



# Ab initio X-ray absorption modeling of Cu-SAPO-34: Characterization of Cu exchange sites under different conditions



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## ABSTRACT

Copper-exchanged SAPO-34 (Cu-SAPO-34) provides excellent catalytic activity and hydrothermal stability in the selective catalytic reduction (SCR) of  $\text{NO}_x$  by using  $\text{NH}_3$  as a reductant. We find that the 6-membered ring (6MR) site is the most energetically favorable for a  $\text{Cu}^+$  ion while the 8-membered ring (8MR) sites are less favorable by about 0.5 eV with respect to the 6MR site in Cu-SAPO-34. Upon adsorption of molecular species ( $\text{H}_2\text{O}$ ,  $\text{O}$ ,  $\text{OH}$ ,  $\text{O}_2$ ), the energy differences between Cu in the 8MR and 6MR sites decreases and almost disappears. Further, a thermodynamic phase diagram study shows that a  $\text{Cu}^+$  ion bound to a single  $\text{H}_2\text{O}$  molecule is the most stable species at low oxygen potential values while a  $\text{Cu}^{2+}$  ion bound to 2 OH species is more stable when the oxygen chemical potential is sufficiently high. By comparing Cu K-edge XANES between Cu-SSZ-13 and Cu-SAPO-34 with Cu in different oxidation states, we conclude that it is difficult to differentiate the simulated XANES of Cu in these structures at a given oxidation state. By studying the Cu K-edge XANES of several favorable structures in Cu-SAPO-34 in the presence of adspecies, the simulated XANES results capture the real trend of the edge shift with oxidation state and gives new insights into the experimentally determined XANES of Cu-SAPO-34 obtained under standard SCR conditions.

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## 1. Introduction

Copper-exchanged silicoaluminophosphate (Cu-SAPO-34) has drawn extensive attention as a catalyst for selective catalytic reduction (SCR) of  $\text{NO}_x$  with an  $\text{NH}_3$  reductant. Cu-SAPO-34 and copper-exchanged aluminosilicate (Cu-SSZ-13) are structurally analogous chabazite zeolites, which have excellent hydrothermal durability [1–3]. SAPO-34 molecular sieves are synthesized using various structure directing agents (or templates), such as morpholine (MA), triethylamine (TEA), diethylamine (DEA), tetraethylammonium hydroxide (TEAOH) or a mixture of them [4,5]. Recent results have shown that the template affects the Si coordination structures in SAPO-34, and that the Si coordination structures further adjust the acid properties and the Cu species distribution on the Cu-SAPO-34 catalyst [5]. They concluded that with the same Si content, the Cu/TEA and Cu/TEAOH samples contain less  $\text{Cu}^{2+}$  species and more  $\text{CuO}$  species than the Cu/MA and

Cu/DEA samples due to the existence of a Si island. It is reported that Cu-SAPO-34 samples are more insensitive to hydrothermal aging than Cu-SSZ-13 [6]. Furthermore, high-temperature aging is found to improve the catalytic performance of Cu-SAPO-34 due to the migration of Cu species in the fresh sample from the external surface into the micropores [3,4,7,8] and the formation of isolated Cu ions at the exchange sites during the aging process [3]. It is also reported that migration of Cu species from the surface upon activation of Cu-SAPO-34 leads to a several-fold increase in catalytic activity for the selective catalytic reduction (SCR) of  $\text{NO}_x$  with  $\text{NH}_3$  as a reductant [7].

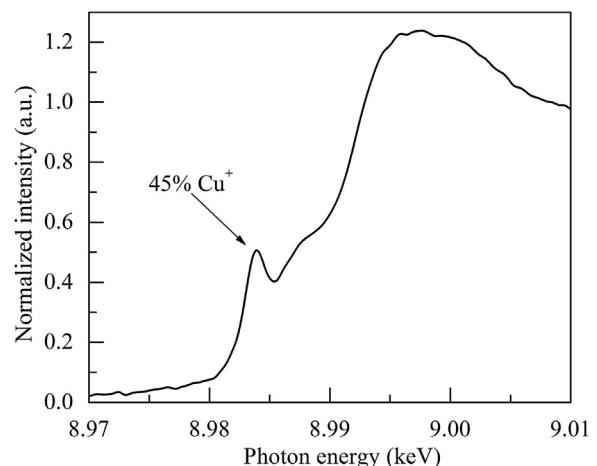
By utilizing different experimental techniques, isolated  $\text{Cu}^{2+}$  species in Cu-SAPO-34 were found to be the active sites of  $\text{NH}_3$ -SCR [3,9–12]. For the relationship between Cu species and Cu loading in Cu-SAPO-34, similar to Cu-SSZ-13 [13], it was reported that the amount of isolated  $\text{Cu}^{2+}$  increased with increasing Cu loading up to 2.0 wt% and only slightly increased with higher Cu loading [9,12]. An increase in the amount of the isolated  $\text{Cu}^{2+}$  caused the improvement of the  $\text{NH}_3$ -SCR activity and a decrease in the amount of  $\text{CuO}$  induced a decline in the  $\text{NH}_3$  oxidation activity [14]. However, the amount of  $\text{Cu}_x\text{O}_y$  clusters continuously increased at higher Cu loading. The presence of  $\text{Cu}_x\text{O}_y$  may promote  $\text{NH}_3$  oxida-

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dation by  $O_2$ , leading to the observed decrease in standard SCR performance at high temperatures [9] where the competing  $NH_3$  oxidation decreases the SCR activity [10]. It was found that the turnover frequency calculated based on the number of isolated  $Cu^{2+}$  ions in samples with varying Cu loading showed a constant value at the same temperature [12]. Based on these results, it was concluded that the isolated  $Cu^{2+}$  species is the active site for the  $NH_3$ -SCR reaction over a Cu-SAPO-34 catalyst. As opposed to Cu-SSZ-13 [15], the Brønsted acid sites in Cu-SAPO-34, act as an  $NH_3$  reservoir rather than being directly involved in the SCR reaction [10,16]. A key step in the proposed mechanism is the formation of surface nitrates and nitrites, which react with  $NH_3$  to form  $NH_4NO_2$  and  $NH_4NO_3$  [16]. By performing the electron paramagnetic resonance (EPR) experiments, Yu et al. also proved that the isolated  $Cu^{2+}$  species are the active sites and the  $NH_4NO_2$  species is the intermediate for  $NH_3$ -SCR over Cu-SAPO-34 [10]. In addition,  $NH_3$ -SCR over Cu-SAPO-34 presents a different mechanism at low and high temperatures [17]. At low temperatures,  $NH_4NO_3$  is a key intermediate while at high temperatures,  $NO_2$  is an important intermediate and  $NH_3$  oxidation is competitive with  $NH_3$ -SCR. They observed a double peak shape with a dip point at the approximately moderate temperature of  $390^\circ C$  [17,18].

Currently, some issues still need to be addressed for CHA-based SCR catalysts such as the unclear effect of reactants on the Cu location and reaction mechanism. Experimental evidence has demonstrated that Cu ions are the active sites for  $NH_3$ -SCR reactions [5,8–11]. However, the location of Cu ions in Cu-SSZ-13 zeolite is still unclear. Understanding the catalytic properties of Cu-SAPO-34 at the atomic and electronic level is important. However, there are few theoretical studies on the properties of Cu-SAPO-34 [19–22]. These studies help us to understand better the locations of Cu ions and molecular adsorption behaviors on the active sites. It has been reported that higher Cu loadings can result in the formation of  $Cu_xO_y$  clusters [9,12]. In the Cu-SAPO-34 zeolite, Cu is located in 8-membered ring and has two facets where it can interact with reactants while Cu located in the 6-membered ring can only interact from one side. It also appears that the Cu species may relocate under reaction conditions. In order to use Cu-SSZ-13 and Cu-SAPO-34 optimally and further develop Cu-based zeolite catalysts, the differences between the Cu-SSZ-13 and Cu-SAPO-34 were discussed in the literature [6,8,17]. In all SCR performance tests,  $NH_3$  oxidation and characterization results consistently indicate that Cu-SAPO-34 is more robust than Cu-SSZ-13 toward hydrothermal aging temperatures higher than  $800^\circ C$  [6,8]. Activity tests indicated that the Cu-SAPO-34 catalyst had a relatively higher  $deNO_x$  performance than the Cu-SSZ-13 catalyst [17]. As a continuation of our work in understanding the properties of Cu-exchanged CHA zeolite catalyst [23,24], the catalytic properties of Cu-SAPO-34 are investigated by using calculations from first-principles. Further, by using *operando* XAS, it has been confirmed that  $Cu^+$  was present under standard SCR reaction conditions over a Cu-SAPO-34 catalyst [25], as shown in Fig. 1. It also demonstrates the importance of performing *operando* experiments and how *in situ* XANES may lead to the incorrect determination of the steady state structure. We will look at several structures and assign the  $Cu^+$  peak by examining Cu K-edge XANES of various  $Cu^+$  species. In this contribution we will study the adsorption of O,  $O_2$ , OH, and  $H_2O$  on a Cu ion in Cu-SAPO-34. We will simulate the corresponding Cu K-edge XANES as well as compare the multiple possible Cu positions through density functional theory (DFT) calculations so as to gain insights into the underlying experimental XANES spectrum measured under standard SCR conditions.

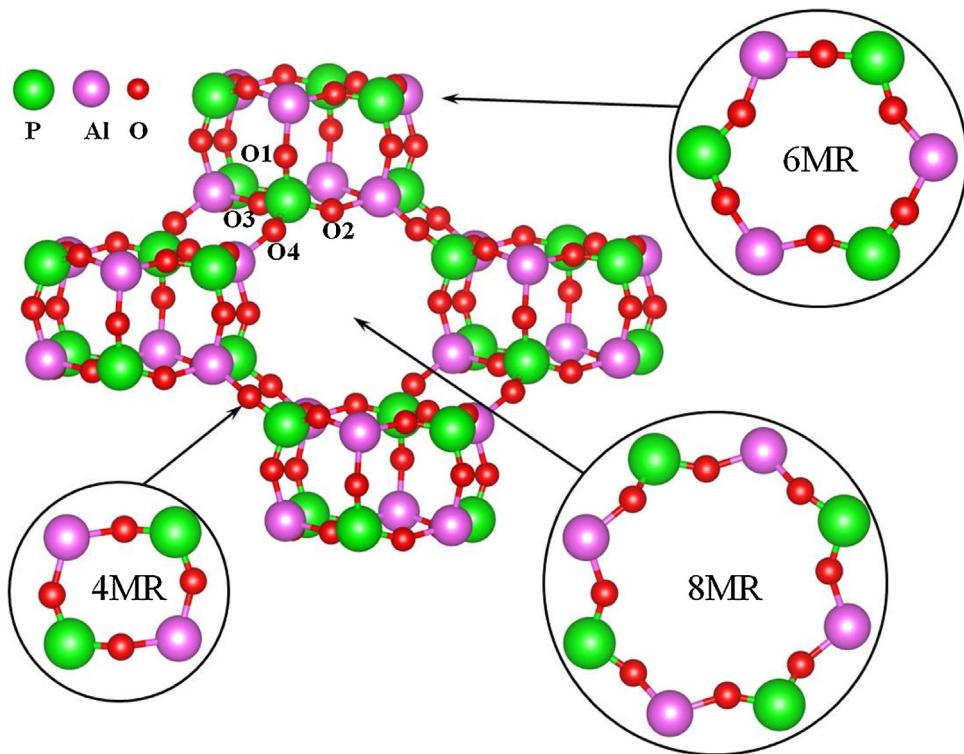


**Fig. 1.** Normalized XANES spectrum of a commercial ~1.75 wt% Cu-SAPO-34 catalyst collected in *operando* reactor (solid line) while feeding a standard SCR mixture (300 ppm NO, 300 ppm  $NH_3$ , 5%  $O_2$ , 5%  $H_2O$ , 5%  $CO_2$  and balance heat  $200^\circ C$ ) [25]. It is identified that the amount of  $Cu^+$  is 45% in the mixture of Cu ions.

## 2. Computational details

DFT calculations were performed with the Vienna *Ab initio* Simulation Package (VASP) code [26,27]. The projector augmented-wave (PAW) [28,29] method and the generalized-gradient approximation (GGA), using the PW91 functional [30], were employed for the treatment of the electron-ion interactions and the exchange-correlation effects, respectively. With its PAW potentials, VASP combines the accuracy of all-electron methods with the computational efficiency of plane-wave approaches. The total energy convergence threshold was set to  $10^{-8}$  eV and the geometries were considered to be fully relaxed when the forces were less than  $0.01$  eV/Å.

As is well known, the Cu-SAPO-34 zeolite belongs to the chabazite structure which is composed of 4-membered rings (4MR), 6-membered rings (6MR), and 8-membered rings (8MR). As shown in Fig. 2, in the pure aluminophosphate ALPO-34, the Al and P atoms on tetrahedral sites (T) obey strictly alternated ordering and there are four nonequivalent O sites, which can be distinguished according to their participation in different rings of the framework. Further information can be found in our previous paper on Cu-SSZ-13 [24]. The calculations in this contribution were performed in a rhombohedral unit cell, consisting of 12 T atoms and 24 O atoms. Monovalent Cu-exchanged SAPO-34 (ZCu) is produced by replacing one Si atom with one P atom and using Cu to compensate the charge deficit.  $Cu^{2+}$ -SAPO-34 (Z<sub>2</sub>Cu) is generated by the replacement of two P atoms with two Si atoms, where the Cu ion presents the oxidation state of 2+. Structures of ALPO-34 and Cu-SAPO-34 were firstly relaxed to obtain the equilibrium volumes. For the pure ALPO-34, an equilibrium rhombohedral volume of  $844.8$  Å<sup>3</sup> was obtained which is consistent with the results of  $829.6$  Å<sup>3</sup> and  $831.9$  Å<sup>3</sup> as reported in the literature [20,31]. With the replacement of a P atom with a Si atom and an exchanged a Cu atom, the calculated equilibrium volume of ZCu is  $847.4$  Å<sup>3</sup> (see Fig. S1 in Supplementary Information), which is slightly larger than that of ALPO-34. However, with the replacement of two P atoms with two Si atom and an exchanged a Cu atom, the equilibrium volume of Z<sub>2</sub>Cu is  $840.8$  Å<sup>3</sup> (see Fig. S1 in Supplementary Information), which is slightly smaller than that of ALPO-34. In this contribution, we start our study on ZCu with the adsorption of adspecies (O, OH and  $H_2O$ ) with different oxidizing power. The 'oxidizing power' refers to the ability to oxidize the  $Cu^+$  ion into a higher oxidation state. In another words, the 'oxidizing power' refers to the ability of the adspecies to obtain electrons from Cu ion. When a neutral



**Fig. 2.** Chabazite structure of ALPO-34, and the compositions of 4MR, 6MR and 8MR are shown. The four nonequivalent O sites are labeled in a P tetrahedral structure. Same distribution of O sites is applied to Al tetrahedral structures. Green, pink and red spheres represent P, Al and O atoms, respectively.

OH (or O) attaches onto the Cu<sup>+</sup> ion in ZCu, an electron transfers from the Cu ion to the OH (or O) species, whereby a [Cu<sup>2+</sup>(OH)<sup>-</sup>]<sup>+</sup> (or [Cu<sup>2+</sup>(O<sup>-</sup>)]<sup>+</sup>) forms. It is reported that the Cu ions can have different oxidation states between +1 and +2 during the SCR process [10].

The Cu binding energy is calculated by

$$E_b = E_{ZCu} - E_{SAPO-34} - E_{\text{bulk}}^{\text{Cu}} \quad (1)$$

where  $E_{ZCu}$ ,  $E_{SAPO-34}$  and  $E_{\text{bulk}}^{\text{Cu}}$  are the total energies of ZCu, ZCu with removing Cu, and bulk Cu, respectively.

For the molecular adsorption calculations, the unit cell of H<sub>2</sub>O adsorbed in the ZCu conformation was fully relaxed using the step by step procedure indicated in Supplementary Information section. Comparing with clean ZCu, the adsorption of H<sub>2</sub>O slightly increases the equilibrium volume to 850.1 Å<sup>3</sup>. The plot of the energy as function of volume can be found in Fig. S1 of Supplementary Information. Other adsorbates were studied in the unit cell using the lattice constants identified for H<sub>2</sub>O adsorbed on ZCu. A 400 eV plane-wave cutoff and a single  $\Gamma$ -point sampling of the Brillouin zone was used for these calculations. Adsorption energies  $E_{\text{ads}}$  are calculated by the following equation:

$$E_{\text{ads}} = E_{\text{tot}} - E_{ZCu} - E_{\text{mol}} \quad (2)$$

where  $E_{\text{tot}}$ ,  $E_{ZCu}$ , and  $E_{\text{mol}}$  are the total energies of ZCu with molecular adsorption, clean ZCu, and the isolated molecules in gas phase, respectively. We note that although the PW91 functional is appropriate for the work done in this contribution, it does not account for the vdW interactions and would not be suitable to determine accurate adsorption energies [32].

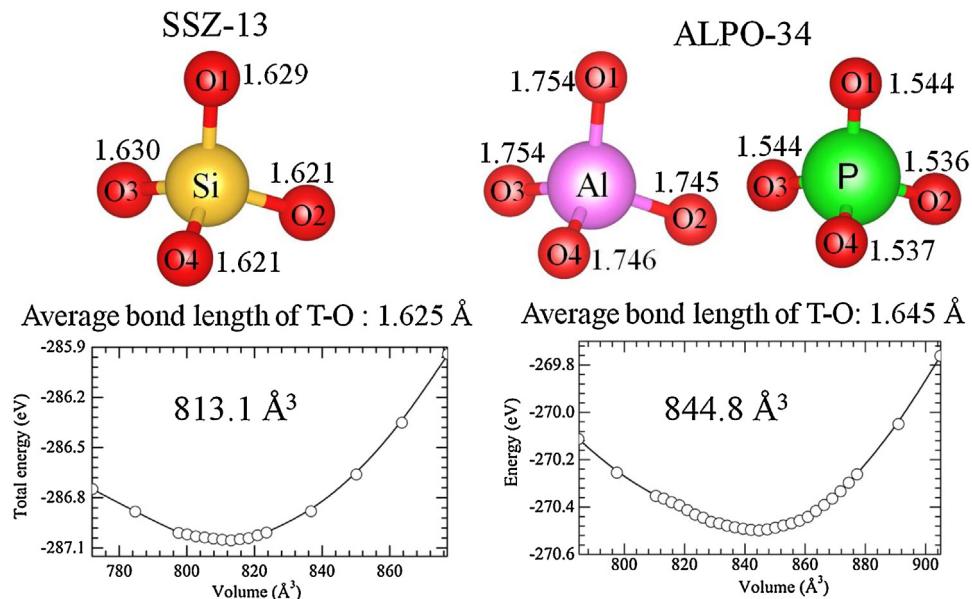
The calculations of the theoretical K-edge XANES of Cu in Cu-SSZ-13 were carried out using the CASTEP code [33]. Here we simulated the X-ray spectra through the calculation of the electron energy loss spectra (EELS) [34]. EELS and XANES are identical in principle. In order to avoid confusion, we use the term of theoretical XANES in this contribution. CASTEP is a density functional theory

code that uses a plane wave basis sets and ultrasoft pseudopotentials. Note that the calculations of the XANES spectra were not affected whether or not one optimized the unit cell within CASTEP (see details in Fig. S2). As a result, the unit cell in CASTEP was fixed to the unit cell as optimized by the VASP program. The GGA-PBE [35] exchange correlation functional was used in these calculations for the optimization of the atomic coordinates using the fixed unit cell geometry and for the simulation of the XANES. We remark that although the PBE, RPBE, or PBEsol functionals are recommended when a GGA functional is required for such calculations, we found that the results of theoretical K-edge XANES of Cu in ZCu with Cu in 6MR site are independent of such exchange-correlation functionals [24]. To calculate the XANES spectra, ultrasoft pseudopotentials were generated on the fly [34], and one core electron was excited from a relevant core level when performing core-hole calculations. It is demonstrated that the core-hole effect is significant on the results of core level spectra [36]. Therefore, we took into account the core-hole effect in our calculations. All core-hole calculations were carried out using supercells sufficiently large so as to eliminate the interactions between periodic images. Previous work recommends a distance between images of 8–10 Å [34,37]. The dimensions of the rhombohedral unit cell used in our calculations satisfy this requirement. Energy cutoffs of 550 eV and a K-point grid of (5 × 5 × 5) were used in the calculations of the XANES. The energy broadening with an instrumental smearing, using the Gaussian method, of 0.6 eV and lifetime broadening of Cu with a value of 1.55 eV were applied [34].

### 3. Results and discussions

#### 3.1. Pure ALPO-34 and clean SSZ-13

Both SSZ-13 and ALPO-34 belong to the chabazite (CHA) structure. Their difference lies in the tetrahedral sites occupied by a Si atom for SSZ-13 whereas Al and P atoms in ALPO-34 occupy these sites. It is reported that this structural difference causes the dif-



**Fig. 3.** The tetrahedral structure in pure SSZ-13 and ALPO-34 are shown as well as plots of total energy as function of volume. The bond lengths of T–O bond are presented.

ferent mechanisms for dealumination of SSZ-13 and desilication of SAPO-34 [38]. Regarding their equilibrium volumes, which are  $813.1\text{ }\text{\AA}^3$  for SSZ-13 and  $844.8\text{ }\text{\AA}^3$  for ALPO-34, ALPO-34 is larger than SSZ-13. The chabazite volume is determined by the tetrahedral structure. **Fig. 3** shows the tetrahedral structures of Si, Al and P atoms in SSZ-13 and ALPO-34, respectively. It is found that the bond length of Si–O is longer than P–O while shorter than Al–O. The average T–O bond lengths are  $1.625\text{ }\text{\AA}$  for SSZ-13 and  $1.645\text{ }\text{\AA}$  for ALPO-34, which results in the equilibrium volume of ALPO-34 being larger than that of SSZ-13. When one replaces Si with P in ALPO-34, the equilibrium volume will also vary and thus needs to be taken into account in our calculations. As mentioned before, the resulting equilibrium volumes that were used when one replaces one P atom with one Si atom or two P atoms with two Si atoms are given in Supplementary Information.

### 3.2. Locations of Cu ion in clean ZCu

Three possible positions of Cu in ZCu are considered in this contribution. One is located in the center of the 6MR and the other two are in the 8MR sites distinguished by forming bonds with different O atoms. We note that there is not enough room for Cu in the 4MR site, and this option was not investigated in this contribution. As shown in **Fig. 4**, for the two positions of Cu in the 8MR sites, Cu atoms are bonded with the O1 and O4 atoms or the O2 and O4 atoms of the zeolite framework, and the resulting structures are called 8MR\_O14 and 8MR\_O24, respectively.

As shown in **Fig. 4**, it was found that Cu in the 6MR site has a 3-fold coordination to O atoms. For the 6MR site, Cu is bonded to an activated O3 atom to form the smallest Cu–O bond length of  $1.944\text{ }\text{\AA}$ , and two non-activated O3 atoms with longer Cu–O bond lengths of  $2.008$  and  $2.306\text{ }\text{\AA}$ , respectively. This finding is consistent with other computational results in the literature [19]. Here we denote an activated O atom as one that is bonded to an adjacent Si atom. When Cu is in the 8MR\_O14 site it is bonded with the activated O1 and O4 atoms. The Cu ion is also close to a non-activated O2 atom with a distance of  $2.353\text{ }\text{\AA}$ . We used the differential charge density to investigate if the Cu ion and O2 atom form a bond. As shown in Fig. S3 in Supplementary Information, there is no sharing of electrons between the Cu ion and O2 atom. It is thus concluded that Cu in 8MR\_O14 site has a coordination number of two. The

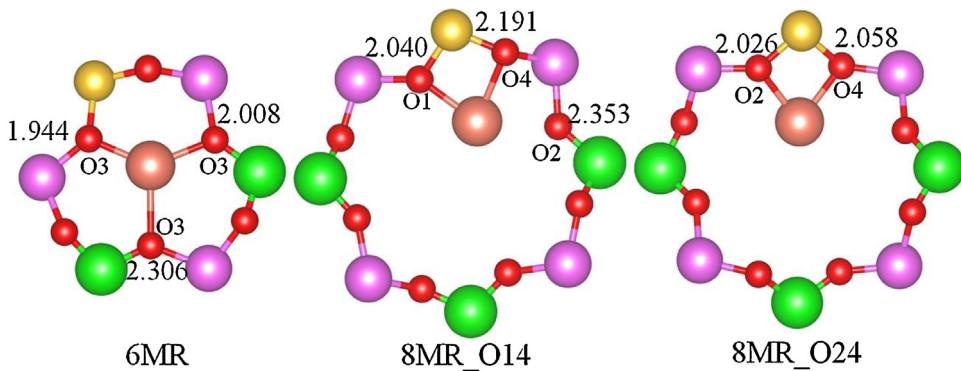
Cu 8MR\_O24 site is 2-fold coordinated with activated O2 and O4 atoms, where the Cu–O bond lengths are  $2.026$  and  $2.058\text{ }\text{\AA}$ . We therefore conclude that the coordination number of Cu in the 6MR site is 3 while that of the Cu in the two 8MR sites is 2.

Comparing the properties of Cu in different positions, it was found that the 6MR site is the most thermodynamically favorable. The configurations of Cu in the 8MR\_O14 and 8MR\_O24 sites are slightly less favorable with total energy differences of  $0.50$  and  $0.52\text{ eV}$ , respectively, with respect to that of Cu in 6MR site. Based on the results of the Cu binding energy, Cu in the 6MR site has a stronger electrostatic interaction with the CHA framework. The Cu binding energies are  $-0.88$ ,  $-0.38$  and  $-0.32\text{ eV}$  for Cu in the 6MR, 8MR\_O14 and 8MR\_O24 sites, respectively. We conclude that the 6MR site is the primary site for Cu to occupy while the 8MR sites are the second most favorable sites where Cu ions can be located. These results support the experimental results that there are two different types of Cu present in the SAPO-34 zeolite [39]. Specifically, Cu ions primarily occupy sites in the 6MR at low Cu loading, while at high Cu loading some Cu ions are located in the large CHA cages and close to the 8MR sites.

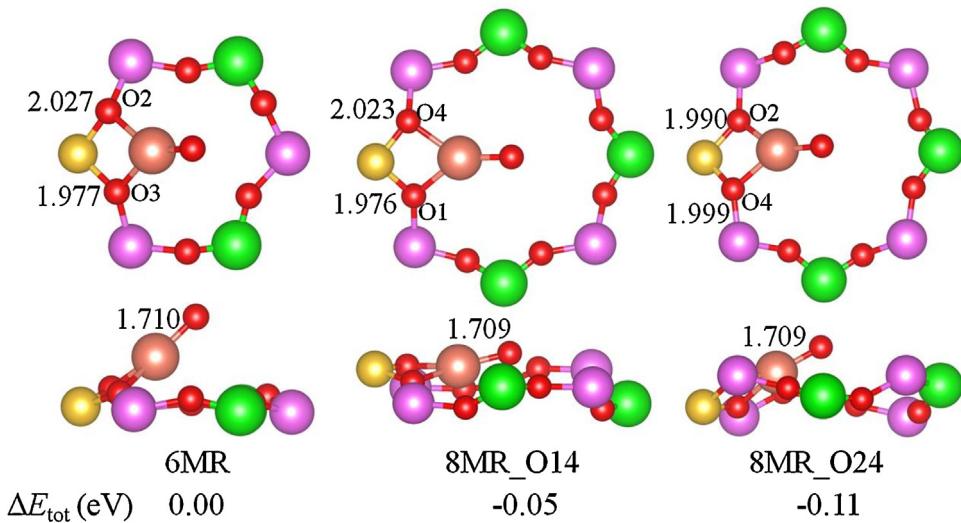
### 3.3. Molecular adsorption on ZCu

The most common and abundant reactive gases under SCR conditions are  $\text{O}_2$  and  $\text{H}_2\text{O}$ , and understanding the interactions of Cu centers with these gases and their decomposition products is central to understanding the nature, oxidation state, and redox activity of these materials. We take a general approach and consider the adsorption of various species of  $\text{H}_2\text{O}$ ,  $\text{OH}$ ,  $\text{O}$ ,  $\text{O}_2$  and  $2\text{OH}$  to a Cu center.

An  $\text{O}^-$  species is the simplest possible adsorbate intermediate under SCR oxidative conditions, and **Fig. 5** shows the relaxed structure for  $[\text{Cu}^{2+}(\text{O}^-)]^+$  in the 6MR, 8MR\_O14 and 8MR\_O24 sites. The  $\text{O}^-$  species draws the Cu ion out of the plane of the 6MR into a location above the 6MR. With the formation of  $[\text{Cu}^{2+}(\text{O}^-)]^+$ , the  $\text{Cu}^{2+}$  is coordinated to the two activated O atoms and the adsorbed  $\text{O}^-$ , which results in a net 3-fold coordination of  $\text{Cu}^{2+}$  in different locations (6MR and 8MR sites). The Cu–O bond length of Cu formed with lattice O is about  $2.0\text{ }\text{\AA}$  while that of Cu formed with adsorbed  $\text{O}^-$  is about  $1.7\text{ }\text{\AA}$ . As mentioned previously, the configuration of Cu in the 6MR is the most favorable for clean ZCu. However, as



**Fig. 4.** Local structures of three possible Cu positions (6MR, 8MR\_O14 and 8MR\_O24) in ZCu. Cu—O distances with unit of Å are indicated in each panel. The atoms represented are the same as previous figures. The different O atoms are labeled as presented in Fig. 2. Please note that these shown structures are portion of the periodic structure of the rhombohedral unit cell.



**Fig. 5.** Local structure of atomic O adsorbed ZCu with Cu in the 6MR, 8MR\_O14, and 8MR\_O24 sites. The color-coding for the spheres and the given distances have the same meaning as previous figures. The total energy differences with respect to the total energy of Cu in 6MR site ( $\Delta E_{\text{tot}}$ ) are given at the bottom of the figure.

**Table 1**

The calculated adsorption energies of  $\text{H}_2\text{O}$ ,  $\text{OH}$ ,  $\text{O}$ ,  $\text{O}_2$  and 2  $\text{OH}$  on Cu in 6MR, 8MR\_O14 and 8MR\_O24 sites according to Eq. 2. The values of adsorption energy for 2 OH adsorbed ZCu is calculated by following the  $\text{ZCuOH} + \text{OH} \rightarrow \text{ZCu}(\text{OH})_2$  process.

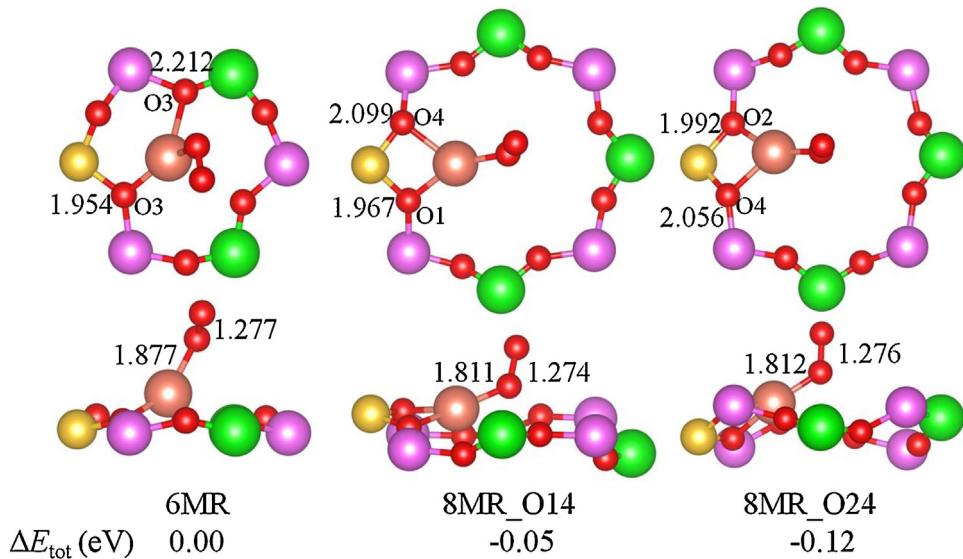
$E_{\text{ads}}$ (eV)	6MR	8MR_O14	8MR_O24
O	0.45	-0.08	-0.21
$\text{O}_2$	-0.55	-1.09	-1.22
$\text{H}_2\text{O}$	-0.92	-1.64	-1.56
OH	-2.67	-3.17	-3.31
2 OH	-2.31	-1.69	-1.61

shown in Fig. 5, it is found that configurations of Cu in the 8MR sites become more favorable under O adsorption, although the energy difference is very small. This means that the thermodynamic stability of molecular species adsorbed in the ZCu conformation is nearly identical for Cu in different sites with the formation of a  $[\text{Cu}^{2+}(\text{O}^-)]^+$  complex. As shown in Table 1, the calculated adsorption energies of O with respect to a  $\text{O}_2$  molecule are 0.45, -0.08 and -0.21 eV for Cu in 6MR, 8MR\_O14 and 8MR\_O24 sites, respectively. The positive value of the adsorption energy of O on Cu in the 6MR site indicates that the adsorption of O is unfavorable. It also implies that the  $\text{O}_2$  molecule does not prefer decomposing to two O atoms on Cu in the 6MR site. We next consider the molecular adsorption of an  $\text{O}_2$  molecule at the Cu sites.

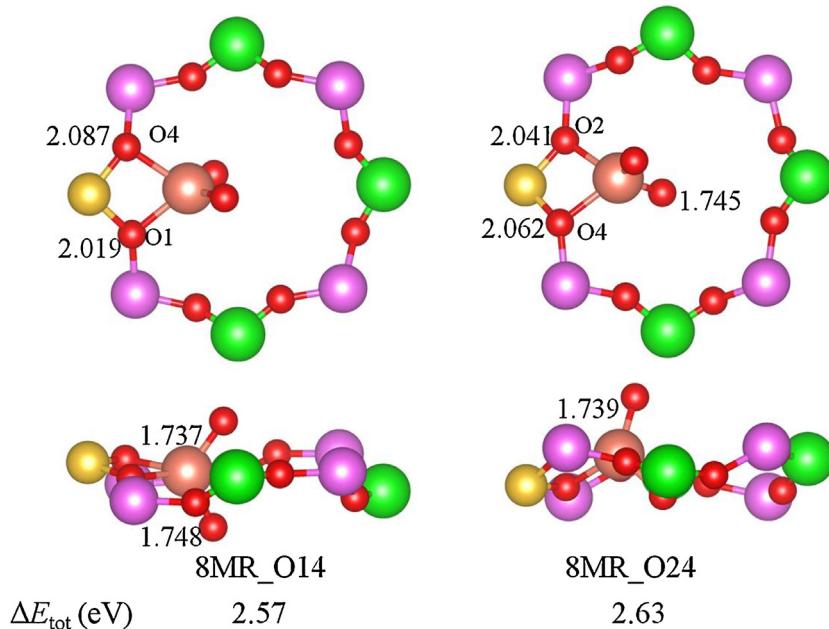
Previous computational results [40] have suggested that a side-on and an end-on configuration of  $\text{O}_2$  with a triplet ground state to be favorable. It is reported that the side-on configuration is more favorable for  $\text{O}_2$  adsorbed on Cu-SSZ-13 [40]. We studied both of these configurations on Cu in the three different sites and found that the end-on configuration is more favorable for  $\text{O}_2$  adsorbed on ZCu. Initial structures of the side-on configuration automatically became an end-on configuration during the optimization. The optimized structures of end-on configuration for  $\text{O}_2$  adsorption are shown in Fig. 6.

The  $\text{O}_2$  molecule draws Cu somewhat less far out of the 6MR than does the O species. Upon the adsorption of an  $\text{O}_2$  molecule, the Cu ion coordinates with two lattice O atoms and one O atom of the  $\text{O}_2$  molecule. The adsorption of the  $\text{O}_2$  molecule in the ZCu conformation also decreases the total energy difference between the 6MR and 8MR sites. Specifically, the total energy differences with respect to Cu in the 6MR are -0.05 and -0.12 eV for Cu in 8MR\_O14 and 8MR\_O24 sites, respectively. As listed in Table 1, the adsorption energies of  $\text{O}_2$  on Cu in the 6MR, 8MR\_O14 and 8MR\_O24 sites are -0.55, -1.09 and -1.22 eV, respectively.

We investigated how an  $\text{O}_2$  molecule could decompose, by examining the adsorption of 2 O atoms on a single  $\text{Cu}^{2+}$  ion. Because there is only one side for the molecule to access in the 6MR, we put 2 O atoms as far as possible from each other. The distance between the 2 O atoms was set to about 2.4 Å in the initial structure. How-



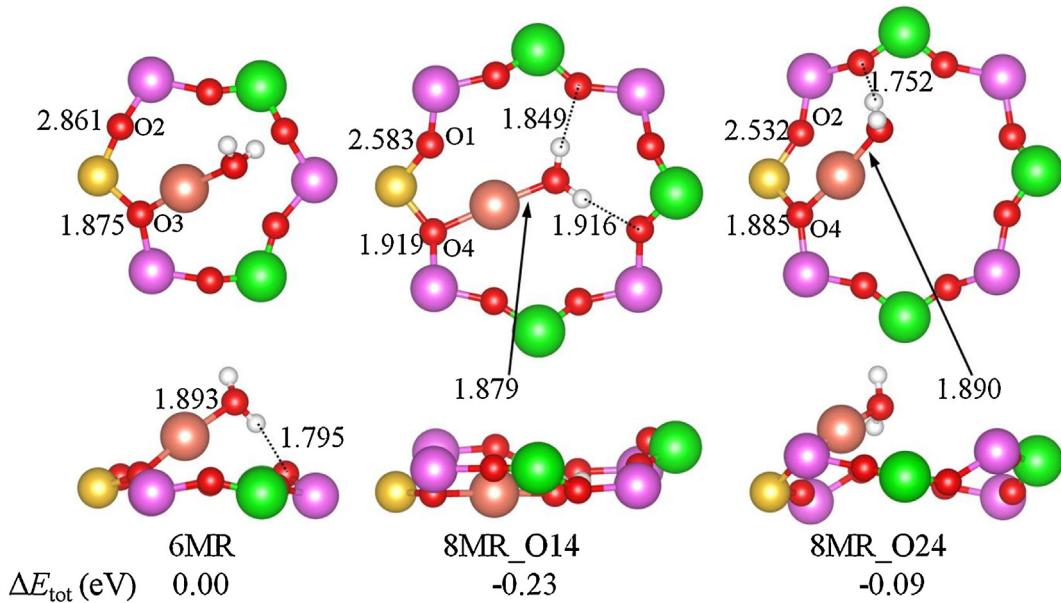
**Fig. 6.** Local structure of  $O_2$  molecule adsorbed ZCu with Cu in the 6MR, 8MR\_O14, and 8MR\_O24 sites. The color coding for the spheres and the given distances have the same meaning as previous figures. The total energy differences with respect to the total energy of Cu in the 6MR site ( $\Delta E_{\text{tot}}$ ) are given at the bottom of the figure.



**Fig. 7.** Local structure of 2 O atoms adsorbed on a  $Cu^+$  ion in the 8MR\_O14 and 8MR\_O24 sites. The color-coding for the spheres and the given distances have the same meaning as in the previous figures.  $\Delta E_{\text{tot}}$  presents the total energy difference with respect to the corresponding configurations with an adsorbed  $O_2$  molecule.

ever, after optimization, an  $O_2$  molecule is formed on the Cu ion in the 6MR. This again confirms that an  $O_2$  molecule will not dissociate when Cu is in a 6MR site. Different from the 6MR site, the 8MR has two sides that a molecule can access. As a result, the 2 O atoms can separately adsorb on both sides of the 8MR site. The optimized structures for Cu in 8MR\_O14 and 8MR\_O24 sites are shown in Fig. 7. Similar to the adsorption of an O atom and an  $O_2$  molecule, the Cu ion approaches two lattice O atoms upon the adsorption of two extra-lattice oxygen atoms. As a result, the Cu ion becomes four-fold coordinated by oxygen. As presented in Fig. 7, the total energy differences with respect to the corresponding  $O_2$  molecule adsorbed on a  $Cu^+$  ion in the 8MR sites are 2.57 and 2.63 eV. These large positive values demonstrate that the decomposition of  $O_2$  on a  $Cu^+$  ion in either of the 8MR sites is thermodynamically unfavorable.

The interaction of  $H_2O$  with the Cu-SSZ-13 zeolite framework was also investigated theoretically for a variety of configurations [24,40]. Fig. 8 displays the optimized structure of  $H_2O$  adsorbed on Cu in different locations. For all considered Cu positions, Cu approaches one activated lattice O atom with a Cu–O bond length of 1.875, 1.919 and 1.885 Å for Cu in 6MR, 8MR\_O14, and 8MR\_O24 sites, respectively. Although  $H_2O$  draws Cu out of the 6MR plane, the H atom of  $H_2O$  tends to interact with a lattice O atom, where the distance between the H and O atoms is 1.795 Å. Similarly, when Cu is in one of the 8MR sites, the H atoms of  $H_2O$  interact with lattice O atoms, as shown in Fig. 8. The Cu coordination is 2-fold upon the adsorption of  $H_2O$ . The adsorption energies of  $H_2O$  on Cu in the 6MR, 8MR\_O14, and 8MR\_O24 sites are -0.92, -1.64 and -1.56 eV, respectively. It is found that  $H_2O$  has a stronger interaction with ZCu than the O atom or the  $O_2$  molecule. Comparing



**Fig. 8.** Local structure of an  $\text{H}_2\text{O}$  molecule adsorbed on a  $\text{Cu}^+$  ion in the 6MR, 8MR.O14, and 8MR.O24 sites. The color-coding for the spheres and the given distances have the same meaning as previous figures. The total energy differences with respect to the total energy of Cu in the 6MR site ( $\Delta E_{\text{tot}}$ ) are presented at the bottom of the figure.

the total energies of the three configurations, we find that  $\text{H}_2\text{O}$  stabilizes the 8MR.O14 configuration as compared to the 6MR sites with an energy difference of  $-0.23$  eV with respect to the 6MR configuration.

Due to the deprotonation of  $\text{H}_2\text{O}$ , the OH species can also be adsorbed on a Cu site. As shown in Table 1, the adsorption energies of OH on Cu in the 6MR, 8MR.O14 and 8MR.O24 sites are  $-2.67$ ,  $-3.17$  and  $-3.31$  eV, respectively. Note that the adsorption energy of OH was calculated by using the reference of neutral OH in the gas phase. OH presents a strong interaction with Cu because of its high activity. Fig. 9a shows the relaxed structure for the OH species adsorbed on Cu in the 6MR, 8MR.O14 and 8MR.O24 sites. Similar to the adsorption of the O atom, the adsorption of OH draws Cu out of the plane of the 6MR into a location above the 6MR. Upon OH adsorption, Cu is coordinated to the two activated O atoms and to the O of the OH adsorbate, which results in a net 3-fold coordination of Cu in each location. The Cu–O bond lengths of Cu with the lattice O atoms are about  $2.0\text{ \AA}$  while the bond distance between the Cu formed with extra-framework O atom of the OH adsorbate is about  $1.8\text{ \AA}$ . As for the total energy difference between these configurations, we find that the thermodynamic stability between the 8MR sites and the 6MR sites of the ZCu conformation in the presence of an OH adsorbate to be nearly identical.

We also considered the adsorption of a second OH species on such Cu sites, for which the relaxed structures are shown in Fig. 9b. The calculation for the adsorption of the second OH molecule follows the  $\text{ZCuOH} + \text{OH} \rightarrow \text{ZCu}(\text{OH})_2$  reaction pathway. The calculated adsorption energies are listed in Table 1. For Cu in the 6MR site, Cu is 4-fold coordinated, with two essentially equivalent short bonds to the OH molecule and two longer bonds to the lattice O. The adsorption energy of the second OH molecule is  $-2.31$  eV for Cu in the 6MR site, which is slightly smaller than  $-2.67$  eV for the first OH molecule. However, Cu in the 8MR sites exhibits a different behavior upon addition of a second OH. As shown in Fig. 9, it is found that the second OH molecule increases the distance between Cu and the O4 oxygen atom from  $2.002$  to  $2.622\text{ \AA}$  for the 8MR.O14 site and from  $1.991$  to  $2.518$  for the 8MR.O24 site, breaking the Cu–O4 bond. This results in a 3-fold coordinated Cu atom with two short bonds to the OH molecule and a longer bond length to the lattice O. The adsorption energies of the second OH molecule are

$-1.69$  and  $-1.61$  eV for Cu in 8MR.O14 and 8MR.O24 sites, respectively, which are just half of values for the adsorption energies of the first OH species ( $-3.17$  and  $-3.31$  eV). We can also examine the average adsorption energies of OH for 2 OH molecules adsorbed in the ZCu conformation using the following Eqs:

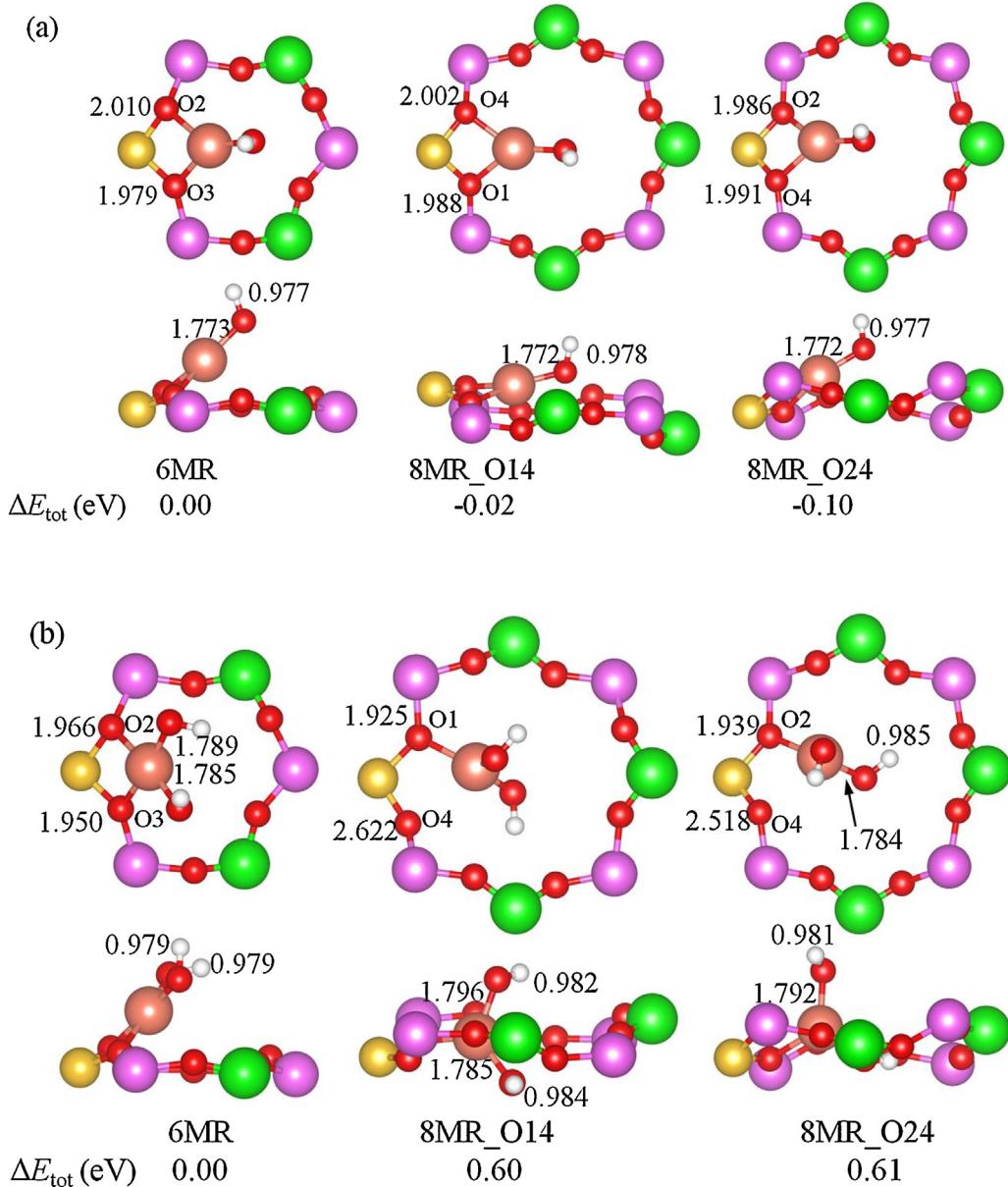
$$E_{\text{ads}}^{\text{OH}} = (E_{\text{tot}} - E_{\text{ZCu}} - 2E_{\text{OH}})/2 \quad (3)$$

where  $E_{\text{tot}}$ ,  $E_{\text{ZCu}}$ , and  $E_{\text{OH}}$  are the total energies of ZCu upon the adsorption of 2 OH species, the clean ZCu conformation, and the isolated OH species in the gas phase, respectively. The calculated average adsorption energies are  $-2.49$ ,  $-2.43$  and  $-2.46$  eV for Cu in the 6MR, 8MR.O14 and 8MR.O24 sites, respectively. It is concluded that, upon the adsorption of 2 OH species, the average adsorption energy of OH is close to that found for the adsorption of one OH species on Cu in the 6MR site ( $-2.67$  eV). A similar comparison reveals that the interaction between OH and Cu is weaker for the adsorption of two OH species than for the adsorption of one OH species when Cu is in one of the 8MR sites ( $-3.17$  and  $-3.31$  eV for 8MR.O14 and 8MR.O24, respectively). In addition, the adsorption of the second OH makes the 6MR site more energetically favorable, as presented in Fig. 9b since this results in a positive value of total energy difference with respect to that of Cu in 6MR site ( $0.60$  and  $0.61$  eV for the 8MR.O14 and 8MR.O24, respectively).

### 3.4. Phase diagram

The first principles phase diagram approach provides a connection between the DFT results and the relative equilibrium stabilities of the  $\text{ZCuO}_x\text{H}_y$  species considered above [40]. A brief summary on how to construct the phase diagram is described here and detailed information can be found in the paper of McEwen et al. [40]. The free energy of a ZCu with adsorbate, which is related to the adsorption energies, is written using the chemical potentials of oxygen and hydrogen:

$$\Delta G = G(\text{ZCuO}_x\text{H}_y) - G(\text{ZCu}) - x_0\mu_{\text{O}} - y_{\text{H}}\mu_{\text{H}} \quad (4)$$



**Fig. 9.** Local structure of (a) OH and (b) 2 OH adsorbed in a ZCu conformation with Cu in the 6MR, 8MR\_O14, and 8MR\_O24 sites. The color coding for the spheres and the given distances have the same meaning as previous figures. The total energy differences with respect to the total energy of Cu in the 6MR site ( $\Delta E_{\text{tot}}$ ) are presented at the bottom of the figure.

The free energies of the zeolite species were approximated with the DFT energies. We take  $\text{H}_2\text{O}$  as the hydrogen reference to relate  $\mu_{\text{H}}$  and  $\mu_{\text{O}}$ :

$$\mu_{\text{H}} = \frac{1}{2} (\mu_{\text{H}_2\text{O}} - \mu_{\text{O}})$$

Then Eq. (4) can be written as:

$$\Delta G = E(\text{ZCuO}_x\text{H}_y) - E(\text{ZCu}) - (x_0 - \frac{y_{\text{H}}}{2})\mu_{\text{O}} - \frac{y_{\text{H}}}{2}\mu_{\text{H}_2\text{O}} \quad (6)$$

We define the relative chemical potential of oxygen and water with respect to the energies of isolated  $\text{O}_2$  and  $\text{H}_2\text{O}$  molecules ( $E_{\text{O}_2}$  and  $E_{\text{H}_2\text{O}}$ ) as reference zero:

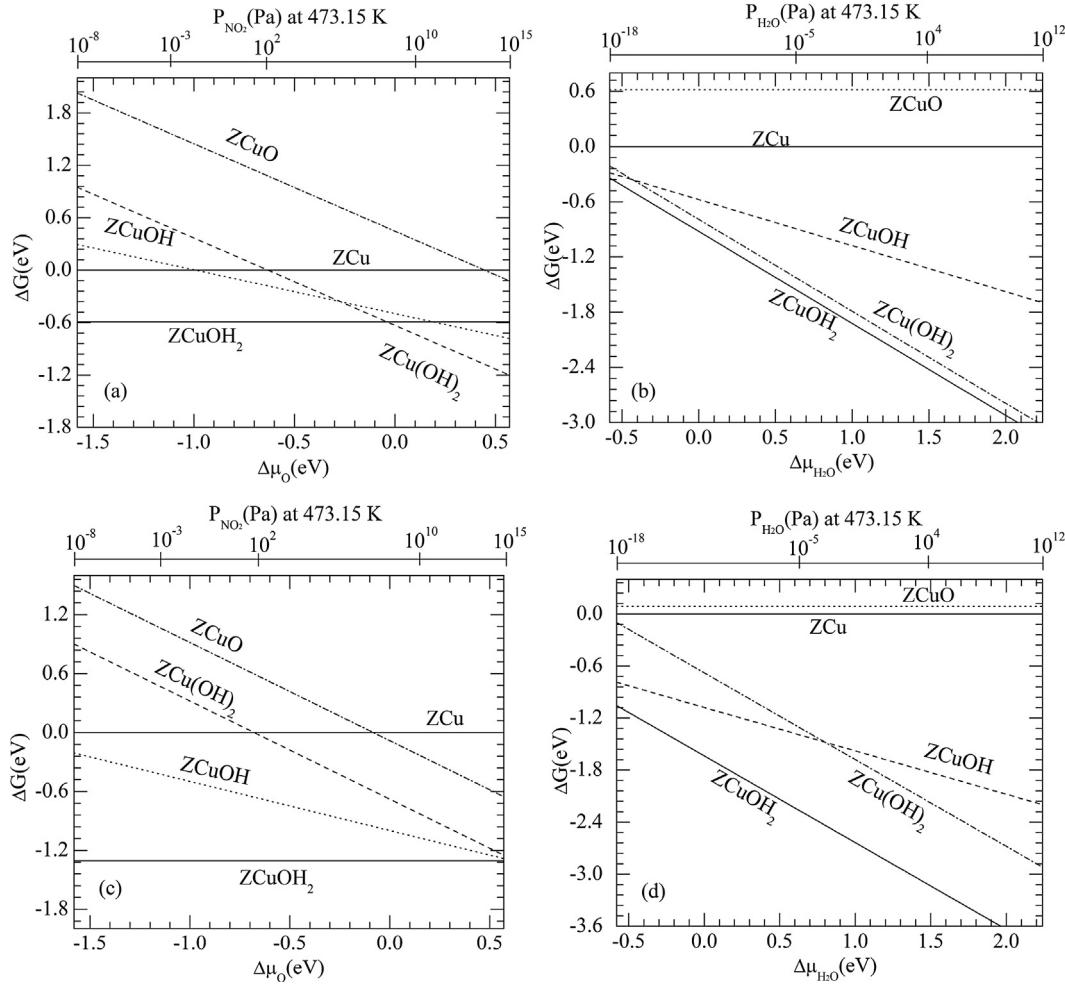
$$\Delta\mu_{\text{O}} = \mu_{\text{O}} - \frac{E_{\text{O}_2}}{2} \text{ and } \Delta\mu_{\text{H}_2\text{O}} = \mu_{\text{H}_2\text{O}} - E_{\text{H}_2\text{O}} \quad (7)$$

As a result, Eq. (6) can be recast as a function of the relative chemical potential of oxygen and water:

$$\Delta G = E(\text{ZCuO}_x\text{H}_y) - E(\text{ZCu}) - \frac{1}{2} \left( x_0 - \frac{y_{\text{H}}}{2} \right) E_{\text{O}_2} - \frac{1}{2} E_{\text{H}_2\text{O}} - \left( x_0 - \frac{y_{\text{H}}}{2} \right) \Delta\mu_{\text{O}} - \frac{y_{\text{H}}}{2} \Delta\mu_{\text{H}_2\text{O}} \quad (8)$$

Other choices of chemical potential reference are possible. The chemical potentials can be related to temperature and gas pressure by using the ideal gas law. Detailed information can be found in the literature and its Supplementary Information [40].

Fig. 10a shows the computed relative free energies of Cu in a 6MR site as a function of the oxygen chemical potential. As described in Ref. [40], in order to understand the SCR reaction environment, the  $\text{NO} \leftrightarrow \text{NO}_2$  equilibrium over the catalyst surface can be assumed to obtain the chemical potential of oxygen, namely,



**Fig. 10.** The phase diagram comparing the relative stabilities of the configurations given in Figs. 4, 5, 8 and 9: phase diagram as a function of  $\Delta \mu_O$  at  $p^{H_2O} = 0.1$  bar and  $T = 473.15$  K with Cu in (a) 6MR site and (c) 8MR.O14 site, phase diagram as a function of  $\Delta \mu_{H_2O}$  at  $p^{O_2} = 0.05$  bar and  $T = 473.15$  K with Cu in (b) 6MR site and (d) 8MR.O14 site. The corresponding pressure scales are given in the figure. The left limit of the diagram corresponds to low  $NO_2$  ( $H_2O$ ) pressures or relatively reducing conditions.

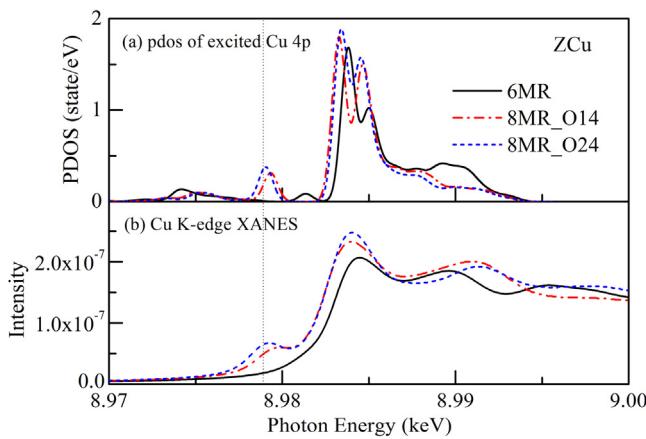
$\mu_O = \mu_{NO_2} - \mu_{NO}$ . Therefore,  $\mu_O$  can be mapped to  $p^{NO_2}$  at a fixed  $p^{NO}O = 300$  ppm at 473.15 K.  $\mu_{H_2O}$  is determined at the condition of  $p^{H_2O}$  (473.15 K) = 0.1 bar. The calculated chemical potentials of  $H_2$ ,  $O_2$ ,  $H_2O$ ,  $NO$  and  $NO_2$  at different temperatures, which were used to obtain the chemical potential at any pressure, are listed in Table S1. The most stable species are at the bottom of the diagram and the less stable ones at increasingly higher free energy. For the location of 6MR site, a  $Cu^+$  bound to a single  $H_2O$  is found to be the most stable species for low chemical potential values. With increasing O chemical potential, and increasing oxidizing conditions the more oxidized Cu species ( $ZCuO$ ,  $ZCuOH$  and  $ZCu(OH)_2$ ) drop in free energy relative the reduced species ( $ZCu$  and  $ZCuOH_2$ ). Further increasing the chemical potential of oxygen,  $ZCu(OH)_2$  becomes the most stable adsorption state. However, this transition occurs at much higher pressures when examining the phase diagram for Cu in the 8 membered ring as shown in Fig. 10c. This phase diagram for Cu-SAPO-34 is similar to that of Cu-SSZ-13 [40]. Fig. 10b shows the computed relative free energies of Cu sites as a function of water chemical potential at a fixed oxygen chemical potential. Here  $ZCu(OH)_2$  is slightly less stable than  $ZCuOH_2$ , and  $ZCuOH_2$  is the most stable species in the potential range studied. This result is similar with the Cu-SSZ-13 study, where the  $ZCuOH_2$  was also found to be the most stable species within the chemical potential range studied [40]. However, as can be seen in Fig. 10d, when Cu is in the 8MR.O14 site,  $ZCuOH_2$  was always found to be the most stable species within the chemical potential range studied whatever the oxygen chem-

ical potential and water chemical potential. Note that the phase diagram for Cu in a 8MR.O24 is similar with Cu in a 8MRO\_14 and detailed information can be found in Fig. S4 in Supplementary Information. As shown in Fig. 1, the standard SCR conditions are 300 ppm NO, 300 ppm NH<sub>3</sub>, 5% O<sub>2</sub>, 5% H<sub>2</sub>O, 5% CO<sub>2</sub> and balance heat 200 °C (473.15 K). Similarly with the discussion in the literature [40],  $\Delta \mu_O$  corresponds approximately to -0.55 eV in Fig. 10a and c at  $p^{NO_2}$  (473.15 K) = 1000 pm and  $p^{NO} = 300$  ppm. Under this condition of O chemical potential, the most stable species is  $ZCuOH_2$ .

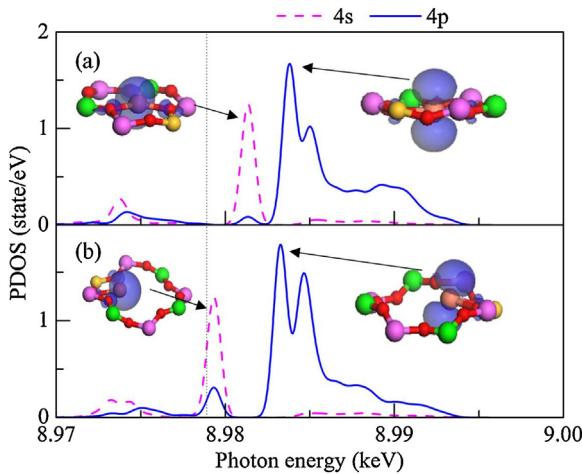
### 3.5. Computational Cu K-edge XANES

#### 3.5.1. Analysis of the XANES spectra of a clean Cu ion in Cu-SAPO-34

A XANES spectrum can provide information about the chemical environment of a species and can be used as a fingerprint for identification of a species. Differences in the Cu K-edge XANES spectra can be interpreted by comparing them to the excited 4p PDOS of Cu within the empty band region, as shown in Fig. 11. The 1s–4s and 1s–3d transitions are forbidden from the dipole selection rules and are not included in Fig. 11a. The 4p PDOS energy has been shifted according to the Fermi level of Cu to allow for direct comparison between the XANES spectra and the PDOS. For the three Cu locations (6MR, 8MR.O14 and 8MR.O24), as shown in Fig. 11a, there is an energy gap in the 4p states between the small peak around 8980 eV and the main peak around 8984 eV. We observe differences



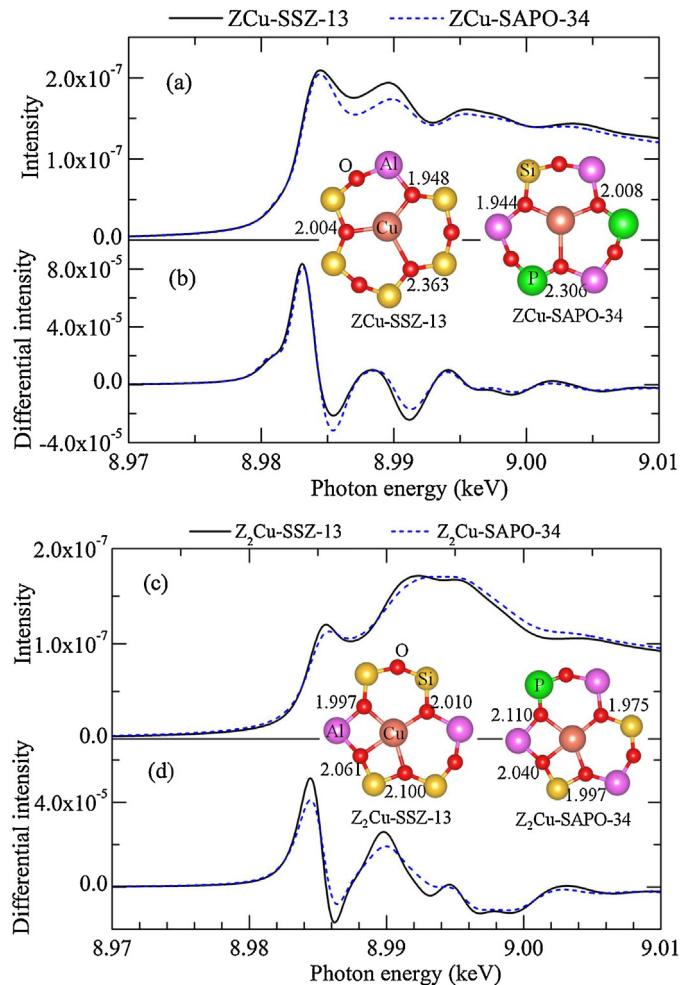
**Fig. 11.** The calculated PDOS of the excited Cu 4p state (a) and the computational K-edge XANES of Cu (b) in the 6MR (solid line), 8MR\_O14 (dash-dotted line) and 8MR\_O24 (dashed line) locations for clean ZCu. The vertical dashed line at 8978.9 eV shows the Fermi level.



**Fig. 12.** The excited Cu ion orbital distributions in the (a) 6MR and (b) 8MR\_O14 sites. We plotted the PDOS of 4s (dashed line) and 4p (dotted line) states because the orbital distribution cannot be separated by each state. The iso-surface value is 0.04 electrons/Å<sup>3</sup>. The vertical dashed line at 8978.9 eV represents the Fermi level. The results for Cu in 8MR\_O24 is similar with Cu in 8MR\_O14 and detailed information can be found in Fig. S6 in Supplementary Information.

between the 4p states for Cu in the 8MR sites as compared to the 4p state for Cu in the 6MR site. The energy gap between the small peak and the main peak is larger for the 8MR conformations as compared to Cu in the 6MR. In addition, the intensity of the small peak for the 4p PDOS for Cu in 8MR sites is stronger than for Cu in the 6MR site. As discussed in our previous work with SSZ-13 [24], we conclude that the presence of the small peak feature around 8980 eV results from 1s to 4p transition when Cu is situated at one of the 8MR sites and that this feature is not present when Cu is in the 6MR site due to the smaller intensity of the 4p state in that energy range. As mentioned before, the coordination number of Cu in the 8MR\_O14 and the 8MR\_O24 sites is 2, as shown in Fig. 4. The fact that there is no big difference between the XANES of Cu in 8MR\_O14 and 8MR\_O24 sites implies that the XANES of Cu in 8MR\_O14 site is independent on the longer Cu–O distance of 2.353 Å.

We analyzed the different peaks for the 4p PDOS of Cu in the 6MR and the 8MR sites by examining the orbital distributions, as displayed in Fig. 12. We confirmed that Cu in a 4p state, with the orbital distribution shown in Fig. 12 being a 4p<sub>z</sub> orbital, mainly contributes the main peak around 8984 eV. However, the orbital distribution around 8982 eV for Cu in the 6MR contributed mainly

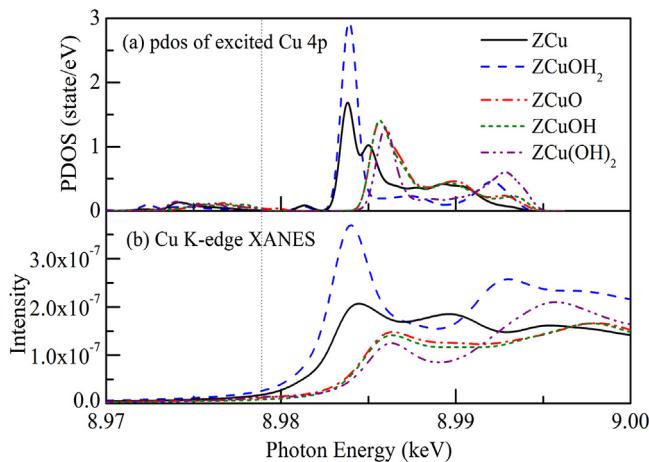


**Fig. 13.** Comparison of the Cu-SSZ-13 (solid line) and Cu-SAPO-34 (dashed line) XANES, with Cu in a (a) Cu<sup>+</sup> (ZCu) or in a (c) Cu<sup>2+</sup> (Z<sub>2</sub>Cu) oxidation state. The Cu ions are located in the 6MR site. The differential plots of the corresponding XANES are displayed in (b) Cu<sup>+</sup> and (d) Cu<sup>2+</sup>, respectively. The local structures of Cu ions are shown in insert figure, as well as the distances between Cu ions and lattice O atoms.

to the 4s state with a small contribution from the 4p state. For Cu in one of the 8MR sites this combined contribution by both the 4s and 4p states is near the Fermi level. The different contributions of the 4p state for Cu in the 6MR and the 8MR sites result in a different shape of the orbital, as shown on the left of Fig. 12. Specifically, the Cu ion in the 6MR is centered in the orbital, while the Cu ion is located toward the edge of the orbital for Cu in 8MR. The orbital distribution of Cu in the 6MR is more symmetrical than that of Cu in the 8MR.

### 3.5.2. XANES comparison of Cu-SSZ-13 and Cu-SAPO-34 in the absence of adsorbates

Fig. 13 shows a comparison between the XANES of a clean Cu-SSZ-13 and Cu-SAPO-34, including both the Cu<sup>+</sup> and Cu<sup>2+</sup> oxidation states. For the Cu<sup>+</sup> species, the coordination number is 3 for both Cu-SSZ-13 and Cu-SAPO-34. The distances between Cu and lattice O atoms are almost the same, respectively 1.948, 2.004, 2.363 Å and 1.944, 2.008, 2.306 Å for Cu-SSZ-13 and Cu-SAPO-34. The same oxidation state of 1+ and same local structure produce nearly identical Cu K-edge XANES for Cu-SSZ-13 and Cu-SAPO-34, as shown in Fig. 13a. The edge position is defined as the maximum of the differential plot of the rising edge in the XANES. Fig. 13b shows the differential plots of the Cu K-edge XANES for Cu<sup>+</sup>-SSZ-13 and Cu<sup>+</sup>-SAPO-34. It is found that the edge position of Cu<sup>+</sup> species in



**Fig. 14.** (a) The excited 4p PDOS of Cu in the ZCu conformation in the presence of adsorbates (H<sub>2</sub>O, O atom, OH and 2 OH) with different oxidizing power. The Cu<sup>+</sup> ion is located in the 6MR site. (b) The corresponding K-edge XANES. The vertical dashed line at 8978.9 eV shows the Fermi level.

**Table 2**

Edge position shifts in the Cu K-edge XANES in the presence of several adsorbates in the ZCu conformation (as shown in Figs. 14 and 15, as well as in Fig. S7) with respect to the corresponding clean ZCu conformation with different Cu locations. The original data of the edge positions can be found in Table S1 of Supplementary Information. The resolution of the computational XANES is 0.05 eV.

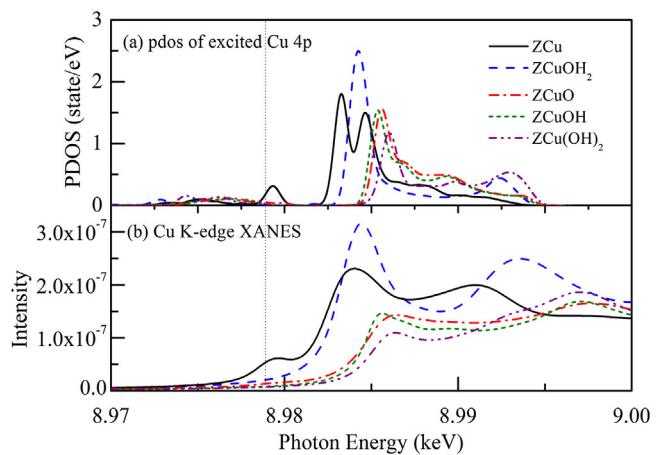
Shift of edge position (eV)	Clean	H <sub>2</sub> O	O	OH <sup>-</sup>	2OH <sup>-</sup>
6MR	0.00	-0.10 <sup>a</sup>	1.75	1.67	1.94
8MR_O14	0.00	0.89	2.50	2.11	3.03
8MR_O24	0.00	0.14	2.30	1.67	2.93

<sup>a</sup> Note that for Cu in the 6MR site, Fig. 16 shows that the Cu edge position in the ZCu conformation in the presence of H<sub>2</sub>O seems to be at a lower energy than that of the clean ZCu conformation. This is confirmed by the edge position shift.

clean Cu/CHA zeolite is located at the photon energy position of 8983.1 eV. A similar analysis can be applied when comparing the Z<sub>2</sub>Cu conformations in Cu-SSZ-13 and Cu-SAPO-34, as shown in Fig. 13c. In such Z<sub>2</sub>Cu conformations, we have replaced two Si atoms for two Al atoms (SSZ-13) or two P atoms for two Si atoms (SAPO-34). Different from the Cu<sup>+</sup> ion, the Cu<sup>2+</sup> ion has a coordination number of 4. The edge position of the Cu<sup>2+</sup> species in the clean Cu/CHA zeolite is located at a photon energy position of 8984.4 eV, which is higher than the Cu<sup>+</sup> species edge position with a difference of 1.3 eV. This result again confirms the trend of the edge shift with its oxidation state. As is well-known, the XANES is determined by the local structure and oxidation state of the exchanged Cu ion. However, it is not intuitive that a ring made from Al and Si atoms (Cu-SSZ-13) or Al, Si and P atoms (Cu-SAPO-34) can give us virtually identical XANES. Indeed, based on our analysis, even though we have completely different atoms making up the ring structures (Cu-SSZ-13 and Cu-SAPO-34), the XANES of Cu with a certain oxidation state would be hard to differentiate experimentally.

### 3.5.3. Influence of adsorbates on the Cu K-edge spectra

We chose several species (H<sub>2</sub>O, O, OH and 2 OH) with different oxidizing powers to examine the relationship between the oxidizing power and the edge position. Figs. 14 and 15 display the XANES results for Cu in the 6MR and 8MR\_O14 sites, respectively. Because the results are very similar for Cu in the 8MR\_O14 and 8MR\_O24 sites, the corresponding XANES and PDOS results are shown in Fig. S7 in Supplementary Information. The edge position shifts are listed in Table 2 for Cu in the 6MR, 8MR\_O14 and 8MR\_O24 sites. We can also interpret the XANES of Cu for each of these adsorbates through the corresponding excited 4p PDOS. For the 6MR conformation, Fig. 14a shows the excited 4p state for Cu as influenced



**Fig. 15.** (a) The excited 4p PDOS of Cu in the ZCu conformation in the presence of adsorbates (H<sub>2</sub>O, O atom, OH and 2 OH) with different oxidizing power. Cu is located in 8MR\_O14 site. (b) The corresponding K-edge XANES. The vertical dashed line at 8978.9 eV shows the Fermi level.

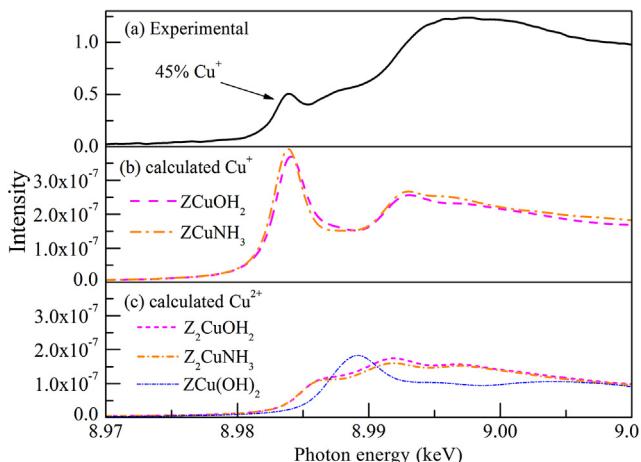
by each of the adsorbates and Fig. 14b shows the corresponding XANES. As can be seen in Fig. 14b, the peak intensity of the Cu K-edge XANES is intensified when H<sub>2</sub>O is adsorbed on the Cu, but this peak intensification does not occur with other adsorbates. Such a high peak intensity might be due to the interaction of the H atoms with lattice O atoms. Also observed in Fig. 14b, the edge positions varies noticeably in the presence of different adsorbates. The edge position is defined as the maximum of the differential plot of the rising edge in the XANES. Overall, one can see in Fig. 14b that, with the exception of H<sub>2</sub>O, the molecular adsorption of these adsorbates results in a shift of the edge position to higher energy. The XANES edge shifts for different molecules adsorbed on a Cu<sup>+</sup> ion with respect to corresponding clean ZCu conformation are listed in Table 2. It is found that the edge position and the oxidizing power are in the same order, namely clean Cu ≈ H<sub>2</sub>O < O ≈ OH < 2(OH) (from low to high energy). As is well-known, one would expect the higher edge position due to the higher binding energy of electrons in a Cu ion with a higher oxidation state. It is concluded that our computational XANES results capture the real trend of the edge shift with oxidation state. While the XANES discussion so far has focused on the situation of Cu in the 6MR site, we arrive at similar conclusions when Cu is located in the two 8MR sites as discussed below. Likewise, a similar conclusion was made in our previous work on the Cu-SSZ-13 zeolite [24].

The Cu K-edge XANES for the plot shown in Fig. 14b, with Cu in the 6MR site, is produced through an excitation of a 1s electron to the 4p state. This is illustrated by the projected density of states of the copper ion for the various adsorbates shown in Fig. 14a. Transition to another s state is dipole forbidden, and s-d-state transitions are highly unlikely [41]. The clean ZCu and the H<sub>2</sub>O adsorbed ZCu conformations have 4p states at about the same energy level. The same trend toward higher energies observed in the XANES spectra is also seen in the p-states of Cu for each of the adsorbates.

Differently with Cu in 6MR site, the Cu K-edge XANES for Cu in the 8MR (8MR\_O14) is shown in Fig. 15. The edge position for Cu in the 8MR follows a trend similar to Cu in the 6MR. For Cu in the 8MR, adsorption of H<sub>2</sub>O results in a slightly higher energy of the edge position, indicating that H<sub>2</sub>O has a slight oxidizing effect on Cu in the 8MR.

### 3.5.4. Comparison of the XANES spectra with experiment

Based on the construction of the phase diagram in Section 3.4, we have selected the most favorable conformations and compared them to the experimental XANES of Cu-SAPO-34. Such a compari-



**Fig. 16.** (a) Experimental XANES spectrum of a commercial ~1.75 wt% Cu-SAPO-34 catalyst collected *operando* under standard SCR conditions [25]. Computational XANES for (b) Cu<sup>+</sup> and (c) Cu<sup>2+</sup> species, where Cu is located in 6MR site. The atomic structures of ZCuNH<sub>3</sub>, ZCuOH<sub>2</sub> and Z<sub>2</sub>CuNH<sub>3</sub> can be found in Fig. S5 of the Supplementary Information.

son procedure of our theoretical K-edge XANES to the experimental results has been detailed in our previous work [24]. However, the construction of the phase diagram does not take into account the possible interaction of Cu exchanged ion with ammonia, which may block the adsorption of H<sub>2</sub>O because the binding preference for NH<sub>3</sub> over H<sub>2</sub>O in Cu-SSZ-13 [42]. As a result, we compare the XANES spectrum of Cu<sup>2+</sup> and Cu<sup>+</sup> ions in the presence of NH<sub>3</sub> in addition to those considered in the construction of the phase diagram since ammonia is an important reactant. We also consider the interaction of water with a Cu<sup>2+</sup> ion (Z<sub>2</sub>CuOH<sub>2</sub>) that has been charged compensated by two Al atoms, which has been shown to be a favorable configuration in the Cu-SSZ-13 system [40]. These additional conformations considered in this section are shown in Fig. S5 of Supplementary Information.

In Fig. 16, we show the experimental XANES spectra. As shown in Fig. 16a, it was determined that as much as 45% of the total Cu ions were Cu<sup>+</sup> under these conditions, where the photon energy of the Cu<sup>+</sup> peak is around 8984 eV. Details of the experimental procedure and quantification of the Cu<sup>+</sup> can be found elsewhere [25]. Using our computational results of the Cu K-edge XANES for Cu-SAPO-34 under different situations, we correlated the XANES of various model species to the experimental XANES collected *operando* under standard SCR conditions. We compare the experimentally assigned Cu<sup>+</sup> peak, with our ZCuOH<sub>2</sub> model in Fig. 16, which was determined to be the most energetically favorable configuration for a wide range of oxygen and water chemical potential values. We also compare the XANES spectrum of an NH<sub>3</sub> molecule bonded to a Cu ion in the ZCu conformation, which we denote as a ZCuNH<sub>3</sub> configuration. The calculated photon energy distribution of the Cu<sup>+</sup> peaks of H<sub>2</sub>O and NH<sub>3</sub> adsorbed ZCu correlate well with the experimental XANES in the same photon energy range, as shown in Fig. 11b. Interestingly, the XANES spectrum of the ZCuOH<sub>2</sub> and ZCuNH<sub>3</sub> conformations are very similar, so it would be hard to distinguish the presence of both species based on the XANES their respective XANES spectra alone.

We also found in the construction of the phase diagram that under oxidizing conditions that the ZCu(OH)<sub>2</sub> species becomes increasingly more energetically favorable. By examining the XANES of the Cu<sup>2+</sup> species, as shown in Fig. 11c, we find that the middle peak of the experimental XANES spectrum at 8988 eV corresponds well to the peak found for the ZCu(OH)<sub>2</sub> species. The XANES spectrum for the other species considered (ZCuOH<sub>2</sub> and ZCuNH<sub>3</sub>) correlate well with the highest energy peak of the XANES spectrum at around 8995 eV. It is also interesting to see that the XANES spec-

tra for Z<sub>2</sub>CuOH<sub>2</sub> and Z<sub>2</sub>CuNH<sub>3</sub> are very similar, as was the case when comparing the XANES spectra for the ZCuOH<sub>2</sub> and the ZCuNH<sub>3</sub> conformations. However, it is found that the peak intensities of the Cu<sup>2+</sup> species in the presence of ammonia and water are much lower than those for a Cu<sup>+</sup> ion in the presence of water or ammonia in a ZCu conformation, as can be seen when comparing Fig. 16b and c.

#### 4. Conclusions

In summary, through calculations from first principles, the properties of Cu-SAPO-34 were studied at the atomic level. For pure SSZ-13 and ALPO-34, the equilibrium volume of ALPO-34 is larger than that of SSZ-13, which is a result of the shorter average bond lengths between the tetrahedral sites on the lattice oxygen atoms for SSZ-13 (1.625 Å) as compared to the corresponding ones for ALPO-34 (1.645 Å). Similar to the ZCu conformation in Cu-SSZ-13, it is found that the 6MR site is the most energetically favorable site as compared to the 8MR sites with total energy differences in Cu-SAPO-34 of about 0.5 eV with respect to the 6MR site. In addition, the Cu binding energies were found to be -0.88, -0.38 and -0.32 eV for Cu in the 6MR, 8MR\_O14 and 8MR\_O24 sites, respectively. Upon the adsorption of the species (H<sub>2</sub>O, O, OH and 2OH) we studied in this contribution, the energy differences between Cu in the 8MR and 6MR sites decreases and almost disappears, which means that the thermodynamic stability of Cu becomes nearly identical in different locations. It is also found that the decomposition of O<sub>2</sub> on Cu ions is thermodynamically unfavorable. By comparing the average adsorption energies per molecule of OH and 2 OH species on a Cu<sup>+</sup> ion, we concluded that upon the adsorption of 2 OH species, the average interaction between OH and the Cu<sup>+</sup> ion is close to that found with the adsorption of one OH species on a Cu<sup>+</sup> ion in the 6MR, however the average adsorption energy is weaker than the adsorption of a single OH species when Cu is in one of the 8MR sites. Further, a thermodynamic phase diagram study showed that for the ZCu conformation in Cu-SAPO-34, at a given chemical potential of H<sub>2</sub>O, Cu<sup>+</sup> bound to a single H<sub>2</sub>O is found to be the most stable species at low oxygen potential values while the ZCu conformation in Cu-SAPO-34 with the adsorption of 2 OH species is the most stable at high oxygen chemical potential values.

The X-ray absorption near edge structure (XANES) of Cu in Cu-SAPO-34 under different conditions was also modeled from first principles. An excellent correlation was found between the excited 4p PDOS of Cu and the K-edge XANES. By comparing the Cu K-edge XANES between Cu-SSZ-13 and Cu-SAPO-34 with Cu in a +1 or +2 oxidation state, we concluded that even though we have completely different atoms making up the structures (Cu-SSZ-13 and Cu-SAPO-34), the XANES of Cu with certain oxidation state is hard to differentiate. As is well-known, one would expect the higher edge position to be due to the higher binding energy of electrons in a higher oxidation state. By studying the Cu K-edge XANES of Cu-SAPO-34 with the adsorption of species of different oxidizing power, it is concluded that our computational XANES results capture the real trends of the edge shift with oxidation state. Finally, we were able to gain a number of insights into the experimental XANES spectrum under standard SCR conditions by comparing it to the simulated XANES spectrum of several favorable conformations determined in part from the construction of the phase diagram. We found the ZCuOH<sub>2</sub> and the ZCuNH<sub>3</sub> conformations correlated well with the experimental Cu<sup>+</sup> peak region. On the other hand, the simulated XANES for the Z<sub>2</sub>CuOH<sub>2</sub>, Z<sub>2</sub>CuNH<sub>3</sub> and ZCu(OH)<sub>2</sub> conformations correlated well with the experimental Cu<sup>2+</sup> peak regions of the XANES spectrum.

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## Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.cattod.2016.01.025>.

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