



Anharmonic Lattice Dynamics set of codes to model materials properties at high temperatures

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$$H^{model} = \sum_i \left(\frac{p_i^2}{2m_i} + \frac{1}{2} \sum_j \phi_{ij} u_i u_j + \frac{1}{3!} \sum_{jkl} \psi_{ijk} u_i u_j u_k + \frac{1}{4!} \sum_{jkl} \chi_{ijkl} u_i u_j u_k u_l + \dots \right) \quad F_i^{model} = - \left(\sum_j \phi_{ij} u_j + \frac{1}{2!} \sum_{jk} \psi_{ijk} u_j u_k + \frac{1}{3!} \sum_{jkl} \chi_{ijkl} u_j u_k u_l + \dots \right); \quad J^\alpha = \frac{1}{2} \sum_{ij} R_{ij}^\alpha u_i^\beta v_j^\gamma (\phi_{ij}^{\beta\gamma} + \frac{2}{3} \psi_{ijk}^{\beta\gamma\delta} u_k^\delta + \dots)$$

Force constants Atomic displacements

FOCEX

Force Constant Extraction from a set of DFT calculations in a supercell

- Up to rank 8
- Can select range of each rank
- Can impose translational rotational and Huan invariance conditions
- Inputs can be from supercells of different shape and size.
- Also outputs phonons, DOS, elastic constants and Gruneisen

THERMACOND

Solves Boltzmann transport equation within and beyond relaxation time approximation

- Includes defect scattering (Tamura's formula)
- Uses full crystal symmetry, requiring only modes within the irreducible Brillouin zone.
- Efficient solution through CG minimization of $\frac{1}{2} C f^2 + D f$ where C = Collision matrix ; f = phonon distribution function

SCOP8

- Finds the state of thermal equilibrium at any given temperature using the Self-Consistent Phonon theory by minimizing a variational free energy $F(K, \eta, u^0)$
- $K(T)$ = effective harmonic force constant
- $\eta(T)$ = strain
- $u^0(T)$ = atomic relaxation
- Also outputs temperature-dependent phonon dispersion, Free energy, elastic constants, thermal expansion

ANFOMOD

Anharmonic FOrce field MOlecular Dynamics

Uses the anharmonic force field generated by FOCEX to do MD simulations and calculate the heat current.

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References

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<https://aladyn.readthedocs.io/en/latest/run.html>
<https://github.com/KeivanS/Anharmonic-lattice-dynamics>

