

Salt Effects on the Phase Behavior and Cocrystallization Kinetics of POCB–Water Mixtures

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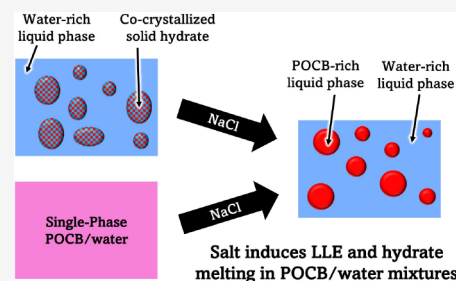


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ABSTRACT: Mixtures of water with polyoxacyclobutane (POCB) have a unique phase diagram which combines liquid–liquid equilibrium (LLE) at high temperatures and cocrystallization of a POCB-hydrate at low temperatures. Such cocrystal hydrate formation is extremely rare among polymers. We report on the effects of adding NaCl salt on the phase behavior of POCB–water mixtures and the kinetics of hydrate crystallization from such mixtures. Salt loadings of less than 0.1 wt % were found to greatly expand the LLE region. Salt loadings of ~10 wt % were found to significantly decrease the melting temperature of the hydrate below its ~37 °C value under salt-free conditions. The hydrate was found to be remarkably tolerant of salt and persists at room temperature even when equilibrated with salt-saturated water. Salt was found to slow down hydrate crystallization, and the degree of slowing was greater than that expected from the salt-induced decrease in undercooling due to melting point depression.



INTRODUCTION

Polyoxacyclobutane (POCB) is a polymer in the polyox-yalkylene series with the structure— $[(CH_2)_3O-]_n$. Mixtures of water with POCB show unusual phase behavior. At room temperature and atmospheric pressure, POCB has a remarkable ability to cocrystallize with water to form a hydrate.¹ However, above the melting temperature of the hydrate, one obtains a mixture in liquid–liquid equilibrium (LLE) between a POCB- and a water-rich phase. Such demixing indicates that—despite its apparent affinity for water in the crystalline hydrate state—POCB is hydrophobic.² Indeed, all other polyoxyalkylenes (except poly(ethylene oxide)) are also hydrophobic with very low solubility in water. This combination of properties makes POCB unique: to our knowledge, it is one of only two³ (possibly three⁴) polymers that can form a crystalline hydrate, and the only one that also phase separates from water under molten conditions. In fact, to our knowledge, no other polymer is able to cocrystallize with a small molecule with which it is immiscible in the liquid state.⁵

Previously, we conducted studies of the phase behavior and hydrate crystallization kinetics of POCB–water mixtures.^{6,7} Briefly, at a molecular weight of 650 g/mol, the phase diagram is a union of hydrate melting behavior and LLE behavior² (Figure 1, discussed in detail in the Results and Discussion section under liquid–liquid equilibrium). Accordingly, mixtures with low water content can be cooled from a homogeneous liquid state to form a hydrate, and this crystallization process resembles homopolymer crystallization.⁶ In contrast, mixtures with a high water content are in LLE prior to crystallization. Thus, hydrate formation involves interfacial mass transport and is, therefore, sensitive to mixing conditions.⁷

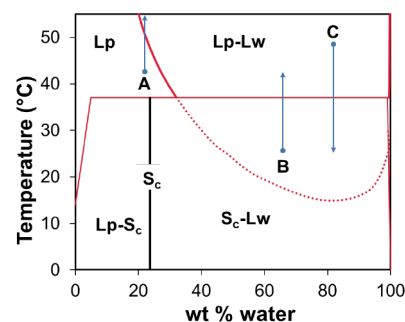


Figure 1. Phase diagram for POCB 650 and water without salt.² The solid black line labeled Sc indicates the composition of the solid hydrate. The solid red curve indicates the liquid–liquid coexistence between the polymer-rich (Lp) and water-rich (Lw) phases, whereas the horizontal red line is the melting point of the hydrate. The dotted red line indicates a metastable portion of the liquid–liquid coexistence curve. The blue arrows indicate the trajectories used for the measurements of interest in this study. (A) Heating a single-phase mixture to locate the cloud point (liquid–liquid equilibrium section). (B) Heating a hydrate–liquid mixture to measure the melting point (melting point section). (C) Cooling a two-phase mixture in LLE to measure the crystallization kinetics (crystallization kinetics section). This diagram is not strictly correct, as discussed in the liquid–liquid equilibria section.

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POCB-hydrate formation has many potential applications including improving the nonvolatile memory storage capabilities of carbon nanotube devices,⁸ drug delivery or other biomedical applications,^{9,10} water purification,¹¹ materials with high proton and ion conductivity for membrane applications,^{12,13} and stimuli-responsive materials.¹⁴ Ionic solutes are expected to be present in virtually all of these applications. The effect of ionic solutes on the phase behavior and hydrate crystallization kinetics of PO CB/water mixtures is unknown and the subject of this paper. Salt is known to affect the solubility of polymers through the Hofmeister effect.¹⁵ Thus, we anticipate that salt promotes the immiscibility of PO CB and water, and indeed this was noted previously¹⁶ as discussed further below. Additionally, any solute can reduce the melting point of a crystal. Thus, salt is expected to affect the phase boundaries of both the LLE and solid–liquid equilibrium in the PO CB–water mixtures. These changes in the phase behavior are also likely to affect the crystallization kinetics. For example, melting point depression of the hydrate would reduce the undercooling (at any specified crystallization temperature), and hence, the addition of salt would also slow crystallization. The goal of this paper is to measure these effects quantitatively. We are aware of only one previous publication of salt effects on PO CB/water mixtures.¹⁶ Lee et al. showed that salt-free PO CB/water mixtures that were transparent, homogeneous mixtures at room temperature reached a cloud point (i.e., demixed) upon heating, and further that the cloud point temperature reduced upon the addition of NaCl. This research was conducted at a PO CB molecular weight of 250 g/mol¹⁶ and did not mention hydrate formation at all. Indeed, our experiments with a similarly low molecular weight show that the hydrate does not form readily. The research in this paper will focus on the effects of NaCl as the salt but will use a MW of 650 g/mol of PO CB at which hydrate crystallization and LLE are coupled with each other. It is this coupling that makes this system unique, and there have been no previous studies of salt effects on any similar polymer–water mixture. The salt-induced demixing seen in PO CB/water mixtures previously¹⁶ and in this paper is common across a variety of water-soluble polymers, wherein the solubility of the polymer in water reduces with increasing salt content. These include polymers of the polyoxyalkene series, such as short chain polyoxymethylene (POM), poly(ethylene oxide) (PEO), poly(propylene oxide) (PPO), and PO CB, as well as other polymers such as polyvinylpyrrolidone (PVP), poly(*N*-isopropylacrylamide) (PNIPAM), or poly(2-oxazoline) (POX).^{17–24} Similar salt effects are also seen in other aqueous nonionic polymer mixtures such as dextran–polyvinylpyrrolidone, dextran–poly(vinyl alcohol), dextran–ficoll, and dextran–PEG.²⁵ These aqueous systems have been known since the late 1800s and have been studied for their use in biological separations since Albertsson’s group pioneered the practice in the 1950s.^{15,26} In contrast to the well-established literature on salt effects on LLE in water–polymer mixtures, we are unaware of any studies on the effects of salt on crystallization of polymer hydrates. There are, however, limited studies of salt effects on homopolymer crystallization in the absence of water. Salt can significantly slow down the kinetics of crystallization,^{27–29} which is at least partially attributed to the reduction in the equilibrium melting temperature of the homopolymer, and thereby a reduction of undercooling. Any reduction beyond the decrease in undercooling may be attributable to more

complex effects such as change in surface energy at the crystal–amorphous interface or transport limitations to crystallization. Incidentally, outside the polymer science literature, salt effects on gas hydrates or other small-molecule clathrate hydrates are well studied. Salt is known to reduce the melting temperature of the hydrate, as well as slow down crystallization.³⁰ However, these clathrate hydrates are very different: they have a water-cage structure (vs the intercalated structure of PO CB-hydrate); the water content of gas hydrates is far higher than in PO CB-hydrate; and the growth mechanism and habit of gas hydrates are entirely distinct from those for PO CB hydrate.

RESULTS AND DISCUSSION

The results section is organized into two parts. The Salt Effects on Phase Behavior section describes the effects of salt on the phase diagram, both on how salt affects LLE (as judged by cloud point measurements, “Liquid–Liquid Equilibria” section), and the melting temperature of the hydrate. In both of these cases, we report changes in phase behavior at a fixed polymer fraction while varying the salt content and fixed salt content while varying the polymer fraction. The Melting Point of the hydrate section describes the effect of salt on the kinetics of hydrate crystallization. Details of the experimental methods and data analysis are given at the end of the paper.

Salt Effects on Phase Behavior. *Liquid–Liquid Equilibria.* As shown in Figure 1, at the molecular weight of 650 g/mol, in the absence of salt, the LLE behavior had the following characteristics. Above 37 °C (the melting temperature of the hydrate), the mixtures are in LLE between water-rich and PO CB-rich phases. The miscibility gap (i.e., the difference between the compositions of the water-rich and the PO CB-rich phases) widens at higher temperatures, suggesting that the LLE curve has a lower-consolute solution temperature (LCST). Below 37 °C, while mixtures may remain in LLE for short periods, the hydrate forms eventually. This portion of the LLE curve is metastable, and we were not able to quantify it fully.

It must be noted that Figure 1 is schematic, and hence, not strictly correct. First, at very low polymer (or very low water) content, there must be a small region of melting point depression of ice (or of pure solid PO CB). These regions could not be explored experimentally since the corresponding polymer or water contents are too low. Second, the hydrate melting points did not show measurable changes with composition, and hence, the hydrate melting line is shown to be horizontal. While this is correct for the three-phase (Lp–Lc–Sc) coexistence region, it may not be true for the Lp–Sc coexistence since the hydrate melting point must be depressed for compositions near the crystal composition (23.6 wt % water). Evidently, this melting point depression is too small to be measured in our experiment. Third, at low water content, crystallization takes a long time and thermodynamic equilibrium may not be maintained. Nevertheless, the phase diagram in Figure 1 is consistent with our experiments and suitable for guiding this paper.

Turning now to the effects of salt, a first set of experiments was conducted at fixed water content (18 wt %) to gauge the amount of salt needed to induce a noticeable depression in the cloud point. Figure 2A shows the cloud point for samples with 0.0 to 0.1 wt % salt. The cloud point is found to reduce from around 67 °C for the salt-free mixture to around 36 °C at 0.1% salt. Above 0.1% salt, the cloud points are below the melting

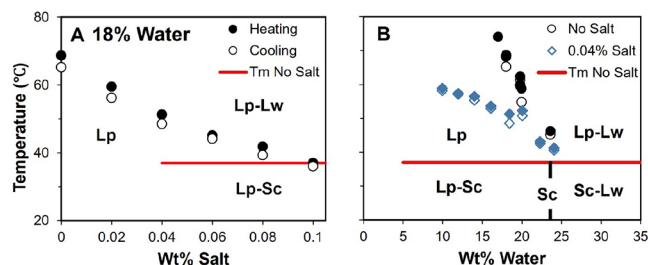


Figure 2. Cloud points for POCB/water/salt mixtures. (A) Cloud points for samples with 18% water vs salt content. Below these cloud points, the mixtures are single-phase liquids, whereas two liquid phases (Lp and Lw) exist above the cloud points. (B) Cloud points for samples without salt and with 0.04% salt at various water contents. Samples are single-phase below the black circles for the salt-free samples and below the blue diamonds at 0.04% salt. The vertical black line labeled Sc indicates the composition of the POCB–water hydrate. In both graphs, the open symbols represent cloud points measured during cooling, and the closed symbols represent cloud points measured during heating. In both graphs, the solid red line is the melting point of the hydrate, which is nearly independent of salt content (see text) and water content.² In part B, the red line does not extend below 5% water because slow crystallization makes it difficult to study hydrate melting. A single pair of heating–cooling points is shown in each graph. Yet, the reproducibility of two independently prepared samples is better than the difference between the heating–cooling pair shown.

polymer reduces steeply, thus, making LLE more favorable. 209 Therefore, samples with lower water content show a larger 210 magnitude of cloud point depression in Figure 2B. 211

Finally, a complete description of LLE also requires 212 examination of the partitioning of the salt into the two 213 coexisting phases. We presume that salt would preferentially 214 partition into the water-rich phase, with very little being 215 present in the POCB-rich phase. This was verified in a single 216 experiment (see ESI), which establishes that the POCB-rich 217 phase can dissolve at most 0.01% salt at 40 °C, even when the 218 aqueous phase is saturated saltwater. When the aqueous phase 219 is much more diluted, e.g., as in Figure 2, we presume that the 220 POCB-rich phase has even lower amounts of salt. 221

Melting Point. Preliminary experiments showed that the 222 mixtures from the previous section (with up to 0.1% salt) 223 induced negligible melting point depression; several percent 224 salts were needed to reduce the hydrate melting point 225 measurably. Accordingly, separate samples were made at 226 higher salt contents. 227

Similar to the previous section, initial experiments were 228 conducted at a fixed water loading to identify the salt content 229 needed to see a measurable decrease in the melting 230 temperature. Similar to previous experiments,² we first cooled 231 the mixtures (which are initially in LLE) in vials to create 232 hydrates, and then gradually heated them under microscope to 233 observe the highest temperature at which hydrate crystals still 234 persist. Figure S1 shows exemplary images during the melting 235 process. These experiments were conducted at 30% POCB, i.e., 236 a much higher water content than in Figure 2 because at 30% 237 POCB, mixtures develop a waxy solid-like consistency during 238 crystallization, making it easy to transfer from the vial to the 239 microscope stage. In contrast, samples with much higher or 240 lower water content undergo large-scale phase separation and 241 sedimentation; and hence, the composition of the sample 242 transferred to the microscope deviates from the original 243 sample. Samples of fixed POCB content (30 wt %) were 244 prepared with salt loadings varying from 0.0 to 15.0 wt %. 245 Their melting points, T_m (Figure 3A), were found to reduce by 246 several degrees over the range of salt content examined. 247

It is interesting to consider the state of the mixtures in 248 Figure 3A prior to melting. We define m_s , m_p , and m_w as the 249 weight fractions of the salt, polymer, and water in the overall 250 mixture and take a unit mass of the mixture as basis. If χ is the 251 fraction of the POCB that crystallizes to form hydrate, then the 252

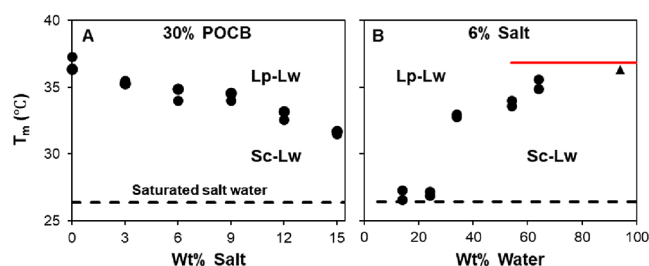


Figure 3. (A) The hydrate melting temperature obtained from optical microscopy for varying salt contents and fixed POCB loading of 30 wt %. (B) Melting temperature for varying water contents with a fixed salt loading of 6 wt %. The solid red line indicates the melting point for hydrate crystals with no salt present. The dashed line indicates the melting temperature of hydrate crystals in equilibrium with saturated salt water. The black triangle denotes a dilute POCB sample in 6% saltwater.

173 temperature of the hydrate; therefore, mixtures in LLE must 174 eventually crystallize. While nonequilibrium cloud points can 175 be measured, in the present case, hydrate crystallization was 176 too rapid to allow such quantification.

177 The water-rich branch of the cloud point curve was not 178 quantified in this research. Previously we noted that in the 179 absence of salt, the addition of even 1% POCB (MW 650 g/ 180 mol) to pure water brings the mixture into the LLE. Thus, the 181 boundary of the LLE region extends to nearly pure water, 182 making it difficult to quantify precisely. This remains true with 183 the addition of salt.

184 The magnitude of cloud point depression observed here is 185 far larger than in Lee et al.¹⁶ who found that a similar 30 °C 186 drop required a salt loading of 5.0 wt % vs less than 0.1 wt % in 187 Figure 2A. This difference may be attributable to the 188 differences in MW between our samples (650 g/mol) vs Lee 189 (250 g/mol). Indeed, in solutions of other polymers such as 190 PEO, PVP, and PNIPAM,^{18,21–23} the magnitude of cloud point 191 depression with added salt is known to increase with MW.

192 Based on the results of Figure 2A, a second set of 193 experiments was then conducted at a fixed salt content of 194 0.04 wt %, varying the water content from 10 to 20 wt %. 195 Figure 2B shows that the magnitude of cloud point reduction is 196 more severe as the water content reduces. This latter 197 observation may be rationalized as follows.

198 The common explanation for the salt effect on cloud point 199 depression is a result of polymer–ion interactions and 200 competition for hydration.^{18,19,26,31–33} Qualitatively, the ions 201 avoid association with the polymer and instead prefer to 202 associate with water. This reduces the level of hydration of the 203 polymer, eventually inducing the formation of a separate, 204 polymer-rich liquid phase. Indeed, this effect is not limited to 205 polymers; homogeneous mixtures of water with organic 206 solvents can be induced to phase separate upon adding 207 salt.²⁶ As the water content reduces while the salt loading is 208 held fixed, the amount of water available for hydrating the

mass of water consumed in hydrate formation is $0.31\chi m_p$ per unit mass of mixture (since the hydrate has a POCB:water ratio of 1:0.31). The salt fraction in the water-rich (Lw) phase is now

$$m_s^{Lw} = \frac{m_s}{1 - m_p(1 + 0.31\chi)} \quad (1)$$

The above assumes that the POCB-rich phase is nearly pure, the water-rich phase has negligible dissolved POCB, and (as discussed in the Melting point of hydrate section) all the salt partitions into the water-rich phase. For the highest salt loading in Figure 3A, $m_s = 0.15$ and $m_p = 0.3$. If we assume full crystallization, $\chi = 1.0$, eq 1 gives $m_s^{Lw} = 0.247$. This last number is close to the weight fraction of salt in salt-saturated water (roughly 0.27), i.e., as per this calculation this fully crystallized mixture would have an aqueous phase that is nearly saturated with salt. The above estimate of the salt fraction of 0.247 is an upper bound, since it assumes full crystallization of POCB, while polymers never crystallize to their full extent. In fact, we noted previously,^{6,7} that in the absence of salt, the volume change of crystallization was approximately half of that expected for full hydrate crystallization. Thus, if we take $\chi = 0.5$, eq 1 gives $m_s^{Lw} = 0.230$, which is still relatively close to full saturation. This calculation raises an interesting question: can the hydrate coexists with saturated water, and if so, what is the melting temperature of the hydrate in equilibrium with salt-saturated water?

To address this, a separate experiment was conducted. A small amount of POCB was added to pure water to precipitate the hydrate crystals. A small quantity of the crystals was transferred to a vial of salt water with excess salt (i.e., the aqueous phase is salt-saturated water), which was then heated gradually until the crystals melted. The corresponding temperature (roughly 26 °C), indicated by the dashed line in Figure 3, serves as a lower bound for the melting point in Figure 3, and corresponds to four-phase equilibrium between hydrate, salt crystals, a POCB-rich liquid phase, and saturated salt water (with very little POCB). It is noteworthy that this temperature exceeds room temperature, i.e., the hydrate is sufficiently salt-tolerant that does not melt even when equilibrated with salt-saturated water at room temperature.

Finally, Figure 3B shows the dependence of melting point on the composition at a fixed salt content of 6 wt %. The point marked with a black triangle represents an experiment in which a small amount of hydrate crystal particles was placed in 6% saltwater and then melted. The corresponding hydrate melting point of $T_m = 36.3$ °C shows no significant melting point depression as compared to the melting of a hydrate in equilibrium with pure water. With decreasing overall water content, the melting point reduces precipitously once the overall water loading in the mixture decreases below 40 wt %, and levels off at about 27 °C, close to the value for the hydrate in equilibrium with salt-saturated water. This may be rationalized from eq 1, once again taking $\chi = 0.5$ for the following example calculations. The overall water loading of 34% in Figure 3B corresponds to $m_s = 0.06$, $m_p = 0.6$, and $m_w = 0.34$. For this composition, eq 1 gives $m_s^{Lw} = 0.195$, thus, at 34% overall water, with crystallization of half of the POCB, the aqueous phase is still well below the saturation point. However, at an overall water loading of 24%, the mixture compositions are $m_s = 0.06$, $m_p = 0.7$, and $m_w = 0.24$. For this composition, eq

1 gives $m_s^{Lw} = 0.31$, corresponding to a supersaturated salt solution. Therefore, the steep drop in T_m below 40% water and the plateau around $T_m = 27$ °C at low water loading are consistent with the aqueous phase first approaching saturation and then becoming supersaturated. Indeed, salt crystals were observed in samples with 70 and 80 wt % POCB prior to melting. Since, the water-rich phase is salt-saturated, it is unsurprising that T_m shows a plateau at a value similar to that of the hydrate crystals placed into a vial of salt-saturated water.

Crystallization Kinetics. The study of phase behavior from the previous section guides our experiments on hydrate crystallization kinetics in two important ways. First, Figure 3 shows that the salt lowers the equilibrium melting temperature. Thus, at any specified crystallization temperature, T_c , increasing salt loading reduces the undercooling ($T_m - T_c$) and is expected to slow down crystallization kinetics. The second is that in mixtures containing over 0.1% salt, above T_m , LLE prevails at almost all POCB:water ratios (Figure 2). Thus, prior to crystallization, the mixture is almost always in LLE, and hence, three phases (two liquid, and the solid hydrate) are present during crystallization.^{6,7} Moreover, in general, neither of the two liquid phases coexisting during crystallization has the same composition as the hydrate. Instead, the water-rich phase is diluted in POCB, whereas the polymer-rich phase is diluted in water; the latter, especially, may change with salt content and crystallization temperature. Therefore, in general, hydrate crystallization may involve interfacial mass transport and hence is expected to depend on the mixing conditions. Accordingly, differential scanning calorimetry, the common method for studying the crystallization kinetics of polymers, cannot be used. Instead, we examined the hydrate crystallization kinetics by dilatometry,⁷ stirring the dilatometer flasks continuously with magnetic stir bars to avoid density-based separation. This is possible only at relatively low viscosity, necessitating a relatively low POCB content. Accordingly, our kinetic study was restricted to POCB–water mixtures with a low POCB content of 20 wt %. The kinetics data on salt-free samples were discussed comprehensively in a separate study by Banerjee et al.⁷

Mixtures with 20 wt % POCB, salt loading ranging from 0.0 to 7 wt %, and the remainder water were prepared in a dilatometer with a magnetic stirrer. For each experiment, samples were held above their melting point in a hot bath at 48 °C and then transferred to a second bath held at a fixed crystallization temperature T_c . Volume changes were measured by quantitative video analysis over the course of 3–6 h. 2–4 samples were prepared at each individual composition, and each sample was crystallized isothermally at various values of T_c .

As described previously,^{6,7} upon cooling to T_c , two forms of volume change were observed. Within the first few minutes, the volume decreased due to thermal contraction as the samples cooled from 48 °C to T_c . Over a longer period, there was a further volume decrease due to crystallization. This latter volume decrease occurred more quickly at lower crystallization temperatures, and hence at sufficiently low T_c values, crystallization started even before the thermal contraction was completed. Such fast crystallization is no longer isothermal and was not analyzed. The volume change associated with crystallization was obtained by subtracting the volume change due to thermal contraction from the total volume change.⁶ Figure 4 shows examples of the specific volume change due to

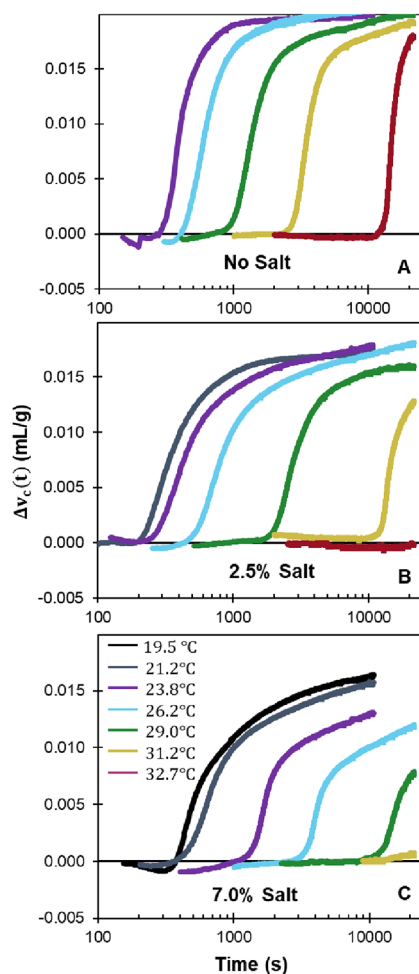


Figure 4. Time-evolution of specific volume change during crystallization at various temperatures. All samples have 20.0 wt % POCB, and salt weight percentages noted at the bottom of each figure.

taken as the average of Δv_c values from the six lowest 398 temperatures available for each composition. Figure 5 shows 399 that the $\Delta v_c^{\text{final}}$ does not change any systematic way with salt 400 content. 401

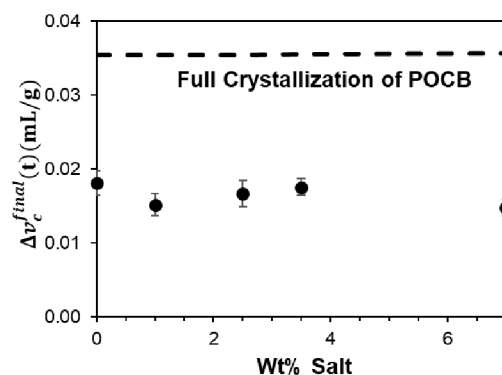


Figure 5. Average specific volume change at long crystallization times for samples with 20 wt % POCB. The dotted line indicates the theoretical maximum value predicted by eq 2.

A theoretical maximum volume change, Δv_c^{max} (assuming all 402 POCB is consumed to form hydrate), can be estimated as 403

$$\Delta v_c^{\text{max}} = \left(\frac{m_w + m_s}{\rho_{\text{aq},i}} + \frac{m_p}{\rho_p} \right) - \left(\frac{\frac{m_{\text{POCB}}}{0.764}}{\rho_c} + \frac{1 - \frac{m_{\text{POCB}}}{0.764}}{\rho_{\text{aq},f}} \right) \quad (2) \quad 404$$

where $\rho_{\text{aq},i}$, $\rho_{\text{aq},f}$, ρ_{POCB} , and ρ_c are the densities of the aqueous 405 phase before crystallization, the aqueous phase after crystallization, POCB, and the hydrate crystal respectively, and 0.764 406 is the weight fraction of POCB in the crystal. The term in the 407 first brackets is the sum of the specific volume of the saltwater 408 and liquid POCB, which are assumed to be completely 409 immiscible. The term in the second brackets is the sum of the 410 specific volumes of the hydrate crystal and the uncrystallized 411 saltwater. The density of the crystal phase is $\rho_c = 1.176$ g/mL 412 (based upon dimensions of the unit cell,³⁴ and the density of 413 POCB is $\rho_{\text{POCB}} = 1.02$ g/mL. The density of the saltwater 414 phase is calculated for each composition based upon the model 415 provided by Simion³⁵ by assuming that all the salt is in the 416 aqueous phase both before and after crystallization. Further all 417 densities are assumed to be independent of temperature. The 418 prediction of eq 2 (dashed line in Figure 5) is found to be 419 nearly independent of salt content (in effect, $\rho_{\text{aq},i}$ and $\rho_{\text{aq},f}$ only 420 weakly depends on salt content). 421

The predicted value is found to be nearly twice of the 423 measured values of $\Delta v_c^{\text{final}}$ suggesting that only roughly 50% of 424 the POCB actually crystallizes at any given salt content. This 425 value of 50% crystallization is similar to that estimated from 426 previous experiments in which the hydrate crystallized from a 427 homogeneous liquid phase with an excess POCB.⁶ Yet, it 428 should be noted that this conclusion of 50% crystallization 429 depends on the estimated crystal phase density. Even a few 430 percent error in the published values of unit cell dimensions 431 change the ρ_c value, and hence the value of Δv_c^{max} 432 significantly. 433

Next, we turned to the effect of salt on the crystallization 434 rate. As in our previous studies^{6,7} to quantify the kinetics, from 435 each $\Delta v_c(t)$ curve, we identified the time τ at which the volume 436 change reached 0.005 mL/g (chosen arbitrarily), i.e., $\Delta v_c(t = 437$

374 crystallization, $\Delta v_c(t)$, for samples with 20 wt % POCB, 375 without salt, with 2.5 wt % salt, and with 7.0 wt % salt. Other 376 intermediate values of salt loadings are shown in Figure S3. As 377 previously described, even though crystallization shrinks the 378 volume of the mixture, Δv_c is shown as a positive quantity.

379 Each crystallization trial follows a similar pattern of an initial 380 latent period without significant crystallization, followed by 381 rapid crystallization and an eventual plateau at some final value. 382 The duration of the initial latent period grew with increasing 383 salt content; compare for instance the time at which 384 crystallization starts at 29 °C in Figure 4A (roughly 1000 s) 385 vs 4B (roughly 2000 s). This trend points toward salt having an 386 inhibiting effect on the cocrystallization kinetics of POCB 387 hydrate. An analogous salt effect was described by Bianchi²⁷ 388 wherein the presence of salt inhibited the crystallization of 389 poly(caproamide).

390 As previously,⁶ we seek to quantify the crystallization 391 behavior in terms of two parameters: the value of Δv_c at 392 long times $\Delta v_c^{\text{final}}$, and the time needed to reach a specified 393 value of Δv_c . To estimate $\Delta v_c^{\text{final}}$, we plotted the value of Δv_c at 394 $t = 10^4$ s (selected arbitrarily) for each experiment. Figure S4 395 shows that this value increases with decreasing temperature T_c 396 and then it shows a plateau. This suggests that at sufficiently 397 low temperature crystallization is complete by 10^4 s. $\Delta v_c^{\text{final}}$ was

$\tau = 0.005 \text{ mL/g}$. This time τ provides a single number to compare the kinetic data at all salt contents. Figure 6 shows τ

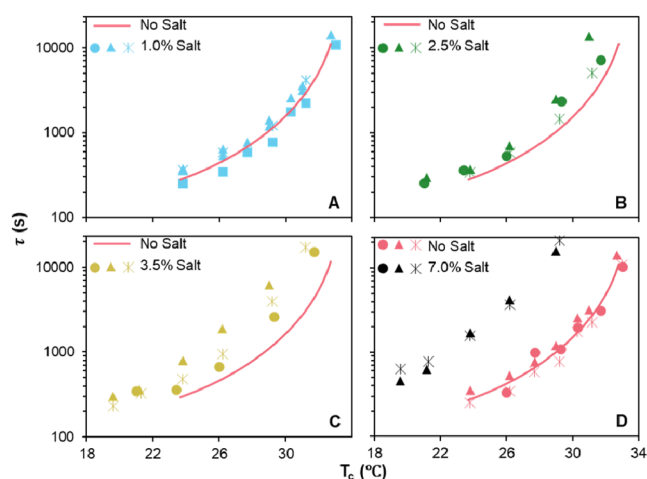


Figure 6. Time for $\Delta\nu_c = 0.005 \text{ mL/g}$ at various crystallization temperatures. All samples have 20 wt % POCE, with varying salt contents. The pink data in D corresponds to the salt-free sample which is 'reproduced with permission from Ref.,⁷ copyright [2023][Elsevier-polymer]' and the pink line in A, B and C are a guide to the eye. Different symbols in each graph represent distinct samples of the same composition.

versus crystallization temperature T_c . The corresponding salt-free data are shown only in Figure 6D, but the solid pink line passing through the salt-free data is shown in Figures 6A–D for comparison. In general, increasing salt content increases τ , i.e., slows down crystallization, although the effect is modest below 3 wt % salt.

As mentioned at the beginning of this section, the salt-induced melting point depression reduces the undercooling $\Delta T = (T_m - T_c)$, and hence, it is expected to slow crystallization. To quantify the extent of this effect, we must therefore compare τ values at fixed undercooling, rather than at fixed T_c . The well-established approach for doing so is the Hoffman–Lauritzen theory³⁶ which relates the kinetics of crystallization to the free energy of secondary nucleation on the face of the growing crystal. It predicts crystallization rate as

$$\text{crystallization rate} \propto \exp\left(-B \frac{T_m}{T_c \Delta T}\right) \quad (4)$$

Note that the quantity T_m/T_c is close to 1 in our case, thus to a first approximation, the right-hand side depends on ΔT alone. Accordingly, eq 4 accounts for the changes in undercooling due to melting point depression; if that is the only factor by which salt affects crystallization kinetics, then one would expect data at all salt contents to collapse onto a single line. That would suggest that the only effect of salt is to slow down the secondary nucleation necessary for crystal growth.

Accordingly, with τ^{-1} as a measure of the crystallization rate, and Figure 7 plots $\ln(\tau^{-1})$ vs $T_m/T_m \Delta T$. While the number of points for each sample are small, the data do appear approximately linear, consistent with eq 4, i.e., the Hoffman–Lauritzen model can represent the data at least approximately. A detailed discussion of the salt-free data was presented previously;⁷ here we only focus on the effects of salt. Even though data at the different salt contents do move closer

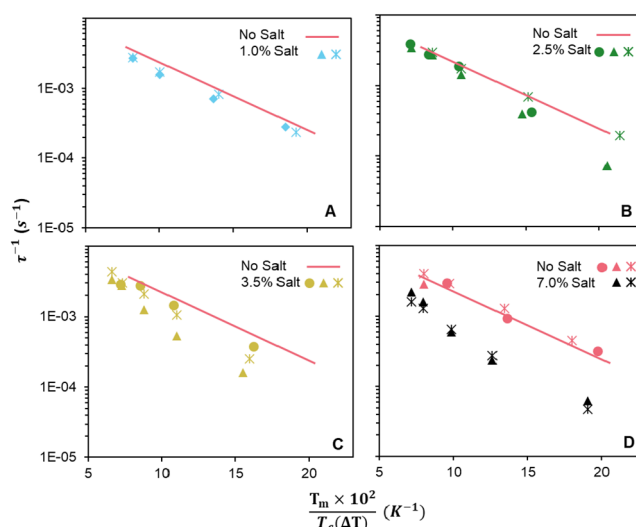


Figure 7. Time for $\Delta\nu_c = 0.005 \text{ mL/g}$ for various salt contents in the form of a Hoffman–Lauritzen plot. Different symbols in each graph represent a distinct sample of the same composition. The pink data in D corresponds to the salt-free sample which is 'reproduced with permission from Ref.,⁷ copyright [2023][Elsevier-polymer]'. The pink straight line corresponds to eq 4 for the salt-free data and is reproduced in A–C as a reference.

together than in Figure 6, data for the various salt samples remain distinctly below the salt-free line. These results indicate that the salt effects on undercooling can account for only a part of the slowing of the crystallization kinetics. We emphasize that this last conclusion does not rely on the validity of the Hoffman–Lauritzen model. The effect of salt-induced melting point depression can be judged without guidance from Eq 4: Simply plotting the results of Figure 6 with ΔT on the x -axis shows that, even when compared at fixed undercooling, salt slows hydrate crystallization. Finally, the samples at 2.5 and 3.5% show a large degree of sample-to-sample variability with some behaving similar to the sample without salt, and some to the sample with 7 wt % salt. It is possible that the mechanism of crystallization changes across this concentration range.

Figure 7 also shows a distinct increase in the temperature-dependence of the crystallization kinetics with increasing salt content. For homopolymers, a decrease in slope of the crystallization kinetics vs $T_m/T_m \Delta T$ indicates a decrease in the surface energy at the crystal–melt interface as per the Hoffman–Lauritzen model.³⁶ Accordingly, Figure 7 indicates that increasing salt concentration reduces the surface energy. In the current situation, however, hydrate crystallization occurs from a mixture of polymer, salt, and water. For a homopolymer crystallizing from a mixture, there is an additional contribution to the slope that comes from the concentration of the polymer.³⁷ Although we keep the polymer loading fixed at 20 wt % in all samples, the compositions of the coexisting liquid phases may change with salt content and may in turn affect the temperature-dependence. Thus, it is difficult to conclusively pin down the reason underlying the increasing temperature-sensitivity of the crystallization kinetics with increasing salt content.

As in Banerjee et al.,⁷ we also considered an alternate method to quantify kinetics which is based on the induction time, i.e., the time up to which $\Delta\nu_c$ remains nearly zero (see short time behavior in Figure 5). This induction time, t_{ind} , has been regarded as the time for primary nucleation³⁸ and serves

as another measure of crystallization kinetics. Analysis of data based on the induction time (see ESI) gives conclusions that are essentially identical to those based on analysis using the time scale τ .

SUMMARY AND CONCLUSIONS

To summarize, inorganic salts are well known to induce liquid–liquid separation in aqueous solutions of many water-soluble polymers. This paper examines the effects of adding salt to mixtures of polyoxacyclobutane (POCB) and water. POCB has the rare ability to cocrystallize with water to form a hydrate, one of only two or three polymers that can do so. Further, above the melting temperature of the hydrate, mixtures of POCB and water can exist in liquid–liquid equilibrium (LLE). This combination of immiscibility in the liquid phase and cocrystallization at low temperature gives POCB–water mixtures a phase diagram that is distinct from all other polymer–solvent pairs. Here, we report on the effect of adding NaCl salt to the phase diagram of POCB–water mixtures and to the kinetics of hydrate crystallization.

The central results of this paper are as follows.

1. Even small loadings of salt (less than 0.1 wt %) can significantly expand the composition range within which LLE appears, i.e., there is a salting-out effect similar to other aqueous polymer solutions. The expansion of LLE, as judged by lowering of the cloud point temperature, is especially severe at low water content. This suggests that the reason why salt drives LLE is that by demixing of the polymer and water and partitioning into the aqueous phase, the salt can avoid association with the polymer.

2. Much larger salt loadings (~10 wt %) reduce the melting temperature of the hydrate.

3. The hydrate is remarkably salt-tolerant and can coexist even with salt-saturated water. Accordingly, the lowest melting point of the hydrate (i.e., the greatest melting point depression of the hydrate) corresponds to a four-phase equilibrium between a POCB-rich liquid phase, a water-rich liquid phase, solid hydrate, and solid NaCl. The corresponding four-phase equilibrium temperature is 26 °C, just above room temperature.

4. Since salt greatly shrinks the homogeneous liquid region, in POCB–water–salt mixtures, hydrate crystallization starts from the LLE state at almost all compositions. Bulk crystallization experiments (conducted with continuous stirring to avoid layering of the two liquids) show that salt decreases the crystallization rate. The decrease in rate is modest for ~1 wt % salt loading but approaches 10x at the highest loading (7% salt) examined. Some, but not all, of the slowing of hydrate crystallization can be explained by the melting point depression, i.e., the fact that at any given crystallization temperature, salt-containing samples are at lower undercooling.

To the best of our knowledge, the latter two items are the first report of any salt effect on the phase behavior or crystallization kinetics of a polymer hydrate cocrystal.

Overall, the effect of salt on the LLE behavior of POCB–water mixtures is similar to that of other aqueous polymer solutions. The effect of salt on the hydrate melting point is qualitatively similar to the melting point depression of any crystal equilibrating with a solute. Finally, the fact that salt slows the hydrate crystallization even when compared to fixed undercooling suggests that salt may have additional interfacial

effects that slow crystallization beyond what may be expected from melting point depression alone.

EXPERIMENTAL

Materials. Polyoxacyclobutane was obtained from DuPont under the trade name Cerenol. The experiments used POCB with a number-average molecular weight of 650 g/mol, as reported by the manufacturer. The glassware used in the dilatometry experiments was prepared in a glass shop at the University of Pittsburgh. As even small salt impurities were found to significantly alter cloud-point results, Millipore water was used in all samples.

Cloud Point Methods. POCB–water–salt mixtures (roughly 3 g total) were weighed into small glass vials. The vial lid was closed and sealed with a silicone sealant to prevent any water loss due to evaporation. The samples were immersed in a water bath with the temperature controlled by a hot plate. The bath temperature was gradually raised until sample cloudiness became visually apparent and then lowered to verify the disappearance of cloudiness. For these experiments, it was necessary for the entire vial to be immersed in a water bath. If any portion of the vial, e.g., the cap, was exposed to cooler air during the experiment, condensation of water on the cooler surface confounded the results.

Melting Point Methods. POCB–water–salt mixtures were weighed into small glass vials and allowed to crystallize at room temperature over many days. A small quantity of the resulting hydrate–liquid mixture was then placed into a polystyrene well plate and flattened. This well plate was placed under a microscope in a temperature-controlled stage and heated in 2 °C increments starting from 22 °C. The temperature at which the hydrate crystals were no longer visible was taken as the melting point temperature for that sample.

Crystallization Measurement Methods. POCB–water–salt mixtures (roughly 1 g in total) were weighed into round-bottom flasks. A magnetic stir bar was added to all samples. The samples were then covered with mineral oil, and the flasks were joined to a capillary stem and sealed with parafilm. The samples were heated to 48 °C to ensure all hydrate crystals were melted and then cooled rapidly in a water bath set to the desired crystallization temperature. All the graphs and the data analysis use the true temperature that was continuously read off of a calibrated digital thermometer immersed in the water bath. Typically, the temperature during any single experiment varied no more than ± 0.1 °C. The samples were stirred continuously during this process (see the next paragraph). The change in volume was measured by imaging the oil meniscus level in the capillary tube and then analyzing the images using Blender motion tracking to determine the meniscus position over time. The volume changes were then calculated and normalized by the sample weight. The procedure and data analysis are explained in detail in our previous study.⁶ The camera resolution allows the change in height of the oil meniscus to be measured with 0.02 mm accuracy. Combined with the cross-sectional area of the capillary, the corresponding volume change is around 0.0007 mL, whereas typical volume changes in each experiment are roughly 0.05 mL. We believe that the greatest variability in the experiments comes from the fact that mixing may not be perfectly reproducible in such small samples. For example, if a large drop of the mixture becomes entrained in the oil phase early during the experiment, it may crystallize earlier or later than the rest of the mixture.

Since samples are in liquid–liquid equilibrium prior to crystallization, the rate of mixing was found to have a significant effect on the kinetics of crystallization. As such, a rotor assembly was designed and implemented to ensure similar mixing in each sample. The rotor assembly consists of five rotors connected by intermeshed gears and is driven by a single motor that drives the center gear by an elastic band. The motor rotation speed was set to 140 rpm for all experiments.

ASSOCIATED CONTENT

Data Availability Statement

Experimental data, including the evolution of volumes with time, and spreadsheets of the data used to plot Figures 2, 3, 4, and 6 will be available on request.

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.langmuir.3c02428>.

Additional experimental data analysis of crystallization kinetics including figures and alternate method of quantifying crystallization kinetics. Also, microscopic images of hydrate melting point, salt crystals (PDF)

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Author Contributions

Michael Gresh-Sill has done the methodology, data curation, writing—original draft preparation; software; validation; formal analysis; and investigation. Sudesna Banerjee is responsible for writing—review and editing. Tara Meyer is responsible for writing—review and editing. Sachin Velankar has done the methodology; supervision; writing—review and editing; and conceptualization.

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Notes

The authors declare no competing financial interest.

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REFERENCES

- (1) Tadokoro, H.; Takahashi, Y.; Chatani, Y.; Kakida, H. Structural studies of polyethers, $[-(\text{CH}_2)_m-\text{O}-]_n$. *Polyoxacyclobutane*. *Makromol. Chem.* **1967**, *109*, 96–111.
- (2) Banerjee, J.; Koronaios, P.; Morganstein, B.; Geib, S. J.; Enick, R. M.; Keith, J. A.; Beckman, E. J.; Velankar, S. S. Liquids That Freeze

When Mixed: Cocrystallization and Liquid–Liquid Equilibrium in Polyoxacyclobutane–Water Mixtures. *Macromolecules* **2018**, *51*, 3176–3183.

(3) Chatani, Y.; Kobatake, T.; Tadokoro, H. Structural studies of poly(ethylenimine). 3. Structural characterization of anhydrous and hydrous states and crystal structure of the hemihydrate. *Macromolecules* **1983**, *16* (2), 199–204.

(4) Benkhira, A.; Franta, E.; Francois, J. Polydioxolane in aqueous solutions. 1. Phase diagram. *Macromolecules* **1992**, *25* (21), 5697–5704.

(5) Guenet, J.-M. *Polymer-Solvent Molecular Compounds*; Elsevier, 2010.

(6) Barker, E.; Banerjee, S.; Meyer, T. Y.; Velankar, S. Liquids that Freeze when Mixed: Homogeneous Cocrystallization Kinetics of Polyoxacyclobutane–Water Hydrate. *ACS Appl. Polym. Mater.* **2022**, *4*, 703–713.

(7) Banerjee, S.; Gresh-Sill, M.; Barker, E. F.; Meyer, T. Y.; Velankar, S. S. Polymer co-crystallization from LLE: Crystallization kinetics of POCB hydrate from two-phase mixtures of POCB and water. *Polymer* **2023**, *282*, 126087.

(8) Chido, M. T.; Koronaios, P.; Saravanan, K.; Adams, A. P.; Geib, S. J.; Zhu, Q.; Sunkara, H. B.; Velankar, S. S.; Enick, R. M.; Keith, J. A. Oligomer hydrate crystallization improves carbon nanotube memory. *Chem. Mater.* **2018**, *30*, 3813–3818.

(9) Badeau, B. A.; DeForest, C. A. Programming stimuli-responsive behavior into biomaterials. *Annu. Rev. Biomed. Eng.* **2019**, *21* (1), 241–265.

(10) Municoy, S.; Álvarez Echazú, M. I.; Antezana, P. E.; Galdopórpora, J. M.; Olivetti, C.; Mebert, A. M.; Foglia, M. L.; Tuttolomondo, M. V.; Alvarez, G. S.; Hardy, J. G. Stimuli-responsive materials for tissue engineering and drug delivery. *Int. J. Mol. Sci.* **2020**, *21*, 4724.

(11) Babu, P.; Nambiar, A.; He, T.; Karimi, I. A.; Lee, J. D.; Englezos, P.; Linga, P. A Review of Clathrate Hydrate Based Desalination To Strengthen Energy–Water Nexus. *ACS Sustainable Chem. Eng.* **2018**, *6*, 8093–8107.

(12) Freier, E.; Wolf, S.; Gerwert, K. Proton transfer via a transient linear water-molecule chain in a membrane protein. *Proc. Natl. Acad. Sci. U. S. A.* **2011**, *108* (28), 11435–11439.

(13) Gadjourova, Z.; Andreev, Y. G.; Tunstall, D. P.; Bruce, P. G. Ionic conductivity in crystalline polymer electrolytes. *Nature* **2001**, *412*, 520–523.

(14) Wei, M.; Gao, Y.; Li, X.; Serpe, M. J. Stimuli-responsive polymers and their applications. *Polym. Chem.* **2017**, *8*, 127–143.

(15) Albertsson, P.-Å. *Aqueous Polymer-Phase Systems. In Partition of Cell Particles and Macromolecules*; Wiley: New York, 1986; 8–39.

(16) Lee, H.-N.; Rosen, B. M.; Fenyvesi, G.; Sunkara, H. B. UCST and LCST phase behavior of poly(trimethylene ether) glycol in water. *J. Polym. Sci. A Polym. Chem.* **2012**, *50*, 4311–4315.

(17) Liu, Y.; Wang, Y.; Cai, W. Salting Effect of Sodium Hydroxide and Sodium Formate on the Liquid–Liquid Equilibrium of Polyoxymethylene Dimethyl Ethers in Aqueous Solution. *Journal Of Chemical & Engineering Data* **2019**, *64* (6), 2578–2592.

(18) Ananthapadmanabhan, K. P.; Goddard, E. D. Aqueous biphasic formation in polyethylene oxide-inorganic salt systems. *Langmuir* **1987**, *3* (1), 25–31.

(19) Thormann, E. On understanding of the Hofmeister effect: how addition of salt alters the stability of temperature responsive polymers in aqueous solutions. *RSC Adv.* **2012**, *2*, 8297.

(20) Zafarani-Moattar, M. T.; Sadeghi, R. Measurement and correlation of liquid–liquid equilibria of the aqueous two-phase system polyvinylpyrrolidone–sodium dihydrogen phosphate. *Fluid Phase Equilib.* **2002**, *203* (1), 177–191.

(21) Zhang, Y.; Foryk, S.; Sagle, L. B.; Cho, Y.; Bergbreiter, D. E.; Cremer, P. S. Effects of Hofmeister Anions on the LCST of PNIPAM as a Function of Molecular Weight. *J. Phys. Chem. C* **2007**, *111*, 8916–8924.

(22) Herbst, J.; Pott, R. W. M. The Effect of Temperature on Different Aqueous Two-Phase Diagrams of Polyethylene Glycol (PEG

- 6000, PEG 8000, and PEG 10000) + Potassium Sodium Tartrate +
Water. *Journal Of Chemical & Engineering Data* **2019**, 64 (7), 3036–
3043.
- (23) Sosa, F. H. B.; Farias, F. O.; Igarashi-Mafra, L.; Mafra, M. R.
Measurement and correlation of aqueous two-phase systems of
polyvinylpyrrolidone (PVP) and manganese sulfate: Effects of
molecular weight and temperature. *Fluid Phase Equilib.* **2018**, 472,
204–211.
- (24) Jana, S.; Uchman, M. Poly(2-oxazoline)-based stimulus-
responsive (Co)polymers: An overview of their design, solution
properties, surface-chemistries and applications. *Prog. Polym. Sci.*
2020, 106, 101252.
- (25) Zaslavsky, B. Y.; Bagirov, T. O.; Borovskaya, A. A.; Gasanova,
G. Z.; Gulaeva, N. D.; Levin, V. Y.; Masimov, A. A.; Mahmudov, A.
U.; Mestechkina, N. M.; Miheeva, L. M.; Osipov, N. N.; Rogozhin, S.
V. Aqueous biphasic systems formed by nonionic polymers I. Effects
of inorganic salts on phase separation. *Colloid. Polymer Sci.* **1986**, 264,
1066–1071.
- (26) Hyde, A. M.; Zultanski, S. L.; Waldman, J. H.; Zhong, Y.-L.;
Shevlin, M.; Peng, F. General Principles and Strategies for Salting-Out
Informed by the Hofmeister Series. *Org. Process Res. Dev.* **2017**, 21,
1355–1370.
- (27) Bianchi, E.; Ciferri, A.; Tealdi, A.; Torre, R.; Valenti, B. Bulk
Properties of Synthetic Polymer-Inorganic Salt Systems. II. Crystal-
lization Kinetics of Salted Poly(caproamide). *Macromolecules* **1974**, 7,
495–500.
- (28) Valenti, B.; Bianchi, E.; Tealdi, A.; Russo, S.; Ciferri, A. Bulk
Properties of Synthetic Polymer-Inorganic Salt Systems. IV. Role of
the Polymeric Substrate. *Macromolecules* **1976**, 9, 117–122.
- (29) Hashifudin, A.; Sim, L. H.; Chan, C. H.; Ramli, H. Phase
behaviour and morphology of composite comprising of poly(ethylene
oxide), polyacrylate and lithium perchlorate. *Compos. Interfaces* **2014**,
21, 797–805.
- (30) Dendy Sloan, E.; Koh, C. A. Chapter 4: Effect of
Thermodynamic Inhibitors on Hydrate Formation. In *Clathrate
Hydrates of Natural Gases*; CRC Press: Boca Raton, FL, 2008; pp
229–236.
- (31) Florin, E.; Kjellander, R.; Eriksson, J. C. Salt effects on the
cloud point of the poly(ethylene oxide)+ water system. *J. Chem. Soc.,
Faraday Trans. 1* **1984**, 80 (11), 2889.
- (32) Huddleston, J. G.; Willauer, H. D.; Griffin, S. T.; Rogers, R. D.
Aqueous Polymeric Solutions as Environmentally Benign Liquid/
Liquid Extraction Media. *Ind. Eng. Chem. Res.* **1999**, 38, 2523–2539.
- (33) Sadeghi, R.; Jahani, F. Salting-In and Salting-Out of Water-
Soluble Polymers in Aqueous Salt Solutions. *J. Phys. Chem. B* **2012**,
116 (17), 5234–5241.
- (34) Kakida, H.; Makino, D.; Chatani, Y.; Kobayashi, M.; Tadokoro,
H. Structural Studies of Polyethers [-(CH₂)mO-]_n. VIII. Polyox-
acyclobutane Hydrate (Modification I). *Macromolecules* **1970**, 3,
569–578.
- (35) Simion, A. I.; Grigoras, C.-G.; Rosu, A.-M.; Gavrila, L.
Mathematical Modelling of Density and Viscosity of NaCl Aqueous
Solutions. *Journal Of Agroalimentary Processes and Technologies* **2014**,
21, 41–52.
- (36) Mandelkern, L. *Crystallization of Polymers: Kinetics &
Mechanism*, 2nd ed.; Cambridge University Press: New York, USA,
2004; 2, Chapter 9
- (37) Mandelkern, L. *Crystallization of Polymers: Kinetics &
Mechanism*, 2nd ed.; Cambridge University Press: New York, USA,
2004; 2, Chapter 11
- (38) Iwamatsu, M. Direct numerical simulation of homogeneous
nucleation and growth in a phase-field model using cell dynamics
method. *J. Chem. Phys.* **2008**, 128 (8), No. 084504.