



# Exceptional Soft Magnetic Properties of an Ordered Multi-principal Element Alloy with Disordered Nanoprecipitates

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## Abstract

In this work, a new non-equiautomic multi-principal element alloy (MPEA)  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  with excellent soft magnetic performance was fabricated. The microstructure and magnetic behavior of the as-cast alloy were investigated experimentally and theoretically using synchrotron X-ray diffraction, transmission electron microscopy, atom probe tomography, vibrating sample magnetometry, and density functional theory calculations. The alloy consists of an ordered B2-phase matrix enriched with Co/Al and uniformly distributed BCC nanoprecipitates enriched with Fe/Mn. The new alloy exhibits a high saturation magnetization of  $\sim 158 \text{ Am}^2/\text{kg}$ , a low coercivity of  $\sim 108 \text{ A/m}$ , a high electrical resistivity of  $\sim 238 \mu\Omega \text{ cm}$ , and a high Curie temperature of  $\sim 1020 \text{ K}$ , which shows an excellent combination of soft magnetic properties compared to previously reported MPEAs and conventional FeCo alloys. The findings thus provide a new perspective for designing high-performance materials for soft magnetic applications.

**Keywords** Multi-principal element alloy · Nanoprecipitates · Soft magnetic properties · Density functional theory

## Introduction

Multi-principal element alloys (MPEAs), often referred to as high entropy alloys (HEAs), are a new class of alloys with multiple equiautomic or near-equiautomic mixing of metallic elements [1, 2]. In contrast to the traditional development of new alloys based on one major element, this multicomponent approach has expanded the compositional space of alloy

design and attracted significant research interest. MPEAs are usually single-phase solid solutions, e.g., face-centered cubic (FCC) or body-centered cubic (BCC), or dual-phase structures produced through the precipitation of ordered compounds (such as FCC/L1<sub>2</sub> or BCC/B2) developed by tuning alloy compositions and/or thermomechanical processing [3–10]. These MPEAs have demonstrated some unusual mechanical properties, such as excellent combination of strength and ductility [7–9], good resistance to high-temperature softening [10] and fracture [4], and attractive tribological properties [11].

Soft magnetic materials are key to efficient power conversion with wide range of applications including wide-bandgap semiconductors, electric vehicles, and aerospace industries [12, 13]. As the world transitions to a more electrified vehicles with sustainable sources of energy, there has been an increasing demand for novel soft magnetic materials which enable improved efficiency of power transformation with less energy losses. Ideal soft magnetic materials for these applications have a high saturation magnetization ( $M_s$ ), low coercivity ( $H_c$ ), and high electrical resistivity ( $\rho$ ). The aforementioned MPEAs offer a new perspective for the design of advanced soft magnetic materials and the soft magnetic performance of several MPEAs have been reported [14–26].

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Zhang et al. investigated a series of  $\text{FeCoNi}(\text{AlSi})_x$  MPEAs with various soft magnetic properties attained by adjusting the Al and Si content with the optimum balance of magnetic and electrical properties ( $M_s = 1.15 \text{ T}$  or  $\sim 131 \text{ Am}^2/\text{kg}$ ,  $H_c = 1400 \text{ A/m}$ , and  $\rho = 69.5 \mu\Omega \text{ cm}$ ) being achieved for the FCC MPEA  $\text{FeCoNiAl}_{0.2}\text{Si}_{0.2}$  [21]. They further studied another  $(\text{Fe}_{0.3}\text{Co}_{0.5}\text{Ni}_{0.2})_{100-x}(\text{Al}_{1/3}\text{Si}_{2/3})_x$  alloy system and successfully optimized the soft magnetic properties with relatively high  $M_s$  close to  $150 \text{ Am}^2/\text{kg}$  and low  $H_c$  of  $96 \text{ A/m}$  for  $(\text{Fe}_{0.3}\text{Co}_{0.5}\text{Ni}_{0.2})_{95}(\text{Al}_{1/3}\text{Si}_{2/3})_5$  alloy prepared via the maglev melting method [26]. It was recently reported that an excellent combination of a low coercivity of  $78 \text{ A/m}$ , a moderate saturation magnetization of  $100 \text{ Am}^2/\text{kg}$ , and good electrical resistivity of  $103 \mu\Omega \text{ cm}$  was obtained via designing a  $\text{FeCo-Ni-Ta-Al}$  multicomponent alloy with ferromagnetic FCC matrix and paramagnetic coherent ordered FCC ( $\text{L1}_2$ ) nanoparticles [3]. Jung et al. examined the effects of varying the Fe and Co content on the phase formation and soft magnetic behavior of  $\text{Al}_{0.1}(\text{Fe}_{1+x}\text{CoCr}_{1-x}\text{Mn})_{0.9}$  MPEAs and found that the MPEA  $\text{Al}_{0.1}(\text{Fe}_{1.6}\text{CoCr}_{0.4}\text{Mn})_{0.9}$ , consisting of a disordered BCC matrix and nanoscale ordered BCC (B2) precipitates, showed the highest  $M_s$  of  $135 \text{ Am}^2/\text{kg}$  [27].

In this study, we designed an MPEA  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  with a B2 matrix containing disordered BCC nanoprecipitates. The microstructure, magnetic properties, and electrical resistivity of the alloy were investigated both experimentally and theoretically. The MPEA has an outstanding combination of soft magnetic and electrical performance, and is, thus, promising for advanced soft magnetic applications where high power density and low hysteresis-related and eddy-current-related energy losses are required.

## Method

### Experimental Procedure

An MPEA with a nominal composition of  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  (at.%) was prepared by arc melting a mixture of the constituent metals (99.97% Fe, 99.5% Co, 99.9% Mn, and 99.9% Al) in a Centorr Series 5 Bell Jar with a water-chilled copper crucible and a 2% lanthanated tungsten stinger under a Ti-gettered high-purity argon atmosphere. The ingot was flipped and remelted three times to ensure chemical homogeneity.

Synchrotron high-energy X-ray diffraction (XRD) of the as-cast alloy was conducted to investigate the crystal structure phases using beamline 11-ID-C (X-ray wavelength =  $0.1173 \text{ \AA}$ ) at the Advanced Photon Source at Argonne National Laboratory. A Thermo Fisher Tecnai F20 field emission gun (FEG) transmission electron microscope (TEM) was utilized for microstructural characterization of

the alloy at an accelerating voltage of  $200 \text{ kV}$ . Specimens for TEM observations were prepared by mechanically grinding and polishing 3-mm-disk samples and then further thinning via twin-jet electropolishing in a Struers TenuPol-5 unit with a solution of 15 v/v% nitric acid in methanol at  $\sim 14 \text{ V}$  at a temperature of  $253 \text{ K}$ . Atom probe tomography (APT) was undertaken to analyze the local chemical compositions of different phases by employing a local electrode atom probe (LEAP), 5000 XR (Cameca Instrument Inc., Madison, WI, USA). Laser-assisted field evaporation was performed at  $50 \text{ K}$  by applying a laser pulse energy of  $40 \text{ pJ}$  at a repetition rate of  $125 \text{ kHz}$ . Samples for APT were prepared from a bulk sample using a Helios Plasma FIB/SEM (FEI, Hillsboro, OR, USA) and placed onto a standard 36-post APT coupon (Cameca Instruments, Inc., Madison, WI, USA).

Cube-shaped specimens with dimensions of  $\sim 2.3 \text{ mm} \times 2.3 \text{ mm} \times 2.3 \text{ mm}$  were used for magnetic properties measurements on a Lakeshore Instruments 7300 vibrating sample magnetometer (VSM). Magnetic hysteresis loops were performed at room temperature under a maximum applied field of  $10 \text{ kOe}$  (or  $\sim 800 \text{ kA/m}$ ) with at least three tests to obtain  $M_s$  and  $H_c$ . The Curie temperature,  $T_c$ , was also measured with the VSM from  $323$  to  $1223 \text{ K}$  under an applied field of  $5 \text{ kOe}$  (or  $\sim 400 \text{ kA/m}$ ). The electrical resistivity  $\rho$  was measured on sheet specimens with thicknesses of  $\sim 0.5 \text{ mm}$  using a Four-Point Probe Resistivity system. The reported values are the average of ten measurements.

### Computational Methodology

Density functional theory (DFT) simulations were employed to investigate the magnetic structures of the B2 and BCC phases in the MPEA. The simulations were performed using the Vienna Ab Initio Simulation Package (VASP) [28, 29], in which the projector-augmented wave method was adopted [30]. The Perdew–Burke–Ernzerhof (PBE) functional [31] was chosen as the exchange–correlation functional while the plane wave energy cut-off was set as  $405 \text{ eV}$ . Three  $4 \times 4 \times 4$  cubic supercells of different atomic arrangements were constructed to represent the B2 matrix and the BCC precipitate, respectively (examples shown in Fig. 5a and 5b). The special quasi-random structure (SQS) technique [32], as implemented in the Alloy Theoretic Automated Toolkit [33, 34], was applied to improve the representativeness of the alloy configuration sampling, with up to third nearest neighbors considered for the pair correlations and first for the triplet. BCC and B2 structured supercells with compositions corresponding to the values measured by APT were used for the DFT calculations (Table 1). The atomic configuration in the sub-lattice of the B2 phase was constructed by assuming that it is similar to a B2 structured  $\text{Fe}_{30}\text{Co}_{40}\text{Al}_{15}\text{Mn}_{15}$  alloy in our previous study [16] in which the atomic site occupancy

**Table 1** Chemical compositions (at.%) of  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  obtained from APT analyses

	Fe	Co	Mn	Al
Overall	$38.0 \pm 0.1$	$30.4 \pm 0.1$	$14.9 \pm 0.1$	$16.6 \pm 0.1$
BCC precipitates	$50.1 \pm 1.8$	$12.2 \pm 1.8$	$28.9 \pm 2.3$	$8.8 \pm 1.1$
B2 matrix	$36.2 \pm 0.1$	$32.4 \pm 0.1$	$13.7 \pm 0.1$	$17.7 \pm 0.1$

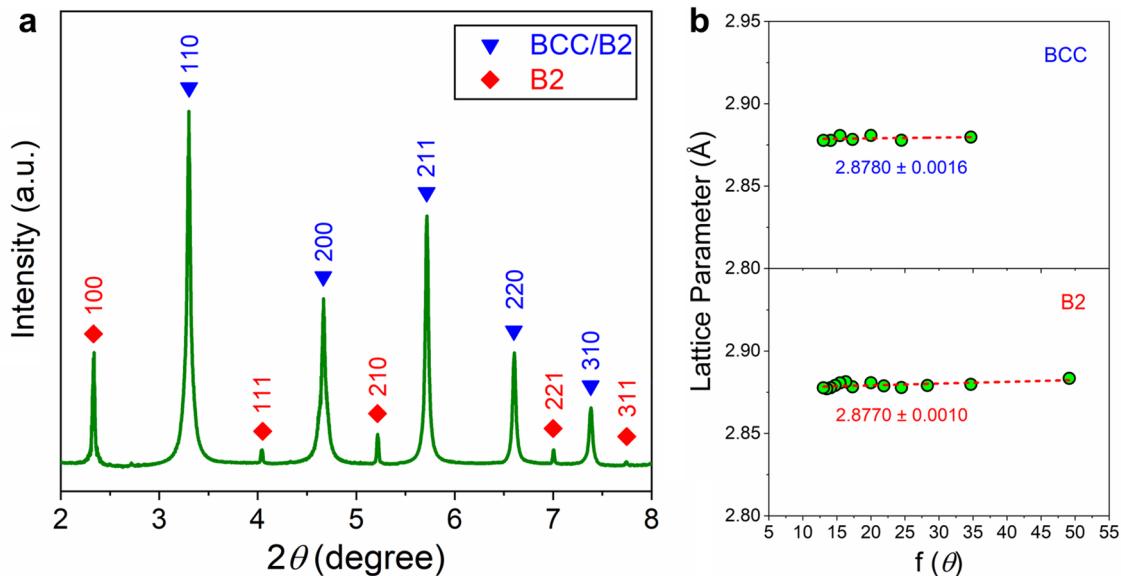
was determined using a TEM/EDS-based technique, i.e., ALCHEMI (Atom Location by CHanneling Enhanced MIcroanalysis) [35]. For the structure optimization, two strategies were employed: in the first strategy we allowed only the ionic movements and fixed the lattice parameters as the experimental ones, while in the second strategy we optimized both the ionic positions and the lattice parameters. The first strategy reflected the relative strain conditions between the matrix and the precipitate as observed in the experiments, while the second would eliminate the influence of possibly excessive strain due to the discrepancy between the DFT and the experimental lattice parameters. The force criterion was 0.01 eV/ Å and the electronic convergence criterion was  $10^{-6}$  eV. The  $2 \times 2 \times 2$  gamma-centered Monkhorst–Pack k-point grid was used in the structural optimization, while the  $4 \times 4 \times 4$  grid of the same scheme was used in the density of state (DOS) calculation. Regarding the initial magnetic structures, collinear magnetism description was adopted. The Fe, Co, and Al atoms were set to have parallel moments, whereas four cases were considered for the moments of Mn, i.e., Mn moments parallel to the rest, Mn

moments antiparallel, and Mn on one sublattices parallel, while those on the other sublattices antiparallel.

## Results

Figure 1a shows a synchrotron XRD pattern of the as-cast  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloy. The diffraction pattern shows peaks associated with B2 ordered structure, indicating that the current alloy could be either single B2 phase or a mixture of both B2 and disordered BCC phases. Dark-field (DF) TEM images of the as-cast specimen viewed along [110] and [100] are shown in Fig. 2a and c. The presence of {001} superlattice reflections in their corresponding selected area diffraction patterns (SAED), in Fig. 2b and d, confirms the B2 ordering. The DF images obtained under  $\mathbf{g} = 001$  and  $\mathbf{g} = 010$  superlattice reflections clearly reveal an ordered B2 matrix with bright contrast and disordered BCC precipitates with dark contrast. These rod-like, BCC nanoscale precipitates, which are  $\sim 9$  nm wide and  $\sim 22$  nm long, are uniformly distributed in the B2 matrix. The lattice parameters determined from synchrotron XRD (Fig. 1b) are  $2.8780 \pm 0.0016$  Å and  $2.8770 \pm 0.0010$  Å for the BCC and B2 phases, respectively.

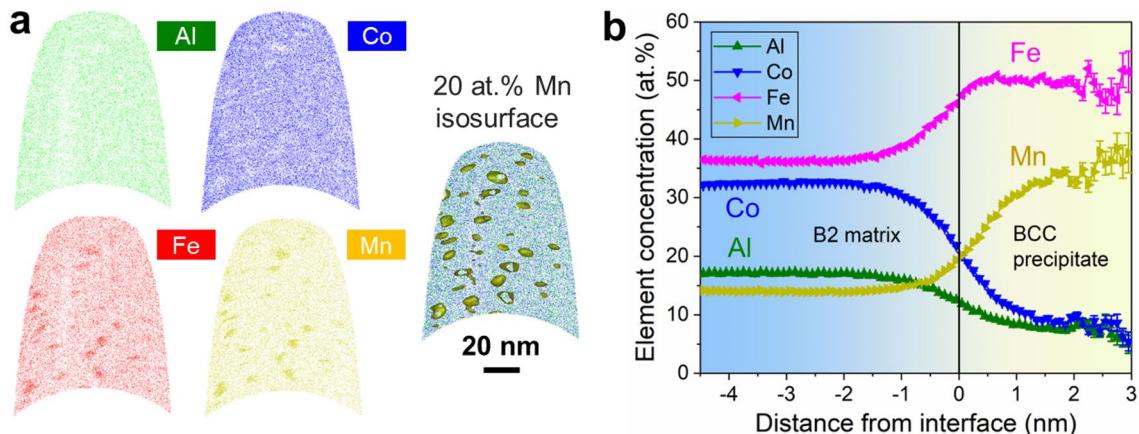
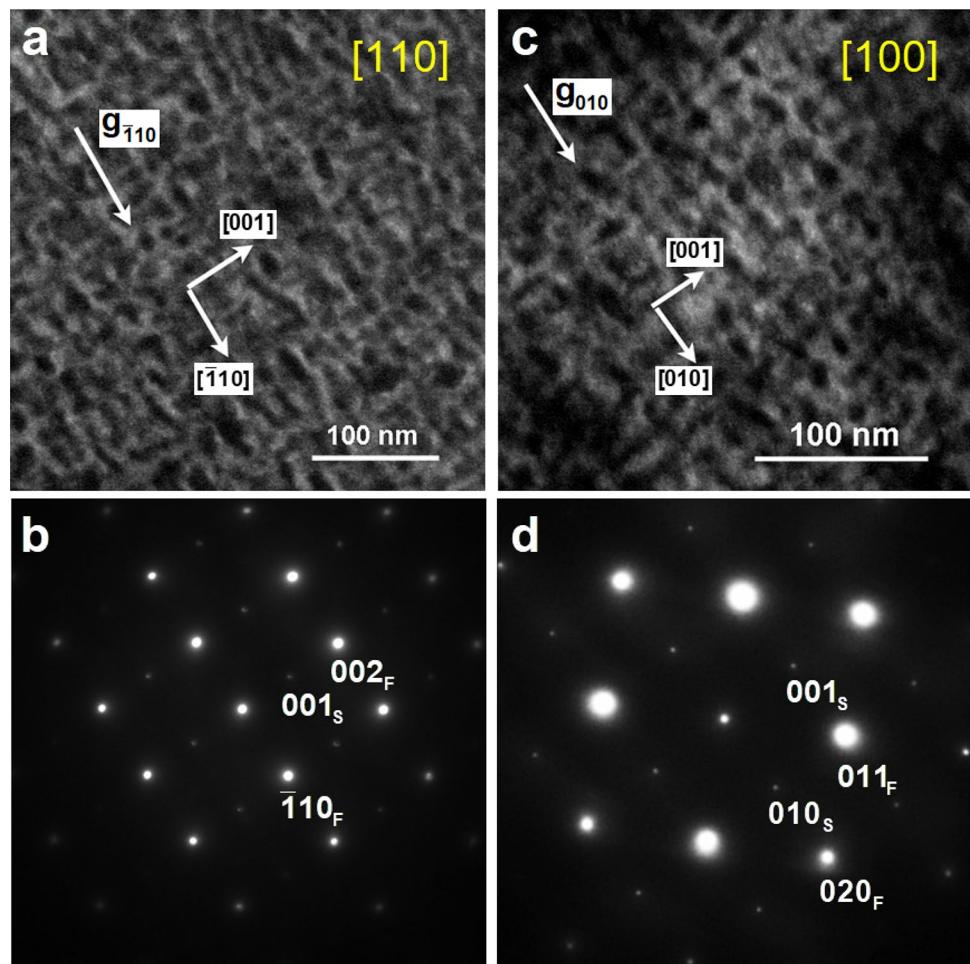
In order to quantitatively analyze the elemental partitioning between the two B2/BCC phases, 3D-APT analysis was performed. The elemental maps and iso-concentration surface of 20 at.% Mn are displayed in Fig. 3a, highlighting the disordered BCC precipitates. The results show an inhomogeneous elemental distributions with Fe and Mn enrichments in the precipitates. A typical compositional profile



**Fig. 1** **a** Synchrotron XRD pattern of  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloy. **b** Plots of measured lattice parameter values versus  $f(\theta)$  of each peak for BCC and B2 phases, where  $f(\theta) = \cos^2(\theta) \cdot (1/\sin \theta + 1/\theta)/2$  and  $\theta$

is the Bragg angle of each peak. The best lattice parameters ( $a$ ) were obtained at  $f(\theta) = 0$  (i.e., y-intercept) [36]

**Fig. 2** Dark-field (DF) TEM images and the corresponding SAED patterns of  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloy along **(a, b)** [110] zone and **c, d** [100] zone axes. The diffraction vectors  $\mathbf{g}$  used to obtain the images are indicated. In the SAED patterns, “F” indicates fundamental reflections and “S” indicates superlattice reflections



**Fig. 3** **a** APT reconstructions of principal elements and iso-concentration surface of 20 at.% Mn from the analysis of  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloy. **b** Elemental concentration profiles across the interface between the B2 matrix and BCC precipitate

across the B2/BCC interface is shown in Fig. 3b. It is readily observed that the Fe and Mn partition to the disordered BCC precipitates, whereas the Co and Al partition to the B2 matrix. Specifically, the BCC phase contains ~50 at.%

Fe and ~29 at.% Mn while the B2 phase contains ~36 at.% Co and ~18 at.% Al, see Table 1. The stoichiometries of the BCC nanoprecipitates and B2 matrix were determined to be  $\text{Fe}_{50}\text{Co}_{12}\text{Mn}_{29}\text{Al}_9$  and  $\text{Fe}_{36}\text{Co}_{32}\text{Mn}_{14}\text{Al}_{18}$  (at.%), respectively.

The elemental partitioning can be further quantified in terms of partitioning coefficient ( $K_i$ ), defined as the ratio of the concentration of element  $i$  in the B2 ( $C_i^{B2}$ ) to the concentration of the same element in the BCC phase ( $C_i^{BCC}$ ) [37]:

$$K_i = C_i^{B2} / C_i^{BCC} \quad (1)$$

The partitioning coefficient is calculated to be 0.7, 2.7, 0.5, 2.0 for Fe, Co, Mn, Al, respectively. For  $K_i$  values in excess of 1, the Co exhibits a slightly higher preferential partitioning to the B2 matrix than the Al. Conversely, as indicated by the  $K_i$  values less than unity, somewhat larger segregation of Mn in the BCC phase than that of Fe can be inferred. Meanwhile, volume fractions of B2 and BCC phases can be calculated based on the lever rule for two-phase alloys [37]:

$$C_i^{bulk} = C_i^{B2} \cdot V_{B2} + C_i^{BCC} (1 - V_{B2}), \quad (2)$$

where  $V_{B2}$  is the volume fraction of B2 matrix and  $C_i^{bulk}$  is the overall concentration of  $i$  element in the alloy. The volume fraction of B2 matrix can be rewritten as

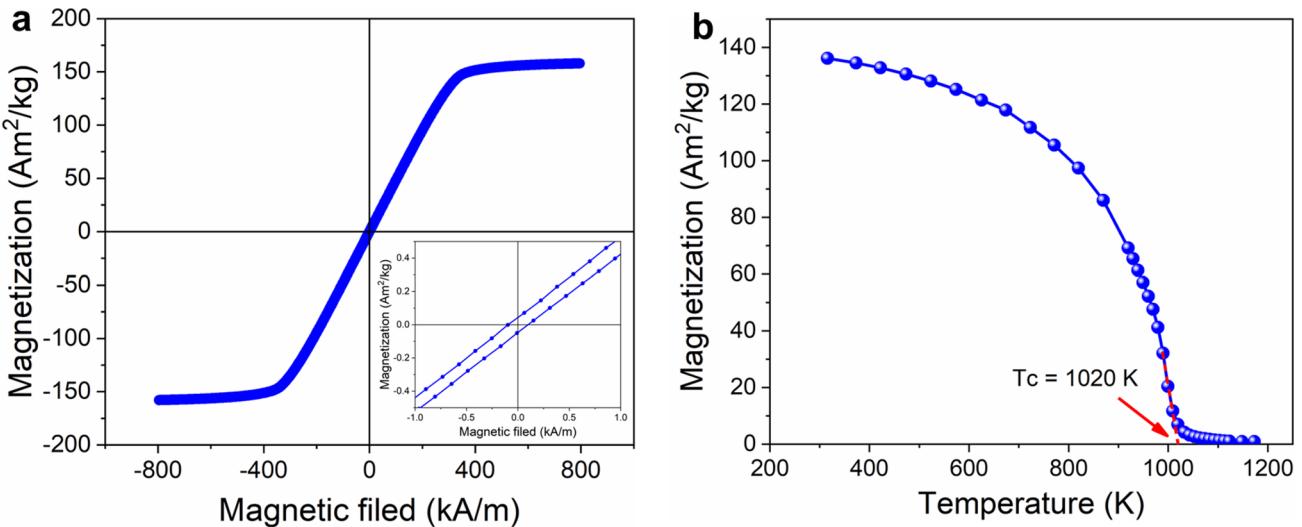
$$V_{B2} = (C_i^{bulk} - C_i^{BCC}) / (C_i^{B2} - C_i^{BCC}). \quad (3)$$

Therefore, the phase volume fractions for B2 matrix and BCC nanoprecipitates are calculated as 89.7% and 10.3%, respectively.

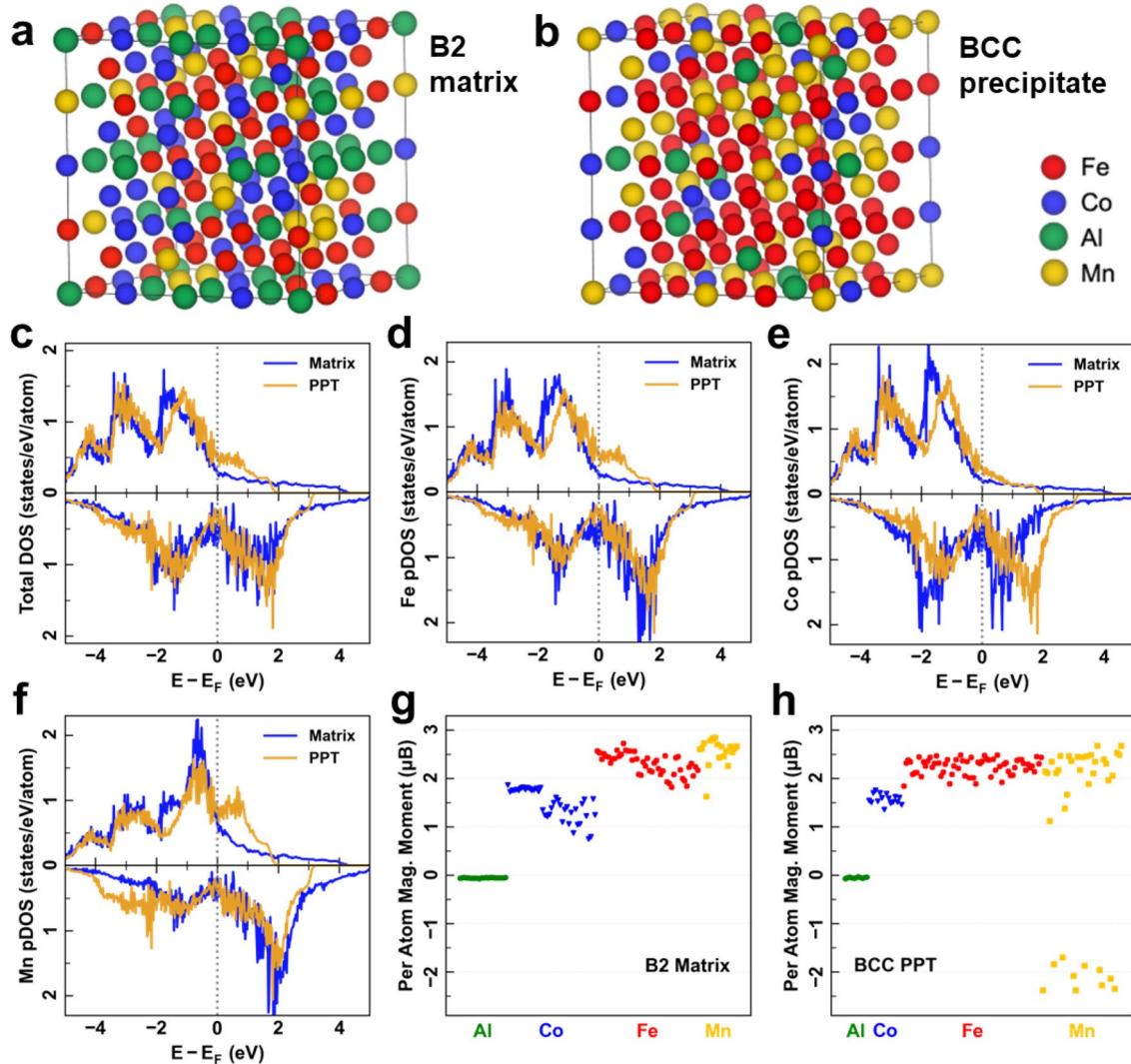
A representative magnetic hysteresis loop for the  $Fe_{40}Co_{30}Mn_{15}Al_{15}$  alloy acquired using the VSM is shown in Fig. 4a. It is readily seen that the MPEA can be easily magnetized to the saturated state and exhibits a low  $H_c$  when

demagnetized. Specifically, an excellent combination of high  $M_s$  of  $157.7 \text{ Am}^2/\text{kg}$  and low  $H_c$  of  $107.8 \text{ A/m}$  indicates its potential as a soft magnetic material ( $H_c < 1000 \text{ A/m}$ ). Interestingly, although the alloy shows a mixture of B2 matrix and BCC precipitates, a low coercivity can still be obtained. It has been shown that the coercivity scales with particle size with a theoretical relationship of  $H_c \propto D_p^6$  when the particles are in nanoscale range [23, 38]. Therefore, these nanoscale precipitates have a relatively small pinning effect on domain wall movement within the material, resulting in the low coercivity. The temperature dependence of  $M_s$  of the alloy is shown in Fig. 4b. As the temperature increases, the  $M_s$  gradually decreases to  $\sim 100 \text{ Am}^2/\text{kg}$  at  $800 \text{ K}$ , followed by a sharp drop to near zero at  $> 1050 \text{ K}$ . The Curie temperature  $T_c$  was determined to be  $\sim 1020 \text{ K}$ , suggesting its potential use at high temperatures. The relatively small change of  $M_s$  at lower temperatures is associated with the fact that the thermal vibration of atoms does not substantially affect the magnetic ordering when the temperature is far below  $T_c$  [15]. Additionally, the alloy exhibits a high electrical resistivity of  $238 \pm 8 \mu\Omega \text{ cm}$ , suggesting a low eddy current loss. Further comparisons of soft magnetic performance with other reported soft magnets will be discussed.

We also performed density functional theory (DFT) calculations to understand the magnetic behavior of the  $Fe_{40}Co_{30}Mn_{15}Al_{15}$  alloy, as shown in Fig. 5. The compositions of the B2 matrix and BCC precipitates measured by APT (Table 1) were used to construct the respective supercells (Fig. 5a, b) during the DFT calculations. The magnetic contributions of each element were analyzed via the total density of states (DOS), partial DOS (pDOS), and elemental magnetic moment. The total DOS of both the B2 matrix and



**Fig. 4** **a** Representative magnetic hysteresis loop of  $Fe_{40}Co_{30}Mn_{15}Al_{15}$  alloy. The inset shows an enlarged view of the loop at low magnetic fields. **b** Temperature dependence of the magnetization of  $Fe_{40}Co_{30}Mn_{15}Al_{15}$  alloy at an applied magnetic field of  $400 \text{ kA/m}$



**Fig. 5** Atomistic configurations of the **a** B2 matrix and **b** BCC precipitate phases. **c** Total, **d** Fe, **e** Co, and **f** Mn density of states (DOS) of B2 and BCC phases. Calculated elemental magnetic moments for the **g** B2 matrix and **h** BCC precipitate phases

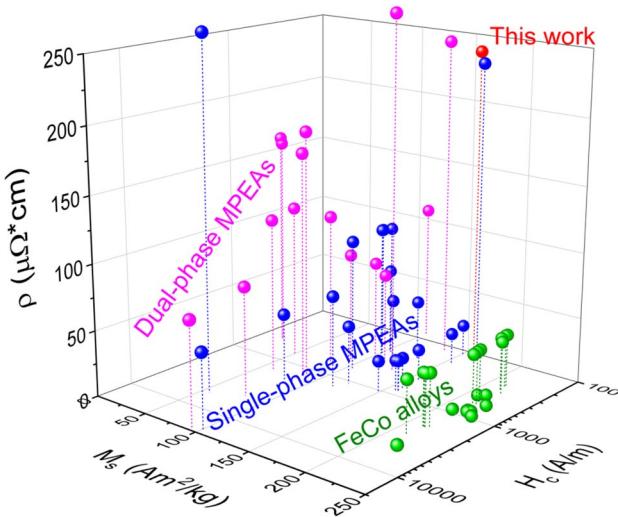
the BCC precipitates exhibit typical ferromagnetic profile (Fig. 5c). They are similar to the pDOS of the two major elements, i.e., Fe (Fig. 5d) and Co (Fig. 5e), which can be reasoned through the rigid band model [39]. The Mn pDOS (Fig. 5f) in the matrix shows smaller difference between the spin-up and spin-down components in comparison with the precipitates, which can be associated with the reduced Al concentration in the BCC precipitates as the presence of Al can reduce the exchange splitting [14, 27]. The pDOS plots are further corroborated by the per-atom magnetic moments shown in Fig. 5g and 5h, where all Fe and Co moments were ferromagnetically coupled for both phases, while the Mn atoms displayed ferromagnetic coupling in the B2 matrix but high variance in the BCC precipitates. Further, it was found that the Mn atoms with negative moments exhibited more local Mn–Mn bonding up to the 2nd nearest neighbors. This

is similar to the relationship between the Mn–Mn distance and the magnetic structure in the NiAs-type Mn compound [40]. According to Slater–Bethe curve [41–43], when the equivalent Mn–Mn distance is lowered due to increased Mn concentration, direct exchange coupling between the Mn pairs is enhanced, inducing the antiferromagnetic coupling because of Mn’s half-filled  $d$  bands.

We also estimated the theoretical  $M_s$  of the material, including both B2 matrix and BCC precipitate phases, via their atomic magnetic moments [27]:

$$M_{s, \text{phase}} = \frac{\mu_{B, \text{supercell}}}{W_{\text{supercell}}}, \quad (4)$$

where  $M_{s, \text{phase}}$  is the theoretical  $M_s$  of each phase,  $\mu_{B, \text{supercell}}$  is the total magnetic moment in either B2 or BCC supercells



**Fig. 6** 3D plot compiling room-temperature  $M_s$ ,  $H_c$ , and  $\rho$  for a variety of single-phase [16–21] and dual-phase [3, 19–23] MPEAs as well as conventional FeCo alloys [23, 44–48]

( $\mu_B = 9.274 \times 10^{-24} \text{ Am}^2$  is the Bohr magneton), and  $W_{\text{supercell}}$  is the total atomic weight of the supercells. The total  $M_{s,\text{total}}$  value of the alloy can be estimated from a rule of mixture:

$$M_{s,\text{total}} = V_{B2}M_{s,B2} + V_{BCC}M_{s,BCC}, \quad (5)$$

where  $V_{B2}$  and  $V_{BCC}$  are the volume fractions of each phase as obtained from the APT analysis. The calculated  $M_s$  for the B2 matrix and the BCC precipitates are  $177.6 \text{ Am}^2/\text{kg}$  and  $169.9 \text{ Am}^2/\text{kg}$ , respectively. Interestingly, both phases show excellent ferromagnetism, i.e., the BCC precipitates do not compromise the magnetization of the material. As a result, the overall magnetization is thus estimated as  $176.8 \text{ Am}^2/\text{kg}$ , which agrees well with the experimentally determined value of  $157.7 \text{ Am}^2/\text{kg}$ . The slight overestimate may result from the fact that the DFT calculations were performed at  $0 \text{ K}$ , whereas the VSM measurements were conducted at room temperature.

To highlight the good combination of soft magnetic properties and electrical resistivity of the  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  MPEA, we compiled its room-temperature  $M_s$ ,  $H_c$ , and  $\rho$  into a 3D plot, in Fig. 6, together with other existing MPEAs, including single-phase and dual-phase MPEAs, and conventional FeCo alloys in literature (summarized in Table 2). It is readily observed that the current alloy (shown as a red sphere) has an excellent combination of relatively high  $M_s$  ( $157.7 \text{ Am}^2/\text{kg}$ ), low  $H_c$  ( $107.8 \text{ A/m}$ ), and high  $\rho$  ( $238 \mu\Omega \cdot \text{cm}$ ), outperforming the most reported MPEAs as well as conventional FeCo alloys. The majority of single-phase MPEAs exhibit relatively low electrical resistivity and most

dual-phase MPEAs display somewhat low saturation magnetization. Two recently developed MPEAs [16, 23] show the most comparable combinations to the currently alloy. The dual-phase B2/BCC  $\text{Al}_{1.5}\text{Co}_4\text{Fe}_2\text{Cr}$  HEA (the pink sphere near the red sphere) shows a higher  $\rho$ , but a lower  $M_s$  and a higher  $H_c$  than for our alloy; and the single-phase B2  $\text{Fe}_{30}\text{Co}_{40}\text{Mn}_{15}\text{Al}_{15}$  MPEA (the blue sphere near the red sphere) shows a slightly higher  $M_s$ , but also a higher  $H_c$  and lower  $\rho$  than the current alloy. It is interesting that similar magnetic properties were obtained for the previous single-phase B2  $\text{Fe}_{30}\text{Co}_{40}\text{Mn}_{15}\text{Al}_{15}$  and the current dual-phase B2/BCC  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloys. Our DFT calculations (Fig. 5) indicate that the Fe/Mn-rich BCC precipitates show good ferromagnetism, i.e., the ferromagnetic BCC precipitates would essentially not impair the magnetization. On the other hand, relatively small pinning effect on domain wall movement leads to low coercivity due to their very fine sizes of nanoprecipitates [23, 38]. Although the  $M_s$  of the current  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  MPEA is not comparable to that of conventional FeCo alloys, its exhibits lower  $H_c$  yet much higher  $\rho$ , allowing lower energy losses from hysteresis and eddy current losses. Furthermore, the new  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  alloy also enables a reduction in the cost in comparison with the conventional FeCo alloys (e.g., commercial FeCo-2V) due to the lower content or replacement of the high-cost elements Co and/or V via substantially alloying with the inexpensive Mn and Al.

## Conclusions

In summary, we have developed a new non-equiautomic  $\text{Fe}_{40}\text{Co}_{30}\text{Mn}_{15}\text{Al}_{15}$  MPEA and investigated its microstructure and soft magnetic properties experimentally and theoretically. The alloy consists of an ordered B2 matrix and nanoscale BCC precipitates with Co and Al elements partitioning to the former phase and Fe and Mn elements partitioning to the latter phase. This alloy unifies excellent soft magnetic properties and electrical resistivity with a high saturation magnetization of  $\sim 158 \text{ Am}^2/\text{kg}$ , a low coercivity of  $\sim 108 \text{ A/m}$ , a high electrical resistivity of  $\sim 238 \mu\Omega \cdot \text{cm}$ , and a high Curie temperature of  $\sim 1020 \text{ K}$ , which outperforms most reported MPEAs and traditional FeCo alloys in the literature. DFT calculations revealed that both B2 matrix and BCC nanoprecipitates are highly ferromagnetic and their overall magnetization agrees well with experimental results. Our current study offers a new alloy design strategy for developing high-performance soft magnetic alloys via ferromagnetic multicomponent B2 matrix and BCC nanoprecipitates.

**Table 2** Alloy composition (at.-%), crystal structures, saturation magnetization ( $M_s$ ), coercivity ( $H_c$ ), and electrical resistivity ( $\rho$ ) of a variety of soft magnetic MPEAs. Conventional FeCo and FeCo–2V alloys are also included for comparison

Alloys	Structure	$M_s$ (Am <sup>2</sup> /kg)	$H_c$ (A/m)	$\rho$ (μΩ cm)	References
FeCo	B2	210–230 <sup>a</sup>	435–4615	1.95	[44–47]
FeCo–2V	B2	212–219 <sup>a</sup>	240–2900	40–46.4	[23, 47, 48]
FeCoNi	FCC	150–160	121–1069	16.7–24	[17, 19–21]
FeCoNi(AlSi) <sub>0.1</sub>	FCC	122.0 <sup>a</sup>	1089	44.4	[21]
FeCoNi(AlSi) <sub>0.2</sub>	FCC	116.7 <sup>a</sup>	1400	69.5	[21]
FeCoNi(AlSi) <sub>0.4</sub>	BCC	102.4 <sup>a</sup>	17,963	57.3	[21]
FeCoNi(AlSi) <sub>0.5</sub>	BCC	82.5 <sup>a</sup>	1937	52.0	[21]
FeCoNi(AlSi) <sub>0.8</sub>	BCC	56.7 <sup>a</sup>	5952	264.0	[21]
FeCoNiAl <sub>0.25</sub>	FCC	130	230.8	46.2	[20]
FeCoNiAl	BCC	101.8	222.8	65	[20]
FeCoNiSi <sub>0.25</sub>	FCC	126	397.9	53	[20]
FeCoNi(MnAl) <sub>0.25</sub>	FCC	101–104	268–629	91–110	[18, 19]
Fe <sub>30</sub> Co <sub>40</sub> Mn <sub>15</sub> Al <sub>15</sub>	B2	162.4	113.6	230	[16]
FeCoNi(AlSi) <sub>0.3</sub>	FCC+BCC	95.0 <sup>a</sup>	19,336	79.7	[21]
FeCoNiAl <sub>0.5</sub>	FCC+BCC	105	358.1	77	[20]
FeCoNiAl <sub>0.75</sub>	FCC+BCC	110	318.3	67.1	[20]
FeCoNiSi <sub>0.5</sub>	FCC+Ni <sub>3</sub> Si	91.5	477.5	84	[20]
FeCoNiSi <sub>0.75</sub>	FCC+Ni <sub>3</sub> Si	81	4535.9	83	[20]
FeCoNi(MnAl) <sub>0.5</sub>	FCC+BCC	52–89	730–1565	118	[19]
FeCoNi(MnAl) <sub>0.75</sub>	BCC+FCC	129.6	445	271	[19]
FeCoNiCrAl	BCC+B2	20–89	467–565	160–187	[22]
Al <sub>1.5</sub> Co <sub>4</sub> Fe <sub>2</sub> Cr	B2+BCC	135.3	127.3	244	[23]
FeCo–Ni–Ta–Al	FCC+L <sub>1</sub> <sub>2</sub>	100	78	103	[3]
Fe <sub>40</sub> Co <sub>30</sub> Mn <sub>15</sub> Al <sub>15</sub>	B2+BCC	157.7	107.8	238	This work

<sup>a</sup>The units for  $M_s$  for conventional FeCo-based alloys and FeCoNi(AlSi)<sub>x</sub> MPEAs were converted from Tesla via equation  $B_s = 4\pi M_s \rho_m / 10^4$ , in which rule of mixture were used for density ( $\rho_m$ ) estimation for FeCoNi(AlSi)<sub>x</sub> MPEAs without available density data in the literature

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**Data Availability** The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

## Declarations

**Conflict of interest** The authors declare no conflict of interest.

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