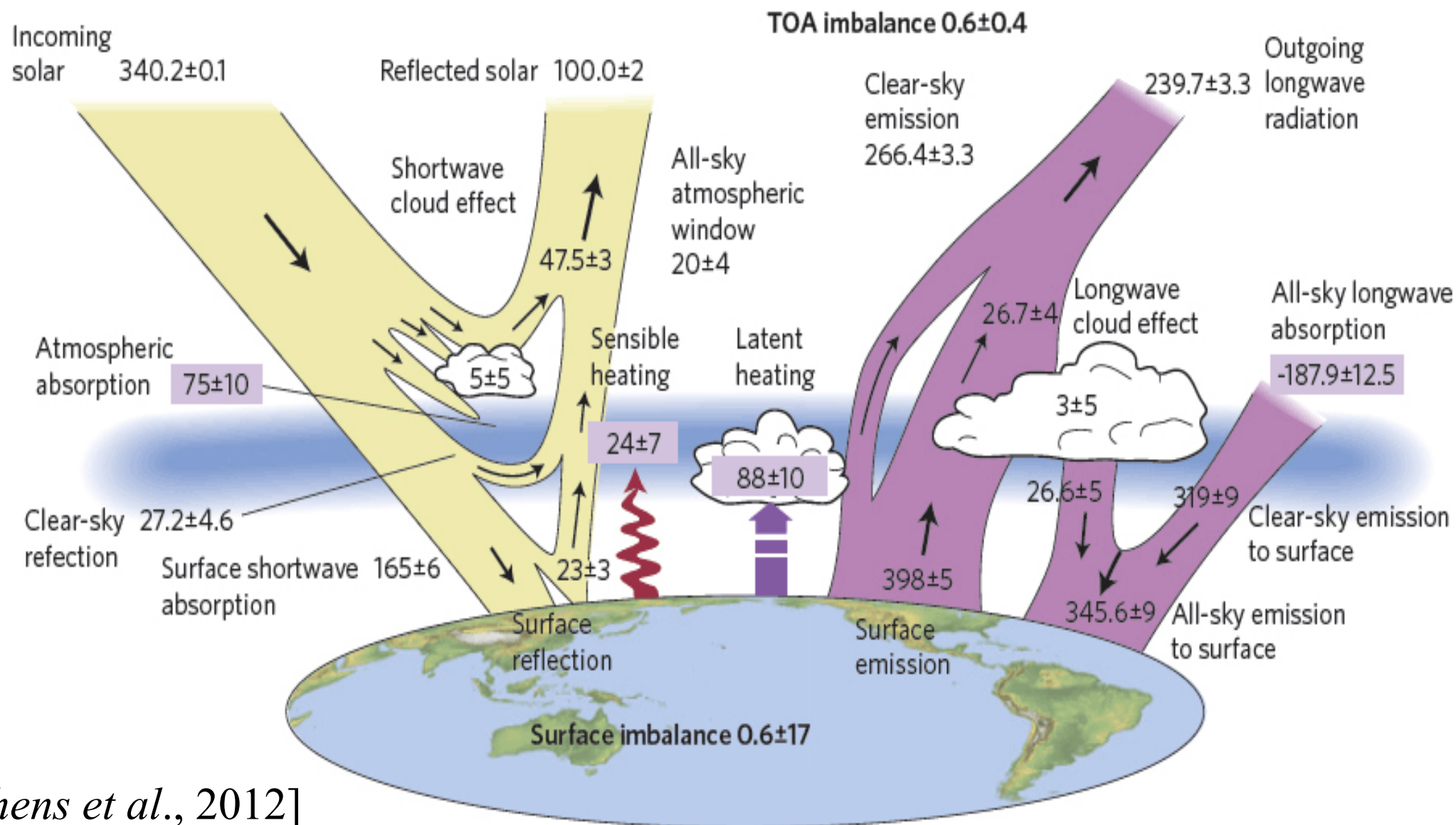
Maximum Entropy Production (MEP) Method for Modeling Surface Energy Budget --- Theory and Applications to Arctic Regions

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[Stephens et al., 2012]

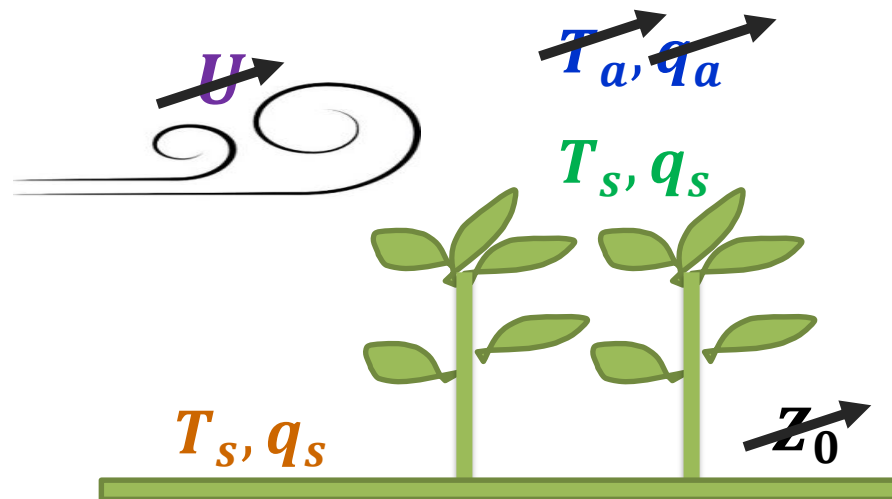


Goals

- Physically based for all types of surfaces (sea-ice, snow, vegetation, frozen ground)
- Closing energy budget at all space-time scales
- Reducing model inputs and parameters
- Using remote sensing data.

Maximum Entropy Production (MEP) Theory

- The Maximum Entropy Production (MEP) Model (Wang and Bras, 2009, 2011)
 - close surface energy budget automatically
 - does not use wind speed, air temperature and humidity, and surface roughness lengths explicitly
 - has reduced uncertainty in surface heat fluxes bounded by that of surface radiations.



- Model Formulation

$$\left[1 + B(\sigma) + \frac{B(\sigma)}{\sigma} \frac{I_s}{I_0} |H|^{-\frac{1}{6}} \right] H = R_n$$

$$E = B(\sigma)H$$

$$Q = R_n - E - H$$

with

$$\sigma = \frac{\lambda^2 q_s}{c_p R_v T_s^2}$$

$$B(\sigma) = 6 \left(\sqrt{1 + \frac{11}{36} \sigma} - 1 \right)$$

Land Surface

$$\min_{\{E, H, Q\}} \{I(E, H, Q) | E + H + Q = R_n\}$$

$$Q = \frac{B(\sigma)}{\sigma} \frac{I_s}{I_0} |H|^{-\frac{1}{6}} H$$

$$E = B(\sigma)H$$

$$E + H + Q = R_n$$

$$B(\sigma) = 6 \left(\sqrt{1 + \frac{11}{36} \sigma} - 1 \right), \quad \sigma = \sqrt{\alpha_K} \frac{\lambda^2}{c_p R_v} \frac{q_s}{T_s^2}$$

Water-Snow-Ice Surface

[Wang et al, 2014]

$$Q = \frac{B(\sigma)}{\sigma} \frac{I_{wsi}}{I_0} |H|^{-\frac{1}{6}} - R_n^S$$

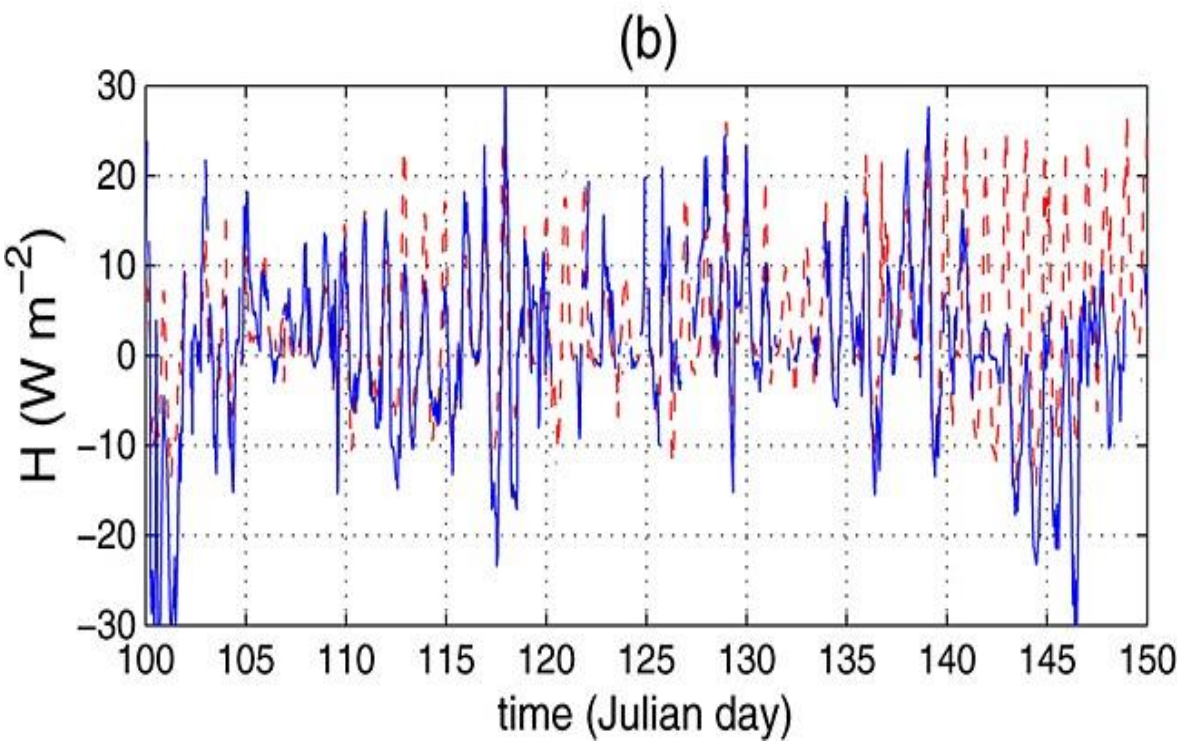
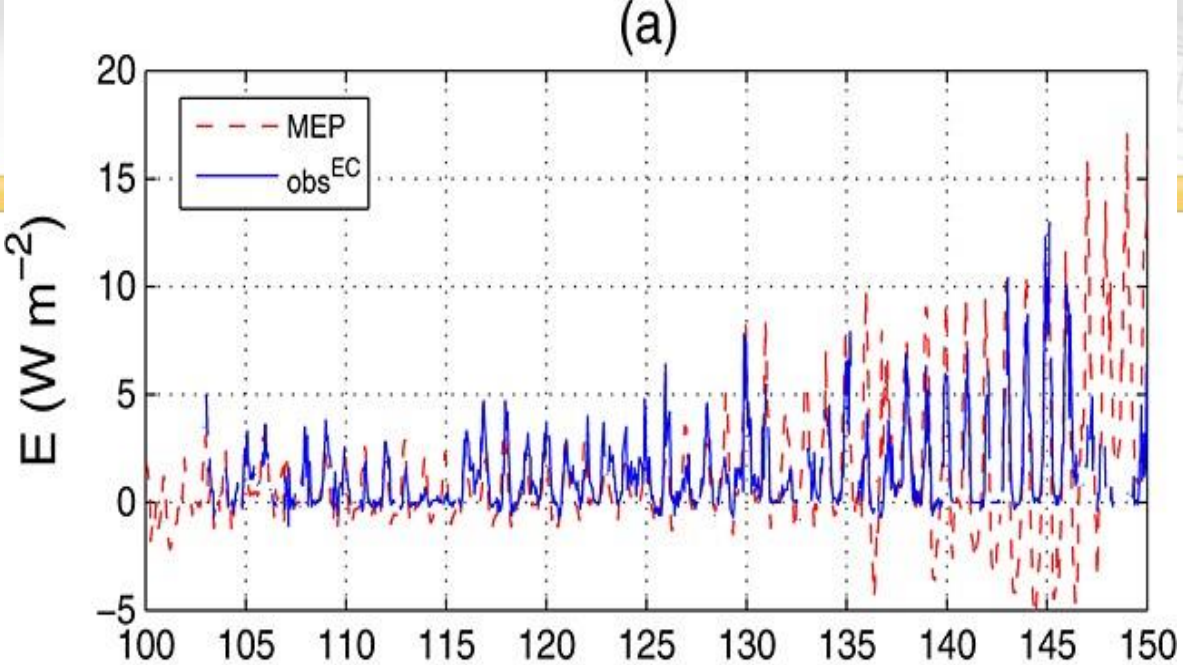
$$E = B(\sigma)H$$

$$E + H + Q = R_n^L$$

$$\sigma(T_s) = \sqrt{\alpha_K} \frac{\lambda^2}{c_p R_v} \frac{q_s^{sat}(T_s)}{T_s^2}$$

Fluxes	Surface Energy Budget	Bulk Variables	Model Parameters	Modeling Error
Bulk	not closed	temperature & moisture gradient	wind speed, roughness, etc.	semi-empirical (first order closure)
MEP	automatically closed	not used	not used	First-principles (MaxEnt, MEP, MOST)

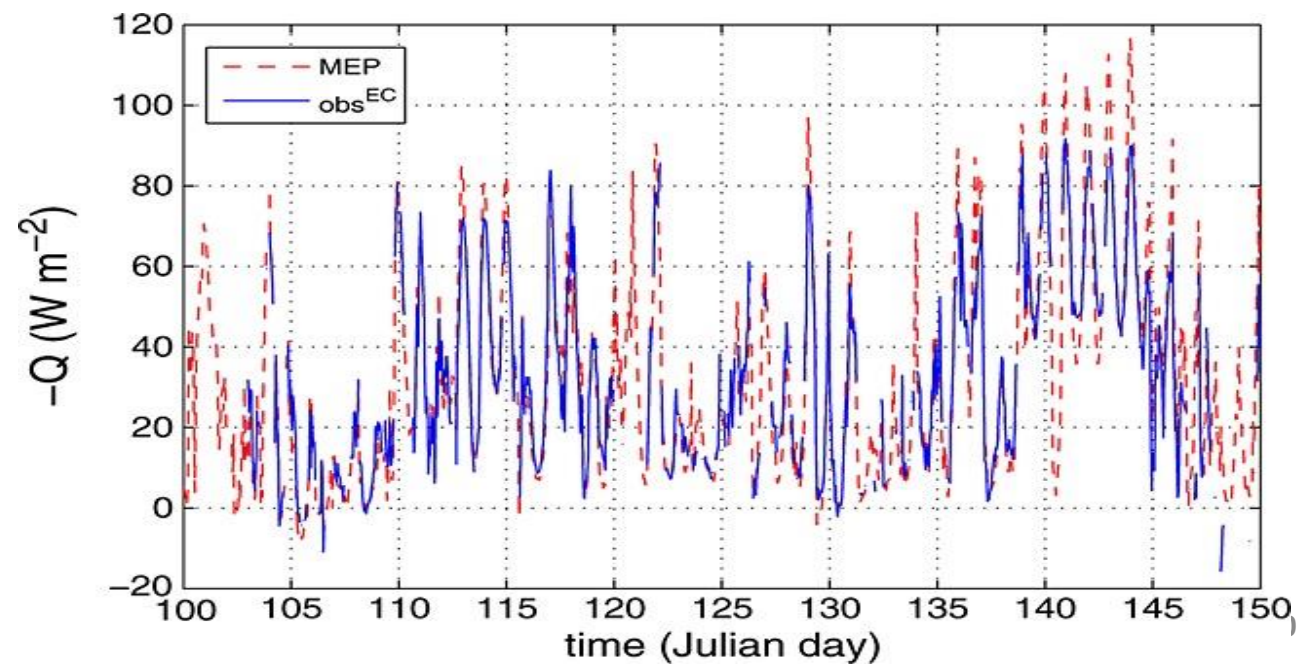
	Surface Energy Budget	Input data	Model Parameters	Modeling Error
Penman Method	Balanced	Air temperature, humidity, ground heat flux	Wind speed, roughness lengths, etc.	Semi-empirical (first order closure)
Bulk Method	Not balanced	Temperature & moisture gradient	Wind speed, roughness lengths, etc.	Semi-empirical (first order closure)
MEP Method	Balanced	Not used	Not used	First-principles (MaxEnt, MEP, MOST) constrained by radiation data



SHEBA field experiment
10 April to 30 May 1998

[*Wang et al.*, 2014]

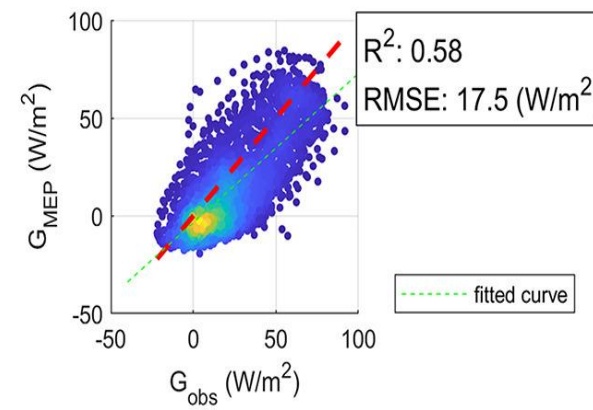
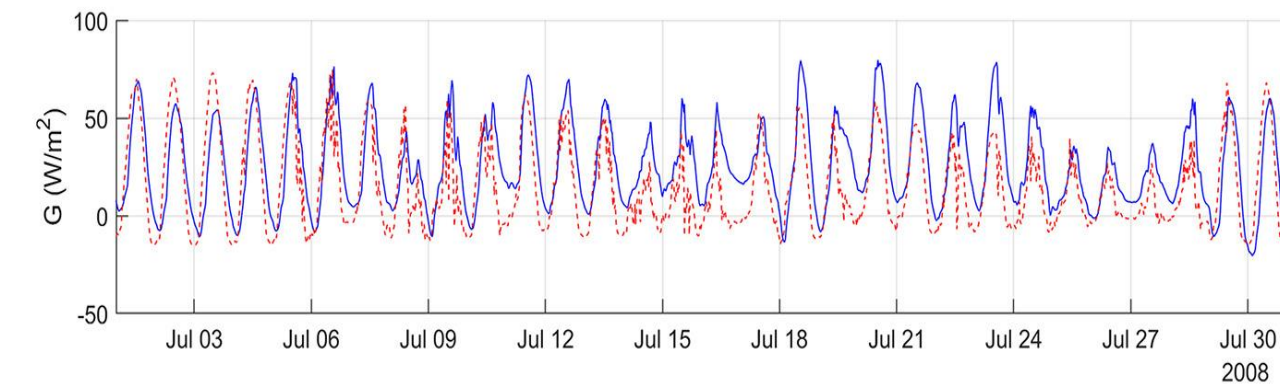
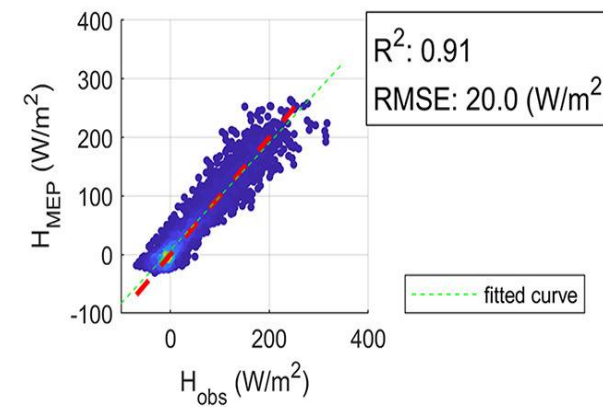
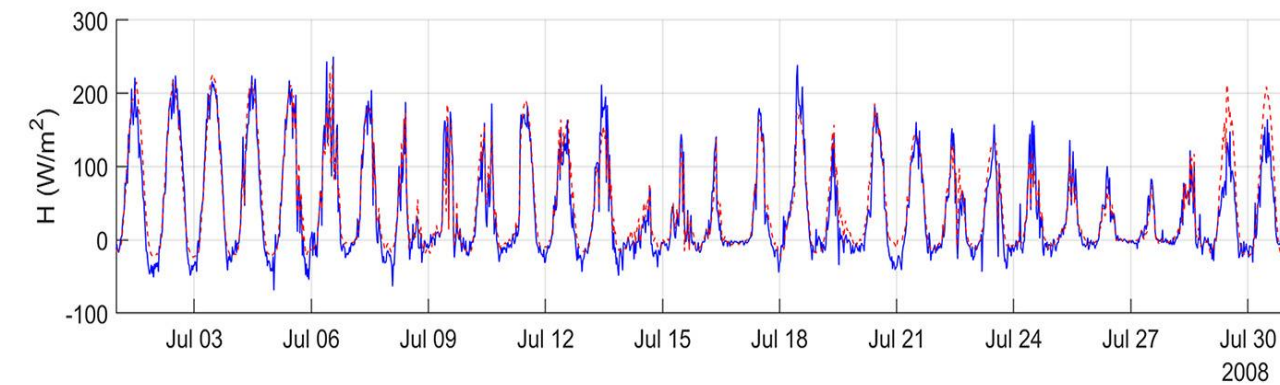
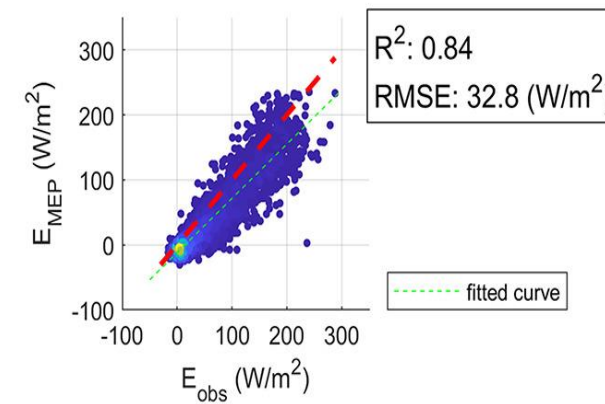
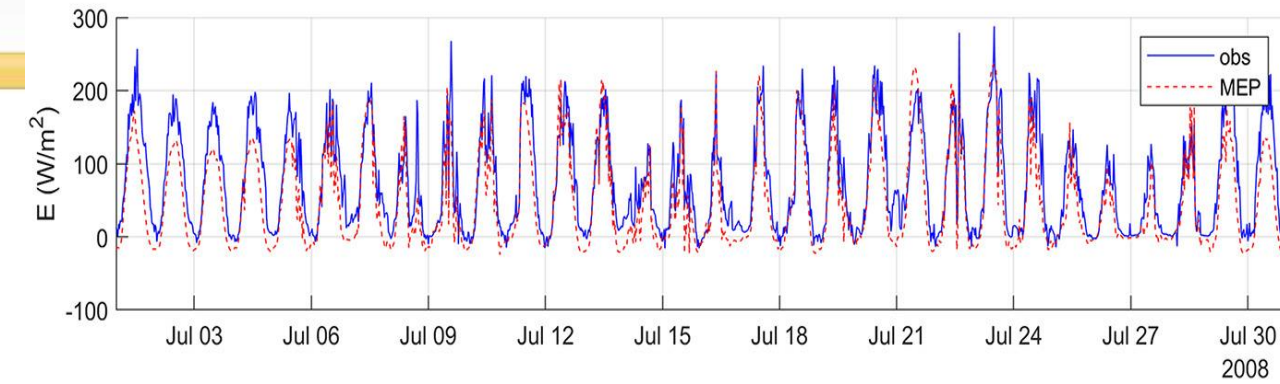
Sea Ice



Vorkuta, Russia

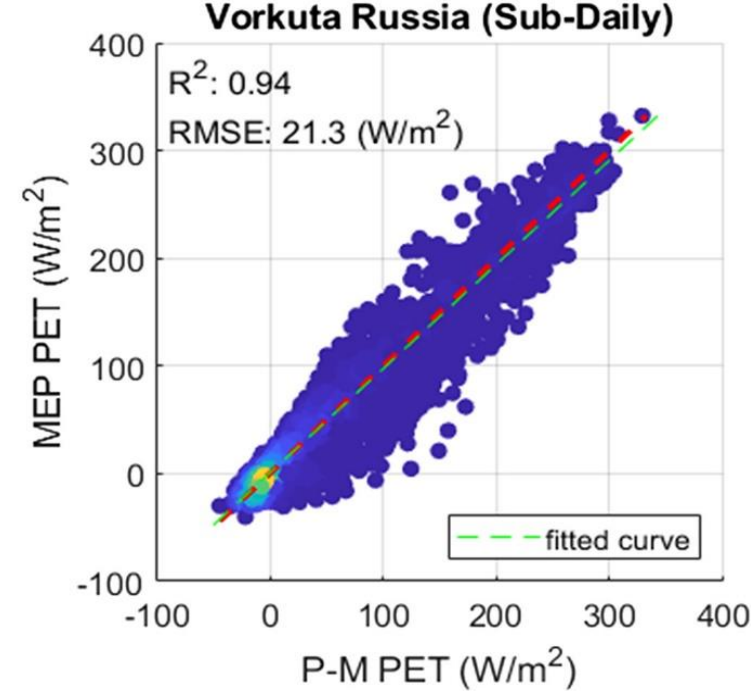
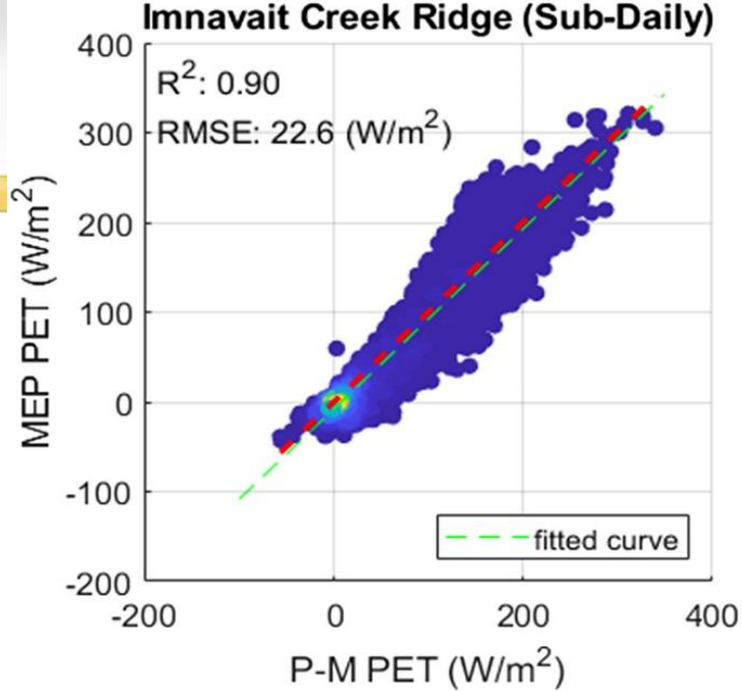


Frozen Ground (Permafrost)

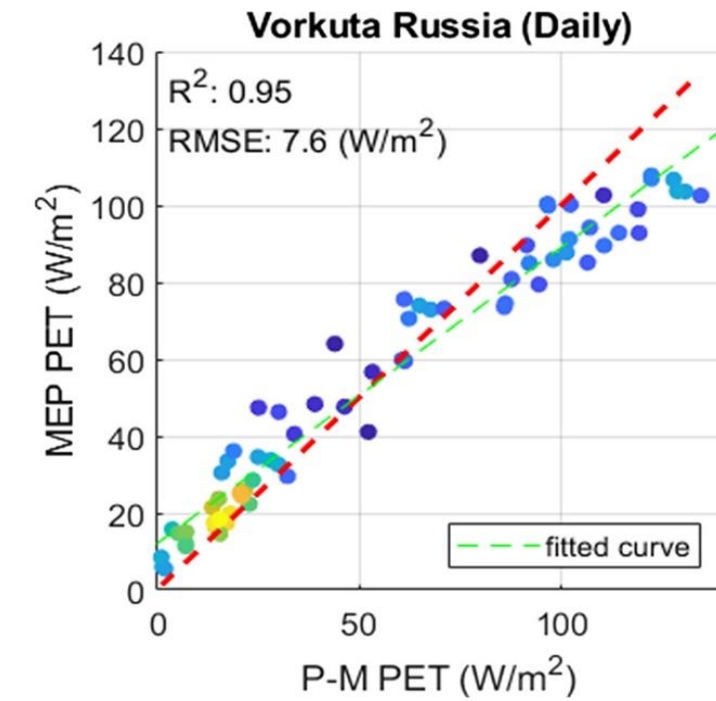
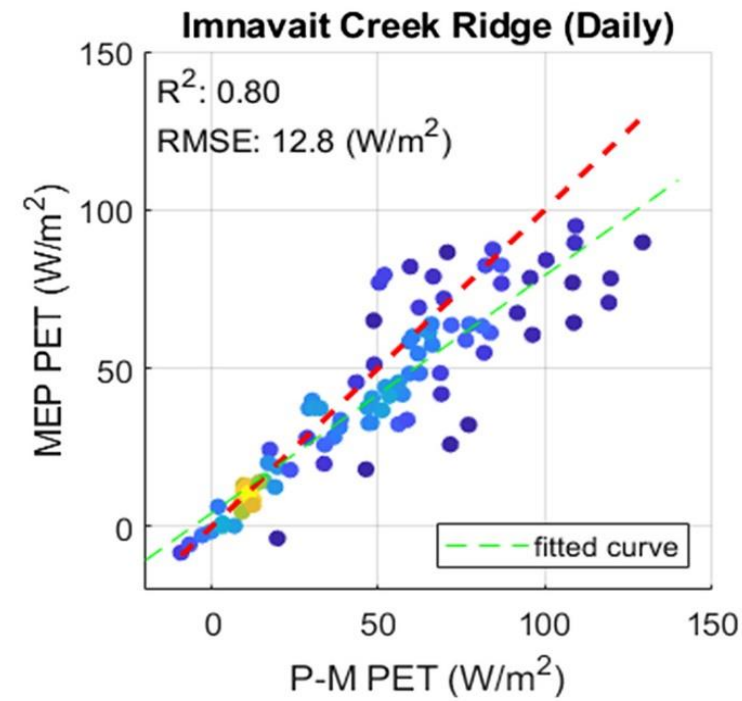


E : latent heat flux
 H : sensible heat flux
 G : ground heat flux

[El Sharif et al., 2019]



**Vegetation
(Tundra)**



PET; potential evapotranspiration
P-M: Penman-Monteith Model

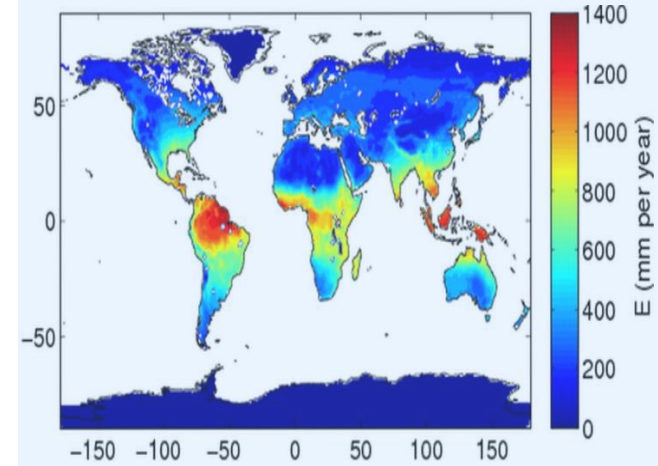
[*El Sharif et al.*, 2019]

Results

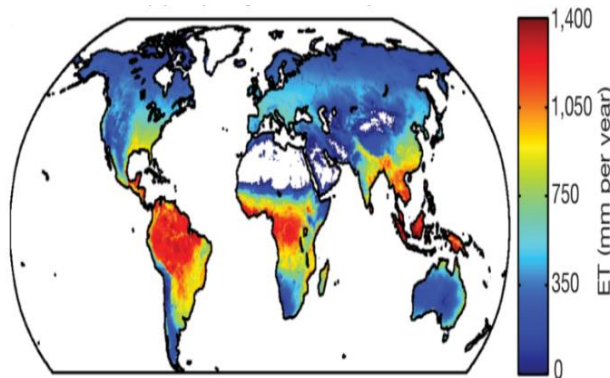
Climatology – Latent Heat Flux

Model Inputs

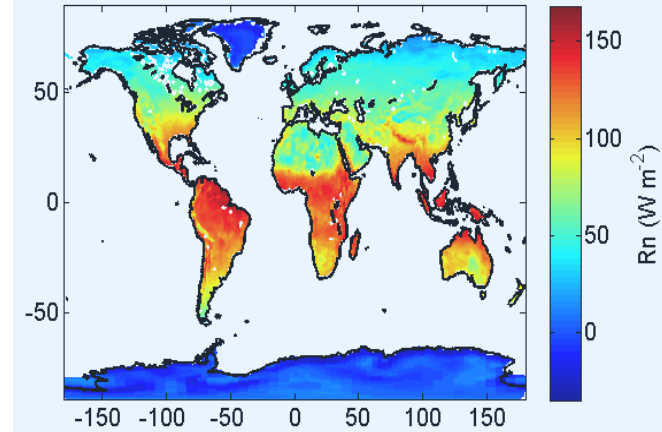
E (MEP)



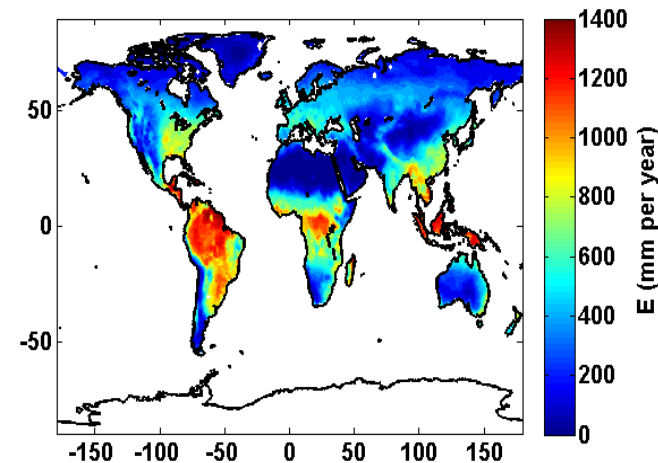
E (Jung et al., 2010)



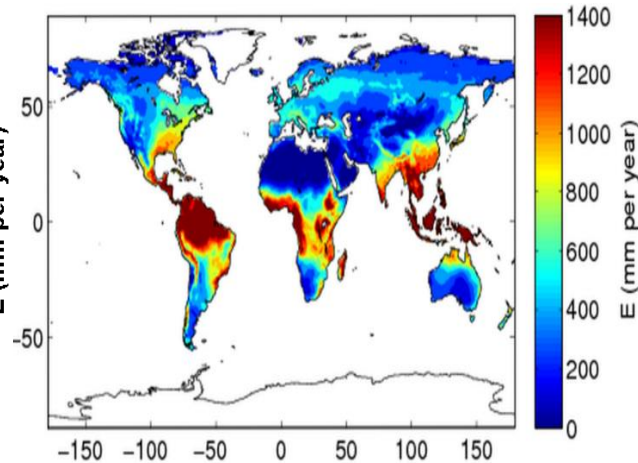
R_n (CERES)



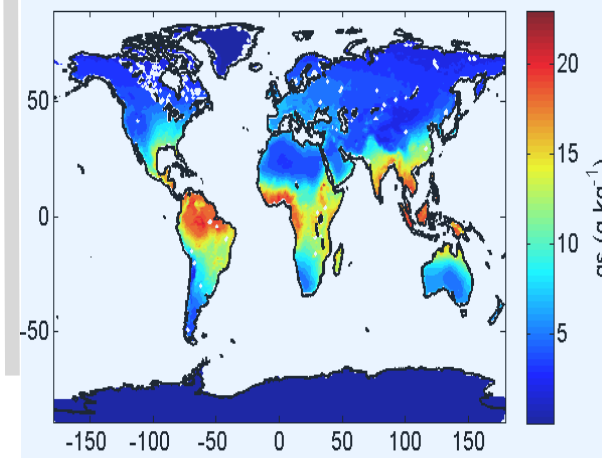
E (GLDAS)



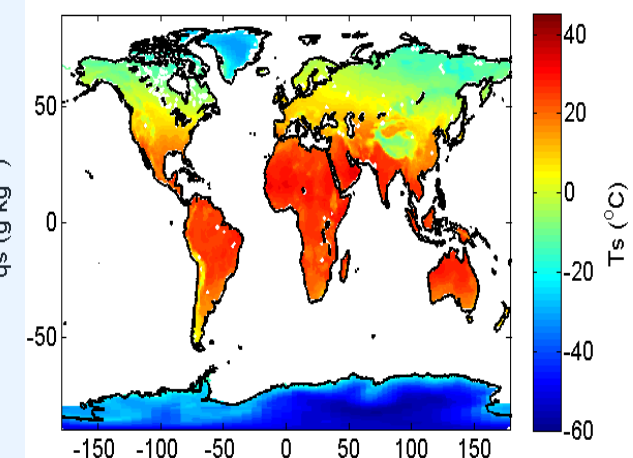
E (MERRA)



q_s (MERRA)



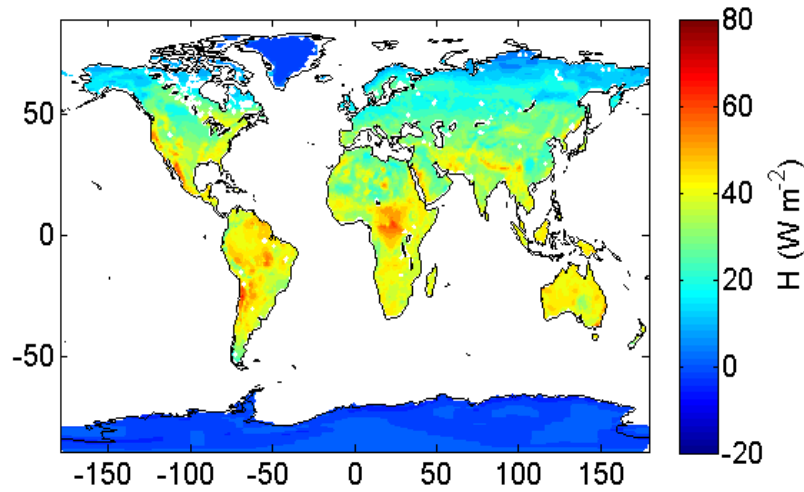
T_s (CERES)



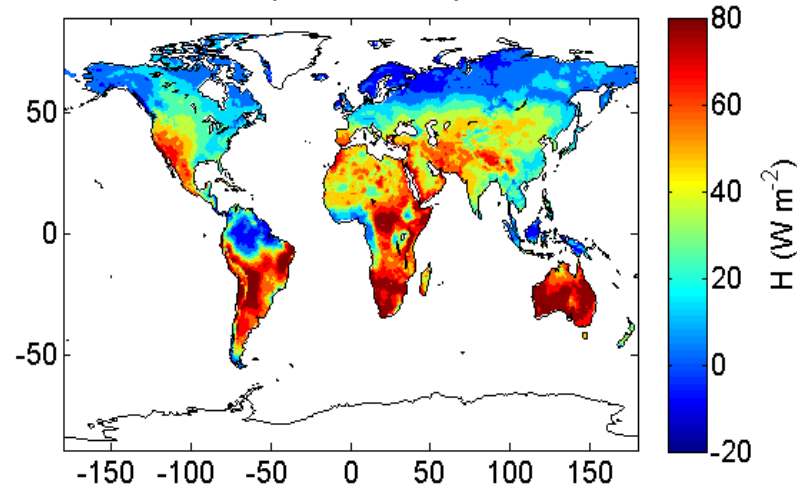
Results

Climatology – Sensible and Ground Heat Fluxes

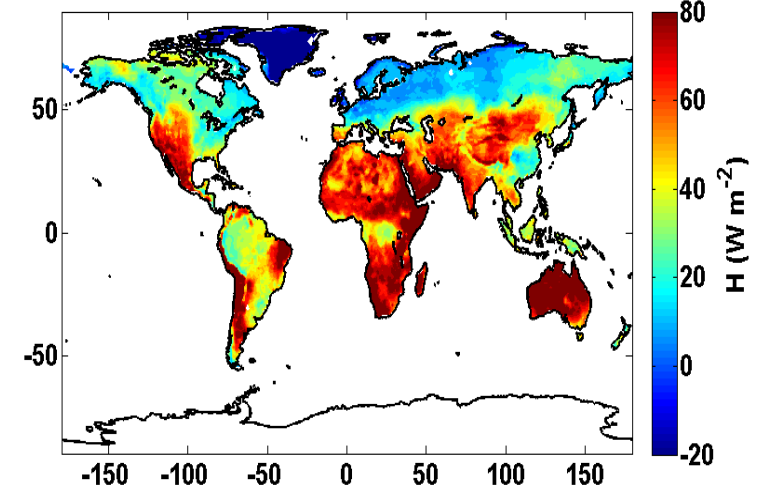
H (MEP)



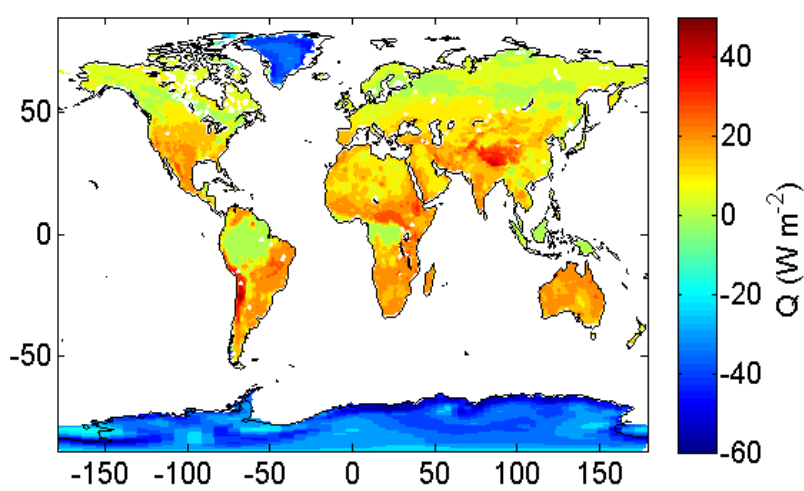
H (MERRA)



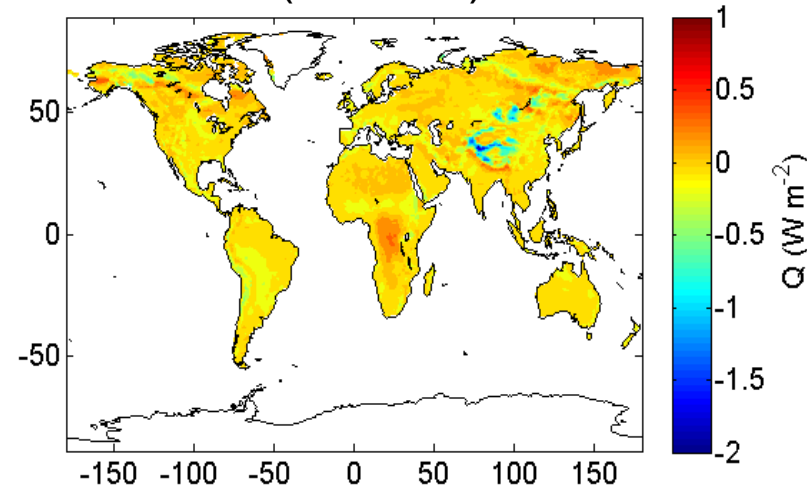
H (GLDAS)



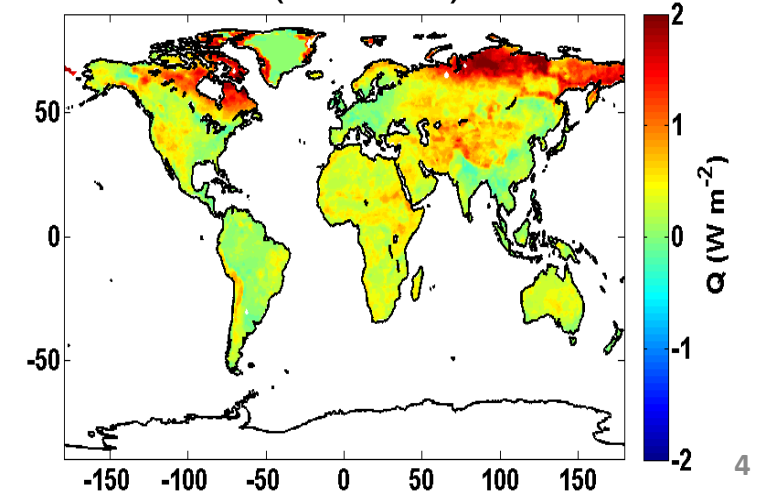
Q (MEP)



Q (MERRA)



Q (GLDAS)



Methodology – The MEP Model

Methodology – The MEP Model

- The trends of global land evapotranspiration are positive ($0.41 \pm 0.23 \text{ W m}^{-2} \text{ yr}^{-1}$) attributed to the increase of surface radiation energy and humidity.
- The trends of sensible heat flux are positive globally but statistically insignificant ($0.18 \pm 0.18 \text{ W m}^{-2} \text{ yr}^{-1}$).
- The ground heat flux over continents has positive trend ($0.21 \pm 0.16 \text{ W m}^{-2} \text{ yr}^{-1}$) during the model period driven by increase of surface radiation.
- The surplus surface radiation energy is mostly used to increase evapotranspiration.
- The sensible heat flux and surface temperature have opposite trends.