



Interpretable Deep Clustering Survival Machines for Alzheimer's Disease Subtype Discovery

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ABSTRACT

Alzheimer's disease (AD) is a complex neurodegenerative disorder that has impacted millions of people worldwide. The neuroanatomical heterogeneity of AD has made it challenging to fully understand the disease mechanism. Identifying AD subtypes during the prodromal stage and determining their genetic basis would be immensely valuable for drug discovery and subsequent clinical treatment. Previous studies that clustered subgroups typically used unsupervised learning techniques, neglecting the *survival information* and potentially limiting the insights gained. To address this problem, we propose an interpretable survival analysis method called Deep Clustering Survival Machines (DCSM), which combines both *discriminative* and *generative* mechanisms. Similar to mixture models, we assume that the timing information of survival data can be *generatively* described by a mixture of parametric distributions, referred to as *expert distributions*. We learn the weights of these expert distributions for individual instances in a *discriminative* manner by leveraging their features. This allows us to characterize the survival information of each instance through a weighted combination of the learned expert distributions. We demonstrate the superiority of the DCSM method by applying this approach to cluster patients with mild cognitive impairment (MCI) into subgroups with different risks of converting to AD. Conventional clustering measurements for survival analysis along with genetic association studies successfully validate the effectiveness of the proposed method and characterize our clustering findings.

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or writing of this report. A complete listing of ADNI investigators can be found at: http://adni.loni.usc.edu/wp-content/uploads/how_to_apply/ADNI_Acknowledgement_List.pdf.

1. Introduction

According to the World Health Organization (WHO)⁴, dementia has affected 55 million people worldwide in 2023. This number could increase to 139 million by 2050 as more people age. Alzheimer's disease (AD) is the most common cause of dementia, accounting for over two-thirds of the cases. However, as a complex and heterogeneous brain disorder, AD remains poorly understood. Finding subtypes of AD and their genetic factors could help develop new drugs and guide treatments in the prodromal stage for this critical condition.

Previous works usually use unsupervised learning methods such as KMeans (Hartigan and Wong, 1979), GMM (Reynolds *et al.*, 2009), DBSCAN (Ester *et al.*, 1996) etc. to stratify AD patients into different clusters/subtypes (Alashwal *et al.*, 2019; Feng *et al.*, 2022). They merely utilize the feature information to find different groups with distinct characteristics. However, these approaches ignore the fact that dementia patients often visit the hospital multiple times to track their disease progression. These results in longitudinal trajectories that capture additional survival information about the patients such as the probability of conversion from mild cognitive impairment (MCI) to AD. Thus, it would be valuable if we can leverage the survival information to facilitate AD subtype discovery.

The goal of survival analysis (Flynn, 2012) is to learn a survival model to build the bridge between features and survival information. When given the feature of a subject, survival models can predict the risk of death or occurrence of some event such as MCI converting to AD. In this way, we have an opportunity to utilize the predicted risk to stratify the MCI patients into different subgroups with different risks of converting to AD. It would thus enable customized treatment for different patients with different risks. In this study, we aim to conduct subtypes discovery for Alzheimer's disease from the survival analysis perspective, which has the potential to improve clinical decision-making by identifying high-risk MCI patients who may require more care or early treatment. It is worth noting that a big challenge in survival analysis is *censoring*, which means the target event of a subject is unobservable after a period of time or no event happens during the monitoring. Therefore, many subjects do not possess complete survival information and we face the problem of semi-supervised learning or weak supervised learning instead of fully supervised learning. Given these circumstances, it becomes impractical to directly employ survival information for the purpose of subgroup stratification. Thus, the development of an effective clustering technique that is capable of leveraging partial survival information becomes imperative.

There are many survival models that have been proposed to predict the risk of an event happening, also known as "time-to-event prediction" (Kvamme *et al.*, 2019). The most classic method is called the Cox PH model (Cox, 1972). It assumes a constant hazard rate over time for every subject, known as the proportional hazard (PH) assumption. There are other methods that do not make any assumptions about the underlying distribution of survival times, such as Kaplan-Meier (Bland

and Altman, 1998), Nelson-Aalen (Klein, 1991), and Life-Table (Tarone, 1975). However, these methods struggle with high-dimensional data. Machine learning techniques can help overcome this high-dimensional challenge and can learn the association between features and survival outcomes efficiently. For example, Deep Survival Machines (DSM) (Nagpal *et al.*, 2021) uses deep neural networks to learn the compact representation of the features and uses the negative log-likelihood as the loss to learn all the parameters, showing promising results in prediction accuracy. Deep Cox (Katzman *et al.*, 2018) utilizes the derived Cox PH loss to optimize the parameter learning of deep neural networks.

Nevertheless, all the survival models aforementioned are not specifically designed for clustering. They are mainly used to do risk prediction. To leverage them to do clustering, we need to set a threshold for the predicted risks to artificially cluster them into subgroups, such as two groups where one is with high risk and the other is with low risk. Survival Clustering Analysis (SCA) (Chapfuwa *et al.*, 2020) and Variational Deep Survival Clustering (VaDeSC) (Manduchi *et al.*, 2021) are two recent works that can do both risk prediction and clustering. However, SCA cannot control the number of clusters because it utilizes the truncated Dirichlet process to realize the automatic identification of the cluster numbers., and VaDeSC as a fully generative method is restricted to a specific distribution of features. Neural Survival Clustering (Jeanselme *et al.*, 2022) is another recent model developed to perform clustering and time-to-event prediction simultaneously. It learns the survival probability for each instance by learning fixed neural networks without any assumptions in a thorough discriminative manner. However, the model requires a considerable amount of training data to avoid overfitting, which may not be feasible for small-scale datasets, particularly in the medical field.

In this study, we propose a hybrid method that leverages both the discriminative and generative strategies to perform clustering and risk prediction simultaneously. Specifically, we assume that there are a certain number of expert distributions in a latent space and each expert distribution can be modeled by parameterized distributions in a generative way. The survival function for each instance is a weighted combination of all the expert distributions and the weight for each instance is learned by a multi-layer perceptron (MLP) directly from the features in a discriminative manner. Consequently, we can naturally cluster all the instances according to how the weights are allocated to different expert distributions for each instance. We demonstrate the advantage of our method by evaluating not only the conventional clustering measurements for survival analysis but also the genetic association discrepancies between different groups of patients with different risks of converting from MCI to AD. In summary, our contributions are five-fold:

- We propose a hybrid survival analysis method called Deep Clustering Survival Machines (DCSM) that integrates the advantages of the discriminative and generative ideas and can perform both clustering and time-to-event prediction simultaneously.
- We apply our method to Alzheimer's imaging data to dis-

⁴<https://www.who.int/news-room/fact-sheets/detail/dementia>

cover AD subtypes. LogRank results and results on genetic association discrepancy validate the effectiveness of the proposed method.

- To further validate the effectiveness of the proposed method, we also conduct experiments on several real-world benchmark datasets. The results show promising clustering results as well as competitive time-to-event prediction performance.
- Our method is interpretable in that the expert distributions are constant for all the instances. Different weightings signify different attention to the expert distributions and thus we can easily tell which subgroup the instance belongs to.
- We perform feature importance for different regions of the brain to interpret what regions the proposed model pays more attention to when clustering the patients into low and high risks. The identified important brain regions show a strong relationship to AD.

2. Related Work

Clustering. Clustering is the most relevant topic to our paper. Clustering is a concept from the machine learning community that involves grouping similar data points together based on certain characteristics. In the medical domain, people may use stratification or subtype discovery to describe similar problems. These terms refer to the process of identifying subgroups within a larger population that share similar characteristics or traits. The paper will use these terms interchangeably. Traditional clustering methods such as KMeans (Hartigan and Wong, 1979), GMM (Reynolds et al., 2009), DBSCAN (Ester et al., 1996) usually use the sample features only to calculate the similarity or distance between samples to discover the subtype among populations (Alashwal et al., 2019; Feng et al., 2022). Considering that patients can visit hospitals several times and thus render longitudinal information, we can also use survival analysis techniques to predict the risk of getting AD for each patient and stratify them using the predicted risk in a post-hoc way. This risk prediction in survival analysis is also called “time-to-event-prediction”.

Time-to-event Prediction. There are many time-to-event prediction methods that have been proposed. One of the most prevalent methods is the Cox proportional hazards regression model (Cox PH) (Cox, 1972). It assumes that the relative proportional hazard between subjects is constant over time. In other words, if subject *A* has a higher risk of death or another event at some time point than another subject *B*, then *A*’s risk will always be higher than *B*’s. Although Cox PH has achieved many successes in survival analysis, it still has a narrow application since its assumption of proportional hazard is too strong to satisfy in reality. Traditional methods including Kaplan-Meier (Bland and Altman, 1998), Nelson-Aalen (Klein, 1991), and Life-Table (Tarone, 1975) are also useful to do survival analysis. However, they can hardly scale to large dimensionality. Recently, many machine learning methods, especially

deep learning methods, have been proposed to do survival analysis. Most of them are dedicated to improving upon Cox PH. A common idea is to use deep neural networks to learn the non-linear relationship between the explanatory variables and outcome by optimizing the partial likelihood of Cox PH (Katzman et al., 2018). However, this is still restricted to the strong assumption of proportional hazard. Recently, a fully parametric method utilizing deep learning called Deep Survival Machines (DSM) (Nagpal et al., 2021) has attracted much attention. It does not make the PH assumption and can achieve competitive predictive performance compared to state-of-the-art methods. However, DSM learns different base distributions for each instance, making the model hard to interpret.

Clustering with Time-to-event Prediction. There are a few other methods that perform both clustering and time-to-event prediction simultaneously. For example, Survival Clustering Analysis (SCA) (Chapfuwa et al., 2020) assumes that the latent space is a mixture of distributions and uses the truncated Dirichlet process to automatically identify the number of clusters. However, SCA cannot control the number of clusters and thus cannot validate its advantages compared to post-hoc methods. Variational deep survival clustering (VaDeSC) (Manduchi et al., 2021), as a fully generative method, uses a Gaussian mixture distribution to model the features in a latent space and uses the Weibull distribution to model the survival timing information. This builds a good bridge between the features and survival information by jointly optimizing both likelihoods. However, there is a trade-off between the discriminative and generative learning paradigms. A fully generative framework may not be a good fit for all types of data since it is difficult to let both the features and survival information obey the prior assumption of their distributions at the same time. Neural Survival Clustering (Jeanselme et al., 2022) attempts to learn the survival probability for each instance by learning fixed neural networks. This framework brings more flexibility due to the lack of assumptions. However, the model needs large amounts of training data to prevent overfitting. Thus, the model may not be applicable to small-scale data, especially in the medical domain.

3. Preliminaries

3.1. Basic Notation

Survival analysis aims to estimate the probability of an event of interest happening after a certain time *t* based on the features *X* of individual subjects (Flynn, 2012). This probability can be modeled by a survival function $S(\cdot|X) = P(T > t|X)$. The data we tackled are assumed to be right-censored. This means our dataset $\mathcal{D}$ consists of tuples $\{\mathbf{x}_i, t_i, \delta_i\}_{i=1}^N$ where $\mathbf{x}_i$ is the feature vector for the *i*th subject, t_i is the last time we followed the *i*th subject, δ_i is the event indicator, and *N* is the number of all subjects. If $\delta_i = 1$, the event will occur at time t_i for the *i*th subject (this means the *i*th subject is uncensored). If $\delta_i = 0$, we lose the *i*th subject at time t_i , or the monitoring ended before the occurrence of the event (this means the *i*th subject is censored). We denote $\mathcal{D}_U$ as the uncensored subset and $\mathcal{D}_C$ as the censored subset.

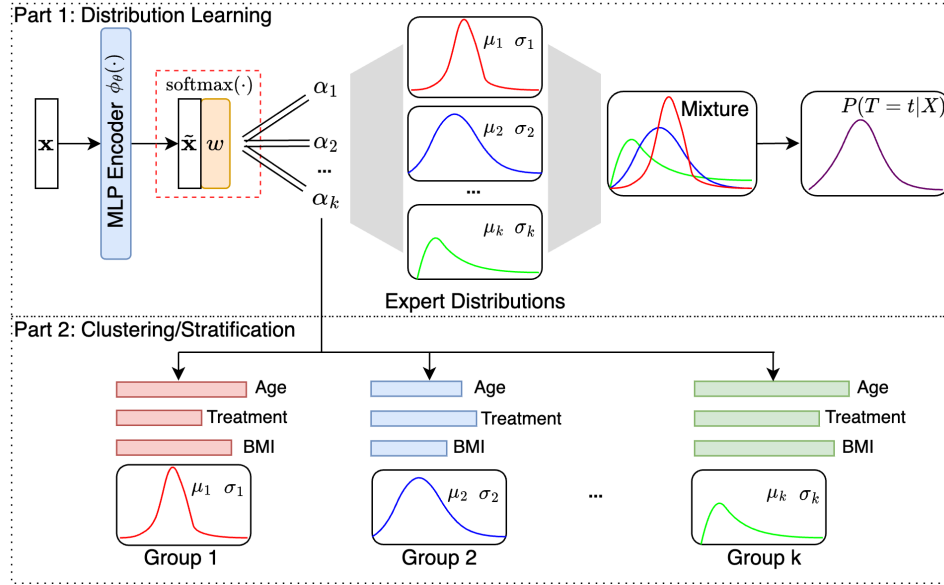


Fig. 1. Mechanism of DCSM.

3.2. Cox PH

Cox PH model (Cox, 1972) is the most popular and conventional survival model. It assumes proportional hazards, meaning the ratio of hazards of two subjects does not change over time. Suppose the parameter of the Cox PH model is β , then the hazard function at time t for the i th subject with feature vector $\mathbf{x}_i$ is

$$\lambda(t|\mathbf{x}_i) = \lambda_0(t) \exp(\mathbf{x}_i \cdot \beta), \quad (1)$$

where $\lambda_0(t)$ is the baseline hazard that describes how the risk of event per time unit changes over time at baseline level of features. To estimate the parameter β , Cox PH model uses the maximum likelihood estimation (MLE) to maximize the Cox partial likelihood:

$$L(\beta) = \prod_{i \in \mathcal{D}_U} \frac{\exp(\mathbf{x}_i \cdot \beta)}{\sum_{j: t_j \geq t_i} \exp(\mathbf{x}_j \cdot \beta)}. \quad (2)$$

By calculating the first and second derivative of this partial likelihood function, β can be obtained using the Newton-Raphson algorithm (Akram and Ann, 2015).

3.3. Deep Cox

The Deep Cox model (also called DeepSurv) (Katzman et al., 2018) is another solution for the Cox PH idea. As opposed to following the traditional solution of maximizing the partial likelihood mentioned above, Deep Cox attempts to leverage deep neural networks to learn a nonlinear mapping $\phi_\theta(\cdot)$ parameterized by θ for the features $\mathbf{x}_i$ and try to get the optimal predictive model by minimizing the negative logarithm of the partial likelihood as the loss function:

$$\ell(\beta) = - \sum_{i \in \mathcal{D}_U} \left(\phi_\theta(\mathbf{x}_i) - \log \sum_{j: t_j \geq t_i} \exp(\phi_\theta(\mathbf{x}_j)) \right). \quad (3)$$

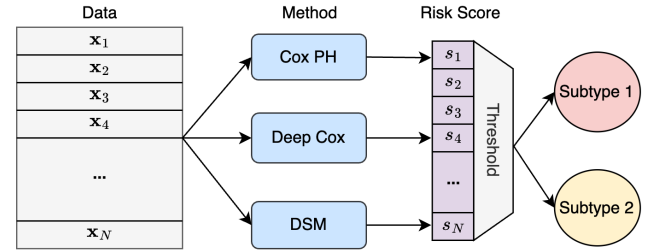


Fig. 2. Post-hoc clustering mechanism of Cox PH, Deep Cox, and DSM.

3.4. Clustering Mechanism

The clustering mechanism of *post-hoc* survival models is illustrated in Fig. 2. Cox PH, Deep Cox and DSM are used as *post-hoc* clustering methods in this paper. To cluster MCI patients, we first obtain their predicted risk scores, and then we set a threshold (usually the median or the mean of the whole risk scores) to get the subtypes. In our paper, it is important to emphasize that we concentrate on two distinct clusters: one associated with low risk and the other with high risk. Our primary objective is to provide valuable insights for patients and clinicians regarding the likelihood of developing AD (Alzheimer's disease). By identifying individuals at high risk, we can emphasize the need for early intervention or more customized treatment strategies. While high and low-risk clusters hold significant relevance, including an additional cluster such as medium risk would only introduce confusion for patients and clinicians, thereby detracting from the overall clarity and effectiveness of our findings.

4. Method

In Part 1 of Fig. 1, the deep clustering survival machines (DCSM) is designed to learn a conditional distribution $P(T|X =$

Table 1. Statistics of AD-related datasets used in the experiments. N refers to number of subjects. m refers to the number of brain regions. The time range t_{max} is noted in days. Education is noted in years.

Dataset	N	m	Event(%)	t_{max}	Age	Gender(M/F)	Education
AV45	466	116	33.52	2258	72.38±7.81	267/199	16.20±2.71
FDG	467	116	32.67	2254	72.36±7.81	266/201	16.18±2.71
VBM	462	116	32.00	2275	72.42±7.91	265/197	16.18±2.74

Table 2. Statistics of benchmark datasets used in the experiments. The time range t_{max} in PBC is noted in years while others are noted in days. “FRAM” refers to “FRAMINGHAM”.

Dataset	SUPPORT	PBC	FRAM	FLCHAIN
Events (%)	68.11	37.28	30.33	30.07
N	9105	1945	11627	6524
d (categorical)	44 (26)	25 (17)	18 (10)	8 (2)
t_{max}	2029	14.31	8766	5167

$\mathbf{x}$) by optimizing the maximum likelihood estimation (MLE) of the time T . Similar to the mixture model learning paradigm, the conditional distribution $P(T|X = \mathbf{x})$ is characterized by learning a mixture over K well-defined parametric distributions, referred to as *expert distributions*. In order to use gradient-based methods to optimize MLE, we choose the Weibull distributions as the expert distributions that are flexible to fit various distributions and have closed-form solutions for the PDF and CDF:

$$\text{PDF}(t) = \frac{\mu}{\sigma} \left(\frac{t}{\sigma} \right)^{\mu-1} e^{-\left(\frac{t}{\sigma}\right)^\mu}, \quad \text{CDF}(t) = e^{-\left(\frac{t}{\sigma}\right)^\mu}, \quad (4)$$

where μ and σ are the shape and scale parameters separately.

Part 1 of Fig. 1 indicates that we firstly need to learn an encoder for the input features $\mathbf{x}$ to obtain a compact and informative representation $\tilde{\mathbf{x}}$. Here we use a multi-layer perceptron (MLP) $\phi_\theta(\cdot)$ parameterized by θ as the backbone model. This representation will be multiplied by a parameter w with softmax to obtain the mixture weight α_k with respect to each (k th) expert distribution that is parameterized by μ_k and σ_k . The final survival distribution for the time T conditioned on each instance is a weighted combination over all K constant expert distributions. Eventually, we have a set of parameters $\Theta = \{\theta, w, \{\mu_k, \sigma_k\}_{k=1}^K\}$ to learn during the training process. Because μ_k and σ_k are the same for different input instances, we can cluster each instance/subject according to the weight α_k that is allocated to each expert distribution, as illustrated in Part 2 of Fig. 1. Specifically, we assign an subgroup/cluster indicator i to each instance when the instance’s corresponding weight α_i is the largest among all K weights.

According to the framework of MLE, our goal is to maximize the likelihood with respect to the timing information T conditioned on $\mathbf{x}$. Given that the likelihood functions are different for uncensored and censored data, we calculate them separately. For the uncensored data, the log-likelihood of T is computed as follows, where α is the hidden variable and **ELBO** is the lower

bound of the likelihood derived by Jensen’s Inequality:

$$\begin{aligned} \ln \mathbb{P}(\mathcal{D}_U|\Theta) &= \ln \left(\prod_{i=1}^{|\mathcal{D}_U|} \mathbb{P}(T = t_i | X = \mathbf{x}_i, \Theta) \right) \\ &= \sum_{i=1}^{|\mathcal{D}_U|} \ln \left(\sum_{k=1}^K \mathbb{P}(T = t_i | \alpha, \mu_k, \sigma_k) \mathbb{P}(\alpha | X = \mathbf{x}_i, w) \right) \\ &= \sum_{i=1}^{|\mathcal{D}_U|} \ln \left(\mathbb{E}_{\alpha \sim (\cdot|\mathbf{x}_i, w)} [\mathbb{P}(T = t_i | \alpha, \mu_k, \sigma_k)] \right) \\ &\geq \sum_{i=1}^{|\mathcal{D}_U|} \left(\mathbb{E}_{\alpha \sim (\cdot|\mathbf{x}_i, w)} [\ln \mathbb{P}(T = t_i | \alpha, \mu_k, \sigma_k)] \right) \\ &= \sum_{i=1}^{|\mathcal{D}_U|} \left(\text{softmax}_K(\ln \text{PDF}(t_i | \mu_k, \sigma_k)) \right) = \mathbf{ELBO}_U(\Theta). \end{aligned} \quad (5)$$

Similarly, the log-likelihood of T for the censored data is:

$$\begin{aligned} \ln \mathbb{P}(\mathcal{D}_C|\Theta) &= \ln \left(\prod_{i=1}^{|\mathcal{D}_C|} \mathbb{P}(T > t_i | X = \mathbf{x}_i, \Theta) \right) \\ &\geq \sum_{i=1}^{|\mathcal{D}_C|} \left(\mathbb{E}_{\alpha \sim (\cdot|\mathbf{x}_i, w)} [\ln \mathbb{P}(T > t_i | \alpha, \mu_k, \sigma_k)] \right) \\ &= \sum_{i=1}^{|\mathcal{D}_C|} \left(\text{softmax}_K(\ln \text{CDF}(t_i | \mu_k, \sigma_k)) \right) = \mathbf{ELBO}_C(\Theta). \end{aligned} \quad (6)$$

In addition, to stabilize the performance, we incorporate prior knowledge for μ_k and σ_k . Specifically, we minimize the prior loss L_{prior} to make them as close as possible to the prior μ and σ that are determined by the MLE result for a single expert distribution:

$$L_{prior} = \sum_{k=1}^K \|\mu_k - \mu\|_2^2 + \|\sigma_k - \sigma\|_2^2. \quad (7)$$

The final objective L_{all} is the sum of the negative of the log-likelihoods of both the uncensored and censored data in addition to the prior loss where λ is a trade-off hyperparameter:

$$L_{all} = L_{prior} - \mathbf{ELBO}_U(\Theta) - \lambda \cdot \mathbf{ELBO}_C(\Theta). \quad (8)$$

5. Experiments

In this section, we first introduce the datasets we used in the experiments. This includes three popular AD-related datasets, four benchmark datasets, and a group of genotyping data relevant to AD. Then, we introduce the metrics, baselines, and settings in our experiments. Finally, we report and discuss the LogRank, C-index, genetic association analysis, and interpretability results.

5.1. Datasets

The genotyping data, demographic data and imaging data used in our experiments were obtained from the Alzheimer’s Disease Neuroimaging Initiative (ADNI) database (Weiner et al., 2017). ADNI was launched in 2003 as a public-private partnership, led by Principal Investigator Michael W. Weiner,

MD. The primary goal of ADNI has been to test whether serial magnetic resonance imaging (MRI), positron emission tomography (PET), other biological markers, and clinical and neuropsychological assessment can be combined to measure the progression of mild cognitive impairment (MCI) and early Alzheimer's disease (AD). Up-to-date information about the ADNI database is available at www.adni-info.org.

We focused our analysis on three ADNI imaging modalities:

- AV45: Florbetapir PET (Jagust et al., 2015) that measures amyloid burden.
- FDG: Fluorodeoxyglucose PET (Jagust et al., 2010) which measures glucose metabolism.
- VBM: Structural magnetic resonance imaging (MRI) (Jack et al., 2015) measuring brain morphometry.

Structural MRI scans were processed with voxel-based morphometry (VBM) using the statistical parametric mapping software tool (Ashburner and Friston, 2000). The MarsBaR region of interest (ROI) toolbox (Tzourio-Mazoyer et al., 2002) was used to extract mean gray matter density, amyloid, and FDG-PET glucose utilization values for each ROI. After extraction, there were 116 ROI-level measures for each modality. All the MCI participants with no missing data were analyzed, and we had $N = 466$ for AV45, $N = 467$ for FDG, and $N = 462$ for VBM. Their characteristics are summarized in Table 1.

For the genetics data, we first downloaded genotyping data from ADNI 1, GO, 2, and 3 studies from the ADNI database (Shen et al., 2014; Saykin et al., 2015; Shen and Thompson, 2020). Then, McCarthy Group Tools (<https://www.well.ox.ac.uk/~wrayner/tools/>) were used for alignment. We aligned the genotyping data to the Homo Sapiens (human) genome assembly NCBI37 (hg19) genome builder, according to 1000 Genome phase 3 dataset (1000 Genomes Project Consortium et al., 2015). To complement the missing data, we imputed those genotypes using the Michigan Imputation Server (Das et al., 2016) with the 1000 Genome phase 3 reference panel of European ancestry. We annotated our imputed genotyping data using ANNOVAR (Wang et al., 2010). After alignment and imputation, we performed the quality control (QC) using the following criteria: genotyping call rate $> 98\%$, minor allele frequency $> 0.1\%$, Hardy-Weinberg Equilibrium $> 1e-6$, missingness per individual $< 5\%$. All the QC was performed using PLINK 1.9 (Chang et al., 2015).

To further validate the effectiveness of the proposed method, we also conducted experiments on four public benchmark datasets that are all real-world datasets:

- SUPPORT (Knaus et al., 1995): The SUPPORT dataset is sourced from a study conducted by Vanderbilt University that aims to estimate the survival rate of seriously ill adults who are hospitalized.
- PBC (Fleming and Harrington, 2013): The dataset known as Primary Biliary Cirrhosis is commonly used to assess the performance of survival analysis models that incorporate time-dependent covariates.

Table 3. LogRank results comparison between KMeans, Cox, Deep Cox, DSM, SCA, VaDeSC, NSC and DCSM on dataset AV45, FDG and VBM. The best one in each block (for specific metric and dataset) is bold.

Methods	AV45	FDG	VBM
KMeans	66.96±1.75	28.84±1.36	16.17±1.01
Cox PH	133.60±3.65	117.80±1.88	89.07±3.97
Deep Cox	121.49±10.99	95.39±16.07	63.49±2.76
DSM	160.62±3.79	124.26±1.74	120.41±2.47
SCA	40.10±26.47	18.15±8.94	4.71±3.41
VaDeSC	108.43±131.86	133.69±203.21	282.08±157.12
NSC	160.88±52.13	213.61±82.60	65.52±27.65
DCSM	317.84±31.89	384.62±24.03	369.29±26.87

Table 4. C-Index results comparison between KMeans, Cox, Deep Cox, DSM, SCA, VaDeSC, NSC and DCSM on dataset AV45, FDG and VBM. The best one in each block (for specific metric and dataset) is bold.

Methods	AV45	FDG	VBM
Cox PH	0.6900±0.0349	0.6864±0.0552	0.6435±0.0602
Deep Cox	0.7683±0.0240	0.7659±0.0308	0.6688±0.0242
DSM	0.7845±0.0421	0.7518±0.0317	0.7181±0.0290
SCA	0.7166±0.0653	0.6609±0.1011	0.6049±0.0676
VaDeSC	0.4166±0.0315	0.4120±0.0314	0.5187±0.0366
NSC	0.7742±0.0239	0.7174±0.0529	0.6872±0.0219
DCSM	0.7708±0.0297	0.7764±0.0413	0.6801±0.0575

- FRAMINGHAM (Dawber et al., 1951): The Framingham dataset consists of 4,434 participants from the well-known and ongoing Framingham Heart study. This dataset is utilized for studying the epidemiology of hypertensive and arteriosclerotic cardiovascular disease.
- FLCHAIN (Kyle et al., 2006): This dataset is a mix of different people, and half of the subjects from a study analyzing the correlation between serum free light chain (FLC) and mortality. The original sample covers around two-thirds of Olmsted County's residents aged 50 or above.

The statistics of the four benchmark datasets are summarized in Table 2.

5.2. Metrics, Baselines and Settings

We use "LogRank" to evaluate the clustering performance of all the methods. LogRank is a statistical test that compares the survival curves of two or more groups of subjects (Mantel et al., 1966) and is popular and widely used for survival analysis. It tests whether or not there is a significant difference in survival between the groups. It is calculated by comparing the observed and expected number of events in each group under the null hypothesis of no difference. To further validate the efficacy of our framework, we also use genetic association analysis to evaluate the clustering results. We want to identify the genetic basis of different AD subtypes to validate our subtype findings.

Rather than that, we also incorporate "Concordance Index" (C-Index) (Harrell et al., 1982) as an additional metric to evaluate the time-to-event prediction performance. The C-Index is a widely used measure in survival analysis. It measures how well the order of survival times matches with predictions made by

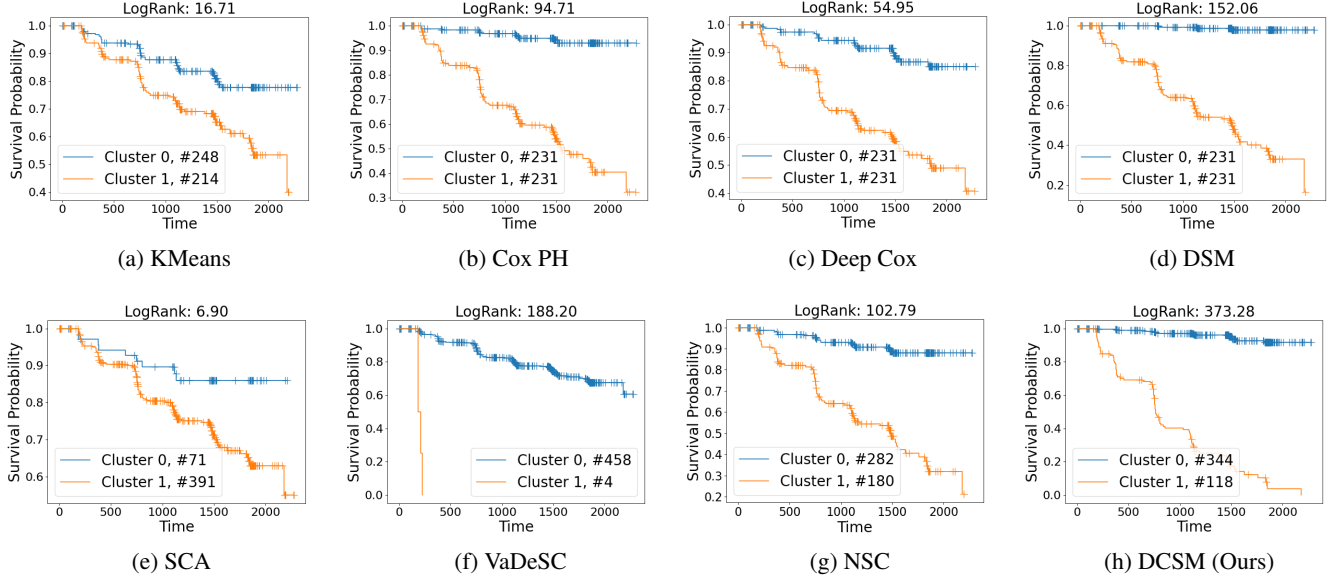


Fig. 3. The Kaplan-Meier plots of KMeans, Cox PH, Deep Cox, DSM, DCSM, SCA, Vadesec on dataset VBM. The cross mark on the curve means censoring. Cluster 0 means low-risk group while Cluster 1 means high-risk group.

models. Note that the time-to-event prediction is actually not our goal. Our DCSM method is specifically designed for clustering and it is sufficient if we our method can achieve state-of-the-art clustering results and behave reasonably well regarding time-to-event prediction.

For the clustering task, we compare our method with seven baseline methods, which are either conventional or state-of-the-art:

- KMeans (Hartigan and Wong, 1979): a traditional and popular clustering method that iteratively updates the clustering means and cluster assignments.
- Cox PH (Cox, 1972): a classic survival model for survival risk prediction, which assumes that the hazard rate for each instance, known as the proportional hazard (PH), is constant over time.
- Deep Cox (Katzman et al., 2018): a deep learning variant of Cox PH that uses Cox PH loss to optimize the parameters of deep neural networks, also called DeepSurv.
- DSM (Nagpal et al., 2021): the Deep Survival Machines model learns different base distributions for different instances using specified prior distributions.
- SCA (Chapfuwa et al., 2020): the Survival Clustering Analysis model assumes that the latent space is a mixture of distributions and uses the truncated Dirichlet process to realize the automatic identification of the number of clusters.
- VaDeSC (Manduchi et al., 2021): the Variational Deep Survival Clustering model uses a Gaussian mixture distribution to model the features in a latent space and uses the Weibull distribution to model the survival timing information.

- NSC (Jeanselme et al., 2022): Neural Survival Clustering is a discriminative variant of DSM that uses neural networks to model the base distributions for each instance.

For Cox PH, Deep Cox, and DSM, we use the mean of all the risk scores as the threshold. In order to demonstrate the difference between the clustering effectiveness of unsupervised learning and semi-supervised learning methods, we also incorporate KMeans (Hartigan and Wong, 1979) as the baseline besides the six survival models to discover the subtypes. For the time-to-event prediction task, we only report the results of all the survival models mentioned above without KMeans.

To obtain the clustering results, we follow the common practice of training and testing on the entire dataset, similar to how other typical clustering methods operate. After training, we down-sampled the testing data (95% are sampled randomly) five times and obtained the average LogRank values along with the standard deviation over the five runs. For time-to-event prediction, we train on 70% data and test on the other 30% data. All the hyperparameters are chosen through grid search. Specifically, the trade-off parameter λ was chosen from [0.5, 0.75, 1], and the learning parameter step size was chosen from [1e-2, 1e-3, 1e-4]. The layer setting of the multiple perceptron was chosen from [[], [50], [50, 50]] where “50” is the number of neurons in each hidden layer and “[]” means there are no hidden layers and the MLP will become a vanilla neural networks with only input and output layers.

5.3. Results on ADNI

5.3.1. LogRank Results

Table 3 gives the LogRank comparison between KMeans, Cox PH, Deep Cox, DSM, SCA, VaDeSC, NSC, and DCSM on the AV45, FDG, and VBM datasets. We can see that KMeans, which merely uses the feature information, achieves the lowest LogRank compared to other survival models excluding SCA.

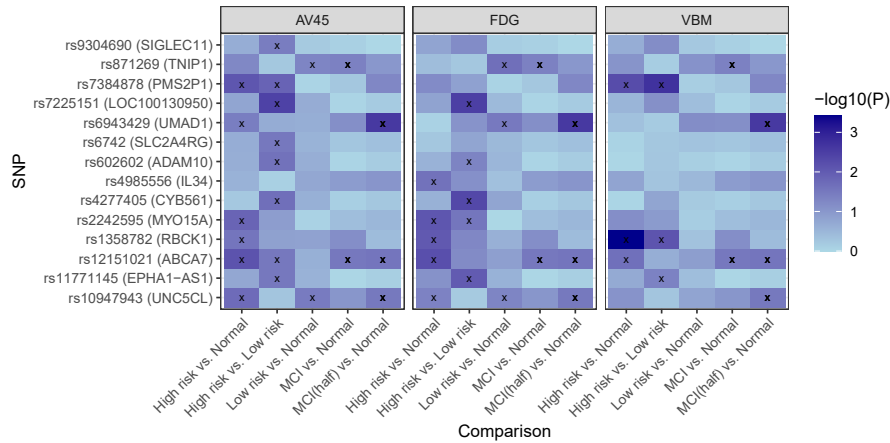


Fig. 4. Targeted genetic association results of DCSM. In the parentheses of the vertical label is the name of the gene closest to the corresponding SNP. The darkness of each blue patch represents the negative logarithm of p -value regarding each SNP. The darker the patch is, the more significant the SNP is. “x” marker on the patch means the SNP is statistically significant after FDR correction. This figure indicates the discrepancy between the high-risk group and the normal group is as large as the discrepancy between the high-risk group and the low-risk group, which reassures the performance of our DCSM algorithm.

SCA cannot explicitly control the number of clusters. It usually sets the upper bound of the number of clusters as 25 and uses the Dirichlet process to automatically identify the number of clusters, which makes it difficult to compare to other baselines. To have a fair comparison, we set the upper bound of the number of clusters as 2 for SCA which results in poor clustering performance. Overall, the results in Table 3 demonstrate that incorporating partial survival information allows survival models to better stratify the groups such that the survival differences between the subgroups are larger than their unsupervised counterparts. DCSM, specifically designed for survival clustering, obtains the highest LogRank results out of all the baseline methods.

To make the results more intuitive, we also provide the corresponding Kaplan-Meier (KM) plots that are shown in Fig. 3. We only provide the KM plots on the VBM dataset. Other similar results are deferred to the Appendix. In general, the smaller the LogRank, the closer the two survival curves. From Fig. 3 we can see that the two survival curves of KMeans are closer to each other compared to survival models. This shows that survival models can more effectively stratify individuals into different subgroups with respect to MCI converting to AD. Note that the two curves of DCSM are farthest apart from each other compared to the other methods with the exception of VaDeSC. The two curves of VaDeSC are farther from each other than DCSM, but the number of patients in Cluster 1 (with high risk) is only 4 which means that the two clusters are very imbalanced and thus not effectively stratified. In addition, the cross marks on the curves indicate censoring, i.e., we do not observe the event of MCI converting to AD. Thus it should be with high probability that the censored samples have low risk to convert to AD. Therefore, we expect that a good clustering results should stratify more censored individuals to the low-risk group. We can see that in the curve of Cluster 1 (with high risk) of DCSM, the number of cross marks is small while most of the censored samples are on the low-risk curve (Cluster 0). This validates the effectiveness of DCSM.

5.3.2. C-Index Results

Our primary focus lies in clustering and subtype discovery, but we also evaluate the time-to-event prediction performance of DCSM in comparison to other methods with the exception of KMeans which is not able to do time-to-event (risk) prediction. To achieve this, we employ five-fold cross-validation, training on 70% of the data and testing on the remaining 30%. The results are summarized in Table 4. Notably, our method demonstrates superior performance compared to other approaches on the FDG dataset, while maintaining competitive results on the other datasets. It is important to emphasize that our method is not specifically optimized for risk prediction; rather, our primary goal is to enhance clustering performance. In this context, the observed outcome is considered acceptable.

5.3.3. Genetic Association Results

To biologically validate our clustering findings derived from the proposed DCSM, we carried out targeted genetic association analyses. Specifically, we first prioritized 57 single nucleotide polymorphism (SNP) variants from ADNI 1, GO, 2, 3 studies using the list of AD loci with genetic evidence compiled by the Alzheimer’s Disease Sequencing Project (ADSP) Gene Verification Committee.⁵ These genetic variants have been well-studied and verified to affect AD risk. Then, we conducted genetic association analyses on the subtypes of “High risk vs. Normal”, “High risk vs. Low risk”, “Low risk vs. Normal”, “MCI vs. Normal”, and “MCI (half) vs. Normal”, where we use half of the MCI subjects (randomly selected) to make the comparison fairer, as the number of subjects in this group is closer to the high-risk, low-risk, and normal groups. In our approach, we employed univariate logistic regression models, designating the risk of AD onset as the dependent variables and individual autosomal SNP variants as independent variables. To account for the potential confounding factors, we adjust our

⁵<https://adsp.niagads.org/gvc-top-hits-list/>

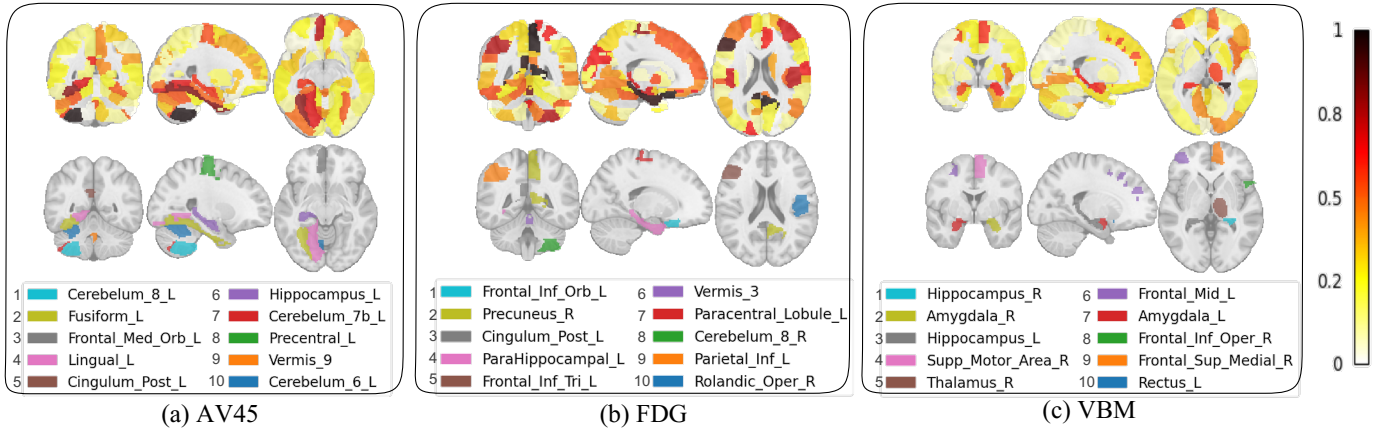


Fig. 5. Brain heat map of AV45, FDG, and VBM using the coefficient of our DCSM model. Each dataset includes three slices to display the brain region extensively. The heat maps in the first row showcase all the brain regions of interest, where darker colors represent greater importance for risk prediction. The second row highlights the top ten significant brain regions in each dataset, which are annotated in the legends in the third row.

model with age, sex, and population structure captured by the first 10 principal components obtained from genotyping data. We use the false discovery rate (FDR) to correct the multiple comparison problems. The software used to perform the association analyses was PLINK1.9 (Chang et al., 2015).

As shown in Fig. 4, we find more significant SNPs in the first two columns than in the last three columns of each dataset. This indicates that the discrepancy between the high-risk group and the normal group is as large as the discrepancy between the high-risk group and the low-risk group. In contrast, the discrepancy between the low-risk group and the normal group, as well as between the whole MCI group and the normal group, is much smaller. This is reasonable since the high-risk group should be significantly different from other groups such as the low-risk group or the normal group, while the discrepancy between other groups should be small. These results validate the efficacy of our DCSM clustering framework, where we successfully identified the high-risk group that should be treated more carefully. Our study underscores the robustness of our clustering findings and contributes to a better understanding of the genetic foundations of AD risk subtypes.

We also showcase the targeted genetic association analysis results of all the methods in Fig. B.9 for a comprehensive comparison in the Appendix. We expect to identify more significant SNPs in the first two columns of each block for each dataset. To clearly compare them, we sum up the number of “x” markers in the first two columns for each method. Based on this, KMeans has 24, Cox PH has 20, Deep Cox has 23, DSM has 22, SCA has 16, Vades has 0, NSC has 29 and our DCSM has 30, which demonstrates the superiority of the proposed method.

5.4. Interpretability Study

Fig. 5 shows the important brain regions that DCSM pays attention to. The first row shows the AD risk importance of all the regions, the darker the color is, the more important. The second row highlights the top ten important regions for each modality. For AV45 data, our method demonstrates high importance for AD risk prediction on the left fusiform, medial

orbitofrontal, posterior cingulate, and precentral gyri. A significant abnormality in amyloid levels has been observed in the medial orbitofrontal cortex in AD patients (Collij et al., 2020). This region is associated with the episodic memory and simulation network and is very susceptible to aging (Fjell et al., 2014). Additionally, amyloid accumulation and gray matter atrophy occur simultaneously in AD patients in the fusiform gyrus (Chang et al., 2016). Furthermore, many studies have reported a significantly increased amyloid level in posterior cingulate Huang et al. (2013); Collij et al. (2020), and the amyloid accumulation is related to the executive function and memory decline Ali et al. (2022). It is evident from the FDG data that the posterior cingulate and the precuneus gyri are two potential AD biomarkers, which is consistent with prior studies showing severe hypometabolism reductions in MCI and AD patients Bailly et al. (2015). Moreover, the reduction of metabolism caused by AD starts from the posterior cingulate cortex and gradually spreads to the frontal lobe such as the orbitofrontal gyrus Mosconi (2005); Bailly et al. (2015). For VBM data, the right hippocampus demonstrates the highest importance, and bilaterally hippocampus and amygdala regions all show a high risk of AD. The hippocampal neurons register places and people in memory, while the amygdala activates related cortical areas to modulate recognition Petrovic et al. (2008). The atrophy of the hippocampus is widely considered as the AD biomarker for early detection citedhikav2011potential, and the study found that amygdala atrophy is related to hippocampus atrophy and global AD severity Poulin et al. (2011). These results also provide directions for discovering potential AD biomarkers.

The Kaplan-Meier plot of DCSM on the PBC benchmark dataset is displayed in Fig. 6. The plot is accompanied by CDF (Cumulative Density Function) curves for expert distributions, which demonstrate interpretability. Notably, the shapes of the two expert distributions closely resemble the Kaplan-Meier curves, offering an intuitive insight into how the expert distributions within the DCSM model effectively steer the patient clustering process and validate the robustness of data stratification. This alignment between the expert distributions and

Table 5. C Index and LogRank results compared to Cox PH, Deep Cox, DSM, SCA, and VaDeSC. The best ones are bold.

Metric	Method	SUPPORT	PBC	FRAMINGHAM	FLCHAIN
C Index	Cox PH	0.8401±0.0070	0.8476±0.0126	0.7580±0.0063	0.7984±0.0046
	Deep Cox	0.8053±0.0058	0.8474±0.0181	0.7612±0.0057	0.7893±0.0063
	DSM	0.8300±0.0045	0.8363±0.0133	0.7593±0.0050	0.8009±0.0036
	SCA	0.8203±0.0121	0.8251±0.0258	0.5311±0.1235	0.7467±0.0091
	VaDeSC	0.8419±0.0041	0.8278±0.0085	0.5802±0.0406	0.7886±0.0100
	NSC	0.8146±0.0072	0.8178±0.0275	0.7396±0.0175	0.7980±0.0052
	DCSM (Ours)	0.8305±0.0028	0.8359±0.0109	0.7530±0.0053	0.7916±0.0074
LogRank	Cox PH	500.3282±60.4977	198.2686±17.3940	576.1450±22.9621	399.0243±25.7657
	Deep Cox	326.1931±54.7026	203.3091±22.8343	593.7317±14.4697	403.4643±35.8034
	DSM	563.4841±0.0045	196.0912±0.0133	587.5718±0.0050	406.4549±0.0036
	SCA	212.5712±26.2629	260.5682±67.4875	278.3525±51.1866	536.1056±109.1680
	VaDeSC	196.8495±19.6887	118.9605±77.4716	348.5500±697.1000	95.5291±108.9488
	NSC	416.4572±31.9528	300.5617±21.3671	313.3190±41.8324	713.7871±40.9787
	DCSM (Ours)	1067.6184±271.6551	302.5395±30.1043	751.9770±48.9725	571.0441±99.0101

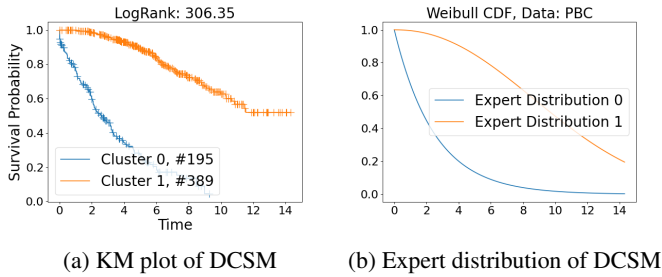


Fig. 6. (a) The Kaplan-Meier plots of DCSM on data PBC. The cross mark indicates censoring. The learned expert distributions are shown in (b). The shape of the two expert distributions resembles our Kaplan-Meier curves, facilitating effective data stratification.

the Kaplan-Meier curves further reinforces the efficacy of our approach.

5.5. Results on Benchmark Datasets

Table 5 shows the C Index values on real data, including the average results of five independent runs and their standard deviations. These results indicate that our method achieves competitive performance compared to other baselines. Although our model's performance was not the best on some datasets, the difference between the results of DCSM and the best-performing model are not significant at a 95% confidence interval.

Table 5 also summarizes the results of the LogRank tests. The LogRank statistic evaluates how well the clustering results with regard to the survival information. A larger value indicates better performance. The results demonstrate that our method outperforms all the baselines on SUPPORT, PBC and FRAMINGHAM and secure the second position on FLCHAIN. This could be more useful than the time-to-event prediction because such information can facilitate personalized treatment planning. Clinicians may not be able to decide how to provide customized treatment merely based on the risk predictions. Instead, clustering results more intuitively differentiate the patients into groups, enabling more informed clinical decision-making.

6. Discussion

Generative and discriminative approaches each have their own strengths and weaknesses. Typically, a generative model assumes that the data follows a specific distribution, like Gaussian or Weibull distributions. This means that the model can be trained effectively even with a relatively small amount of data, as long as the data matches the assumed distribution. However, if the actual data doesn't match this assumption, the resulting model could be biased and lose its ability to work well in different situations. For instance, consider the VaDeSC Manduchi et al. (2021) model mentioned in our paper. It is a fully generative model that makes assumptions about both the features and the survival information in the data. If either of these assumptions is not satisfied, the model will be inferior. Discriminative models, on the other hand, do not make any assumptions about the data distribution. This means that they can learn the true pattern from the data, even if the data is not well-behaved. However, this approach often requires larger amounts of data to find the right parameters for the model. An example of a discriminative model is NSC Jeanselme et al. (2022). NSC is a fully discriminative method that does not make any assumptions about the data. However, if the sample size is small, the model may not be able to learn the true pattern from the data.

A combination of discriminative and generative mechanisms can mitigate the drawbacks of both approaches. In our case, we do not make any assumptions about the features, as we believe that the distribution of features can vary from case to case. Making assumptions about the features can limit the model's capability. Instead, we assume that the survival information follows the Weibull distribution, which is a commonly used distribution for modeling survival timing data. The Weibull distribution is flexible in that it can mimic different distributions with different shapes and scales. For example, when the shape parameter is close to 3, the Weibull distribution approximates a normal distribution. When the shape parameter is equal to 1, the Weibull distribution is equivalent to a two-parameter exponential distribution. Therefore, the Weibull distribution is a suitable choice for modeling survival timing information. Our method also has

its own limitations. For example, if the number of samples is limited, the feature information may not be learned well. This is a common problem in the medical domain, where data is often scarce. This may be the reason why DCSM does not outperform the baseline methods in time-to-event prediction tasks. Additionally, if the survival timing data are too skewed to be modeled by the Weibull distribution, the model's performance may also be degraded. There is no perfect method that can fit all cases. However, by combining discriminative and generative mechanisms, we can develop more robust models that can handle a wider range of data distributions.

Finally, we want to emphasize that we only focus on two clusters for Alzheimer's disease (AD) subtype discovery in this study. One subtype is associated with a low risk of developing AD, and the other is associated with a high risk. Our goal is to help patients and clinicians understand their risk of developing AD. By identifying people who are at high risk, we can emphasize the need for early intervention or more customized treatment. While the high- and low-risk clusters are important, adding a medium-risk cluster would only confuse patients and clinicians. This would make our findings less clear and effective.

7. Conclusion

In this paper, we have proposed a deep hybrid method that integrates the discriminative and generative strategies into one framework. Assuming the survival function for each instance is a weighted combination of constant expert distributions, our method is capable of learning the weight for each expert distribution discriminatively and the distribution of the survival information generatively. We demonstrate our method's superiority by applying it to Alzheimer's disease subtype discovery. Genetic association studies along with feature importance analysis further validate the effectiveness of our proposed method.

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Appendix

In this appendix, we provide additional experimental results including the Kaplan-Meier plots for dataset AV45 and FDG. We also exhibit the targeted genetic association analyses for all the methods on all the ADNI datasets. Finally, we provide the statistics of low- and high-risk groups with respect to Age, Education and Gender and use histogram to illustrate the difference between low- and high-risk groups.

Appendix A. KM Plot on AV45 and FDG

In Fig. A.7 and Fig. A.8 we provide the Kaplan-Meier (KM) plots that corresponds to Table 3. The smaller the LogRank, the closer the two survival curves. As can be seen, the two survival curves of KMeans are closer to each other compared to survival models. This shows that survival models can more effectively stratify people into different subgroups with respect to MCI converting to AD. Especially, the two curves of DCSM are farthest apart from each other. You may notice that the two curves of VaDeSC are farther to each other than ours, but the number of patients in cluster 1 is only 5 and 6 in Fig. A.7 and Fig. A.8 respectively, which means that the two clusters are very imbalanced. In addition, the cross mark on the curve indicates censoring and it indicates that we do not observe the event of MCI converting to AD happens. Thus it is with high probability that the censored samples have low risk to convert to AD. We can see that in the curve of Cluster 1 of DCSM, the number of cross marks is small while most of the censored samples are on the low risk data. This validates the effectiveness of DCSM as well.

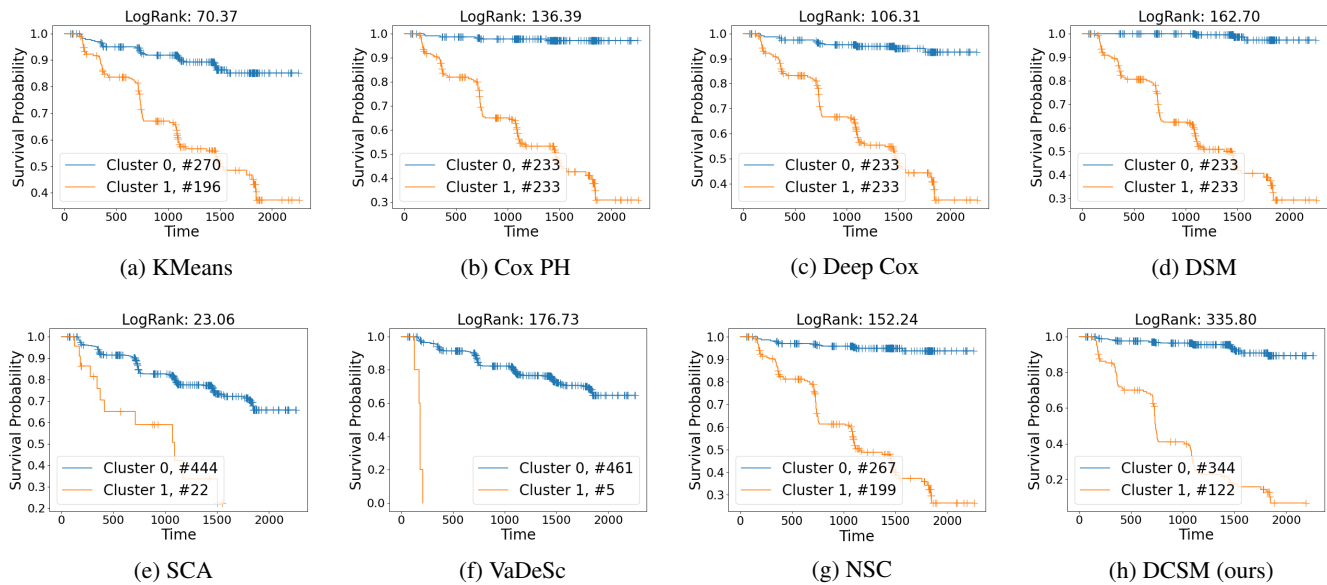


Fig. A.7. The Kaplan-Meier plots of KMeans, Cox PH, Deep Cox, DSM, SCA, Vades, NSC and DCSM on dataset AV45 of one run. The cross mark on the curve means censoring. Cluster 0 means low-risk group while Cluster 1 means high-risk group.

Appendix B. Targeted genetic association analyses for other clustering methods

In Fig. B.9, we provide the targeted genetic association analysis results of all the methods. We expect to identify more significant SNPs in the first two columns of each block for each dataset. To clearly compare them, we sum up the number of “x” markers in the first two columns for each method. Based on this, KMeans has 24, Cox PH has 20, Deep Cox has 23, DSM has 22, SCA has 16, Vades has 0, NSC has 29 and our DCSM has 30, which demonstrates the superiority of the proposed method.

Appendix C. Statistics Regarding Age, Education and Sex

We provide the statistics of high- and low-risk groups with respect to Age, Education and Gender and use histogram to illustrate the difference between low- and high-risk groups. Table C.6 summarizes the subject characteristics of high- and low-risk group clustered by all methods. Fig. C.10-C.12 shows the histogram of all methods. We find that the average age of subjects in high-risk group are higher than that in low-risk group. This is reasonable since older people are more risky to have cognition impairment. Besides, the cluster results indicates that more education time could reduce the risk to be diagnosed to be AD. Finally, for AV45 and FDG datasets, the ratio of high risk and low risk in female group are smaller than that in male group, while for VBM dataset, the ratio of high risk and low risk in female group are larger than that in male group.

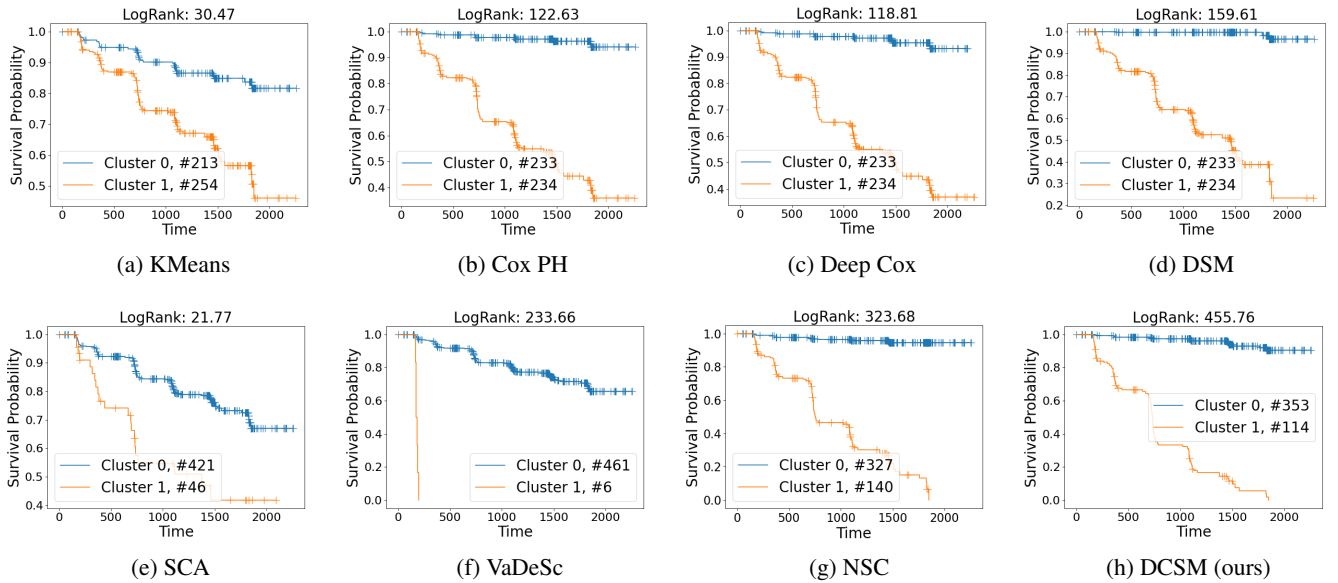


Fig. A.8. The Kaplan-Meier plots of KMeans, Cox PH, Deep Cox, DSM, SCA, Vadesec, NSC and DCSM on dataset FDG of one run. The cross mark on the curve means censoring. Cluster 0 means low-risk group while Cluster 1 means high-risk group.

Table C.6. Subject characteristics of high- and low-risk group clustered by all methods.

Dataset	Method	Age		Education		Gender (M / F)	
Risk Group		High risk	Low risk	High risk	Low risk	High risk	Low risk
AV45	KMeans	73.67±6.78	70.82±7.71	16.03±2.84	16.28±2.63	126 / 69	140 / 129
	Cox PH	73.03±7.15	70.99±7.64	16.06±2.86	16.29±2.57	140 / 93	126 / 105
	Deep Cox	73.32±6.92	70.73±7.76	16.04±2.88	16.31±2.55	136 / 95	130 / 103
	DSM	73.18±7.15	70.85±7.59	15.99±2.81	16.36±2.62	133 / 99	133 / 99
	SCA	73.56±4.69	71.94±7.57	15.59±2.84	16.20±2.71	13 / 9	253 / 189
	VaDeSC	73.96±5.53	71.99±7.48	16.80±1.10	16.16±2.74	4 / 1	262 / 197
	NSC	72.98±7.42	71.31±7.43	16.04±2.82	16.27±2.65	114 / 83	152 / 115
	DCSM	73.67±6.99	71.43±7.54	15.93±2.73	16.26±2.71	69 / 52	197 / 146
FDG	KMeans	74.67±6.69	68.85±7.09	15.86±2.83	16.50±2.55	154 / 99	111 / 101
	Cox PH	73.67±7.25	70.35±7.30	15.97±2.89	16.33±2.54	134 / 99	131 / 101
	Deep Cox	73.42±7.22	70.60±7.44	15.86±2.86	16.44±2.55	137 / 96	128 / 104
	DSM	72.82±7.19	71.20±7.64	16.16±2.80	16.14±2.65	141 / 92	124 / 108
	SCA	75.79±7.04	71.60±7.39	15.48±2.76	16.22±2.71	25 / 21	240 / 179
	VaDeSC	73.82±7.87	71.99±7.46	16.67±1.03	16.14±2.74	5 / 1	260 / 199
	NSC	71.51±7.41	72.23±7.48	16.31±2.68	16.08±2.74	78 / 61	187 / 139
	DCSM	73.40±7.09	71.56±7.52	15.99±2.67	16.20±2.74	62 / 51	203 / 149
VBM	KMeans	75.33±6.60	69.01±6.90	15.91±2.85	16.37±2.66	136 / 78	128 / 118
	Cox PH	73.46±7.29	70.44±7.32	16.19±2.76	16.12±2.77	138 / 92	126 / 104
	Deep Cox	73.46±7.38	70.45±7.23	16.20±2.79	16.11±2.74	131 / 99	133 / 97
	DSM	73.44±7.40	70.47±7.23	16.13±2.84	16.18±2.68	138 / 92	126 / 104
	SCA	73.25±7.07	64.82±5.15	16.12±2.80	16.34±2.53	242 / 147	22 / 49
	VaDeSC	74.45±9.38	71.93±7.45	17.50±1.91	16.14±2.76	1 / 3	263 / 193
	NSC	71.24±7.02	72.41±7.70	16.07±2.70	16.21±2.80	103 / 76	161 / 120
	DCSM	74.24±6.70	71.17±7.55	16.30±2.63	16.10±2.80	72 / 45	192 / 151

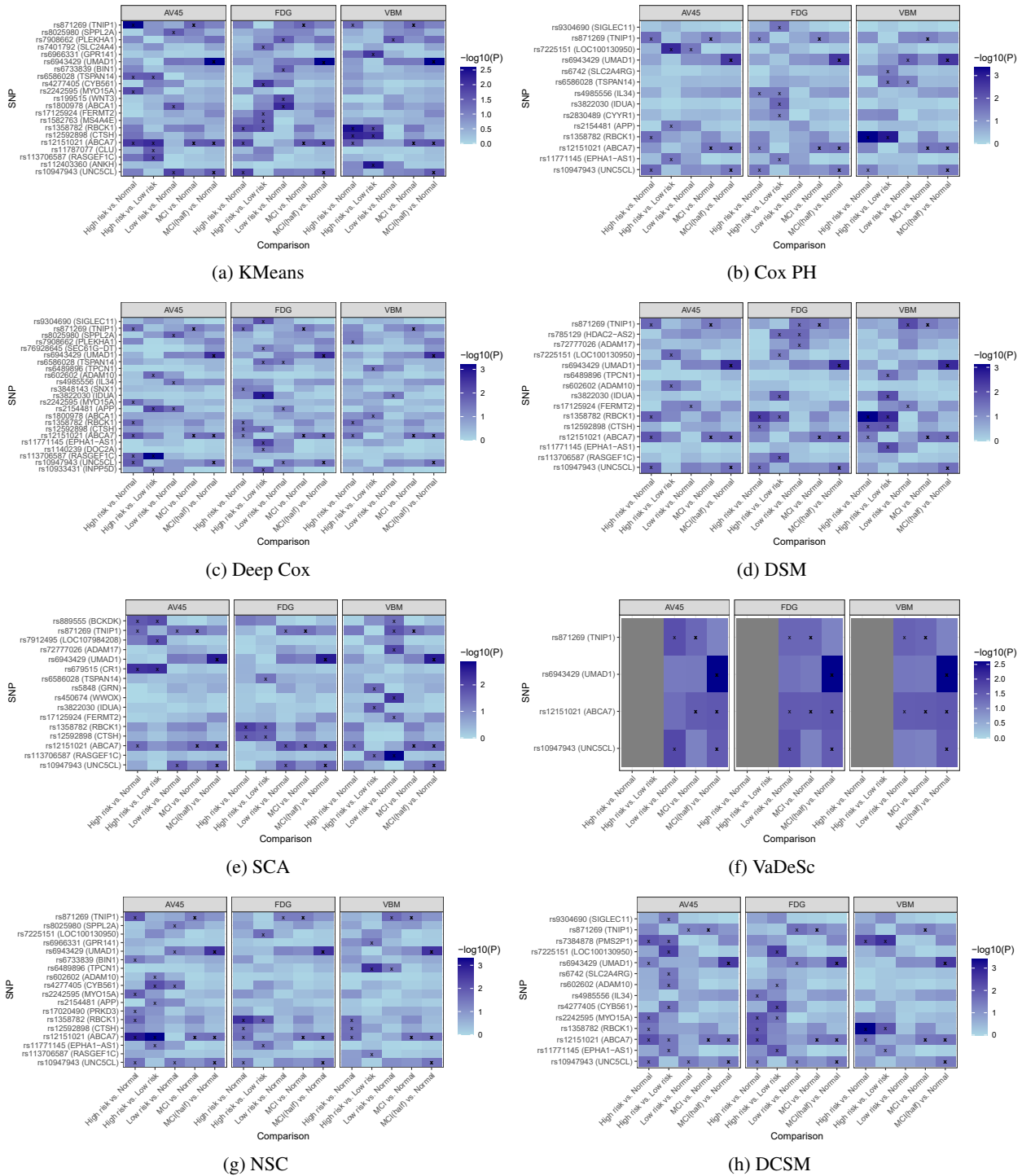


Fig. B.9. Targeted genetic association results of Kmeans. In the parentheses of the vertical label is the name of the gene closest to the corresponding SNP. The darkness of each blue patch represents the negative logarithm of p -value regarding each SNP. The darker the patch is, the more significant the SNP is. "x" marker on the patch means the SNP is statistically significant after FDR correction.

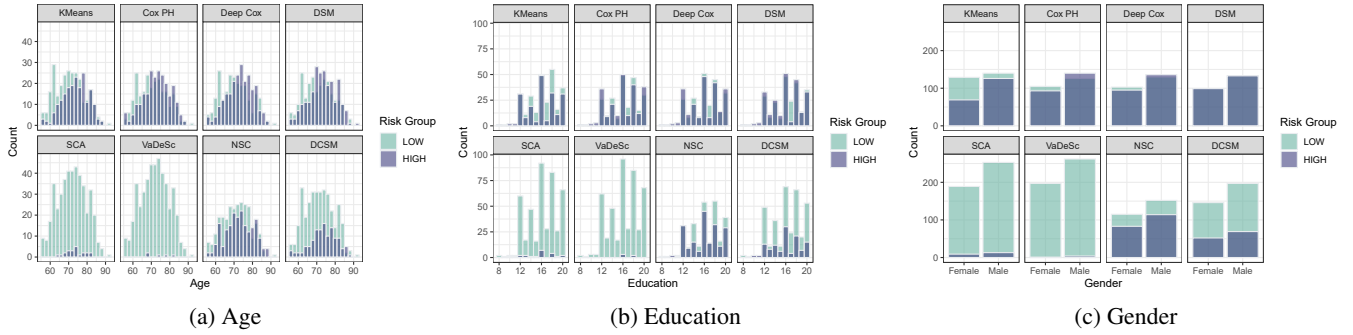


Fig. C.10. Distribution of (a) age, (b) education and (c) gender of high and low risk group. Dataset is AV45.

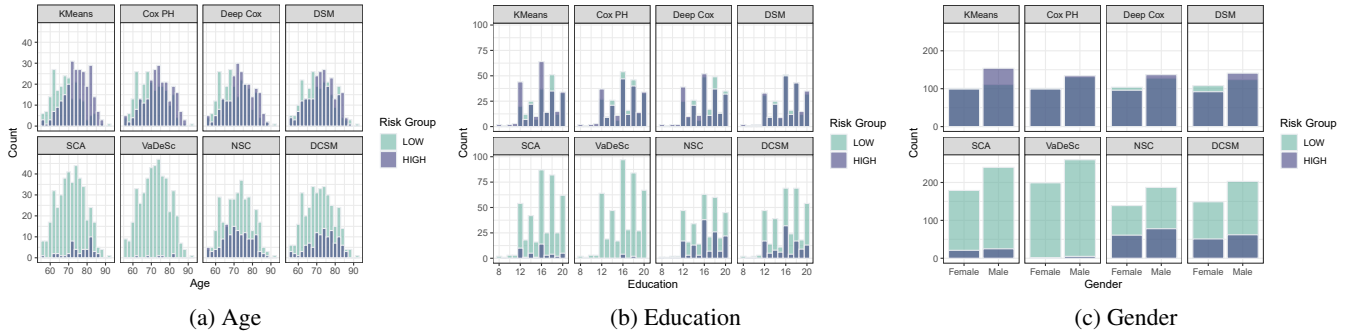


Fig. C.11. Distribution of (a) age, (b) education and (c) gender of high and low risk group. Dataset is FDG.

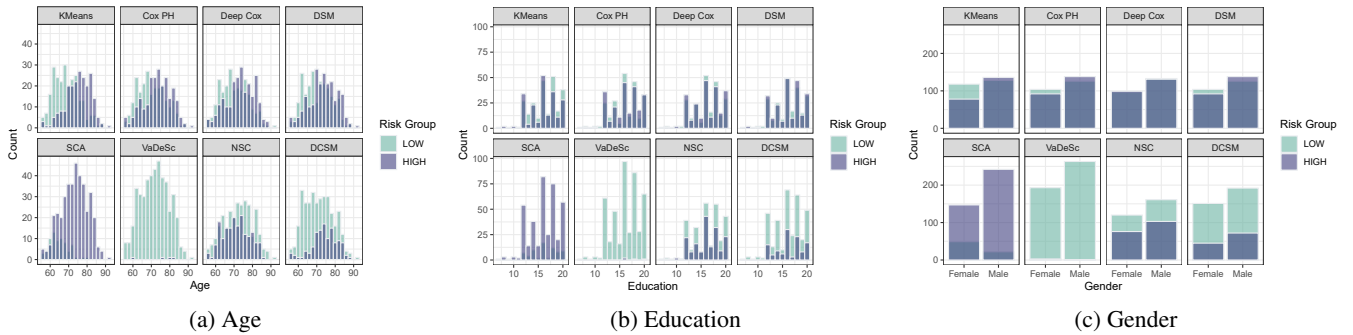


Fig. C.12. Distribution of (a) age, (b) education and (c) gender of high and low risk group. Dataset is VBM.