

Aioli: A unified optimization framework for language model data mixing

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Abstract

Language model performance depends on identifying the optimal mixture of data groups to train on (e.g., law, code, math). Prior work has proposed a diverse set of methods to efficiently learn mixture proportions, ranging from fitting regression models over training runs to dynamically updating proportions throughout training. Surprisingly, we find that no existing method consistently outperforms a simple stratified sampling baseline in terms of average test perplexity. To understand this inconsistency, we unify existing methods into a standard framework, showing they are equivalent to solving a common optimization problem: minimize average loss subject to a method-specific *mixing law*—an implicit assumption on the relationship between loss and mixture proportions. This framework suggests that measuring the fidelity of a method’s mixing law can offer insights into its performance. Empirically, we find that existing methods set their mixing law parameters inaccurately, resulting in the inconsistent mixing performance we observe. Using this insight, we derive a new online method named **AIOLI**, which directly estimates the mixing law parameters throughout training and uses them to dynamically adjust proportions. **AIOLI** outperforms stratified sampling on 6 out of 6 datasets by an average of 0.27 test perplexity points, whereas existing methods fail to consistently beat stratified sampling, doing up to 6.9 points worse. Moreover, in a practical setting where proportions are learned on shorter runs due to computational constraints, **AIOLI** can dynamically adjust these proportions over the full training run, consistently improving performance over existing methods by up to 12.012 test perplexity points.

1 Introduction

It is important to determine what data to train on for a language model (LM) to acquire a range of capabilities, from generating code to understanding scientific literature and conversing with users [3, 34, 39]. To achieve this, practitioners mix data from various groups (such as code files, scientific papers, and chat logs) in specific proportions to compose an overall training dataset—a procedure known as *data mixing*. Identifying the optimal mixture proportions is critical to LLM performance. However, a brute-force trial-and-error search over the proportions is computationally expensive, requiring many training runs.

Recent work introduces two types of data mixing algorithms that *learn* mixture proportions: offline and online methods. Offline methods conduct multiple training runs with varying proportions, fit a regression model to predict performance, and use this model to determine the optimal static mixture [37, 72]. Online methods adjust the mixture proportions dynamically throughout training using information from the model, such as its loss and gradients [2, 14, 22, 70]. All mixing methods require at least one training run to learn the proportions but are more efficient than a brute-force search.

Given the wide range of methods available, it is important to determine which ones are effective. However, when we evaluated existing methods, we found that *no method consistently outperformed stratified sampling*—a simple baseline that uniformly mixes groups and requires zero extra training runs—across all sets of data groups in terms of average test perplexity (Table 2). This surprising outcome suggests that all existing methods suffer from some common weaknesses. To make progress in data mixing, we identify three objectives: 1) improve our **understanding** of the underlying assumptions of existing methods, 2) assess the **fidelity** of these assumptions in practice to better understand performance, and 3) apply our insights to develop principled **new data mixing methods**.

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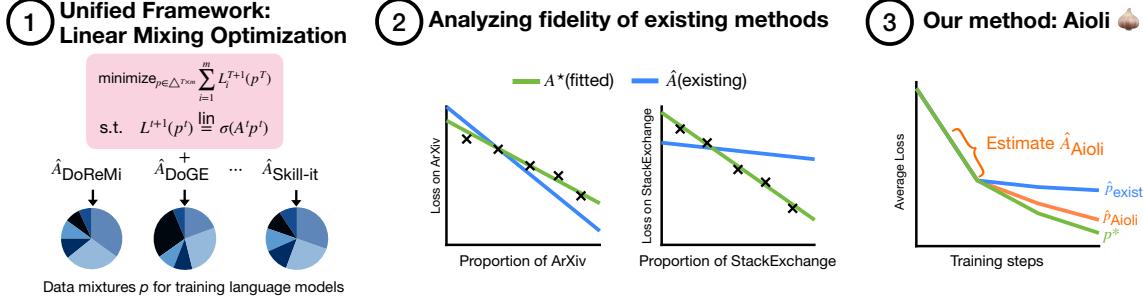


Figure 1: Left: existing methods can be expressed in a unified optimization framework, in which they implicitly assume a linear or log-linear loss-proportion relationship. Center: the (log)-linear parameterizations are well-specified, but existing methods set their parameters incorrectly. Right: AIOLI, an online mixing method that more accurately estimates the parameters that capture the true loss-proportion relationship.

In this paper, we improve our **understanding** of data mixing methods by showing that many existing methods can be expressed in a unified optimization framework, which we call Linear Mixing Optimization (LMO) (Section 3). These methods are equivalent to solving an optimization problem that sets proportions to minimize the average loss per data group, subject to an implicit method-dependent *mixing law*—an assumption relating loss per group and mixture proportions. We find that all current mixing laws share the same parameterization: for training round t from 1 to T ,

$$L^{t+1}(p^t) \stackrel{\text{lin}}{=} \sigma(A^t p^t),$$

where $p^t \in \Delta^m$ (the simplex) are mixing proportions over m given data groups at time t , $L^{t+1}(p^t) : \Delta^m \rightarrow (\mathbb{R}^+)^m$ are the losses per group at the next timestep, $A^t \in \mathbb{R}^{m \times m}$ is a parameter matrix, $\sigma = \text{Id}$ or \exp , and $\stackrel{\text{lin}}{=}$ means equal up to linear transformation. Existing offline methods assume a static ($T = 1$) log-linear parameterization of the mixing law, while online methods assume a linear dynamic mixing law. All methods set the parameters of their mixing laws differently (Table 1), and offline methods solve the optimization problem directly while online methods solve it greedily using exponentiated gradient descent. Our framework reveals the underlying assumptions of each method in terms of the mixing law’s parameterization, the values of the parameters, and how the optimization problem is solved. Furthermore, the fidelity of the mixing law and solving strategy dictates the optimality of the method, providing us with a new tool for understanding data mixing methods.

Applying the LMO framework, we test the **fidelity** of existing methods’ assumptions, examining if they hold in practice (Section 4). Both the log-linear static and linear dynamic parameterizations capture the true loss-proportion relationship across datasets, achieving an average of 0.0005 MSE and 0.969 R^2 . We then show that although existing mixing laws are well-specified, methods can set their parameters (A^t) inaccurately, causing poor performance. We compare each method’s parameters to the optimal parameters, which we approximate by fitting the mixing laws to training runs. We find that the method’s parameters can differ significantly from the optimal parameters, and the extent of these deviations is correlated with method performance relative to stratified sampling (Figure 3), helping explain our initial observations. Finally, we validate the assumptions used in solving the optimization problem, finding that the greedy approximation in online methods is a reasonable proxy for the full objective. Our analysis shows that existing methods’ parameterizations and solving strategies are of high fidelity, but their parameters are not.

To validate these insights, we develop AIOLI, a **simple new online data mixing method** derived from the LMO framework (Section 5). Unlike existing online methods, AIOLI directly estimates the parameters A^t from the current training run by fitting the mixing law on the history of losses and dynamic mixture proportions so far. AIOLI is thus able to dynamically adjust proportions without requiring any extra training runs.

We evaluate AIOLI in two settings by training 160M models on various combinations of data sources from SlimPajama [54] (Section 6). First, we compare AIOLI to existing data mixing methods and find that AIOLI consistently outperforms stratified sampling on all 6 datasets, by an average of 0.274 and up to 0.439 points in test perplexity. On the other hand, existing data mixing methods do worse than stratified on at least one dataset by up to 6.9 perplexity points, despite using extra training runs. As we expect, the parameters of AIOLI are also more consistently close to the optimal parameters (Figure 2). Second, we consider a scenario with limited additional computational resources, in which practitioners cannot run experiments for learning mixture proportions for the full training duration. In this setting, mixture proportions learned on a shorter run may not perform well on the longer final run. We find that using AIOLI to dynamically adjust these learned proportions throughout the final training run can improve performance by an average of 1.202 perplexity points in 28 out of 30 cases, compared to using the learned proportions directly.

2 Problem Setup

We formalize the data mixing problem and establish notation. In data mixing, we have m data groups of text, such as GitHub, BooksCorpus, and arXiv. We are given train, validation, and test sets for each data group, which we denote as $D_{\text{train}}^i, D_{\text{val}}^i, D_{\text{test}}^i$ for the i th group. Define $D_{\text{train}} = \{D_{\text{train}}^1, \dots, D_{\text{train}}^m\}$, and similarly define D_{val} and D_{test} .

Data & Mixing. During training, we show the model a total of N examples from D_{train} over S training steps. To express how data proportions can change throughout training, we divide training into T equal rounds. Each round t uses a mixture proportion from the probability simplex: $p^t = [p_1^t, \dots, p_m^t] \in \Delta^m$. *Static mixtures* use only a single round ($T = 1$): $\mathbf{p} = (p^1)$, while *dynamic mixtures* use several ($T > 1$): $\mathbf{p} = (p^1, \dots, p^T)$.

Model & Loss. Let $f(\mathbf{p}, t)$ refer to the language model, f , at the beginning of round t where the model has been trained on data sampled using mixture proportions p^1, \dots, p^{t-1} so far. Given a model f , we can compute its loss on each group using the training data, $L_{\text{train}}(f) = (L_{\text{train},1}(f), \dots, L_{\text{train},m}(f))$, and similarly with the validation, $L_{\text{val}}(f)$, and test data, $L_{\text{test}}(f)$. In this notation, the loss at the end of training can be expressed as $L_{(\cdot)}(f(\mathbf{p}, T+1))$. When the f being referred to is obvious, we simply write $L_{(\cdot)}^t(\mathbf{p})$, and for static mixtures we drop the superscript: $L_{(\cdot)}(\mathbf{p})$.

Data Mixing Problem. Given a set of data groups, an LM f to train for S steps with N samples, and T rounds of training (i.e., whether we use static or dynamic proportions), we aim to determine the \mathbf{p} that minimizes the total test loss across groups: $\underset{\mathbf{p} \in \Delta^{T \times m}}{\text{minimize}} \sum_{i=1}^m L_{\text{test},i}^{T+1}(\mathbf{p})$.

This objective aims to produce a trained model that does well on many data groups, which can serve as a proxy for downstream performance. However, without assuming additional structure on $L^{T+1}(\mathbf{p})$, this problem can only be solved with a brute-force search over \mathbf{p} , which requires training many different models. In the next section, our LMO framework imposes a constraint on $L^{t+}(\mathbf{p})$ that allows many existing methods to be expressed as approaches to solving this problem.

3 A Unified Optimization Framework for Data Mixing

We introduce the LMO framework by stating the general optimization problem (Section 3.1). Then, we show how this framework can express several existing methods (Section 3.2, 3.3), with a summary of our insights regarding these methods in Section 3.3.3.

3.1 Linear Mixing Optimization (LMO) Framework

The LMO framework consists of an optimization problem that is equivalent to the data mixing minimization problem (Section 2), subject to an additional constraint:

$$\underset{\mathbf{p} \in \Delta^{T \times m}}{\text{minimize}} \sum_{i=1}^m L_{\text{val},i}^{T+1}(\mathbf{p}) \quad (1)$$

$$\text{s.t. } L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t + b_i^t \sigma \left(\sum_{j=1}^m -A_{ij}^t p_j^t \right) \forall i \in [m], t \in [T] \quad (2)$$

for some A^t, b^t, c^t , and σ . $A^t \in \mathbb{R}^{m \times m}$ is a matrix that encodes cross-group interactions, where A_{ij}^t intuitively describes how much training on group j at t impacts group i 's loss. $b^t, c^t \in \mathbb{R}^m$ are group-specific parameters. $\sigma : \mathbb{R} \rightarrow \mathbb{R}$ is either the identity function (Id) or the exponential function (exp). We refer to the constraint in (2) as a *mixing law* that specifies the assumed relationship between loss and proportions.

There are three components of this problem that need to be specified to yield a way to set \mathbf{p} : a) the parameterization of the mixing law (T, σ), b) the values of the parameters (A^t, b^t, c^t), and c) how to solve the problem. We express existing methods in LMO by specifying these components.

3.2 Preliminaries for unifying methods

We discuss preliminaries before presenting existing methods and explaining how they can be expressed in the LMO framework. First, we formally define what it means for a method to be *expressed* in the LMO framework. Then, we present a result that allows us to convert between linear dynamic mixing laws and a way to set \mathbf{p} , which we will use to express online methods in our framework in Section 3.3.

Method	1) Mixing Law Parameterization	2) Parameters	3) Solver
DML	$L_{\text{val},i}(\mathbf{p}) = c_i + b_i \exp\left(\sum_{j=1}^m -A_{ij}p_j\right)$	Fit from $\geq m+1$ training runs	Direct
Skill-It	$L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$	$A_{ij}^t = L_{\text{val},i}^t(\mathbf{p})(L_{\text{val},i}^{t+1}(\mathbf{1}_j) - L_{\text{val},i}^t(\mathbf{1}_j))/L_{\text{val},i}^t(\mathbf{1}_j)$	EGD
DoReMi	$L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$	$A_{ii}^t = \min\{L_{\text{train},i}^t(\mathbf{p}) - L_{\text{train},i}^t(f_{\text{ref}}), 0\}$	EGD
DoGE	$L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$	$A_{ij}^t = \langle \nabla L_{\text{val},i}^t(\mathbf{p}), \nabla L_{\text{train},j}^t(\mathbf{p}) \rangle$	EGD
AIOLI	$L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - \sum_{j=1}^m A_{ij}^t p_j^t$	Fit from history of L_{val} and \mathbf{p}	EGD

Table 1: Summary of how existing methods and AIOLI are expressed in the LMO framework (1).

Definition 1. We say that a data mixing method can be **expressed** in the LMO framework if its exact algorithm—how it sets proportions \mathbf{p} and trains model f in terms of \mathbf{p} —can be equivalently constructed by specifying a mixing law and way of solving the LMO optimization problem.

This definition allows us to cast existing methods as a way of solving the LMO optimization problem based on how they set \mathbf{p} and train according to \mathbf{p} , even if the methods themselves are not originally designed to minimize average test loss.

Converting mixing laws into update rules. When $T > 1$, a natural way to solve the LMO optimization problem is via exponentiated gradient descent (EGD) [5, 31], which updates p^t greedily while ensuring that it remains on the probability simplex. The following lemma presents the EGD update rule for the LMO optimization problem when $\sigma = \text{Id}$.

Lemma 1. The EGD update rule for (1) subject to $L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t - b_i^t \sum_{j=1}^m A_{ij}^t p_j^t \forall i \in [m]$ is

$$p_j^{t+1} = \frac{1}{Z^t} \cdot p_j^t \exp\left(\eta \sum_{i=1}^m b_i^t A_{ij}^t\right) \forall j \in [m], \quad (3)$$

where $\eta > 0$ is the step size and Z^t is a normalizing constant such that $p_j^{t+1} \in \Delta^m$.

This lemma shows how to adjust p^t dynamically to solve the LMO optimization problem. Notably, this update rule is defined in terms of the mixing law parameters, A^t and b^t . This gives us a way to convert between how a method sets \mathbf{p} and the implicit *assumption* it makes in the mixing law.

3.3 Unifying Existing Methods

We discuss four existing data mixing methods and express them as specific instances of the LMO framework. A summary of our insights is provided in Section 3.3.3 and Table 1. In Appendix B.1, we comment on how several other online and offline data mixing methods are related to our framework, and all proofs for this section are in Appendix B.2.

3.3.1 Offline methods

Data Mixing Laws (DML). Ye et al. [72] propose an offline method using a static mixing law ($T = 1$): $L_{\text{val},i}(\mathbf{p}) = c_i + b_i \exp(\sum_{j=1}^m -A_{ij}p_j)$ for $i \in [m]$, with A, b, c learned by sweeping training runs over static proportions ($\geq m+1$ runs to avoid being underdetermined). They select the proportion that minimizes the predicted validation loss. This law can be derived from (2) with $\sigma = \exp$, showing that LMO with a) log-linear static mixing law, b) fitted parameters, and c) direct computation of \mathbf{p} can express DML.

3.3.2 Online Methods

We provide a colloquial description and an algorithmic description of the following three online methods. Then, in Theorem 1 we demonstrate how they all are expressed in LMO using a linear dynamic mixing law, the EGD update rule, and method-specific mixing law parameters.

Skill-It. Chen et al. [14] is an online method motivated by curriculum learning that dynamically adjusts mixture proportions. Data group interactions are expressed in a “skills graph,” where each edge denotes how much the loss on one group changes when trained on another. The skills graph is learned in advance using m training runs and then used to update proportions p^t throughout training.

Concretely, the skills graph matrix A^{SG} has entries $A_{ij}^{\text{SG}} = (L_{\text{val},i}^{T+1}(\mathbf{1}_j) - L_{\text{val},i}^1(\mathbf{1}_j))/L_{\text{val},i}^1(\mathbf{1}_j)$ indicating the relative decrease in loss on group i when training a model on group j only. This is used in the Skill-It update rule, $p_j^{t+1} \propto p_j^t \exp(\eta \sum_{i=1}^m A_{ij}^{\text{SG}} L_{\text{val},i}^t(\mathbf{p}))$ for all $j \in [m]$ and learning rate $\eta > 0$. This rule determines p^{t+1} , which is then used to sample D_{train} for training f in the next round.

DoReMi. Xie et al. [70] is an online method that applies ideas from distributionally robust optimization to data mixing, where the training objective minimizes the worst-group excess loss over a model trained with stratified sampling. p^t is

updated dynamically to minimize this excess loss and then averaged for the final run. DoReMi requires two additional runs to learn a static \mathbf{p} .

Concretely, let $f_{\text{ref}} = f(\text{Unif}(m), T+1)$ denote a “reference model” that is first trained using stratified sampling. Then, a “proxy model” uses dynamic proportions according to the update rule $p_j^{t+1} \propto p_j^t \exp(\eta \max\{L_{\text{train},j}^t(\mathbf{p}) - L_{\text{train},j}(f_{\text{ref}}), 0\})$ for all $j \in [m]$ and step size $\eta > 0$. This p^{t+1} is used to weight the training objective, such that the proxy model is updated to minimize $\sum_{i=1}^m p_i^{t+1} L_{\text{train},i}(f)$ at the next timestep. The averaged static proportions $\frac{1}{T} \sum_{t=1}^T p^t$ are then used in the final run.

DoGE. Fan et al. [22] is an online method that solves a bi-level optimization problem in which p^t is updated to minimize the average training loss at each step. By using a first-order Taylor approximation of the training loss, p^t is updated using the gradient of each data group. The dynamic proportions are then averaged for the final run. DoGE requires one additional run to learn a static \mathbf{p} .

Concretely, a proxy model is trained using $p_j^{t+1} \propto p_j^t \exp(\eta \langle \nabla L_{\text{train},j}(f^t), \sum_{i=1}^m \nabla L_{\text{val},i}(f^t) \rangle)$, and f is updated to minimize the training loss weighted by p^t , similar to DoReMi. The averaged static proportions $\frac{1}{T} \sum_{t=1}^T p^t$ are used in the final run.

Framework expression. All three online methods use an update rule $p_j^{t+1} \propto p_j^t \exp(\cdot)$, which is similar to (3). This provides intuition for our main theorem, which expresses these methods in LMO.

Theorem 1. Define the following parameters for each method:

- $A^{t, \text{Skill-It}} \in \mathbb{R}^{m \times m}$, where $A_{ij}^{t, \text{Skill-It}} = L_{\text{val},i}^t(\mathbf{p})(L_{\text{val},i}^{T+1}(\mathbf{1}_j) - L_{\text{val},i}^1(\mathbf{1}_j)) / L_{\text{val},i}^1(\mathbf{1}_j)$ for all $i, j \in [m]$,
- $A^{t, \text{DRM}} \in \mathbb{R}^{m \times m}$, where $A_{ii}^{t, \text{DRM}} = \min\{L_{\text{train},i}^t(\mathbf{p}) - L_{\text{train},i}(f_{\text{ref}}), 0\}$ and $A_{ij}^{t, \text{DRM}} = 0$ for $i \neq j$,
- $A^{t, \text{DoGE}} \in \mathbb{R}^{m \times m}$, where $A_{ij}^{t, \text{DoGE}} = \langle \nabla L_{\text{val},i}^t(\mathbf{p}), \nabla L_{\text{train},j}^t(\mathbf{p}) \rangle$ for all $i, j \in [m]$.

Instantiating the LMO framework (1) with a) a linear dynamic mixing law $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$, b) parameters $A^t = A^{t, \text{Skill-It/DRM/DoGE}}$, and c) EGD to solve for \mathbf{p} allows for us to express Skill-It, DoReMi, and DoGE, respectively.

3.3.3 Summary of LMO Framework Insights

Table 1 summarizes how existing methods are expressed in the LMO framework. LMO reveals the assumptions each method makes through how the components of the framework are specified. First, all mixing laws are either linear or log-linear. Second, the mixing laws differ in the values of the parameters used. For example, Skill-It’s A^t is the current loss times a static skills graph matrix, while DoReMi’s A^t is diagonal. Third, offline mixing methods solve for \mathbf{p} directly while online mixing methods use EGD, which uses a greedy approximation. If the mixing law and solving strategy assumptions hold true in practice, then the method yields optimal mixture proportions. In the next section, we study the fidelity of these assumptions.

4 Analyzing Fidelity of Existing Methods with the LMO Framework

We examine the fidelity of the assumptions made by existing methods in terms of the three components of the LMO framework: a) the mixing law parameterization, b) values of the mixing law parameters, and c) how to solve the optimization problem for \mathbf{p} . After providing experiment details (Section 4.1), we discuss these three components in order (Section 4.2-4.4).

4.1 Experiment Details

Data settings. We use a sampled version of SlimPajama [54, 73], a pre-processed version of the RedPajama pretraining dataset [62]. SlimPajama consists of 7 data groups: ArXiv, Books, CommonCrawl, C4 [51], Github, StackExchange, and Wikipedia. To develop a fine-grained understanding of data mixing, we create 6 settings by extracting combinations of these groups. We study three settings with $m = 2$: Arxiv/Stackexchange, Github/C4, and Book/StackExchange. We study two settings with $m = 3$: Arxiv/Book/StackExchange and CommonCrawl/Github/Wikipedia. Finally, we study mixing over the full SlimPajama dataset with $m = 7$.

Models. We train 160M parameter GPT-style decoder-only LLMs with batch size 8 and context length 2048. For $m = 2, 3$, we train for 5K steps, and for $m = 7$, we train for 40K steps.

Training sweeps. To assess the true loss-proportion relationship and compare it to the assumptions made by existing methods, we conduct training sweeps over different mixture proportions, denoted as \mathcal{P} . For $m = 2$, we set

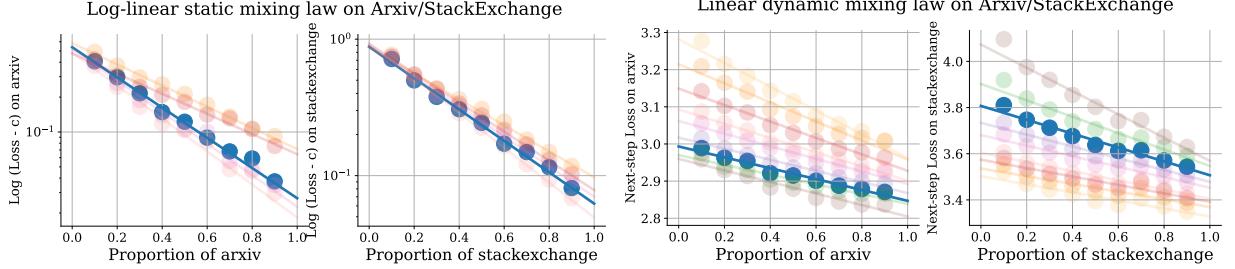


Figure 2: Left: p_i vs $\log(L_{\text{val},i}(\mathbf{p}) - c_i)$ with fitted static log-linear mixing law. Right: p_i^t vs $L_{\text{val},i}(\mathbf{p})$ with fitted linear dynamic mixing law. Colors represent random seeds (left) and initial $p^0 \in \mathcal{P}$ (right, blue is 0.7, 0.3). Both laws fit the true loss-proportion relationship well.

$\mathcal{P} = \{[0.1, 0.9], [0.2, 0.8], \dots, [0.9, 0.1]\}$. For $m = 3$ and 7 , we set \mathcal{P} equal to $10 \mathbf{p}$ ’s and $40 \mathbf{p}$ ’s drawn from the Dirichlet distribution with $\alpha = 1.0$ and 1.5 , respectively.

4.2 Mixing law parameterization

We examine whether existing methods’ mixing law parameterizations—log-linear static and linear dynamic—capture the true loss-proportion relationship. By empirically fitting them to loss-proportion pairs, we find that both parameterizations are indeed well-specified. Full results for both mixing laws are in Table 5 in Appendix C.1. We discuss the generality of these parameterizations across training scales and other datasets, as well as higher-order parameterizations, in Appendix C.1.1.

Setup. For the *log-linear static mixing law*, we study if there exists A, b, c such that $L_{\text{val},i}(\mathbf{p})$ can be expressed as $c_i + b_i \exp(\sum_{j=1}^m -A_{ij}p_j)$ for all $i \in [m]$. We fit the parameters using full training runs on \mathcal{P} . For the *linear dynamic mixing law*, we study if there exists A^t such that $L_{\text{val},i}^{t+1}(\mathbf{p})$ can be expressed as $L_{\text{val},i}^t(\mathbf{p}) - \sum_{j=1}^m A_{ij}^t p_j^t$, for all $i \in [m]$ (b^t is absorbed into A^t). To fit A^t , we select a timestep t and train on a static proportion $p^0 \in \mathcal{P}$ for all p^1, \dots, p^t until time t , and at $t + 1$ we sweep the values of $p^{t+1} \in \mathcal{P}$.

Results. On average across our 6 data settings, the mean squared error (MSE) of the fitted log-linear static mixing law is 8.9×10^{-4} , and the R^2 coefficient of determination is 0.991. The average MSE of the fitted linear dynamic mixing law is 1.0×10^{-4} and the R^2 is 0.947. See Figure 2 for examples. Since both parameterizations have high R^2 and low MSE, we conclude that they capture the true loss-proportion relationship well and are of high fidelity.

4.3 Values of mixing law parameters

As shown in Table 1, each method sets the parameters of its mixing law differently. We study how close the method-specific parameters are to the optimal parameters that are obtained when fitting the method’s mixing law to the true loss-proportion relationship, and if these parameter disparities are reflected in method performance. We find that existing methods’ differences in mixing law parameters are largely responsible for their performance. We omit studying DML since its parameters are fitted from full training runs and hence differ from the optimal in estimation error only.

Setup. For Skill-It, DoReMi, and DoGE, we select a step t and obtain the method-specific A^t . We then sweep \mathcal{P} for the next round $t + 1$. This sweep is used to approximate an optimal A^{t*} that captures the true loss-mixture relationship, $L_{\text{val}}^{t+1}(\mathbf{p}) = L_{\text{val}}^t(\mathbf{p}) - A^{t*}p^t$, as well as fit a $b^t \in \mathbb{R}$ used for scaling A^t (details in Appendix C.2). We study the relationship between $\tilde{A}^t := b^t A^t$ and A^{t*} , and how it is related to the performance of the method.

To express similarity between \tilde{A}^t and A^{t*} in a way that is reflected in performance, we observe that from Lemma 1, p^t is updated using the column sum of A^t , $\mathbf{1}^\top A^t$. Moreover, the magnitude of A^t is not critical to performance since the step size η can always be tuned to control this. Therefore, we compare the vectors $\tilde{a}^t = \mathbf{1}^\top \tilde{A}^t / \|\mathbf{1}^\top \tilde{A}^t\|_2$ and $a^{t*} = \mathbf{1}^\top A^{t*} / \|\mathbf{1}^\top A^{t*}\|_2$. Finally, we note that the order of the elements of \tilde{a}^t determines the update direction from p^t to p^{t+1} in Lemma 1. Therefore, we propose a similarity score that is an average of cosine similarity and the

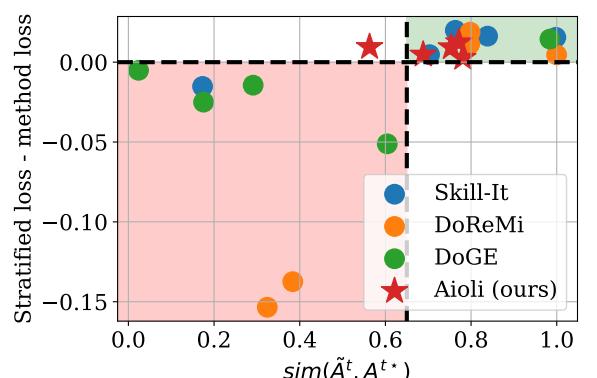


Figure 3: Improvement over stratified sampling versus optimality of A^t . Each dot represents a method applied to a dataset. The red region shows that existing methods are worse than stratified on at least 1 dataset. The vertical dashed line serves as a visual aid.

Spearman rank correlation, $\text{sim}(\tilde{A}^t, A^{t*}) = 0.5\text{cossim}(\tilde{a}^t, a^{t*}) + 0.5\text{Spearman}(\tilde{a}^t, a^{t*})$. This metric is bounded between -1 and 1 , where 1 indicates $\tilde{a}^t = a^{t*}$ and -1 indicates $\tilde{a}^t = -a^{t*}$.

Results. In Figure 3, we plot each method’s $\text{sim}(\tilde{A}^t, A^{t*})$ versus each method’s improvement over the stratified sampling baseline, which sets $p_i = 1/m$ for all $i \in [m]$, for each dataset in the $m = 2, 3$ data settings. We find that no existing online method works well across all datasets (also see Table 2), and that our metric and loss improvement have a moderate positive correlation ($R^2 = 0.491$). This suggests that A^t ’s accuracy is critical to the performance of online methods, and that existing methods’ A^t are not consistently accurate across the datasets. In Appendix C.2.1, we give more details on the structure of A^{t*} , providing intuition for why existing methods’ parameters cannot express it.

4.4 Solving strategy

We study the assumptions made in how existing methods solve the LMO optimization problem. We find that the greedy approximation used by EGD, $\text{minimize}_{p^t} \sum_{i=1}^m L_{\text{val},i}^{t+1}(p)$, does not significantly compromise performance compared to full optimization of dynamic proportions, which has an exponentially large solution space. In particular, we study if greedily selecting p^t from \mathcal{P} at each t yields the optimal dynamic proportions in \mathcal{P}^T , and we find that this holds in 2 out of 3 data settings (Table 10). This suggests that the greedy approximation can simplify optimization without substantial performance loss. We also comment on other possible solving strategies in Appendix C.3.

5 AIOLI: a Method for Improved Data Mixing

To validate our insights from Section 4, we develop AIOLI, an online method derived from the LMO framework. We have three takeaways from section 4:

- a) A linear dynamic mixing law, $L_{\text{val},i}^{t+1}(p) = L_{\text{val},i}^t(p) - \sum_{j=1}^m A_{ij}^t p_j^t$ for all $i \in [m]$, can capture the loss-proportion relationship with high fidelity (Section 4.2).
- b) Existing online methods often set the parameters A^t to be very different from true A^{t*} (Section 4.3).
- c) Exponentiated gradient descent can recover near-optimal performance while simplifying the optimization problem, avoiding an exponential solution space (Section 4.4).

We thus directly specify the linear dynamic mixing law parameterization and EGD as two out of three LMO components of AIOLI since we found that their assumptions generally hold in practice. According to Lemma 1, the update rule given these two components is $p_j^{t+1} \propto p_j^t \exp(\eta \sum_{i=1}^m A_{ij}^t)$ (b^t is absorbed into A^t). Thus, our primary mandate in creating AIOLI is to construct and utilize an A^t that is an accurate estimate of the true A^{t*} in the linear dynamic mixing law, which existing online methods fail to achieve.

Estimating A^{t*} . To build intuition, we first consider a high-cost naive approach. For each round, we could conduct a training sweep of m different proportions $p^{t,1}, \dots, p^{t,m}$, and observe each resulting change in loss. We could then solve a system of m equations for each i : $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,s}) = \sum_{j=1}^m A_{ij}^t p_j^{t,s}$ for $s \in [m]$, obtaining vectors A_1^t, \dots, A_m^t . However, this approach effectively requires m extra training runs.

AIOLI similarly solves a system of equations, but it computes loss changes per sweep mixture without requiring extra training. First, it allocates δ fraction of the training round for learning A^t . Second, it partitions this δ into $K = mk$ intervals and trains according to an interleaved order on $p^{t,1}, \dots, p^{t,m}$. After training on each $p^{t,j}$, we record the resulting change in validation losses, and we average over all of $p^{t,j}$ ’s intervals. Intuitively, the interleaving ensures that the model is trained on each $p^{t,j}$ for several intervals throughout δ , which can approximate if we were to train on $p^{t,j}$ for the entire δ (which approximates the entire round). This procedure is outlined in LEARNPARAMS (Alg. 2), with more details in Appendix D and Figure 7.

AIOLI. First, we set p^0 to be uniform. In each round, we estimate A^t using LEARNPARAMS and then normalize the entries of A^t , producing \bar{A}^t . Otherwise, A^t decreases along with loss over time, resulting in the first few p^t updates being much larger in magnitude than others. Then, we update the proportions using $p_j^t \propto p_j^{t-1} \exp(\eta \sum_{i=1}^m \bar{A}_{ij}^t)$, as in Lemma 1, and train for the remainder of that round using p_j^t .

Finally, we design AIOLI so that it can also be used to improve other data mixing methods, which we study in Section 6.2. Mixture proportions can be updated using AIOLI either from the start of training or from the middle of a run. In the latter case, we denote an initial static mixture $p_{\text{init}}^t \in \Delta^m$ and initial number of steps S_{init} . If S_{init} is nonzero, AIOLI trains according to p_{init} for the first S_{init} steps before updating the mixture proportions. AIOLI is presented in Algorithm 1.

Algorithm 1 AIOLI

- 1: **Input:** data $D_{\text{train}}, D_{\text{val}}$, model f^1 . Initial steps S_{init} , initial proportions $p^{\text{init}} \in \Delta^m$. T rounds over $S - S_{\text{init}}$ remaining steps, δ fraction per round for learning parameters, learning rate η , one-hot smoothing factor ε .
- 2: If $S_{\text{init}} \neq 0$, train f^1 on p^{init} for S_{init} steps.
- 3: Set $p^0 = \text{Unif}(m)$.
- 4: **for** $t = 1, \dots, T$ **do**
- 5: Set $A^t, f^{t+\delta} \leftarrow \text{LEARNPARAMS} (D_{\text{train}}, D_{\text{val}}, \delta, f^t, \varepsilon)$ (Alg. 2), and normalize A^t to get \bar{A}^t .
- 6: $p_j^t \propto p_j^{t-1} \exp(\eta \sum_{i=1}^m \bar{A}_{ij}^t)$ for all $j \in [m]$.
- 7: Train model $f^{t+\delta}$ with $\frac{S}{T}(1 - \delta)$ steps from mixture p^t over D_{train} . Obtain updated f^{t+1} .

Algorithm 2 LEARNPARAMS

- 1: **Input:** $D_{\text{train}}, D_{\text{val}}, \delta$, model f^t , number of sweeps k , one-hot smoothing factor ε .
- 2: Split the fraction of a training round δ into K intervals, where $K = mk$.
- 3: Set $\beta = 0_{m,m}$
- 4: Define $p^{t,i} = (1 - \varepsilon)\mathbf{1}_i + \varepsilon \text{Unif}(m)$ for $i \in [m]$, and define $P = [p^{t,1}, \dots, p^{t,m}] \in \Delta^{m \times m}$
- 5: Randomly shuffle k instances of each $i \in [m]$ to create an order $\mathcal{I} \in [m]^K$.
- 6: **for** $\tau = 1, \dots, K$ **do**
- 7: Let $j = \mathcal{I}_\tau$. Train model on mixture $p^{t,j}$ of D_{train} for one interval, obtain $f^{t+\tau\delta/K}$.
- 8: **for** $i \in [m]$ **do**
- 9: Update $\beta_{ij} \leftarrow \beta_{ij} + L_{\text{val},i}(f^{t+(\tau-1)\delta/K}) - L_{\text{val},i}(f^{t+\tau\delta/K})$ with loss difference on D_{val}^i .
- 10: Update $\beta \leftarrow \frac{\beta}{k}$.
- 11: Set $A_i^t = P^{-1}\beta_i$ for each $i \in [m]$.
- 12: **Return** $A^t \in \mathbb{R}^{m \times m}, f^{t+\delta}$

6 Experimental Results

We evaluate all methods in the LMO framework, including AIOLI, in two settings. First, we consider an **unrestricted** additional training budget setting to assess how AIOLI compares to other methods in their original form, since each method uses a different number of extra training runs to learn proportions (Section 6.1). Second, we consider a **restricted** training budget setting to assess if AIOLI can enhance existing methods in practical, budget-constrained conditions, where existing methods have less than a full training run to learn mixing proportions (Section 6.2). Hyperparameters and experimental details, including proportion trajectories are available in Appendix E. Downstream evaluation, ablations, experiments on larger models, and results adapting AIOLI to an out-of-domain setting are in Appendix F.

Data settings and models. We use the same data settings and models as in Section 4.1, where we train for $S = 5\text{K}$ steps for $m = 2, 3$ -group settings and $S = 40\text{K}$ steps for the full SlimPajama.

Baselines and evaluation. We consider three online methods (Skill-It, DoGE, DoReMi) and one offline method (DML). We also consider grid search (GS), which sweeps training runs and selects p with the lowest average validation loss, and stratified sampling, which sets $p_i = \frac{1}{m}$ for all $i \in [m]$. For each method, we report the average test perplexity per group of the trained model. This metric is considered a proxy for downstream performance [22] and also represents the objective in the data mixing problem.

6.1 Unrestricted Setting

Setup. We allow methods up to $10S$ additional training steps to learn the mixture proportions. Approaches like grid search and DML can use the entire budget (searching and fitting over 10 full runs), while Skill-It, DoReMi, and DoGE use mS , $2S$, and S extra training steps, respectively (see Section 3.3). Stratified sampling and AIOLI use no extra training steps. We evaluate AIOLI with $S_{\text{init}} = 0$.

Results. In Table 2, we find that AIOLI robustly outperforms stratified sampling in all 6 data settings by an average of 0.274 perplexity points, while all other methods do worse than stratified sampling on at least 1 set of data groups by up to 6.9 points. The performance of AIOLI and other online methods is additionally reflected in Figure 3, in which we find that AIOLI's A^t similarity with A^{t*} is correlated with performance. While AIOLI's parameter similarity is not always the highest, we note that its lowest similarity score is much higher than that of other methods, providing evidence that AIOLI's parameter estimation procedure is more consistently accurate than that of other methods. Lastly, regarding offline methods,

Table 2: Difference in average test perplexity compared to stratified sampling in the unrestricted setting, where all methods can use ≤ 10 extra runs to learn p . Negative values (green) = improvement. A=Arxiv, B=Books, GH=GitHub, SE=StackExchange, W=Wikipedia.

Method	A/SE	GH/C4	B/SE	A/B/SE	CC/GH/W	SlimPajama	# < stratified	# extra runs
Stratified	16.532	35.991	47.192	35.114	41.583	26.426	-	0
GS	-0.399	-0.407	-0.645	-0.247	0.298	0.490	4	10
DML	-0.241	-0.110	-0.644	-0.599	0.242	1.641	4	10
Skill-It	-0.326	0.551	-0.728	-0.568	-0.195	-0.184	5	<i>m</i>
DoReMi	-0.307	5.303	-0.217	-0.393	6.898	0.703	3	2
DoGE	0.419	0.184	-0.678	1.843	0.604	0.949	1	1
AIOLI	-0.205	-0.340	-0.439	-0.226	-0.196	-0.240	6	0

Table 3: Average test perplexity in the restricted setting, where each method learns p on shortened runs, and AIOLI +method dynamically adjusts p throughout training. green=AIOLI +method outperforms method.

Method	Arxiv/SE	GH/C4	Books/SE	Arxiv/Books/SE	CC/GH/Wiki	SlimPajama
GS	16.573	36.345	47.063	35.174	42.767	27.741
AIOLI + GS	16.388	35.925	46.667	34.705	41.378	25.654
DML	16.659	36.658	46.846	34.585	42.731	37.696
AIOLI + DML	16.277	35.856	46.710	34.529	41.595	25.654
Skill-it	16.246	37.255	46.667	34.539	42.069	26.734
AIOLI + Skill-it	16.261	36.153	46.586	34.565	41.732	26.073
DoReMi	16.522	37.812	46.489	34.934	42.738	28.762
AIOLI + DoReMi	16.347	35.626	46.163	34.770	41.800	26.587
DoGE	16.853	35.795	46.743	35.775	41.790	32.301
AIOLI + DoGE	16.473	35.632	46.145	34.771	41.378	26.073

we hypothesize that their poor performance on settings with larger m is due to the training budget being limited to $10S$, and that increasing this budget would eventually allow them to perform well.

6.2 Restricted Setting

Motivation. We introduce the restricted setting because practitioners may not have the resources or desire to complete multiple full training runs, especially as recent LLMs are trained for longer and on more data [45]. As a result, practitioners may only use data mixing methods on shortened runs, producing learned proportions that may be suboptimal on the full run. We study if AIOLI is able to improve performance by dynamically adjusting previously learned proportions throughout the full training run.

Setup. We allow all existing methods up to $0.5S$ additional training steps to learn the mixture proportions. This requires methods to learn p^{method} over shorter runs of S_{method} steps each. For instance, grid search will conduct 10 runs of length $S/20$ (see Table 11). We evaluate each method by using p^{method} learned from shorter runs to train the model on the full run of S steps. We use AIOLI to dynamically adjust each p^{method} throughout the full run. That is, for each existing method, we run AIOLI with $p^{\text{init}} = p^{\text{method}}$ and $S_{\text{init}} = S_{\text{method}}$, referring to this as AIOLI +method.

Results. In Table 3, we find that adding AIOLI to any existing method that learns proportions over shorter runs improves average test perplexity per group in 28 out of 30 settings, by an average of 1.202 and a maximum of 12.012 points. Furthermore, AIOLI can help methods that initially underperform stratified sampling surpass it, such as DoGE across all settings. In some settings, such as Books/StackExchange, AIOLI improves methods that already outperform stratified sampling. This shows that AIOLI can enhance a wide variety of static proportions, regardless of their initial performance. For the two settings where AIOLI underperforms the base method, the base method already outperforms stratified, and adding AIOLI maintains this trend, worsening perplexity by at most 0.025 points.

7 Related Work

Data mixing. Beyond the data mixing methods explored in our framework, Albalak et al. [2] frames online data mixing as a multi-armed bandit problem with loss as the reward function. In concurrent work, Jiang et al. [28] also set data mixtures online and adaptively by using a credit assignment score that predicts how data from each domain affects loss on that domain. In our language, Jiang et al. [28] use a diagonal A^t matrix, and the values on the diagonal are defined by their credit

assignment function and the per-group losses. Recent works have also studied how to mix data on smaller models and use these learned proportions on larger models [24, 30, 37]. In a similar vein, Na et al. [46] show that one can simulate a model trained on a particular data mixture by averaging together models trained on different (possibly disjoint) partitions of data groups. Thrush et al. [60] mixes data to optimize performance on downstream tasks, constructing an A^t -like interaction matrix by using pretrained model perplexities.

Curriculum Learning. Bengio et al. [6] initially introduced curriculum learning as training models over samples from easiest to hardest. While early work focused on manually designed curricula, later work emphasizes model-driven ones [21, 26, 41, 65]. Curricula can encourage skills-based generalization [27], or emphasize high quality data to improve downstream task performance [10]. Online mixing methods can be also viewed as curriculum learning over data groups.

Data Selection. A common way to curate datasets besides mixing is to select data at the per-sample level [3]. Techniques here can be broadly classified as data filtering, data matching, and data condensation. In data filtering, low-quality samples are removed using simple heuristics, such as GitHub file lengths [62, 64], or via deduplication [1, 32, 61]. In data matching, samples that are most similar to a reference dataset are selected. Similarity can be defined in terms of embeddings [71], gradients [20, 69], or directly using machine learning models to score samples [11, 25, 44]. Lastly, data condensation aims to identify a subset of samples that captures the full training dataset’s properties. Selection mechanisms include using gradients, model predictions, and embedding distances [50, 56, 63].

Hyperparameter Optimization and Truncation Bias. Many data mixing methods utilize extra training runs to learn the static mixture proportions before the final training run. This allows us to view data mixing as a hyperparameter optimization problem in p . [72] and [37] mitigate the inefficiency of grid search in higher dimensions by combining it with data mixing laws to impose additional structure. However, both grid search and these offline methods can have poor performance when p is searched for or fitted on shorter runs, as in the restricted setting. To understand these results, we note that many popular hyperparameter optimization methods carefully control truncation, and some runs are allowed to continue longer than others [19, 35, 57]. Thus, generic hyperparameter optimization methods may also prove effective for tuning data mixes.

8 Discussion

We introduce the LMO framework, which unifies existing data mixing methods by viewing them as solutions to a common optimization problem involving an implicit method-dependent mixing law. Using this framework, we find that existing methods perform poorly on some datasets due to inaccurate mixing law parameters. This insight inspires AIOLI, whose performance gains are rooted in its ability to estimate parameters A^t of the linear dynamic mixing law throughout training.

Limitations and Future Work AIOLI incurs extra inference cost via the repeated evaluations in LEARNPARAMS (Alg. 2). This can be reduced by computing L_{val} over a subset of D_{val} , and by using each A^t for longer (decreasing T). Another direction is understanding the role of data group partitions. For example, C4 is a subset of CommonCrawl, and it is unclear if disjoint groups could improve performance.

The LMO framework itself is an invitation for future work. It shows that data mixing methods can be improved and analyzed by studying their assumptions on how models learn from data. By exposing such assumptions, LMO identifies key axes for improvement (mixing law parameterization, parameter estimation, and how to solve for p), which we hope will inspire new principled data mixing methods.

8.1 Reproducibility Statement

See Appendix B.2 for the full proofs on how to express Skill-it, DoReMi, and DoGE using the LMO framework. See Appendix C for details on how to reproduce our analyses of mixing law parameterization validity, A^t parameter fit, and assessing whether greedy optimization is sufficient for data mixing. Finally, to reproduce the experimental results, please see Appendix E.

Code release. Code for reproducing our results is available at <https://github.com/HazyResearch/aioli>.

8.2 Ethics Statement

Our work focuses on improving the efficiency and performance of language model training. While our research does not directly address ethical concerns, it can contribute to more responsible AI development by optimizing training, which can reduce computational costs and energy consumption.

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Appendix

In Appendix A, we provide a glossary of notation used in the paper. In Appendix B, we discuss how additional data mixing methods are related to the LMO framework and provide proofs that existing methods can be expressed in our framework. In Appendix C, we provide additional results on our analysis of existing data mixing methods. In Appendix E we provide additional details for our results in Section 6, and in Appendix F we provide additional results, including downstream evaluation and ablations.

A Notation

The glossary is given in Table 4 below.

Symbol	Used for
m	The number of data groups. Examples of data groups include a pre-training domain or an instruction-tuning task.
$D_{\text{train/val/test}}$	Training, validation, and test datasets comprised of m groups, where $D_{(\cdot)}^i$ is group i 's training/validation/test data.
N	Total number of samples from D_{train} to train on.
S	Number of steps to train for (i.e., $S = N \times \text{batch size}$).
T	Number of rounds to divide training into, where each round is $\frac{S}{T}$ steps.
\mathbf{p}	Mixture proportions are $\mathbf{p} = (p^1)$ for $T = 1$ (static) and $\mathbf{p} = (p^1, \dots, p^T)$ for $T > 1$ (dynamic), where $p^t = [p_1^t, \dots, p_m^t] \in \Delta^m$ is a probability distribution.
f	A language model (can be either pre-trained or initialized from scratch).
$f(\mathbf{p}, t)$	The model f at the beginning of round t after being trained on p^1, \dots, p^{t-1} so far.
$L_{\text{train/val/test}}(f)$	$L_{\text{train}}(f) = (L_{\text{train},1}(f), \dots, L_{\text{train},m}(f))$ is the vector of f 's training losses over each data group; similarly defined for validation and test losses.
$L_{(\cdot)}^t(\mathbf{p})$	Shorthand for $L_{(\cdot)}(f(\mathbf{p}, t))$. When dealing with static mixtures, we also use $L_{(\cdot)}(\mathbf{p})$.
A^t	Parameter matrix $A^t \in \mathbb{R}^{m \times m}$ used in mixing laws (2), capturing cross-group interactions.
b^t, c^t	See Table 1 for instantiations.
b^t, c^t	Group-specific parameters $b^t, c^t \in \mathbb{R}^m$ used in mixing laws 2. Note that the value of c^t does not impact the LMO framework, and neither does b^t when all b_i^t are equal.
σ	Either $\sigma : \mathbb{R} \rightarrow \mathbb{R} = \text{Id}$ or \exp .
Z^t	Used for normalization in proportion update rule.
η	Step size $\eta > 0$ used in proportion update rule.
\mathcal{P}	The set of mixture proportions that comprises a training sweep.
A^{t*}	Approximately optimal A^t for the linear dynamic mixing law, obtained by fitting $L_{\text{val}}^{t+1}(\mathbf{p}) = L_{\text{val}}^t(\mathbf{p}) - A^{t*}\mathbf{p}$ over training sweeps.
\tilde{A}^t	Method-specific $\tilde{A}^t = b^t A^t$, where A^t is obtained directly from the method and $b^t \in \mathbb{R}$ is learned from training sweeps.
$\text{sim}(\tilde{A}^t, A^{t*})$	Similarity between method-specific and optimal A^t , defined as an average of cosine similarity and Spearman rank correlation over A^t 's normalized column sums.
ε	one-hot smoothing factor used to define $p^{t,i} = (1 - \varepsilon)\mathbf{1}_i + \varepsilon \text{Unif}(m)$, smoothed one-hot distributions we use to learn A^t in AIOLI.
δ	The fraction per round dedicated to learning A^t in AIOLI.
k	Number of sweeps per group to average A^t estimates over in AIOLI.
\mathbf{p}^{init}	Initial mixture $\mathbf{p}^{\text{init}} \in \Delta^m$ that AIOLI can dynamically adjust.
S_{init}	Number of steps to train according to \mathbf{p}^{init} .

Table 4: Glossary of variables and symbols used in this paper.

B LMO framework details

B.1 Additional existing methods

We comment on two other popular data mixing methods, Online Data Mixing (ODM) [2] and RegMix [37].

In ODM [2], data mixing is framed as a multi-armed bandit problem, where each arm is a data group that a batch is trained on, and the reward function is defined in terms of the training loss of each group. ODM uses the EXP3 algorithm to explore training on different data groups. p^t , which is used to determine which group the entire training batch is comprised of, is updated according to $p_j^{t+1} = (1 - m\varepsilon_t) \frac{\exp(\varepsilon_{t-1} R_j^t)}{\sum_{i=1}^m \exp(\varepsilon_{t-1} R_i^t)} + \varepsilon_t$. ε_t is an exploration rate, and the reward function is

$R_j^t = \alpha R_j^{t-1} + (1 - \alpha) \frac{L_{\text{train},j}^t(\mathbf{p})}{p_j^t}$ if the j th group is selected at time t ; otherwise, $R_j^t = R_j^{t-1}$. While the exploration and the smoothing of p^t and R^t make this method not directly expressible in our framework, we note that the update rule can be loosely interpreted as allocating larger proportions to groups that have high loss. This update rule does not consider cross-group interactions and is thus similar to DoReMi's update rule, which utilizes a diagonal A^t defined in terms of current loss.

RegMix [37] conducts many training runs on smaller models at shorter scales. Similar to DML [72], a regression model is fit to these runs and used to predict mixture proportions for a longer run on a larger model. They consider using a linear regression model, i.e., the mixing law $L_{\text{val},i}(\mathbf{p}) = c_i - \sum_{j=1}^m A_{ij}p_j^t$, but find that the R^2 is relatively low (0.87). Instead, their main approach uses LightGBM, a tree-based gradient boosting approach, i.e., using an ensemble of non-linear decision trees as a mixing law. We note that AIOLI could be used in conjunction with RegMix in their settings, an exciting direction for future work.

B.2 Proofs for section 3.3

B.2.1 Background on Exponentiated Gradient Descent

We provide background on exponentiated gradient descent (EGD) taken from Kakade [29]. In EGD, we have a sequence of decisions w^1, \dots, w^T , where $w^t = [w_1^t, \dots, w_m^t] \in \Delta^m$. We also have a sequence of cost functions $c^1, \dots, c^T : \Delta^m \rightarrow \mathbb{R}$. To minimize the total cost $\sum_{t=1}^T c^t(w^t)$, the EGD update rule sets $w^0 = \text{Unif}(m)$, and updates according to $w_j^{t+1} = \frac{w_j^t \exp(-\eta \nabla_j c^t(w^t))}{Z_t}$. Z_t ensures that $w^{t+1} \in \Delta^m$, η is a step size, and $\nabla_j c^t(w^t)$ denotes $\frac{\partial c^t(w^t)}{\partial w_j^t}$. EGD is known to have certain regret guarantees on the value of costs incurred by playing w^1, \dots, w^T versus always playing the best fixed point in hindsight: $\sum_{t=1}^T c^t(w^t) - \inf_{w \in \Delta^m} \sum_{t=1}^T c^t(w)$.

We now are ready to prove Lemma 1.

Lemma 1. *The EGD update rule for (1) subject to $L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t - b_i^t \sum_{j=1}^m A_{ij}^t p_j^t \forall i \in [m]$ is*

$$p_j^{t+1} = \frac{1}{Z^t} \cdot p_j^t \exp\left(\eta \sum_{i=1}^m b_i^t A_{ij}^t\right) \forall j \in [m], \quad (3)$$

where $\eta > 0$ is the step size and Z^t is a normalizing constant such that $p_j^{t+1} \in \Delta^m$.

Proof. The cost function at each timestep in our setting is $\sum_{i=1}^m L_{\text{val},i}^{t+1}(\mathbf{p})$, and the decision we make is p^t . The mixing law constraint in (2) with $\sigma = \text{Id}$ is $L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t - b_i^t \sum_{j=1}^m A_{ij}^t p_j^t$ for all $i \in [m]$, so our objective (1) can be written as

$$\sum_{i=1}^m \left(c_i^t - b_i^t \sum_{j=1}^m A_{ij}^t p_j^t \right). \quad (4)$$

The gradient of this expression with respect to p_j^t for $j \in [m]$ is $-\sum_{i=1}^m b_i^t A_{ij}^t$. Plugging this into the EGD update rule, we obtain the update $p_j^{t+1} = \frac{1}{Z^t} p_j^t \exp(\eta \sum_{i=1}^m b_i^t A_{ij}^t)$. \square

B.2.2 Proof of Theorem 1

To prove Theorem 1, we write out individual propositions 1, 2, 3 for expressing each online method in the LMO framework.

By our definition of what it means to express a method in LMO, we must consider how each method 1) trains f and 2) sets p^t . We must see if this procedure can be replicated by solving some specification of the LMO optimization problem in our data mixing setup.

Critically, note that this definition of “expression” does not claim that the optimization problems proposed in existing methods are exactly the same as the LMO optimization problem. Instead, we are stating that the training procedures used in their methods can be equivalently viewed as a way of solving the LMO optimization problem subject to certain assumptions on the loss-proportion relationship.

Proposition 1 (Skill-It Derivation). *Using a) a linear dynamic parameterization $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$, b) parameters $A_{ij}^t = L_{\text{val},i}^t(\mathbf{p}) \cdot (L_{\text{val},i}^{T+1}(\mathbf{1}_j) - L_{\text{val},i}^1(\mathbf{1}_j)) / L_{\text{val},i}^1(\mathbf{1}_j)$, and c) exponentiated gradient descent (EGD) to solve for \mathbf{p} , the LMO framework (1) can express Skill-It.*

Proof. The Skill-It algorithm sets p^t in each round and then samples from D_{train} according to p^t to train f for a round. This training procedure is directly specified in our data mixing problem setup (Section 2). Therefore, we simply need to show that the Skill-It update rule can be converted into a linear dynamic mixing law. By comparing Lemma 1 and the Skill-It update rule $p_j^{t+1} = \frac{1}{Z_t} \cdot p_j^t \exp(\eta \sum_{i=1}^m A_{ij}^{\text{SG}} L_{\text{val},i}^t(\mathbf{p}))$, we can match A_{ij}^t in the lemma with A_{ij}^{SG} in Skill-It, and we can match b_i^t in the lemma with $L_{\text{val},i}^t(\mathbf{p})$. Therefore, Lemma 1 tells us that using $L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t - b^t \sum_{j=1}^m L_{\text{val},i}^t(\mathbf{p}) A_{ij}^{\text{SG}} p_j^t$ in the LMO framework with exponentiated gradient descent recovers Skill-It (since the b^t and c_i^t can be dropped and are only used for scaling A^t).

Using the definition of A_{ij}^{SG} , we can rewrite the mixing law as $L_{\text{val},i}^{t+1}(\mathbf{p}) = c_i^t - b^t \sum_{j=1}^m A_{ij}^{t, \text{Skill-It}} p_j^t$ where $A_{ij}^{t, \text{Skill-It}} = L_{\text{val},i}^t(\mathbf{p})(L_{\text{val},i}^{T+1}(\mathbf{1}_j) - L_{\text{val},i}^1(\mathbf{1}_j))/L_{\text{val},i}^1(\mathbf{1}_j)$. Lastly, note that we can replace c_i^t with any other value, including $L_{\text{val},i}^t(\mathbf{p})$, due to the fact that p^t has $m - 1$ degrees of freedom (see Lemma 2).

We note that [14] explicitly specify their mixing law in equation 2 of their paper, along with the same objective function as ours in the LMO framework. \square

Proposition 2 (DoReMi Derivation). *Using a) a linear dynamic parameterization $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$, b) parameters $A_{ij}^t = \min\{L_{\text{train},i}^t(\mathbf{p}) - L_{\text{train},i}^t(f_{\text{ref}}), 0\}$ for $i = j$ and $A_{ij} = 0$ otherwise, and c) EGD to solve for \mathbf{p} , the LMO framework (1) can express DoReMi's proxy model.*

Proof. When training the proxy model for DoReMi, p^t is set in each round, and then f is updated to minimize $\sum_{i=1}^m p_i^t L_{\text{train},i}(f)$. Using Lemma 3, we establish that DoReMi's weighted training objective at each timestep is equal in expectation to the objective of training on data sampled from p^t , which is what our problem setup focuses on. Having established that the training procedure is the same in expectation, we now need to show that the DoReMi p^t update rule can be converted into a linear dynamic mixing law. By comparing Lemma 1 and the DoReMi update rule $p_j^{t+1} \propto p_j^t \exp(\eta \max\{L_{\text{train},j}^t(\mathbf{p}) - L_{\text{train},j}^t(f_{\text{ref}}), 0\})$, we can match A_{ij}^t in the lemma with 0 for $i \neq j$, and A_{ii}^t with $\max\{L_{\text{train},j}^t(\mathbf{p}) - L_{\text{train},j}^t(f_{\text{ref}}), 0\}$. Therefore, Lemma 1 tells us that using $L_{\text{val},i}^{t+1} = c_i^t - b^t \sum_{j=1}^m A_{ij}^t p_j^t$ with $A_{ii}^t = \max\{L_{\text{train},j}^t(\mathbf{p}) - L_{\text{train},j}^t(f_{\text{ref}}), 0\}$ can express the DoReMi proxy model training. We include b^t to allow for scaling A^t , but since this does not impact the optimal \mathbf{p} , it is not in the update rule. Lastly, applying Lemma 2 lets us write the mixing law as $L_{\text{val},i}^{t+1} = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$.

We comment on the fact that DoReMi's proxy model is trained with a DRO (distributionally robust optimization) min-max objective, namely, $\text{minimize}_f \text{maximize}_{\mathbf{p}} \sum_{i=1}^m p_i L_{\text{train},i}^{T+1}(f)$. This objective, which differs from our data mixing objective, yields the p^t gradient ascent and f^t gradient descent updates. However, we are still able to express this training procedure in the LMO framework, since our claim is: if we assume that the $L_{\text{val},i}^{t+1} = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^{t, \text{DRM}} p_j^t$ mixing law captures the relationship between L_{val} and p^t , then training according to the DoReMi proxy run should not only guide f and \mathbf{p} to optimize the DRO objective, but also to optimize the average validation loss per group. \square

Proposition 3 (DoGE Derivation). *Using a) a linear dynamic parameterization $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$, b) parameters $A_{ij}^t = \langle \nabla L_{\text{val},i}^t(\mathbf{p}), \nabla L_{\text{train},j}^t(\mathbf{p}) \rangle$ for all $i, j \in [m]$, and c) EGD to solve for \mathbf{p} , the LMO framework (1) can express DoGE's proxy model.*

Proof. When training the proxy model for DoGE, p^t is set in each round, and then f is updated to minimize $\sum_{i=1}^m p_i^t L_{\text{train},i}(f)$. Using Lemma 3, we establish that DoGE's weighted training objective at each timestep is equal in expectation to the objective of training on data sampled from p^t . Next, we show that the DoGE update rule can be converted into a linear dynamic mixing law. By comparing Lemma 1 and the DoGE update rule $p_j^{t+1} \propto p_j^t \exp(\eta \langle \nabla L_{\text{train},j}(f^t), \sum_{i=1}^m \nabla L_{\text{val},i}(f^t) \rangle)$, we can see that A_{ij}^t in the Lemma can be matched with $\langle \nabla L_{\text{train},j}(f^t), \nabla L_{\text{val},i}(f^t) \rangle$. Therefore, using the mixing law $L_{\text{val},i}^{t+1} = c_i^t - b^t \sum_{j=1}^m A_{ij}^t p_j^t$ with $A_{ij}^t = \langle \nabla L_{\text{train},j}(f^t), \nabla L_{\text{val},i}(f^t) \rangle$ allows LMO to express DoGE proxy model training. Again, b^t is included for scaling but does not impact optimization, and by applying Lemma 2, we can replace c_i^t with $L_{\text{val},i}^t(\mathbf{p})$. \square

Lemma 2. *Let $L_i^{t+1}(\mathbf{p}) = c_i^t - \sum_{j=1}^m A_{ij}^t p_j^t$ for some c^t and A^t . Then, there exists an B_{ij}^t such that $L_i^{t+1}(\mathbf{p}) = L_i^t(\mathbf{p}) - \sum_{j=1}^m B_{ij}^t p_j^t$.*

Proof. Since $p^t \in \Delta^m$, we can write the probability p_m^t as $1 - \sum_{j=1}^{m-1} p_j^t$. Then, the first equation can be written as

$$\begin{aligned}
L_i^{t+1}(\mathbf{p}) &= c_i^t - \sum_{j=1}^{m-1} A_{ij}^t p_j^t - A_{im}^t \left(1 - \sum_{j=1}^{m-1} p_j^t\right) \\
&= c_i^t - \sum_{j=1}^{m-1} (A_{ij}^t - A_{im}^t) p_j^t - A_{im}^t \\
&= L_i^t(\mathbf{p}) - \sum_{j=1}^{m-1} (A_{ij}^t - A_{im}^t) p_j^t - (A_{im}^t - c_i^t + L_i^t(\mathbf{p})) \\
&= L_i^t(\mathbf{p}) - \sum_{j=1}^{m-1} (A_{ij}^t - A_{im}^t + A_{im}^t - c_i^t + L_i^t(\mathbf{p})) p_j^t - (A_{im}^t - c_i^t + L_i^t(\mathbf{p})) (1 - \sum_{j=1}^{m-1} p_j^t) \\
&= L_i^t(\mathbf{p}) - \sum_{j=1}^{m-1} (A_{ij}^t - c_i^t + L_i^t(\mathbf{p})) p_j^t - (A_{im}^t - c_i^t + L_i^t(\mathbf{p})) (1 - \sum_{j=1}^{m-1} p_j^t).
\end{aligned} \tag{5}$$

Let $B_{ij}^t = A_{ij}^t - c_i^t + L_i^t(\mathbf{p})$ for all $j \in [m]$. Then, this equation becomes

$$\begin{aligned}
L_i^{t+1}(\mathbf{p}) &= L_i^t(\mathbf{p}) - \sum_{j=1}^{m-1} B_{ij}^t p_j^t - B_{im}^t (1 - \sum_{j=1}^{m-1} p_j^t) \\
&= L_i^t(\mathbf{p}) - \sum_{j=1}^m B_{ij}^t p_j^t.
\end{aligned} \tag{6}$$

□

Lemma 3. Let $L_B^t(f, p)$ be the total training loss of f on a batch of size B sampled from D_{train} according to $p \in \Delta^m$, and let $L_{B,i}^t(f, p)$ be the total training loss on samples from group i in that batch. Then, the average loss over a uniformly sampled batch weighted by p^t is equal in expectation to the average loss per group over a batch sampled according to p^t :

$$\mathbb{E} \left[\sum_{i=1}^m p_i^t L_{B,i}^t(f, \text{Unif}(m)) \right] = \mathbb{E} \left[\frac{L_B^t(f, p^t)}{m} \right] \tag{7}$$

Proof. Let each group i consist of samples x from the distribution \mathcal{P}_i , and let $\tilde{L}_{\text{train},i}(f) = \mathbb{E}_{x \sim \mathcal{P}_i} [\ell(f, x)]$ be the population-level loss on group i , where $\ell(f, x)$ is f 's loss on sample x .

If a batch is uniformly sampled, each group has B/m samples. We can then write $L_{B,i}^t(f, \text{Unif}(m)) = \sum_{k=1}^{B/m} \ell(f, x_k^i)$, where x_k^i is the k th sample of group i . Then,

$$\mathbb{E} \left[\sum_{i=1}^m p_i^t L_{B,i}^t(f, \text{Unif}(m)) \right] = \mathbb{E} \left[\sum_{i=1}^m p_i^t \sum_{k=1}^{B/m} \ell(f, x_k^i) \right] = \sum_{i=1}^m \frac{p_i^t B}{m} \tilde{L}_{\text{train},i}(f). \tag{8}$$

Next, if a batch is sampled according to p^t , then group i has Bp_i^t samples in the batch. We can then write $L_B^t(f, p^t) = \sum_{i=1}^m \sum_{k=1}^{p_i^t B} \ell(f, x_k^i)$. Then,

$$\mathbb{E} \left[\frac{L_B^t(f, p^t)}{m} \right] = \mathbb{E} \left[\sum_{i=1}^m \sum_{k=1}^{p_i^t B} \frac{\ell(f, x_k^i)}{m} \right] = \sum_{i=1}^m \frac{p_i^t B}{m} \tilde{L}_{\text{train},i}(f). \tag{9}$$

This hence establishes the equivalence in expectation between a weighted training objective and training on data sampled according to p .

□

Table 5: Comparison of log-linear static and linear dynamic mixing law parameterizations across different data settings with MSE and R^2 metrics. Both log-linear and linear dynamic mixing laws fit the relationship between mixing proportions and losses well.

Parameterization	Arxiv/SE		GH/C4		Books/SE	
	MSE	R^2	MSE	R^2	MSE	R^2
Log-linear static	2e-4	0.990	5e-4	0.989	6e-4	0.987
Linear dynamic	2e-4	0.936	1e-4	0.948	4e-5	0.926
Arxiv/Books/SE		CC/GH/Wiki		SlimPajama		
MSE	R^2	MSE	R^2	MSE	R^2	
Log-linear static	6e-4	0.991	0.001	0.989	0.002	0.997
Linear dynamic	6e-5	0.957	1e-4	0.975	5e-6	0.938

C Analysis Details

C.1 Mixing Law Parameterization

We describe how we performed the linear and log-linear parameterization experiments. For the log-linear static parameterizations, we train our model on $p \in \mathcal{P}$ sweeps and fit the parameters using code provided in Ye et al. [72] (i.e., using PyTorch and L-BFGS to minimize the Huber loss of the mixing law). We do this over 5 random seeds for $k = 2, 3$ and over 3 seeds for the full SlimPajama.

For the linear dynamic parameterizations, for $k = 2, 3$ we train the model for 2000 steps according to some $p^0 \in \mathcal{P}$, and then sweep over \mathcal{P} for the next 100 steps. We do this for one random seed, performing $|\mathcal{P}|^2$ total runs. For the full SlimPajama setting, we train the model for 10000 steps using stratified sampling, and then sweep over \mathcal{P} for the next 5000 steps. We fit the parameters using Pytorch and L-BFGS.

C.1.1 Additional parameterization experiments

Parameterization across checkpoints. We investigate whether the log-linear static and linear dynamic mixing laws remain well-specified in later stages of training and on other datasets. To do so, we take various Pythia 160M checkpoints [8], sweep mixing proportions, and fit the linear dynamic and log-linear static mixing laws. We train for 2000 steps according to the learning rates and learning rate scheduler reported in [8]. We fit the static mixing law on full runs of 2000 steps, and the linear dynamic mixing law at $t = 500$, after which we do a training sweep over the next 500 steps. In Tables 6 and 7, we find that the strong fit for log-linear static mixing laws continues to hold during pre-training at checkpoint 72K (roughly halfway through training Pythia-160M) and after pre-training, with an average R^2 of 0.982 and 0.991, respectively. However, the linear dynamic mixing law’s R^2 coefficient is lower, averaging 0.815 at checkpoint 72K and 0.830 at the end of pre-training. It thus may be interesting to further study if the dynamics of the loss-proportion relationship evolve in a structured way throughout training, or if these results are due to more noise in how models learn at later stages of training.

Parameterization across other sets of data groups. In Figure 4, we identify an example set of data groups that exhibits a *non-linear* relationship between loss and proportion: Books/C4 from SlimPajama. For these two data groups, we see that as the proportion of Books increases while C4 decreases, the loss on Books starts *increasing* past a certain p , suggesting quite counterintuitively that performance on Books is optimized by allocating some proportion to C4. In this case, neither log-linear static or linear dynamic mixing laws have good fit to the proportion-loss relationship, as neither can represent the non-linearity. In particular, the average MSE and R^2 for the log-linear static mixing law is 0.003 and 0.558, respectively, and the average MSE and R^2 for the linear dynamic mixing law is 0.0002 and 0.721.

Fortunately, because these nonlinearities exist on the boundary of the simplex and tend to incur high loss, they tend to have little impact on the optimization of p , which strives to minimize the average loss. For instance, we found that the optimal proportion according to Ye et al. [72]’s log-linear static mixing law on one random seed was [0.176, 0.824], and the true optimal from grid search was [0.2, 0.8]. However, it is important to further investigate this non-linear phenomenon on additional data groups and training regimes, which we defer to future work.

Table 6: Comparison of log-linear static and linear dynamic mixing law parameterizations when training from the 72K Pythia-160M checkpoint.

Parameterization	Arxiv/SE		GH/C4		Books/SE	
	MSE	R^2	MSE	R^2	MSE	R^2
Log-linear static	2e-4	0.975	7e-5	0.992	2e-4	0.981
Linear dynamic	4e-4	0.834	7e-4	0.815	6e-4	0.796

Table 7: Comparison of log-linear static and linear dynamic mixing law parameterizations when training from the pre-trained Pythia-160M.

Parameterization	Arxiv/SE		GH/C4		Books/SE	
	MSE	R^2	MSE	R^2	MSE	R^2
Log-linear static	3e-6	0.994	4e-6	0.992	6e-6	0.986
Linear dynamic	5e-5	0.896	8e-5	0.824	1e-4	0.769

C.1.2 Parameterization on instruction-tuning mixtures

Previously, we studied if training on SlimPajama (from scratch, at a pre-training checkpoint, and at the end of pre-training) exhibited linear dynamic or log-linear static mixing. We now study if supervised fine-tuning on a mixture of task types exhibits similar mixing laws. The data mixing groups we consider are instruction-following tasks. It is important to know how to optimally mix these groups so that the model can follow a variety of instructions, as shown by how existing datasets consist of a diverse set of commands [15, 38, 47, 58, 67, 75].

We select $m = 9$ tasks from Natural Instructions [42, 67]: AbductiveNLI, BoolQ, HellaSwag, MathQA, PIQA, SemEval, SQuAD 1.1, SST2, and XSum. We selected tasks with many samples, prioritizing diversity of capabilities and formats. We construct validation and test splits that are 100 samples per group. More information is provided in Table 8.

To conduct the sweeps, we set \mathcal{P} to be 50 mixing proportions drawn from the Dirichlet distribution with $\alpha = 1.5$. For the static parameterization, we conduct 50 training runs over \mathcal{P} , for 1000 steps each, and we do this over 5 random seeds. For the dynamic parameterization, we train on 10 proportions from \mathcal{P} for 500 steps and then sweep over the entire \mathcal{P} for the next 100 steps. We do this over 1 random seed. We ensure there are no repeated samples in training. We use a pre-trained Pythia-160M model [8], consistent with the rest of our experiments, and use a linear scheduler with learning rate 1e-5 and 100 warmup steps.

Our results are in Table 9. In addition to displaying the averaged MSE and R^2 across all 9 groups, we also display per-group results. We find that the log-linear static mixing law attains an average R^2 of 0.888 over these instruction tasks. However, the linear dynamic mixing law only attains an average R^2 of 0.419. Interestingly, we observe that the 4 instruction tasks that involve open-ended generation have higher R^2 (average of 0.73) while the binary and multiple choice tasks have a lower R^2 (average of 0.17) for the linear dynamic law. We hypothesize that this is because tasks that do not require open-ended generation are easier to learn and more susceptible to overfitting. We observed that their validation losses often

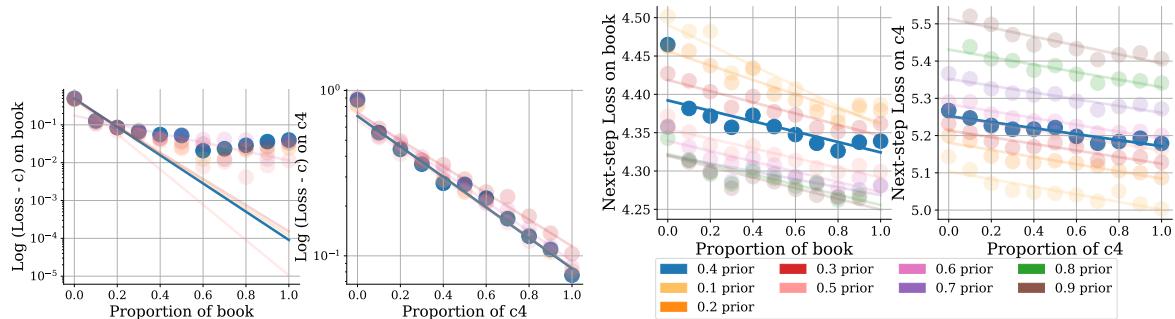


Figure 4: Top: Log-linear static mixing law fit on Books/C4 across 5 random seeds. Bottom: Linear dynamic mixing law fit on Books/C4 on 1 random seed. Each color is a different initial mixture $p^0 \in \mathcal{P}$ trained for 2000 steps, and the fitting sweeps are done over 100 additional steps.

Table 8: Overview of Instruction Tasks

Task	Task number in Natural Instructions	# Samples	Output Format
AbductiveNLI [7]	task067	6499	Open-ended
BoolQ [16]	task380	6500	Yes/No
HellaSwag [74]	task1389	6494	Multiple choice
MathQA [4]	task1420	6452	Multiple choice
PIQA [9]	task080	6500	Open-ended
SemEval [66]	task295	5996	Multiple choice
SQuAD 1.1 [52]	task075	6498	Open-ended
SST2 [55]	task363	6495	Pos/Neg
XSum [48]	task1290	6493	Open-ended

plateau before 500 steps, and increasing the proportions after this point does not consistently decrease loss. Finally, we also include a log-linear dynamic mixing law—that is, $\log(L_{\text{val},i}^t(\mathbf{p})) = \log(L_{\text{val},i}^{t-1}(\mathbf{p})) - \sum_{j=1}^m A_{ij}^t p_j^t$. This can be thought of as a piecewise version of the log-linear static mixing law, and we find that this slightly improves MSE and R^2 compared to the linear dynamic mixing law.

Table 9: Comparison of log-linear static, linear dynamic, and log-linear dynamic mixing law parameterizations over instruction-tuning tasks in terms of MSE and R^2 .

Task	Log-linear static		Linear dynamic		Log-linear dynamic	
	MSE	R^2	MSE	R^2	MSE	R^2
AbductiveNLI	3e-4	0.939	4e-4	0.586	4e-5	0.599
BoolQ	1e-3	0.941	8e-2	0.215	2e-2	0.276
HellaSwag	6e-4	0.848	6e-3	0.225	2e-3	0.256
MathQA	8e-4	0.787	6e-3	0.090	2e-3	0.115
PIQA	5e-4	0.916	3e-4	0.754	2e-5	0.761
SemEval	9e-4	0.974	4e-3	0.239	3e-3	0.254
SQuAD 1.1	8e-3	0.947	4e-3	0.742	9e-4	0.766
SST2	3e-3	0.662	2e-2	0.082	4e-2	0.118
XSum	1e-4	0.977	1e-4	0.838	1e-5	0.841
Average	2e-3	0.888	1e-2	0.419	8e-3	0.443

Checking for interactions among groups. It is natural to ask whether a *linear* mixing law is sufficient to model how mixing proportions affect the loss. In linear regression, such assumptions are often evaluated using visual diagnostics called *residual plots* [43]. Residual plots graph the prediction error from each data point (the *residuals*) in order to reveal different kinds of structure. For example, it is common to plot the residual against the predicted value to check for nonlinearity.

Figure 5 shows several such residual plots for the dynamic mixing law experiments with 3 domains (Arxiv, Books, and Stackexchange). The figure checks for interactions when predicting Arxiv’s loss. The corresponding plots for the other domains look similar.

The top row visualizes the residuals inside the simplex. If strong interactions were present, then they would cause clustered patterns in the residuals—regions where the linear model consistently gives predictions that are too low or too high. Strong patterns do not seem apparent.

The bottom three rows plot the residuals against different interaction terms. A consistent trend in the residuals above or below zero would suggest the term captures a meaningful interaction. The scatter plots show no consistent trend. The first three charts on the bottom row hint that a small interaction could be present in those cases; however, it is difficult to say without larger samples. Considering the linear model’s excellent fit and high R^2 , if such an interaction is present then it is likely small.

To summarize: the linear model seems sufficient. While we can not rule out the possibility of small interactions, the diagnostics do not reveal any major departures from linearity that might compel us to use a more complex model.

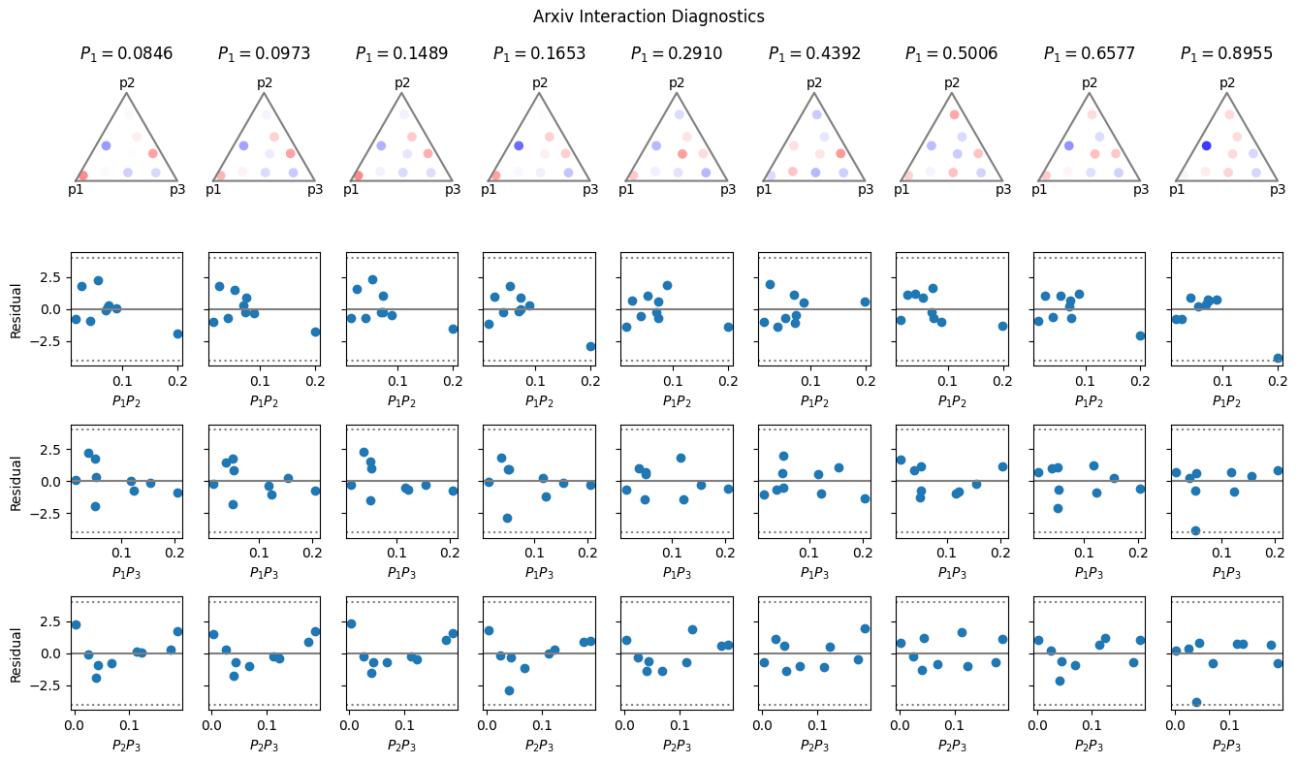


Figure 5: Residuals plots to check for interactions in the dynamic mixing law experiments with 3 domains (Arxiv, Books, and StackExchange). The target loss is Arxiv. Columns correspond to different initial mixing proportions. Data points show the (externally studentized) residuals of different mixing proportions after fitting the linear mixing law. Top row: Each point in the simplex corresponds to a different mixture of the 3 domains, with its color giving the residual's value at that point (red is positive, blue is negative). Bottom 3 rows: each row shows the residual plotted against a different interaction term: P_1P_2 , P_1P_3 , and P_2P_3 . Dotted gray lines show upper and lower 99% confidence limits for the residuals, assuming the linear regression assumptions hold.

C.2 Values of mixing law parameters

We explain how to compare method-specific A^t 's to an approximation of the true A^{t*} . First, after performing method-specific initialization, such as training reference models, we run each online method (Skill-It, DoReMi's proxy model DoGE's proxy model, Skill-it, and AIOLI) for t steps. For Skill-It, DoReMi, and DoGE, we use the unrestricted setting configuration of hyperparameters presented in Section E. For AIOLI, we analyze the parameters of AIOLI +GS from the restricted setting, since we found that this had less noisy fluctuation in the weights than in the unrestricted setting. For $m = 2$, we set $t = 1000$ for Skill-It and $t = 500$ for DoGE, DoReMi, and AIOLI since Skill-It is updated less frequently. For $m = 3$, we set $t = 1000$ for DoGE, DoReMi and Skill-It, and $t = 1500$ for AIOLI. We then checkpoint the language model and the method's A^t . For DoGE and DoReMi, we compute a smoothed $A^t = \frac{1}{100} \sum_{i=1}^{100} A^{t-100+i}$ because each A^t is computed at the batch level, and can thus be noisy. For AIOLI, we also smooth the A^t by averaging the previous timestep parameters.

To approximate A^{t*} , we then run a training sweep of p^t over \mathcal{P} for 100 steps on the checkpoint. We use this training sweep to fit A^{t*} from the dynamic mixing law $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - \sum_{j=1}^m A_{ij}^{t*} p_j^t$.

Before we compare parameters, we scale A^t by some b^t where $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - b^t \sum_{j=1}^m A_{ij}^t p_j^t$ for all $i \in [m]$. This is allowed since b^t does not influence the optimal \mathbf{p} and does not need to be in the update rule. We fit a single b^t across each group's mixing law and set $\tilde{A}^t = b^t A^t$. We can then compare A^t and A^{t*} using the metric $\text{sim}(\tilde{A}^t, A^{t*}) = 0.5\text{cossim}(\tilde{a}^t, a^{t*}) + 0.5\text{Spearman}(\tilde{a}^t, a^{t*})$, which we proposed in Section 4.3.

C.2.1 Properties of A^{t*}

We discuss some properties of A^{t*} , finding that 1) A^{t*} can vary significantly across time, and 2) A^{t*} needs to be modeled as a full matrix. To do this, for each initial mixture $p^0 \in \mathcal{P}$, we train for $t = 2000$ steps and then sweep over \mathcal{P} for the next 100 steps. We repeat this setup for $t = 4000$ to obtain A^{2000*} and A^{4000*} . We do this experiment for Arxiv/Stackexchange and Github/C4.

Extent of time variation of A^t . We find that the column sums of A^t can change order over time, meaning that the p^t “changes direction” in terms of which group has the largest proportion. In particular, for $p^0 = [0.5, 0.5]$ and Github/C4, we have that

$$A^{2000*} = \begin{bmatrix} 0.148 & 0.011 \\ -0.013 & 0.087 \end{bmatrix} \quad A^{4000*} = \begin{bmatrix} 0.015 & 0.001 \\ 0.001 & 0.015 \end{bmatrix} \quad (10)$$

The column sums are $\mathbf{1}^\top A^{2000*} = [0.135, 0.098]$ and $\mathbf{1}^\top A^{4000*} = [0.016, 0.017]$, showing that the ordering of proportions of the groups changes. This suggests that the optimal p^t can change significantly across time, prioritizing Github initially and later C4, which is also reflected for Github/C4 in the greedy row of Table 10.

However, for Arxiv/Stackexchange, the column sums of A^{2000*} and A^{4000*} never change in terms of the ordering of proportions of the data groups, across all $p^0 \in \mathcal{P}$. As a result, the optimal p^t never changes direction. This suggests that how much A^t varies in ordering over time depends on the data groups. As a result, methods like Skill-It, which use a time-invariant A^{SG} multiplied by validation loss, may not be able to match the true A^{t*} if the groups' validation losses do not change in ranking across time, which we observe in Github/C4.

Modeling A^{t*} as a full vs diagonal matrix. We find that modeling the off-diagonal entries of A^{t*} is important. For each sweep, we fit both A^{t*} as described above and a diagonal matrix A_d^{t*} . We compare if the column sums of A^{t*} and A_d^{t*} differ in the order of elements.

We find that for Arxiv/StackExchange, $p^0 = 0.4$, and both $t = 2000$ and $t = 4000$, setting p^t based on the full matrix would put a larger proportion on StackExchange, while setting p^t based on the diagonal matrix would put a larger weight on ArXiv. In particular, the full and diagonal matrices for $t = 2000$ are

$$A^{2000*} = \begin{bmatrix} 0.249 & 0.058 \\ 0.025 & 0.224 \end{bmatrix} \quad A_d^{2000*} = \begin{bmatrix} 0.284 & 0 \\ 0 & 0.238 \end{bmatrix} \quad (11)$$

The second column sum is larger for A^{2000*} and smaller for A_d^{2000*} . We also have similar findings on Github/C4; for $p^0 = 0.6$ and $t = 2000$, we have

$$A^{2000*} = \begin{bmatrix} 0.119 & 0.027 \\ -0.010 & 0.104 \end{bmatrix} \quad A_d^{2000*} = \begin{bmatrix} 0.135 & 0 \\ 0 & 0.098 \end{bmatrix} \quad (12)$$

Using the diagonal matrix for Github/C4 would result in prioritizing training on Github, even though the full matrix suggests that C4 should be prioritized. Therefore, it is important to model A^{t*} as a full matrix. As a result, methods like DoReMi, which use a diagonal A^t , can perform suboptimally.

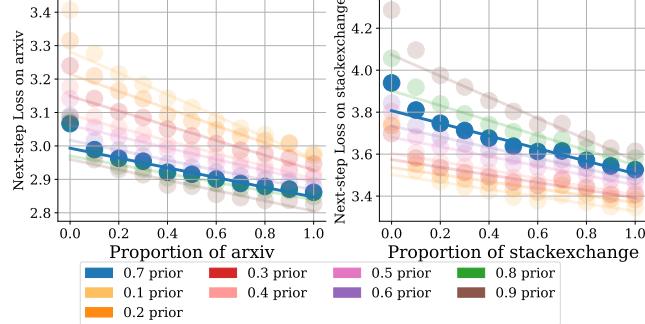


Figure 6: The linear dynamic parameterization results from Figure 2 (right), with $p^t = [0, 1]$ and $[1, 0]$ also plotted. We see that the linear dynamics are misspecified at $p_i^t = 0$ for both i .

C.3 Solving strategy

We present our results on examining the assumptions made in how existing methods solve the LMO optimization problem. All online methods use exponentiated gradient descent, which updates p^t using the gradient at the current timestep. This involves a greedy approximation of the objective function. We study if the greedy approximation yields a \mathbf{p} is close to the true optimal \mathbf{p} .

For $m = 2$ data settings, we take our $S = 5000$ steps and split it into $T = 2$ rounds. We perform a brute-force sweep at each round over \mathcal{P} , which sweeps $p_1 = 0.1, 0.2, \dots, 0.9$. In total over one random seed, we conduct 81 training runs for each of Arxiv/Stackexchange, Github/C4, and Books/Stackexchange.

We determine the greedy-approximate \mathbf{p} by selecting the best p^1 . Then, conditioning on this p^1 , we select the best p^2 . We report what the greedy \mathbf{p} and its performance is in the first row of Table 10, and we report the optimal \mathbf{p} and its performance in the second row. Note that this protocol does not depend on the mixing law or a method for setting \mathbf{p} .

We find that for Arxiv/StackExchange and Books/StackExchange, the greedy proportions and the optimal proportions are identical. However, for Github/C4, the greedy approximation fails to recover the optimal proportions. Therefore, the greedy approximation recovers the optimal dynamic proportions in 2 out of 3 cases.

Table 10: Comparison of the greedily selected p^1, p^2 versus the optimal p^1, p^2 for a $T = 2$ rounds data mixing problem. On 2 out of 3 datasets, the greedily selected proportions match the optimal proportions.

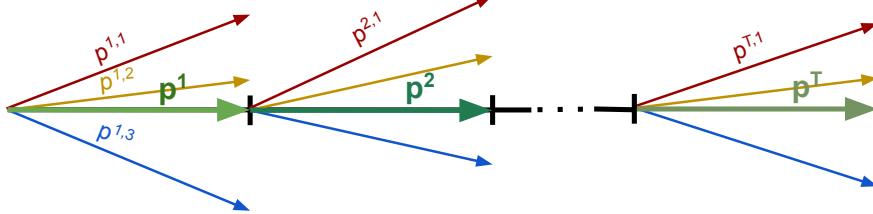
Solving	Arxiv/SE		GH/C4		Books/SE	
	p_1^1, p_1^2	Avg test PPL	p_1^1, p_1^2	Avg test PPL	p_1^1, p_1^2	Avg test PPL
Greedy	0.4, 0.4	16.039	0.6, 0.4	36.525	0.3, 0.6	45.513
Optimal	0.4, 0.4	16.039	0.3, 0.6	34.709	0.3, 0.6	45.513

Beyond exponentiated gradient descent, one may wonder if exactly solving the greedy objective could suffice. For the linear dynamic mixing law $L^{t+1}(\mathbf{p}) = L^t(\mathbf{p}) - A^t p^t$, the optimal p^t is $\mathbf{1}_j$, where $j = \arg \max \sum_{i=1}^m A_{ij}^t$. However, we find in Figure 6 that the loss-proportion relationship can be nonlinear at the edge of the simplex where $p^t = \mathbf{1}_j$. Exponentiated gradient descent, which uses entropy regularization, is hence able to implicitly avoid extreme \mathbf{p} where the linear mixing law is misspecified and thus is a practical technique for LMO.

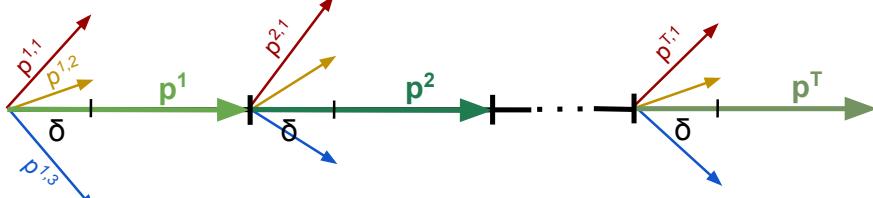
D Additional Algorithmic Details

In AIOLI, LEARNPARAMS is used in each round to learn A^t . Then, A^t is used to compute p^t , which is used for training during the round. We provide a derivation of LEARNPARAMS by first presenting a naive, high-cost method for estimating A^t (Appendix D.1). This involves checkpointing the model at each round, running a training sweep over the round and observing the changes in validation losses, and fitting A^t to these changes. Then, we layer on two modifications that compute slightly different loss changes, helping lower the cost of estimation. First, we shorten the training sweep to be only over a fraction of the round, δ , and use these shortened changes in validation losses to fit A^t (Appendix D.2). Second, we simulate a simultaneous training sweep by partitioning the δ fraction of the round into many small parts, interleaving the different sweep mixtures at a fine granularity and averaging the loss changes for each sweep mixture (Appendix D.3). This idea, with

1. Naive approach with full training sweeps



2. Shorten training sweeps



3. Aioli: interleave training sweeps

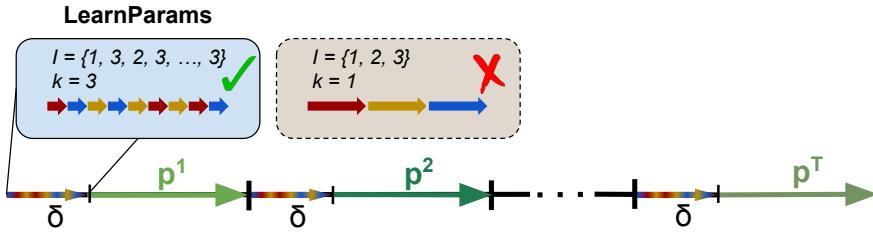


Figure 7: Derivation of AIOLI. Top: a naive high-cost approach where training sweeps are conducted to fit A^t at each round (Appendix D.1). Middle: a modification that shortens the training sweeps used to learn A^t (Appendix D.2). Bottom: a final modification that interleaves the sweep mixtures at a high frequency (large k) in one single run, enabling AIOLI’s LEARNPARAMS to require no additional training (Appendix D.3).

similarity to concepts like time-division multiplexing in signal processing [12], enables AIOLI to require no extra training while trading off accuracy of the estimate. We provide a sketch of our derivation in Figure 7.

D.1 Naive training sweep approach

This approach is depicted in Figure 7 (top). By conducting a training sweep over round t , we can use a linear system of equations to estimate A^t from the linear dynamic mixing law $L_{\text{val},i}^{t+1}(\mathbf{p}) = L_{\text{val},i}^t(\mathbf{p}) - \sum_{j=1}^m A_{ij}^t p_j^t$. Let $p^{t,1}, p^{t,2}, \dots, p^{t,m} \in \Delta^m$ comprise a training sweep over the duration of round t . First, we checkpoint the model f^t , and for simplicity denote f^t ’s validation loss on group i as $L_{\text{val},i}^t$. For each $p^{t,j}$, we train f^t for the entire round using $p^{t,j}$. We then record how much the validation loss on each group changes, $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,j})$ for all $i \in [m]$. By the end of this procedure on each $p^{t,j}$, we have the following system of equations for each $i \in [m]$:

$$\begin{aligned}
 \sum_{j=1}^m A_{ij}^t p_j^{t,1} &= L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,1}) \\
 \sum_{j=1}^m A_{ij}^t p_j^{t,2} &= L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,2}) \\
 &\vdots \\
 \sum_{j=1}^m A_{ij}^t p_j^{t,m} &= L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,m})
 \end{aligned} \tag{13}$$

This is a system of linear equations with m unknowns: A_{i1}, \dots, A_{im} . We can write it in matrix form as:

$$\begin{bmatrix} p_1^{t,1} & p_2^{t,1} & \dots & p_m^{t,1} \\ p_1^{t,2} & p_2^{t,2} & \dots & p_m^{t,2} \\ \vdots & \vdots & & \vdots \\ p_1^{t,m} & p_2^{t,m} & \dots & p_m^{t,m} \end{bmatrix} \begin{bmatrix} A_{i1}^t \\ A_{i2}^t \\ \vdots \\ A_{im}^t \end{bmatrix} = \begin{bmatrix} L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,1}) \\ L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,2}) \\ \vdots \\ L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,m}) \end{bmatrix} \quad (14)$$

Let $P \in \mathbb{R}^{m \times m}$ be the leftmost matrix and $\beta_i \in \mathbb{R}^m$ be the vector on the right hand side. Then, we can write $A_i^t = P^{-1}\beta_i$. We solve this system for each $i \in [m]$ to obtain A^t .

The advantage of this method is that it directly estimates the optimal A^{t*} that is used in the mixing law. However, it requires m sweeps per round, because the key quantity we must observe to learn A^t is $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p)$: the change in loss after training through the *entire* round t . As a result, this approach requires m extra full training runs to learn A^t . Below, we will describe how we can compute cheaper alternatives to $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p)$.

D.2 Modification 1: shortening training sweeps

This modification is depicted in Figure 7 (middle). A simple way to reduce the number of extra training runs needed to estimate A^t is to train on each mixture $p^{t,j}$ for less than a round. Let δ denote the fraction of the round we use for the training sweep. Then, our system of equations in 14 uses $L_{\text{val},i}^t - L_{\text{val},i}^{t+\delta}(p^{t,j})$; we simply record the loss difference over δ of the round rather than the entire round, and use this to solve for A^t . Now, this approach effectively requires $m\delta$ extra training runs; however, this cost is still linear in the number of data groups. Moreover, there is some inaccuracy incurred by using δ of a round to approximate the entire round.

D.3 Modification 2: “interleaving” training sweeps

This modification is depicted in Figure 7 (bottom). Our final modification to derive LEARNPARAMS is to convert the training sweep—where we checkpoint the model and execute m separate runs for δ of a round—into one round without requiring any checkpointing or rolling back of training. Our intuition is that if we interleave different mixtures sequentially at a high frequency, we can simulate executing these mixtures simultaneously. This is similar to a concept in signal processing called time-division multiplexing, in which two or more signals or bit streams are transferred appearing simultaneously as sub-channels in one communication channel, but are physically taking turns on the channel¹.

Formally, we break down the $\delta S/T$ steps allocated for learning A^t into K intervals, where $K = mk$ and k is the number of sweeps per mixture. We construct an interleaved order of $p^{t,1}, \dots, p^{t,m}$ over these K intervals, and we denote their index order as $\mathcal{I} \in [m]^K$. Let \mathcal{I}_τ denote the mixture at the τ th position in \mathcal{I} . We can denote the model at the end of each interval as $t + \delta/K, t + 2\delta/K, \dots, t + \delta$. During the τ th interval, we train on one p^{t,\mathcal{I}_τ} and observe the change in loss, $L_{\text{val},i}(f^{t+(\tau-1)\delta/K}) - L_{\text{val},i}(f^{t+\tau\delta/K})$ for each validation group i . Let $\mathcal{T}_j = \{\tau : \mathcal{I}_\tau = j\}$ be all the intervals where $p^{t,j}$ is assigned. We approximate $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p^{t,j})$ with $\frac{1}{|\mathcal{T}_j|} \sum_{\tau \in \mathcal{T}_j}^k L_{\text{val},i}(f^{t+(\tau-1)\delta/K}) - L_{\text{val},i}(f^{t+\tau\delta/K})$. These approximated loss differences are then used to recover A^t from the system of linear equations.

Lastly, note that the choice of k controls the interleaving frequency and the bias of the estimated A^t . Suppose that $k = 1$. This means that each mixture is only assigned to one interval, and this could be at the beginning, middle, or end of the δ round. Then, the change in loss is a poor approximation of the original quantity $L_{\text{val},i}^t - L_{\text{val},i}^{t+1}(p)$ due to dependence on time. However, as we increase k , the mixture $p^{t,j}$ will be trained on in the beginning, middle, and end of the δ round, allowing for a less time-biased estimate of the loss change.

With this modification, LEARNPARAMS now requires *no extra training*. However, there are still some performance tradeoffs. First, in order to save compute, our estimate of A^t via the shortened interleaved sweeps is less accurate than the naive approach. Second, without rolling back training, AIOLI has both an “explore” and “exploit” phase, where the former learns A^t over δ of the round and the latter uses A^t to set p^t and mix data accordingly for the remainder of the round. If δ is large, the estimate of A^t may be relatively more accurate. However, training for longer on the sweep mixtures $p^{t,1}, \dots, p^{t,m}$ may be suboptimal for the performance of the model. Moreover, the training duration that utilizes the p^t that is updated using the more accurate A^t is now shortened. Therefore, adjusting δ is key to ensuring that A^t is accurate and the model performs well.

¹https://en.m.wikipedia.org/wiki/Time-division_multiplexing

E Experimental Details

E.1 Data

To obtain a test set, we shuffle and split the validation set from SlimPajama-6B [54, 73] in half.

To perform training sweeps and emulate grid searches in static settings for $m = 3, 7$, we oversampled from the Dirichlet with $\alpha = 1$ by $4x$ the number of points and then hierarchically merged closest points into a centroid until we obtained x points. For example, to obtain 10 points in the 7-dimensional simplex for SlimPajama-full, we would sample 40 points in the simplex and hierarchically merge closest points until 10 points remain. This is to ensure that near-duplicate p 's are not included in the sweep. This procedure is used in Grid Search (GS) and DML in Section 6 and in our analysis in Section 4

E.1.1 Training

Here, we discuss the training setups for the restricted and unrestricted settings. For the $m = 2, 3$ settings, we train a 160M model using Pythia-160M's configuration for $S = 5000$ steps and results are averaged over 5 random seeds. For $m = 7$, we train a 160M model using Pythia-160M's configuration for $S = 40000$ steps results are averaged over 3 random seeds. All settings use FlashAttention [18], batch size of 8, context size of 2048, and cosine learning rate decay from a starting learning rate of 5e-5 to 1e-5 with 500 steps of learning rate warmup.

For the $m = 2, 3$ settings, experiments were run on a NVIDIA RTX 6000 Ada Generation GPU. For the $m = 7$ setting, experiments were run on a NVIDIA A100 80 GB GPU.

Restricted versus unrestricted. Both the restricted and unrestricted settings share the same length of the final training runs (5000 and 40000 steps, as above). The unrestricted setting gives all methods up to 10 training runs to initialize mixing algorithm parameters, or $10S$ steps, while the restricted setting give $0.5S$ steps. See Table 11 for training budget allocations in each setting. AIOLI and stratified sampling do not use extra training runs.

Table 11: Training budget allocations for restricted and unrestricted settings.

Setting	m	Method	Runs within training budget
Unrestricted	2	DML	10 runs, 5000 steps
		Skill-it	2 runs, 5000 steps
		DoReMi	2 runs, 5000 steps
		DoGE	1 run, 5000 steps
	3	DML	10 runs, 5000 steps
		Skill-it	3 runs, 5000 steps
		DoReMi	2 runs, 5000 steps
		DoGE	1 run, 5000 steps
	7	DML	10 runs, 40000 steps
		Skill-it	7 runs, 40000 steps
		DoReMi	2 runs, 40000 steps
		DoGE	1 run, 40000 steps
Restricted	2	DML	10 runs, 250 steps
		Skill-it	2 runs, 1250 steps
		DoReMi	2 runs, 1250 steps
		DoGE	1 run, 2500 steps
	3	DML	10 runs, 250 steps
		Skill-it	3 runs, 833 steps
		DoReMi	2 runs, 1250 steps
		DoGE	1 run, 2500 steps
	7	DML	10 runs, 2000 steps
		Skill-it	7 runs, 2814 steps
		DoReMi	2 runs, 10000 steps
		DoGE	1 run, 20000 steps

E.2 Data mixing methods

AIOLI-specific hyperparameters In the unrestricted setting, we found it sometimes helpful to use an exponential moving average with proportion γ over A^t for AIOLI. Formally, the standard p^t update rule in Algorithm 1 can be unrolled as $p_j^{t+1} \propto p_j^0 \exp(\eta \sum_{\tau=1}^t \sum_{i=1}^m A_{ij}^\tau)$, which places equal weight on every A_{ij}^τ . To incorporate the EMA, we define $A_{\text{ema}}^1 = \bar{A}^1$ and $A_{\text{ema}}^t = (1 - \gamma)\bar{A}^t + \gamma A_{\text{ema}}^{t-1}$. We then use the update rule $p_j^{t+1} \propto p_j^0 \exp(\eta A_{\text{ema}}^t)$. This allows AIOLI to gradually decay the contributions of A^t , such that the value of p^t is less dependent on earlier proportions in the training.

We summarize the hyperparameters used in AIOLI, providing their default values as well as guidelines for how to set them. Refer to Algorithm 1 and 2 to see how they are used:

- Number of rounds T : we set this to 20 in all experiments. Larger T means more frequent updates to the mixture proportions.
- Sweeps k : we set this to be 4 for $m = 2, 3$ and 2 for the full SlimPajama experiments. We did not adjust this hyperparameter otherwise. Intuitively, a larger k will give a more accurate A^t , because this means that each $p^{i,t}$ will be trained on more frequently throughout the δ proportion of the round; however, this will also result in less of the round being allocated to exploiting A^t via using p^t .
- ε one-hot smoothing factor: we set this to be 0.75 in all experiments. In general, ε must be set between 0 and 1, where 0 results in the training sweep using one-hot mixture proportions to learn A^t , which means that each batch only consists of one data group and can result in poor learning dynamics. $\varepsilon = 1$, on the other hand, means that our training sweep would only consist of uniform proportions.
- EGD step size η : we sweep $\{0.1, 0.2, 0.3, 0.5\}$, with higher η resulting in greater magnitude of the proportion update.
- Proportion of round δ dedicated to learning A^t : We use $\delta = 0.128, 0.288, 0.007$ for $m = 2, 3, 7$, respectively. Intuitively, a larger δ will give more accurate A^t because the parameter is learned on more data, but this will also result in less of the round being allocated to exploiting A^t via using p^t .
- EMA parameter γ : we sweep None, 0.1, 0.5. Intuitively, None means that the p^t update is equally dependent on all previous p^t 's, while a small $\gamma = 0$ means that the p^t update is only a function of the current A^t .

For the last three hyperparameters, η, δ, γ , we used different values of them in different experiments. Tables 12, 13, 14, 15, 16, and 17 list exact values for the unrestricted and restricted settings for $m = 2, 3, 7$. In addition, Appendix F.3 provides results on hyperparameter sensitivity for η, δ , and γ .

Table 12: **Unrestricted** hyperparameter values for each data mixing algorithm for experiments where $m = 2$ (corresponding to Table 2 results).

Data groups	Hyperparameter	Value
arXiv/SE	· proportion of round δ	0.128
	· EGD learning rate η	0.2
	· EMA parameter γ	0.1
GitHub/C4	· proportion of round δ	0.128
	· EGD learning rate η	0.3
	· EMA parameter γ	0.5
Books/SE	· proportion of round δ	0.128
	· EGD learning rate η	0.1
	· EMA parameter γ	None

Baseline hyperparameters. We consulted the original papers and implementations to determine how to set the hyperparameters for each baseline, ensuring that the updated proportions were changing significantly but not oscillating under these configurations.

- **Skill-It**: the hyperparameters are the number of rounds T , the EGD learning rate η , and the multiplicative weights window w . Our default configuration was $T = 10$, $\eta = 0.2$, and $w = 3$. However, we made two exceptions in the unrestricted setting after conducting a sweep over $T \in \{5, 10\}$ and $\eta \in \{0.1, 0.2, 0.5, 0.8\}$; for GitHub/C4, we used $T = 5$ and $\eta = 0.1$, and for Books/StackExchange, we used $\eta = 0.8$.
- **DoReMi**: the hyperparameters are the EGD learning rate η and a smoothing factor ε (0 = no smoothing). For all experiments, we set $\eta = 0.01$ and $\varepsilon = 1e-3$.

Table 13: **Restricted** hyperparameter values for each data mixing algorithm for experiments where $m = 2$ (corresponding to Table 3 results).

Data groups	Hyperparameter	Value
arXiv/SE	· proportion of round δ	0.128
	· EGD learning rate η	0.2
	· EMA parameter γ	None
GitHub/C4	· proportion of round δ	0.128
	· EGD learning rate η	0.2
	· EMA parameter γ	None
Books/SE	· proportion of round δ	0.128
	· EGD learning rate η	0.2
	· EMA parameter γ	None

Table 14: **Unrestricted** hyperparameter values for each data mixing algorithm for experiments where $m = 3$ (corresponding to Table 2 results).

Data groups	Hyperparameter	Value
arXiv/Books/SE	· proportion of round δ	0.288
	· EGD learning rate η	0.5
	· EMA parameter γ	None
CommonCrawl/GitHub/Wiki	· proportion of round δ	0.288
	· EGD learning rate η	0.3
	· EMA parameter γ	0.5

Table 15: **Restricted** hyperparameter values for each data mixing algorithm for experiments where $m = 3$ (corresponding to Table 3 results).

Data groups	Hyperparameter	Value
arXiv/Books/SE	· proportion of round δ	0.288
	· EGD learning rate η	0.2
	· EMA parameter γ	None
CommonCrawl/GitHub/Wiki	· proportion of round δ	0.288
	· EGD learning rate η	0.2
	· EMA parameter γ	None

Table 16: **Unrestricted** hyperparameter values for each data mixing algorithm for experiments where $m = 7$ (corresponding to Table 2 results).

Data groups	Hyperparameter	Value
SlimPajama, full	· proportion of round δ	0.07
	· EGD learning rate η	0.2
	· EMA parameter γ	0.1

- **DoGE**: the hyperparameters are the EGD learning rate η , the smoothing factor ε , and the proportion of the training batch that is allocated for the validation dataset r ; this is needed to compute the gradient dot-product at each step. We use $\varepsilon = 0$ for all experiments. For $m = 2$, we set $r = 0.25$ and for $m = 3, 7$, we set $r = 0.5$. For all experiments besides Github/C4 and SlimPajama, we use $\eta = 0.01$. For Github/C4, we use $\eta = 0.1$ and for SlimPajama we used $\eta = 0.1$ and $\eta = 0.03$ for unrestricted and restricted settings, respectively.

Weight trajectories. In Table 18, we provide the mixture proportions for each method (averaged across training steps) for each dataset on one random seed. In Figure 8, we provide all of AIOLI’s proportion trajectories throughout training

Table 17: **Restricted** hyperparameter values for each data mixing algorithm for experiments where $m = 7$ (corresponding to Table 3 results).

Data groups	Hyperparameter	Value
SlimPajama, full	· proportion of round δ	0.07
	· EGD learning rate η	0.2
	· EMA parameter γ	0.1

in both the unrestricted and restricted settings on one random seed for the $m = 2$ settings. In Figure 9 and Figure 10, we provide AIOLI’s trajectories in the unrestricted and restricted settings on one random seed for Arxiv/Books/StackExchange and CommonCrawl/Github/Wikipedia, respectively. All of our trajectories demonstrate that AIOLI can significantly adjust proportions over time, and that conditioning on different initial proportions can drastically change the behavior of AIOLI.²

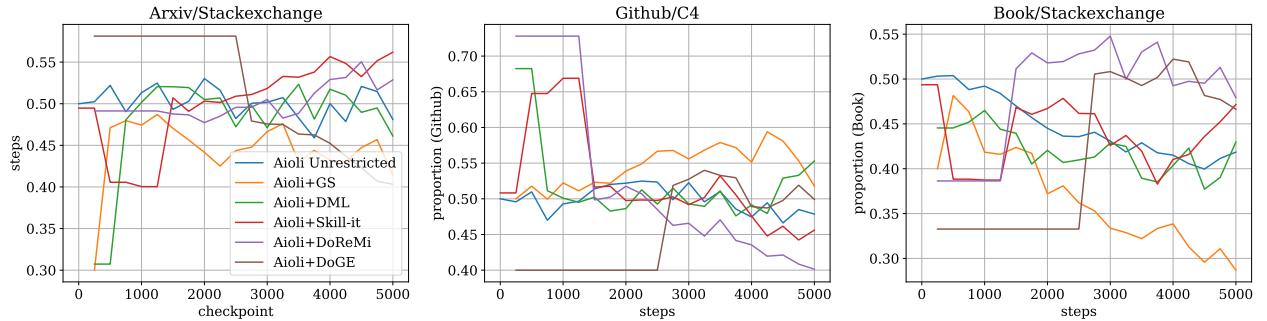


Figure 8: AIOLI’s proportions throughout training for both unrestricted and restricted settings on Arxiv/StackExchange, Github/C4, and Book/StackExchange. These trajectories show that AIOLI meaningfully alters the mixture proportions over time.

F Additional Experiments

F.1 Downstream Tasks

We find that lower perplexity is positively correlated with worse performance on downstream tasks. We evaluated all models trained on SlimPajama on ARC-Challenge, ARC-Easy [17], BoolQ [16], HellaSwag [74], LAMBADA [49], OpenBookQA [40], PiQA [9], and WinoGrande [53] using the Language Model Evaluation Harness [23] (Table 19). The correlation between perplexity and the macroaverage of our downstream tasks is 0.529, indicating that lower perplexity is predictive of *worse* downstream performance. In fact, DML obtains the best overall performance, even though it omits three out of seven datasets in SlimPajama (see the average proportions in Table 18).

One potential reason for this disparity is the distribution shift between pre-training data and downstream evaluation data; for example, the DML results suggest that training on Books, C4, and Github is not needed to do well on the above selection of downstream tasks. Many recent works have also noted that perplexity and downstream performance are uncorrelated [36, 59, 68]. Furthermore, Levy et al. [33] proposes a question answering dataset where the perplexity of the pretrained model is positively correlated with performance, similar to our results. This mismatch between training objective and downstream evaluations also extends to post-training, where better learning of human preferences does not translate to better win-rate against other post-trained models [13].

Resolving the disconnect between training objective and downstream evaluations is an area of active research. In the case of data mixing, AIOLI remains the only algorithm in our tests that robustly minimizes average test perplexity—essentially, AIOLI achieves what it sets out to achieve in the LMO framework in (1). Conversely, other data mixing algorithms might be implicitly doing something else with respect to minimizing downstream evaluations. Considering how to incorporate downstream evaluations into data mixing is a fruitful area for future work.

²Note that for the restricted setting, AIOLI’s trajectory consists of using the base method for a certain amount of steps, and then roughly reverting to the uniform distribution before adjusting the proportions. This is expected behavior, since our initial proportions p^0 are uniform in Algorithm 1; this avoids a “biased” proportion update.

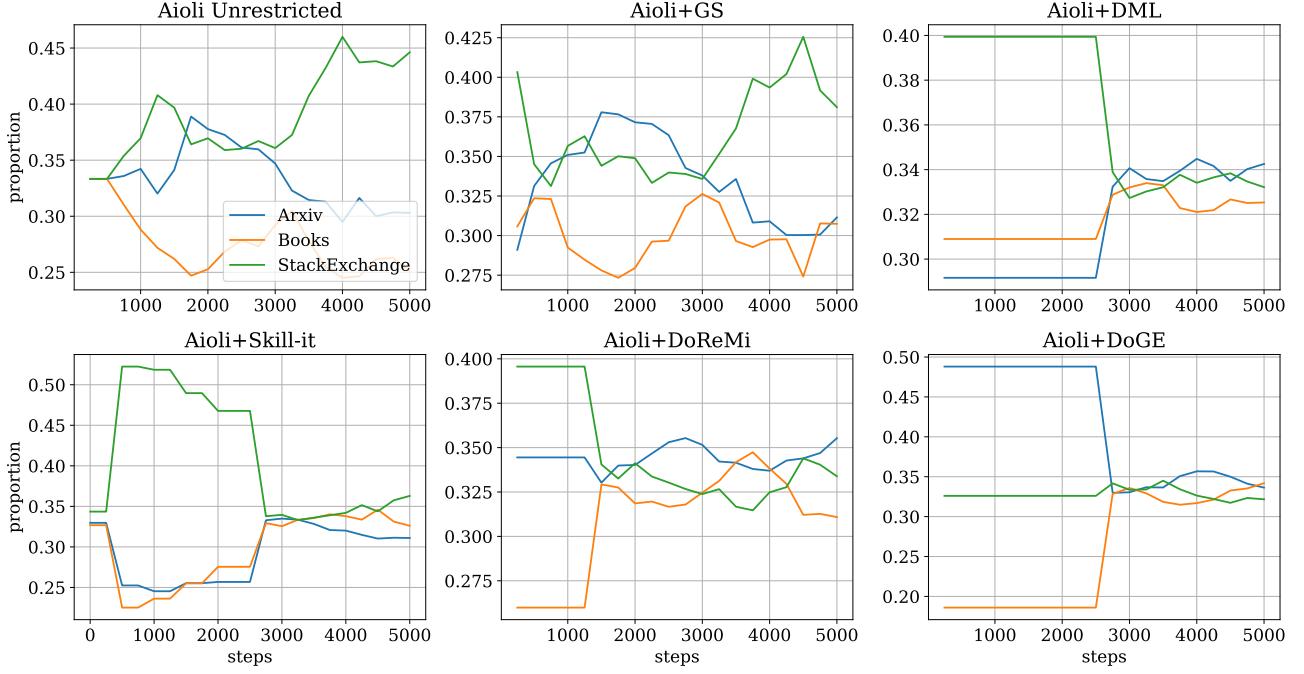


Figure 9: AIOLI’s proportions throughout training for both unrestricted and restricted settings on Arxiv/Book/StackExchange. These trajectories show that AIOLI meaningfully alters the mixture proportions over time.

F.2 Ablations

We ablate AIOLI by studying performance when two key properties of A^t (Appendix C.2.1) are changed: when $T = 1$ (i.e., A^t is only learned once at the beginning of training and used throughout), and when A^t is assumed to be diagonal. We evaluate these two ablations in the unrestricted setting presented in Section 6.1 and Table 2:

- **AIOLI-STATIC:** We set $T = 1$ in Algorithm 1. That is, we learn A^1 at the beginning of training. We use this A^1 to set p^1 , and use this p^1 for the remainder of the training run. This approach tests if A^t needs to be adjusted throughout training.
- **AIOLI-DIAGONAL:** We assume that each A^t is diagonal in this ablation. In particular, in LEARNPARAMS we do $A_{ii}^t = \beta_{ii}/p^{t,i}$ rather than $A_i^t = P^{-1}\beta_i$ for each $i \in [m]$ in line 11. This approach tests if it is sufficient to not model cross-group interactions and instead only capture how much group i ’s performance improves when trained on group i itself.

For both AIOLI-STATIC and AIOLI-DIAGONAL, we use the same set of hyperparameters as AIOLI as described in Appendix E. For AIOLI-STATIC, we additionally sweep over EGD learning rates $\{\eta, 2\eta, 3\eta, 4\eta\}$ where η is the EGD learning rate used by AIOLI.

Our results are in Table 20. We find that AIOLI outperforms both ablations in 3 out of 6 settings, and obtains the lowest test perplexity on average over these settings. This suggests that both $T > 1$ and modeling off-diagonal entries are important to AIOLI’s consistent performance across datasets.

F.3 Hyperparameter sensitivity

We study how robust AIOLI is to changes in its hyperparameters. From the experimental details in Appendix E, the main hyperparameters that we modify are η (EGD step size), δ (proportion of round allocated for learning A^t), and γ (the EMA parameter). In Tables 21, 22, and 23, we report results on AIOLI in the unrestricted setting for Arxiv/StackExchange and Arxiv/Books/StackExchange. We sweep $\eta \in \{0.1, 0.2, 0.3, 0.5\}$, $\delta/m \in \{0.064, 0.096, 0.128\}$, and $\gamma \in \{\text{None}, 0.1, 0.5\}$. We find that AIOLI still yields lower test perplexity than stratified sampling across all η , δ , and γ we evaluated.

F.4 Results on Larger Models

We examine if our findings—both in terms of the mixing law and in terms of AIOLI’s performance—hold on larger models. We train 1.4B-parameter models. We use a learning rate of $3\text{e-}4$ and keep all other training details the same. We use a

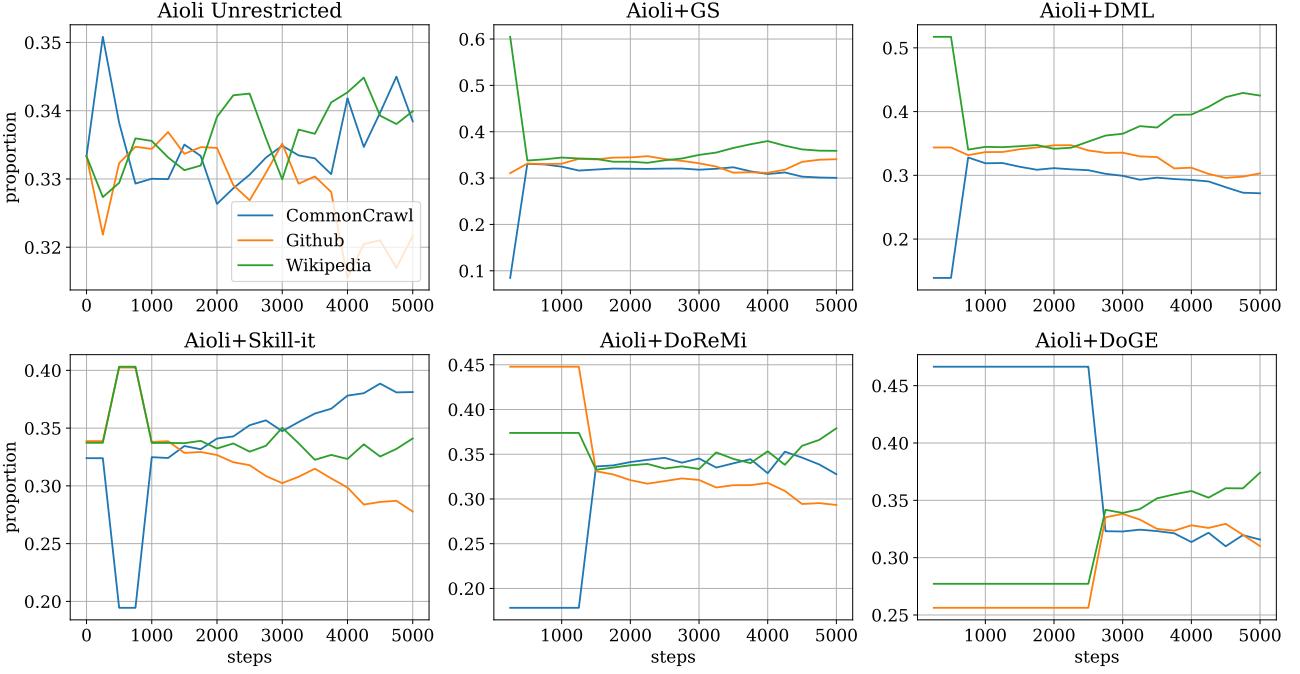


Figure 10: AIOLI’s proportions throughout training for both unrestricted and restricted settings on CommonCrawl/Github/Wikipedia. These trajectories show that AIOLI meaningfully alters the mixture proportions over time.

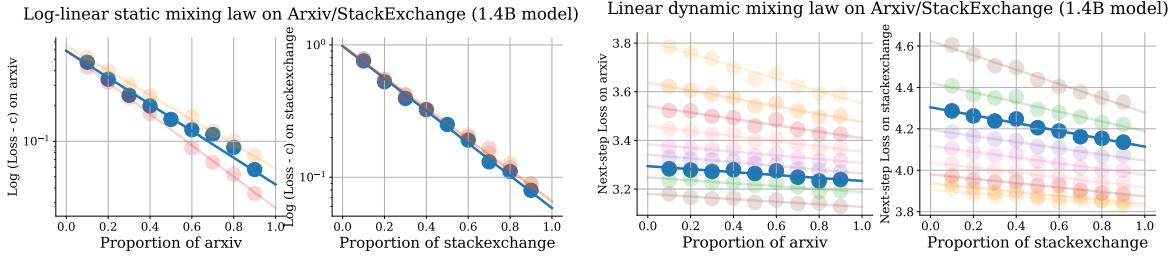


Figure 11: Left: log-linear static mixing law fit on Arxiv/Stackexchange on 1.4B parameter model, in which each color represents a different random seed. Right: linear dynamic mixing law fit on Arxiv/Stackexchange on 1.4B parameter model on 1 random seed. Each color is a different initial mixture $p^0 \in \mathcal{P}$ trained for 2000 steps, and the fitting sweeps are done over 100 additional steps.

subsample of our data settings, focusing on when we mix Arxiv/StackExchange ($m = 2$) and Arxiv/Book/StackExchange ($m = 3$).

First, we measure if the log-linear static and linear-dynamic mixing laws are well-specified for 1.4B models. We use the same fitting procedure as described in Section 4.1 and Appendix C.1. Figure 11 describes the fit of the static and dynamic mixing laws on Arxiv/StackExchange. The full results are in Table 24, which show that the average R^2 for the static and dynamic mixing laws for the 1.4B model are 0.989 and 0.929, respectively. This accuracy of the mixing law parameterization on the 1.4B model is a prerequisite for AIOLI’s performance, which we evaluate next.

Second, we evaluate AIOLI in the unrestricted setting on the 1.4B models. We compare AIOLI to stratified sampling and DoGE. Our results on three random seeds are in Table 25. Similar to our results on the 160M models, we find that AIOLI outperforms stratified sampling in both data settings. Moreover, from Table 2, we see that DoGE originally performed worse than stratified sampling at the 160M scale. Our results here confirm that even at the 1.4B model scale, DoGE continues to underperform stratified sampling. Altogether, we see that AIOLI consistently outperforms stratified sampling while existing methods do not—at both the 160M and 1.4B scale.

F.5 Out-of-domain setting

We consider the *out-of-domain* setting, in which the training data groups are disjoint from the groups that the model will be evaluated on. This is a practical scenario where we have access to a separate validation dataset that we wish our model to perform well on [14, 20, 22, 69, 71]. We will demonstrate how 1) the LMO framework can be adjusted to capture this setting, recovering the out-of-domain versions of Skill-It and DoGE proposed in their respective papers; 2) the linear mixing laws are still well-specified in this setting; and 3) AIOLI adjusted for this setting can still more consistently outperform out-of-domain baselines.

LMO framework for OOD setting. Concretely, we suppose we have m training data groups such that D_{train} is still $\{D_{\text{train}}^1, \dots, D_{\text{train}}^m\}$, and we have one separate out-of-domain data group that we do not train on; we have IID validation and test datasets for this out-of-domain data group. Let $L_{\text{val}, \text{OOD}}$ be the validation and test loss on the out-of-domain data group, respectively. Then, the LMO framework can be slightly modified:

$$\underset{\mathbf{p} \in \Delta^{T \times m}}{\text{minimize}} L_{\text{val}, \text{OOD}}^{T+1}(\mathbf{p}) \quad (15)$$

$$\text{s.t. } L_{\text{val}, \text{OOD}}^{t+1}(\mathbf{p}) = c^t + b^t \sigma \left(\sum_{j=1}^m -A_{\text{OOD}, j}^t p_j^t \right) \forall t \in [T], \quad (16)$$

where $A_{\text{OOD}, j}^t \in \mathbb{R}^m$ is now a vector representing how much each training group influences the validation group. There are two changes to the optimization problem: first, the objective is now to minimize the out-of-domain validation loss; second, the mixing law captures the relationship between the validation loss and the mixture proportions over the training data groups. Note that the DML method can still be applied in the OOD setting by directly minimizing $c + b \exp(\sum_{j=1}^m -A_{\text{OOD}, j}^t p_j)$. More importantly, applying Lemma 1 to this optimization problem, we get the update rule $p_j^{t+1} \sim p_j^t \exp(\eta A_{\text{OOD}, j}^t) \forall j \in [m]$. This expression recovers the Skill-It and DoGE OOD update rules, and can be incorporated into AIOLI as demonstrated in Algorithms 3 and 4. These algorithms are identical to AIOLI (Alg 1) and LEARNPARAMS (Alg 2), with the exception of lines 6 and lines 3, 8, and 11 respectively, which reflect that A_{OOD}^t is now a vector rather than an $m \times m$ matrix.

Algorithm 3 AIOLI-OOD

- 1: **Input:** data $D_{\text{train}}, D_{\text{val}}$, model f^1 . Initial steps S_{init} , initial proportions $\mathbf{p}^{\text{init}} \in \Delta^m$. T rounds over $S - S_{\text{init}}$ remaining steps, δ fraction per round for learning parameters, learning rate η , one-hot smoothing factor ε .
- 2: If $S_{\text{init}} \neq 0$, train f^1 on \mathbf{p}^{init} for S_{init} steps.
- 3: Set $p^0 = \text{Unif}(m)$.
- 4: **for** $t = 1, \dots, T$ **do**
- 5: Set $A_{\text{OOD}}^t, f^{t+\delta} \leftarrow \text{LEARNPARAMS-OOD}(D_{\text{train}}, D_{\text{val}}, \delta, f^t, \varepsilon)$ (Alg. 4), and normalize A^t to get \bar{A}^t .
- 6: $p_j^t \propto p_j^{t-1} \exp(\eta \bar{A}_{\text{OOD}, j}^t)$ for all $j \in [m]$.
- 7: Train model $f^{t+\delta}$ with $\frac{S}{T}(1 - \delta)$ steps from mixture p^t over D_{train} . Obtain updated f^{t+1} .

Algorithm 4 LEARNPARAMS-OOD

- 1: **Input:** $D_{\text{train}}, D_{\text{val}}, \delta$, model f^t , number of sweeps k , one-hot smoothing factor ε .
- 2: Split the fraction of a training round δ into K time segments, where $K = mk$.
- 3: Set $\beta = \vec{0} \in \mathbb{R}^m$.
- 4: Define $p^{t,i} = (1 - \varepsilon)\mathbf{1}_i + \varepsilon \text{Unif}(m)$ for $i \in [m]$, and define $P = [p^{t,1}, \dots, p^{t,m}] \in \Delta^{m \times m}$
- 5: Randomly shuffle k instances of each $i \in [m]$ to create an order $\mathcal{I} \in [m]^K$.
- 6: **for** $\tau = 1, \dots, K$ **do**
- 7: Let $j = \mathcal{I}_\tau$. Train model on mixture $p^{t,j}$ of D_{train} for one time segment, obtain $f^{t+\tau\delta/K}$.
- 8: Update $\beta_j \leftarrow \beta_j + L_{\text{val}, \text{OOD}}(f^{t+(\tau-1)\delta/K}) - L_{\text{val}, \text{OOD}}(f^{t+\tau\delta/K})$ with loss difference on OOD validation dataset.
- 9: Update $\beta \leftarrow \frac{\beta}{k}$.
- 10: Set $A_{\text{OOD}}^t = P^{-1}\beta$.
- 11: **Return** $A_{\text{OOD}}^t \in \mathbb{R}^m, f^{t+\delta}$

Mixing law parameterization results. We study a setting where our training data groups are Arxiv, Book, and Github from SlimPajama and our validation data group is StackExchange. Using the same setup as other $m = 3$ settings in Section 4.2 (160M model, 5K steps, sweep over 9 runs), we measure the MSE and R^2 of the log-linear static mixing law, $L_{\text{val}, \text{OOD}}(\mathbf{p}) =$

$c + b \exp\left(\sum_{j=1}^m -A_{\text{OOD},j} p_j\right)$, and of the linear dynamic mixing law, $L_{\text{val}, \text{OOD}}^{t+1}(\mathbf{p}) = c^t + b^t \sum_{j=1}^m -A_{\text{OOD},j}^t p_j^t$. The MSE and R^2 for the log-linear static mixing law are 1.5×10^{-3} and 0.964, respectively. The MSE and R^2 for the linear dynamic mixing law are 1.1×10^{-4} and 0.796. The linear dynamic mixing law fits the true loss-proportion relationship less accurately than the log-linear static law. Nevertheless, both MSEs are low, and the R^2 still suggests that at least 79% of the variability in validation loss can be explained by the mixing law.

AIOLI results. We evaluate stratified sampling, and OOD versions of AIOLI, Skill-It, DoGE, and DML in the unrestricted setting on 3 random seeds. We train on Arxiv, Books, and Github and evaluate on StackExchange. Our results are in Table 26.

We find that all methods, including AIOLI, attain lower test perplexity than the stratified sampling baseline, which both the Skill-It and DoGE papers use as a comparison point for the OOD setting. AIOLI is the only method that achieves this improvement without requiring additional training runs. This improvement over stratified sampling across OOD methods is expected, since stratified sampling can include irrelevant data due to the distribution shift between training and evaluation. On the other hand, stratified sampling is a strong baseline in the in-distribution scenarios studied in the rest of this work.

G Why the method is called AIOLI

An aioli is an emulsion, where individual components remain chemically separate from each other, despite being combined into one mixture. Similarly, our A^t matrix is formed from separate test runs (the $p^{t,1}, \dots, p^{t,m}$ in Section 5), despite being combined into one update for p^t .

Table 18: Average proportions over the entire training trajectory for the unrestricted setting, on one random seed.

Data groups		Method	Average Proportions
arXiv/SE	Grid search		[0.4, 0.6]
	DML		[0.404, 0.596]
	Skill-it		[0.437, 0.563]
	DoReMi		[0.37, 0.63]
	DoGE		[0.624, 0.376]
	AIOLI		[0.507, 0.493]
GitHub/C4	Grid search		[0.3, 0.7]
	DML		[0.46, 0.54]
	Skill-it		[0.583, 0.417]
	DoReMi		[0.858, 0.142]
	DoGE		[0.352, 0.648]
	AIOLI		[0.505, 0.495]
Books/SE	Grid search		[0.3, 0.7]
	DML		[0.381, 0.619]
	Skill-it		[0.316, 0.684]
	DoReMi		[0.286, 0.714]
	DoGE		[0.325, 0.675]
	AIOLI		[0.456, 0.544]
arXiv/Books/SE	Grid search		[0.291, 0.306, 0.403]
	DML		[0.245, 0.277, 0.477]
	Skill-it		[0.292, 0.238, 0.469]
	DoReMi		[0.318, 0.180, 0.502]
	DoGE		[0.592, 0.132, 0.276]
	AIOLI		[0.342, 0.275, 0.383]
CC/GitHib/Wiki	Grid search		[0.291, 0.306, 0.403]
	DML		[0.157, 0.472, 0.371]
	Skill-it		[0.275, 0.3, 0.425]
	DoReMi		[0.101, 0.714, 0.185]
	DoGE		[0.536, 0.220, 0.244]
	AIOLI		[0.342, 0.325, 0.333]
SlimPajama, full (A/B/C4/CC/G/SE/W)	Grid search		[0.202, 0.022, 0.28, 0.038, 0.018, 0.376, 0.064]
	DML		[0.042, 0, 0, 0.579, 0, 0.249, 0.013]
	Skill-it		[0.098, 0.111, 0.204, 0.103, 0.138, 0.266, 0.076]
	DoReMi		[0.08, 0.047, 0.057, 0.11, 0.467, 0.078, 0.157]
	DoGE		[0.056, 0.162, 0.343, 0.28, 0.038, 0.067, 0.051]
	AIOLI		[0.142, 0.143, 0.143, 0.144, 0.140, 0.144, 0.143]

Table 19: Downstream evaluation metrics for various data mixing methods after training on SlimPajama across three random seeds in the unrestricted setting.

Method	Average	ARC-C	ARC-E	BoolQ	HellaSwag	LAMBADA	OpenBookQA	PiQA	WinoGrande
Stratified	0.305	0.176	0.314	0.394	0.261	0.116	0.117	0.563	0.499
AIOLI	0.311	0.172	0.315	0.447	0.264	0.114	0.111	0.559	0.504
GS	0.322	0.176	0.329	0.502	0.262	0.117	0.124	0.568	0.500
DML	0.333	0.181	0.330	0.608	0.261	0.109	0.128	0.554	0.490
Skill-it	0.316	0.182	0.322	0.462	0.261	0.124	0.122	0.559	0.492
DoReMi	0.324	0.177	0.323	0.507	0.264	0.127	0.122	0.574	0.499
DoGE	0.314	0.173	0.313	0.471	0.262	0.116	0.115	0.557	0.504

Table 20: Ablations on AIOLI. The table reports the difference in average test perplexity compared to stratified sampling. Negative values (green) = improvement, and bolded = best performing method for given data setting. A=Arxiv, B=Books, GH=GitHub, SE=StackExchange, W=Wikipedia. AIOLI outperforms ablations in 3 out of 6 settings and attains the lowest test perplexity on average.

Method	A/SE	GH/C4	B/SE	A/B/SE	CC/GH/W	SlimPajama	Average
Stratified	16.532	35.991	47.192	35.114	41.583	26.426	33.806
AIOLI	-0.205	-0.340	-0.439	-0.226	-0.196	-0.240	-0.274
AIOLI-STATIC	-0.065	-0.333	-0.226	-0.117	0.092	-0.330	-0.140
AIOLI-DIAGONAL	-0.182	-0.178	-0.354	-0.246	-0.215	-0.202	-0.230

Table 21: The difference in average test perplexity of AIOLI with varying η step size hyperparameter compared to stratified sampling. Bolded result is the original number reported in Table 2.

Method	A/B	A/B/SE
Stratified	16.532	35.114
AIOLI ($\eta = 0.1$)	-0.110	-0.212
AIOLI ($\eta = 0.2$)	-0.205	-0.221
AIOLI ($\eta = 0.3$)	-0.155	-0.186
AIOLI ($\eta = 0.5$)	-0.166	-0.226

Table 22: The difference in average test perplexity of AIOLI with varying δ/m , the fraction of each round for learning A^t , compared to stratified sampling. Bolded result is the original number reported in Table 2.

Method	A/B	A/B/SE
Stratified	16.532	35.114
AIOLI ($\delta/m = 0.064$)	-0.205	-0.152
AIOLI ($\delta/m = 0.096$)	-0.283	-0.226
AIOLI ($\delta/m = 0.128$)	-0.003	-0.296

Table 23: The difference in average test perplexity of AIOLI with varying γ , the hyperparameter for computing p^t with an exponential moving average, compared to stratified sampling. Bolded result is the original number reported in Table 2.

Method	A/B	A/B/SE
Stratified	16.532	35.114
AIOLI ($\gamma = \text{None}$)	-0.11	-0.226
AIOLI ($\gamma = 0.1$)	-0.205	-0.185
AIOLI ($\gamma = 0.5$)	-0.141	-0.213

Table 24: Comparison of log-linear static and linear dynamic mixing law parameterizations when training a 1.4B model.

Parameterization	Arxiv/SE		Arxiv/Books/SE	
	MSE	R^2	MSE	R^2
Log-linear static	2e-4	0.995	1e-3	0.984
Linear dynamic	7e-5	0.916	2e-4	0.943

Table 25: Difference in average test perplexity compared to stratified sampling in the unrestricted setting for 1.4B models. For AIOLI, we use $\eta = 0.5, \delta/m = 0.096, \gamma = 0.1$ for A/SE and $\eta = 0.1, \delta/m = 0.096, \gamma = 0.5$ for A/B/SE.

Method	A/SE	A/B/SE
Stratified	15.799	34.733
DoGE	0.551	0.922
AIOLI	-0.276	-0.403

Table 26: Out-of-domain data evaluation, in which we mix training data from Arxiv, Books, and Github and evaluate on StackExchange data. The table reports the difference in average test perplexity compared to stratified sampling on the training data groups. For AIOLI, we use $\eta = 0.8, \delta/m = 0.096, \gamma = \text{None}$.

Method	Arxiv/Book/Github → StackExchange	# extra runs
Stratified	39.644	0
GS	-7.244	10
DML	-6.316	10
Skill-It (OOD)	-5.786	3
DoGE (OOD)	-7.626	1
AIOLI (OOD)	-4.028	0