
Learn more, but bother less: parameter efficient continual learning

Fuli Qiao

Pennsylvania State University
fvq5015@psu.edu

Mehrdad Mahdavi

Pennsylvania State University
mzm616@psu.edu

Abstract

Large Language Models (LLMs) have demonstrated profound capabilities due to their extensive pre-training on diverse corpora. However, LLMs often struggle with catastrophic forgetting when engaged in sequential task learning. In this paper, we propose a novel parameter-efficient approach for continual learning in LLMs, which empirically investigates knowledge transfer from previously learned tasks to new tasks through low-rank matrix parameters, enhancing the learning of new tasks without significant interference. Our method employs sensitivity-based analysis of low-rank matrix parameters to identify knowledge-specific parameters between sequential tasks, which are used to initialize the low-rank matrix parameters in new tasks. To maintain orthogonality and minimize forgetting, we further involve the gradient projection technique that keeps the low-rank subspaces of each new task orthogonal to those of previous tasks. Our experimental results on continual learning benchmarks validate the efficacy of our proposed method, which outperforms existing state-of-the-art methods in reducing forgetting, enhancing task performance, and preserving the model’s ability to generalize to unseen tasks.

1 Introduction

Large Language Models (LLMs) [1, 5, 32, 40] have demonstrated exceptional performance across a broad spectrum of tasks, significantly revolutionizing the landscape in diverse areas driven by artificial intelligence. Full fine-tuning all the parameters of the pre-trained models becomes prohibitive in adapting pre-trained models to a large number of downstream tasks. Thus, following LoRA [11], multiple variants [24, 50] of low-rank adaptation have been proposed to prompt parameter-efficient learning for LLMs. AdaLoRA [50] enhances the flexibility of low-rank matrices for various device budgets by parameterizing the increments through singular value decomposition. It generalizes the matrices, enabling layer-specific rank adjustments to meet different parameter constraints.

Despite the tremendous success of pre-trained models on static tasks, learning multiple sequential tasks, known as continual learning (CL), still poses significant challenges [45]. There are two primary challenges: (i) overcoming catastrophic forgetting, where a model’s performance on previous tasks significantly deteriorates upon training with new data [28, 34], and (ii) facilitating forward transfer, where knowledge from old tasks is harnessed to enhance the learning of new tasks. In the context of LLMs, continual learning extends beyond merely enhancing linguistic and reasoning capabilities and it encompasses a multi-faceted process, including continual pertaining [12], continual instruction [52], and continual alignment [49].

While existing parameter-efficient tuning (PET) methods for CL [27, 31, 39, 43] have primarily focused on mitigating the forgetting issue, they often overlook the equally important objective of facilitating forward knowledge transfer. This transfer is crucial as it allows the model to leverage previously acquired knowledge to better generalize to new tasks or domains. For instance, O-LoRA [43], operating within the PET framework, proposes an orthogonal low-rank adaptation

for continual instruction. This method incrementally learns new tasks in an orthogonal subspace, ensuring that the LoRA parameters from previous tasks remain fixed to minimize forgetting. Besides, compared to full fine-tuning, LoRA inherently forgets less of the source domain, serving as a form of regularization [2]. However, O-LoRA does not explicitly address knowledge transfer across different tasks.

Focusing on knowledge transfer among tasks, many existing non-PET knowledge transfer methods in CL, such as Progressive Network [37] which tackles forward knowledge transfer, and CUBER [22] which employs backward knowledge transfer, while having distinctive approaches to managing knowledge across tasks, they are not directly applicable to the continual learning setting in the PET framework due to their prohibitive computational costs. Although there have been recent attempts at parameter-efficient fine-tuning of LLMs, these methods have failed when applied to CL. For instance, while the parametric knowledge transfer paradigm [53] in PET harnesses the rich knowledge embedded within a teacher’s parameters by extracting task-specific parameters and injecting them into a student model via sensitivity metrics, such methods do not exist in CL for LLMs.

To investigate the impact of leveraging parametric knowledge in the incremental learning of LoRA parameters on a new task, we conduct an experiment where layers from the previous task’s LoRA-based layers are simply replaced at the training initialization of the new task’s LoRA layers, without a predefined strategy for selecting key parameters. The results, presented in Tab. 1 and Fig. 1 using the pre-trained model T5-large [32] with incremental LoRAs for Amazon Reviews and Yahoo Answers [51], indicate that this simple layer replacement can enhance performance. Notably, Tab. 1 reveals that the best replacement strategy significantly improves the performance of both the new task \mathcal{T}_2 and the old task \mathcal{T}_1 compared to scenarios with no replacement.

The aforementioned observations motivate that an ideal approach for continual learning of LLMs in the PET framework should take the best of both worlds by simultaneously overcoming catastrophic forgetting and promoting forward transfer for enhanced generalization across a continual stream of tasks. Motivated by these needs, we seek to explore a new dimension in CL for LLMs:

*How can we effectively inject knowledge from previous tasks into new tasks (for improving **generalization**) while maintaining the orthogonality of each task’s low-rank subspaces (for mitigating **forgetting**) to facilitate parameter-efficient continual learning?*

To answer this question, we propose a novel *all-for-all parameter-efficient* approach for continual learning in LLMs, which empirically investigates knowledge transfer from previously learned tasks to new tasks using low-rank matrix parameters evaluated by sensitivity scores while maintaining orthogonality via gradient projection techniques. We name this method LB-CL (Learn more but bother less Continual Learning). Specifically, LB-CL first calculates sensitivity metrics for SVD-based low-rank parameters of previous tasks to guide the injection of parametric knowledge into new task parameters. Then, it supports incremental learning of new tasks in orthogonal subspaces by preserving low-rank parameters of previous tasks. When transferring knowledge, LB-CL prioritizes low-rank triplets (consisting of a singular value and its corresponding singular vectors) from past tasks based on their sensitivity scores, enabling the new task to learn more from higher-scoring triplets. To preserve the orthogonality of low-rank subspaces, we project the gradients of the new task onto the subspaces formed by previously learned low-rank triplets, encouraging the new task to deviate appropriately from more impactful triplets. Our experimental results validate that LB-CL surpasses previous state-of-the-art methods on standard continual learning benchmarks. Moreover, our analysis highlights the critical role of initialization strategies in promoting generalization through effective parametric knowledge transfer, while also using low-rank orthogonal gradient projection to mitigate catastrophic forgetting.

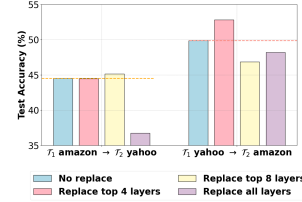


Figure 1: Comparison performance of the model after training task \mathcal{T}_2 with different layers replacement.

Table 1: Testing accuracy of \mathcal{T}_1 and \mathcal{T}_2 after training \mathcal{T}_2 with different layer replacements, highlighting the best-performing strategy as shown in Fig. 1.

		\mathcal{T}_1 (amazon) $\rightarrow \mathcal{T}_2$ (yahoo)			
		no	top 4	top 9	all
\mathcal{T}_1		15.4	15.0	16.6	0.2
\mathcal{T}_2		73.6	73.9	73.7	73.3
		\mathcal{T}_1 (yahoo) $\rightarrow \mathcal{T}_2$ (amazon)			
		no	top 4	top 9	all
\mathcal{T}_1		46.8	50.7	39.1	42.5
\mathcal{T}_2		52.9	54.9	54.5	53.9

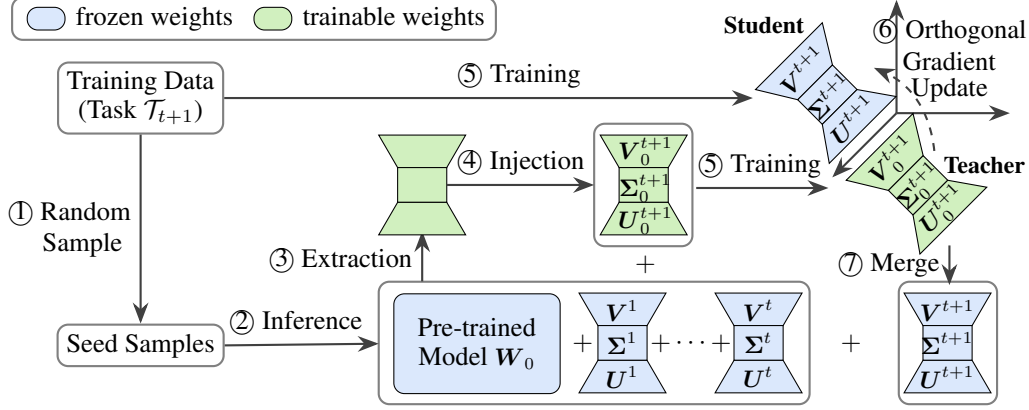


Figure 2: Overview of our LB-CL framework. Starting with the pre-trained model including SVD weights of previous tasks, sensitivity metrics are calculated using a set of seed samples, facilitating the extraction of task-specific knowledge. Subsequently, the extracted layer triplets initialize SVD weights for the new task. Then, the new task is trained in an orthogonal subspace, employing orthogonal gradient projection to minimize forgetting.

■ **Summary of Contributions.** This paper makes three key contributions: (1) A novel parameter-efficient continual learning framework for LLMs that balances generalization through parametric knowledge transfer and the mitigation of forgetting through low-rank orthogonal subspace learning for new tasks; (2) Through comprehensive evaluations, our method demonstrates superior performance over existing state-of-the-art approaches on standard continual learning benchmarks; and (3) We provide an in-depth analysis that deepens our understanding of the dynamics of parametric knowledge transfer within continual learning for LLMs, pinpointing critical factors that drive its effectiveness.

2 Continual Learning Maestro: Learn More but Bother Less

We consider a continual learning scenario where the learner is presented with a sequence of tasks $\{\mathcal{T}_1, \mathcal{T}_2, \dots, \mathcal{T}_T\}$ over time. Each task \mathcal{T}_k is associated with a data distribution \mathcal{D}_k and contains a separate target dataset $\mathcal{S}_k = \{(\mathbf{x}_{k,i}, y_{k,i})\}_{i=1}^{n_t}$ where $\mathbf{x}_{k,i} \in \mathcal{X}_k$ and $y_{k,i} \in \mathcal{Y}_k$. The goal of continual learning is to find a set of parameters $\theta \in \Theta$ that can effectively solve all tasks up to the current task \mathcal{T}_k , while minimizing catastrophic forgetting of previously learned tasks. In continual learning of LLMs, we are given a pre-trained model \mathbf{W}_0 , and would like to continually fine-tune on a sequence of tasks, utilizing the incremental SVD-based low-rank matrix parameters $\mathbf{U}^k \Sigma^k \mathbf{V}^k$ to fine-tune on task \mathcal{T}_k , where $\mathbf{U}^k \in \mathbb{R}^{d_1 \times r}$ and $\mathbf{V}^k \in \mathbb{R}^{r \times d_2}$ represent the left/right singular vectors and the diagonal matrix $\Sigma^k \in \mathbb{R}^{r \times r}$ contains the singular values $\{\lambda_i\}_{1 \leq i \leq r}$ with $r \ll \min(d_1, d_2)$. To enforce the orthogonality of \mathbf{U} and \mathbf{V} , i.e. $\mathbf{U}^\top \mathbf{U} = \mathbf{V} \mathbf{V}^\top = \mathbf{I}$, we use the regularizer: $\mathcal{R}(\mathbf{U}, \mathbf{V}) = \|\mathbf{U}^\top \mathbf{U} - \mathbf{I}\|_F^2 + \|\mathbf{V} \mathbf{V}^\top - \mathbf{I}\|_F^2$. The continual learning model parameters after fine-tuning on task \mathcal{T}_k is: $\theta_k = \mathbf{W}_0 + \sum_{m=1}^k \mathbf{U}^m \Sigma^m \mathbf{V}^m$. Our continual learning goal is to optimize the following objective across all tasks:

$$\max_{\theta} \sum_{k=1}^T \sum_{(\mathbf{x}, y) \in \mathcal{T}_k} \log p_{\theta}(y|\mathbf{x}), \quad (1)$$

where $\theta = \mathbf{W}_0 + \sum_{k=1}^T \mathbf{U}^k \Sigma^k \mathbf{V}^k$. Our method contains two important stages: (i) Learning from knowledge extraction and injection, which transfers knowledge from previously learned tasks to new tasks by incremental SVD triplet sensitivity metric; (ii) Training in Orthogonal Subspaces, which keeps the low-rank subspaces of new tasks orthogonal to those of old tasks. The detailed description of our proposed method, LB-CL, is shown in Fig. 2.

■ **Generalization and Forgetting Tradeoff of Low-rank Finetuning.** Before delving into the detailed steps of proposed algorithm, here we motivate these steps by investigating the forgetting and generalization tradeoff of SVD based low-rank parameter-efficient methods in CL. The performance of a CL algorithm is typically evaluated using two key metrics [3, 4, 16, 21, 23, 25] as defined below: (i) *Forgetting error*: which quantifies the performance degradation on previously learned tasks after acquiring a new task formulated as:

$$\mathcal{F}(\theta_1, \dots, \theta_T) = \sum_{t=1}^{T-1} \mathcal{L}_t(\theta_T) - \mathcal{L}_t(\theta_t) \quad (2)$$

where $\theta_t = \mathbf{W}_0 + \sum_{k=1}^t \mathbf{U}^k \Sigma^k \mathbf{V}^k$, $\mathcal{L}_t(\cdot)$ is the generalization error on task \mathcal{T}_t , and $\mathcal{L}_t(\theta_T) - \mathcal{L}_t(\theta_t)$ is the performance degradation (forgetting) on tasks \mathcal{T}_t between the model after training on task \mathcal{T}_t and the model after training on the final task \mathcal{T}_T .

(ii) *Generalization error*: which measures the algorithm's capability to effectively learn a new task while preserving the knowledge gained from prior tasks defined as:

$$\mathcal{I}(\theta_1, \dots, \theta_T) = \sum_{t=1}^T \mathcal{L}_t(\theta_t) - \mathcal{L}_t(\theta_t^*) \quad (3)$$

where $\mathcal{L}_t(\theta_t) - \mathcal{L}_t(\theta_t^*)$ measures the generalization gap between the CL model θ_t and the optimally fine-tuned model $\theta_t^* = \mathbf{W}_0 + \mathbf{U}_*^t \Sigma_*^t \mathbf{V}_*^t$ on task \mathcal{T}_t . The generalization of final model on all tasks can be decomposed in terms of forgetting generalization errors as follows:

$$\sum_{t=1}^T \mathcal{L}_t(\theta_T) - \mathcal{L}_t(\theta_t^*) = \mathcal{F}(\theta_1, \dots, \theta_T) + \mathcal{I}(\theta_1, \dots, \theta_T) \quad (4)$$

It is crucial to note that the generalization error is based on the final model over all tasks, which may not fully capture each task-specific optimal setting since each task could potentially achieve better performance metrics when fine-tuned individually. Given the complexities in addressing our generalization error due to limited theoretical support, we utilize initialization parameters to further decompose the per-task generalization term on the left-hand side of Eq. 4. This involves measuring the performance difference between the CL model θ_t after learning on tasks \mathcal{T}_t and its initialization $\theta_t^{(0)}$, evaluated on task \mathcal{T}_t as:

$$\mathcal{L}_t(\theta_T) - \mathcal{L}_t(\theta_t^*) = \underbrace{\left(\mathcal{L}_t(\theta_T) - \mathcal{L}_t(\theta_t) \right)}_{\text{(I): forgetting error}} + \underbrace{\left(\mathcal{L}_t(\theta_t) - \mathcal{L}_t(\theta_t^{(0)}) \right)}_{\text{(II): improvement by fine-tuning}} + \underbrace{\left(\mathcal{L}_t(\theta_t^{(0)}) - \mathcal{L}_t(\theta_t^*) \right)}_{\text{(III): generalization of initial model}}$$

From this decomposition, it is clear that all three terms must be carefully calibrated to enhance the overall performance of CL algorithm. In the context of SVD-based low-rank fine-tuning, we have:

- The term (I) captures the forgetting error. It is evident that models that undergo minimal changes when fine-tuned to a new target domain will exhibit less forgetting of the source domain. This automatically holds for fine-tuning with low-rank updating methods as it acts as a regularization. This can be further amplified by fine-tuning in orthogonal subspace.
- The term (II) captures the performance of fine-tuning algorithm itself. Since fine-tuning with low-rank updates is not capable of approximating full fine-tuning accuracy [2], and in order to balance between stability (retaining old knowledge) and plasticity (acquiring new knowledge) we need to leverage methods such as orthogonal gradient projection to better align with current task.
- The term (III) captures the generalization of the initial model. Since the knowledge transfer from previous tasks happens through the initial model, naive averaging of low-rank models from previous tasks might entail a dramatically poor generalization on the current task, in particular when there is a larger domain shift among tasks. Consequently, the contribution of each task should be proportional to its similarity to the current task, measured by leveraging effective discrepancy estimation methods. We formulate this process as the parametric knowledge extraction:

$$\hat{\beta} = \arg \min_{\beta} \mathcal{L}_t \left(\mathbf{W}_0 + \sum_{k=1}^{t-1} \beta^k \mathbf{U}^k \Sigma^k \mathbf{V}^k \right) \quad (5)$$

where $\beta = [\beta^1, \dots, \beta^{t-1}]^\top$ extracts optimal coefficients approximating the influence of new task data on each previous task SVD-based low-rank adapters. Then the parametric knowledge injection in the CL model initialization for task \mathcal{T}_t is constructed as follows:

$$\theta_t^{(0)} = \mathbf{W}_0 + \sum_{k=1}^{t-1} \mathbf{U}^k \Sigma^k \mathbf{V}^k + \sum_{k=1}^{t-1} \hat{\alpha}^k \mathbf{U}^k \Sigma^k \mathbf{V}^k, \text{ where } 1 + \hat{\alpha}^k = \hat{\beta}^k \quad (6)$$

In summary, while updating with low-rank models in CL can provide an implicit regularization effect to mitigate the forgetting issue, their generalization capability is limited due to the low-rank perturbation of parameters. This necessitates effective initialization to overcome the generalization limitations of low-rank updates. Specifically, an initialization that can effectively capture the shared knowledge across tasks based on their similarities to augment the knowledge captured by the pre-trained model is required to facilitate knowledge transfer and improve generalization when performing low-rank updates in a CL setting.

2.1 Learning from Knowledge Extraction and Injection

■ **Sequential Task Low-rank Adapter.** In our continual learning framework, for a pre-trained weight matrix W_0 , it parameterizes the incremental updates for task \mathcal{T}_t by SVD-based low-rank matrices: $\theta_t = \theta_{t-1} + \Delta = W_0 + \sum_{k=1}^{t-1} U^k \Sigma^k V^k + U^t \Sigma^t V^t$. Similar to [50], we define $\mathcal{G}_{l,i}^t = \{U_{l,*i}^t, \lambda_{l,i}^t, V_{l,i*}^t\}$ as the i -th triplet (i -th singular value and its vectors) of layer l for task \mathcal{T}_t , which is different from the dependent and not orthogonal doublet in LoRA-based low-rank matrices. With the SVD-based flexible regularizer, the training objective for task \mathcal{T}_t is represented as $\mathcal{L}_t(U^t, \Sigma^t, V^t) = \mathcal{L}_t(U^t, \Sigma^t, V^t) + \gamma \sum_{i=1}^n \mathcal{R}(U_i^t, V_i^t)$, where n is the number of weight matrices and $\gamma > 0$ is the regularization coefficient.

■ **Sensitivity of the Parameters.** Parameter sensitivity quantifies the impact on the loss function when a specific parameter is altered, typically set to zero, providing insight into the parameter's importance [14, 19, 26, 30, 53]. Consider a teacher model with parameters $\theta = [\theta_1, \dots, \theta_{N_t}]$, where N_t denotes the total number of parameters, the i -th parameter is $\theta_i = [0, \dots, \theta_i, \dots, 0]$. The sensitivity $S_{i,j}$ for sample x_j from task \mathcal{T} is calculated as $S_{i,j} = |\theta_i \nabla_{\theta} \mathcal{L}(x_j)| \approx |\mathcal{L}(\theta) - \mathcal{L}(\theta - \theta_i)|$, where the approximation uses the first-order Taylor expansion of $\mathcal{L}(\cdot)$ at θ_i . Thus, we formulate the sensitivity of each triplet of low-rank matrices, rather than each parameter of the model. By masking the l -th layer i -th triplet $\mathcal{G}_{l,i}^k = \{U_{l,*i}^k, \lambda_{l,i}^k, V_{l,i*}^k\}$ of low-rank matrices for previous task \mathcal{T}_k , following [50], we can obtain the sensitivity score of the l -th layer i -th triplet of low-rank matrices for previous task \mathcal{T}_k , where $k \in \{1, \dots, t-1\}$, on new data sample x_t from new task \mathcal{T}_t :

$$S_{l,i}^k = S(\lambda_{l,i}^k) + \frac{1}{d_1} \sum_{j=1}^{d_1} S(U_{l,j*}^k) + \frac{1}{d_2} \sum_{j=1}^{d_2} S(V_{l,i*}^k) \quad (7)$$

■ **Knowledge Extraction and Injection.** For simplicity in analysis and mathematical expression, we assume that each layer within every task shares the same SVD-based low-rank adapter rank r . Our first step is to assess the layers of the previous task \mathcal{T}_k low-rank matrices where $k \in \{1, \dots, t-1\}$, by Eq. 7, we calculate triplet-specific sensitivity scores in layer l and this layer sensitivity score is represented as $S_l^k = \sum_{i=1}^r S_{l,i}^k$. To preserve the inherent structure of the tasks' low-rank adapters, the layers are subsequently mapped to the new task \mathcal{T}_t adapter maintaining their original sequential order. Having computed the sensitivity scores of all triplets for layer l in previous tasks $\{\mathcal{T}_1, \dots, \mathcal{T}_{t-1}\}$, we proceed to arrange them with weighted sensitivity scores to initialize the layer l in new task \mathcal{T}_t :

$$\mathcal{G}_{l,i}^t = \{U_{l,*i}^t, \lambda_{l,i}^t, V_{l,i*}^t\} = \left\{ \sum_{k=1}^{t-1} \alpha_{l,i}^k U_{l,*i}^k, \sum_{k=1}^{t-1} \alpha_{l,i}^k \lambda_{l,i}^k, \sum_{k=1}^{t-1} \alpha_{l,i}^k V_{l,i*}^k \right\} \quad (8)$$

where $\alpha_{l,i}^k$ is the weight for the components of the triplet $\mathcal{G}_{l,i}^k$, and $\alpha_{l,i}^k = \frac{S_{l,i}^k}{\sum_{k=1}^{t-1} S_{l,i}^k}$ obtained from the sensitivity founded in Eq. 7. By aggregating weighted triplets across layers, we derive the extracted triplets from previous tasks' adapters and inject these triplets into the new task's adapter.

2.2 Training in Orthogonal Subspaces

We utilize the SVD-based adapter's low-rank subspace to represent the gradient subspaces of previous tasks, asserting that these parameters capture essential model update directions rather than just numerical adjustments [43]. This hypothesis allows us to minimize interference with previously learned tasks by training within a subspace orthogonal to that of the SVD-based subspace. We approximate the layer l subspace for task \mathcal{T}_k as the subspace consisting of the triplets \mathcal{G}_l^k . To ensure orthogonal to the previously learned tasks layer subspaces, we first project the gradients of layer triplets of new task \mathcal{T}_t onto the previously learned tasks layer subspaces spanned by $\{\mathcal{G}_l^k\}$, where $k \in \{1, \dots, t-1\}$, and then make the gradients far away from these subspaces. The gradients of layer l triplets of data x_t from new task \mathcal{T}_t become:

$$\nabla_{\mathcal{G}_l^t} \mathcal{L}_t(\mathcal{G}_l^t; x_t) = \nabla_{\mathcal{G}_l^t} \mathcal{L}_t(\mathcal{G}_l^t; x_t) - \sum_{k=1}^{t-1} \text{proj}(\nabla_{\mathcal{G}_l^t} \mathcal{L}_t(\mathcal{G}_l^t; x_t), \mathcal{G}_l^k) \quad (9)$$

where $\text{proj}(u, v) = \frac{\langle u, v \rangle}{\langle v, v \rangle} v$ is the projection of u in the direction of v [7].

3 Experiments

3.1 Experimental Setup

Our experiments employ the encoder-decoder architecture of the T5-large and T5-base models [32], consistent with previous work in CL for NLP. All experiments are conducted on NVIDIA A6000 GPUs, utilizing the DeepSpeed repository.

■ **Standard CL benchmark.** We evaluate our approach using a CL benchmark specifically designed for language models. This benchmark comprises five text classification datasets: AG News, Amazon Reviews, Yelp Reviews, DBpedia, and Yahoo Answers, as introduced by [51]. We adhere to the CL setup for the T5 model as outlined in LFPT5 [31] and experiment with three different task orders within this benchmark.

■ **Large number of tasks.** Our method’s efficacy is further tested on extended task sequences through a comprehensive CL benchmark encompassing 15 datasets, as detailed in [35]. This benchmark integrates tasks from three sources: five from the standard CL benchmark, four from the GLUE benchmark (MNLI, QQP, RTE, SST-2), five from the SuperGLUE benchmark (WiC, CB, COPA, MultiRC, BoolQ), and the IMDB movie reviews dataset. For each task, we train using 1000 randomly selected samples and validate using 500 samples per class, following the methodology of [35].

■ **Metrics.** We define the testing accuracy on the task \mathcal{T}_i after training on the task \mathcal{T}_j as $a_{i,j}$. The main metric for evaluation is **Average Accuracy (AA)**, calculated as the mean accuracy across all tasks after training on the last task: $\frac{1}{T} \sum_{i=1}^T a_{i,T}$.

■ **Baselines.** We compare our method against various baseline approaches:

- SeqFT [6]: train all model parameters on a sequence of tasks (without adding any regularization or replaying samples from the previous tasks).
- SeqLoRA: fixed-size LoRA parameters are trained on a sequence of tasks (without adding any regularization or replaying samples from the previous tasks).
- IncLoRA: incremental learning of new LoRA parameters on a sequence of tasks (without adding any regularization or replaying samples from the previous tasks).
- SeqSVD: fixed-size SVD parameters are trained on a sequence of tasks (without adding any regularization or replaying samples from the previous tasks).
- Replay: fine-tune the whole model with a memory buffer, and replay samples from old tasks when learning new tasks to avoid forgetting.
- EWC [13]: fine-tune the whole model with a regularization loss that prevents updating parameters that could interfere with previously learned tasks.
- LwF [18]: constrains the shared representation layer to be similar to its original state before learning the new task.
- L2P [44]: uses the input to dynamically select and update prompts from the prompt pool in an instance-wise fashion.
- LFPT5 [31]: continuously train a soft prompt that simultaneously learns to solve the tasks and generate training samples, which are subsequently used in experience replay.
- L-CL: incremental learning of new SVD parameters on a sequence of tasks with initialization and SVD regularization.
- B-CL: incremental learning of new SVD parameters on a sequence of tasks with gradient projection and SVD regularization.
- NLNB-CL: incremental learning of new SVD parameters on a sequence of tasks (with adding only SVD regularization and without replaying samples from the previous tasks), also called IncSVD.
- ProgPrompt [35]: adopts task-specific soft prompts for each task, training distinct models per task and using task IDs during inference.
- O-LoRA [43]: incrementally train new tasks in an orthogonal subspace while fixing the LoRA matrices of previous tasks.
- PerTaskFT: train a separate model for each task.
- MTL: train a model on all tasks as multi-task learning, serving as the benchmark’s upper bound of the performance limit.

3.2 Main Results

Tab. 2 presents a performance comparison of LB-CL and baseline continual learning methods across two CL benchmarks. Following LFPT5, we report results from three random runs with different task orders on the CL benchmark. For fairness, we use the same rank of the LoRA-based and SVD-based matrix in each corresponding comparison experiment. To reduce computation time,

Table 2: Testing performance on two standard CL benchmarks with T5-large.

	Standard CL Benchmark				Large Number of Tasks			
	Order-1	Order-2	Order-3	avg	Order-4	Order-5	Order-6	avg
SeqFT	18.9	24.9	41.7	28.5	7.4	7.3	7.4	7.4
SeqLoRA	39.5	31.9	46.6	39.3	4.9	3.5	4.2	4.2
IncLoRA	63.4	62.2	65.1	63.6	63.0	57.9	60.4	60.5
SeqSVD	40.0	63.3	44.9	49.4	13.7	13.8	12.2	13.2
Replay	50.3	52.0	56.6	53.0	54.5	54.3	53.5	54.1
EWC	46.3	45.3	52.1	47.9	44.9	44.0	45.4	44.8
LwF	52.7	52.9	48.4	51.3	49.7	42.8	46.9	46.5
L2P	59.0	60.5	59.9	59.8	57.7	53.6	56.6	56.0
LFPT5	66.6	71.2	76.2	71.3	69.8	67.2	69.2	68.7
L-CL	75.3	73.5	71.9	73.6	66.5	64.0	69.0	66.5
B-CL	76.4	71.5	75.1	74.3	65.7	66.4	69.2	67.1
NLNB-CL	76.0	73.4	74.0	74.5	67.6	65.3	62.6	65.2
O-LoRA	74.9	75.3	75.9	75.4	70.5	65.5	70.5	68.8
LB-CL	76.9	76.5	76.8	76.7	68.4	67.3	71.8	69.2
ProgPrompt	76.1	76.0	76.3	76.1	78.7	78.8	77.8	78.4
PerTaskFT	70.0	70.0	70.0	70.0	78.1	78.1	78.1	78.1
MTL	80.0	80.0	80.0	80.0	76.3	76.3	76.3	76.3

we reasonably focus on some high-level layers to narrow the searching range of exploring critical parametric knowledge, since previous research, e.g. [43, 50], has already demonstrated that high-level layers are important for model performance.

■ **Results on Standard Continual Learning Benchmarks.** Across all task orders of the standard CL benchmark, LB-CL consistently surpasses previous methods by a significant margin. Notably, LB-CL achieves performance improvements in all task orders compared to O-LoRA, the prior state-of-the-art. Our approach demonstrates performance on par with multi-task learning and significantly exceeds that of PerTaskFT. This indicates that LB-CL not only effectively prevents catastrophic forgetting but also efficiently utilizes knowledge from prior tasks to enhance the learning of new tasks.

■ **Performance with Large Number of Tasks.** In a more demanding benchmark featuring a large number of tasks, LB-CL surpasses the state-of-the-art, O-LoRA, in terms of average performance across three task orders. Although ProgPrompt shows superior performance in managing long-sequence tasks, its limitations are notable. ProgPrompt is strictly dependent on the tasks it has been trained on and relies heavily on task IDs during inference, which restricts its generalization capabilities and adaptability for use in LLMs. However, LB-CL does not use task ID during testing, which keeps its generalization. It is important to note that nearly all existing continual learning methods fall significantly short of the performance achieved by PerTaskFT and MTL, underscoring that continual learning with a large array of tasks remains a formidable challenge.

3.3 Discussions

■ **How do initialization and gradient projection effectively influence the performance of LB-CL?**

We systematically evaluated the influence of two components: initialization and gradient projection. The results across various orders and their average performances, as presented in the last rows in Tab. 2, reveal distinct trends. L-CL, which employs only initialization, suggests that while this component does provide a beneficial starting point for task learning, it falls short of maintaining knowledge across tasks in Order 3. B-CL, utilizing only gradient projection, demonstrates slightly higher performance than L-CL in Order 1 and Order 3. However, the absence of initialization limits its effectiveness, particularly in establishing a robust foundation in Order 2. NLNB-CL, which neither initializes nor employs gradient projection, surprisingly performs slightly better than both L-CL and B-CL on average, but it does not excel in any specific order. This outcome suggests that the model may possess inherent adaptive capabilities or rely on other compensatory mechanisms. LB-CL, integrating both initialization and gradient projection, exhibits the highest overall performance with consistent scores across all orders. This robust performance indicates that the synergistic contribution of both components significantly enhances the model’s ability to effectively handle CL tasks.

■ **How do different initialization strategies affect the performance?** To elucidate the impact of distinct initialization strategies, we compare two different initialization strategies motivated by [29] to initialize new task \mathcal{T}_t : (i) with previous tasks low-rank matrix triplets \mathcal{G}^k , and (ii) without the singular values Σ^k but leveraging $\{U^k, V^k\}$ where $k \in \{1, \dots, t-1\}$. These strategies are assessed using T5-large model over three task orders in the standard CL benchmark. Our results, depicted in Fig. 3, reveal that utilizing only $\{U, V\}$ from prior tasks’ triplets surpass the full triplet configuration in average performance across three task orders. While “with Σ ” strategy exhibits peak performance in Order 3, “without Σ ” approach demonstrates better consistency and stability. This suggests that excluding Σ may lead to a more robust generalization across diverse tasks, but it cannot fully represent previously learnt tasks’ important subspaces, thus we use “with Σ ” as the initialization of LB-CL, and “without Σ ” can be used as an improvement strategy in implementation. Furthermore, both strategies outperform the performance of the O-LoRA method over these three orders.

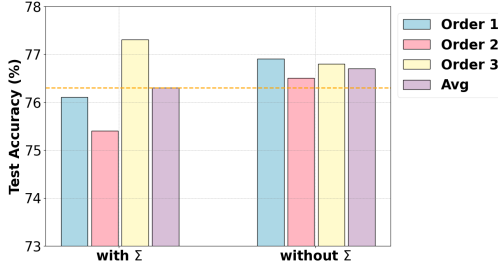


Figure 3: Comparison of different initialization strategies across three orders of standard CL benchmark. The "Avg" value represents the average testing accuracy, illustrating how each strategy stabilizes learning performance.

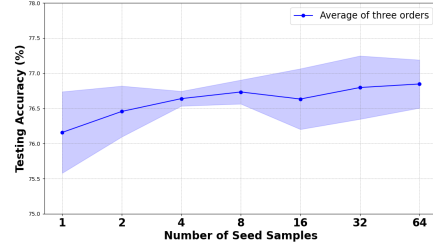


Figure 4: Impact analysis of seed sample quantity on the performance in LB-CL, evaluated across three orders of standard CL benchmark. This investigation highlights the influence of initial seed samples on model effectiveness.

■ **How does the number of seed samples affect the performance of the model?** The number of seed samples significantly influences the reliability and efficiency of the sensitivity score computations derived from the teacher model. We explored the impact of varying the number of seed samples from new tasks on the sensitivity of parameters from previous tasks. As illustrated in Fig. 4, increasing the number of seed samples improves performance incrementally at a slight rate. Notably, the variance in performance metrics is considerably lower with 4 and 8 seed samples. Based on these findings, we have selected 8 seed samples as the optimal number for our hyperparameter setting.

■ **How does the training computation cost perform?** We compare the training computation cost between LB-CL and O-LoRA in Tab. 3, using Order 1 in the standard CL benchmark with T5-large model. Tab. 3 shows that the GPU memory consumption of both methods is similar, indicating comparable resource efficiency during training. For the number of training parameters, we examine a single layer and denote r as the rank of SVD-based and LoRA-based matrix, m as the input dimension, and n as the output dimension of the layer. Given that $r \ll \min(m, n)$, the number of training parameters for both methods remains close, further highlighting their efficiency in parameter.

Table 3: Comparison of training computation cost between LB-CL and O-LoRA.

Method	GPU Memory	Num of training params/task
O-LoRA	24.82 GB	$r(m + n)$
LB-CL	28.28 GB	$r(m + n) + r$

■ **What’s the distribution of parametric knowledge across layers of the model?** We analyze the distribution of parametric knowledge across the model’s layers to identify those most critical for retaining task-specific information. In Fig. 5, our analysis of sensitivity and Fisher information on the average of three task orders in standard CL benchmark, reveals that higher-level layers, particularly in decoder layers, exhibit significant sensitivity. Particularly, the top 4 layers of the decoder are notably sensitive, suggesting that focusing sensitivity analyses on these layers could represent the entire decoder effectively, thus reducing computational demands. Validation with Fisher information confirms that these high-level layers are crucial in both the encoder and decoder, especially the top 3 layers of the decoder. This alignment underscores that our sensitivity scores effectively identify the most crucial layers for task-specific knowledge transfer. Given the time-intensive nature of

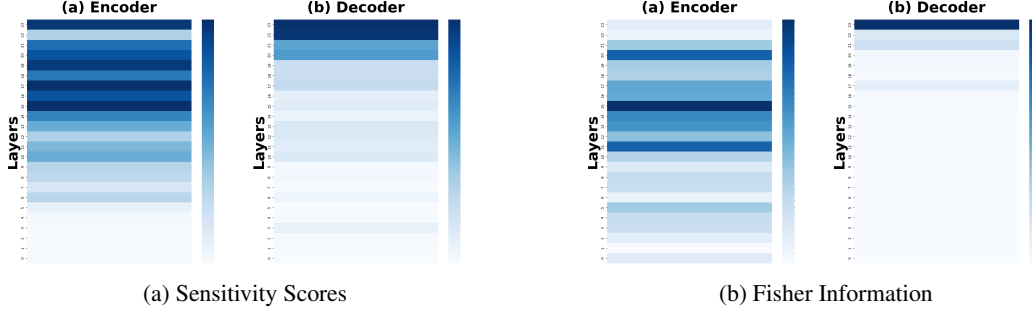


Figure 5: Comparison of sensitivity scores and Fisher information of encoder and decoder Layers, and both results are the average results of three task orders in standard CL benchmark.

Fisher information calculations, our sensitivity score approach provides a more efficient alternative, enhancing training efficiency by focusing on several critical high-level layers.

Table 4: Comparisons of different rank r of low-rank matrix. This experiment is conducted based on T5-large in standard CL benchmark.

r-dim	Order			
	1	2	3	avg
2	76.7	77.2	75.2	76.3
4	77.0	76.8	75.9	76.6
8	76.9	76.5	76.8	76.7
16	77.4	76.0	75.5	76.3
Std	0.25	0.44	0.60	0.18

Table 5: Comparisons of different models’ performances across three task orders in standard CL benchmark.

(T5-base)		Order			
Method		1	2	3	avg
O-LoRA	72.9	72.3	72.6	72.6	
LB-CL	73.8	74.4	72.4	73.5	
(T5-large)		Order			
Method		1	2	3	avg
O-LoRA	74.9	75.3	75.9	75.4	
LB-CL	76.9	76.5	76.8	76.7	

■ **What’s the optimal rank r for LB-CL?** To explore the impact of the rank r on the performance of LB-CL, we conduct experiments using the T5-large model on the standard CL benchmark. The results, presented in Tab. 4, examine how varying r affects the accuracy across different task orders. It shows that increasing the rank r does not lead to a significant improvement in model performance. Furthermore, the small standard deviations across different orders for each rank underscore the model’s consistent performance, irrespective of rank variations. This suggests that by leveraging more knowledge from previous tasks, our method allows the gradient space of the new task to diverge more significantly from those of prior tasks, thereby enhancing stability across various ranks.

■ **How do different pre-trained models influence performance?** We investigate the impact of model scale on performance by comparing T5-base and T5-large models using a standard CL benchmark. We evaluate both our method and O-LoRA across three task orders. The results, presented in Tab. 5, clearly demonstrate significant performance differences between the two model sizes and the methods employed. For the T5-base model, LB-CL consistently outperforms O-LoRA. While for the T5-large model, LB-CL significantly surpasses O-LoRA’s outcomes. Moreover, LB-CL shows exceptional consistency across all task orders in the T5-large model, highlighting its robustness and effectiveness when scaled up. This analysis confirms the influence of model size on the success of different continual learning strategies, with LB-CL proving particularly effective in larger models.

4 Conclusion

In this paper, we investigate the balance between overcoming forgetting and achieving generalization in the continual learning of LLMs, decompose the generalization error with the task low-rank matrix initialization, then propose a novel framework, exploring parametric knowledge transfer between tasks and utilizing the inherent forgetting less ability of low-rank matrix. Instead of storing extra task-specific auxiliary parameters, we just utilize the low-rank parameters which would be merged into the pre-trained model. Our experiments across standard CL benchmarks validate the effectiveness of this approach. Furthermore, we analyze the critical factors influencing initialization in CL, providing insights for further enhancements in this field.

Acknowledgment

This work is partially supported by NSF CAREER Award #2239374 and NSF EFMA Award # 2318101.

References

- [1] Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni Aleman, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, et al. Gpt-4 technical report. *arXiv preprint arXiv:2303.08774*, 2023.
- [2] Dan Biderman, Jose Gonzalez Ortiz, Jacob Portes, Mansheej Paul, Philip Greengard, Connor Jennings, Daniel King, Sam Havens, Vitaliy Chiley, Jonathan Frankle, et al. Lora learns less and forgets less. *arXiv preprint arXiv:2405.09673*, 2024.
- [3] Arslan Chaudhry, Puneet K Dokania, Thalaiyasingam Ajanthan, and Philip HS Torr. Riemannian walk for incremental learning: Understanding forgetting and intransigence. In *Proceedings of the European conference on computer vision (ECCV)*, pages 532–547, 2018.
- [4] Arslan Chaudhry, Marc’Aurelio Ranzato, Marcus Rohrbach, and Mohamed Elhoseiny. Efficient lifelong learning with a-gem. *arXiv preprint arXiv:1812.00420*, 2018.
- [5] Aakanksha Chowdhery, Sharan Narang, Jacob Devlin, Maarten Bosma, Gaurav Mishra, Adam Roberts, Paul Barham, Hyung Won Chung, Charles Sutton, Sebastian Gehrmann, et al. Palm: Scaling language modeling with pathways. *Journal of Machine Learning Research*, 24(240):1–113, 2023.
- [6] Cyprien de Masson D’Autume, Sebastian Ruder, Lingpeng Kong, and Dani Yogatama. Episodic memory in lifelong language learning. *Advances in Neural Information Processing Systems*, 32, 2019.
- [7] Mehrdad Farajtabar, Navid Azizan, Alex Mott, and Ang Li. Orthogonal gradient descent for continual learning. In *International Conference on Artificial Intelligence and Statistics*, pages 3762–3773. PMLR, 2020.
- [8] Xu Han, Yi Dai, Tianyu Gao, Yankai Lin, Zhiyuan Liu, Peng Li, Maosong Sun, and Jie Zhou. Continual relation learning via episodic memory activation and reconsolidation. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics*, pages 6429–6440, 2020.
- [9] Junxian He, Chunting Zhou, Xuezhe Ma, Taylor Berg-Kirkpatrick, and Graham Neubig. Towards a unified view of parameter-efficient transfer learning. *arXiv preprint arXiv:2110.04366*, 2021.
- [10] Neil Houlsby, Andrei Giurgiu, Stanislaw Jastrzebski, Bruna Morrone, Quentin De Laroussilhe, Andrea Gesmundo, Mona Attariyan, and Sylvain Gelly. Parameter-efficient transfer learning for nlp. In *International conference on machine learning*, pages 2790–2799. PMLR, 2019.
- [11] Edward J Hu, Yelong Shen, Phillip Wallis, Zeyuan Allen-Zhu, Yuanzhi Li, Shean Wang, Lu Wang, and Weizhu Chen. Lora: Low-rank adaptation of large language models. *arXiv preprint arXiv:2106.09685*, 2021.
- [12] Xisen Jin, Dejiao Zhang, Henghui Zhu, Wei Xiao, Shang-Wen Li, Xiaokai Wei, Andrew Arnold, and Xiang Ren. Lifelong pretraining: Continually adapting language models to emerging corpora. *arXiv preprint arXiv:2110.08534*, 2021.
- [13] James Kirkpatrick, Razvan Pascanu, Neil Rabinowitz, Joel Veness, Guillaume Desjardins, Andrei A Rusu, Kieran Milan, John Quan, Tiago Ramalho, Agnieszka Grabska-Barwinska, et al. Overcoming catastrophic forgetting in neural networks. *Proceedings of the national academy of sciences*, 114(13):3521–3526, 2017.
- [14] Namhoon Lee, Thalaiyasingam Ajanthan, and Philip HS Torr. Snip: Single-shot network pruning based on connection sensitivity. *arXiv preprint arXiv:1810.02340*, 2018.

- [15] Brian Lester, Rami Al-Rfou, and Noah Constant. The power of scale for parameter-efficient prompt tuning. *arXiv preprint arXiv:2104.08691*, 2021.
- [16] Haoran Li, Jingfeng Wu, and Vladimir Braverman. Fixed design analysis of regularization-based continual learning. In *Conference on Lifelong Learning Agents*, pages 513–533. PMLR, 2023.
- [17] Xilai Li, Yingbo Zhou, Tianfu Wu, Richard Socher, and Caiming Xiong. Learn to grow: A continual structure learning framework for overcoming catastrophic forgetting. In *International conference on machine learning*, pages 3925–3934. PMLR, 2019.
- [18] Zhizhong Li and Derek Hoiem. Learning without forgetting. *IEEE transactions on pattern analysis and machine intelligence*, 40(12):2935–2947, 2017.
- [19] Chen Liang, Haoming Jiang, Simiao Zuo, Pengcheng He, Xiaodong Liu, Jianfeng Gao, Weizhu Chen, and Tuo Zhao. No parameters left behind: Sensitivity guided adaptive learning rate for training large transformer models. *arXiv preprint arXiv:2202.02664*, 2022.
- [20] Yan-Shuo Liang and Wu-Jun Li. Inflora: Interference-free low-rank adaptation for continual learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 23638–23647, 2024.
- [21] Sen Lin, Peizhong Ju, Yingbin Liang, and Ness Shroff. Theory on forgetting and generalization of continual learning. In *International Conference on Machine Learning*, pages 21078–21100. PMLR, 2023.
- [22] Sen Lin, Li Yang, Deliang Fan, and Junshan Zhang. Beyond not-forgetting: Continual learning with backward knowledge transfer. *Advances in Neural Information Processing Systems*, 35:16165–16177, 2022.
- [23] Sen Lin, Li Yang, Deliang Fan, and Junshan Zhang. Trgp: Trust region gradient projection for continual learning. *arXiv preprint arXiv:2202.02931*, 2022.
- [24] Shih-Yang Liu, Chien-Yi Wang, Hongxu Yin, Pavlo Molchanov, Yu-Chiang Frank Wang, Kwang-Ting Cheng, and Min-Hung Chen. Dora: Weight-decomposed low-rank adaptation, 2024.
- [25] David Lopez-Paz and Marc’Aurelio Ranzato. Gradient episodic memory for continual learning. *Advances in neural information processing systems*, 30, 2017.
- [26] Ekdeep Singh Lubana and Robert P Dick. A gradient flow framework for analyzing network pruning. *arXiv preprint arXiv:2009.11839*, 2020.
- [27] Andrea Madotto, Zhaojiang Lin, Zhenpeng Zhou, Seungwhan Moon, Paul Crook, Bing Liu, Zhou Yu, Eunjoon Cho, and Zhiguang Wang. Continual learning in task-oriented dialogue systems. *arXiv preprint arXiv:2012.15504*, 2020.
- [28] Michael McCloskey and Neal J Cohen. Catastrophic interference in connectionist networks: The sequential learning problem. In *Psychology of learning and motivation*, volume 24, pages 109–165. Elsevier, 1989.
- [29] Nikhil Mehta, Kevin Liang, Vinay Kumar Verma, and Lawrence Carin. Continual learning using a bayesian nonparametric dictionary of weight factors. In *International Conference on Artificial Intelligence and Statistics*, pages 100–108. PMLR, 2021.
- [30] Michael C Mozer and Paul Smolensky. Skeletonization: A technique for trimming the fat from a network via relevance assessment. *Advances in neural information processing systems*, 1, 1988.
- [31] Chengwei Qin and Shafiq Joty. Lfpt5: A unified framework for lifelong few-shot language learning based on prompt tuning of t5. *arXiv preprint arXiv:2110.07298*, 2021.
- [32] Colin Raffel, Noam Shazeer, Adam Roberts, Katherine Lee, Sharan Narang, Michael Matena, Yanqi Zhou, Wei Li, and Peter J Liu. Exploring the limits of transfer learning with a unified text-to-text transformer. *Journal of machine learning research*, 21(140):1–67, 2020.

- [33] Dushyant Rao, Francesco Visin, Andrei Rusu, Razvan Pascanu, Yee Whye Teh, and Raia Hadsell. Continual unsupervised representation learning. *Advances in neural information processing systems*, 32, 2019.
- [34] Roger Ratcliff. Connectionist models of recognition memory: constraints imposed by learning and forgetting functions. *Psychological review*, 97(2):285, 1990.
- [35] Anastasia Razdaibiedina, Yuning Mao, Rui Hou, Madian Khabisa, Mike Lewis, and Amjad Almahairi. Progressive prompts: Continual learning for language models. In *The Eleventh International Conference on Learning Representations*, 2023.
- [36] David Rolnick, Arun Ahuja, Jonathan Schwarz, Timothy Lillicrap, and Gregory Wayne. Experience replay for continual learning. *Advances in neural information processing systems*, 32, 2019.
- [37] Andrei A Rusu, Neil C Rabinowitz, Guillaume Desjardins, Hubert Soyer, James Kirkpatrick, Koray Kavukcuoglu, Razvan Pascanu, and Raia Hadsell. Progressive neural networks. *arXiv preprint arXiv:1606.04671*, 2016.
- [38] James Seale Smith, Yen-Chang Hsu, Lingyu Zhang, Ting Hua, Zsolt Kira, Yilin Shen, and Hongxia Jin. Continual diffusion: Continual customization of text-to-image diffusion with c-lora. *arXiv preprint arXiv:2304.06027*, 2023.
- [39] Chenyang Song, Xu Han, Zheni Zeng, Kuai Li, Chen Chen, Zhiyuan Liu, Maosong Sun, and Tao Yang. Conpet: Continual parameter-efficient tuning for large language models. *arXiv preprint arXiv:2309.14763*, 2023.
- [40] Hugo Touvron, Thibaut Lavril, Gautier Izacard, Xavier Martinet, Marie-Anne Lachaux, Timothée Lacroix, Baptiste Rozière, Naman Goyal, Eric Hambro, Faisal Azhar, et al. Llama: Open and efficient foundation language models. *arXiv preprint arXiv:2302.13971*, 2023.
- [41] Alex Wang, Yada Pruksachatkun, Nikita Nangia, Amanpreet Singh, Julian Michael, Felix Hill, Omer Levy, and Samuel Bowman. Superglue: A stickier benchmark for general-purpose language understanding systems. *Advances in neural information processing systems*, 32, 2019.
- [42] Alex Wang, Amanpreet Singh, Julian Michael, Felix Hill, Omer Levy, and Samuel R Bowman. Glue: A multi-task benchmark and analysis platform for natural language understanding. *arXiv preprint arXiv:1804.07461*, 2018.
- [43] Xiao Wang, Tianze Chen, Qiming Ge, Han Xia, Rong Bao, Rui Zheng, Qi Zhang, Tao Gui, and Xuanjing Huang. Orthogonal subspace learning for language model continual learning. *arXiv preprint arXiv:2310.14152*, 2023.
- [44] Zifeng Wang, Zizhao Zhang, Chen-Yu Lee, Han Zhang, Ruoxi Sun, Xiaoqi Ren, Guolong Su, Vincent Perot, Jennifer Dy, and Tomas Pfister. Learning to prompt for continual learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 139–149, 2022.
- [45] Tongtong Wu, Massimo Caccia, Zhuang Li, Yuan-Fang Li, Guilin Qi, and Gholamreza Haffari. Pretrained language model in continual learning: A comparative study. In *International conference on learning representations*, 2021.
- [46] Jaehong Yoon, Eunho Yang, Jeongtae Lee, and Sung Ju Hwang. Lifelong learning with dynamically expandable networks. *arXiv preprint arXiv:1708.01547*, 2017.
- [47] Jiazuo Yu, Yunzhi Zhuge, Lu Zhang, Ping Hu, Dong Wang, Huchuan Lu, and You He. Boosting continual learning of vision-language models via mixture-of-experts adapters. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 23219–23230, 2024.
- [48] Elad Ben Zaken, Shauli Ravfogel, and Yoav Goldberg. Bitfit: Simple parameter-efficient fine-tuning for transformer-based masked language-models. *arXiv preprint arXiv:2106.10199*, 2021.

- [49] Han Zhang, Lin Gui, Yuanzhao Zhai, Hui Wang, Yu Lei, and Ruifeng Xu. Copf: Continual learning human preference through optimal policy fitting. *arXiv preprint arXiv:2310.15694*, 2023.
- [50] Qingru Zhang, Minshuo Chen, Alexander Bukharin, Pengcheng He, Yu Cheng, Weizhu Chen, and Tuo Zhao. Adaptive budget allocation for parameter-efficient fine-tuning. In *The Eleventh International Conference on Learning Representations*, 2023.
- [51] Xiang Zhang, Junbo Zhao, and Yann LeCun. Character-level convolutional networks for text classification. *Advances in neural information processing systems*, 28, 2015.
- [52] Zihan Zhang, Meng Fang, Ling Chen, and Mohammad-Reza Namazi-Rad. Citb: A benchmark for continual instruction tuning. *arXiv preprint arXiv:2310.14510*, 2023.
- [53] Ming Zhong, Chenxin An, Weizhu Chen, Jiawei Han, and Pengcheng He. Seeking neural nuggets: Knowledge transfer in large language models from a parametric perspective. In *The Twelfth International Conference on Learning Representations*, 2024.

A Appendix

A.1 Additional Related Works

Continual Learning. Continual learning is a field focused on developing algorithms that can accumulate and refine knowledge over time, particularly as they encounter non-stationary data streams. The primary challenge in this domain is overcoming catastrophic forgetting, where the performance of a model on old tasks significantly diminishes when trained with new data. To address this, existing research has generally been divided into three main categories: (i) The *rehearsal-based methods* utilize a memory buffer to retain data samples from previous tasks, incorporating techniques such as experience replay [36], or constrained optimization to simultaneously train the model on current and previous tasks [8, 25]. (ii) The *regularization-based methods* introduce additional terms into the loss function to penalize changes in important model parameters, thereby limiting interference with previously learned tasks [7, 13, 18, 38]. EWC [13] remembers old tasks by selectively slowing down learning on the weights important for those tasks. OGD [7] constrains the parameters to move within the orthogonal space defined by the stored gradients of previous tasks. (iii) The *architecture-based methods* the aim is to minimize interference between tasks by dynamically expanding model capacity or creating isolated components for each task [17, 33, 35, 37, 46]. Progressive Prompts [35] enhances forward transfer and mitigates catastrophic forgetting by learning a distinct prompt for each new task and sequentially appending these new task-specific soft prompts to the ones previously learned.

Parameter-efficient Tuning. Recent works on parameter efficient tuning (PET) [9] have shown that training only a subset of model parameters can yield performance comparable to training the full model, reducing computational demands and annotation efforts [10, 11, 15, 48, 50]. BitFit [48] finds that updating only the bias-items during fine-tuning is very effective. Prompt tuning [15] uses learnable 'soft prompts' through back-propagation to condition frozen language models for specific tasks. LoRA [11] uses low-rank adapters in adapting models to new tasks with minimal additional parameters, and AdaLoRA [50] improves the performance of LoRA by adaptively allocating the parameter budget based on the weight matrices importance score. While the majority of PET has focused on learning one single task, there has been several efforts to apply PET to continual learning. AdapterCL [27] introduces an individual adapter block for each task. LFPT5 [31] utilizes a large soft prompt that is continuously trained on all tasks. O-LoRA [43] incrementally learns new tasks in orthogonal subspaces while keeping the LoRA parameters learned from previous tasks fixed to minimize catastrophic forgetting. InfLoRA [20] mitigates catastrophic forgetting by reparameterizing pre-trained weights with a small set of parameters, enabling fine-tuning within a subspace to maintain previous knowledge. The proposed MoE-Adapters and DDAS collaborate in [47] mitigates long-term forgetting by dynamically expanding a pre-trained CLIP model with Mixture-of-Experts adapters and preserves zero-shot recognition through a Distribution Discriminative Auto-Selector for routing in- and out-of-distribution inputs. ConPET [39] adapts existing continual learning strategies, originally developed for relatively smaller models to LLMs by incorporating PET with a dynamic replay approach. While O-LoRA addresses catastrophic forgetting through its incremental learning within orthogonal subspaces, it focuses on LoRA-based architecture rather than more general low-rank matrices and does not explore the knowledge transfer across different tasks.

A.2 Implementation Details

All our experiments involving T5 models were performed on a server outfitted with four NVIDIA A6000 GPUs, utilizing the DeepSpeed repository for implementation. For every sequence of tasks across different orders, we standardized our experimental setup as follows: A constant rate of $1e-3$ was maintained throughout the experiments. We used a total batch size of 32, distributed as 8 per GPU to leverage the computational capabilities of all four A6000 GPUs efficiently. We set the dropout rate at 0.1. We applied a regularization rate of 0.1 to the orthogonal matrices derived from the Singular Value Decomposition (SVD). A rate of 0.0 was employed, indicating no additional penalty on the model's weights during training.

A.3 Datasets

Tab. 6 provides detailed information on the 15 datasets utilized in our continual learning (CL) experiments, including the evaluation metrics used for assessment. Our selection encompasses datasets

from established benchmarks:: the standard CL benchmark [51], GLUE [42], and SuperGLUE benchmarks [41], and added IMDB movie reviews dataset.

Table 6: The details of 15 datasets used in our CL experiments. NLI denotes natural language inference, QA denotes questions and answers task. The first five tasks correspond to the standard CL benchmark, all other tasks are used in long-sequence experiments.

Dataset name	Category	Task	Domain	Metric
1. Yelp	CL Benchmark	Sentiment Analysis	Yelp Reviews	Accuracy
2. Amazon	CL Benchmark	Sentiment Analysis	Amazon Reviews	Accuracy
3. DBpedia	CL Benchmark	Topic Classification	Wikipedia	Accuracy
4. Yahoo	CL Benchmark	Topic Classification	Yahoo Q&A	Accuracy
5. AG News	CL Benchmark	Topic Classification	News	Accuracy
6. MNLI	GLUE	NLI	Various	Accuracy
7. QQP	GLUE	Paragraph Detection	QUora	Accuracy
8. RTE	GLUE	NLI	News, Wikipedia	Accuracy
9. SST-2	GLUE	Sentiment Analysis	Movie Reviews	Accuracy
10. WiC	SuperGLUE	Word Sense Disambiguation	Lexical Databases	Accuracy
11. CB	SuperGLUE	NLI	Various	Accuracy
12. COPA	SuperGLUE	QA	Blogs, Encyclopedia	Accuracy
13. BoolQA	SuperGLUE	Boolean QA	Wikipedia	Accuracy
14. MultiRC	SuperGLUE	QA	Various	Accuracy
15. IMDB	SuperGLUE	Sentiment Analysis	Movie Reviews	Accuracy

Table 7: Six different task sequence orders utilized in continual learning experiments. Orders 1-3 follow the standard continual learning benchmark as established by previous research, focusing on a more traditional task sequence. Orders 4-6 customized for long-sequence experimentation, encompass 15 tasks each and are structured according to the methodologies outlined in [35].

Order	Model	Task Sequence
1	T5-large, T5-base	dbpedia → amazon → yahoo → ag
2	T5-large, T5-base	dbpedia → amazon → ag → yahoo
3	T5-large, T5-base	yahoo → amazon → ag → dbpedia
4	T5-large	mnli → cb → wic → copa → qqp → boolqa → rte → imdb → yelp → amazon → sst-2 → dbpedia → ag → multirc → yahoo
5	T5-large	multirc → boolqa → wic → mnli → cb → copa → qqp → rte → imdb → sst-2 → dbpedia → ag → yelp → amazon → yahoo
6	T5-large	yelp → amazon → mnli → cb → copa → qqp → rte → imdb → sst-2 → dbpedia → ag → yahoo → multirc → boolqa → wic

A.4 Sensitivity Scores v.s. Fisher Information

In our analysis, we aim to elucidate the distribution of parametric knowledge intrinsic to different task orders and compare the sensitivity scores with Fisher Information. The insights from Fig. 6,7,8 indicate the distributions of parametric knowledge across layers remains consistent among different task orders. It suggests that regardless of the task sequence, the layer-wise distribution of parameters critical for task performance does not significantly vary. Both sensitivity scores and Fisher Information depict similar patterns, underscoring the robustness of our model’s learning mechanisms. Our findings also highlight that higher-level decoder layers exhibit increased sensitivity compared to their lower-level counterparts. This heightened sensitivity in the decoder suggests that these layers play a more crucial role in refining the outputs, possibly due to their direct involvement in generating end task results. Notably, the sensitivity scores of the encoder layers in task order 3 are higher than those observed in the first two task orders. This variation could be attributed to the specific nature or complexity of the tasks in order 3, which might demand more nuanced feature extraction capabilities from the encoder layers.

Table 8: Instructions for different tasks

Task	Prompts
NLI	What is the logical relationship between the "sentence 1" and the "sentence 2"? Choose one from the option.
QQP	Whether the "first sentence" and the "second sentence" have the same meaning? Choose one from the option.
SC	What is the sentiment of the following paragraph? Choose one from the option.
TC	What is the topic of the following paragraph? Choose one from the option.
BoolQA	According to the following passage, is the question true or false? Choose one from the option.
MultiRC	According to the following passage, is the question true or false? Choose one from the option.
WiC	Given a word and two sentences, whether the word is used with the same sense in both sentence? Choose one from the option.

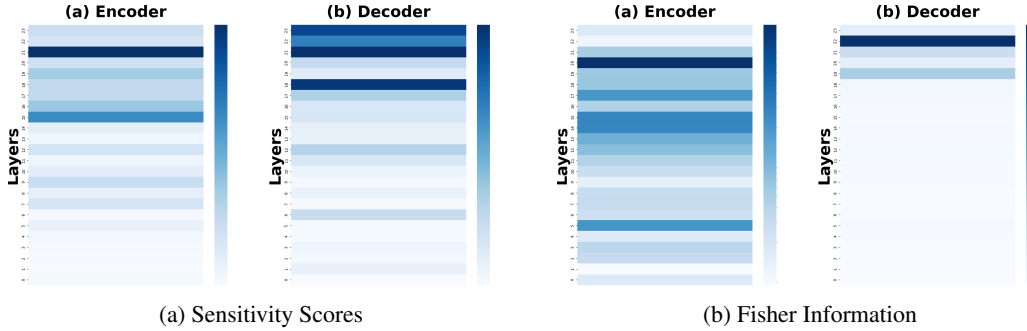


Figure 6: Order 1: Sensitivity scores and Fisher information of encoder and decoder Layers

A.5 Comparison of ROUGE score

We compare Average ROUGE-L scores (measures the longest common subsequence between the predicted and reference summaries, capturing sentence-level structure similarity) between O-LoRA and LB-CL on the standard CL benchmark in Tab. 9. It shows that the ROUGE-L scores of LB-CL achieve performance improvements across all three task orders of the Standard CL benchmark compared to O-LoRA, demonstrating the effectiveness of LB-CL.

Table 9: Comparison of ROUGE score between LB-CL and O-LoRA

Method	Order 1	Order 2	Order 3
O-LoRA	0.7902	0.7868	0.7859
LB-CL	0.8169	0.8090	0.7894

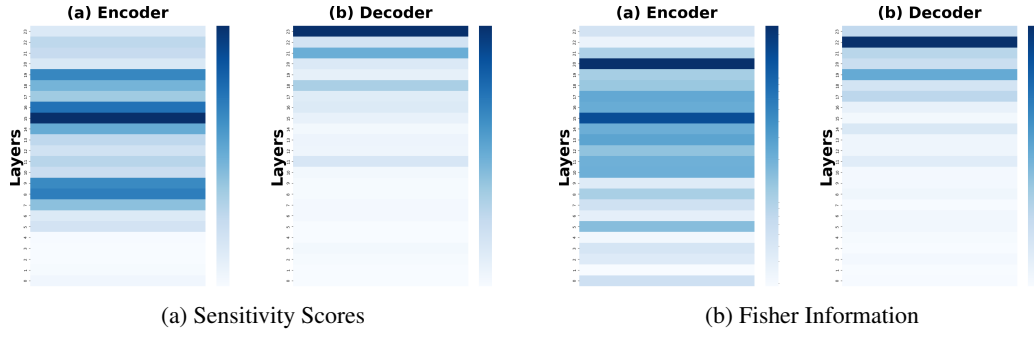


Figure 7: Order 2: Sensitivity scores and Fisher information of encoder and decoder Layers

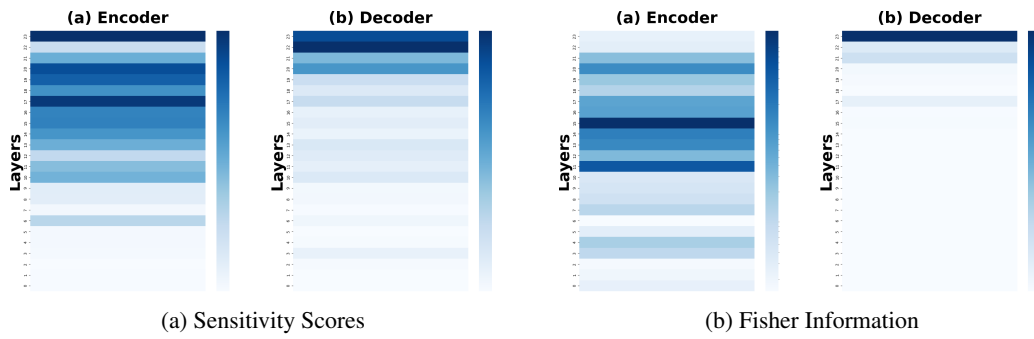


Figure 8: Order 3: Sensitivity scores and Fisher information of encoder and decoder Layers

NeurIPS Paper Checklist

1. Claims

Question: Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope?

Answer: [Yes]

Justification: In the abstract and introduction, we list our contributions.

Guidelines:

- The answer NA means that the abstract and introduction do not include the claims made in the paper.
- The abstract and/or introduction should clearly state the claims made, including the contributions made in the paper and important assumptions and limitations. A No or NA answer to this question will not be perceived well by the reviewers.
- The claims made should match theoretical and experimental results, and reflect how much the results can be expected to generalize to other settings.
- It is fine to include aspirational goals as motivation as long as it is clear that these goals are not attained by the paper.

2. Limitations

Question: Does the paper discuss the limitations of the work performed by the authors?

Answer: [No]

Justification: The paper has limitations, but those are not discussed in the paper.

Guidelines:

- The answer NA means that the paper has no limitation while the answer No means that the paper has limitations, but those are not discussed in the paper.
- The authors are encouraged to create a separate "Limitations" section in their paper.
- The paper should point out any strong assumptions and how robust the results are to violations of these assumptions (e.g., independence assumptions, noiseless settings, model well-specification, asymptotic approximations only holding locally). The authors should reflect on how these assumptions might be violated in practice and what the implications would be.
- The authors should reflect on the scope of the claims made, e.g., if the approach was only tested on a few datasets or with a few runs. In general, empirical results often depend on implicit assumptions, which should be articulated.
- The authors should reflect on the factors that influence the performance of the approach. For example, a facial recognition algorithm may perform poorly when image resolution is low or images are taken in low lighting. Or a speech-to-text system might not be used reliably to provide closed captions for online lectures because it fails to handle technical jargon.
- The authors should discuss the computational efficiency of the proposed algorithms and how they scale with dataset size.
- If applicable, the authors should discuss possible limitations of their approach to address problems of privacy and fairness.
- While the authors might fear that complete honesty about limitations might be used by reviewers as grounds for rejection, a worse outcome might be that reviewers discover limitations that aren't acknowledged in the paper. The authors should use their best judgment and recognize that individual actions in favor of transparency play an important role in developing norms that preserve the integrity of the community. Reviewers will be specifically instructed to not penalize honesty concerning limitations.

3. Theory Assumptions and Proofs

Question: For each theoretical result, does the paper provide the full set of assumptions and a complete (and correct) proof?

Answer: [NA]

Justification: The paper does not include theoretical results.

Guidelines:

- The answer NA means that the paper does not include theoretical results.
- All the theorems, formulas, and proofs in the paper should be numbered and cross-referenced.
- All assumptions should be clearly stated or referenced in the statement of any theorems.
- The proofs can either appear in the main paper or the supplemental material, but if they appear in the supplemental material, the authors are encouraged to provide a short proof sketch to provide intuition.
- Inversely, any informal proof provided in the core of the paper should be complemented by formal proofs provided in appendix or supplemental material.
- Theorems and Lemmas that the proof relies upon should be properly referenced.

4. Experimental Result Reproducibility

Question: Does the paper fully disclose all the information needed to reproduce the main experimental results of the paper to the extent that it affects the main claims and/or conclusions of the paper (regardless of whether the code and data are provided or not)?

Answer: [Yes]

Justification: We present datasets, models, and implementation details in the experimental section and appendix.

Guidelines:

- The answer NA means that the paper does not include experiments.
- If the paper includes experiments, a No answer to this question will not be perceived well by the reviewers: Making the paper reproducible is important, regardless of whether the code and data are provided or not.
- If the contribution is a dataset and/or model, the authors should describe the steps taken to make their results reproducible or verifiable.
- Depending on the contribution, reproducibility can be accomplished in various ways. For example, if the contribution is a novel architecture, describing the architecture fully might suffice, or if the contribution is a specific model and empirical evaluation, it may be necessary to either make it possible for others to replicate the model with the same dataset, or provide access to the model. In general, releasing code and data is often one good way to accomplish this, but reproducibility can also be provided via detailed instructions for how to replicate the results, access to a hosted model (e.g., in the case of a large language model), releasing of a model checkpoint, or other means that are appropriate to the research performed.
- While NeurIPS does not require releasing code, the conference does require all submissions to provide some reasonable avenue for reproducibility, which may depend on the nature of the contribution. For example
 - (a) If the contribution is primarily a new algorithm, the paper should make it clear how to reproduce that algorithm.
 - (b) If the contribution is primarily a new model architecture, the paper should describe the architecture clearly and fully.
 - (c) If the contribution is a new model (e.g., a large language model), then there should either be a way to access this model for reproducing the results or a way to reproduce the model (e.g., with an open-source dataset or instructions for how to construct the dataset).
 - (d) We recognize that reproducibility may be tricky in some cases, in which case authors are welcome to describe the particular way they provide for reproducibility. In the case of closed-source models, it may be that access to the model is limited in some way (e.g., to registered users), but it should be possible for other researchers to have some path to reproducing or verifying the results.

5. Open access to data and code

Question: Does the paper provide open access to the data and code, with sufficient instructions to faithfully reproduce the main experimental results, as described in supplemental material?

Answer: [No]

Justification: We use open-source datasets and models, but do not attach the code.

Guidelines:

- The answer NA means that paper does not include experiments requiring code.
- Please see the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- While we encourage the release of code and data, we understand that this might not be possible, so “No” is an acceptable answer. Papers cannot be rejected simply for not including code, unless this is central to the contribution (e.g., for a new open-source benchmark).
- The instructions should contain the exact command and environment needed to run to reproduce the results. See the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- The authors should provide instructions on data access and preparation, including how to access the raw data, preprocessed data, intermediate data, and generated data, etc.
- The authors should provide scripts to reproduce all experimental results for the new proposed method and baselines. If only a subset of experiments are reproducible, they should state which ones are omitted from the script and why.
- At submission time, to preserve anonymity, the authors should release anonymized versions (if applicable).
- Providing as much information as possible in supplemental material (appended to the paper) is recommended, but including URLs to data and code is permitted.

6. Experimental Setting/Details

Question: Does the paper specify all the training and test details (e.g., data splits, hyper-parameters, how they were chosen, type of optimizer, etc.) necessary to understand the results?

Answer: [Yes]

Justification: We present datasets, models, and implementation details in the experimental section and appendix.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The experimental setting should be presented in the core of the paper to a level of detail that is necessary to appreciate the results and make sense of them.
- The full details can be provided either with the code, in appendix, or as supplemental material.

7. Experiment Statistical Significance

Question: Does the paper report error bars suitably and correctly defined or other appropriate information about the statistical significance of the experiments?

Answer: [No]

Justification: The experimental results are not presented as error bars.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The authors should answer "Yes" if the results are accompanied by error bars, confidence intervals, or statistical significance tests, at least for the experiments that support the main claims of the paper.
- The factors of variability that the error bars are capturing should be clearly stated (for example, train/test split, initialization, random drawing of some parameter, or overall run with given experimental conditions).
- The method for calculating the error bars should be explained (closed form formula, call to a library function, bootstrap, etc.)
- The assumptions made should be given (e.g., Normally distributed errors).
- It should be clear whether the error bar is the standard deviation or the standard error of the mean.
- It is OK to report 1-sigma error bars, but one should state it. The authors should preferably report a 2-sigma error bar than state that they have a 96% CI, if the hypothesis of Normality of errors is not verified.

- For asymmetric distributions, the authors should be careful not to show in tables or figures symmetric error bars that would yield results that are out of range (e.g. negative error rates).
- If error bars are reported in tables or plots, The authors should explain in the text how they were calculated and reference the corresponding figures or tables in the text.

8. Experiments Compute Resources

Question: For each experiment, does the paper provide sufficient information on the computer resources (type of compute workers, memory, time of execution) needed to reproduce the experiments?

Answer: [Yes]

Justification: We report the details in the appendix.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The paper should indicate the type of compute workers CPU or GPU, internal cluster, or cloud provider, including relevant memory and storage.
- The paper should provide the amount of compute required for each of the individual experimental runs as well as estimate the total compute.
- The paper should disclose whether the full research project required more compute than the experiments reported in the paper (e.g., preliminary or failed experiments that didn't make it into the paper).

9. Code Of Ethics

Question: Does the research conducted in the paper conform, in every respect, with the NeurIPS Code of Ethics <https://neurips.cc/public/EthicsGuidelines>?

Answer: [Yes]

Justification: We follow the ethics.

Guidelines:

- The answer NA means that the authors have not reviewed the NeurIPS Code of Ethics.
- If the authors answer No, they should explain the special circumstances that require a deviation from the Code of Ethics.
- The authors should make sure to preserve anonymity (e.g., if there is a special consideration due to laws or regulations in their jurisdiction).

10. Broader Impacts

Question: Does the paper discuss both potential positive societal impacts and negative societal impacts of the work performed?

Answer: [NA]

Justification: We focus on the techniques.

Guidelines:

- The answer NA means that there is no societal impact of the work performed.
- If the authors answer NA or No, they should explain why their work has no societal impact or why the paper does not address societal impact.
- Examples of negative societal impacts include potential malicious or unintended uses (e.g., disinformation, generating fake profiles, surveillance), fairness considerations (e.g., deployment of technologies that could make decisions that unfairly impact specific groups), privacy considerations, and security considerations.
- The conference expects that many papers will be foundational research and not tied to particular applications, let alone deployments. However, if there is a direct path to any negative applications, the authors should point it out. For example, it is legitimate to point out that an improvement in the quality of generative models could be used to generate deepfakes for disinformation. On the other hand, it is not needed to point out that a generic algorithm for optimizing neural networks could enable people to train models that generate Deepfakes faster.
- The authors should consider possible harms that could arise when the technology is being used as intended and functioning correctly, harms that could arise when the

technology is being used as intended but gives incorrect results, and harms following from (intentional or unintentional) misuse of the technology.

- If there are negative societal impacts, the authors could also discuss possible mitigation strategies (e.g., gated release of models, providing defenses in addition to attacks, mechanisms for monitoring misuse, mechanisms to monitor how a system learns from feedback over time, improving the efficiency and accessibility of ML).

11. Safeguards

Question: Does the paper describe safeguards that have been put in place for responsible release of data or models that have a high risk for misuse (e.g., pretrained language models, image generators, or scraped datasets)?

Answer: [NA]

Justification: Our paper poses no such risks.

Guidelines:

- The answer NA means that the paper poses no such risks.
- Released models that have a high risk for misuse or dual-use should be released with necessary safeguards to allow for controlled use of the model, for example by requiring that users adhere to usage guidelines or restrictions to access the model or implementing safety filters.
- Datasets that have been scraped from the Internet could pose safety risks. The authors should describe how they avoided releasing unsafe images.
- We recognize that providing effective safeguards is challenging, and many papers do not require this, but we encourage authors to take this into account and make a best faith effort.

12. Licenses for existing assets

Question: Are the creators or original owners of assets (e.g., code, data, models), used in the paper, properly credited and are the license and terms of use explicitly mentioned and properly respected?

Answer: [Yes]

Justification: We cite the datasets and baseline papers in the experiment section.

Guidelines:

- The answer NA means that the paper does not use existing assets.
- The authors should cite the original paper that produced the code package or dataset.
- The authors should state which version of the asset is used and, if possible, include a URL.
- The name of the license (e.g., CC-BY 4.0) should be included for each asset.
- For scraped data from a particular source (e.g., website), the copyright and terms of service of that source should be provided.
- If assets are released, the license, copyright information, and terms of use in the package should be provided. For popular datasets, paperswithcode.com/datasets has curated licenses for some datasets. Their licensing guide can help determine the license of a dataset.
- For existing datasets that are re-packaged, both the original license and the license of the derived asset (if it has changed) should be provided.
- If this information is not available online, the authors are encouraged to reach out to the asset's creators.

13. New Assets

Question: Are new assets introduced in the paper well documented and is the documentation provided alongside the assets?

Answer: [NA]

Justification: The paper does not release new assets.

Guidelines:

- The answer NA means that the paper does not release new assets.

- Researchers should communicate the details of the dataset/code/model as part of their submissions via structured templates. This includes details about training, license, limitations, etc.
- The paper should discuss whether and how consent was obtained from people whose asset is used.
- At submission time, remember to anonymize your assets (if applicable). You can either create an anonymized URL or include an anonymized zip file.

14. **Crowdsourcing and Research with Human Subjects**

Question: For crowdsourcing experiments and research with human subjects, does the paper include the full text of instructions given to participants and screenshots, if applicable, as well as details about compensation (if any)?

Answer: [NA]

Justification: Our paper does not involve crowdsourcing nor research with human subjects.

Guidelines:

- The answer NA means that the paper does not involve crowdsourcing nor research with human subjects.
- Including this information in the supplemental material is fine, but if the main contribution of the paper involves human subjects, then as much detail as possible should be included in the main paper.
- According to the NeurIPS Code of Ethics, workers involved in data collection, curation, or other labor should be paid at least the minimum wage in the country of the data collector.

15. **Institutional Review Board (IRB) Approvals or Equivalent for Research with Human Subjects**

Question: Does the paper describe potential risks incurred by study participants, whether such risks were disclosed to the subjects, and whether Institutional Review Board (IRB) approvals (or an equivalent approval/review based on the requirements of your country or institution) were obtained?

Answer: [NA]

Justification: Our paper does not involve crowdsourcing nor research with human subjects

Guidelines:

- The answer NA means that the paper does not involve crowdsourcing nor research with human subjects.
- Depending on the country in which research is conducted, IRB approval (or equivalent) may be required for any human subjects research. If you obtained IRB approval, you should clearly state this in the paper.
- We recognize that the procedures for this may vary significantly between institutions and locations, and we expect authors to adhere to the NeurIPS Code of Ethics and the guidelines for their institution.
- For initial submissions, do not include any information that would break anonymity (if applicable), such as the institution conducting the review.