

Demographics of young stars and their protoplanetary disks: lessons learned on disk evolution and its connection to planet formation

Carlo F. Manara

European Southern Observatory (ESO)

Megan Ansdell

National Aeronautics and Space Administration (NASA)

Giovanni P. Rosotti

University of Leicester & Università degli Studi di Milano

A. Meredith Hughes

Wesleyan University

Philip J. Armitage

Flatiron Institute & Stony Brook University

Giuseppe Lodato

Università degli Studi di Milano

Jonathan P. Williams

Institute for Astronomy, University of Hawaii

Since Protostars and Planets VI (PPVI), our knowledge of the global properties of protoplanetary and debris disks, as well as of young stars, has dramatically improved. At the time of PPVI, mm-observations and optical to near-infrared spectroscopic surveys were largely limited to the Taurus star-forming region, especially of its most massive disk and stellar population. Now, near-complete surveys of multiple star-forming regions cover both spectroscopy of young stars and mm interferometry of their protoplanetary disks. This provides an unprecedented statistical sample of stellar masses and mass accretion rates, as well as disk masses and radii, for almost 1000 young stellar objects within 300 pc from us, while also sampling different evolutionary stages, ages, and environments. At the same time, surveys of debris disks are revealing the bulk properties of this class of more evolved objects. This chapter reviews the statistics of these measured global star and disk properties and discusses their constraints on theoretical models describing global disk evolution. Our comparisons of observations to theoretical model predictions extends beyond the traditional viscous evolution framework to include analytical descriptions of magnetic wind effects. Finally, we discuss how recent observational results can provide a framework for models of planet population synthesis and planet formation.

1. INTRODUCTION

Protoplanetary disks evolve during their lifetime, changing their gas and dust content and morphology in response to the effects of various physical processes. A thorough understanding on how this evolution happens, and how it can be described in models to accurately predict the properties of disks at the time of planet formation, is key to understand how planets come to be (e.g., [Morbidelli and Raymond 2016](#)).

Simple descriptions of disk evolution are the best way

for setting up population synthesis models aimed at ab-initio descriptions of how planets form (e.g., [Benz et al. 2014](#)). The viscous evolution framework for protoplanetary disks ([Lynden-Bell and Pringle 1974](#); [Pringle 1981](#)) has been extensively used to interpret observations (e.g., [Hartmann et al. 1998](#); [Alexander et al. 2014](#); [Ercolano and Pascucci 2017](#)). However, the limits of this model have called for new developments within this framework, and revamping of other models to describe how angular momentum is transported in disks, in particular as the result of the

presence of magnetically induced disk winds (e.g., *Pudritz et al. 2007*). Indeed, the inclusion of non-ideal magneto-hydrodynamic (MHD) effects in simulations is showing the relevance of such disk winds in disk evolution (e.g., *Lesur et al. 2013; Bai 2016*). Each of these models also provide clues on the final phases of the evolution of protoplanetary disks and how this could be connected to the properties of debris disks (e.g., *Hughes et al. 2018*). Finally, the description of how the dust content of disks evolves with time (e.g., *Testi et al. 2014*) is beginning to be coupled with global disk evolution models (e.g., *Pinilla et al. 2020; Sellek et al. 2020b*).

Since around the time of the Protostars and Planets VI (PPVI) conference, a conspicuous number of surveys of young stellar objects in different star-forming regions covering a range of ages have been carried out with optical spectroscopy and millimeter interferometry (Fig. 1). This recent availability of large statistical samples of hundreds of young stellar objects with measured stellar and disk masses, mass accretion rates, disk radii and other properties opens new ways to test disk evolution models (e.g., *Manara et al. 2016; Tazzari et al. 2017*). Similarly, improved knowledge of debris disks around young main sequence stars shows the fate of (some) protoplanetary disks and hints of a connection to planetary system formation and early evolution (*Hughes et al. 2018*).

This chapter focuses on the results from surveys of young stellar objects - starting from the optically visible Class II stage - and debris disks, describing how stellar and global disk properties are derived and the main observational results (§ 2). These results are collected and homogenized in this review, and provided to the community to be used in future works¹. After reviewing predictions from the two main classes of models, the viscous framework and the disk-wind driven evolution model, the latter described with a simple analytical framework (§ 3), we perform a meta-analysis of the constraints on these models by comparing with the measured global stellar and disk properties (§ 4). We briefly describe how advances in disk evolution inform planet formation and population synthesis models (§ 5) and conclude with our perspective for the future (§ 6).

2. OBSERVATIONS OF YOUNG STARS AND DISKS

The key observational properties needed to constrain disk evolution models are the stellar mass, stellar age, and mass accretion rate onto the central star (§ 2.1) as well as the disk bulk mass and size, in both the gas and dust, during the main disk evolution phase (§ 2.2) and at the end of the disk lifetime and during the debris disk phase (§ 2.3). These properties are observed to be related to each other (§ 4.1), constraining the disk evolution mechanisms to be used. Here we describe all these global properties, shortly assessing also the current biases and limitations of the performed surveys (§ 2.4), and neglecting the effect of disk

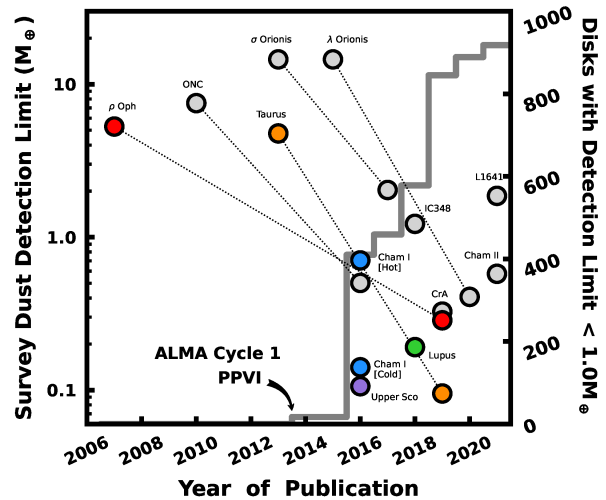


Fig. 1.— The improvement of (sub-)mm protoplanetary disk survey dust detection limits from PPVI to now. The left axis is 3σ survey sensitivity translated into dust mass, where the corresponding circles are colored if the region is closer than 300 pc and included in Table 1, and gray otherwise; dotted lines connect the same region re-observed at a later date. The gray histogram corresponds to the right axis for the number of disks with dust detection limits $\lesssim 1 M_{\odot}$.

structures, discussed in the Chapter by *Bae et al.*

2.1. Stellar and accretion properties for young stellar objects from spectroscopy

The determination of the basic observables, stellar temperature (T_{eff}) and luminosity ($L_{\star}$), is essential to derive the physical properties such as stellar mass ($M_{\star}$). In young stars with disks, the contribution of veiling (filling in of absorption lines) due to accretion and from extinction is non-negligible, and must be accounted for when determining the photospheric parameters. In turn, this allows one to measure the accretion luminosity (L_{acc}) and infer the mass accretion rate ($\dot{M}_{\text{acc}}$). Here we review the methods currently used to measure the stellar and accretion properties for populations of young stars with disks.

2.1.1. Spectral types, stellar, and accretion luminosity

The determination of stellar properties for Pre-Main-Sequence (PMS) stars was first carried out with optical spectroscopy (e.g., *Cohen and Kuhi 1979; Kenyon and Hartmann 1995; Hillenbrand 1997*). However, it was soon realized that for these young, extincted, and accreting stars it is important to simultaneously describe the expected underlying photospheric emission and the continuum excess due to accretion (e.g., *Bertout et al. 1988*), together with a correct determination of the extinction. This requires the use of broad wavelength coverage and absolute flux-calibrated spectra. Whereas the spectral range from $\lambda \sim 4000 - 7000 \text{ \AA}$ allows spectral types (SpT) to be accu-

¹Table 1 is available publicly at <http://ppvii.org/chapter/15/>

rately determined (*Herczeg and Hillenbrand 2014; Fang et al. 2021*), extending the coverage to $\lambda < 4000\text{\AA}$ —thereby including the Balmer jump and continuum region and, with the *Hubble Space Telescope* (HST), the near-ultraviolet (NUV) region—considerably improves the determination of the extinction and the contribution of the excess emission due to accretion (e.g., *Gullbring et al. 1998; Calvet et al. 2000; Herczeg and Hillenbrand 2008; Ingleby et al. 2013; Manara et al. 2013a*).

The best stellar templates for the photospheric properties of young stars are non-accreting PMS stars (e.g., *Gullbring et al. 1998*), as they have similar gravity as accreting PMS stars (e.g., *Stelzer et al. 2013; Herczeg and Hillenbrand 2014; Frasca et al. 2015a, 2017*), while at the same time having similar chromospheric emission properties as accreting targets (e.g., *Ingleby et al. 2011; Manara et al. 2013b*). The latter is a particularly relevant point since the chromospheric activity in these targets is much higher than in main-sequence stars. The analyses by *Manara et al. (2013b, 2017a)* have shown how this chromospheric emission scales with stellar temperature in PMS stars, allowing one to discriminate between emission lines dominated by chromospheric or accretion-related emission. In recent years, larger libraries of empirical templates covering broad wavelength ranges ($\lambda \sim 3000\text{--}25000\text{ \AA}$) have been collected and are publicly available for low-mass PMS stars and brown dwarfs (*Manara et al. 2013b, 2017a; Manjavacas et al. 2016, 2020*). Additional empirical templates have been collected with HST (e.g., *Ingleby et al. 2014*). All these empirical templates are being used to determine the stellar properties of accreting stars, and they can be used to compare with and to improve synthetic models. Related to the latter, the conversion from a spectral type (SpT) to a value of T_{eff} has been subject of discussion in the last years. Simultaneous measurements of T_{eff} from comparison with synthetic spectra and SpT from empirical templates (e.g., *Frasca et al. 2017; Manara et al. 2021*) highlight the limits of previously used relations (e.g., *Kenyon and Hartmann 1995; Luhman et al. 2003*). New relations have been empirically calibrated by *Pecaut and Mamajek (2013)* and *Herczeg and Hillenbrand (2014)*, and should be used to convert SpT in T_{eff} for PMS stars.

Equally important, a good description of the excess emission due to accretion is required to describe the observed spectra of accreting young stars. As discussed in the review by *Hartmann et al. (2016)*, the complex structure of the accretion shock region has been described with a physical model by *Calvet et al. (2000)* and used among others by *Gullbring et al. (1998)* or *Ingleby et al. (2013, 2014)* to model HST spectra. The recent revision of these shock models by *Robinson and Espaillat (2019)* now includes a treatment of the postshock and preshock regions with CLOUDY (*Ferland et al. 2017*), leading to higher emissivity of the postshock region, and multiple components of the model can be considered in order to match the measured veiling at optical wavelengths. At the same time, the simpler and less physical isothermal hydrogen slab

models are still being used to model the excess emission due to accretion (e.g., *Herczeg and Hillenbrand 2008; Rigliaco et al. 2012; Manara et al. 2013a; Rugel et al. 2018; Alcalá et al. 2014, 2017; Venuti et al. 2019b*). Finally, simpler assumptions on the shape of the accretion excess emission at optical wavelengths, such as a constant flux, are used in some cases (*Herczeg and Hillenbrand 2014; Fang et al. 2021*). The combination of high-resolution spectra taken from the ground with nearly contemporaneous HST spectra promises to constrain these accretion models and quantify the effects of simple assumptions (e.g., *Alcalá et al. 2019; Manara et al. 2021; Espaillat et al. 2022*).

In tandem with the refinements in modeling, there has been significant advances in spectroscopic capability. In particular, the X-Shooter instrument has been offered on the ESO Very Large Telescope (VLT) with its unique capability to cover simultaneously at medium resolution ($R \sim 10,000 - 20,000$) the wide wavelength range $\lambda \sim 0.3 - 2.5\mu\text{m}$ (*Vernet et al. 2011*). Thanks to its sensitivity and to its location in the Southern Hemisphere, this instrument is being used to survey a number of star-forming regions, including Lupus (*Alcalá et al. 2014, 2017*), Chamaeleon I (*Manara et al. 2016, 2017b*), η -Chamaeleon (*Rugel et al. 2018*), TWA (*Venuti et al. 2019b*), and Upper Scorpius (*Manara et al. 2020*). Surveys carried out with this instrument for brown dwarfs (*Manara et al. 2015; Manjavacas et al. 2020*) are still incomplete, whereas surveys of the Herbig Ae/Be star populations (*Fairlamb et al. 2015, 2017*) include all the known targets prior to *Gaia* (*Vioque et al. 2020*) visible from the VLT. Photospheric templates of spectra of non-accreting pre-main sequence stars obtained with this instrument are available for a wide range of spectral types from G- to L-type (*Manara et al. 2013b, 2017a; Manjavacas et al. 2016, 2020*). For earlier type stars the synthetic spectra by *Castelli and Kurucz (2003)* are typically used.

The wide simultaneous wavelength coverage with absolute flux-calibration of the X-Shooter spectra allows the accretion luminosity to be determined from the UV-excess in the Balmer continuum region (*Manara et al. 2013a*), and also the luminosity of a number of permitted emission lines, from the high- n Balmer series lines in the near-UV, to the Bracket series lines in the near-infrared, including emission lines of helium and calcium (e.g., *Alcalá et al. 2014*). This has allowed the re-calibration of the relations between emission line luminosity and UV-excess measured accretion luminosity known from the literature (e.g., *Muzerolle et al. 1998; Mohanty et al. 2005; Natta et al. 2006; Herczeg and Hillenbrand 2008*) using a significantly larger number of targets and covering a wider range of spectral types and accretion luminosities. As demonstrated by *Alcalá et al. (2014)*, the line luminosities are more reliable tracers of L_{acc} than the measurement of the width of the $H\alpha$ line. The new line to accretion luminosity relations (*Alcalá et al. 2017*) can now be applied to spectroscopic datasets not covering the Balmer continuum region but a number of emission lines. Indeed, *Rigliaco et al. (2012)* and others (e.g., *Alcalá et al. 2017*) have shown that the combination of accretion

luminosity measured with a significant number of emission lines (≥ 5 -6) leads to estimates of accretion luminosity with small uncertainties (~ 0.2 - 0.3 dex) and good agreement with the values obtained from the fit of the Balmer continuum. Comparing accretion luminosity determinations from lines at different wavelengths also provides a way to independently determine extinction (e.g., [Pinilla et al. 2021](#)). However, it should be noted that only a proper inclusion of the impact of extinction and of veiling due to accretion at all stages of the spectral analysis overcomes the degeneracies between these parameters, and that the UV-excess is key for determining the excess due to accretion (e.g., [Manara et al. 2013a](#); [Herczeg and Hillenbrand 2014](#)). This implies that methods based on assumptions of either stellar temperatures and/or extinction and/or veiling would have larger degenerate uncertainties in the derived parameters.

Other methods to derive stellar and accretion parameters of young stars based on photometric surveys (e.g., [De Marchi et al. 2013](#); [Beccari et al. 2015](#); [De Marchi et al. 2017](#); [Venuti et al. 2014a](#); [Kalari et al. 2015](#); [Kalari 2019](#); [Biazio et al. 2019](#)) and multi-object spectroscopic surveys (e.g., [Randich et al. 2013](#); [Lanzafame et al. 2015](#); [Frasca et al. 2015b](#); [Rigliaco et al. 2016](#); [Venuti et al. 2018](#)) have also proven valuable, in particular in providing large statistical samples. These large samples allow us to understand the typical extent of accretion variability (see § 2.1.3) and to find populations of strong accretors on the outskirts of known star-forming regions, which could represent a different episode of star-formation (e.g., [De Marchi et al. 2017](#); [Beccari et al. 2015](#)).

Finally, both temperature and luminosity estimates are affected by stellar spots. Due to the presence of spots, different values for these parameters are obtained using high-resolution blue spectra or medium- to low-resolution spectra at the reddest optical wavelength and in the near-infrared (e.g., [Gully-Santiago et al. 2017](#)). Moreover, stellar variability also impacts the measured $L_\star$ (see chapter by [Fischer et al.](#)).

2.1.2. Determination of stellar masses and ages

The classical method to determine $M_\star$ (and stellar age with all its caveats, see [Soderblom et al. 2014](#)) is to compare the position of the PMS stars on the Hertzsprung-Russell Diagram (HRD) with the PMS evolutionary model tracks. Building on pioneering work (e.g., [Siess et al. 2000](#)), recent years have seen the development of a number of new and more advanced models. One of the main issues that these new models aimed to address is the fact that a large spread in $L_\star$ is observed at a given temperature in any nearby cluster even with the most advanced analysis methods coupled with accurate membership vetting (e.g., [Herczeg and Hillenbrand 2015](#); [Alcalá et al. 2017](#); [Fang et al. 2021](#)). This spread is either a real age spread or due to missing physical mechanisms. Recent *Gaia*-based analysis of nearby star-forming regions support the idea that an age spread is present in individual regions, in particular between the on-

cloud and off-cloud populations (e.g., [Beccari et al. 2018](#); [Krolikowski et al. 2021](#); [Esplin and Luhman 2022](#)).

The models by [Baraffe et al. \(2015\)](#) have updated the assumptions on the atmospheric conventions and metallicity from previous models. Some of these models start to include the effect of accretion prior to and during the PMS evolution, which is a possible solution of the luminosity spread issue (e.g., [Baraffe et al. 2012](#)). In addition, [Feiden \(2016\)](#) developed new PMS evolutionary models which, in some cases, include the effect of magnetic fields on the evolution of PMS stars. The latter is modelled extrapolating 1D simulations to 3D, but already show a promising agreement with the high-luminosity, low-mass stars. Furthermore, the models by [Somers et al. \(2020\)](#) have recently included the effect of stellar spots on the position of a PMS star on the HRD. Each model dramatically changes the inferred stellar age, and also in some cases the value of $M_\star$.

Different tests of these models are being carried out. [Herczeg and Hillenbrand \(2015\)](#) has shown that the non-magnetic models by [Baraffe et al. \(2015\)](#) and [Feiden \(2016\)](#) are in better agreement with the empirically determined isochrones for a number of young stellar clusters and associations. Similarly, eclipsing binaries provide a further tests of the models ([Stassun et al. 2014](#); [Rizzuto et al. 2020](#)) but can only be applied to a limited number of systems. In recent years, the availability of spectrally resolved observations of CO emission from disks with the Atacama Large Millimeter/submillimeter Array (ALMA) has also enabled the use of dynamical stellar mass estimates to test models (e.g., [Czekala et al. 2016](#); [Yen et al. 2018](#); [Sheehan et al. 2019](#); [Simon et al. 2017, 2019](#); [Premnath et al. 2020](#); [Pegues et al. 2021](#)). The results from these works are still diverse, with some studies showing that a better agreement with dynamical mass estimates is reached when using magnetic models in the range $M_\star \sim 0.4 - 1 M_\odot$ ([Simon et al. 2019](#)) or $M_\star \sim 0.6 - 1.3 M_\odot$ ([Braun et al. 2021](#)). The non-magnetic models provide instead a better agreement for lower-mass stars ([Braun et al. 2021](#)). However, recent works have also shown the limit of comparing dynamical masses measured from different molecules, as these can have systematic uncertainty ([Premnath et al. 2020](#)) and discrepancy between dynamical masses with non-magnetic evolutionary models also for very low-mass stars, although on a small number of targets ([Pegues et al. 2021](#)). Further work is still needed in this respect.

2.1.3. Mass accretion rate determination and uncertainty

The combination of the stellar parameters $M_\star$ and $R_\star$, the latter inferred usually from T_{eff} and $L_\star$, can be used to convert the estimated L_{acc} , either from the UV-excess or from line emission, into $\dot{M}_{\text{acc}}$ ([Hartmann et al. 2016](#)).

The main sources of uncertainties in this step are the uncertainty in the stellar parameters, in particular $M_\star/R_\star$, and possible variability of the accretion rate. Estimating the typical variability of accretion has been a topic of research in the last years. Several works are showing that, typically, ac-

cretion variability in disk-bearing PMS stars peaks at about a factor ~ 3 ($\lesssim 0.4$ dex) on timescales of $\sim$ days to weeks (e.g., [Biazzo et al. 2012, 2014](#); [Costigan et al. 2014](#); [Venuti et al. 2014b](#); [Robinson and Espaillat 2019](#); [Hartmann et al. 2016](#); [Manara et al. 2021](#), and more). However, secular variability could be more intense, at least for some objects (see also Chapter by [Fischer et al.](#)).

Now with well determined *Gaia* distances, the uncertainties in the determination of stellar and accretion properties imply a total fractional uncertainty on individual measurements of $\dot{M}_{\text{acc}}$ at any given time of ~ 0.35 dex ([Alcalá et al. 2014, 2017](#)).

2.2. Protoplanetary disk masses and sizes from mm interferometry

Millimeter interferometry is one of the best ways to measure the bulk properties of disks, in particular their masses, sizes, and large-scale spatial features (e.g., [Williams and Cieza 2011](#)). ALMA’s combination of sensitivity and resolution has enabled near-complete surveys of these bulk properties for disk populations across all the major nearby star-forming regions (e.g., [Ansdell et al. 2016](#); [Barenfeld et al. 2016](#); [Pascucci et al. 2016](#); [Eisner et al. 2018](#); [Ruíz-Rodríguez et al. 2018](#); [Cieza et al. 2019](#); [Cazzoletti et al. 2019](#); [Grant et al. 2021](#); [Villenave et al. 2021](#); [van Terwisga et al. 2022](#)), which have led to a significant improvement of detection rate and number of surveyed regions (see Fig. 1). These surveys have almost all been carried out in Band 6/7 of ALMA ($\sim 890\mu\text{m} - 1.3\text{ mm}$) with only one survey to date in Band 3 ($\sim 3\text{ mm}$, [Tazzari et al. 2021b](#)).

The mm continuum and several mm emission lines can be used to measure the total disk masses (e.g., [Bergin and Williams 2017](#)). However, these tracers are indirect as the vast majority of the disk mass is in unobservable cold H_2 gas. Moreover, converting observable emission into disk masses requires significant assumptions about dust opacity, gas-to-dust ratio, chemical abundances, temperature, and optical depth that are not well constrained for most disks (see the Chapter by [Miotello et al.](#) for more details).

The continuum emission is the most efficiently observed tracer but requires the most fundamental assumptions: that the flux scales with the dust mass assuming optically thin emission and with a conversion that depends on temperature and dust opacity, and then that this dust mass converts to the total disk mass through an interstellar medium measure of the gas-to-dust ratio. Moreover, this approach assumes the bulk of the solid mass of the disk is still in mm-sized grains and would provide a lower limit if planet formation and/or inward drift operate on timescales of a few Myr. Under these assumptions and caveats, which we quantify in § 2.5, two clear trends emerge from mm disk surveys: higher mass stars tend to host more massive dust disks, and disk dust masses decline rapidly with age on timescales of a few Myr (e.g., [Ansdell et al. 2016, 2017](#); [Pascucci et al. 2016](#); [Barenfeld et al. 2016](#), see § 4.1).

The most readily observed mm gas lines are rotational

transitions of CO and its isotopologues. However, these lines are relatively weak, probably due to CO depletion rather than an overall decline of gas content ([Bergin and Williams 2017](#)), and thus do not appear to be a good measure of the total disk gas mass ([Williams and Best 2014](#); [Miotello et al. 2016, 2017](#); [Long et al. 2017](#)). ALMA surveys have therefore concentrated more on the continuum rather than spectral lines to date, and a full understanding of CO depletion, disk chemistry, and gas masses awaits the results from new, deeper surveys focused on the lines, such as MAPS ([Öberg et al. 2021](#)), but for much larger samples of objects, including low-mass compact disks.

Disk dust sizes are measured either by fitting resolved data in the visibility plane (e.g., [Tazzari et al. 2017](#); [Tripathi et al. 2017](#); [Andrews et al. 2018a](#); [Hendler et al. 2020](#)) or image plane (e.g., [Ansdell et al. 2018](#); [Barenfeld et al. 2017](#)). Although the extent of the disk dust emission is commonly assumed to trace the disk radius (e.g., [Trapman et al. 2019](#)), we will present key caveats in § 4.1 (e.g., [Rosotti et al. 2019a](#)). Gas disk sizes have been measured in different regions ([Barenfeld et al. 2017](#); [Andrews et al. 2018a](#); [Sanchis et al. 2021](#)). Ideally, an optically thin tracer would be best suited for this task since we would like to identify where the disk mass is. Unfortunately, due to observational constraints, most existing measurements of disk radii are for the optically thick ^{12}CO . Based on this tracer, gas disk sizes have generally been found to be several times larger than the dust (e.g., [de Gregorio-Monsalvo et al. 2013](#); [Ansdell et al. 2018](#); [Sanchis et al. 2021](#)), suggesting radial drift of mm-sized particles, though a full interpretation requires careful accounting of radiative transfer and sensitivity effects (e.g., [Rosotti et al. 2019a](#)) and is discussed further in § 4.1.

2.3. Observations of final stages of protoplanetary disk evolution and debris disks

In this section we will review observational constraints on protoplanetary disk dissipation and the debris disk phase, with an emphasis on recent results from the far-IR and millimeter-wavelength regime. For a thorough review of debris disk structure, composition, and evolution, we refer the reader to more comprehensive review articles like [Wyatt \(2008\)](#); [Krivov \(2010\)](#); [Matthews et al. \(2014\)](#); [Hughes et al. \(2018\)](#). Debris disks are the more-evolved cousins of protoplanetary disks, in which the dust that we observe is optically thin at all wavelengths and generated primarily through destructive processes (e.g., in a collisional cascade). The gas mass also tends to be much lower than in the protoplanetary disk stage, and mounting evidence suggests that its composition is dominated by Carbon and Oxygen rather than H_2 as in the protoplanetary stage (see § 2.3.3).

2.3.1. Observations of the final stages of protoplanetary disks and the debris disk phase

Observations of the transition from the protoplanetary to debris disk stage in the infrared and submillimeter have

suggested that the transition occurs rapidly and in several distinct stages (e.g., [Wyatt et al. 2015](#); [Hardy et al. 2015](#)), although with the caveat that these surveys relied on pre-ALMA data and were therefore strongly biased toward the brightest protoplanetary disks and did not account for the now-established correlation between stellar spectral type and disk mass. In particular, the fractional excess luminosity in the infrared exhibits a gap with very few objects falling near a value of 10^{-2} , leading [Hughes et al. \(2018\)](#) to propose that the delineation between protoplanetary and debris disks should fall at a value of approximately 8×10^{-3} , with HD 141569 as the most likely truly “transitional” system so far observed (see also recent work by [Miley et al. 2018](#); [Di Folco et al. 2020](#)). In recent years, surveys with far-IR and millimeter instruments like *Herschel*, JCMT, ALMA, and *WISE* have revealed how debris disk mass changes with age across a range of stellar temperatures ([Moór et al. 2016](#); [Holland et al. 2017](#); [Pawellek et al. 2021](#)). Recent work by [Michel et al. \(2021\)](#) has proposed a separate evolutionary pathway for debris disks: a radial-drift dominated mode leading to rapid dust dissipation in featureless disks (which then do not become observable debris disks), and a slower evolution of structured disks, suggesting that most observed cold debris disks inherit some amount of structure from their protoplanetary predecessors. This proposal is supported by recent theoretical modeling work ([Najita et al. 2022](#)) and studies of large samples of exoplanet properties and ALMA disk observations ([van der Marel and Mulders 2021](#)). Recent multiwavelength and time-domain observations have also codified the existence of so-called “Extreme debris disks” (EDDs), which are characterized by unusually high excess luminosity and time variability in the near- to mid-IR even at relatively late (> 100 Myr) ages (e.g., [Balog et al. 2009](#); [Meng et al. 2014, 2015](#); [Su et al. 2019](#); [Moór et al. 2021](#); [Melis et al. 2021](#)). While these systems have infrared excess luminosities higher than the 8×10^{-3} level typical of debris disks, they are classified as debris disks based on the age of the central star and their lack of gas. For comparison, studies of dust excess show that the evolutionary timescale of protoplanetary disks is somewhere in the neighborhood of 10 Myr; see Section 4.1.2 below for more detail.

Another way of learning about debris disk evolution is to observe Class III disks within young clusters, and to determine whether or not they share properties of older debris disks. Recent work has suggested that many of the Class III members of nearby young clusters are more like debris disks than protoplanetary disks in their dust properties, which is surprising given the cluster ages of < 5 Myr and suggests that at least some systems might undergo rapid dispersal of primordial gas and dust with an early transition to the debris disk phase ([Espanlat et al. 2017](#); [Lovell et al. 2021b,a](#)). This conclusion is strengthened by the survey of Ophiuchus protostars across evolutionary stages (ODISEA, [Cieza et al. 2019](#)), which shows that, while dust mass does decrease with protostellar evolutionary stage, disk dust masses do not decrease monotonically with age

([Williams et al. 2019](#)), in line with other surveys ([Cazzoletti et al. 2019](#)). However, with the advent of *Gaia*, more rigorous membership determination has called the ages of some of these sources into question and demonstrated for example that many of the Class III sources previously identified with Lupus might actually be part of the older surrounding Sco-Cen region, for example Upper Centaurus Lupus with an age of 16 Myr ([Pecaut et al. 2012](#); [Luhman 2020a](#); [Michel et al. 2021](#)).

While debris disks are usually observed around A and B dwarfs, the lower-mass counterparts are less studied, making comparison with protoplanetary disk populations more uncertain (e.g., [Michel et al. 2021](#)). Debris disks around M dwarfs are difficult to observe due to the relatively low masses and temperatures in these systems ([Luppe et al. 2020](#)). Only a handful of M dwarf debris disks have been directly imaged, but recent imaging advances with SPHERE and ALMA observations have added some new examples in the TW Hya association ([Choquet et al. 2016](#)), in the Fomalhaut system ([Cronin-Coltsmann et al. 2021](#)), and notably around a nearby M dwarf without previously known infrared excess ([Sissa et al. 2018](#); [Adam et al. 2021](#)). From the perspective of disk dissipation, M dwarf debris disks are notable for the discovery of a new and surprising class of $\gtrsim 20$ Myr-old debris disks with measurable accretion rates onto the central star, which suggests that some M dwarf debris disks may dissipate more slowly than disks around higher-mass stars. The prototypical example is WISE J080822.18-644357.3, which was first shown to have an anomalously large infrared excess ([Silverberg et al. 2016](#)), followed by an accretion signature ([Murphy et al. 2018](#)), but without ALMA-detectable quantities of cold CO gas in the outer disk ([Flaherty et al. 2019](#)). Since then, four additional disks sharing similar features have been discovered ([Silverberg et al. 2020](#)), and modeling work has shown that these disks must meet specific conditions to be detectable, namely (1) high disk masses, (2) extremely low external photoevaporation rates, and (3) moderately low ($\alpha \sim 10^{-4}$) viscosity parameters, with assumed corresponding low accretion rates ([Coleman and Haworth 2020](#)). Further modelling work has shown how these disks survive around M dwarf stars ([Wilhelm and Portegies Zwart 2022](#)).

Along some other dimensions of debris disk demographics, recent work has revealed that multiplicity is an important factor in studying the fraction of debris disks and its evolution as a function of age. The debris disk fraction drops for binaries with separation of order a few tens of au ([Yelverton et al. 2019](#)), and when the role of multiplicity is taken into account in a comparison between known radial velocity exoplanet hosts and matched controls, there is no significant difference in the disk fractional luminosity distribution ([Yelverton et al. 2020](#)). Finally, some progress has been made in the study of the long-wavelength spectral index of debris disks and its interpretation, with substantial samples of debris disks detected out to $\sim$ cm wavelengths ([MacGregor et al. 2016](#); [Marshall et al. 2017](#); [Norfolk et al. 2021](#)). A detailed review of the interpretation

of such measurements by [Löhne \(2020\)](#) concludes that numerical fits to observed systems result in steeper size distributions on average than previously derived, placing more emphasis on size-dependent material strengths and impact velocity rather than drag forces.

2.3.2. Structure in debris disks

While this chapter’s focus is on global disk properties, here we briefly review some highlights related to debris disk (sub)structure – radial, vertical, and azimuthal – over the past few years. Direct comparisons are difficult because of differences in the observational constraints on protoplanetary vs. debris disks. Protoplanetary disks are found in young stellar associations, and the nearest disks tend to cluster at distances of order 100–200 pc, whereas debris disks are more likely to be found around isolated main sequence stars that are on average much closer to the Sun. Debris disks are also orders of magnitude fainter than protoplanetary disks on average, and the combination of large angular size and low surface brightness can be quite challenging, especially for interferometers. Imaging the closest targets is difficult because their angular sizes tend to be larger than the primary beam and therefore require mosaicking, and for smooth, broad intensity profiles, the maximum recoverable scale can make the disk unobservable on the scale of the short baselines of the main ALMA array. High-resolution observations of debris disks have therefore tended to focus on the brightest debris disks (which also biases the sample towards earlier spectral types; [Sibthorpe et al. 2018](#)), as well as those located at intermediate (not too close, not too far) distances, generally a few tens of pc from the Sun.

The first large *Herschel* studies of debris disk radial structure at scales of tens to hundreds of au demonstrated a relationship between stellar luminosity and grain size ([Pawellek et al. 2014](#); [Pawellek and Krivov 2015](#)). As resolved millimeter-wavelength observations of samples of debris disks shifted firmly to the scale of tens of au with ALMA and the SMA, evidence emerged of a relationship between planetesimal belt radius and stellar luminosity, which can only be extracted with careful attention to observational bias ([Matrà et al. 2018a](#); [Esposito et al. 2020](#); [Marshall et al. 2021](#)), although the inclusion of new debris disks with lower stellar luminosities tends to decrease the significance of the correlation ([Adam et al. 2021](#)). The REASONS survey, which is in progress at the time of writing, promises to provide the largest sample to date of resolved planetesimal belt structure at scales of tens of au ([Sepulveda et al. 2019](#)).

At smaller scales, down to $\sim$ au, ALMA imaging of large dust grains has now revealed radial substructure in a handful of disks – essentially all of the broad ($\Delta R/R \gtrsim 1$) disks that have been imaged with sufficient resolution and sensitivity to detect substructure. There are gaps detected in HD 107146 ([Ricci et al. 2015](#); [Marino et al. 2018](#)), HD 15115 ([MacGregor et al. 2019](#)), HD 92945 ([Marino et al.](#)

[2019](#)), HD 206893 ([Marino et al. 2020a](#); [Nederlander et al. 2021](#)), and tentatively in the AU Mic disk ([Daley et al. 2019](#)). There is also evidence for local dust maxima in two disks with broad radial profiles: 49 Ceti ([Hughes et al. 2017](#)) and HR 8799 ([Faramaz et al. 2021](#)). While some systems with radial substructure in millimeter-wavelength thermal emission appear smooth in scattered light, HIP 73145 is a recent example of a debris disk that has gaps in scattered light ([Feldt et al. 2017](#)). The interpretation of the presence of gaps in debris disks of course centers around the possibility of planets. High-contrast imagers are just beginning to penetrate the parameter space of planets consistent with the width and depth of the observed gaps (e.g., [Lombart et al. 2020](#); [Mesa et al. 2021](#)). However, considerations like potential resonance chains, secular interactions, and even debris disk self-gravity complicate the picture ([Pearce and Wyatt 2015](#); [Dong et al. 2020](#); [Sefilian et al. 2021](#)). The capabilities of *JWST* should prove particularly exciting in this area.

Another exciting development in high-resolution imaging of thermal emission is the ability to study the vertical structure of the large grains in debris disks, which was not previously possible due to limitations in sensitivity. While vertical structure has been previously studied in scattered light, the longer-wavelength thermal emission probes larger grains that are less susceptible to effects like radiation pressure and stellar winds than smaller grains, which makes it an excellent probe of the dynamical state of the system. Observations of the β Pictoris disk by [Matrà et al. \(2019a\)](#) have revealed that the vertical structure is best fit by a double Gaussian or Lorentzian, indicating two dynamical populations similar to the Kuiper belt’s cold classical belt and scattered belt components. Unusually flat structure in the AU Mic disk points to a dearth of Uranus and Neptune analogs in the system, despite the presence of radial velocity planets at smaller (sub-au) separations ([Daley et al. 2019](#)).

Non-axisymmetric structure is also present in many debris disks. Swept-back “wings” in edge-on systems have been variously attributed to interactions with the ISM or eccentric planets, but the presence of millimeter emission in the haloes favors a dynamical explanation (like an eccentric planet) over gas drag that should act more strongly on smaller grains ([MacGregor et al. 2018](#)). The phenomenon of “apocenter glow” at millimeter wavelengths, due to the pileup of material that orbits more slowly at apocenter than at pericenter, has been definitively observed and is now being used as a tool to probe dust grain properties and the orbital properties of putative planets sculpting debris disks ([Pan et al. 2016](#); [MacGregor et al. 2017](#); [Regály et al. 2018](#); [Kim et al. 2018](#); [Faramaz et al. 2019](#)).

2.3.3. Gas in debris disks

One rapid-moving area in debris disk studies during the ALMA era has been the characterization of their molecular gas content. While previously it was generally assumed that molecular gas would dissipate on timescales comparable to

that of the protoplanetary disk dust, we now know that it is common for debris disks to host detectable quantities of CO gas, although many questions remain about the composition and origin of the gas. For a thorough review of the subject please see [Hughes et al. \(2018\)](#); here we will provide a brief update on recent progress.

Studies of the demographics of gas-bearing debris disks have shown that gas is most commonly observed around young (~ 10 Myr-old) A and B stars; however, it has also been observed around both low-mass and older stars (e.g., [Lieman-Sifry et al. 2016](#); [Moór et al. 2017](#); [Matrà et al. 2017, 2019b](#)). Studies of the composition of the gas at late stages have shown abundant [CI], which is a photodissociation product of CO, including a $[^{13}\text{CI}]$ detection that indicates that it is optically thick ([Higuchi et al. 2017](#); [Cataldi et al. 2018](#); [Higuchi et al. 2019b,a](#)). Searches for molecules other than CO have yielded low upper limits, to such an extent that the abundance of CO relative to other molecules is anomalously high compared with protoplanetary disks, comets, or models of second-generation gas production and supports theoretical models of shielding of CO gas by neutral carbon ([Kral et al. 2016, 2017, 2019](#); [Matrà et al. 2018b](#); [Cavallius et al. 2019](#); [Moór et al. 2019](#); [Klusmeyer et al. 2021](#)). One interesting metric that is likely to be explored in the near future is the degree of viscous spreading of the gas ([Cataldi et al. 2020](#); [Marino et al. 2020b](#)). Debris disk gas is predicted to be more highly ionized than gas in protoplanetary disks, making it more likely that magnetohydrodynamic angular momentum transport processes are efficient ([Kral and Latter 2016](#)). On the whole, gas observations so far are consistent with the detection of vaporized second-generation gas from icy grains/comets/planetesimals, with some systems exhibiting larger amounts of CO that require shielding from CI to sustain. Some systems are clearly of second-generation origin, while some ambiguity remains about the origin of the CO in systems with relatively large gas masses.

2.4. Biases and limitations of survey properties and strategies

The surveys carried out in the past years with spectroscopy and millimeter interferometry have revealed the bulk properties of unprecedentedly large samples of disks and their host stars. However, these surveys are still affected by some biases and limitations, as described in this section.

2.4.1. Completeness of the samples

The surveys reviewed here are of star-disk samples usually defined from mid-infrared *Spitzer* observations (e.g., [Evans et al. 2009](#); [Dunham et al. 2014, 2015](#)). The *Spitzer* sensitivity was sufficient to identify infrared excesses above low-mass stellar photosphere levels for targets out to ~ 1 kpc, and thus was able to reveal all the disks in nearby star-forming regions *within the areas that were mapped*. The *Spitzer* maps generally encompassed most of the pre-

main sequence stars known in each region at the time, but *Gaia*'s exquisite 3D vision ([Gaia Collaboration et al. 2016](#)) has revealed additional members in many cases (e.g., [Manara et al. 2018](#); [Beccari et al. 2018](#); [Herczeg et al. 2019](#); [Venuti et al. 2019a](#); [Galli et al. 2020, 2021](#); [Luhman 2020b](#); [Luhman and Esplin 2020](#); [Esplin and Luhman 2020, 2022](#)). Since most of the disk-bearing stars are co-located with the molecular clouds in the regions targeted with *Spitzer*, especially in the younger ($\lesssim 3$ Myr) and denser regions, the follow-up stellar spectroscopy and ALMA disk imaging surveys are indeed incomplete, but the degree of completeness on the disk population ($\gtrsim 80 - 90\%$) is sufficient that the statistical properties are robust. Nevertheless, some of the *Gaia*-discovered members that are more isolated from the rest of the star-forming region may have a different history or environmental dependence that should be investigated in the future, with accurate membership vetting and spectroscopic and mm-interferometry followup. The sample incompleteness is particularly relevant for the older Upper Scorpius region. The newly discovered disk-bearing members of this region ([Luhman 2020a](#)) are currently being observed with ALMA.

The spectroscopic surveys are typically sufficiently sensitive to study stars down to late-M spectral types in nearby star-forming regions $\lesssim 300$ pc away, and at these distances the dust mass detection limit of ALMA disk surveys is typically a few tenths of an Earth mass. This is sufficient for drawing inferences about planet formation, but is about an order of magnitude greater than the dust masses of debris disks. This means that there is a significant gap in our knowledge of the late stages of disk dispersal, as testified by contradictory results in recent work ([Lovell et al. 2021a](#); [Michel et al. 2021](#)).

2.4.2. Limited spatial resolution

It is now known that many disks observed at spatial resolutions on the order of $\lesssim 10$ au show substructures, i.e., cavities, rings, spirals, and vortices (see review by [Andrews 2020](#)). The ALMA disk surveys reviewed here were often the first deep reconnaissance of the star-forming region at mm wavelengths and were therefore designed to measure total masses independent of surface brightness, rather than to produce detailed images, and thus used relatively modest resolutions of at least a few tens of au; it was also not known at the time of the surveys that many disks exhibit substructures when observed at sufficiently high resolution. Consequently, many disks are unresolved and size distributions are much more incomplete than mass distributions; in general, the ALMA disk surveys to date have $\sim 30\%$ of the disks resolved (thus have size measurements) and $\sim 80\%$ of the disks detected (thus have mass measurements).

Nevertheless, these surveys provided some information on large disk structures and in particular unbiased samples of transition disks with large central cavities ([van der Marel et al. 2018](#)) that are directly imaged rather than (often incompletely and sometimes erroneously) inferred through

TABLE 1

Region	Name	RA ICRS	DEC ICRS	Dist [pc]	$M_{\star}$ [$M_{\odot}$]	$\log \dot{M}_{\text{acc}}$ [$M_{\odot}/\text{yr}$]	M_{disk} [$M_{\oplus}$]	R_{disk} [au]
Lupus	Sz65	15:39:27.780	-34:46:17.400	153.5	0.61	-9.48	21.19	21.5
ÜSco	J15514032-2146103	15:51:40.320	-21:46:10.300	140.8	0.143	-10.15	0.15	87.3
ChamI	J10555973-7724399	10:55:59.730	-77:24:39.900	183.5	0.79	-8.42	11.89	20.2
...								

Notes. Example of the table with the data collected as described in § 2.5. M_{disk} and R_{disk} are the dust mass and size of disks, respectively. Full table available at <http://ppvii.org/chapter/15/>.

SEDs. The resolution was also sufficient to extend earlier studies on the strong effect of stellar multiplicity on disk lifetime and masses (e.g., [Harris et al. 2012](#)) to sizes and radial profiles (e.g., [Akeson et al. 2019](#); [Manara et al. 2019b](#); [Zurlo et al. 2020, 2021](#); [Zagaria et al. 2021](#)).

A notable, and unfortunate, exception is Taurus. As a northern target, it was the best-surveyed region in the mm pre-ALMA ([Beckwith et al. 1990](#); [Andrews and Williams 2005](#)). Although many ALMA programs observed subsamples of the disk population, Taurus lacks the same uniform, complete survey now available for all the other nearby star-forming regions. It is hoped that this oversight will be rectified by PPVIII. For now, our analysis here relies on relatively low-resolution, low-sensitivity SMA data ([Andrews et al. 2013](#)) augmented with a small fraction imaged by ALMA (e.g., [Long et al. 2019](#); [Akeson et al. 2019](#)). This incompleteness of the Taurus sample similarly affects the stellar and accretion properties of the stellar population in this region. Whereas multiple studies with different low-resolution spectroscopic instruments were carried out in the past, homogeneous studies of the stellar populations are only available from [Herczeg and Hillenbrand \(2014\)](#), who only derived the stellar properties, and are being carried out by [Alcalá et al. \(2021\)](#) also for the accretion properties.

2.5. Collected sample

In this review, we use publicly available stellar and disk properties to compare observations with models of disk evolution. The regions selected for this review are all within 300 pc, as these surveys have higher completeness in both sample size and sensitivity to low-mass objects. These regions include: Lupus, Taurus, Ophiuchus, Chamaeleon I, Chamaeleon II, Corona Australis, and Upper Scorpius. Table 1 shows the collected information and is available to the community in its integrity online². For all targets, we assume the individual distances inverting the parallaxes from Gaia EDR3 ([Gaia Collaboration et al. 2021](#)), unless the values were unreliable – RUWE > 1.8 and/or distance differing more than 60 pc from the median distance to the region – or not available, in which case we assumed the median distance to the members of the region.

The stellar and accretion parameters used here are mainly obtained from surveys carried out with the VLT/X-Shooter instrument, since these values are reliable and coherent. In particular, data for the Lupus region are from [Alcalá et al. \(2014, 2017\)](#), for Chamaeleon I from [Manara et al. \(2016, 2017b\)](#), for Upper Scorpius from [Manara et al. \(2020\)](#). For the remaining regions, we collected data from [Testi et al. \(2022\)](#) for Ophiuchus and Corona Australis, from [Villenave et al. \(2021\)](#) for Chamaeleon II, and from [Herczeg and Hillenbrand \(2014\)](#) when possible, for Taurus, with some information from other works (e.g., [Ingleby et al. 2013](#); [Manara et al. 2014](#); [Alcalá et al. 2021](#); [Testi et al. 2022](#)). We rescale all luminosities ($L_{\star}$, L_{acc}) to the new distances and convert T_{eff} from SpT using the conversion by [Herczeg and Hillenbrand \(2014\)](#). This is a difference with respect to all the VLT/X-Shooter surveys. To derive $M_{\star}$, and thus $\dot{M}_{\text{acc}}$, we use the non-magnetic models of [Baraffe et al. \(2015\)](#) for targets with $T_{\text{eff}} \leq 3900$ K (M-type) and of [Feiden \(2016\)](#) for hotter stars, in line with [Pascucci et al. \(2016\)](#), among others. In a tiny fraction of cases, the models by [Siess et al. \(2000\)](#) were used for targets having stellar properties outside of the range of validity of the other models. Determining typical ages for the regions considered here is complicated also for the aforementioned uncertainties and possible age spreads in individual regions. According to the latest Gaia-based studies, typical ages for the on-cloud populations are as follows: Ophiuchus ~1-2 Myr ([Esplin and Luhman 2020](#)), Corona Australis ~1-2 Myr ([Esplin and Luhman 2022](#)), Taurus ~1-3 Myr ([Krolikowski et al. 2021](#)), Lupus $\lesssim 3$ Myr ([Luhman 2020b](#)), Chamaeleon ~1-2 Myr ([Galli et al. 2021](#)), Upper Scorpius ~ 5 – 10 Myr ([Pecaut and Mamajek 2016](#); [Luhman and Esplin 2020](#)). These estimates are affected by several uncertainties ([Soderblom et al. 2014](#)) and are typically correct only in relative terms. However, a homogeneous reassessment of the ages of these regions with Gaia information is still lacking. We therefore only use these ages for illustrative purposes in the plots.

The dust dust properties are inferred from the published ALMA Band 6 or 7 continuum data for Lupus ([Ansdell et al. 2016, 2018](#); [Sanchis et al. 2020](#)), Chamaeleon I ([Pascucci et al. 2016](#); [Long et al. 2018](#)), Upper Scorpius ([Barenfeld et al. 2016](#); [van der Plas et al. 2016](#); [Carpenter](#)

²Table 1 is available publicly at <http://ppvii.org/chapter/15/>

et al. 2014), Chamaeleon II (Villenave *et al.* 2021), Ophiuchus (Cieza *et al.* 2019; Williams *et al.* 2019), and Corona Australis (Cazzoletti *et al.* 2019). For Taurus, we used ALMA measurements from Akesson and Jensen (2014), Ward-Duong *et al.* (2018a), Akesson *et al.* (2019), and Long *et al.* (2019) and completed them with the pre-ALMA data from Andrews *et al.* (2013). When available, we use the measured flux in Band 6, as the disks are more optically thin at longer wavelengths. These fluxes are then converted to dust masses following Ansdell *et al.* (2016), using a prescription for the opacity, $\kappa_\nu = 2.3(\nu/230 \text{ GHz}) \text{ cm}^2/\text{g}$, which originates from the classic Beckwith *et al.* (1990) paper. We use a single dust temperature, $T_{\text{dust}} = 20 \text{ K}$, which has been empirically demonstrated to be a good disk-average value (Tazzari *et al.* 2021b). The total disk mass is then obtained from the dust mass via the substantial extrapolation of multiplying by a gas-to-dust ratio of 100.

We note that, for a disk at inclination i , the average dust opacity, $\tau_\nu = \kappa_\nu \Sigma_{\text{dust}} / \cos i$, exceeds unity at $\lambda = 1.3 \text{ mm}$ for a typical value $\Sigma_{\text{dust}} \gtrsim 0.2 \text{ g cm}^{-2}$ which corresponds to an Earth mass of dust uniformly spread over a circular area with radius 6.5 au. Consequently, the continuum emission is generally optically thin in most resolved disks. Exceptions are dense central regions or highly concentrated substructures (both of which may contain significant hidden mass).

Finally, disk dust sizes are taken from Hendler *et al.* (2020), who fit all the available data in the uv-plane with a Nuker profile. Here we report the radius containing 68% of the disk dust emission.

In total, we have compiled information for 845 targets, with measures of disk masses for 831, stellar masses for 494, and accretion rates for 289.

3. MODELS OF GLOBAL DISK EVOLUTION

The evolution of protoplanetary disks is regulated by several physical processes (§ 3.1). Here we present in § 3.2 the analytical global models available to-date to describe the effects of these processes, and how these develop and connect to the formation of inner disk cavities (§ 3.3).

3.1. Physical processes

Secular disk evolution results from the combined action of internal stresses ($T_{r\phi}$), surface stresses ($T_{z\phi}$), and mass infall or loss (see Fig. 2). Self-gravity (Kratter and Lodato 2016) and infall (Lesur *et al.* 2015) are important at early times, while the key determinant of subsequent evolution is the disk’s *net vertical* magnetic field. The field strength can be parameterized via the ratio of the thermal to magnetic pressure,

$$\beta(r, t) = \frac{\rho_0 c_{s0}^2}{B_{z0}^2 / 8\pi}, \quad (1)$$

where ρ_0 and c_{s0} are the mid-plane density and sound speed, and B_{z0} is the vertical magnetic field. In the limit as $\beta \rightarrow \infty$, disks would evolve due to relatively weak turbulent stresses

from the Vertical Shear Instability (Nelson *et al.* 2013; Flock *et al.* 2020), other hydrodynamic processes (Lyra and Umurhan 2019), and photoevaporative mass loss (Alexander *et al.* 2014; Ercolano and Pascucci 2017). Weak but non-zero net fields, with $\beta \sim 10^3 - 10^5$, stimulate levels of turbulent and laminar MHD transport that can exceed that in non-magnetized disks (Simon *et al.* 2013; Béthune *et al.* 2017; Lesur 2020). They are accompanied by mass and angular momentum loss through MHD winds (Bai and Stone 2013). Lower values of β are plausible outcomes of the star formation process (Xu and Kunz 2021), and simplified calculations suggest that they represent equilibrium configurations for net magnetic fields in protoplanetary disks (Guilet and Ogilvie 2014a). More strongly magnetized disks may also form, and would be expected to have shorter lifetimes due to magnetic braking. This theoretical understanding motivates two questions. First, is disk evolution predominantly due to turbulent transport or due to MHD winds? Second, is turbulence – which must be present at some level even if it is not the main driver of disk evolution – predominantly sourced by hydrodynamic or MHD processes? Observations of disk winds (see chapter by Pascucci *et al.*), and direct measurements (or lack thereof) of disk turbulence in a small number of systems (e.g., Pinte *et al.* 2016; Flaherty *et al.* 2017; Teague *et al.* 2018; Flaherty *et al.* 2020, see also the chapters by Lesur *et al.* and Pinte *et al.*), provide important constraints on these questions. We note that the answers may not be as simple as yes / no, for example disks that form with relatively strong net fields may evolve due to MHD winds, while disks with weaker fields evolve due to turbulence. There could also be variations with radial distance and time.

Hydrodynamic and MHD transport processes can now be simulated, over short time scales, using physical parameters (such as the strength of ambipolar diffusion) that match those expected in disks. Linking simulation snapshots together into a long term evolutionary model requires additional, challenging, steps. At a fundamental level, all MHD transport processes depend on $\beta(r, t)$. One-dimensional effective theories (analogous to the evolution equation for $\Sigma(r, t)$ for β exist (Lubow *et al.* 1994; Guilet and Ogilvie 2014b; Leung and Ogilvie 2019), but require further validation against simulations. Less fundamentally, but at least as importantly, no commonly available tracer directly yields the gas surface density. Observational comparisons require dust evolution (Birnstiel *et al.* 2012; Rosotti *et al.* 2019b) or chemical models (Miotello *et al.* 2014; Woitke *et al.* 2016) as an intermediate step, and these models introduce substantial additional uncertainties.

Finally, external processes impact the evolution of disks through disk truncation in multiple systems and fly-bys and/or external photoevaporation from massive stars (e.g., Winter *et al.* 2018; Parker *et al.* 2021). These processes are not discussed in this review. We note however that external photoevaporation is not a significant effect in the star-forming regions considered here (see § 2.5).

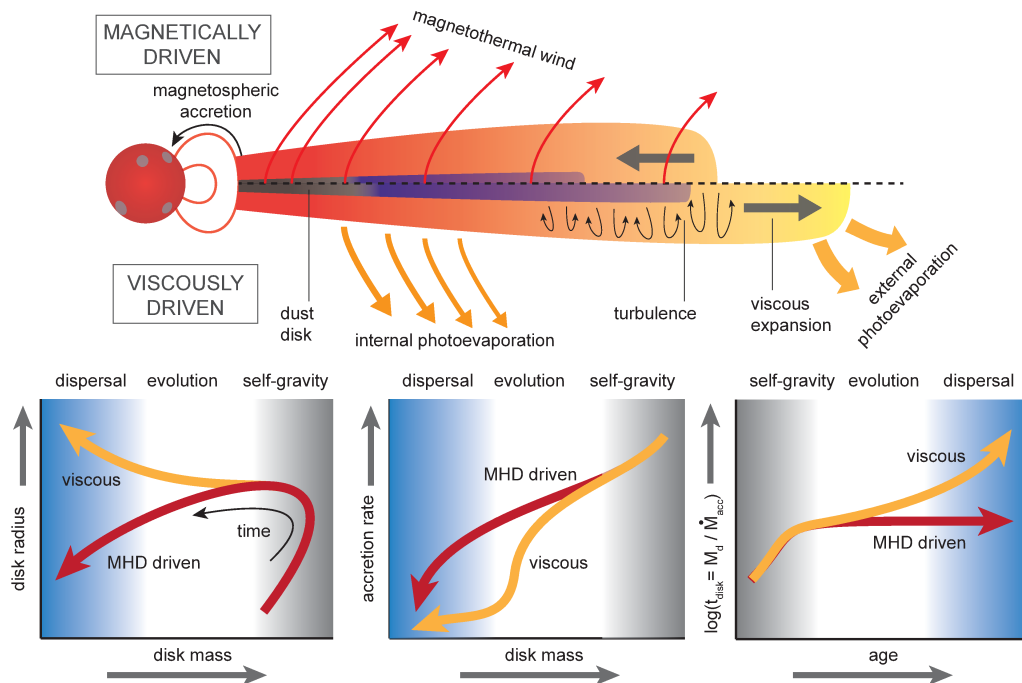


Fig. 2.— Schematic illustration of disk evolution under the two end-member evolutionary models: a viscous model in which accretion is driven by internal turbulent redistribution of angular momentum, with dispersal effected by photoevaporation, and a magnetically driven model where accretion occurs due to loss of angular momentum in an MHD wind. In either model, the dust disk evolves under the additional influence of aerodynamic effects. The lower panels show possible differences in observational diagnostics, including an earlier self-gravitating phase that we do not focus on in the text. Potentially observable population-level differences occur because the ratio of angular momentum to mass removed by MHD winds exceeds photoevaporative winds, affecting the mass-weighted radius evolution. Internal photoevaporation leads to the formation of an inner cavity, and low stellar accretion rates, immediately prior to dispersal.

3.2. Analytic and semi-analytic models

Here we focus on the predictions for how the global disk properties (disk gas mass, radius, accretion rate) should evolve in time in the context of the analytical predictions of the two main global scenarios, viscous evolution and MHD driven evolution.

3.2.1. Viscous models

Historically, the ‘standard’ models of protoplanetary disk evolution are based on classical accretion disk theory, where the main driver of angular momentum transport is some form of ‘anomalous’ viscosity, generally associated with turbulence, that may be generated either by MHD instabilities, such as the MRI (Balbus and Hawley 1991), or by hydrodynamical instabilities, such as the vertical-shear instability (Nelson et al. 2013), or - under certain circumstances - the gravitational instability (Lodato and Rice 2004; Rice et al. 2005). Traditionally, global evolutionary disk models have relied on the Shakura and Sunyaev (1973) α -prescription for viscosity, according to which the kinematic viscosity $\nu = \alpha c_s H$, where $\alpha \sim (\delta v / c_s)^2$ is a dimensionless parameter that scales with the square of the turbulent velocity in units of the sound speed. The simplest

form of the evolution equation for a Keplerian, viscous disk is:

$$\frac{\partial \Sigma}{\partial t} = \frac{3}{R} \frac{\partial}{\partial R} \left(R^{1/2} \frac{\partial}{\partial R} (\nu \Sigma R^{1/2}) \right), \quad (2)$$

to which several additional effects can be added, such as photoevaporation (either internal or external) (Clarke et al. 2001), tidal torques from a planet (Lin and Papaloizou 1986; Syer and Clarke 1995; Lodato and Clarke 2004), tidal truncation from a binary companion (Rosotti and Clarke 2018), or even dust evolution and radial drift (e.g., Laibe and Price 2014; Birnstiel et al. 2010; Booth et al. 2017).

In protoplanetary disk studies, one specific solution to the above equation has had a significant success, to the point of being used as a standard reference even outside of the immediate scope of describing viscously evolving disks. This is the so-called ‘self-similar’ solution by Lynden-Bell and Pringle (1974), that describes the evolution of an initially power-law disk, exponentially truncated at a radius R_c , and with viscosity proportional to R^γ :

$$\Sigma(R, t) = \frac{M_0}{2\pi R_c^2} (2-\gamma) \left(\frac{R}{R_c} \right)^{-\gamma} T^{-\eta} \exp \left(-\frac{(R/R_c)^{(2-\gamma)}}{T} \right), \quad (3)$$

where M_0 is the initial disk mass, $\eta = (5/2 - \gamma)/(2 - \gamma)$, $T = 1 + t/t_v$, and the viscous time $t_v = R_c^2/3(2 - \gamma)\nu(R_c)$. Very often, this solution is considered for the special case where $\gamma = 1$ (e.g. [Hartmann et al. 1998](#)), in which case $\eta = 3/2$ and $2 - \gamma = 1$. In this case, we can simply evaluate t_v as a function of the main disk parameters:

$$t_v \approx 0.87 \text{ Myrs} \left(\frac{\alpha}{10^{-3}} \right)^{-1} \left(\frac{H/R}{0.1} \right)^{-2}_{R=R_c} \left(\frac{1M_\odot}{M_\star} \right)^{1/2} \left(\frac{R_c}{30 \text{ au}} \right)^{3/2}, \quad (4)$$

from which we see that, in order for the viscous time to be a few Myrs, α should be in the range $10^{-4} - 10^{-3}$.

Global properties associated with the self-similar solution are the evolution of disk mass and accretion rate, that both turn out to be power-laws with time:

$$M_d(t) = M_0 T^{1-\eta}, \quad (5)$$

$$\dot{M}(t) = (\eta - 1) \frac{M_0}{t_v} T^{-\eta}, \quad (6)$$

and one can define a typical evolutionary time-scale

$$t_{\text{disk}} = \frac{M_d(t)}{\dot{M}(t)} = 2(2 - \gamma)(t + t_v). \quad (7)$$

We can therefore easily see that, for such solutions, the ‘disk lifetime’ t_{disk} is proportional to the age of the system t for $t \gg t_v$ and to the viscous time t_v for $t \ll t_v$ (see lower right panel of [Figure 2](#)).

Notable properties of this solution are: (i) for $t \gg t_v$ the relation between disk mass and accretion rate is linear, and does not depend on initial conditions or even viscosity; (ii) it is possible to derive analytical expressions for the ‘isochrones’, i.e., loci of points in the $\dot{M} - M_d$ plane for a population of disks of the same age (see [Fig. 3](#), [Lodato et al. 2017](#)). Two examples for different initial disk masses are shown as the blue lines in [Figure 3](#); (iii) the exponential cut-off radius grows with time (see lower left panel of [Figure 2](#)). This last property is often considered to be one of the unique signatures of viscous evolution, although one should note that the observed disk gas radius does not necessarily coincide with the analytical exponential cut-off radius ([Trapman et al. 2020](#)), as we discuss further in § 4.1. For example, if the observed disk radius corresponds to a given threshold in surface density (which might be the case for CO observations), then such radius initially grows (in a phase where probably the disk is less accessible observationally), then its growth slows down and eventually reverses, shrinking to low values for $t \rightarrow \infty$ ([Rosotti et al. 2019a](#); [Trapman et al. 2020](#)).

As mentioned above, the simple viscous evolution equation can be generalized to add several additional physical processes and in a few cases attempts have been done to a populations of disks evolving under such more general circumstances. We show schematically the results of including these effects in [Figure 3](#). Photoevaporation can be easily included once a prescription for the mass-loss rate (either due to UV or X-ray photons) is provided ([Clarke et al. 2001](#);

[Owen et al. 2011](#)). Population studies of photoevaporative viscous disks have been provided by [Rosotti et al. \(2017\)](#), who show that, while for purely viscous disks $t_{\text{disk}} \sim t$ for evolved disks, external photoevaporation leads to $t_{\text{disk}} \gtrsim t$ and internal photoevaporation leads instead to $t_{\text{disk}} \lesssim t$. [Somigliana et al. \(2020\)](#) have further explored the role of internal photoevaporation in a population of evolving disks, confirming the general expectation that $t_{\text{disk}} \lesssim t$, and showing that in this case a steep cut-off in the isochrone in the accretion rate - disk mass plane appears at low disk masses, that effectively “disappear” from the population. Such cut-off occurs at a typical mass $M_c \sim \dot{M}_w t$, where $\dot{M}_w$ is the wind outflow rate. [Sellek et al. \(2020a\)](#) have studied the combined effect of internal photoevaporation and, most importantly, of dust evolution in a population of viscous disks, comparing their results to the observed Lupus and Upper Scorpius data. The main effect of dust evolution is that, because of radial drift, the dust-to-gas ratio is significantly reduced. They show that masses estimated from the sub-mm continuum flux are thus *under-estimates* of the gas mass, effectively moving observational points to the left (see [Figure 3](#)). On top of this, the amount of depletion depends on the initial condition, increasing the scatter in the $\dot{M} - M_d$ plane (whereas pure gas evolution would predict a tight correlation for large ages), potentially explaining the observed scatter in the Upper Scorpius region ([Manara et al. 2020](#)). In principle, planetary torques can also be easily included in viscous evolution (e.g., [Lodato and Clarke 2004](#); [Alibert et al. 2005](#)), but detailed population synthesis models in this case have been more limited. The only study in this respect is the one by [Manara et al. \(2019a\)](#), who report the effect of planet formation and (mainly external) photoevaporation on the disk evolution models used by [Mordasini et al. \(2015\)](#), showing that planet formation leads to a decrease in t_{disk} at high disk masses with respect to a purely viscous disk.

3.2.2. A simple model for MHD driven wind accretion

In the context of MHD wind driven evolution, disk evolution is driven by the *removal* of angular momentum rather than by *transport* as it is the case for viscosity. The wind is launched by the magnetic field which mediates the exchange of angular momentum between the material left in the disk (which spins down) and the wind (which spins up). Locally at a radius R , a wind is characterized by the rate $\dot{\Sigma}_w$ at which it removes mass and by the rate at which it removes angular momentum. To characterize the latter it is common ([Blandford and Payne 1982](#)) to introduce the dimensionless parameter $\lambda = L/(R\Omega(R))$, where L is the specific angular momentum in the wind. The parameter has a straightforward interpretation as the ratio between the angular momentum in the wind and the Keplerian value; to extract angular momentum $\lambda > 1$. Conservation of mass and angular momentum dictates that in this picture the master equation of disk evolution is

$$\frac{\partial \Sigma}{\partial t} = \frac{2}{R} \frac{\partial}{\partial R} [(\lambda - 1) R^2 \dot{\Sigma}_w] - \dot{\Sigma}_w. \quad (8)$$

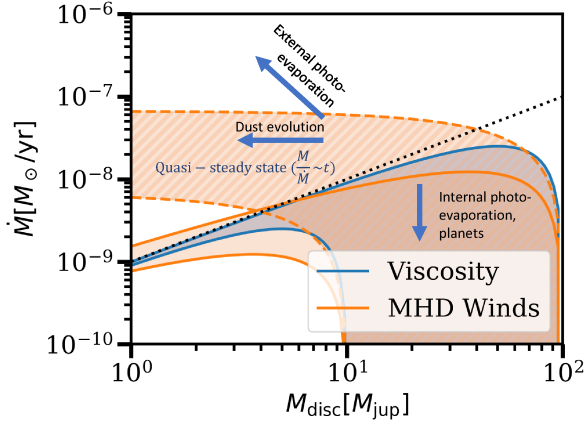


Fig. 3.— $\dot{M}_{\text{acc}}$ vs M_{disc} with expectations from models. The colored solid and dashed lines are isochrones, obtained letting the various models for two different values of the initial disk mass (0.1 and 0.01 $M_\odot$) evolve for $t=1$ Myr; for reference the black dotted line shows where $M_{\text{disc}}/\dot{M}_{\text{acc}}$ is equal to 1 Myr. For each case we have colored the region between the lines with different initial masses, to show the region of the parameter space that can be covered by each model when starting from reasonable initial conditions. For the MHD wind case, dashed lines are for a more complex case than that described in the text, in which α_{DW} depends on time.

Solving the equation requires assuming parameterizations for λ and $\dot{\Sigma}_w$, in the same way as in the viscous scenario one is required to assume a parametrization for the viscosity ν . However, while in the viscous picture the α prescription has become a *de facto* standard, there is no commonly used equivalent for the wind case, with various parametrizations available in the literature (Suzuki et al. 2010; Armitage et al. 2013; Bai 2016; Chambers 2019), based on the results of MHD simulations. In line with the spirit of this chapter we will consider instead here the simple approach of Tabone et al. (2022b), who constructed the equivalent of the Shakura and Sunyaev (1973) parameterization for the wind case. Qualitatively the results we will discuss in what follows for this simple case are similar to those from the more sophisticated approaches, and therefore relevant for the discussion here while pedagogically easier to illustrate. (Tabone et al. 2022b) introduces a parameter α_{DW} such that the mass loss rate $\dot{\Sigma}_w$ reads

$$\dot{\Sigma}_w = \frac{3\alpha_{\text{DW}}c_s^2}{4(\lambda-1)\Omega r^2}\Sigma, \quad (9)$$

where the pre-factors have been chosen so that α_{DW} is equivalent to the viscous α , i.e. for a given surface density the accretion rate would be the same as the viscous case: $\dot{M}_{\text{acc}}^{\text{DW}}/\dot{M}_{\text{acc}}^{\text{visc}} \simeq \alpha_{\text{DW}}/\alpha$. The parameter α_{DW} should therefore be thought of as the *efficiency* at which the wind is able

to extract angular momentum from the disk and physically it should be linked to the magnetization of the disk material (Lesur 2020). With this choice the master equation becomes

$$\frac{\partial \Sigma}{\partial t} = \frac{3}{2r} \frac{\partial}{\partial R} \left(\frac{\alpha_{\text{DW}} \Sigma c_s^2}{\Omega} \right) - \frac{3\alpha_{\text{DW}} \Sigma c_s^2}{4(\lambda-1)r^2 \Omega}, \quad (10)$$

which also admits self-similar analytical solutions. Tabone et al. (2022b) presents an extensive analysis of this family of solutions but here we concentrate only on the simplest case in which α_{DW} does not vary with time and viscosity is not taken into account:

$$\Sigma(R, t) \simeq \frac{M_D(t)}{2\pi r_c(t)^2} \left(\frac{R}{R_c} \right)^{-\gamma+\xi} \exp \left[-(R/R_c)^{(2-\gamma)} \right], \quad (11)$$

where $\xi = \frac{1}{2(\lambda-1)}$, called the ejection index (Ferreira and Pelletier 1995) - which vanishes for $\lambda \rightarrow \infty$ -, γ is defined such that $c_s^2 \alpha_{\text{DW}} \propto r^{\gamma-3/2}$ (equivalently to the viscous case) and we have used the approximate sign to neglect factors of order unity in the mass normalisation. Now specialising to the $\gamma = 1$ case for simplicity, the disk mass and the mass accretion rate evolve as

$$M_d(t) = M_0 \exp(-t/t_{\text{acc}}) \quad (12)$$

$$\dot{M}(t) = \frac{M_0}{2t_{\text{acc}}(1+f_M)} \exp(-t/t_{\text{acc}}), \quad (13)$$

where $t_{\text{acc}} = R_c^2/3c_s H \alpha_{\text{DW}}$ is the equivalent of the viscous time and $f_M = \ln(R_c/R_{\text{in}})/(2(\lambda-1))$ (expression valid in the limit of $R_c \gg R_{\text{in}}$) is the ratio between the wind mass-loss rate and the mass accretion rate onto the star. A low (high) f_M means that the wind is (in)efficient at extracting angular momentum and requires low (high) mass-loss rates to drive accretion. The relevant timescale t_{acc} here is the equivalent of the viscous time in viscosity driven models, and we have that $t_{\text{acc}} = (\alpha/\alpha_{\text{DW}}) t_\nu$ (see Eq. 4), that can be larger or smaller than the viscous time depending on the importance of disk winds as measured from α_{DW} . The disk evolutionary timescale reads

$$t_{\text{disk}} = \frac{M_d(t)}{\dot{M}(t)} = 2t_{\text{acc}}(1+f_M). \quad (14)$$

Compared to the viscous case, there are several important differences: (i) the exponential cut-off radius does not grow with time (see lower left panel of Fig. 2): there is no viscous spreading because there is no transport of angular momentum at large radii (ii) the mass and the accretion rate decrease exponentially with time: the disk clears faster because the lack of viscous spreading does not lead to disk evolution slowing down. This is a significant difference with respect to the viscous case, in which disk dispersal needs to be attributed to another process such as photo-evaporation (Clarke et al. 2001, see lower middle panel of Fig. 2), and can reproduce disk dispersal timescales as shown in the population synthesis exercise of Tabone et al. (2022a); (iii) the surface density is flatter and the accretion

rate is reduced by a factor $(1+f_M)$ because the wind removes mass from the disk; (iv) the disk evolutionary timescale does not become longer with time (see lower right panel of Figure 2) and differences with the viscous case are therefore expected when $t \gg t_{\text{acc}}$ (or t_v for the viscous case); (v) the relation between disk mass and accretion rate is still almost linear, but the normalisation does depend on the initial conditions and the properties of the wind.

Fig. 3 shows isochrones for viscous and wind models, i.e. the loci of points in the $\dot{M} - M_{\text{disk}}$ plane occupied by disks that have the same age, starting from the same initial disk mass but with different t_{acc} . While in this case the isochrones are reasonably similar to the viscous case, in Fig. 3 we also plotted with the dashed line isochrones for a more complex case, not discussed above, in which α_{DW} depends on time (Tabone et al. 2022b), showing that MHD winds can also fill the upper left corner of the parameter space, not accessible to purely viscous models. As discussed in Tabone et al. (2022b), physically this corresponds to a different assumed evolution of the disk magnetic field, and in particular to the case in which the magnetic flux is conserved throughout disk evolution. Conversely, the case of constant α_{DW} corresponds to a case in which the magnetic flux decrease at roughly the same rate as the disk mass. Which of the two scenarios is more correct is currently an open question.

Because it is relatively newer, there are fewer studies of disks evolution under the influence of winds coupled with other effects. In particular, dust evolution is expected to have a similar effect to the viscous case in depleting the dust reservoir and move the models to the upper left corner of Figure 3, but this has not been studied yet quantitatively.

3.3. Formation of inner cavities

Protoplanetary disks commonly exhibit substructure, in the form of cavities, rings, arcs, and spirals (Andrews 2020, and also chapter by Bae et al.). The presence of inner cavities was initially inferred from SED modeling, leading to the definition of transitional disks (Espanlat et al. 2014), and subsequently confirmed via mm-imaging. Transitional morphologies can be produced by massive planets or binary companions (Calvet et al. 2002; Rosotti et al. 2016; Price et al. 2018), or in some cases as a consequence of the angular momentum transport processes that lead to disk evolution and dispersal (Alexander et al. 2014; Ercolano and Pascucci 2017). Although not the topic of this chapter, it is relevant to mention here how the models described in § 3.2 can explain these observations. Viscous evolution would predict smooth evolution with a nearly homogeneous depletion of material. On the other hand, the radial dependence of photoevaporative mass loss, when combined with viscous evolution, results in late-time formation of an inner cavity (Clarke et al. 2001). Recent models of X-ray photoevaporation predict that up to half of the observed transitional disks could be compatible with this cavity formation pathway (Picogna et al. 2019). MHD models (Suzuki et al.

2016) can yield “inverted” surface density profiles (increasing with radial distance from the star), which would trap dust and produce broadly transitional morphologies, but unlike in the viscous plus photoevaporative case cavity formation is not a generic prediction.

4. CONSTRAINTS ON DISK EVOLUTION MODELS

In this Section, we use the data from Table 1 compiled as discussed in § 2.5 to describe the main observed relations between disk and stellar/accretion parameters and the possible explanations of these observed relations (§ 4.1). We then use this information to derive constraints on the theoretical models and parameters (§ 4.2).

4.1. Relations between stellar, accretion, and disk properties

The survey of properties of young stars and their disks performed in various star-forming regions with the observational methods presented in § 2.1-2.2 have revealed different relations between the various parameters. Here we report the observational findings using the most up-to-date data available. We then consider the theoretical attempts at reproducing the observed correlations and trends.

4.1.1. Dependence of mass accretion rates on stellar masses

The fact that mass accretion rates scale with stellar mass with a steeper-than-linear relation is well established (e.g., Hillenbrand et al. 1992; Muzerolle et al. 2003; Mohanty et al. 2005; Natta et al. 2006). The spectroscopic surveys carried out in more recent years have confirmed this relation, reporting slopes of $\sim 1.6-2$ and typical spreads in $\dot{M}_{\text{acc}}$ values of about 1–2 dex (e.g., Alcalá et al. 2014, 2017; Manara et al. 2016, 2017b; Venuti et al. 2014a, 2019b; Hartmann et al. 2016), as shown in the past. This is illustrated in Fig. 4, where the $\dot{M}_{\text{acc}} \propto M_{\star}^2$ line is also shown.

Given the more advanced analysis techniques used in the most recent surveys (§ 2.1), it is now clear that most of the observed large spread of $\dot{M}_{\text{acc}}$ values is physical, and not only related to observational uncertainty. Moreover, accretion variability is usually found to produce accretion variations of the order of ~ 0.4 dex (e.g., Biazzo et al. 2014; Costigan et al. 2014; Venuti et al. 2014b), thus smaller than the observed spread, unless secular variability is more important (see chapter by Fischer et al.). Manara et al. (2017b), and similarly Alcalá et al. (2017), have shown that, in a complete sample in a given star-forming region, the values of $\dot{M}_{\text{acc}}$ fill the range between the highest values at $L_{\text{acc}}=L_{\star}$ and the chromospheric noise barrier (Manara et al. 2013a, 2017a), with a small empty region in the $M_{\star}$ range $0.2 - 0.5 M_{\odot}$ at $\dot{M}_{\text{acc}} \sim 10^{-10} M_{\odot}/\text{yr}$, that could be where internal photoevaporation causes rapid disk dispersal (Alexander et al. 2014).

As recently reviewed by Ercolano and Pascucci (2017), it is unclear to what extent the $\dot{M}_{\text{acc}} \propto M_{\star}^2$ reflects features

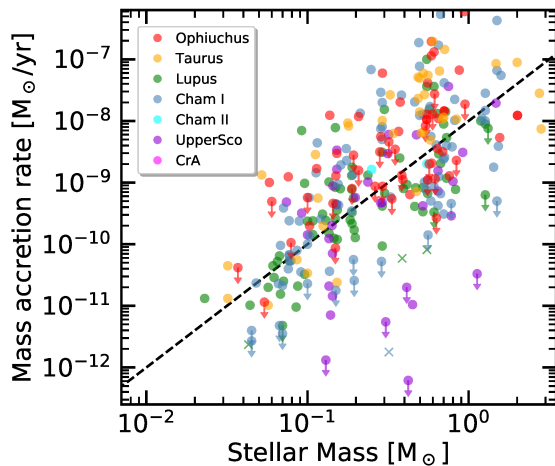


Fig. 4.— $\dot{M}_{\text{acc}}$ vs $M_{\star}$ for the targets for which both quantities are available in Table 1. The dashed line shows the $\dot{M}_{\text{acc}} \propto M_{\star}^2$ line, plotted to guide the eye, but it does not represent a fit to the data.

of the disk evolutionary process or it is simply a by-product of how the initial conditions scale with stellar mass. It is likely that both aspects cooperate to establish the observed correlation, but no work so far has attempted to fully disentangle the two possibilities. In the context of viscously evolving models *Dullemond et al. (2006)* and *Alexander and Armitage (2006)* have explored which initial conditions lead to the observed correlation at the present time. The former work attempted to link explicitly this correlation with simple models of disk formation from a rotating collapsing core, finding that they were able to provide an explanation under the assumption that $t \gg t_v$. The latter work instead explored which correlations with stellar mass in the initial conditions are needed to reproduce the observed correlation, without trying to motivate them from disk formation models, and favored the opposite case in which $t \ll t_v$ and the observed correlation was already present in the initial conditions. As an imprint of the initial conditions the correlation has received comparably less attention in the recent years, but recently *Somigliana et al. 2022* conducted a full investigation of which initial conditions lead to the observed correlation in the viscous framework, both for the $t \gg t_v$ and for the $t \ll t_v$ case. In this case they also considered the correlation between disk mass and stellar mass (see § 4.1.3) which was not known at the time of the two previous studies. Their main result is that, given enough time, in the viscous picture disk mass and accretion rate must scale in this same way with stellar mass, with an exponent which is set by the initial conditions. In the opposite view in which the correlation is a result of the evolutionary process, *Clarke and Pringle (2006)* and *Ercolano et al. (2014)* proposed that the correlation could be an imprint of the disk clearing process. In particular, the latter demonstrated that the correlation is found in the case of disk

dispersal driven by X-ray photo-evaporation, since the observed correlation would merely reflect the scaling of the X-ray photo-evaporation rate with stellar mass. It is still unexplored if this holds true regardless of the initial conditions, and what are the consequences for the scaling of disk mass with stellar mass.

The data in the Chamaeleon I and Lupus regions by *Alcalá et al. (2017)* and *Manara et al. (2017b)* have also shown evidence that a double power-law fit of this relation could be a more statistically robust representation than a simple power-law fit. This would imply a very steep relation at $M_{\star} < 0.2\text{--}0.3 M_{\odot}$, followed by a flatter relation (slope ~ 1) at higher $M_{\star}$. Similar trends are probably already observable also in other regions (e.g., *Venuti et al. 2014b*). On the other hand, the fact that this double power-law behaviour is not observed in younger regions (*Manara et al. 2015*; *Fiorellino et al. 2021*) could suggest that this is an evolutionary effect, with lower-mass stars having a more rapid decrease of $\dot{M}_{\text{acc}}$ than higher-mass stars.

The double power law behavior could be due to different physical regimes operating in the early phases of disk formation and evolution; *Vorobyov and Basu (2008, 2009)* suggested that disk self-gravity plays an important role soon after formation around stars more massive than $M_{\star} \sim 0.5 M_{\odot}$. This drives large accretion torques which leaves less material available in the class II phase and therefore a lower accretion rate which flattens the correlation. Self-gravity is less important and disks evolve more viscously around lower mass stars.

Finally, work is being done to determine the relation between $\dot{M}_{\text{acc}}$ and $M_{\star}$ in the younger phases of PMS and disk evolution. *Fiorellino et al. (2021)* have shown that Class I targets have higher $\dot{M}_{\text{acc}}$ than their Class II counterparts in NGC 1333, and appear to lie in the upper part of the $\dot{M}_{\text{acc}}\text{--}M_{\star}$ relation. New near-infrared surveys of other young star-forming regions are needed to confirm this result.

4.1.2. Disk dust mass as a function of age

By sampling star-forming regions with different ages, the recent ALMA surveys have been able to demonstrate that, in general, the continuum emission, interpreted as disk dust mass, systematically decreases with the age of the region (e.g., *Ansdell et al. 2016, 2017*; *Barenfeld et al. 2016*; *Pascucci et al. 2016*; *Eisner et al. 2018*; *Ruíz-Rodríguez et al. 2018*; *Cox et al. 2017*; *Cieza et al. 2019*; *van Terwisga et al. 2019, 2020*; *Villenave et al. 2021*, see Fig. 5), likely reflecting disk dispersal, dust evolution and/or grain growth (e.g., *Pinilla et al. 2020*). However, this monotonic decrease is not observed in the young Ophiuchus region (*Williams et al. 2019*) and in the possibly young CrA region (*Cazzoletti et al. 2019*). These two surveys pose questions on the simple interpretation of a decrease in mm-size content in disks with age, and possibly suggest that the evolution of the dust content in disks is subject to replenishment, maybe due to planetesimals collisions (e.g., *Turrini et al. 2012, 2019*; *Gerbig et al. 2019*; *Bernabò et al. 2022*).

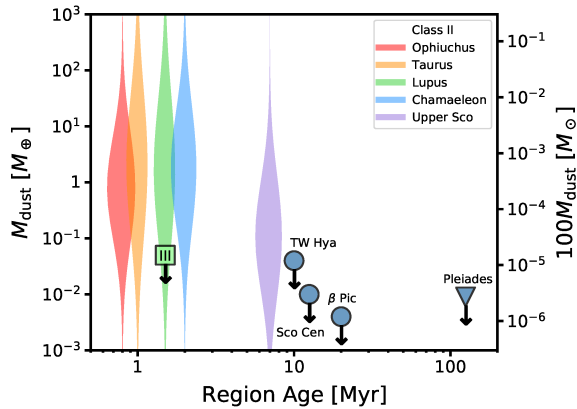


Fig. 5.— The distribution of protoplanetary disk dust masses in regions of different ages. For the Class II disks where there are near-complete samples, the violin plots are log-normal probability distribution functions that best match the cumulative distributions derived from Kaplan Meier survival analysis. The symbols show the upper limits to Class III disks in Lupus and debris disks in the TW Hydra, Sco Cen, β Pic and Pleiades associations.

The star-forming histories of most regions are more complex than a single age indicates and new *Gaia* data on the 3D structure and kinematics are improving our understanding of different subgroups therein (e.g., *Krolkowski et al. 2021*). Similarly, there is an overlap in both sky position and proper motion between the young stars in Lupus with older stars in Sco-Cen that may complicate the interpretation of a rapid disk dispersal from Class II to Class III (*Michel et al. 2021*). Resolving this issue will likely require a thorough analysis of individual stellar properties. Nevertheless, although region-scale demographics are inherently noisy, the large deep ALMA surveys of disks from Class II to Class III and debris disks (*Lovell et al. 2021a*) reveal a clear trend of decreasing disk dust mass (or, more precisely, the amount of dust grains smaller than about a millimeter in size) with mean region age (Fig. 5) and is a robust signature of disk evolution. Dissecting into finer time (and stellar mass) bins is an important goal but may ultimately be limited by the intrinsically small sample sizes.

4.1.3. Dependence of disk dust masses with stellar mass

In the last years, it has been observed that disk dust mass scales with stellar mass. This relation was first reported using pre-ALMA data for the Taurus region (*Andrews et al. 2013*) and the more recent ALMA surveys have confirmed this as a general property of disk populations, and also reported a potential steepening of the relation with age (e.g., *Pascucci et al. 2016*; *Ansdell et al. 2016, 2017*). In particular, *Pascucci et al. (2016)* reported that regions less than a few Myr of age have typically $M_{\text{dust}} \propto M_{\star}^{1.8}$ whereas the older Upper Sco region has a steeper relation of $M_{\text{dust}} \propto M_{\star}^{2.7}$. *Ansdell et al. (2017)* reported consistent

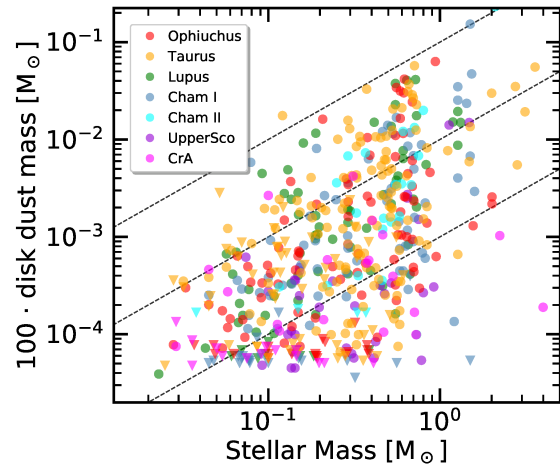


Fig. 6.— Disk dust mass vs stellar mass taken from Table 1. The dashed lines report the value of $M_{\text{disk}} = 0.1, 0.01$, and $0.001 \cdot M_{\star}$, from top to bottom.

results and included the middle-aged σ Orionis region with an intermediate power-law index of 2.0. While the steepening of the relation with age was observed, it is tentative due to large errors on the power-law index, the scaling of disk dust mass with stellar mass in individual regions is now well established. When combining the data collected in Table 1 altogether, the correlation between disk dust mass and stellar mass is not evident (Fig. 6), mainly due to the intrinsic scatter in any single region and the large age difference between regions. The relation between the disk dust mass and $M_{\star}$ in individual regions holds also when including brown dwarfs in the samples (*Testi et al. 2016*; *Ward-Duong et al. 2018b*; *Sanchis et al. 2021*; *Rilinger and Espaillat 2021*), although with hints of deviations that should be checked when larger samples of BDs become available.

Similar to the relation of mass accretion rate and stellar mass (§ 4.1.1), there is a large dispersion of ~ 0.6 – 0.9 dex in M_{dust} values for a given stellar mass (*Pascucci et al. 2016*; *Ansdell et al. 2017*, see also Fig. 6) and the possibility of double power laws providing better fits to the data (e.g., *Akeson et al. 2019*). The large dispersion is present for all regions where this relation has been measured, suggesting it is an inherent property of disk populations that reflects the range of disk conditions (e.g., dust opacities, disk evolutionary stages, and dust temperatures) rather than the age and/or environment of the region.

From the theoretical side this correlation has been studied less than the others. The correlation is probably a mixture of both the initial conditions and the evolutionary process. *Pascucci et al. (2016)* proposed that the steepening of the correlation with time is a result of dust grain growth being in the fragmentation regime, as in this case dust clears faster around stars of smaller mass. This would imply high levels of viscosity ($\alpha \sim 10^{-2}$), which is potentially at odds

with other constraints on this parameter, or values of the fragmentation velocity lower than the few m/s normally used in dust evolution models (e.g. [Birnstiel et al. 2012](#)), based on the results of lab experiments. [Pinilla et al. \(2020\)](#) reconsidered the problem including the effect of dust traps stopping radial drift, finding that in this case the relation can be recovered without invoking high levels of viscosity as long as some correlation between disk mass and stellar mass is present in the initial conditions. However, the models tend to predict that, for $M_\star < 1 M_\odot$, dust inside the traps should efficiently grow up to boulder size and become invisible to sub-mm observations, and this effect had to be artificially suppressed to reconcile with observations. One hypothesis to reconcile this issue could be that substructure are less common around lower mass stars, as recently proposed by [van der Marel and Mulders \(2021\)](#), though the prevalence of sub-structure in the disk population is still unclear as only the largest and brightest disks have been imaged at high resolution.

4.1.4. The relation between mass accretion rates and disk dust mass

As reported in § 3, the models describing disk evolution predict how the mass accretion rate is related to the global disk mass. In particular, it has long been recognized that viscous evolution models predict a tight correlation between these two quantities (e.g., [Hartmann et al. 1998](#); [Dullemond et al. 2006](#)). The range of disk masses and mass accretion rates available was insufficient to show a correlation between these two quantities in the past (e.g., [Hartmann et al. 1998](#); [Najita et al. 2007](#)) but initial empirical suggestions of a linear correlation between these two quantities appeared when including Herbig Ae/Be stars in the sample [Mendigutía et al. \(2012\)](#). The larger samples provided by ALMA and spectroscopic surveys have recently revealed that the relation between disk dust mass and accretion rates in the T Tauri star range is slightly sub-linear in the young Lupus and Chamaeleon I star-forming regions ([Manara et al. 2016](#); [Mulders et al. 2017](#)). Protoplanetary disks in older star-forming regions, like Upper Scorpius, also follow the same relation, although with higher $\dot{M}_{\text{acc}}$ values at low disk dust masses than expected from simple viscous evolution models ([Manara et al. 2020](#)) but within the spread observed in the other younger regions. This spread of ~ 1 dex is typically distributed around the line $M_{\text{disk}}/\dot{M}_{\text{acc}} = 1$ Myr, as shown in Fig. 7 and does not appear to be due to the dependence of both parameters on $M_\star$ ([Mulders et al. 2017](#)).

Finally, initial results on this relation in the Brown Dwarf regime suggests that these objects are located systematically in the lowest part of the distribution ([Sanchis et al. 2021](#)), but the sample size is still limited.

Following the discussion of § 3.2.1, the relation between M_{disk} and $\dot{M}_{\text{acc}}$ is a natural consequence of the viscous scenario in the limit of $t \gg t_v$ ([Jones et al. 2012](#); [Rosotti et al. 2017](#)), with a normalisation that should be roughly equal

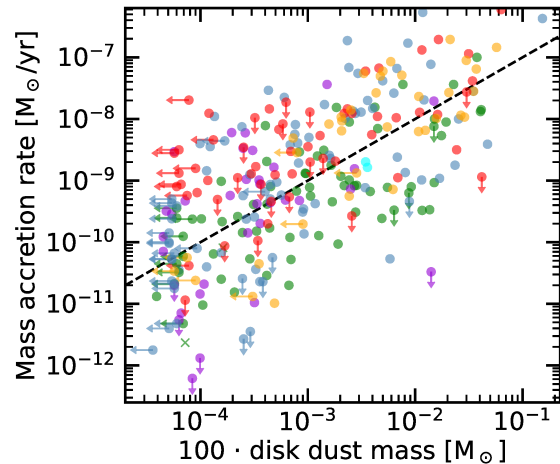


Fig. 7.— Mass accretion rate vs 100 times the disk dust mass obtained using the data from Table 1. The dashed line shows a ratio of $M_{\text{disk}}/\dot{M}_{\text{acc}} = 1$ Myr. Colors as in Fig. 4.

to the age of the region and that, crucially, does not depend on the value of the viscosity. This is roughly what is observed in Lupus ([Manara et al. 2016](#)) and Chameleon ([Mulders et al. 2017](#)), but population studies ([Mulders et al. 2017](#); [Lodato et al. 2017](#)) show that there is information encoded also in the scatter of this relation. For a population of viscously evolving disks, the correlation is established after roughly a viscous time, and the spread of the correlation should reduce with time, until eventually becoming negligible. The relatively large spread observed in Lupus therefore rules out the hypothesis that the viscosity is high and the viscous time correspondingly short ([Lodato et al. 2017](#)), pointing to typical values of $t_v \sim 1$ Myr, which translates into $\alpha \sim 5 \cdot 10^{-4} h_{0.1}^{-2} R_{10}^{3/2}$, where $h_{0.1}$ is the aspect ratio in units of 0.1 and R_{10} is the initial disk size in units of 10 au.

A key prediction of viscous evolution is that, when observing older regions such as Upper Scorpius, the normalisation of the correlation should decrease and the observed spread should become smaller. As mentioned, this is however not observed ([Manara et al. 2020](#)). As shown by [Sellek et al. \(2020a\)](#), these results can be reconciled with viscous theory when taking into account that disk masses are measured through the continuum flux. At the age of Upper Scorpius the dust has undergone significant radial drift, leading to an apparent reduction of the measured disk mass and increasing the spread of the correlation. The inclusion of other processes such as internal photo-evaporation also tends to increase the scatter in the correlation ([Rosotti et al. 2017](#)) and is theoretically needed to reproduce the lowest mass accretion rates observed ([Somigliana et al. 2020](#)). Theoretically it is also expected that photo-evaporation should disperse low disk masses more rapidly, leading to a counter-intuitive *increase*

of the average disk mass in the remaining disk population (Somigliana *et al.* 2020). However, both the disk mass (see §4.1.3) and the photo-evaporation rate (Alexander *et al.* 2014; Picogna *et al.* 2021) scale strongly with the stellar mass, although the importance of this effect has not yet been explored in a population study.

Regarding the MHD wind scenario, there is no general expectation that the $M_{\text{disk}}-\dot{M}_{\text{acc}}$ correlation should hold as for the viscous scenario. It is still possible, however, to reproduce the correlation provided that one chooses suitable, *ad hoc* initial conditions, as done by the initial investigation of Mulders *et al.* (2017) and shown also by Shadmehri and Ghoreyshi (2019). More recently, Tabone *et al.* (2022b) looked in detail at this problem. They showed that, both for the simple model presented in § 3.2.2 and for a more sophisticated case in which α_{DW} varies with time, the observed correlation is reproduced by choosing a disk population with a relatively narrow distribution of t_{acc} . This is expected by inspecting Eqs. 12 and 13, since in this case disk mass and accretion rate are initially proportional to each other and maintain this property throughout the evolution. It is reassuring that these initial conditions, while *ad hoc*, for the more sophisticated case also naturally reproduce the evolution of the disk fraction with time (e.g., Fedele *et al.* 2010), lending some credence to this hypothesis. Please note that Michel *et al.* (2021) recently proposed that these observational timescales should be revised upwards, but the effect of these possibly longer timescales have not been yet addressed. Finally, in this case there is no expectation that the spread should depend on time, a significant difference from the viscous model. In principle this should naturally reproduce the results in Upper Sco of Manara *et al.* (2020) reported above without the need to invoke other effects, though so far this has not been modelled in detail.

Lastly, models that include the presence of a giant planet in the disk predict that the accretion rate should decrease as the planet intercepts part of the mass flow (e.g., Lubow and D’Angelo 2006). Indeed, transition disks with large cavities show values of $\dot{M}_{\text{acc}}$ in line with those of systems of the same stellar mass surrounded by full disks (Manara *et al.* 2014, 2017b; Alcalá *et al.* 2017), whereas they show lower values of $\dot{M}_{\text{acc}}$ when compared with full disks of the same disk mass (Najita *et al.* 2007, 2015; Manara *et al.* 2016; Mulders *et al.* 2017). However, the observed decrease in $\dot{M}_{\text{acc}}$ is smaller than expected for disk models with accreting planets (e.g., Mordasini *et al.* 2015), possibly pointing to the fact that the mass accretion onto planets is overestimated by the models (Manara *et al.* 2019a). Migration of giant planets could be a way to reconcile the observed high accretion rates in transition disks (Rometsch *et al.* 2020).

4.1.5. Findings about disk radii

The measurement of disk dust radii, mainly traced by the extent of the dust continuum emission, have revealed a relation with the luminosity of the disks, first suggested by An-

draws *et al.* (2010), then confirmed with ALMA data (Tripathi *et al.* 2017; Tazzari *et al.* 2017; Andrews *et al.* 2018b). This relation is sub-linear ($R_{\text{disk}} \propto L_{\text{mm}}^{0.5}$) and holds also in the Brown Dwarf regime (e.g., Sanchis *et al.* 2021) and at different millimeter wavelengths (Tazzari *et al.* 2021a).

Hendler *et al.* (2020) have collected literature SMA measurements and re-derived the disk dust radii from all the previous ALMA surveys in the star-forming regions of Lupus, Chamaeleon I, Ophiuchus, Taurus, and Upper Scorpius to confirm that this correlation between disk dust size and disk continuum luminosity is present in all regions. However, they demonstrated that the slope of this correlation is pretty stable with a slope of ~ 0.5 in all regions but Upper Scorpius, which presents a shallower slope ~ 0.2 . Finally, they also show that, in general, disk dust sizes in Lupus and Chamaeleon I are similar, whereas they are slightly smaller in the older Upper Scorpius region. Similarly to Tazzari *et al.* (2017), the disk dust sizes in the younger regions of Ophiuchus and Taurus are possibly slightly larger than in the older regions, but this last finding is heavily based on pre-ALMA data.

From theory it is known that the dust, while being the most accessible observational tracer, is highly affected by radial drift, as well as depending on features of the dust opacity (Rosotti *et al.* 2019a). Indeed, Rosotti *et al.* (2019b) proposed that the observed correlation between dust radii and flux is a signature of dust grain growth in the drift regime, pointing to relatively low levels of viscosity. Alternatively, the correlation could also arise due to the presence of optically thick substructure in disks, as proposed by Tripathi *et al.* (2017) and Andrews *et al.* (2018a). Given plausible disk temperatures, the disk fluxes are lower than would be expected if the disks were completely optically thick, implying that only parts of the disks should be optically thick, as expected if the emission is dominated by the bright rings often imaged by ALMA. Zormpas *et al.* (2022) modelled dust drift and growth including the effect of substructure, finding that in this case disks are compatible with the observed correlation for a wide variety of initial conditions. By stopping radial drift and therefore the shrinking of the disk, the presence of substructures in most disks would also explain why the ratio between dust and gas radii from ^{12}CO emission in most observed disks is ~ 2 (e.g., Ansdell *et al.* 2018), while in models of smooth disks it rapidly goes above 5 (Trapman *et al.* 2019; Toci *et al.* 2021). This could be the case for the high ratios observed in some disks (e.g., Facchini *et al.* 2019; Long *et al.* 2022). This would help reconciling these models with observations of the disk spectral index (e.g., Tazzari *et al.* 2021a). Because of the current observational biases in the sample of disks with measured radii (favoring bright and large disks), it is however still unclear whether sub-structure is present in all disks or whether disks fall into two categories, with and without sub-structure, as proposed by van der Marel and Mulders (2021). This is also suggested by the results of Banzatti *et al.* (2020) and Kalyaan *et al.* (2021), who find a bimodality in the presence of water in the inner disks, pos-

sibly linked to the presence of structures. In an alternative view instead, as proposed by [Zhu et al. \(2019\)](#), disks could be completely optically thick but characterized by a very high albedo, which due to self-scattering tends to reduce the resulting brightness.

The measurement of disk radii should in principle be the best tool to distinguish between viscosity and winds, as illustrated schematically by Fig. 2: in the viscous picture the radius should expand while in the wind scenario it should shrink. One of the main issues in this attempt is the aforementioned radial drift and opacity impact on dust disk radii ([Rosotti et al. 2019a](#)). While a comparison between viscous and MHD models ([Zagaria et al. 2022](#)) confirms that dust radii should expand only in the viscous case, tracing this expansion requires very deep and expensive observations. This leads to exploring the *gas* tracers to measure disk radii.

[Najita and Bergin \(2018\)](#) did an initial attempt at collecting existing measurements and found hints that the disk gas size increases with time, possibly supporting the viscous hypothesis. While encouraging, these initial findings call for detailed modelling. The first question is whether available observational tracers should be expected to reflect the theoretical trend, and in the affirmative case, assembling a large enough observational sample comprized of disks of different age is not a small task. Measurements of disk radii with ^{12}CO are to date available only for two regions, Lupus and Upper Scorpius ([Barenfeld et al. 2017](#); [Ansdell et al. 2018](#); [Sanchis et al. 2021](#)), and for some disks in Taurus ([Long et al. \(2022\)](#)). Through detailed thermo-chemical modelling [Trapman et al. \(2020\)](#) showed that the general trend that viscous disks expand with time is preserved. They showed that the small ^{12}CO radii measured in Lupus rule out high viscosities and imply $\alpha \lesssim 10^{-3}$. However, viscosity cannot account for the fact that disks in Upper Sco are smaller than in Lupus, pointing to other effects such as external photo-evaporation, MHD winds, or chemical effects.

[Trapman et al. \(2022\)](#) modeled the corresponding case of how the CO radius should evolve in the wind case, confirming that it should decrease but too slowly to explain the small disks in Upper Scorpius. Invoking factors of 10-100 levels of CO depletion (see the chapter by [Miotello et al](#)) would be able to explain the observed trend.

4.2. Implications for disk evolution models

We show in Fig. 8 the ratio of the total disk mass, assumed to be 100 times the dust mass, to the mass accretion rate, i.e. t_{disk} , as a function of age for the sample collected here (see § 2.5 and Table 1). In the same figure, we overplot the expectations from viscous evolution models (§ 3.2.1) and from the simple model to describe MHD wind evolution of disks (§ 3.2.2). On top of that, we also show the line $t_{\text{disk}} = \text{age}$, and the effect of dust evolution on the viscous evolution expectations ([Rosotti et al. 2019a](#); see also [Sellek et al. 2020a](#)).

As described in § 3.2, t_{disk} is constant with time in the MHD disk wind model, and it only depends on the disk

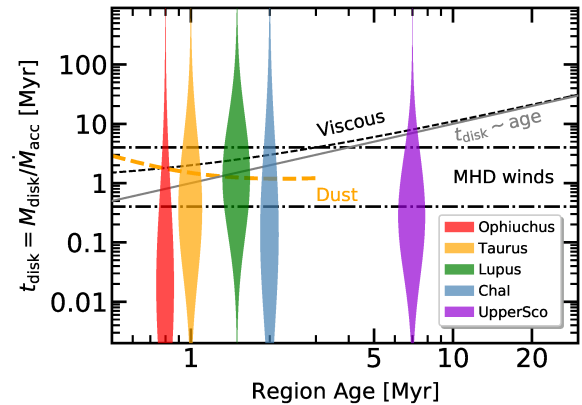


Fig. 8.— Violin plot for t_{disk} , the ratio of 100 times the disk mass to the mass accretion rate, as a function of the age of the regions. The solid line reports values of t_{disk} equal to the age of the regions. The dashed line shows the expectation of a viscous model with $t_v = 1$ Myr and $\gamma = 1.5$. The dot-dashed lines are used for expectations from MHD wind models with $t_{\text{acc}} = 0.1$ and 1 Myr, respectively. The thick dashed orange line represents the evolution of a viscous model with $\gamma = 1$, $\alpha = 10^{-3}$, $M_0 = 10^{-1} M_\odot$, $R_0 = 30$ au when the effect of dust evolution is included.

wind parameters, whereas the value of t_{disk} grows with time in the viscous framework (e.g., [Lodato et al. 2017](#); [Rosotti et al. 2017](#); [Mulders et al. 2017](#)). Finally, including the effects of dust evolution to the viscous model leads to a decrease of t_{disk} with time ([Sellek et al. 2020b](#)). The available data do not show a clear trend of increasing t_{disk} with time (see also [Manara et al. 2020](#)), and are thus only marginally compatible with pure viscous evolution (e.g., [Lodato et al. 2017](#); [Mulders et al. 2017](#); [Sellek et al. 2020a](#)). A simple MHD disk wind model would also agree with most of the data (e.g., [Mulders et al. 2017](#); [Tabone et al. 2022b](#)). Finally, including the dust evolution in the models leads to a better agreement with the data in the regions older than ~ 1.5 – 2 Myr, but it is unable to reproduce the data in the younger regions ([Sellek et al. 2020b,a](#)).

It is clear that simple viscous models with high viscosity ($\alpha \sim 10^{-2}$) are not able to reproduce the observations. Indeed, in order to have viscous times of the order of several Myrs, as shown in Eq. 4, we need low viscosities, with $\alpha \simeq 10^{-4} - 10^{-3}$. Different flavors of low-viscosity models, including dust evolution and MHD disk wind models, should be considered to match predictions with observations (e.g., [Mulders et al. 2017](#); [Lodato et al. 2017](#)). The MHD disk wind models are promising but not yet sufficiently constrained. In both frameworks, a range of model parameters is needed to reproduce the observed spread of t_{disk} . This may be expressed either in different values of α (e.g., [Mulders et al. 2017](#)), or t_v (e.g., [Lodato et al. 2017](#)), or disk wind parameters ([Tabone et al. 2022b](#)). Whether and how much this spread is related to the differences in ages

measured in individual regions (see § 2.1.2) or to additional effects, such as binarity, remains to be seen.

It is also evident that models must include the effects of dust evolution must to compare with observations. As shown by *Sellek et al. (2020b,a)* and in Fig. 8, models with dust evolution show better agreement with data in regions with ages ≥ 1.5 –2 Myr. However, dust evolution is currently treated in a very simple way and should be better linked with knowledge of disk structures (e.g., *Andrews 2020; Toci et al. 2021; Zormpas et al. 2022*). Moreover, these models do not yet include any dependence on stellar mass. Doing so could reveal new ways of testing the models than Fig. 8, especially because this is readily available for several targets (§ 2.1.2).

5. IMPACTS ON PLANET FORMATION AND EARLY DYNAMICS MODELS

Following § 4.2, we can now assess whether the current assumptions used in models of planet population synthesis analysis and planetesimal formation should be modified to take into account the new results from the recent surveys of young stars and their disks. Details on these models are provided in the chapter by *Drążkowska et al.* In most of these works, the disks viscously evolve in a way that is parameterized by a constant α parameter typically assumed to be $\alpha \sim 10^{-3}$ (e.g., *Ida and Lin 2004; Benz et al. 2014; Mordasini et al. 2012, 2015; Coleman and Nelson 2014; Bitsch et al. 2015a,b; Drążkowska and Dullemond 2018; Emsenhuber et al. 2021*), and matched to older observations, such as *Hartmann et al. (1998)*. Photoevaporative winds are included in many cases to describe disk dispersal and also to compare with and explain the distribution of giant planet semimajor axes (e.g., *Alexander and Pascucci 2012; Ercolano and Rosotti 2015; Coleman and Nelson 2016*). Only a limited number of models include the effect of MHD disk winds on the evolution of disks. *Ogihara et al. (2015, 2018)* have used the disk structure of *Suzuki et al. (2016)*, where disk winds dominate the disk evolution, and combined this with models of planet formation and migration to show that Type I migration is suppressed.

Detailed comparison between the models by *Mordasini et al. (2012)* and observations has been recently carried out by *Manara et al. (2019a)*, who showed that the constant values of $\alpha = 2 \times 10^{-3}$ assumed in those models lead to a smaller spread of $\dot{M}_{\text{acc}}$ in the models when compared with observed values on the $\dot{M}_{\text{acc}}-\dot{M}_{\text{disk}}$ plane. In summary, it appears that the assumptions used in various planet formation synthesis models should be revised including a significant spread of values for α , and possibly also including the effects of MHD disk winds. A comparison of the assumed disk model parameters with the observed ones, for example on the $\dot{M}_{\text{acc}}-\dot{M}_{\text{disk}}$ plane (see *Manara et al. 2019a*), should also be shown to demonstrate that the underlying hypotheses match observations. This kind of comparison with the observations of disks should be part of the tests carried out on the models in the same way as they are tested against

observed properties of exoplanet populations.

The latest generation of planetesimal formation models pave the way toward a new interpretation of disk observations where collisional growth and destruction affect the millimeter emission (e.g., *Gerbige et al. 2019*) and even its relation with accretion onto the central star (e.g., *Appelgren et al. 2020*). Such ab-initio simulations that include both treatment of gas and dust evolution represent a promising new way to test models of disk evolution and compare with observational data.

6. CONCLUSIONS AND FUTURE PERSPECTIVE

The surveys of young stars and their disks carried out in the last years have provided us with a statistically sound sample of data to test the models of disk evolution and planet formation. We have learned that several relations between disk and stellar properties are observed, and we are beginning to see evolutionary links at the boundary between protoplanetary and debris disks. However, both the steps to connect protoplanetary and debris disks and the explanation of the observed correlation between disk properties and stellar mass are not yet thoroughly treated in theoretical works. Indeed, a big draw-back of the current disk evolution models is the lack of a clear description of how these models scale with stellar mass. This parameter, readily measured for many targets, could be a discriminant between the models. However, further constraints on the model parameters must be obtained in order to predict the scaling with both disk and stellar parameters. In particular, we think that measurements or limits on disk magnetic fields are essential for constraining MHD disk wind models, and mass loss rates from the winds are also key to constrain both MHD and photoevaporative wind models (see also Chapter by *Pascucci et al.*).

The relation between disk dust mass and mass accretion rate, currently the best way to test disk evolution models, has been now observed in star-forming regions with different ages but still shows an unexpected similarity between regions and a large spread of values. Based on the current analytical descriptions, it is not yet possible to firmly exclude some of the theoretical frameworks, but only to start to learn the limits of the various models, and how they must be improved. In particular, the effect of the evolution of dust should be included in the models, and models with low viscosity should be used. Population studies considering different effects in the models are also promising ways to better constrain the models.

In our discussions here, and in most of the literature on this topic, we are perhaps overly bound to a legacy that dates back to observational studies of the ISM. However there are profound differences between the interstellar and circumstellar medium that, although we now know quite well, we often do not take sufficiently into account.

Dust grains grow rapidly, fragment, and drift (*Testi et al. 2014*). Disk dust mass measurements readily take account the resultant changes in the opacity relative to the ISM, as

maximum grain sizes change from microns to millimeters, but they ignore the growth into planetesimals (see Chapter by *Miotello et al.*). Cosmochemistry tells us that some differentiated, and therefore gravitationally cohesive, bodies formed very early in the history of the Solar System, within ~ 0.1 Myr after collapse of the protosolar nebula. Streaming instabilities can efficiently form abundant planetesimals on such a timescale, with mass fractions as large as 50% relative to the particles that we observe at millimeter wavelengths. Solid-gas separation leads to divergent evolutionary paths resulting in local (definitely) and global (likely) changes in the gas-to-dust ratio from the ISM value of 100. More succinctly, protoplanetary disks are definitely not protoplanesimal and the range of sizes of solid particles is multiple orders of magnitude greater than in the ISM.

If we interpret the millimeter continuum observations as a modified ISM with large grains, the inferred disk dust masses have an approximately lognormal distribution in any given star-forming region. Young regions have remarkably similar distributions but older regions with ages greater than a few Myr, shift systematically to lower masses. Curiously, however, the dispersion around the decreasing mean mass does not significantly evolve. In addition, disks have shallower millimeter spectral indices than molecular cores or clouds indicating more efficient emission from approximately millimeter-sized grains. The distribution of these spectral indices is also remarkably similar from region to region, both young and old, showing that grains grow quickly to millimeter sizes and such grains persist during any further growth to centimeters and beyond.

If, instead, we interpret these observations in terms of disk processes, then we might conclude that while the millimeter flux declines with time due to a steady loss of small particles, the spectral index remains the same because the limited range of grain sizes that we see are distributed in a balance between growth and fragmentation. The large dispersion, ~ 1 dex, in the dust mass distribution probably reflects a wide range of disk initial conditions. Any diversity in subsequent evolution should further broaden the distribution with time but the reason this is not seen may be because the millimeter emitting dust is in quasi-equilibrium and relatively insensitive to any divergence at the upper end of the size distribution. From this perspective, global dust demographics may have limited utility for understanding the next steps of planet formation. Future progress will come from making use of what we can see to infer more about what we cannot, through resolved observations of disk structures that trap dust and modeling them as sites of planetesimal formation. Unbiased high resolution ALMA surveys of disk structure to follow its evolution will be a key part of this strategy and, hopefully, a chapter in PPVIII.

The observations of disk gas radii could also be a promising additional piece of information to test disk evolution mechanisms. Only a small sub-set of disks have been studied with deep line observations (*Öberg et al. 2021*, and see Chapter by *Miotello et al.*) to date. To make progress, dedicated sensitive gas surveys of large samples of disks at

moderate resolution are needed.

Finally, our inventory of disks is still relatively small and it remains instructive to carry out unresolved observations of young stars and disks beyond the nearby young star-forming regions in different environments or different ages. These surveys should be as unbiased and complete in the target selection as possible, in order to cover a large parameter space to be tested with models.

Acknowledgments

We thank the referees, the editor Kengo Tomida, the SAC advisor of this chapter Doug Johnstone, and David Wilner for their suggestions to improve the manuscript. We thank F. Zagaria for carefully checking the data table attached to this chapter. We thank Erin Readling and Jamar Kittling for help with the data analysis. This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 823823 (DUSTBUSTERS). This work was partly supported by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) - Ref no. FOR 2634/1 TE 1024/1-1. GR acknowledges support from the Netherlands Organisation for Scientific Research (NWO, program number 016.Veni.192.233) and from an STFC Ernest Rutherford Fellowship (grant number ST/T003855/1). AMH is supported by a Cottrell Scholar Award from the Research Corporation for Science Advancement. JPW is supported by the National Science Foundation through grant AST-1907486. Funded by the European Union under the European Union's Horizon Europe Research & Innovation Programme 101039452 (WANDA) and 101039651 (DiscEvol). Views and opinions expressed are however those of the author(s) only and do not necessarily reflect those of the European Union or the European Research Council. Neither the European Union nor the granting authority can be held responsible for them.

This work has made use of data from the European Space Agency (ESA) mission *Gaia* (<https://www.cosmos.esa.int/gaia>), processed by the *Gaia* Data Processing and Analysis Consortium (DPAC, <https://www.cosmos.esa.int/web/gaia/dpac/consortium>). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the *Gaia* Multilateral Agreement.

REFERENCES

- Adam C. et al., 2021 *A&A*, 653, A88.
- Akeson R. L. and Jensen E. L. N., 2014 *ApJ*, 784, 1, 62.
- Akeson R. L. et al., 2019 *ApJ*, 872, 2, 158.
- Alcalá J. M. et al., 2014 *A&A*, 561, A2.
- Alcalá J. M. et al., 2017 *A&A*, 600, A20.
- Alcalá J. M. et al., 2019 *A&A*, 629, A108.
- Alcalá J. M. et al., 2021 *A&A*, 652, A72.
- Alexander R. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 475.
- Alexander R. D. and Armitage P. J., 2006 *ApJL*, 639, 2, L83.
- Alexander R. D. and Pascucci I., 2012 *MNRAS*, 422, 1, L82.
- Alibert Y. et al., 2005 *A&A*, 434, 1, 343.

- Andrews S. M., 2020 *ARA&A*, 58, 483.
- Andrews S. M. and Williams J. P., 2005 *ApJ*, 631, 2, 1134.
- Andrews S. M. et al., 2010 *ApJ*, 723, 2, 1241.
- Andrews S. M. et al., 2013 *ApJ*, 771, 2, 129.
- Andrews S. M. et al., 2018a *ApJ*, 865, 2, 157.
- Andrews S. M. et al., 2018b *ApJL*, 869, 2, L41.
- Ansdell M. et al., 2016 *ApJ*, 828, 1, 46.
- Ansdell M. et al., 2017 *AJ*, 153, 5, 240.
- Ansdell M. et al., 2018 *ApJ*, 859, 1, 21.
- Appelgren J. et al., 2020 *A&A*, 638, A156.
- Armitage P. J. et al., 2013 *ApJL*, 778, 1, L14.
- Bai X.-N., 2016 *ApJ*, 821, 2, 80.
- Bai X.-N. and Stone J. M., 2013 *ApJ*, 769, 1, 76.
- Balbus S. A. and Hawley J. F., 1991 *ApJ*, 376, 214.
- Balog Z. et al., 2009 *ApJ*, 698, 2, 1989.
- Banzatti A. et al., 2020 *ApJ*, 903, 2, 124.
- Baraffe I. et al., 2012 *ApJ*, 756, 2, 118.
- Baraffe I. et al., 2015 *A&A*, 577, A42.
- Barenfeld S. A. et al., 2016 *ApJ*, 827, 2, 142.
- Barenfeld S. A. et al., 2017 *ApJ*, 851, 2, 85.
- Beccari G. et al., 2015 *A&A*, 574, A44.
- Beccari G. et al., 2018 *MNRAS*, 481, 1, L11.
- Beckwith S. V. W. et al., 1990 *AJ*, 99, 924.
- Benz W. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 691.
- Bergin E. A. and Williams J. P., 2017 *Formation, Evolution, and Dynamics of Young Solar Systems*, vol. 445 of *Astrophysics and Space Science Library* (M. Pessah and O. Gressel), p. 1.
- Bernabò L. M. et al., 2022 *ApJL*, 927, 2, L22.
- Bertout C. et al., 1988 *ApJ*, 330, 350.
- Béthune W. et al., 2017 *A&A*, 600, A75.
- Biazzo K. et al., 2012 *A&A*, 547, A104.
- Biazzo K. et al., 2014 *A&A*, 572, A84.
- Biazzo K. et al., 2019 *ApJ*, 875, 1, 51.
- Birnstiel T. et al., 2010 *A&A*, 513, A79.
- Birnstiel T. et al., 2012 *A&A*, 539, A148.
- Bitsch B. et al., 2015a *A&A*, 582, A112.
- Bitsch B. et al., 2015b *A&A*, 575, A28.
- Blandford R. D. and Payne D. G., 1982 *MNRAS*, 199, 883.
- Booth R. A. et al., 2017 *MNRAS*, 469, 4, 3994.
- Braun T. A. M. et al., 2021 *ApJ*, 908, 1, 46.
- Calvet N. et al., 2000 *Protostars and Planets IV* (V. Mannings, A. P. Boss, and S. S. Russell), p. 377.
- Calvet N. et al., 2002 *ApJ*, 568, 2, 1008.
- Carpenter J. M. et al., 2014 *ApJ*, 787, 1, 42.
- Castelli F. and Kurucz R. L., 2003 *Modelling of Stellar Atmospheres*, vol. 210 (N. Piskunov, W. W. Weiss, and D. F. Gray), p. A20.
- Cataldi G. et al., 2018 *ApJ*, 861, 1, 72.
- Cataldi G. et al., 2020 *ApJ*, 892, 2, 99.
- Cavallius M. et al., 2019 *A&A*, 628, A127.
- Cazzoletti P. et al., 2019 *A&A*, 626, A11.
- Chambers J., 2019 *ApJ*, 879, 2, 98.
- Choquet É. et al., 2016 *ApJL*, 817, 1, L2.
- Cieza L. A. et al., 2019 *MNRAS*, 482, 1, 698.
- Clarke C. J. and Pringle J. E., 2006 *MNRAS*, 370, 1, L10.
- Clarke C. J. et al., 2001 *MNRAS*, 328, 2, 485.
- Cohen M. and Kuhl L. V., 1979 *ApJS*, 41, 743.
- Coleman G. A. L. and Haworth T. J., 2020 *MNRAS*, 496, 1, L111.
- Coleman G. A. L. and Nelson R. P., 2014 *MNRAS*, 445, 1, 479.
- Coleman G. A. L. and Nelson R. P., 2016 *MNRAS*, 460, 3, 2779.
- Costigan G. et al., 2014 *MNRAS*, 440, 4, 3444.
- Cox E. G. et al., 2017 *ApJ*, 851, 2, 83.
- Cronin-Coltsmann P. F. et al., 2021 *MNRAS*, 504, 3, 4497.
- Czekala I. et al., 2016 *ApJ*, 818, 2, 156.
- Daley C. et al., 2019 *ApJ*, 875, 2, 87.
- de Gregorio-Monsalvo I. et al., 2013 *A&A*, 557, A133.
- De Marchi G. et al., 2013 *ApJ*, 775, 1, 68.
- De Marchi G. et al., 2017 *ApJ*, 846, 2, 110.
- Di Folco E. et al., 2020 *A&A*, 635, A94.
- Dong J. et al., 2020 *ApJ*, 889, 1, 47.
- Drążkowska J. and Dullemond C. P., 2018 *A&A*, 614, A62.
- Dullemond C. P. et al., 2006 *ApJL*, 645, 1, L69.
- Dunham M. M. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 195.
- Dunham M. M. et al., 2015 *ApJS*, 220, 1, 11.
- Eisner J. A. et al., 2018 *ApJ*, 860, 1, 77.
- Emsenhuber A. et al., 2021 *A&A*, 656, A69.
- Ercolano B. and Pascucci I., 2017 *Royal Society Open Science*, 4, 170114.
- Ercolano B. and Rosotti G., 2015 *MNRAS*, 450, 3, 3008.
- Ercolano B. et al., 2014 *MNRAS*, 439, 1, 256.
- Espaillat C. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 497.
- Espaillat C. C. et al., 2017 *ApJ*, 844, 1, 60.
- Espaillat C. C. et al., 2022 *AJ*, 163, 3, 114.
- Esplin T. L. and Luhman K. L., 2020 *AJ*, 159, 6, 282.
- Esplin T. L. and Luhman K. L., 2022 *AJ*, 163, 2, 64.
- Espósito T. M. et al., 2020 *AJ*, 160, 1, 24.
- Evans Neal J. I. et al., 2009 *ApJS*, 181, 2, 321.
- Facchini S. et al., 2019 *A&A*, 626, L2.
- Fairlamb J. R. et al., 2015 *MNRAS*, 453, 1, 976.
- Fairlamb J. R. et al., 2017 *MNRAS*, 464, 4, 4721.
- Fang M. et al., 2021 *ApJ*, 908, 1, 49.
- Faramaz V. et al., 2019 *AJ*, 158, 4, 162.
- Faramaz V. et al., 2021 *AJ*, 161, 6, 271.
- Fedele D. et al., 2010 *A&A*, 510, A72.
- Feiden G. A., 2016 *A&A*, 593, A99.
- Feldt M. et al., 2017 *A&A*, 601, A7.
- Ferland G. J. et al., 2017 *RMxAA*, 53, 385.
- Ferreira J. and Pelletier G., 1995 *A&A*, 295, 807.
- Fiorellino E. et al., 2021 *A&A*, 650, A43.
- Flaherty K. et al., 2019 *ApJ*, 872, 1, 92.
- Flaherty K. et al., 2020 *ApJ*, 895, 2, 109.
- Flaherty K. M. et al., 2017 *ApJ*, 843, 2, 150.
- Flock M. et al., 2020 *ApJ*, 897, 2, 155.
- Frasca A. et al., 2015a *A&A*, 575, A4.
- Frasca A. et al., 2015b *A&A*, 575, A4.
- Frasca A. et al., 2017 *A&A*, 602, A33.
- Gaia Collaboration et al., 2016 *A&A*, 595, A1.
- Gaia Collaboration et al., 2021 *A&A*, 649, A1.
- Galli P. A. B. et al., 2020 *A&A*, 634, A98.
- Galli P. A. B. et al., 2021 *A&A*, 646, A46.
- Gerbig K. et al., 2019 *A&A*, 629, A116.
- Grant S. L. et al., 2021 *ApJ*, 913, 2, 123.
- Guilet J. and Ogilvie G. I., 2014a *MNRAS*, 441, 1, 852.
- Guilet J. and Ogilvie G. I., 2014b *MNRAS*, 441, 1, 852.
- Gullbring E. et al., 1998 *ApJ*, 492, 1, 323.
- Gully-Santiago M. A. et al., 2017 *ApJ*, 836, 2, 200.
- Hardy A. et al., 2015 *A&A*, 583, A66.
- Harris R. J. et al., 2012 *ApJ*, 751, 2, 115.
- Hartmann L. et al., 1998 *ApJ*, 495, 1, 385.
- Hartmann L. et al., 2016 *ARA&A*, 54, 135.
- Hendler N. et al., 2020 *ApJ*, 895, 2, 126.

- Herczeg G. J. and Hillenbrand L. A., 2008 *ApJ*, 681, 1, 594.
- Herczeg G. J. and Hillenbrand L. A., 2014 *ApJ*, 786, 2, 97.
- Herczeg G. J. and Hillenbrand L. A., 2015 *ApJ*, 808, 1, 23.
- Herczeg G. J. et al., 2019 *ApJ*, 878, 2, 111.
- Higuchi A. E. et al., 2017 *ApJL*, 839, 1, L14.
- Higuchi A. E. et al., 2019a *ApJL*, 885, 2, L39.
- Higuchi A. E. et al., 2019b *ApJ*, 883, 2, 180.
- Hillenbrand L. A., 1997 *AJ*, 113, 1733.
- Hillenbrand L. A. et al., 1992 *ApJ*, 397, 613.
- Holland W. S. et al., 2017 *MNRAS*, 470, 3, 3606.
- Hughes A. M. et al., 2017 *ApJ*, 839, 2, 86.
- Hughes A. M. et al., 2018 *ARA&A*, 56, 541.
- Ida S. and Lin D. N. C., 2004 *ApJ*, 604, 1, 388.
- Ingleby L. et al., 2011 *ApJ*, 743, 2, 105.
- Ingleby L. et al., 2013 *ApJ*, 767, 2, 112.
- Ingleby L. et al., 2014 *ApJ*, 790, 1, 47.
- Jones M. G. et al., 2012 *MNRAS*, 419, 2, 925.
- Kalari V. M., 2019 *MNRAS*, 484, 4, 5102.
- Kalari V. M. et al., 2015 *MNRAS*, 453, 1, 1026.
- Kalyaan A. et al., 2021 *ApJ*, 921, 1, 84.
- Kenyon S. J. and Hartmann L., 1995 *ApJS*, 101, 117.
- Kim M. et al., 2018 *A&A*, 618, A38.
- Klusmeyer J. et al., 2021 *ApJ*, 921, 1, 56.
- Kral Q. and Latter H., 2016 *MNRAS*, 461, 2, 1614.
- Kral Q. et al., 2016 *MNRAS*, 461, 1, 845.
- Kral Q. et al., 2017 *MNRAS*, 469, 1, 521.
- Kral Q. et al., 2019 *MNRAS*, 489, 4, 3670.
- Kratter K. and Lodato G., 2016 *ARA&A*, 54, 271.
- Krivov A. V., 2010 *Research in Astronomy and Astrophysics*, 10, 5, 383.
- Krolikowski D. M. et al., 2021 *AJ*, 162, 3, 110.
- Laibe G. and Price D. J., 2014 *MNRAS*, 444, 2, 1940.
- Lanzafame A. C. et al., 2015 *A&A*, 576, A80.
- Lesur G., 2020 *arXiv e-prints*, arXiv:2007.15967.
- Lesur G. et al., 2013 *A&A*, 550, A61.
- Lesur G. et al., 2015 *A&A*, 582, L9.
- Leung P. K. C. and Ogilvie G. I., 2019 *MNRAS*, 487, 4, 5155.
- Lieman-Sifry J. et al., 2016 *ApJ*, 828, 1, 25.
- Lin D. N. C. and Papaloizou J., 1986 *ApJ*, 309, 846.
- Lodato G. and Clarke C. J., 2004 *MNRAS*, 353, 3, 841.
- Lodato G. and Rice W. K. M., 2004 *MNRAS*, 351, 2, 630.
- Lodato G. et al., 2017 *MNRAS*, 472, 4, 4700.
- Löhne T., 2020 *A&A*, 641, A75.
- Lombart M. et al., 2020 *A&A*, 639, A54.
- Long F. et al., 2017 *ApJ*, 844, 2, 99.
- Long F. et al., 2018 *ApJ*, 863, 1, 61.
- Long F. et al., 2019 *ApJ*, 882, 1, 49.
- Long F. et al., 2022 *ApJ*, 931, 1, 6.
- Lovell J. B. et al., 2021a *MNRAS*, 500, 4, 4878.
- Lovell J. B. et al., 2021b *MNRAS*, 502, 1, L66.
- Lubow S. H. and D'Angelo G., 2006 *ApJ*, 641, 1, 526.
- Lubow S. H. et al., 1994 *MNRAS*, 267, 2, 235.
- Luhman K. L., 2020a *AJ*, 160, 4, 186.
- Luhman K. L., 2020b *AJ*, 160, 4, 186.
- Luhman K. L. and Esplin T. L., 2020 *AJ*, 160, 1, 44.
- Luhman K. L. et al., 2003 *ApJ*, 590, 1, 348.
- Luppe P. et al., 2020 *MNRAS*, 499, 3, 3932.
- Lynden-Bell D. and Pringle J. E., 1974 *MNRAS*, 168, 603.
- Lyra W. and Umurhan O. M., 2019 *PASP*, 131, 1001, 072001.
- MacGregor M. A. et al., 2016 *ApJ*, 823, 2, 79.
- MacGregor M. A. et al., 2017 *ApJ*, 842, 1, 8.
- MacGregor M. A. et al., 2018 *ApJ*, 869, 1, 75.
- MacGregor M. A. et al., 2019 *ApJL*, 877, 2, L32.
- Manara C. F. et al., 2013a *A&A*, 558, A114.
- Manara C. F. et al., 2013b *A&A*, 551, A107.
- Manara C. F. et al., 2014 *A&A*, 568, A18.
- Manara C. F. et al., 2015 *A&A*, 579, A66.
- Manara C. F. et al., 2016 *A&A*, 591, L3.
- Manara C. F. et al., 2017a *A&A*, 605, A86.
- Manara C. F. et al., 2017b *A&A*, 604, A127.
- Manara C. F. et al., 2018 *A&A*, 615, L1.
- Manara C. F. et al., 2019a *A&A*, 631, L2.
- Manara C. F. et al., 2019b *A&A*, 628, A95.
- Manara C. F. et al., 2020 *A&A*, 639, A58.
- Manara C. F. et al., 2021 *A&A*, 650, A196.
- Manjavacas E. et al., 2016 *MNRAS*, 455, 2, 1341.
- Manjavacas E. et al., 2020 *MNRAS*, 491, 4, 5925.
- Marino S. et al., 2018 *MNRAS*, 479, 4, 5423.
- Marino S. et al., 2019 *MNRAS*, 484, 1, 1257.
- Marino S. et al., 2020a *MNRAS*, 498, 1, 1319.
- Marino S. et al., 2020b *MNRAS*, 492, 3, 4409.
- Marshall J. P. et al., 2017 *MNRAS*, 468, 3, 2719.
- Marshall J. P. et al., 2021 *MNRAS*, 501, 4, 6168.
- Matrà L. et al., 2017 *ApJ*, 842, 1, 9.
- Matrà L. et al., 2018a *ApJ*, 859, 1, 72.
- Matrà L. et al., 2018b *ApJ*, 853, 2, 147.
- Matrà L. et al., 2019a *AJ*, 157, 4, 135.
- Matrà L. et al., 2019b *AJ*, 157, 3, 117.
- Matthews B. C. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 521.
- Melis C. et al., 2021 *ApJ*, 923, 1, 90.
- Mendigutía I. et al., 2012 *A&A*, 543, A59.
- Meng H. Y. A. et al., 2014 *Science*, 345, 6200, 1032.
- Meng H. Y. A. et al., 2015 *ApJ*, 805, 1, 77.
- Mesa D. et al., 2021 *MNRAS*, 503, 1, 1276.
- Michel A. et al., 2021 *ApJ*, 921, 1, 72.
- Miley J. M. et al., 2018 *A&A*, 615, L10.
- Miotello A. et al., 2014 *A&A*, 572, A96.
- Miotello A. et al., 2016 *A&A*, 594, A85.
- Miotello A. et al., 2017 *A&A*, 599, A113.
- Mohanty S. et al., 2005 *ApJ*, 626, 1, 498.
- Moór A. et al., 2016 *ApJ*, 826, 2, 123.
- Moór A. et al., 2017 *ApJ*, 849, 2, 123.
- Moór A. et al., 2019 *ApJ*, 884, 2, 108.
- Moór A. et al., 2021 *ApJ*, 910, 1, 27.
- Morbidelli A. and Raymond S. N., 2016 *Journal of Geophysical Research (Planets)*, 121, 10, 1962.
- Mordasini C. et al., 2012 *A&A*, 547, A111.
- Mordasini C. et al., 2015 *International Journal of Astrobiology*, 14, 2, 201.
- Mulders G. D. et al., 2017 *ApJ*, 847, 1, 31.
- Murphy S. J. et al., 2018 *MNRAS*, 476, 3, 3290.
- Muzerolle J. et al., 1998 *AJ*, 116, 6, 2965.
- Muzerolle J. et al., 2003 *ApJ*, 592, 1, 266.
- Najita J. R. and Bergin E. A., 2018 *ApJ*, 864, 2, 168.
- Najita J. R. et al., 2007 *MNRAS*, 378, 1, 369.
- Najita J. R. et al., 2015 *MNRAS*, 450, 4, 3559.
- Najita J. R. et al., 2022 *ApJ*, 925, 1, 45.
- Natta A. et al., 2006 *A&A*, 452, 1, 245.
- Nederlander A. et al., 2021 *ApJ*, 917, 1, 5.
- Nelson R. P. et al., 2013 *MNRAS*, 435, 3, 2610.
- Norfolk B. J. et al., 2021 *MNRAS*, 507, 3, 3139.
- Öberg K. I. et al., 2021 *ApJS*, 257, 1, 1.
- Ogihara M. et al., 2015 *A&A*, 579, A65.

- Ogihara M. et al., 2018 *A&A*, 615, A63.
- Owen J. E. et al., 2011 *MNRAS*, 412, 1, 13.
- Pan M. et al., 2016 *ApJ*, 832, 1, 81.
- Parker R. J. et al., 2021 *MNRAS*, 502, 2, 2665.
- Pascucci I. et al., 2016 *ApJ*, 831, 2, 125.
- Pawellek N. and Krivov A. V., 2015 *MNRAS*, 454, 3, 3207.
- Pawellek N. et al., 2014 *ApJ*, 792, 1, 65.
- Pawellek N. et al., 2021 *MNRAS*, 502, 4, 5390.
- Pearce T. D. and Wyatt M. C., 2015 *MNRAS*, 453, 3, 3329.
- Pecaut M. J. and Mamajek E. E., 2013 *ApJS*, 208, 1, 9.
- Pecaut M. J. and Mamajek E. E., 2016 *MNRAS*, 461, 1, 794.
- Pecaut M. J. et al., 2012 *ApJ*, 746, 2, 154.
- Pegues J. et al., 2021 *ApJ*, 908, 1, 42.
- Picogna G. et al., 2019 *MNRAS*, 487, 1, 691.
- Picogna G. et al., 2021 *MNRAS*, 508, 3, 3611.
- Pinilla P. et al., 2020 *A&A*, 635, A105.
- Pinilla P. et al., 2021 *A&A*, 649, A122.
- Pinte C. et al., 2016 *ApJ*, 816, 1, 25.
- Premnath P. H. et al., 2020 *Research Notes of the American Astronomical Society*, 4, 7, 100.
- Price D. J. et al., 2018 *MNRAS*, 477, 1, 1270.
- Pringle J. E., 1981 *ARA&A*, 19, 137.
- Pudritz R. E. et al., 2007 *Protostars and Planets V* (B. Reipurth, D. Jewitt, and K. Keil), p. 277.
- Randich S. et al., 2013 *The Messenger*, 154, 47.
- Regály Z. et al., 2018 *MNRAS*, 473, 3, 3547.
- Ricci L. et al., 2015 *ApJ*, 798, 2, 124.
- Rice W. K. M. et al., 2005 *MNRAS*, 364, 1, L56.
- Rigliaco E. et al., 2012 *A&A*, 548, A56.
- Rigliaco E. et al., 2016 *A&A*, 588, A123.
- Rilinger A. M. and Espaillat C. C., 2021 *ApJ*, 921, 2, 182.
- Rizzuto A. C. et al., 2020 *ApJ*, 889, 2, 175.
- Robinson C. E. and Espaillat C. C., 2019 *ApJ*, 874, 2, 129.
- Rometsch T. et al., 2020 *A&A*, 643, A87.
- Rosotti G. P. and Clarke C. J., 2018 *MNRAS*, 473, 4, 5630.
- Rosotti G. P. et al., 2016 *MNRAS*, 459, 3, 2790.
- Rosotti G. P. et al., 2017 *MNRAS*, 468, 2, 1631.
- Rosotti G. P. et al., 2019a *MNRAS*, 486, 1, L63.
- Rosotti G. P. et al., 2019b *MNRAS*, 486, 4, 4829.
- Rugel M. et al., 2018 *A&A*, 609, A70.
- Ruíz-Rodríguez D. et al., 2018 *MNRAS*, 478, 3, 3674.
- Sanchis E. et al., 2020 *A&A*, 633, A114.
- Sanchis E. et al., 2021 *A&A*, 649, A19.
- Sefilian A. A. et al., 2021 *ApJ*, 910, 1, 13.
- Sellek A. D. et al., 2020a *MNRAS*, 498, 2, 2845.
- Sellek A. D. et al., 2020b *MNRAS*, 492, 1, 1279.
- Sepulveda A. G. et al., 2019 *ApJ*, 881, 1, 84.
- Shadmehri M. and Ghoreyshi S. M., 2019 *MNRAS*, 488, 4, 4623.
- Shakura N. I. and Sunyaev R. A., 1973 *A&A*, 500, 33.
- Sheehan P. D. et al., 2019 *ApJ*, 874, 2, 136.
- Sibthorpe B. et al., 2018 *MNRAS*, 475, 3, 3046.
- Siess L. et al., 2000 *A&A*, 358, 593.
- Silverberg S. M. et al., 2016 *ApJL*, 830, 2, L28.
- Silverberg S. M. et al., 2020 *ApJ*, 890, 2, 106.
- Simon J. B. et al., 2013 *ApJ*, 775, 1, 73.
- Simon M. et al., 2017 *ApJ*, 844, 2, 158.
- Simon M. et al., 2019 *ApJ*, 884, 1, 42.
- Sissa E. et al., 2018 *A&A*, 613, L6.
- Soderblom D. R. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 219.
- Somers G. et al., 2020 *The Astrophysical Journal*, 891, 1, 29.
- Somigliana A. et al., 2020 *MNRAS*, 492, 1, 1120.
- Somigliana A. et al., 2022 *MNRAS*, 514, 4, 5927.
- Stassun K. G. et al., 2014 *NewAR*, 60, 1.
- Stelzer B. et al., 2013 *A&A*, 558, A141.
- Su K. Y. L. et al., 2019 *AJ*, 157, 5, 202.
- Suzuki T. K. et al., 2010 *ApJ*, 718, 2, 1289.
- Suzuki T. K. et al., 2016 *A&A*, 596, A74.
- Syer D. and Clarke C. J., 1995 *MNRAS*, 277, 3, 758.
- Tabone B. et al., 2022a *MNRAS*, 512, 1, L74.
- Tabone B. et al., 2022b *MNRAS*, 512, 2, 2290.
- Tazzari M. et al., 2017 *A&A*, 606, A88.
- Tazzari M. et al., 2021a *MNRAS*, 506, 2, 2804.
- Tazzari M. et al., 2021b *MNRAS*, 506, 4, 5117.
- Teague R. et al., 2018 *ApJ*, 864, 2, 133.
- Testi L. et al., 2014 *Protostars and Planets VI* (H. Beuther, R. S. Klessen, C. P. Dullemond, and T. Henning), p. 339.
- Testi L. et al., 2016 *A&A*, 593, A111.
- Testi L. et al., 2022 *A&A*, 663, A98.
- Toci C. et al., 2021 *MNRAS*, 507, 1, 818.
- Trapman L. et al., 2019 *A&A*, 629, A79.
- Trapman L. et al., 2020 *A&A*, 640, A5.
- Trapman L. et al., 2022 *ApJ*, 926, 1, 61.
- Tripathi A. et al., 2017 *ApJ*, 845, 1, 44.
- Turrini D. et al., 2012 *ApJ*, 750, 1, 8.
- Turrini D. et al., 2019 *ApJ*, 877, 1, 50.
- van der Marel N. and Mulders G. D., 2021 *AJ*, 162, 1, 28.
- van der Marel N. et al., 2018 *ApJ*, 854, 2, 177.
- van der Plas G. et al., 2016 *ApJ*, 819, 2, 102.
- van Terwisga S. E. et al., 2019 *A&A*, 628, A85.
- van Terwisga S. E. et al., 2020 *A&A*, 640, A27.
- van Terwisga S. E. et al., 2022 *A&A*, 661, A53.
- Venuti L. et al., 2014a *A&A*, 570, A82.
- Venuti L. et al., 2014b *A&A*, 570, A82.
- Venuti L. et al., 2018 *A&A*, 609, A10.
- Venuti L. et al., 2019a *A&A*, 621, A14.
- Venuti L. et al., 2019b *A&A*, 632, A46.
- Vernet J. et al., 2011 *A&A*, 536, A105.
- Villenave M. et al., 2021 *A&A*, 653, A46.
- Vioque M. et al., 2020 *A&A*, 638, A21.
- Vorobyov E. I. and Basu S., 2008 *ApJL*, 676, 2, L139.
- Vorobyov E. I. and Basu S., 2009 *ApJ*, 703, 1, 922.
- Ward-Duong K. et al., 2018a *AJ*, 155, 2, 54.
- Ward-Duong K. et al., 2018b *AJ*, 155, 2, 54.
- Wilhelm M. J. C. and Portegies Zwart S., 2022 *MNRAS*, 509, 1, 44.
- Williams J. P. and Best W. M. J., 2014 *ApJ*, 788, 1, 59.
- Williams J. P. and Cieza L. A., 2011 *ARA&A*, 49, 1, 67.
- Williams J. P. et al., 2019 *ApJL*, 875, 2, L9.
- Winter A. J. et al., 2018 *MNRAS*, 478, 2, 2700.
- Woitke P. et al., 2016 *A&A*, 586, A103.
- Wyatt M. C., 2008 *ARA&A*, 46, 339.
- Wyatt M. C. et al., 2015 *Ap&SS*, 357, 2, 103.
- Xu W. and Kunz M. W., 2021 *MNRAS*, 508, 2, 2142.
- Yelverton B. et al., 2019 *MNRAS*, 488, 3, 3588.
- Yelverton B. et al., 2020 *MNRAS*, 495, 2, 1943.
- Yen H.-W. et al., 2018 *A&A*, 616, A100.
- Zagaria F. et al., 2021 *MNRAS*, 507, 2, 2531.
- Zagaria F. et al., 2022 *MNRAS*, 514, 1, 1088.
- Zhu Z. et al., 2019 *ApJL*, 877, 2, L18.
- Zormpas A. et al., 2022 *A&A*, 661, A66.
- Zurlo A. et al., 2020 *MNRAS*, 496, 4, 5089.
- Zurlo A. et al., 2021 *MNRAS*, 501, 2, 2305.