Auto-scoring Student Responses with Images in Mathematics

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ABSTRACT

Teachers often rely on the use of a range of open-ended problems to assess students' understanding of mathematical concepts. Beyond traditional conceptions of student openended work, commonly in the form of textual short-answer or essay responses, the use of figures, tables, number lines, graphs, and pictographs are other examples of open-ended work common in mathematics. While recent developments in areas of natural language processing and machine learning have led to automated methods to score student open-ended work, these methods have largely been limited to textual answers. Several computer-based learning systems allow students to take pictures of hand-written work and include such images within their answers to open-ended questions. With that, however, there are few-to-no existing solutions that support the auto-scoring of student hand-written or drawn answers to questions. In this work, we build upon an existing method for auto-scoring textual student answers and explore the use of OpenAI/CLIP, a deep learning embedding method designed to represent both images and text, as well as Optical Character Recognition (OCR) to improve model performance. We evaluate the performance of our method on a dataset of student open-responses that contains both text- and image-based responses, and find a reduction of model error in the presence of images when controlling for other answer-level features.

Keywords

Auto-scoring, Open-ended responses, Image responses, Online Learning Platform

1. INTRODUCTION

The blending of educational technologies with machine learning and statistical modeling has led to the emergence of tools designed to augment instruction. While some such tools are designed to automate certain tasks for the teacher (e.g. [3, 17, 2]), others attempt to improve the efficiency with which teachers are able to assess student work and write directed

feedback to guide learning.

In the context of mathematics education, teachers utilize a range of question formats to assess students' understanding of covered topics. Prior work has described these question types in terms of "close-ended" and "open-ended" problems, distinguishing various types of problems by the difficulty with which answers to such questions may be automatically assessed by a simple matching algorithm. Multiple choice or fill-in-the-blank problems, as examples of close-ended problems, often allow for a small number of acceptable "correct" answers (i.e. in most cases, there is a single answer considered as correct). Although prior works have demonstrated the utility of these types of answers for measuring student knowledge (e.g. the extensive work on knowledge tracing [9, 25]), teachers often rely on the use of open-ended problems to gain deeper insights into the processes and strategies employed by students to solve such problems, as well as their ability to articulate their approach using proper mathematical terminologies. Short answer and essay question types are common in this regard, often with prompts such as "explain your reasoning", but other open-ended formats are also common in the domain of mathematics.

For mathematics, teachers often rely on the use of visual representations in conveying mathematical concepts. The use of diagrams, number lines, graphs, tables, and sometimes even pictographs are commonly used to portray numerical and algebraic relationships. Just as these are used for instruction, students are also commonly asked to generate these types of visual representations to demonstrate their understanding. While open-ended work has typically referred to the use of text and natural language within prior research (e.g. [13, 36, 4]), the definition extends to drawings and similar artifacts produced by students. Tools such as GeoGebra[18] and Desmos[12] are examples of computer-based applications that allow students to interact with graphs and algebraic expressions. While tools like these exist, many teachers still prefer to use more traditional technologies, often in the form of paper and pencil or other physical media (e.g. blocks) in conjunction with computer-based technologies; some systems encourage this blending of media by allowing students to take pictures of their work and upload them as responses to open-ended problems.

This paper builds on prior work which focused on the development of an automated scoring tool for student answers to open response problems in mathematics [4]. BLINDED AU-

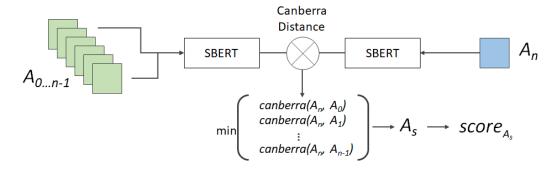


Figure 1: Simplified representation of the SBERT-Canberra method to generate a predicted score by identifying the most similar historic response to a given new student answer using Canberra distance within an embedding space.

THORS, reported on how many student responded to openresponse problems with images of their work (in the form of written mathematical equations and expressions as well as drawings of graphs, number lines, and other visual representations), where as several others preferred to respond with a combinations of an image of their work combined with a typed textual explanations within a single student responses (e.g. the student draws a graph, uploads the image and then types a description of their thought process with the image of the graph). These cases were, unsurprisingly, found to contribute significantly to the model error as the presence of images in student responses were not previously accounted for within the developed methods. This work seeks to take initial steps toward understanding how recent advancements in areas of deep learning-based image and text embedding methods may help to address these challenges.

Specifically, this paper addresses the following research questions:

- 1. Does the use of pre-trained deep learning image and text embedding methods lead to improved performance in the context of previously-developed open response scoring models?
- 2. Are there differences in terms of the resulting model performance when comparing across different types of image-supporting embedding methods?
- 3. Does the incorporation of image-supporting embedding methods reduce the correlation between the presence of images in student responses and modeling error when accounting for other answer-level covariates?

2. RELATED WORKS

2.1 Automated Scoring Models

With the development of online learning platforms, there has been a growing body of research in the development of automated methods of assessment for analyzing and providing immediate feedback on students' work. These developments have prevailed in multiple domains of science [23, 7], programming[24, 26, 35], writing[21, 1, 8, 29, 38], mathematics[22, 13, 4] and college level courses[11]. In the domain of mathematics, auto-scoring have been developed for closedended problems with single or limited correct answers(e.g.,

multiple-choice question, fill-in-the-blank, check all that apply) [3, 17] to more open-ended problems with multiple possible solutions (eg. short answer, long answer, Explain in plain english.) [22, 13, 14, 4, 36, 37, 5, 32]. Some of these works support pure mathematical content [22], while others support combination of both mathematical and textual answers[13, 4, 5, 37]. However, most of these auto-scoring methods in mathematical domains are limited to either text or mathematical content, and a very few have started focusing on automating responses for image-based responses.

2.2 Methods for Image Analysis and Representation

Optical Character Recognition (OCR) is an extensive field of research in image processing, that explores the recognition and conversion of handwritten textual information to machine-encoded text, such that this information could be further processed and analyzed. Studies such as Shaikh et al. (2019) [31], utilizes OCR-based methods, combined with Convolutional Neural Networks (CNN) in auto-scoring structured handwritten answer sheets of multiple choice questions. Other studies like [34] propose an automated scoring system for handwritten student essays in reading comprehension tests, utilizing handwriting recognition and machine learning-based automated essay scoring methods. Khuong et. al [20] in their work proposes clustering handwritten mathematical answers scanned from paper-based exams, to improve the efficiency of human raters in scoring these answer sheets. Another study from Gold et. al [15], in their attempt to auto-score handwritten answers, presents the challenges of using handwriting in intelligent tutoring systems. Further, they present, how the lack of better recognition systems in these cases leads to poor scoring performances.

Recent advancements in the areas of deep learning and computer vision have led to the development of large-scale models of image representation and classification. ImageNet [10] is a large-scale image dataset widely used for training and evaluating computer vision models. Trained over 14 million images belonging to more than 22,000 different classes, ImageNet is considered a benchmark for image classification tasks. CLIP (Contrastive Language-Image Pretraining) [27] is a recently introduced image classification model based on transformer architecture, commonly used in natural language processing tasks. This method is able to encode both natural languages (text) and images in the same

vector space by using a multi-modal pre-training approach. The proposed methods in this work utilizes the CLIP model to represent image and text-based answers.

2.3 The SBERT-Canberra Model

This work utilizes an auto-scoring method developed through several prior works [4, 6], referred to as the SBERT-Canberra model. As illustrated in Figure 1, the method produces a predicted score, $score_{A_s}$, for a new student answer, A_n , by leveraging the single-most-similar historic student answer, A_s . The method utilizes Sentence-BERT [28] to first generate a 768-valued feature vector for both A_n as well as all teacher-scored historic student answers, $A_{0...n-1}$ before then making a full pairwise comparison of A_n to these historic answers using Canberra distance [19]; Canberra distance is a rank-order-based distance measure that was found to more closely align to how teachers identify similarity in comparison to other distance measures such as Euclidean and Cosine Similarity [6]. From this, A_s is identified and its teachergiven score is used as the prediction for A_n ; the method, therefore, adopts a variation of K-Nearest-Neighbors and has exhibited notable performance when evaluated compared to a range of baseline models [4, 13], despite its simplicity.

Through prior work, several weaknesses of the auto-scoring method have also been identified by means of a multi-level regression-based error analysis [4]. From this, four primary areas of weakness were identified: 1) model error varied greatly from problem to problem, 2) there seemed to be variation in teacher grading, 3) the presence of numbers, expressions, and equations in textual explanations correlated with higher error, and 4) the presence of images in student answers correlated with higher error. Subsequent follow-up works have explored three out of these four weaknesses, examining how answers from similar problems can be leveraged to improve predictive power for problems with smaller sample sizes [30], explore the contextual factors that contribute to variance in teacher grading practices [16], and leverage the most-frequent mathematic terms, numbers, and expressions to reduce modeling error [5]. Following these works, this paper seeks to address the fourth weakness by exploring potential methods of representing both textual and image data within similar embedding spaces.

3. DATASET

In this study, we utilize a dataset of student open-ended answers in mathematics from the prior studies [4], to compare directly with the prior works. This dataset consists of 150,477 students' answers to 2,076 different open-ended mathematics problems and scores given by 970 different teachers to these responses. The scores given by teachers to these responses are on an ordinal 5-point scale ranging from 0 to 4. The student responses given to these math-based questions are typically seen as a combination of textual responses (typed directly into the learning platform), mathematical expressions and equations, and images uploaded as a part of their work. The current dataset includes 3712 image responses in total to 311 different math problems. Some example image responses given by students are presented in Figure 2. As seen from these examples, the image-based student answers are of different types – some are handwritten, whereas others are digitally drawn images. In addition to this, these images can include handwritten text, diagrams,

and graphs on a piece of paper. We can see lots of variations in these responses, in both text and image format.

4. METHODOLOGY

Utilizing the dataset from [4] and a similar model design to auto-scoring student open-response answers, we propose an extension to this prior work to support image-based responses. Similar to [4], we train a separate model per problem and perform a 10-fold cross-validation for training. For the problems without any training data, a default model based on word counts, trained across all problem data is used similarly to the prior works. In this paper, we explore and compare three different methods which we describe in detail in the following sections.

4.1 CLIP-Text Method

As stated earlier, the prior works [4], is a similarity ranking-based method, that first converts each student's answers to a 768-valued vector representation using Sentence-BERT[28], and compares answers using this vector representation and Canberra distance[19]. In our current method, we use a similar model structure with a different embedding method. This method is based on CLIP (Contrastive Language–Image Pre-training)[27] for encoding textual responses.

In the first method which we call the 'CLIP-Text' Method, we perform a text comparison similar to the prior SBERT-Canberra model, without accounting for image-based responses. Using the CLIP[27] model, we first embed the textual responses ignoring all the image responses. For any new answer in the test dataset, we compare them with the training set, by first generating a vector representation, and then comparing the vectors using Canberra distance to find the most similar pair of text responses. Using the most similar text, we utilize the score given by teachers to this similar response, in suggesting a score for the new response. In the CLIP-Text Method, we ignore the images, as we want to see how well the CLIP model does with just the text responses to directly compare it to the prior method. For any empty student responses, the model assigns a score of '0', and also for responses with no textual answers (images are discarded in this method, so if a response contains only an image, it is assigned a score of 0).

4.2 CLIP-Image Method

The second method which we call 'CLIP-Image' method, addresses both images and text in student responses. This method is similar to the 'CLIP-Text' method, with the addition of image embeddings in comparing the similarity of responses. The CLIP model uses separate text and image encoders and allows embedding text and images into the same vector space. With the CLIP model, we first encode textual and image responses into a vector representation. If a student response contains both text and images, the text part is discarded and just the images are encoded in this method. Once all the responses in the training data are encoded, for a new student answer (with either image or text-based response), its corresponding encoding is calculated and compared to the embeddings in the training data, and the most similar response is selected based on the shortest Canberra distance between the new response and the responses in the training set.

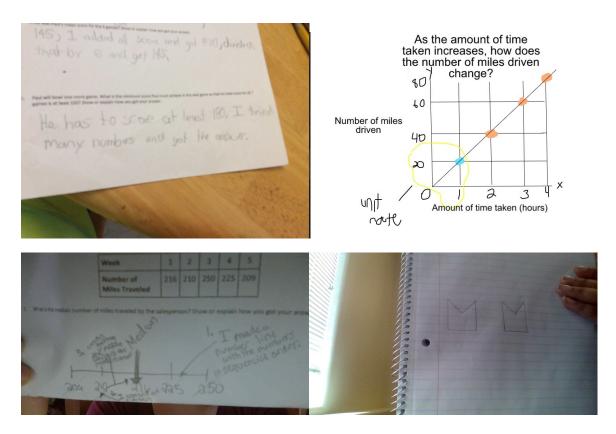


Figure 2: Examples of image-based responses from students given in response to Open-ended math problems

4.3 CLIP-OCR Method

The third method is called 'CLIP-OCR' method which is based on state-of-the-art Optical Character Recognition (OCR). This method uses the Tesseract engine[33] from Google for text extraction. Tesseract is an open-source OCR engine, that extracts both printed and written text from images. Similar to the 'CLIP-Text', this method, then encodes the original textual responses, and also the extracted text from images (without completely ignoring the image responses). The text information from the responses is then encoded using the CLIP model, and finally, any new response is compared to the historic responses in the training data using the encodings and Canberra distance, to get a score prediction.

5. RESULTS

To compare the current approaches directly to the prior methods from [4], we utilize similar evaluation methods, using a Rasch model. The use of the Rasch model allows a fairer comparison that accounts for factors external to the observed student response, such as student ability and problem difficulty. We evaluate the methods using three different metrics – AUC score, Root Mean Squared Error (RMSE), and multi-class Cohen's Kappa. The AUC score here is calculated as an average AUC over each score category and Root Mean Squared Error(RMSE) is calculated using the model estimates as a continuous-valued integer scale. The results of three methods as compared to the prior works [4] are presented in Table 1.

The result suggests that the CLIP-Text that uses the sentence embeddings from OpenAI CLIP model [27] has an

AUC score of 0.852, RMSE error of 0.594, and Kappa of 0.469. Though the model doesn't outperform the prior SBERT-Canberra method [4] of auto-scoring, the difference in each of the scores is very small. The next method CLIP-Image, which compares both sentence and image embeddings using the OpenAI CLIP model, outperforms the CLIP-Text method across all three evaluation metrics used (though the difference in these scores is minimal). This method has an AUC score of 0.854, RMSE error of 0.587, and Kappa of 0.469. The next method CLIP-OCR, based on text extraction from images using OCR methods, has a similar performance to the CLIP-Image model. Though the newly introduced methods do not outperform the prior text-based method, the introduction of auto-scoring image responses is something novel that this work explores. And we can see improved performance with the addressing content from imageresponse in the CLIP-Image and CLIP-OCR model, than solely using text-based responses in the CLIP-Text model.

6. ERROR ANALYSIS

As previously introduced, prior work conducted an error analysis to understand the limitations of the SBERT-Canberra method [4]. This error analysis involved the calculation of several student answer-level features and using a linear regression analysis with the absolute prediction error (absolute difference between the teacher-provided score and the prediction from the model) as the dependent variable. This analysis reported that the largest amount of error in the SBERT-Canberra model was correlated with the presence of mathematical terms and equations and the presence of images in the answer text.

Table 1: Model Performance compared to the auto-scoring methods developed in the prior works [4]

Model	AUC	RMSE	Kappa
Current Paper			
$Rasch^* + CLIP\text{-}Text$	0.852	0.594	0.469
$Rasch^* + CLIP-Image$	0.854	0.587	0.471
$Rasch^* + CLIP-OCR$	0.854	0.588	0.471
Prior works[4]			
Baseline Rasch	0.827	0.709	0.370
$Rasch^* + Random Forest$	0.850	0.615	0.430
$Rasch^* + SBERT-Canberra$	0.856	0.577	0.476

^{*}These rasch models also included the number of words.

Table 2: The resulting model coefficients for the linear regression model of error for the auto-scoring method, conducted as a part of the error analysis similar to the prior method from BLINDED AUTHORS [4].

	CLIP-Text		CLIP	CLIP-Image		CLIP-OCR			
	В	Std. Error	В	Std. Error	В	Std. Error			
Intercept	0.356***	0.006	0.324***	0.006	0.324***	0.006			
Length of Answer	0.002***	0.000	0.002***	0.000	0.002***	0.000			
Avg. Word Length	0.014***	0.001	0.016***	0.001	0.016***	0.001			
Numbers Count	0.0001***	0.000	0.0001***	0.000	0.0001***	0.000			
Operators Count	-0.001**	0.000	-0.001***	0.000	-0.001***	0.000			
Equation Percent	0.161***	0.009	0.211***	0.009	0.208***	0.009			
Presence of Images	2.432***	0.019	0.496***	0.018	0.585***	0.018			

^{*}p <0.05 **p<0.01 ***p<0.001;

In this paper, we propose a method to auto-score responses in presence of both text and images. Although the proposed methods do not outperform the previous method on autoscoring strictly text-based answers, we hypothesize that this could be a result of using a different method of embedding text; there may be an inherent trade-off where performance is reduced for textual responses but results in improved performance where there are images (averaging out to little-tono overall improvement). Also, from the results, we have seen improvements in the performance of the 'CLIP-Image' and 'CLIP-OCR' methods (that addresses the content of the image when auto-scoring) over the 'CLIP-Text' method (which is just based on text responses). To further study the factors that contribute to the error of these models, and to verify whether introducing image components in the textbased models actually improve the performance in presence of images, we replicate the error analysis from BLINDED AUTHORS [4]. Using features from student answers including 'Length of answer', 'Average word length', 'Total numbers count', 'Total operators', 'Percentage of equations' and 'Presence of images' as the dependent variables and Absolute model error as the independent variable, we perform three different linear regression analyses corresponding to the three proposed methods for auto-scoring.

6.1 Results of Error Analysis

The results of the error analysis are presented in Table 2. All the features from student answers are statistically significant in predicting the modeling error in all three proposed methods. However, most of these features have low coefficient values, suggesting a relatively small effect, with the

except of 'Equation Percent' and 'Presence of Images' which are positively correlated with the model error in all three cases. This is similar to the results of error analysis from prior study [4]. For the 'CLIP-Text' model, the coefficient for the presence of images is 2.432, suggesting that the presence of images in answers attributes to a notable amount of error in the model prediction, even when considering the difference in feature scaling. However, the coefficient value decreases to 0.496 in the 'CLIP-Image' method, and 0.585 in the 'CLIP-OCR' method. This decrease suggests that the introducing image component to the 'CLIP-Text' method using embedding and OCR-based text extraction actually helped the model improve in presence of images. It is also important to note that this work does not explicitly address mathematical terms (including numbers, expressions and equations) in the score prediction as has been suggested by other work [5]. Also, we see an increase in the coefficient values for equation percentage from 'CLIP-Text' to 'CLIP-Image' and 'CLIP-OCR'. For the 'CLIP-Text' method, we discard any images from the answer text, whereas for the other two methods, if there is a response that contains both image and text we discard the text from these responses and just consider the images. The change in the coefficient values for equation percent could be a result of this quality.

7. LIMITATIONS AND FUTURE WORKS

This paper represents an initial step toward improving stateof-the-art methods for auto-scoring student responses to mathematical problems in presence of images. This is a preliminary work conducted towards exploring the feasibility and challenges in auto-scoring student image responses in the mathematical domain. Thus, the methods presented have several limitations and challenges that can be addressed with future work.

The proposed methods in this work use CLIP model [27] trained on a large variety of datasets of images and natural language available over the internet. While this method shows promising results in recognizing a range of common objects, the pre-trained model may not have been exposed to the dataset of student hand-written or hand-drawn mathematics; the model was trained for application in very broad domains to recognize objects and is not optimized for identifying similar responses on paper. It has also been found that while the CLIP model learns a capable OCR system, it exhibits low accuracy in the case of handwritten digits in the widely-used MNIST dataset [27]. Further, fine-tuning this model on a mathematical dataset could lead to better model performance.

It is also important to note that the OCR method is based on the Tesseract [33] engine; this is known to be sensitive to poor quality images, complex backgrounds, variation in the handwriting styles and ambiguity in the characters [33]. All of these are the common qualities of the images found in our dataset. While this method supports digital images (that are screenshots of work done on a computer), the method has low accuracy in extracting textual information from handwritten answers. Thus, exploring better OCR methods that support both handwritten and digital textual answers would better improve these auto-scoring methods for images. Further, both of the proposed methods that support images, inherently discard the additional text if present in the response. These texts may present additional supporting information to the image-based answers, so it is important to explore how to address this when evaluating these responses.

Apart from the limitation mentioned above, the process of analyzing and processing these image-based answers in itself is a challenging task, as we can see a lot of variation in these images of student-provided answers. Figure 2, presents some examples of image-based student answers. The student work in these images are not always clearly presented and structured - some handwriting is hard to read, the images sometimes are of low resolution and are blurry, the use of pencils makes the writing feint and hard to read, and lacks consistent formatting. Due to the freedom provided to students by the use of paper and pencil to draw out their solution, the resulting answer is not always structured in the same way from student to student. Future work could help address some of these challenges by implementing a more rigorous cleaning and preprocessing procedure prior to applying any image representation models. Cropping images to focus on the prominent aspects of student work, rotating images to improve the consistency of orientation, and even color correction can help improve the clarity of the work.

In all of this work, there are also several ethical concerns that should be considered in developing and applying these various methods. Images may contain Personally Identifiable Information(PII) such as students' names, faces, skin color, etc. which exposes a potential risk of biases or disparate performance in regard to the machine learning models. Future works could mitigate some of these challenges by utilizing

some of the pre-processing methods described above, but also emphasizes the importance of evaluating these scoring models for potential biases or unfairness in their predictions.

8. CONCLUSION

In this study, we have presented preliminary work towards developing an auto-scoring method for student response in mathematics that includes images. By building upon the prior research in auto-scoring text-based mathematical answers, we have proposed methods for representing and scoring image-based responses. While our proposed methods did not outperform the current state-of-the-art approach for auto-scoring, they showed comparable accuracy across all three evaluation metrics used. The results of the conducted error analysis further indicate that using pre-existing methods of text and image embeddings can enhance the performance of the auto-scoring models in presence of images.

Our findings from this study points toward new directions for research in the area of analyzing and processing imagebased student responses in mathematics.

9. ACKNOWLEDGMENTS

Blinded for submission

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