Generated using the official AMS $\ensuremath{ \mbox{LAT}}\xspace_EX$ template v5.0

1	Using climate model simulations to constrain observations
2	Benjamin D. Santer ^{<i>a</i>,*} , Stephen Po-Chedley ^{<i>a</i>} , Carl Mears ^{<i>b</i>} , John C. Fyfe ^{<i>c</i>} , Nathan Gillett ^{<i>c</i>} , Qiang
3	Fu ^d , Jeffrey F. Painter ^a , Susan Solomon ^e , Andrea K. Steiner ^f , Frank J. Wentz ^b , Mark D.
4	Zelinka ^{<i>a</i>} , and Cheng-Zhi Zou ^{<i>g</i>}
5	^a Program for Climate Model Diagnosis and Intercomparison, Lawrence Livermore National
6	Laboratory, Livermore, CA 94550, USA.
7	^b Remote Sensing Systems, Santa Rosa, CA 95401, USA.
8	^c Canadian Centre for Climate Modelling and Analysis, Environment and Climate Change
9	Canada, Victoria, British Columbia, V8W 2Y2, Canada.
10	^d Dept. of Atmospheric Sciences, University of Washington, Seattle, WA 98195, USA.
11	^e Massachusetts Institute of Technology, Earth, Atmospheric, and Planetary Sciences, Cambridge,
12	MA 02139, USA.
13	^f Wegener Center for Climate and Global Change, University of Graz, A-8010 Graz, Austria.
14	^g Center for Satellite Applications and Research, NOAA/NESDIS, Camp Springs, Maryland
15	20746, USA.

¹⁶ **Corresponding author*: santer1@llnl.gov.

ABSTRACT

We compare atmospheric temperature changes in satellite data and in older and newer multi-model 17 and single-model ensembles performed under phases 5 and 6 of the Coupled Model Intercomparison 18 Project (CMIP5 and CMIP6). In the lower stratosphere, multi-decadal stratospheric cooling during 19 the period of strong ozone depletion is smaller in newer CMIP6 simulations than in CMIP5 or 20 satellite data. In the troposphere, however, despite differences in the forcings and climate sensitivity 21 of the CMIP5 and CMIP6 ensembles, their ensemble-average global warming over the satellite 22 era is remarkably similar. We also examine four well-understood properties of tropical behavior 23 governed by basic physical processes. The first three properties are ratios between trends in water 24 vapor (WV) and trends in sea surface temperature (SST), the temperature of the lower troposphere 25 (TLT), and the temperature of the mid- to upper troposphere (TMT). The fourth property is the ratio 26 between TMT and SST trends. All four trend ratios are tightly constrained in CMIP simulations. 27 Observed ratios diverge markedly when calculated with SST, TLT, and TMT trends produced by 28 different groups. Observed data sets with larger warming of the tropical ocean surface and tropical 29 troposphere yield atmospheric moistening that is closer to model results. For the TMT/SST ratio, 30 model-data consistency depends on the selected combination of observed data sets used to estimate 31 TMT and SST trends. If model expectations of these four covariance relationships are realistic, 32 one interpretation of our findings is that they reflect a systematic low bias in satellite tropospheric 33 temperature trends. Alternately, the observed atmospheric moistening signal may be overestimated. 34 Given the large structural uncertainties in observed tropical TMT and SST trends, and because 35 satellite WV data are available from one group only, it is difficult to determine which interpretation 36 is more credible. Nevertheless, our analysis illustrates the diagnostic power of simultaneously 37 considering multiple complementary variables and points towards possible problems with certain 38 observed data sets. 39

40 **1. Introduction**

Since publication of the first assessment report of the Intergovernmental Panel on Climate Change 41 (IPCC) in 1990, there have been major improvements in our ability to model the climate system 42 (Randall et al. 2007; Trenberth et al. 2007; Flato et al. 2013; Hartmann et al. 2013). Thirty 43 years ago, the climate science community performed single simulations with a small number of 44 pioneering atmosphere-ocean models. Today, more complex Earth System Models (ESMs) are 45 used to generate large multi-model and single-model ensembles of simulations (Kay et al. 2015; 46 Fyfe et al. 2017; Eyring et al. 2019; Deser et al. 2020). Standard benchmark simulations, performed 47 repeatedly with improved versions of uncoupled and coupled models, have over the last several 48 decades exposed and in some cases reduced systematic errors in model representation of many 49 different aspects of Earth's climate (Gates et al. 1999; Randall et al. 2007; Flato et al. 2013; Sperber 50 et al. 2013; Bellenger et al. 2014). 51

In tandem with advances in modeling, there have been improvements in the forcings used in model simulations of historical climate change (Solomon et al. 2011; Fyfe et al. 2013; Schmidt et al. 2014; Checa-Garcia et al. 2018). Observations have also improved with advances in the ability of scientists to identify and adjust for non-climatic effects (Wentz and Schabel 1998; Mears et al. 2003; Fu and Johanson 2005; Mears and Wentz 2005; Karl et al. 2006, 2015; Po-Chedley et al. 2015). This evolution of models, forcings, and observations is ongoing.

The last IPCC assessment report, published in 2013, relied on CMIP5 simulations performed with roughly four dozen models (Taylor et al. 2012). The 2021 IPCC assessment will evaluate output from a larger collection of CMIP6 models and an expanded set of experiments (Eyring et al. 2016, 2019). Our interest here is in comparing atmospheric temperature changes in CMIP5, CMIP6, the latest satellite data (Mears and Wentz 2017; Zou and Wang 2011; Spencer et al. 2017), and a state-of-the-art reanalysis of weather observations with a weather forecast model (Simmons et al. 2020). We seek to determine whether: 1) there are important differences between atmospheric temperature changes in CMIP5 and CMIP6; and 2) models and observations show consistency in theoretically and physically based constraints on tropical behavior – the amplification of tropical warming with increasing height, and the ratios between trends in tropical water vapor and trends in temperature at different levels. We show that the combination of these constraints provides new information on model/data consistency.

There are several reasons for our focus on atmospheric temperature. First, discrepancies between 70 modeled and observed atmospheric temperature changes have received scientific and political at-71 tention for over 20 years (NRC 2000; Karl et al. 2006; Thorne et al. 2011; Fu et al. 2011; Po-Chedley 72 and Fu 2012; US Senate 2015; Santer et al. 2017a,b; Po-Chedley et al. 2021). Determining the 73 causes of these differences remains a priority. Second, estimates of atmospheric temperature from 74 satellites have recently undergone important revision, primarily due to improved understanding of 75 the effects of drifts in satellite orbits and instrument calibration (Po-Chedley et al. 2015; Mears and 76 Wentz 2016, 2017; Zou and Qian 2016; Zou et al. 2018; Spencer et al. 2017). Reanalysis models 77 and data assimilation systems have also evolved (Hersbach et al. 2020; Simmons et al. 2020). 78 Our goal is to reassess model-data consistency in the light of these improvements to observations, 79 models, and external forcings. 80

The structure of our paper is as follows. Sections 2 and 3 introduce the observational and model data analyzed in our study. Section 4 discusses basic features of atmospheric temperature time series and trends. Trend comparisons are over the full satellite era and over periods of stratospheric ozone depletion and recovery. Section 5 examines the relative sizes of forced and unforced temperature changes on different timescales, and considers whether observed changes are consistent with results from the forced simulations. The statistical methodology in Section 5 follows Santer et al. (2011)

and is provided in the Supplementary Materials (SM) with only minor modifications. Section 87 6 focuses on the covariability of different aspects of tropical climate change. We examine ratios 88 between tropical trends in column-integrated water vapor (WV) and sea surface temperature (SST), 89 WV and the temperature of the lower troposphere (TLT), WV and the temperature of the mid-90 to upper troposphere (TMT), and TMT and SST. These four ratios are compared in observations 91 and multi-model and single-model ensembles. Prospects for using such covariability information 92 to constrain divergent observations are considered in Section 7. Appendices A and B provide 93 information regarding the calculation of synthetic satellite temperatures and the adjustment of 94 tropospheric temperature for stratospheric cooling influence. 95

2. Observational data

⁹⁷ a. Satellite temperature data

Since late 1978, NOAA polar-orbiting satellites have monitored the microwave emissions from oxygen molecules using the Microwave Sounding Unit (MSU) and the Advanced Microwave Sounding Unit (AMSU; Mears and Wentz 2017; Spencer et al. 2017; Zou et al. 2018). Microwave emissions are proportional to the temperature of broad atmospheric layers. By measuring at different microwave frequencies, MSU and AMSU provide estimates of TLT, TMT, and the temperature of the lower stratosphere (TLS).

We analyze TLS and TMT data sets produced by RSS (Mears and Wentz 2016), STAR (Zou and Qian 2016), and UAH (Spencer et al. 2017). Only RSS and UAH supply TLT measurements. We rely on the most recent data set versions: RSS 4.0, STAR 4.1, and UAH 6.0. The University of Washington (UW) also produces a TMT data set, but this is available for the tropics only (Po-Chedley et al. 2015). We did not use UW TMT data for the present study.

109	We consider three different versions of the RSS atmospheric temperature data. As noted in
110	Mears and Wentz (2017), "a total of nine MSU instruments cover the period from 1978 to 2005,
111	followed by a series of AMSU instruments that began in mid-1998 and continue to the present".
112	MSU and AMSU do not measure at the same microwave frequencies; different plausible choices
113	can be made in merging their estimated brightness temperatures.
114	Mears and Wentz (2016) employed three approaches to merge MSU and AMSU data:
115	1. MSU and AMSU measurements were used during the merge period from mid-1998 to 2003.
116	2. Only AMSU data were used after 1999. MSU data were excluded after 1999.
117	3. MSU data were used after 1999. AMSU data were excluded before 2003.
118	These approaches are referred to subsequently as "baseline", "AMSU merge", and "MSU merge"
119	(respectively), and are described in more detail in the SM. In Sections 5 and 6, we address the
120	question of whether these three RSS data sets yield different statistical inferences regarding the
121	correspondence between simulated and observed measures of climate change.
122	All satellite temperature data sets analyzed here are in the form of monthly means on the same
123	$2.5^{\circ} \times 2.5^{\circ}$ latitude/longitude grid. Near-global averages of TLS, TMT and TLT were calculated
124	over areas of common coverage in the RSS, UAH, and STAR datasets (82.5°N to 82.5°S for
125	TLS and TMT, and 82.5°N to 70°S for TLT). At the time this analysis was performed, satellite
126	temperature data for full 12-month years were available for the 492-month period from January
127	1979 to December 2019.

128 *b. SST data*

¹²⁹ Section 6 considers two ratio statistics involving SST. The first is $R_{\{WV/SST\}}$, the ratio between ¹³⁰ tropical trends in WV and SST (Wentz and Schabel 2000; Held and Soden 2006; Mears et al.

131	2007; Mears and Wentz 2016). The second is $R_{\text{TMT/SST}}$, the ratio of tropical TMT and SST trends
132	(Wentz and Schabel 2000; Santer et al. 2005; Po-Chedley et al. 2015). We seek to determine
133	whether simulated and observed values of these ratio statistics are consistent, and how model-data
134	agreement is affected by structural uncertainty in observed SST data. This uncertainty arises from
135	differences in raw data, the methods used to adjust raw data for known inhomogeneities, treatment
136	of sea ice, and the decisions made in merging information from ship-based measurements, buoys,
137	floats, and satellites (Karl et al. 2006, 2015; Morice et al. 2012; Hausfather et al. 2017). We quantify
138	structural uncertainty in SST data by calculating $R_{\{WV/SST\}}$ and $R_{\{TMT/SST\}}$ with four commonly
139	used observational records (Po-Chedley et al. 2021):

- Version 2 of the Centennial In Situ Observation-Based Estimates of the Variability of SST
 and Marine Meteorological Variables (COBE; Hirahara et al. 2014).
- ¹⁴² 2. Version 5 of the NOAA Extended Reconstructed SST data set (ERSST; Huang et al. 2017).
- ¹⁴³ 3. Version 1 of the Hadley Center Sea Ice and SST data set (HadISST; Rayner et al. 2003).
- 4. Version 3 of the Hadley Center SST data set (HadSST; Kennedy et al. 2011).
- ¹⁴⁵ All data sets except HadSST are spatially complete over the ocean domain of interest $(20^{\circ}N-20^{\circ}S)$.

146 c. Satellite water vapor data

The satellite WV data used here were produced by RSS and are from 11 different satellitebased microwave radiometers (Wentz 2013). The procedures for intercalibrating and merging information from these instruments and for estimating uncertainties in satellite WV trends are described in detail elsewhere (Mears et al. 2018). The WV retrievals are based on measurements of microwave emissions from the 22-GHz water vapor absorption line. The distinctive shape of this line provides robust retrievals that are less problematic than other types of satellite measurement. The signal-to-noise ratio (S/N) for detecting moistening in the lower troposphere by a measurement of water vapor is several times larger than for MSU-based measurements of air temperature (Wentz and Schabel 2000). Relative to WV information from radiosondes and early reanalysis products, the RSS WV data set was judged by Trenberth et al. (2005) to provide the most credible estimate of means, variability, and trends over oceans.

RSS WV data were available for the 384 months from January 1988 to December 2019 on a 1^{58} 1° × 1° latitude/longitude grid. Due to the high emissivity of the land surface, WV retrievals are provided over oceans only. Our focus here is on WV trends spatially averaged over tropical oceans (20°N-20°S), where there is well-understood covariability between temperature and saturation vapor pressure (Iribarne and Godson 1981).

Because of changes in satellite capabilities, footprint size, and rain and land masking, the spatial coverage of the RSS WV data changes over time. This results in the systematic addition of grid cells with WV data in the western Pacific and near the maritime continent. To avoid the introduction of trend biases arising from coverage changes, we imposed a "fixed coverage" mask – i.e., our analysis of the satellite WV data was restricted to the subset of grid-points with continuous coverage over the 384-month analysis period. After regridding model WV data to the observational grid, the same "fixed coverage" mask was applied to all model simulations of historical climate change.

170 d. Reanalysis data

Reanalyses employ an atmospheric numerical weather forecast model with no changes over time in the model itself (Bengtsson and Shukla 1988; Kalnay et al. 1996). They provide a well-tested framework for blending and constraining assimilated weather information from different sources; each source is typically characterized by different accuracy and different temporal and spatial coverage.

8

The ERA5 reanalysis product of the European Centre for Medium-Range Weather Forecasts (ECMWF) recently superseded the ERA-Interim reanalysis. ERA5 was generated with a highresolution version (\approx 31 km horizontal resolution, 137 vertical levels) of the ECMWF operational forecast model and a 4-D variational data assimilation system (Hersbach et al. 2020). According to Simmons et al. (2020), ERA5 exhibited "a pronounced cold bias for the years 2000 to 2006". ERA5.1, which spans the affected 2000 to 2006 period, corrects this error and yields "analyses with better global-mean temperatures in the stratosphere and uppermost troposphere than provided

¹⁸³ by ERA5" (Simmons et al. 2020). Inclusion of ERA5.1 results allows us to test whether blending ¹⁸⁴ model and observational information in a state-of-the-art reanalysis framework provides layer-¹⁸⁵ average atmospheric temperature information similar to those available from actual RSS, STAR, ¹⁸⁶ and UAH satellite data.

187 **3. Model output**

a. CMIP5 simulations

¹⁸⁹ We used model output from phase 5 of the Coupled Model Intercomparison Project (CMIP5) ¹⁹⁰ (Taylor et al. 2012). The description of the CMIP5 data sets provided in the next two paragraphs ¹⁹¹ follows Santer et al. (2017a).

¹⁹² Our focus here is on three different types of CMIP5 numerical experiment: 1) simulations ¹⁹³ with estimated historical changes in human and natural external forcings; 2) simulations with ¹⁹⁴ 21st century changes in greenhouse gases and anthropogenic aerosols prescribed according to ¹⁹⁵ the Representative Concentration Pathway 8.5 (RCP8.5; Meinshausen et al. 2011);ⁱ and 3) pre-¹⁹⁶ industrial control runs with no changes in external influences on climate.

ⁱRCP8.5 has radiative forcing of approximately 8.5 W/m² in 2100, eventually stabilizing at roughly 12 W/m².

¹⁹⁷ Most CMIP5 historical simulations end in December 2005. RCP8.5 simulations were initiated ¹⁹⁸ from conditions of the climate system at the end of the historical run. To avoid truncating ¹⁹⁹ comparisons between modeled and observed climate change trends in December 2005, we spliced ²⁰⁰ together output from the historical simulations and the RCP8.5 runs. We refer to these spliced ²⁰¹ simulations subsequently as "extended HIST" runs.

In total, we analyzed 123 individual extended HIST realizations performed with 28 different CMIP5 models. We excluded models that did not consider the scattering and absorption of radiation by stratospheric volcanic aerosols (Santer et al. 2013), and therefore lack short-term lower stratospheric warming signals after the eruptions of El Chichón in 1982 and Pinatubo in 1991. Including these models in the calculation of multi-model average (MMA) temperature changes would bias the MMA estimate of volcanic TLS signals.

Details of the start dates, end dates, and lengths of the historical integrations and RCP8.5 runs are given in Supplemental Table S1. Supplemental Table S2 provides information on the 36 CMIP5 pre-industrial control runs used to calculate climate noise estimates. The control integrations allow us to determine S/N characteristics of atmospheric temperature changes (see Section 5).

212 b. CMIP6 simulations

²¹³ We also analyze TLS, TMT, TLT, WV, and SST from model simulations performed under ²¹⁴ phase 6 of CMIP. These simulations rely on newer versions of CMIP5 models, often with more ²¹⁵ comprehensive representation of earth system processes (Eyring et al. 2016), and with contributions ²¹⁶ from modeling groups that did not participate in CMIP5. Efforts were made in CMIP6 to improve ²¹⁷ the representation of external forcings with known systematic errors in CMIP5, such as volcanic ²¹⁸ and solar forcing in the early 21st century (Solomon et al. 2011; Kopp and Lean 2011; Ridley et al. ²¹⁹ 2014; Schmidt et al. 2014; Gillett et al. 2016). At the time this research was performed, the CMIP6 archive was still being populated with model simulation output. For pre-industrial control runs, output was available from 30 different models. For the analysis of forced simulations, the CMIP6 historical runsⁱⁱ from 22 different models were spliced with results from scenario integrations.

Multiple Shared Socioeconomic Pathway (SSP) scenarios were available for splicing (Riahi et al. 2017). We chose the SSP5 scenario here. SSP5 most closely approximates the radiative forcing in the CMIP5 RCP8.5 simulation. The differences in radiative forcing between the five SSPs are very small over the satellite era (Riahi et al. 2017), so the choice of scenario is unlikely to affect our model-versus-data comparisons.

In the case of TMT, TLT, SST, and WV, we analyzed 166 realizations. For reasons discussed in Section 3c, the sample size was smaller for TLS (116 extended HIST realizations performed with 21 models). Further details of the CMIP6 extended HIST and control simulations are provided in Supplemental Tables S3 and S4, respectively.

233 c. Large initial condition ensembles

Large initial condition ensembles (LEs) are routinely performed by climate modeling groups (Deser et al. 2012; Fyfe et al. 2017; Deser et al. 2020). Typical LE sizes range from 30 to 100. Individual LE members are generated with the same model and external forcings, but are initialized from different conditions of the climate system. Each LE member provides a unique realization of the "noise" of natural internal variability superimposed on the underlying climate "signal" (the response to the changes in forcing).

We used four different LEs to quantify uncertainties in temperature and WV trends arising from multi-decadal internal variability. Two LEs applied CMIP5 historical forcing until 2005 and CMIP

ⁱⁱThe CMIP6 historical runs typically end in December 2014.

RPC8.5 forcing thereafter. The other two LEs relied on CMIP6 forcing until 2014 and SSP5 242 forcing from 2015 to 2100. The CMIP5 LEs were performed with version 1 of the Community 243 Earth System Model (CESM1; Deser et al. 2012) and with version 2 of the Canadian Earth System 244 Model (CanESM2; Fyfe et al. 2017; Swart et al. 2018). The CESM1 and CanESM2 LEs consist of 245 40 and 50 members, respectively. The two 50-member CMIP6 LEs relied on version 5 of CanESM 246 (CanESM5; Fyfe et al. 2021) and on version 6 of the Model for Interdisciplinary Research on 247 Climate (MIROC6; Tatebe et al. 2019). All four LEs used different strategies for initialization of 248 the individual ensemble members.ⁱⁱⁱ 249

The CanESM5 LE exhibits anomalous aperiodic 1-2 month lower stratospheric warming events in certain ensemble members. These warming events are sufficiently large to influence decadaltimescale TLS trends but have minimal impact on decadal variability in tropospheric temperature. We therefore excluded the CanESM5 LE from the multi-model analysis of CMIP6 TLS trends, but included CanESM5 LE results in the multi-model analysis of TMT, TLT, WV, and SST.

4. Temperature time series and trends

a. Lower stratosphere

Figure 1A shows time series of near-global averages of TLS. The lower stratosphere cools over the full satellite era in all observational data sets and model extended HIST simulations. The main cause of this cooling is human-induced depletion of stratospheric ozone, with a smaller contribution from anthropogenic increases in atmospheric CO₂ (Solomon 1999; Ramaswamy et al. 2006; Thompson et al. 2012; Aquila et al. 2016; Maycock et al. 2018; Bandoro et al. 2018). Satellite-era decreases in TLS are punctuated by large episodic warming signals after the major eruptions of El Chichón

ⁱⁱⁱDifferences include the selected starting year for the simulation, the strategy for perturbing initial conditions, and whether perturbations were applied to the atmosphere only or to the atmosphere and the ocean.

in 1982 and Pinatubo in 1991. Warming arises from absorption of incoming solar radiation and 263 outgoing long-wave radiation by stratospheric volcanic aerosols (Robock 2000; Shine et al. 2003). 264 The CMIP6 multi-model average has an unrealistically small TLS signal after El Chichón (Fig. 2). 265 Based on the MMA root-mean-square (RMS) errors between observed and simulated volcanic TLS 266 signals, the TLS response to El Chichón is better captured in CMIP5 (Figs. 3A,C). For Pinatubo, 267 the MMA RMS error is smaller in CMIP6 (Figs. 3B,D). These CMIP5-versus-CMIP6 differences 268 are significant at the 5% level for the El Chichón signal, but not for the Pinatubo signal (see SM). 269 Volcanic signal differences in CMIP5 and CMIP6 arise from multiple factors. These include 270 differences in the type and time history of information used for prescribing historical changes in 271 volcanic aerosol loadings, the aerosol optical properties, and the implementation of these properties 272 in calculating volcanic radiative forcing (Thomason et al. 2018). Rather than prescribing volcanic 273 aerosol, at least one CMIP6 modeling group calculated volcanic aerosol loadings based on observed 274 estimates of volcanically produced SO₂ (Mills et al. 2016; Danabasoglu et al. 2020). Separating 275 and quantifying the impact of these different factors on volcanic temperature signals requires 276 systematic numerical experimentation (Rieger et al. 2020; Fyfe et al. 2021). 277

Recent studies suggest that the Montreal Protocol led to a partial recovery of lower stratospheric 278 ozone and TLS in the early 21st century (Solomon et al. 2016, 2017; Philipona et al. 2018; 279 Petropavlovskikh et al. 2019; Banerjee et al. 2020). All model and observational TLS data sets 280 analyzed here exhibit behavior consistent with ozone recovery: pronounced global-mean cooling 281 of the lower stratosphere over the ozone depletion portion of the satellite record, followed by weaker 282 cooling or near-zero trends over the recovery period (Solomon et al. 2017; Philipona et al. 2018; 283 Steiner et al. 2020; Mitchell et al. 2020; see Fig. 4). The multi-model average TLS trends for these 284 two periods are -0.36 and -0.07°C/decade in CMIP5 and -0.26 and -0.06°C/decade in CMIP6. 285 During the ozone depletion period, the larger multi-model average lower stratospheric cooling in 286

the older CMIP5 simulations is in better accord with satellite TLS trends, which range from -0.42to -0.49° C/decade. This is partly due to the larger (negative) ozone-induced stratospheric radiative forcing in CMIP5 (Checa-Garcia et al. 2018).

Other factors may also contribute to reduced lower stratospheric cooling in CMIP6 over 1979 290 to 2000. These factors include CMIP5-versus-CMIP6 differences in forcing from tropospheric 291 ozone (Checa-Garcia et al. 2018), volcanoes (see above) and stratospheric water vapor (Keeble 292 et al. 2020), along with differences in the behavior of tropical upwelling. The zonal-mean structure 293 of trends in TLS and TMT (Fig. 5) reveals prominent differences between CMIP5 and CMIP6 in 294 the tropics, where any differences in the behavior of tropical upwelling should manifest (Ball et al. 295 2020). More detailed analyses and more systematic numerical experimentation will be required 296 to quantify the relative contributions of forcing, response, chemistry, and dynamics to differences 297 between CMIP5 and CMIP6 TLS trends (Checa-Garcia et al. 2018; Fyfe et al. 2021). 298

²⁹⁹ b. Troposphere

Multi-decadal warming of the global troposphere is a ubiquitous feature of the observations 300 and all CMIP5 and CMIP6 forced simulations (Figs. 1B, C). Over the full satellite era, the 301 MMA tropospheric warming rate is very similar in CMIP5 and CMIP6 (0.28 and 0.29°C/decade, 302 respectively). This holds both for TMT and TLT (Fig. 6A). The similarity of the CMIP5 and CMIP6 303 results is noteworthy given that CMIP6 has a larger number of models with higher Transient Climate 304 Response (TCR) and higher Effective Climate Sensitivity (ECS) (Zelinka et al. 2020; Flynn and 305 Mauritsen 2020; Meehl et al. 2020). An independent analysis of surface temperature supports our 306 finding: despite higher average TCR and ECS in CMIP6, the MMA historical surface warming rate 307 is comparable in older and newer generations of CMIP models, possibly due to a larger response 308 to anthropogenic aerosol forcing in CMIP6 (Flynn and Mauritsen 2020; Fyfe et al. 2021). 309

In the four single-model large ensembles, the spread of TMT and TLT trends arising from internal variability is substantial, spanning 31 to 47% of the trend spread in the CMIP5 and CMIP6 multi-model ensembles (Fig. 6A).^{iv} These results are consistent with other recent comparisons of LE spread to multi-model ensemble spread (Mitchell et al. 2020; Po-Chedley et al. 2021).

Observed trends in global-mean tropospheric temperature range from 0.13 to 0.19°C/decade 314 for TMT and from 0.13 to 0.21°C/decade for TLT (Fig. 6A). For TLT, over 84% of the total 315 number of CMIP5 and CMIP6 extended HIST realizations analyzed here have trends exceeding the 316 largest observational result; the corresponding figure is 91% for corrected TMT trends. Related 317 work suggests that the smaller observed warming is partly due to an unusual manifestation of 318 natural internal variability. Model realizations with phasing of internal variability similar to the 319 observations yield global-mean and tropical tropospheric temperature trends that are within the 320 range of satellite results (Po-Chedley et al. 2021). 321

In all individual extended HIST realizations, the ratio $R_{\text{TMT/TLT}}$ between global-mean trends in 322 TMT and TLT is close to unity (Fig. 6B). This narrow range occurs despite differences in external 323 forcings, ECS, and internal variability in the multi-model and single-model ensembles, and despite 324 differences in the patterns of warming in TMT and TLT (Santer et al. 2019). The CMIP5 and 325 CMIP6 sampling distributions of $R_{\text{TMT/TLT}}$ encompass the UAH, ERA5.1, and RSS "MSU merge" 326 results. The latter data set relies solely on information from earlier MSU instruments during the 327 1999 to 2003 overlap period between MSU and AMSU measurements (see Section 2a). The 328 other two RSS data sets, "AMSU merge" and baseline, depart noticeably from the model-based 329 expectations, yielding $R_{\{\text{TMT/TLT}\}}$ values significantly less than one. 330

^{iv}This percentage represents (s_{LE}/s_{CMIP}) * 100, where s_{LE} is the standard deviation of the sampling distribution of trends in an individual CMIP5 LE or CMIP6 LE and s_{CMIP} is the standard deviation of the sampling distribution of ensemble-mean trends in the corresponding CMIP5 or CMIP6 multi-model ensemble containing the LE.

It is now recognized that there were systematic deficiencies in the early 21st century solar and 331 volcanic forcing used in CMIP5 (Kopp and Lean 2011; Solomon et al. 2012; Flato et al. 2013; 332 Schmidt et al. 2014). Efforts were made to improve representation of both forcings in CMIP6 333 (Eyring et al. 2016; Gillett et al. 2016; Thomason et al. 2018; Rieger et al. 2020). We find, 334 however, that CMIP5 and CMIP6 multi-model average trends in TMT are virtually identical over 335 2001 to 2019 (Fig. 7). Since other external forcings also changed between these two generations 336 of models (Checa-Garcia et al. 2018), isolating the climate impact of improvements in volcanic 337 or solar forcing is challenging. Such diagnosis will benefit from simulations in which the same 338 physical climate model is run with different versions of individual forcings (Fyfe et al. 2021). 339

Tropospheric trends in ERA5.1 exhibit several notable differences relative to the satellite data sets (Hersbach et al. 2020). Reanalysis TMT trends are smaller than in all satellite data sets over 1979 to 2000 and larger than in all satellite data sets over 2001 to 2019 (Fig. 7). Over the 2002 to 2018 period covered by Global Positioning Satellite (GPS) radio occultation measurements, both GPS data and radiosondes yield trends in the middle troposphere that are in reasonable accord with the ERA5.1 results (Steiner et al. 2020).

³⁴⁶ While the satellite data analyzed here are derived from measurements of microwave emissions ³⁴⁷ alone, ERA5.1 uses a state-of-the-art 4D assimilation system to constrain a weather forecast model ³⁴⁸ with a wide range of multi-variable measurements from satellites, radiosondes, and surface stations ³⁴⁹ (Hersbach et al. 2020; Simmons et al. 2020). Detailed observing system experiments can help ³⁵⁰ to understand the impact of different features of the assimilation system and assimilated data ³⁵¹ (Bormann et al. 2019). Such studies will be useful in reconciling the trend differences found here ³⁵² and elsewhere (Steiner et al. 2020) between microwave sounders and ERA5.1.

5. Signal-to-noise properties and model-data signal differences

In previous statistical comparisons of modeled and observed temperature changes, discussion often focused on the appropriateness of different comparison periods (Santer et al. 2011). This can be uninformative if attention is restricted to a short segment of the overall temperature record. Here we analyze atmospheric temperature changes over all N_L maximally overlapping *L*-year periods (see SM). We consider four different values of *L*: 10, 20, 30, and 40 years. For each value of *L*, sampling variability is reduced by averaging over all N_L individual measures of temperature change. As we show below, examining timescale-average behavior can have diagnostic value.

Figure 8 shows two different types of statistic: trends and regression coefficients. Results are from individual observational data sets and from distributions of statistics in forced and unforced simulations.

³⁶⁴ Consider the trend results first. Rows 1-3 of Fig. 8 display trends in TLS, TMT, and TLT ³⁶⁵ (respectively) for our four selected values of the timescale *L*. With increasing *L*, the amplitude ³⁶⁶ of internally generated trends decreases. As a result, the standard deviations of the forced and ³⁶⁷ unforced trend distributions decrease. For all three atmospheric layers, forced and unforced trend ³⁶⁸ distributions are completely separated at L = 40 years (Figs. 8D, H, and L). This is a simple visual ³⁶⁹ illustration of the timescale-dependence of signal and noise, and of the difficulty in their separation ³⁷⁰ on shorter, noisier timescales of 1-2 decades (Santer et al. 2011).

³⁷¹ Despite the evolution in model complexity and resolution between CMIP5 and CMIP6, the ³⁷² sampling distributions of unforced atmospheric temperature trends are remarkably similar in the ³⁷³ two generations of coupled models. The same is true for the sampling distributions of forced trends ³⁷⁴ on 10- and 20-year timescales. On longer 30- and 40-year timescales, however, small differences ³⁷⁵ are apparent in the distributions of forced tropospheric temperature trends in CMIP5 and CMIP6. These may arise because CMIP5 and CMIP6 do not have identical multi-decadal evolution of certain external forcings (Checa-Garcia et al. 2018; Fyfe et al. 2021).

Figure 8 also provides information on the consistency between global-mean temperature trends 378 in observations and the extended HIST simulations. On shorter 10- and 20-year timescales, all 379 observed TLS, TMT, and TLT trends are contained within the respective CMIP5 and CMIP6 380 distributions of forced trends. The same is true for observed TLS trends on longer 30- and 40-381 year timescales (Figs. 8C, D). For TMT and TLT, however, only observed data sets with larger 382 tropospheric warming rates are within the model 30- and 40-year distributions of forced trends. 383 The UAH-inferred warming on these timescales is invariably smaller than model expectations 384 (Figs. 8G, H, K, and L). 385

Amplification of warming with increasing height is a well-known and well-understood property 386 of the tropical atmosphere (Stone and Carlson 1979; Santer et al. 2005; Held and Soden 2006). 387 Figures 8M-P display one measure of tropical amplification behavior – the regression coefficient 388 $b_{\text{TMT:TLT}}$ between time series of tropical ocean averages of TMT and TLT. All model and obser-389 vational values of b_{TMTTLT} are greater than 1, indicating that temperature changes in the mid- to 390 upper troposphere exceed those in the lower troposphere. The means and widths of the CMIP5 and 391 CMIP6 sampling distributions of $b_{\{\text{TMT:TLT}\}}$ are relatively insensitive to increases in L, and show 392 substantial overlap for the forced and unforced runs. The model results imply that $b_{\text{TMT:TLT}}$ is both 393 timescale-invariant and insensitive to forcing, and that its values may impose a robust, physically 394 based constraint on observations (Santer et al. 2005; Held and Soden 2006). 395

Observational values of $b_{\{TMT:TLT\}}$ show a number of interesting features. First, the ERA5.1 and RSS "MSU merge" results are well within the range of model expectations on all four timescales considered here. In terms of this tropical amplification metric, therefore, there is no fundamental discrepancy between simulations and all observations.

Second, as in the model simulations, b_{TMTTLT} is timescale-invariant for UAH, ERA5.1, and 400 the RSS "MSU merge" case. While the three RSS sensitivity tests have almost identical $b_{\text{{TMT:TLT}}}$ 401 values for L = 10 years (Fig. 8M), the RSS baseline and "AMSU correct" data sets yield regression 402 coefficients that decrease in size as L increases, and are generally outside the range of model results 403 for 30- and 40-year timescales (Figs. 8O-P). On these longer timescales, the maximally overlapping 404 L-year windows always sample the 1998 to 2003 transition between earlier and more advanced 405 microwave sounders, and thus are more likely to reflect the impact of different merging choices on 406 amplification behavior (see Section 2a). 407

Third, the UAH $b_{\text{TMT:TLT}}$ value is ≈ 1.1 on all four timescales and is smaller than almost all 408 model results. The anomalous UAH value is due to a change in the method used by the UAH group 409 to estimate TLT (Spencer et al. 2017). The impact of this change was to increase the height of 410 the effective weighting function for TLT, thus decreasing the vertical separation between the TLT 411 and corrected TMT weighting functions. This leads to a smaller amplification ratio. To maintain 412 continuity with previous tropical amplification studies (Santer et al. 2017b) and to increase the 413 amplification signal, the model, RSS, and ERA5.1 results shown here do not use the new UAH 414 approach for calculating TLT. 415

6. Covariability of different aspects of tropical climate change

⁴¹⁷ Properties of the climate system that are controlled by well-understood physical mechanisms ⁴¹⁸ and are tightly constrained in model simulations may be useful for reducing large uncertainties ⁴¹⁹ in observed temperature trends (Santer et al. 2005). We consider four such properties here. The ⁴²⁰ first three properties are ratios between tropical WV trends and trends in tropical SST, TLT, and ⁴²¹ corrected TMT.^v We refer to these ratios as $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, and $R_{\{WV/TMT\}}$ (respectively).

^vBecause satellite WV data are available over ocean only, we computed $R_{\text{{WV/TLT}}}$ and $R_{\text{{WV/TMT}}}$ using "ocean only" TLT and TMT trends.

The relationship between temperature and saturation vapor pressure changes is governed by the Clausius-Clapeyron (C-C) equation (Iribarne and Godson 1981). If relative humidity remains approximately constant as temperature increases, C-C predicts the increase in columnar content of WV (Wentz and Schabel 2000; Held and Soden 2006; Mears et al. 2007; O'Gorman and Muller 2010).

The fourth property we examine, the trend ratio $R_{\text{TMT/SST}}$, is a measure of the amplification of tropical SST changes in the tropical troposphere. Its behavior is governed by moist thermodynamics (Stone and Carlson 1979; Held and Soden 2006). $R_{\text{TMT/SST}}$ provides information that differs from that of $b_{\text{TMT:TLT}}$, the regression-based amplification metric considered in Section 5.^{vi}

In a climate model, these four ratios are internally and physically consistent. The observed covariability of tropical WV, tropospheric temperature, and SST should also exhibit internal and physical consistency. As we show below, however, observed values of $R_{WV/SST}$, $R_{WV/TLT}$, $R_{WV/TMT}$, and $R_{TMT/SST}$ can be inconsistent for certain combinations of observed data sets, and may depart noticeably from model expectations.

Such departures can have at least three explanations. First, WV, tropospheric temperature, and SST are measured independently by different instruments on different satellites and/or measurement platforms. Each variable has different measurement accuracy and errors. These measurement differences can affect the estimated covariability between multidecadal trends in WV, tropospheric temperature, and SST.

and ocean has minimal impact on our results. To be consistent in terms of the domain analyzed, the TMT trends in $R_{\text{TMT/SST}}$ also rely on data averaged over tropical oceans only.

 $^{{}^{}vi}b_{\{\text{TMT:TLT}\}}$ was useful for examining whether the TMT and TLT time series produced by an individual research group yielded internally consistent amplification behavior. $b_{\{\text{TMT:TLT}\}}$ used TMT and TLT information from the same microwave sensors flown on the same satellites. In contrast, observed values of $R_{\{\text{TMT/SST}\}}$ provide information on the physical consistency between multidecadal trends in SST and TMT measurements that are processed by different research groups, and that are obtained using different types of measurement platforms.

Second, the tropospheric temperature and SST data sets analyzed here were generated by multiple 441 research groups. In the case of TMT and TLT, each research group uses different procedures to 442 adjust for drifts in satellite orbits and instrument calibration, to merge measurements from multiple 443 satellites, and to merge brightness temperatures estimated from earlier and more recent microwave 444 sounders. For SST, groups use different methods to blend information from ships, buoys, drifting 445 floats, and satellites, to adjust for changes over time in how SST measurements were made, and to 446 infill SSTs in data-sparse regions. The decisions made in adjusting tropospheric temperature and 447 SST for these known non-climatic influences can affect trends (Karl et al. 2006, 2015; Hausfather 448 et al. 2017; Mears et al. 2011; Mears and Wentz 2016, 2017; Zou and Qian 2016; Zou et al. 2018; 449 Spencer et al. 2017; Po-Chedley et al. 2015), and can therefore influence the estimated covariability 450 between real-world tropical temperature and WV changes (or between observed trends in SST and 451 TMT). Trends in satellite WV data are also sensitive to data set construction choices (Mears et al. 452 2018), but we currently have uncertainty estimates from the RSS group only.^{v_{11}} 453

Third, models may have incomplete or inaccurate representation of the basic physics driving observed tropical covariability relationships on multidecadal timescales. This seems unlikely (Held and Soden 2006), particularly given the fact that on interannual timescales, observed tropical covariability relationships between surface and tropospheric temperature (Santer et al. 2005) and between temperature and WV (Mears et al. 2007) are well captured by models (see Section 7).

Figure 9 shows scatter plots of the individual trend components of the four ratio statistics. For each statistic, model results are tightly constrained in the CMIP5 and CMIP6 multi-model ensembles. At least 96% of the variance in simulated WV trends (plotted on the *y*-axis in panels A-C) and in simulated TMT trends (plotted on the *y*-axis of panel D) is explained by simulated trends in the

viiWe do not use the reanalysis-derived WV trend in estimating structural uncertainties in observed WV trends. Other research has found possible problems with WV trends inferred from reanalysis products (Bengtsson et al. 2004; Wang et al. 2020).

⁴⁶³ independent (*x*-axis) variable. This indicates that the four covariance relationships of interest here
⁴⁶⁴ are relatively insensitive to model differences in the applied historical forcings, the temperature and
⁴⁶⁵ WV responses to these forcings, and the properties of simulated multi-decadal internal variability.
⁴⁶⁶ A related inference is that even though most of the mass of atmospheric water vapor resides in the
⁴⁶⁷ lower troposphere, simulated tropical SST, TLT, and TMT trends impose similar constraints on
⁴⁶⁸ simulated tropical WV trends – i.e., there is no evidence that on multidecadal timescales, SST or
⁴⁶⁹ TLT explain noticeably more of the WV variance than TMT.

The regression fits to the CMIP5 and CMIP6 trends are 8.5 and 8.7%/decade for WV and SST, 470 6.3 and 6.4%/decade for WV and TLT, and 5.3 and 5.5%/decade for WV and TMT (Figs. 9A-C, 471 respectively). The decrease in regression slope in the progression from panels A to C in Fig. 9 472 reflects the fact that tropical temperature changes closely follow a moist adiabatic lapse rate (Stone 473 and Carlson 1979). As the magnitude of warming amplifies with increasing height, the slope of 474 the regression between temperature trends and moisture trends decreases. The regression slope 475 for simulated tropical SST and TMT trends (1.6 for both CMIP5 and CMIP6; see Fig. 9D) is also 476 consistent with MALR expectations. 477

⁴⁷⁸ Unlike the model covariance relationships in Fig. 9, all four sets of observed covariance re-⁴⁷⁹ lationships show substantial spread. The tight clustering of model expectations and the large ⁴⁸⁰ observational uncertainty are clearer if we directly compare trend ratios (Fig. 10).^{viii} This com-⁴⁸¹ parison reveals that observed SST and tropospheric temperature data sets with the largest tropical ⁴⁸² warming over 1988 to 2019 have $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, and $R_{\{WV/TMT\}}$ ratios closest to the model ⁴⁸³ results (Figs. 10A-C).

viii The lowest and highest observational values for $R_{\text{\{WV/SST\}}}$, $R_{\text{\{WV/TLT\}}}$, $R_{\text{\{WV/TMT\}}}$, and $R_{\text{\{TMT/SST\}}}$ vary by factors of 1.6, 1.7, 1.8, and 2.9, respectively. The larger range for $R_{\text{\{TMT/SST\}}}$ arises because there is appreciable observational uncertainty in both the numerator and denominator of the ratio. In the three ratios involving WV, the structural uncertainty of observed trends can be estimated in the denominator only.

For all three ratios involving WV trends, there is minimal overlap between simulations and observations – observed ratios generally exceed model expectations. For $R_{\{WV/SST\}}$, only the COBE SST trend leads to a result consistent with model expectations (Fig. 10A). For both $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$, observed trend ratios are larger than almost all of the 289 model results (Figs. 10B,C).^{ix} The agreement between model and observed $R_{\{TMT/SST\}}$ values is closer, but depends on the selected combination of observed TMT and SST data sets (Fig. 10D).

We calculated Z-scores to summarize and synthesize the information in Fig. 10. For each 490 observed ratio in Fig. 10, the Z-score is simply the difference between the observed result and the 491 mean of the CMIP5 or CMIP6 multi-model average ratio, normalized by the CMIP5 or CMIP6 492 standard deviation of the sampling distribution of the ratio in question. The Z-scores in Fig. 11A 493 are averages over the individual scores arising from structural uncertainty in observed SST trends; 494 they are measures of the consistency between the simulated values of $R_{\text{\{WV/TLT\}}}$, $R_{\text{\{WV/TMT\}}}$, and 495 $R_{\text{TMT/SST}}$ and the observed values of these ratios estimated with a specific TLT or TMT data set. 496 The Z-scores in Fig. 11B are defined analogously, and are averages over the individual Z-scores 497 arising from structural uncertainty in observed tropospheric temperature trends. 498

⁴⁹⁹ Under the assumption that the model-generated distributions of the four ratios are realistic rep-⁵⁰⁰ resentations of the true (but uncertain) real-world covariance relationships, the *Z*-scores allow us ⁵⁰¹ to make certain inferences about the likelihood that individual observed SST and tropospheric ⁵⁰² temperature data sets are consistent with model expectations and with other other observations. In ⁵⁰³ Fig. 11A, for example, STAR and RSS "MSU merge" – the data sets with the largest observed tro-⁵⁰⁴ pospheric warming trends – are closest to the model expectations of WV/tropospheric temperature ⁵⁰⁵ trend ratios, and therefore have the smallest *Z*-scores for $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$. In contrast, the

^{ix}For each ratio, there are 123 values for CMIP5 and 166 for CMIP6. For $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$, only 4 and 3 of the 289 extended HIST realizations (respectively) have scaling ratios exceeding the smallest observed value.

⁵⁰⁶ muted tropospheric warming in UAH leads to $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$ values that are significantly ⁵⁰⁷ larger than model expectations, thus leading to large UAH *Z*-scores for these two ratios. Based ⁵⁰⁸ on $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$ alone, therefore, we might infer that the smaller tropical tropospheric ⁵⁰⁹ warming trend is UAH is less credible.

This inference assumes that the observed trend in tropical WV is accurate. A substantially smaller observed WV trend would decrease the UAH-derived $R_{\{WV/TLT\}}$ and $R_{\{WV/TMT\}}$ ratios, bringing them in closer agreement with model expectations. Since we do not have estimates of the observed WV trend from multiple research groups, it is difficult to assess the likelihood that the true (but uncertain) real-world WV trend is markedly smaller than the RSS WV trend estimate.

By considering the $R_{\text{TMT/SST}}$ ratio, however, we can bring in independently monitored observed 515 SST data. This allows us to explore the constraint that observed SST trends impose on the size of 516 observed TMT trends. The COBE, ERSST, and HadSST data sets, when considered in combination 517 with the UAH TMT trend, lead to UAH-based $R_{\text{TMT/SST}}$ ratios that are significantly smaller than 518 climate model and MALR expectations (Fig. 10D). Only the muted tropical surface warming 519 in the HadISST data set yields a UAH-based $R_{\text{TMT/SST}}$ ratio that is marginally consistent with 520 model expectations. The weaker surface warming in HadISST is inconsistent with independently 521 monitored WV data (see Figs. 10A and 11B). 522

To summarize, the reduced tropical tropospheric warming in UAH is not supported by: 1) an independent estimate of atmospheric moistening from satellite data; 2) all independent estimates of observed sea surface warming except HadISST; and 3) all model and theoretical expectations of $R_{WV/TLT}$, $R_{WV/TMT}$, and $R_{TMT/SST}$. In turn, the HadISST tropical SST trend that is marginally consistent with the muted UAH tropospheric warming is not supported by independently monitored satellite WV or TMT data, or by model and theoretical expectations of $R_{WV/SST}$ and $R_{TMT/SST}$.

24

The above analysis focused on comparing simulated and observed measures of tropical covariability. It is also of interest to compare modeled and observed values of the individual components of these covariability metrics. In the case of WV, 21% of the model WV trends are smaller than the satellite-estimated WV trend in Fig. 9A. For SST, TLT, and TMT, only 17%, 12%, and 12% of the model trends are within the range of observed results (Figs. 9A-C, respectively).

There are multiple interpretations of this finding. One interpretation is that the higher level of consistency between simulated and observed tropical WV trends reflects a systematic low bias in observed tropical TLT and TMT trends over 1988 to 2019. An alternative explanation is that the satellite WV trend is overestimated. It is difficult to discriminate between these two possibilities without additional information, such as well-quantified estimates of uncertainties in observed WV trends from different research groups.

540 7. Conclusions

Relative to CMIP5, the more recent CMIP6 models have higher resolution (on average), more 541 complete numerical portrayal of Earth's climate system, and nominally improved representation 542 of external forcings (Eyring et al. 2016). These advances do not guarantee improved agreement 543 between simulations and observations. This is apparent in at least two aspects of model performance 544 analyzed here: lower stratospheric cooling over the ozone depletion period and the stratospheric 545 temperature response to the El Chichón eruption. Understanding why these features are more 546 accurately represented in CMIP5 will require more systematic diagnostic efforts to disentangle 547 evolutionary changes in models from evolutionary changes in model forcings (Fyfe et al. 2021). 548

The development of satellite temperature data sets remains a work in progress. Adjustments for known non-climatic factors can have significant impact on observed trends in tropospheric temperature, as well as on basic physical properties related to tropospheric warming (Karl et al.

2006; Mears et al. 2011; Mears and Wentz 2016, 2017; Zou and Qian 2016; Zou et al. 2018; 552 Spencer et al. 2017; Po-Chedley et al. 2015). Multi-model and single-model large ensembles 553 tightly constrain four such physical properties – the ratio between tropical trends in WV and SST, 554 WV and TLT, WV and TMT, and TMT and SST. These are denoted here by $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, 555 $R_{\text{\{WV/TMT\}}}$, and $R_{\text{\{TMT/SST\}}}$, respectively. Comparing modeled and observed values of such basic 556 covariance relationships has the advantage (relative to single-variable comparisons) that results are 557 less sensitive to model-versus-observed differences in the phasing of internal variability (Santer 558 et al. 2005; Po-Chedley et al. 2021). 559

⁵⁶⁰ We find significant differences between simulated and observed values of $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, ⁵⁶¹ $R_{\{WV/TMT\}}$, with observations exceeding model expectations in most cases (Figs. 10A-C). Observed ⁵⁶² data sets with larger warming of the tropical ocean surface and tropical troposphere yield trend ⁵⁶³ ratios that are closer to model results. For $R_{\{TMT/SST\}}$, model-data consistency depends on the ⁵⁶⁴ selected combination of observed data sets used to estimate TMT and SST trends (Fig. 10D).

One interpretation of our findings is that they are due to a systematic low bias in satellite 565 tropospheric temperature trends - i.e., that the size of the observed tropical moistening signal is 566 greater than can be explained by the independently observed warming of the tropical troposphere. 567 Alternately, the observed atmospheric moistening signal may be overestimated. Given the large 568 structural uncertainties in observed tropical TMT and SST trends, and because satellite WV data 569 are available from one group only, it is difficult to determine which interpretation is more credible. 570 What we can say with confidence, however, is that decisions regarding how to merge MSU 571 and AMSU TMT data have substantial impact on observed tropical TMT trends. This is evident 572 from the three RSS sensitivity tests examined here. These sensitivity tests point towards merging 573 decisions as a significant contributory factor to uncertainties in observed $R_{\{WV/TMT\}}$ and $R_{\{TMT/SST\}}$ 574 trend ratios (Figs. 10C,D). 575

Two further points are relevant to the question of whether the model-observed differences in 576 Figs. 10A-C are mainly due to underestimated observed tropospheric temperature trends or to an 577 overestimated satellite WV trend. First, there is some evidence that observational uncertainties may 578 be smaller in satellite WV data than in satellite tropospheric temperature data (Wentz 2013; see 579 Section 2c). Second, when the individual trend components of our four trend ratios are examined, 580 the agreement between models and observations is better for WV and SST trends than for TMT or 581 TLT trends. This difference in model-data consistency, taken together with higher measurement 582 accuracy of WV and the results of the RSS sensitivity tests, suggests that underestimated observed 583 tropospheric warming is plausible. This inference is predicated on the assumption that the model-584 based covariance constraints are realistic. 585

⁵⁹⁶ While our analysis does not definitively resolve the cause or causes of significant differences ⁵⁹⁷ between modeled and observed tropospheric warming trends, it does illustrate the diagnostic power ⁵⁹⁸ of simultaneously considering multiple complementary variables (Wentz and Schabel 2000). Our ⁵⁹⁹ study also highlights the strong internal and physical consistency between the model constraints ⁵⁹⁰ derived from multidecadal tropical trends in WV, TMT, and SST. Examining additional inde-⁵⁹¹ pendently monitored constraints may be helpful in reducing the currently large uncertainties in ⁵⁹² observations of tropical climate change.

Acknowledgments. We acknowledge the World Climate Research Programme's Working Group 593 on Coupled Modelling, which is responsible for CMIP, and we thank the climate modeling groups 594 for producing and making available their model output. For CMIP, the U.S. Department of En-595 ergy's Program for Climate Model Diagnosis and Intercomparison (PCMDI) provides coordinating 596 support and led development of software infrastructure in partnership with the Global Organiza-597 tion for Earth System Science Portals. This work was performed under the auspices of the U.S. 598 Department of Energy (DOE) by Lawrence Livermore National Laboratory under Contract DE-599 AC52-07NA27344. At LLNL, B.D.S., S.P.-C., M.D.Z., and J.P. were supported by the Regional 600 and Global Model Analysis Program of the Office of Science at the DOE. S.P.-C. was also supported 601 under LDRD 18-ERD-054. All primary satellite, reanalysis, and model temperature data sets used 602 here are publicly available. Synthetic satellite temperatures calculated from model simulations 603 and the ERA 5.1 reanalysis are provided at: https://pcmdi.llnl.gov/research/DandA/. We thank 604 Adrian Simmons at ECMWF for assistance with ERA 5.1 data and internal reviewers at NOAA 605 and CCCma for helpful comments. 606

607

APPENDIX A

608

Calculation of synthetic satellite temperatures from model data

a. Calculation of synthetic satellite temperatures

We use a local weighting function method developed at RSS to calculate synthetic satellite temperatures from CMIP5 and CMIP6 output and from the ERA5.1 reanalysis (Santer et al. 2017b). At each grid-point, simulated temperature profiles were convolved with local weighting functions. The weights depend on the grid-point surface pressure, the surface type (land, ocean, or sea ice), and the selected layer-average temperature (TLS, TMT, or TLT). The local weighting ⁶¹⁵ function method provides more accurate estimates of synthetic satellite temperatures than use of a ⁶¹⁶ global-mean weighting function, particularly over high elevation regions.

617

618

APPENDIX B

Method used for correcting TMT data

Trends in TMT estimated from microwave sounders receive a substantial contribution from the 619 cooling of the lower stratosphere (Fu et al. 2004; Fu and Johanson 2004, 2005; Johanson and Fu 620 2006). In Fu et al. (2004), a regression-based method was developed for removing the bulk of 621 this stratospheric cooling component of TMT. This method has been validated with both observed 622 and model atmospheric temperature data (Fu and Johanson 2004; Gillett et al. 2004; Kiehl et al. 623 2005). We calculated two different versions of corrected TMT, the first with latitudinally fixed 624 and the second with latitudinally varying regression coefficients. We refer to these subsequently 625 as TMT₁ and TMT₂, respectively. The main text discusses corrected TMT₁ only, and does not use 626 the subscript 1 to identify corrected TMT. 627

The regression equation applied in Fu and Johanson (2005) for calculating corrected TMT is:

$$TMT = a_{24}TMT + (1 - a_{24})TLS$$
(B1)

For TMT₁, we use $a_{24} = 1.1$ at each latitude. For TMT₂, $a_{24} = 1.1$ between 30°N and 30°S, and $a_{24} = 1.2$ poleward of 30°. This is consistent with how we have calculated TMT₁ and TMT₂ in previous work (Santer et al. 2017b).

The advantage of TMT_2 is that lower stratospheric cooling makes a larger contribution to TMT_{632} trends at mid- to high latitudes. The latitudinally varying regression coefficients in TMT_2 remove more of this extratropical cooling. We prefer to use the more conservative TMT_1 here. In practice, the choice of TMT_1 or TMT_2 has minimal influence on the statistical significance of differences ⁶³⁶ between the modeled and observed statistics of interest here (temperature trends and a regression-

⁶³⁷ based measure of the amplification of warming with increasing height in the tropical atmosphere).

638 References

- Aquila, V., W. H. Swartz, D. W. Waugh, P. R. Colarco, S. Pawson, L. M. Polvani, and R. S. Stolarski,
 2016: Isolating the roles of different forcing agents in global stratospheric temperature changes
 using model integrations with incrementally added single forcings. *J. Geophys. Res.*, 121, 8067–
 8082, doi:10.1002/2015JD023841.
- Ball, W. T., G. Chiodo, M. Abalas, and J. Alsing, 2020: Inconsistencies between chemistry
 climate model and observed lower stratospheric trends since 1998. *Atmos. Chem. Phys.*, doi:
 doi.org/10.5194/acp-2019-734, (in review).
- Bandoro, J., S. Solomon, B. D. Santer, D. Kinnison, and M. Mills, 2018: Detectability of the
 impacts of ozone-depleting substances and greenhouse gases upon global stratospheric ozone
 accounting for nonlinearities in historical forcings. *Atmos. Chem. Phys.*, 18, 143–166, doi:
 doi.org/10.5194/acp-18-143-2018.
- Banerjee, A., J. C. Fyfe, L. M. Polvani, D. Waugh, and K.-L. Chang, 2020: A pause in Southern
 Hemisphere circulation trends due to the Montreal Protocol. *Nature*, **579**, 544–548.
- Bellenger, H., E. Guilyardi, J. Leloup, M. Lengaigne, and J. Vialard, 2014: ENSO representation in climate models: from CMIP3 to CMIP5. *Cli. Dyn.*, **42**, 1999–2018, doi: 10.1007/s00382-013-1783-z.
- Bengtsson, L., S. Hagemann, and K. I. Hodges, 2004: Can climate trends be calculated from
 reanalysis? J. Geophys. Res., 109, D11111, doi:10.1029/2004JD004536.

30

- ⁶⁵⁷ Bengtsson, L., and J. Shukla, 1988: Integration of space and in situ observations to study global ⁶⁵⁸ climate change. *Bull. Am. Meteorol. Soc.*, **69**, 1130–1143.
- Bormann, N., H. Lawrence, and J. Farnan, 2019: Global observing system experiments in
 the ECMWF assimilation system. Technical Memo 839, European Centre for Medium-Range
 Weather Forecasts, 24 pp. doi:10.21957/sr184iyz.
- ⁶⁶² Checa-Garcia, R., M. I. Hegglin, D. Kinnison, D. A. Plummer, and K. P. Shine, 2018: Historical
 ⁶⁶³ tropospheric and stratospheric ozone radiative forcing using the CMIP6 database. *Geophys. Res.* ⁶⁶⁴ Lett., 45, 3264–3273, doi:10.1002/2017GL076770.
- Danabasoglu, G., and Coauthors, 2020: The Community Earth System Model Version 2
 (CESM2). *Journal of Advances in Modeling Earth Systems*, **12**, e2019MS001916, doi:
 10.1029/2019MS001916.
- ⁶⁶⁸ Deser, C., A. Phillips, V. Bourdette, and H. Teng, 2012: Uncertainty in climate projections: The ⁶⁶⁹ role of internal variability. *Cli. Dyn.*, **38**, 527–546.
- ⁶⁷⁰ Deser, C., and Coauthors, 2020: Insights from Earth system model initial-condition large ensembles
 ⁶⁷¹ and future prospects. *Nat. Clim. Change*, **10**, 277–286.
- Eyring, V., S. Bony, G. A. Meehl, C. A. Senior, B. Stevens, R. J. Stouffer, and K. E. Taylor, 2016:
- ⁶⁷³ Overview of the Coupled Model Intercomparison Project Phase 6 (CMIP6) experimental design ⁶⁷⁴ and organization. *Geosci. Mod. Dev.*, **9(5)**, 1937–1958, doi:10.5194/gmd-9-1937-2016.
- Eyring, V., and Coauthors, 2019: Taking model evaluation to the next level. *Nat. Clim. Change*, **9**, 102–110.
- Flato, G., and Coauthors, 2013: Evaluation of climate models. Climate Change 2013: The
- Physical Science Basis. Contribution of Working Group I to the Fifth Assessment i Report of the

- Intergovernmental Panel on Climate Change, T. F. Stocker, D. Qin, G.-K. Plattner, M. Tignor,
 S. K. Allen, J. Boschung, A. Nauels, Y. Xia, V. Bex, and P. M. Midgley, Eds., Cambridge
- ⁶⁸¹ University Press, 741–866.

⁶⁸² Flynn, C. M., and T. Mauritsen, 2020: On the climate sensitivity and historical warming evolution
 ⁶⁸³ in recent coupled model ensembles. *Atmos. Chem. Phys.*, **20**, 7829–7842, doi:doi.org/10.5194/
 ⁶⁸⁴ acp-2019-1175.

- ⁶⁸⁵ Fu, Q., and C. M. Johanson, 2004: Stratospheric influences on MSU-derived tropospheric temper-⁶⁸⁶ ature trends: A direct error analysis. *J. Clim.*, **17**, 4636–4640.
- ⁶⁸⁷ Fu, Q., and C. M. Johanson, 2005: Satellite-derived vertical dependence of tropical tropospheric ⁶⁸⁸ temperature trends. *Geophys. Res. Lett.*, **32**, L10703, doi:10.1029/2004GL022266.
- ⁶⁰⁹ Fu, Q., C. M. Johanson, S. G. Warren, and D. J. Seidel, 2004: Contribution of stratospheric cooling
 ⁶⁰⁰ to satellite-inferred tropospheric temperature trends. *Nature*, **429**, 55–58.
- ⁶⁹¹ Fu, Q., S. Manabe, and C. M. Johanson, 2011: On the warming in the tropical upper troposphere: ⁶⁹² Models versus observations. *Geophys. Res. Lett.*, **38**, L15704, doi:10.1029/2011GL048101.
- ⁶⁹³ Fyfe, J. C., V. Kharin, B. D. Santer, R. N. S. Cole, and N. P. Gillett, 2021: Significant impact of
 ⁶⁹⁴ forcing uncertainty in a large ensemble of climate model simulations. *Proc. Nat. Acad. Sci.*, (in
 ⁶⁹⁵ review).
- ⁶⁹⁶ Fyfe, J. C., K. von Salzen, J. N. S. Cole, N. P. Gillett, and J.-P. Vernier, 2013: Surface response
 ⁶⁹⁷ to stratospheric aerosol changes in a coupled atmosphere-ocean model. *Geophys. Res. Lett.*, 40,
 ⁶⁹⁸ 584–588.
- ⁶⁹⁹ Fyfe, J. C., and Coauthors, 2017: Large near-term projected snowpack loss over the western United
 ⁷⁰⁰ States. *Nature Communications*, **8**, doi:10.1038/ncomms14996.

701	Gates, W. L., and Coauthors, 1999: An overview of the results of the Atmospheric Model Inter-
702	comparison Project (AMIP I). Bull. Am. Meteor. Soc., 29, 29-55.
703	Gillett, N. P., B. D. Santer, and A. J. Weaver, 2004: Quantifying the influence of stratospheric cool-
704	ing on satellite-derived tropospheric temperature trends. <i>Nature</i> , 432 , doi:10.1038/nature03209.
705	Gillett, N. P., and Coauthors, 2016: The detection and attribution model intercomparison project
706	(DAMIP v1.0) contribution to CMIP6. Geosci. Mod. Dev., 9, 3685–3697.
707	Hartmann, D. L., and Coauthors, 2013: Observations: Atmosphere and Surface. Climate Change
708	2013: The Physical Science Basis. Contribution of Working Group I to the Fifth Assessment
709	Report of the Intergovernmental Panel on Climate Change, T. F. Stocker, D. Qin, GK. Plattner,
710	M. Tignor, S. K. Allen, J. Boschung, A. Nauels, Y. Xia, V. Bex, and P. M. Midgley, Eds.,
711	Cambridge University Press, 159–254.
712	Hausfather, Z., K. Cowtan, D. C. Clarke, P. Jacobs, M. Richardson, and R. Rohde, 2017: Assessing
713	recent warming using instrumentally homogeneous sea surface temperature records. Sci. Adv.,
714	3 , e1601207, doi:10.1126/sciadv.1601207.
715	Held, I. M., and B. J. Soden, 2006: Robust responses of the hydrological cycle to global warming.
716	J. Clim., 19 , 5686–5699.
717	Hersbach, H., and Coauthors, 2020: The ERA5 global reanalysis. Q. J. Roy. Met. Soc., 146,
718	1999–2049.
719	Hirahara, S., M. Ishii, and Y. Fukuda, 2014: Centennial-scale sea surface temperature analysis and
720	its uncertainty. J. Clim., 27, 57–75.
721	Huang, B., and Coauthors, 2017: Extended Reconstructed Sea Surface Temperature, Version 5

(ERSSTv5): Upgrades, validations, and intercomparisons. J. Clim., **30**, 8179–8205.

- Iribarne, J. V., and W. L. Godson, 1981: Atmospheric Thermodynamics. D. Reidel, 276 pp. 723
- Johanson, C. M., and Q. Fu, 2006: Robustness of tropospheric temperature trends from MSU 724 Channels 2 and 4. J. Clim., 19, 4234–4242. 725
- Kalnay, E., and Coauthors, 1996: The NCEP/NCAR 40-year reanalysis project. Bull. Am. Meteorol. 726 Soc., 77, 437–471. 727
- Karl, T. R., S. J. Hassol, C. D. Miller, and W. L. Murray, Eds., 2006: Temperature trends in the 728 lower atmosphere: Steps for understanding and reconciling differences. A Report by the U.S.

Climate Change Science Program and the Subcommittee on Global Change Research. National

Oceanic and Atmospheric Administration, 164 pp. 731

729

730

- Karl, T. R., and Coauthors, 2015: Possible artifacts of data biases in the recent global surface 732 warming hiatus. Science, 348, 1469–1472. 733
- Kay, J. E., and Coauthors, 2015: The Community Earth System Model: Large ensemble project. 734 Bull. Amer. Met. Soc., 96, 1333–1349. 735
- Keeble, J., and Coauthors, 2020: Evaluating stratospheric ozone and water vapor changes in cmip6 736 models from 1850-2100. Atmos. Chem. Phys., doi:10.5194/acp-2019-1202. 737
- Kennedy, J. J., N. A. Rayner, R. O. Smith, D. E. Parker, and M. Saunby, 2011: Reassessing biases 738

and other uncertainties in sea surface temperature observations measured in situ since 1850: 2. 739

Kiehl, J. T., J. Caron, and J. J. Hack, 2005: On using global climate model simulations to assess the 741

accuracy of MSU retrieval methods for tropospheric warming trends. J. Clim., 18, 2533–2539. 742

- Kopp, G., and J. L. Lean, 2011: A new, lower value of total solar irradiance: Evidence and climate 743
- significance. Geophys. Res. Lett., 38, L01706, doi:10.1029/2010GL045777. 744

Biases and homogenization. J. Geophys. Res., 116, D14104, doi:10.1029/2010JD015220. 740

745	Maycock, A. C., and Coauthors, 2018: Revisiting the mystery of recent stratospheric temperature
746	trends. Geophys. Res. Lett., 45, 9919-9933, doi:10.1029/2018GL078035.
747	Mears, C., D. K. Smith, L. Ricciardulli, J. Wang, H. Huelsing, and F. J. Wentz, 2018: Construction
748	and uncertainty estimation of a satellite-derived total precipitable water data record over the
749	world's oceans. Earth and Space Sci., 5, 197–210.
750	Mears, C., and F. J. Wentz, 2016: Sensitivity of satellite-derived tropospheric temperature trends
751	to the diurnal cycle adjustment. J. Clim., 29, 3629–3646.
752	Mears, C., and F. J. Wentz, 2017: A satellite-derived lower-tropospheric atmospheric temperature
753	dataset using an optimized adjustment for diurnal effects. J. Clim., 30, 7695–7718.
754	Mears, C., F. J. Wentz, P. Thorne, and D. Bernie, 2011: Assessing uncertainty in estimates of
755	atmospheric temperature changes from MSU and AMSU using a Monte-Carlo technique. J.
756	Geophys. Res., 116, D08112, doi:10.1029/2010JD014954.
757	Mears, C. A., B. D. Santer, F. J. Wentz, K. E. Taylor, and M. Wehner, 2007: The relationship
758	between temperature and precipitable water changes over tropical oceans. Geophys. Res. Lett.,
759	34 , L2470, doi:10.1029/2007GL031936.
760	Mears, C. A., M. C. Schabel, and F. J. Wentz, 2003: A reanalysis of the MSU channel 2 tropospheric
761	temperature record. J. Clim., 16, 3650–3664.
762	Mears, C. A., and F. J. Wentz, 2005: The effect of diurnal correction on satellite-derived lower
763	tropospheric temperature. Science, 309 , 1548–1551.
764	Meehl, G. A., C. A. Senior, V. Eyring, G. Flato, JF. Lamarque, R. J. Stouffer, K. E. Taylor, and
765	M. Schlund, 2020: Context for interpreting equilibrium climate sensitivity and transient climate

response from the CMIP6 Earth system models. *Sci. Advances*, **6**, doi:10.1126/sciadv.aba1981.

- ⁷⁶⁷ Meinshausen, M., and Coauthors, 2011: The RCP greenhouse gas concentrations and their exten-⁷⁶⁸ sions from 1765 to 2300. *Climatic Change*, **109**, 213–241.
- ⁷⁶⁹ Mills, M. J., and Coauthors, 2016: Global volcanic aerosol properties derived from emissions,
 ⁷⁷⁰ 1990–2014, using CESM1 (WACCM). *J. Geophys. Res. Atmos.*, **121**, 2332–2348.
- Mitchell, D. M., Y. T. E. Lo, W. J. M. Seviour, L. Haimberger, and L. M. Polvani, 2020: The
 vertical profile of recent tropical temperature trends: Persistent model biases in the context
 of internal variability. *Env. Res. Lett.*, (in press), [https://iopscience.iop.org/article/10.1088/
 1748-9326/ab9af7].
- ⁷⁷⁵ Morice, C. P., J. J. Kennedy, N. A. Rayner, and P. D. Jones, 2012: Quantifying uncertainties
 ⁷⁷⁶ in global and regional temperature change using an ensemble of observational estimates: The
 ⁷⁷⁷ HadCRUT4 data set. *J. Geophys. Res.*, **117**, D08101, doi:10.1029/2011JD017187.
- NRC, 2000: *Reconciling observations of global temperature change*. National Academy Press,
 Washington D.C., 169 pp.
- O'Gorman, P. A., and C. J. Muller, 2010: How closely do changes in surface and column water
 vapor follow Clausis-Clapeyron scaling in climate change simulations? *Env. Res. Lett.*, 5,
 doi:10.1088/1748-9326/5/2/025207.
- Petropavlovskikh, I., S. Godin-Beekmann, D. Hubert, R. Damadeo, B. Hassler, and V. S.
 (Eds.), 2019: SPARC/IO3C/GAW Report on Long-term Ozone Trends and Uncertainties in
 the Stratosphere. Tech. Rep. SPARC Report No. 9, GAW Report No. 241, WCRP-17/2018.
 [http://www.sparc-climate.org/publications/sparc-reports/sparc-report-no9].

- Philipona, R., and Coauthors, 2018: Radiosondes show that after decades of cooling, the
 lower stratosphere is now warming. *J. Geophys. Res.*, **123**, 12509–12522, doi:10.1029/
 2018JDR028901.
- Po-Chedley, S., and Q. Fu, 2012: Discrepancies in tropical upper tropospheric warming between atmospheric circulation models and satellites. *Environ. Res. Lett.*, 7, doi:10.1088/1748-9326/7/4/044018.
- Po-Chedley, S., B. D. Santer, S. Fueglistaler, M. D. Zelinka, P. Cameron-Smith, J. F. Painter, and
 Q. Fu, 2021: Natural variability drives model-observational differences in tropical tropospheric
 warming. *Proc. Nat. Acad. Sci.*, (in press).
- Po-Chedley, S., T. J. Thorsen, and Q. Fu, 2015: Removing diurnal cycle contamination in satellite derived tropospheric temperatures: Understanding tropical tropospheric trend discrepancies. *J. Clim.*, 28, 2274–2290.
- Ramaswamy, V., M. D. Schwarzkopf, W. J. Randel, B. D. Santer, B. J. Soden, and G. L. Stenchikov,
 2006: Anthropogenic and natural influences in the evolution of lower stratospheric cooling.
 Science, **311**, 1138–1141.
- Randall, D. A., and Coauthors, 2007: Climate Models and Their Evaluation. *Climate Change* 2007: The Physical Science Basis. Contribution of Working Group I to the Fourth Assessment
- ⁸⁰⁴ Report of the Intergovernmental Panel on Climate Change, S. Solomon, D. Qin, M. Manning,
- Z. Chen, M. Marquis, K. B. Averyt, M. Tignor, and H. L. Miller, Eds., Cambridge University
 Press, 589–662.
- Rayner, N. A., D. E. Parker, E. B. Horton, C. K. Folland, L. V. Alexander, D. P. Rowell, E. C.
- Kent, and A. Kaplan, 2003: Global analyses of sea surface temperature, sea ice, and night

- marine air temperature since the late nineteenth century. *J. Geophys. Res.*, **108**, 4407, doi: 10.1029/2002JD002670.
- Riahi, K., and Coauthors, 2017: The Shared Socioeconomic Pathways and their energy, land use,
 and greenhouse gas emissions implications: An overview. *Glob. Env. Change*, 42, 153–168,
 doi:10.1016/j.gloenvcha.2016.05.009.
- Ridley, D. A., and Coauthors, 2014: Total volcanic stratospheric aerosol optical depths and
 implications for global climate change. *Geophys. Res. Lett.*, **41**, 7763–7769, doi:10.1002/
 2014GL061541.
- Rieger, L. A., J. N. S. Cole, J. C. Fyfe, S. Po-Chedley, P. Cameron-Smith, P. J. Durack, N. P. Gillett,
 and Q. Tang, 2020: Quantifying CanESM5 and EAMv1 sensitivities to volcanic forcing for the
 CMIP6 historical experiment. *Geosci. Mod. Dev.*, 13, 4831–4843, doi:https://doi.org/10.5194/
 gmd-13-4831-2020.
- Robock, A., 2000: Volcanic eruptions and climate. *Rev. Geophys.*, **38**, 191–219.
- Santer, B. D., J. Fyfe, S. Solomon, J. Painter, C. Bonfils, G. Pallotta, and M. Zelinka, 2019:
 Quantifying stochastic uncertainty in detection time of human-caused climate signals. *Proc. Nat. Acad. Sci.*, **116**, 19821–19827, doi:doi.org/10.1038/s41558-019-0424-x.
- Santer, B. D., and Coauthors, 2005: Amplification of surface temperature trends and variability in
 the tropical atmosphere. *Science*, **309**, 1551–1556.
- ⁸²⁷ Santer, B. D., and Coauthors, 2011: Separating signal and noise in atmospheric tempera-⁸²⁸ ture changes: The importance of timescale. *J. Geophys. Res.*, **116**, D22105, doi:10.1029/ ⁸²⁹ 2011JD016263.

38

- Santer, B. D., and Coauthors, 2013: Human and natural influences on the changing thermal structure
 of the atmosphere. *Proc. Nat. Acad. Sci.*, **110**, 17 235–17 240, doi:10.1073/pnas.1305332110.
- Santer, B. D., and Coauthors, 2017a: Causes of differences between model and satellite tropo spheric warming rates. *Nat. Geosci.*, **10**, 478–485.
- Santer, B. D., and Coauthors, 2017b: Comparing tropospheric warming in climate models and satellite data. *J. Clim.*, **30**, 3–4.
- Schmidt, G. A., D. T. Shindell, and K. Tsigaridis, 2014: Reconciling warming trends. *Nat. Geosci.*,
 7, 1–3.
- ⁸³⁸ Shine, K. P., and Coauthors, 2003: A comparison of model-simulated trends in stratospheric ⁸³⁹ temperatures. *Q. J. Roy. Met. Soc.*, **129**, 1565–1588, doi:10.1256/qj.02.186.
- Simmons, A., and Coauthors, 2020: Global stratospheric temperature bias and other stratospheric
 aspects of ERA5 and ERA5.1. Technical Memo 859, European Centre for Medium-Range
 Weather Forecasts, 40 pp.
- Solomon, S., 1999: Stratospheric ozone depletion: A review of concepts and history. *Rev. Geophys.*,
 37, 275–316.
- Solomon, S., J. S. Daniel, R. R. Neely, J.-P. Vernier, E. G. Dutton, and L. W. Thomason, 2011:
 The persistently variable "background" stratospheric aerosol layer and global climate change.
 Science, 333, 866–870.
- Solomon, S., D. J. Ivy, D. Kinnison, M. J. Mills, R. R. N. III, and A. Schmidt, 2016: Emergence
- of healing in the Antarctic ozone layer. *Science*, **353**, 269–274, doi:10.1126/science.aae0061.

Solomon, S., P. J. Young, and B. Hassler, 2012: Uncertainties in the evolution of stratospheric ozone
 and implications for recent temperature changes in the tropical lower stratosphere. *Geophys. Res. Lett.*, **39**, L17706, doi:10.1029/2012GL052723.

Solomon, S., and Coauthors, 2017: Mirrored changes in Antarctic ozone and stratospheric tem perature in the late 20th versus early 21st centuries. *J. Geophys. Res.*, 122, 8940–8950, doi:
 10.1002/2017JD026719.

Spencer, R. W., J. R. Christy, and W. D. Braswell, 2017: UAH version 6 global satellite
temperature products: Methodology and results. *Asia-Pac. J. Atmos. Sci.*, 53, 121–130, doi:
10.1007/s13143-017-0010-y.

Sperber, K. R., H. Annamalai, I.-S. Kang, A. Kitoh, A. Moise, A. Turner, B. Wang, and T. Zhou,
2013: The Asian summer monsoon: an intercomparison of CMIP5 vs. CMIP3 simulations of
the late 20th century. *Cli. Dyn.*, **41**, 2711–2744, doi:10.1007/s00382-012-1607-6.

Steiner, A., and Coauthors, 2020: Observed temperature changes in the troposphere and stratosphere from 1979 to 2018. *J. Clim.*, **33**, 8165–8194, doi:https://doi.org/10.1175/ JCLI-D-19-0998.1.

Stone, P. H., and J. H. Carlson, 1979: Atmospheric lapse rate regimes and their parameterization.
 J. Atmos. Sci., 36, 415–423.

⁸⁶⁷ Swart, N. C., S. T. Gille, J. C. Fyfe, and N. P. Gillett, 2018: Recent Southern Ocean warming and ⁸⁶⁸ freshening driven by greenhouse gas emissions and ozone depletion. *Nat. Geosci.*, **11**, 836–841.

Tatebe, H., and Coauthors, 2019: Description and basic evaluation of simulated mean state, internal
 variability, and climate sensitivity in MIROC6. *Geoscientific Model Development*, **12** (**7**), 2727–

⁸⁷¹ 2765, doi:10.5194/gmd-12-2727-2019.

40

- Taylor, K. E., R. J. Stouffer, and G. A. Meehl, 2012: An overview of CMIP5 and the experiment design. *Bull. Amer. Meteor. Soc.*, **93**, 485–498, doi:10.1175/BAMS-D-11-00094.1.
- Thomason, L. W., and Coauthors, 2018: A global space-based stratospheric aerosol climatology: 1979–2016. *Earth Syst. Sci. Data*, **10**, 469–492, doi:doi.org/10.5194/essd-10-469-2018.
- Thompson, D. W. J., and Coauthors, 2012: The mystery of recent stratospheric temperature trends.
 Nature, **491**, 692–697, doi:10.1038/nature11579.
- Thorne, P. W., J. R. Lanzante, T. C. Peterson, D. J. Seidel, and K. P. Shine, 2011: Tropospheric
- temperature trends: History of an ongoing controversy. *Wiley Inter. Rev.*, **2**, 66–88.
- ⁸⁸⁰ Trenberth, K. E., J. Fasullo, and L. Smith, 2005: Trends and variability in column-integrated ⁸⁸¹ atmospheric water vapor. *Cli. Dyn.*, **24**, 741–758.
- ⁸⁸² Trenberth, K. E., and Coauthors, 2007: Observations: Surface and Atmospheric Climate Change.
- Climate Change 2007: The Physical Science Basis. Contribution of Working Group I to the
- Fourth Assessment Report of the Intergovernmental Panel on Climate Change, S. Solomon,
- D. Qin, M. Manning, Z. Chen, M. Marquis, K. B. Averyt, M. Tignor, and H. L. Miller, Eds.,
 Cambridge University Press, 235–336.

 ⁸⁸⁷ US Senate, 2015: Data or Dogma? Promoting open inquiry in the debate over the magnitude of
 ⁸⁸⁸ human impact on Earth's climate. Hearing before the U.S. Senate Committee on Commerce,
 ⁸⁸⁹ Science, and Transportation, Subcommittee on Space, Science, and Competitiveness, One
 ⁸⁹⁰ Hundred and Fourteenth Congress, first session, December 8. [https://clio.columbia.edu/catalog/
 ⁸⁹¹ 12267036].

- Wang, S., T. Xu, W. Nie, C. Jiang, Y. Yang, Z. Fang, M. Li, and Z. Zhang, 2020: Evaluation of
 precipitable water vapor from five reanalysis products with ground-based GNSS bbservations.
 Remote Sensing, 12, 1817, doi:10.3390/rs12111817.
- Wentz, F. J., 2013: SSM/I Version-7 Calibration Report. Tech. Rep. Technical Report
 011012, 46 pp. [http://www.remss.com/papers/tech_reports/2012_Wentz_011012_Version-7_
 SSMI_Calibration.pdf].
- Wentz, F. J., and M. Schabel, 1998: Effects of orbital decay on satellite-derived lower-tropospheric
 temperature trends. *Nature*, **394**, 661–664.
- Wentz, F. J., and M. C. Schabel, 2000: Precise climate monitoring using complementary satellite
 data sets. *Nature*, 403, 414–416.
- Zelinka, M. D., T. A. Myers, D. T. McCoy, S. Po-Chedley, P. M. Caldwell, P. Ceppi, S. A. Klein,
 and K. E. Taylor, 2020: Causes of higher climate sensitivity in CMIP6 models. *Geophys. Res. Lett.*, 47, doi:10.1029/2019GL085782.
- Zou, C.-Z., M. D. Goldberg, and X. Hao, 2018: New generation of U.S. satellite microwave
 sounder achieves high radiometric stability performance for reliable climate change detection.
 Sci. Adv., **4**, eaau0049.
- ⁹⁰⁸ Zou, C.-Z., and H. Qian, 2016: Stratospheric temperature climate record from merged ⁹⁰⁹ SSU and AMSU-A observations. *J. Atmos. Ocean. Tech.*, **33**, 1967–1984, doi:10.1175/ ⁹¹⁰ JTECH-D-16-0018.1.
- ⁹¹¹ Zou, C.-Z., and W. Wang, 2011: Inter-satellite calibration of AMSU-A observations for weather ⁹¹² and climate applications. *J. Geophys. Res.*, **116**, D23113, doi:10.1029/2011JD016205.

913 LIST OF FIGURES

914 915 916 917 918 919 920 921 922 922 922 924 925 926	Fig. 1.	Time series of monthly-mean near-global averages of the temperature of the lower strato- sphere (TLS; panel A), the mid- to upper troposphere (TMT; panel B), and the lower troposphere (TLT; panel C). For TLS and TMT, observations are the average of the RSS "baseline", STAR, and UAH satellite data sets and the ERA 5.1 reanalysis. Since STAR does not produce a TLT data set, the observational average for TLT was calculated with RSS "baseline", UAH, and ERA5.1 only. CMIP5 synthetic satellite temperatures were computed from 123 realizations of historical climate change ("extended HIST") performed with 28 models. For CMIP6, 116 extended HIST realizations were used for TLS and 166 realizations for TMT and TLT (performed with 21 and 22 models, respectively). All temperature changes are defined as anomalies relative to climatological monthly means over 1979 to 2019. TMT is adjusted for the contribution it receives from stratospheric cooling (see Appendix B). Calculation of the multi-model average (MMA) involves first averaging over realizations of an individual model, then averaging over models.	. 46
927 928 929 930 931 932 933	Fig. 2.	Time series of monthly-mean anomalies of the temperature of the lower stratosphere (TLS) in CMIP6 extended HIST simulations. Results are for 21 individual CMIP6 models (in grey) and for the RSS "baseline" satellite data (in red). The CMIP6 multi-model average is also shown (bottom right panel). All anomalies are spatially averaged over 82.5°N-82.5°S and are defined relative to climatological monthly means over 1979 to 2019. The number of extended HIST realizations is indicated in parentheses. Vertical lines denote the times of maximum lower stratospheric warming in the RSS "baseline" data after the eruptions of El	
934 935 936 937 938 939 940 941 942 943	Fig. 3.	Chichón and Pinatubo	. 47
944 945 946 947 948 949 950 951 952 953 954 955 956 957 958	Fig. 4.	Least-squares linear trends in near-global average lower stratospheric temperature over ozone depletion and ozone recovery periods (1979 to 2000 and 2001 to 2019, respectively). Model results are from 123 and 116 extended HIST simulations performed with 28 different CMIP5 and 21 different CMIP6 models (respectively). CMIP5 trends include results from the 40-member CESM1 and 50-member CanESM2 large ensembles (LEs). CMIP6 trends incorporate the 50-member MIROC6 LE. Observed estimates of TLS trends rely on satellite data (RSS, STAR, and UAH) and the ERA5.1 reanalysis. Three different versions of the RSS data are shown. The 1:1 line (with trends of equal size over the the ozone depletion and ozone recovery periods) is marked in purple. For both periods, the CMIP5 multi-model average TLS trend is closer to the satellite data results. No individual CMIP5 or CMIP6 realization has larger lower stratospheric cooling in the ozone recovery period than in the ozone depletion period. This underscores the fact that the non-linear behavior of TLS over the satellite era is dominated by the response to ozone forcing, not by multi-decadal internal variability (Solomon et al. 2017). The shaded ellipses are the 2σ confidence intervals for each of the three LEs. For information on spatial averaging and calculation of multi-model	40

Fig. 5. Zonal-mean trends in monthly-mean lower stratospheric temperature (panels A,B) and in cor-960 rected mid- to upper tropospheric temperature (panels C,D). Results are for ozone depletion 961 and ozone recovery periods (left and right columns, respectively). For information regarding 962 the numbers of CMIP5 and CMIP6 models and extended HIST realizations, calculation of 963 multi-model averages, spatial averaging, and observational data, refer to Fig. 1. 50 964 Fig. 6. Scatter plot (panel A) of linear trends in near-global mean lower tropospheric temperature 965 (TLT) and mid- to upper tropospheric temperature (TMT) and histograms of the TMT/TLT 966 trend ratio (panel B). All trends are over 1979 to 2019. TMT is corrected for lower strato-967 spheric cooling. The multi-model averages include information from the 50- and 40-member CanESM2 and CESM1 LEs (for CMIP5) and from the 50-member CanESM5 and MIROC6 969 LEs (for CMIP6). The shaded ellipses in panel A are the 2σ confidence intervals for each 970 LE. Because TLT is not produced by STAR, the STAR TMT trend is plotted as a horizontal 971 line in panel A. Selected isopleths of equal values of the TMT/TLT trend ratio are denoted 972 by dashed grey lines in panel A. For further details of CMIP5 and CMIP6 realizations and 973 models, calculation of multi-model averages, spatial averaging, observational data sources, 974 and fits to histograms, refer to caption of Fig. 1 and SM. 51 975 Fig. 7. As for Fig. 4 but for linear trends in near-global average mid- to upper tropospheric temper-976 ature (TMT) over 1979 to 2000 (x-axis) and over 2001 to 2019 (y-axis). TMT is corrected 977 for the influence of lower stratospheric cooling. While Fig. 4 excluded TLS results from 978 the 50-member CanESM5 LE because of anomalous TLS variability, TMT trends from the 979 CanESM5 LE are minimally affected by this anomalous variability and are included here. 980 The 1:1 line (with TMT trends of equal size over the two periods) is marked in purple. 981 Simulated TMT trends are larger in the second analysis period in approximately 90% of the 982 realizations. In satellite data, trends in the two periods are of roughly equivalent size. 52 983 Fig. 8. Trends and regression coefficients in CMIP5, CMIP6, and observations. Maximally over-984 lapping L-year trends were calculated from time series of monthly-mean, near-global spatial 985 averages of TLS, TMT, and TLT (panels A-D, E-H, and I-L, respectively). The regression 986 coefficient $b_{\text{{TMT:TLT}}}$, a measure of amplification of warming in the tropical troposphere, 987 was computed with maximally overlapping L-year time series of monthly-mean TMT and 988 TLT, spatially averaged over ocean areas between 20°N-20°S (panels M-P). The four selected 989 timescales shown here are 10, 20, 30, and 40 years (columns 1-4, respectively). Histograms 990 of these L-year trends and regression coefficients are shown for CMIP5 and CMIP6 extended 991 HIST simulations and for pre-industrial control runs. Histograms are weighted to account 992 for model differences in the number of extended HIST simulations or in control run length. 993 For each histogram, results are normalized by the total number of trend or regression coef-994 ficient samples. Fits to the model trend and $b_{\{\text{TMT:TLT}\}}$ distributions were performed with 995 kernel density estimation (see SM). The vertical lines for the observed trends and regression 996 coefficients are the averages across the maximally overlapping L-year analysis periods. For 997 trends in TMT, the RSS "MSU merge" and STAR results are almost identical. 53 998 **Fig. 9.** Scatter plot of tropical trends in WV and SST (panel A), WV and TLT (panel B), WV 999 and corrected TMT (panel C), and corrected TMT and TLT (panel D). Trends are over 1000 1988 to 2019, the period of availability of observed WV data from 7 different microwave 1001 radiometers (Mears et al. 2018), and were calculated with WV, TLT, TMT and SST data 1002 averaged over tropical oceans (20°N-20°S). Before computing WV trends, monthly-mean 1003 WV anomalies were expressed as percentages with respect to climatological monthly means. 1004 Because satellite-derived WV is produced by RSS only, all satellite TLT and TMT trends in 1005 panels B and C are plotted against the RSS WV trend. ERA5.1 TLT and TMT trends are

plotted against the WV trend from the reanalysis. Since there are 4 different observed SST

data sets and 6 different observed TMT data sets, there are 4×6 combinations of SST and

1006

1007

1008

1009 1010 1011 1012 1013 1014		TMT trends in panel D. The <i>x</i> -axis position of observational symbols in panel D reflects the observed SST trend; the <i>y</i> -axis position depends on the observed TMT trend. The CMIP5 multi-model average trend in each panel include results from the CanESM2 and CESM1 LEs; the CMIP6 multi-model average trend include results from the CanESM5 and MIROC6 LEs. The regression fits and slopes were estimated with Orthogonal Distance Regression and are given separately for CMIP5 and CMIP6 results (see SM).	54
1015 1016 1017 1018 1019 1020 1021 1022 1023 1024	Fig. 10.	Histograms of the ratios between the model trends plotted in each of the four panels of Figure 9. Results are for $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, $R_{\{WV/TMT\}}$, and $R_{\{TMT/SST\}}$ (panels A-D, respectively). Observational trend ratios in panels A-C are plotted as vertical lines. Each satellite TMT data set in panel D can be paired with 4 different observed SST trends, yielding 4 different observed values of $R_{\{TMT/SST\}}$ (see Fig. 9 caption). Observed $R_{\{TMT/SST\}}$ values in panel D are plotted in six rows, one row per satellite TMT data set. The vertical spacing and <i>y</i> -axis location of rows is nominal; the vertical ordering of rows reflects the size of the observed tropical TMT trend over 1988 to 2019. The largest TMT trend (in the STAR data set) has the largest <i>y</i> -axis offset in panel D. For details regarding fits to the model histograms and histogram weighting, refer to SM.	. 55
1025 1026 1027 1028 1030 1031 1032 1033 1034 1035 1036 1037	Fig. 11.	Normalized differences (<i>Z</i> -scores) between observed scaling ratios and the mean of model scaling ratio distributions. Results in panel A are for tests of $R_{\{WV/TLT\}}$ ratios based on 5 different observed TLT data sets and for tests of $R_{\{WV/TMT\}}$ and $R_{\{TMT/SST\}}$ ratios based on 6 different observed TMT data sets. Panel B involves tests of $R_{\{WV/SST\}}$ and $R_{\{TMT/SST\}}$ with 4 different observed SST data sets. All <i>Z</i> -scores were calculated with the scaling ratio data in Fig. 10. For each ratio tested, the observed ratio is subtracted from the mean of the CMIP5 or CMIP6 sampling distribution of the ratio. These differences are normalized by the CMIP5 or CMIP6 standard deviation of the ratio's sampling distribution; CMIP5 and CMIP6 <i>Z</i> -scores are then averaged. For the $R_{\{TMT/SST\}}$ ratios in panel A, there is an additional averaging step: each observed TMT data set can be paired with 4 different observed SST data set, yielding 4 different <i>Z</i> -scores (see rows in Fig. 10D). We average these 4 values per TMT data set. Likewise, each observed SST data set in panel B can be paired with 6 different TMT data sets, yielding 6 different values of $R_{\{TMT/SST\}}$ (see columns in Fig. 10D). We average these 6 values per SST data set. The brown bars are average <i>Z</i> -scores for different types of scaling	
1039		ratio	. 56



FIG. 1: Time series of monthly-mean near-global averages of the temperature of the lower stratosphere (TLS; panel A), the mid- to upper troposphere (TMT; panel B), and the lower troposphere (TLT; panel C). For TLS and TMT, observations are the average of the RSS "baseline", STAR, and UAH satellite data sets and the ERA 5.1 reanalysis. Since STAR does not produce a TLT data set, the observational average for TLT was calculated with RSS "baseline", UAH, and ERA5.1 only. CMIP5 synthetic satellite temperatures were computed from 123 realizations of historical climate change ("extended HIST") performed with 28 models. For CMIP6, 116 extended HIST realizations were used for TLS and 166 realizations for TMT and TLT (performed with 21 and 22 models, respectively). All temperature changes are defined as anomalies relative to climatological monthly means over 1979 to 2019. TMT is adjusted for the contribution it receives from stratospheric cooling (see Appendix B). Calculation of the multi-model average (MMA) involves first averaging over realizations of an individual model, then averaging over models.



FIG. 2: Time series of monthly-mean anomalies of the temperature of the lower stratosphere (TLS) in CMIP6 extended HIST simulations. Results are for 21 individual CMIP6 models (in grey) and for the RSS "baseline" satellite data (in red). The CMIP6 multi-model average is also shown (bottom right panel). All anomalies are spatially averaged over 82.5°N-82.5°S and are defined relative to climatological monthly means over 1979 to 2019. The number of extended HIST realizations is indicated in parentheses. Vertical lines denote the times of maximum lower stratospheric warming in the RSS "baseline" data after the eruptions of El Chichón and Pinatubo.



FIG. 3: Root-Mean-Square (RMS) differences between simulated and observed volcanic signals in lower stratospheric temperature in CMIP5 models (panels A, B) and CMIP6 models (panels C, D). RMS differences were calculated for 24-month periods after the 1982 eruption of El Chichón (panels A, C) and the 1991 Pinatubo eruption (panels B, D). The observational target is the RSS "baseline" TLS time series, spatially averaged over 82.5°N-82.5°S. Blue dots denote RMS values from individual realizations of the CMIP5 and CMIP6 extended HIST runs. Horizontal bars are average RMS differences for individual models. The dashed vertical lines are the multi-model average RMS differences, calculated by first averaging RMS values over a model's individual realizations, and then averaging over models.



FIG. 4: Least-squares linear trends in near-global average lower stratospheric temperature over ozone depletion and ozone recovery periods (1979 to 2000 and 2001 to 2019, respectively). Model results are from 123 and 116 extended HIST simulations performed with 28 different CMIP5 and 21 different CMIP6 models (respectively). CMIP5 trends include results from the 40-member CESM1 and 50-member CanESM2 large ensembles (LEs). CMIP6 trends incorporate the 50-member MIROC6 LE. Observed estimates of TLS trends rely on satellite data (RSS, STAR, and UAH) and the ERA5.1 reanalysis. Three different versions of the RSS data are shown. The 1:1 line (with trends of equal size over the the ozone depletion and ozone recovery periods) is marked in purple. For both periods, the CMIP5 multi-model average TLS trend is closer to the satellite data results. No individual CMIP5 or CMIP6 realization has larger lower stratospheric cooling in the ozone recovery period than in the ozone depletion period. This underscores the fact that the non-linear behavior of TLS over the satellite era is dominated by the response to ozone forcing, not by multi-decadal internal variability (Solomon et al. 2017). The shaded ellipses are the 2σ confidence intervals for each of the three LEs. For information on spatial averaging and calculation of multi-model averages, refer to Fig. 1.



FIG. 5: Zonal-mean trends in monthly-mean lower stratospheric temperature (panels A,B) and in corrected mid- to upper tropospheric temperature (panels C,D). Results are for ozone depletion and ozone recovery periods (left and right columns, respectively). For information regarding the numbers of CMIP5 and CMIP6 models and extended HIST realizations, calculation of multi-model averages, spatial averaging, and observational data, refer to Fig. 1.



FIG. 6: Scatter plot (panel A) of linear trends in near-global mean lower tropospheric temperature (TLT) and mid- to upper tropospheric temperature (TMT) and histograms of the TMT/TLT trend ratio (panel B). All trends are over 1979 to 2019. TMT is corrected for lower stratospheric cooling. The multi-model averages include information from the 50- and 40-member CanESM2 and CESM1 LEs (for CMIP5) and from the 50-member CanESM5 and MIROC6 LEs (for CMIP6). The shaded ellipses in panel A are the 2σ confidence intervals for each LE. Because TLT is not produced by STAR, the STAR TMT trend is plotted as a horizontal line in panel A. Selected isopleths of equal values of the TMT/TLT trend ratio are denoted by dashed grey lines in panel A. For further details of CMIP5 and CMIP6 realizations and models, calculation of multi-model averages, spatial averaging, observational data sources, and fits to histograms, refer to caption of Fig. 1 and SM.



FIG. 7: As for Fig. 4 but for linear trends in near-global average mid- to upper tropospheric temperature (TMT) over 1979 to 2000 (*x*-axis) and over 2001 to 2019 (*y*-axis). TMT is corrected for the influence of lower stratospheric cooling. While Fig. 4 excluded TLS results from the 50-member CanESM5 LE because of anomalous TLS variability, TMT trends from the CanESM5 LE are minimally affected by this anomalous variability and are included here. The 1:1 line (with TMT trends of equal size over the two periods) is marked in purple. Simulated TMT trends are larger in the second analysis period in approximately 90% of the realizations. In satellite data, trends in the two periods are of roughly equivalent size.



FIG. 8: Trends and regression coefficients in CMIP5, CMIP6, and observations. Maximally overlapping *L*-year trends were calculated from time series of monthly-mean, near-global spatial averages of TLS, TMT, and TLT (panels A-D, E-H, and I-L, respectively). The regression coefficient $b_{\{\text{TMTTLT}\}}$, a measure of amplification of warming in the tropical troposphere, was computed with maximally overlapping *L*-year time series of monthly-mean TMT and TLT, spatially averaged over ocean areas between 20°N-20°S (panels M-P). The four selected timescales shown here are 10, 20, 30, and 40 years (columns 1-4, respectively). Histograms of these *L*-year trends and regression coefficients are shown for CMIP5 and CMIP6 extended HIST simulations and for pre-industrial control runs. Histograms are weighted to account for model differences in the number of extended HIST simulations or in control run length. For each histogram, results are normalized by the total number of trend or regression coefficient samples. Fits to the model trend and $b_{\{\text{TMTTLT}\}}$ distributions were performed with kernel density estimation (see SM). The vertical lines for the observed trends and regression coefficients are the averages across the maximally overlapping *L*-year analysis periods. For trends in TMT, the RSS "MSU merge" and STAR results are almost identical.



FIG. 9: Scatter plot of tropical trends in WV and SST (panel A), WV and TLT (panel B), WV and corrected TMT (panel C), and corrected TMT and TLT (panel D). Trends are over 1988 to 2019, the period of availability of observed WV data from 7 different microwave radiometers (Mears et al. 2018), and were calculated with WV, TLT, TMT and SST data averaged over tropical oceans ($20^{\circ}N-20^{\circ}S$). Before computing WV trends, monthly-mean WV anomalies were expressed as percentages with respect to climatological monthly means. Because satellite-derived WV is produced by RSS only, all satellite TLT and TMT trends in panels B and C are plotted against the RSS WV trend. ERA5.1 TLT and TMT trends are plotted against the WV trend from the reanalysis. Since there are 4 different observed SST data sets and 6 different observed TMT data sets, there are 4×6 combinations of SST and TMT trends in panel D. The *x*-axis position of observational symbols in panel D reflects the observed SST trend; the *y*-axis position depends on the observed TMT trend. The CMIP5 multi-model average trend in each panel include results from the CanESM2 and CESM1 LEs; the CMIP6 multi-model average trend include results from the CanESM5 and MIROC6 LEs. The regression fits and slopes were estimated with Orthogonal Distance Regression and are given separately for CMIP5 and CMIP6 results (see SM).



FIG. 10: Histograms of the ratios between the model trends plotted in each of the four panels of Figure 9. Results are for $R_{\{WV/SST\}}$, $R_{\{WV/TLT\}}$, $R_{\{WV/TMT\}}$, and $R_{\{TMT/SST\}}$ (panels A-D, respectively). Observational trend ratios in panels A-C are plotted as vertical lines. Each satellite TMT data set in panel D can be paired with 4 different observed SST trends, yielding 4 different observed values of $R_{\{TMT/SST\}}$ (see Fig. 9 caption). Observed $R_{\{TMT/SST\}}$ values in panel D are plotted in six rows, one row per satellite TMT data set. The vertical spacing and y-axis location of rows is nominal; the vertical ordering of rows reflects the size of the observed tropical TMT trend over 1988 to 2019. The largest TMT trend (in the STAR data set) has the largest y-axis offset in panel D. For details regarding fits to the model histograms and histogram weighting, refer to SM.



FIG. 11: Normalized differences (Z-scores) between observed scaling ratios and the mean of model scaling ratio distributions. Results in panel A are for tests of $R_{\{WV/TLT\}}$ ratios based on 5 different observed TLT data sets and for tests of $R_{\{WV/TMT\}}$ and $R_{\{TMT/SST\}}$ ratios based on 6 different observed SST data sets. Panel B involves tests of $R_{\{WV/TMT\}}$ and $R_{\{TMT/SST\}}$ with 4 different observed SST data sets. All Z-scores were calculated with the scaling ratio data in Fig. 10. For each ratio tested, the observed ratio is subtracted from the mean of the CMIP5 or CMIP6 sampling distribution of the ratio. These differences are normalized by the CMIP5 or CMIP6 standard deviation of the ratio's sampling distribution; CMIP5 and CMIP6 Z-scores are then averaged. For the $R_{\{TMT/SST\}}$ ratios in panel A, there is an additional averaging step: each observed TMT data set can be paired with 4 different observed SST data sets, yielding 4 different Z-scores (see rows in Fig. 10D). We average these 4 values per TMT data sets, yielding 6 different values of $R_{\{TMT/SST\}}$ (see columns in Fig. 10D). We average these 6 values per SST data set. The brown bars are average Z-scores for different types of scaling ratio.