

Efficient Photon Recycling and Radiation Trapping in Cesium Lead Halide Perovskite Waveguides

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S Supporting Information

ABSTRACT: Cesium lead halide perovskite materials have attracted considerable attention for potential applications in lasers, light-emitting diodes, and photodetectors. Here, we provide the experimental and theoretical evidence for photon recycling in CsPbBr₃ perovskite microwires. Using two-photon excitation, we recorded photoluminescence (PL) lifetimes and emission spectra as a function of the lateral distance between PL excitation and collection positions along the microwire, with separations exceeding 100 μ m. At longer separations, the PL spectrum develops a red-shifted emission peak accompanied by an appearance of well-resolved rise times in the PL kinetics. We developed quantitative modeling that accounts for bimolecular recombination and photon recycling within the microwire waveguide and is sufficient to account for the observed decay modifications. It relies on a high radiative efficiency in CsPbBr₃ perovskite microwires and provides crucial information about the potential impact of photon recycling and waveguide trapping on optoelectronic properties of cesium lead halide perovskite materials.



Solution-processed organic—inorganic hybrid perovskitebased semiconductors have rapidly progressed as versatile and promising materials for low-cost and highperformance optoelectronics applications in the past five years^{1–11} due to their remarkable light absorption,¹² long carrier diffusion length,^{12,13} controllable dimensionalities,^{14–21} and tunable band gaps.²² Recently, all-inorganic CsPbX₃ (X = Br⁻, I⁻ or Cl⁻) perovskites have attracted particular attention for light-emitting diodes (LEDs)^{23,24} and lasers^{25–27} due to enhanced light emission and photo- and thermal stability.^{28,29} The wavelength tunability of photoluminescence (PL) emission can be further manipulated via the choice of the desired halide precursor or anion exchange reactions. Facile, solutionprocessable methods allow these materials to be fabricated in a variety of configurations such as nanowires,^{30–32} nanocryst-

als,^{33,34} and microrods.³⁵ Wavelength-scale sizes of these microstructures make them suitable for potential integration with on-chip, miniaturized devices such as coherent light sources, LEDs, and photodetectors.

Laser and LED applications of $CsPbX_3$ materials require detailed knowledge of the dynamics of mode propagation and spectral redistribution of the emission in the waveguiding structures. Repeated incoherent absorption and re-emission of photons in strongly absorbing media is expected to substantially affect carrier recombination dynamics and mode propagation,

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influencing quantum efficiency and light dynamics. Significant processes of self-absorption and light trapping have been observed in solid-state materials with high PL quantum yields (PLQY), such as III–V semiconductors (GaAs)^{36–38} and rareearth doped fibers,^{39,40} leading to large modifications of the emission line shape and significantly affecting emission lifetime measurements. *Photon recycling*, i.e. numerous iterative self-absorbance and photon re-emissions events within the photoactive layer, has been known to substantially enhance the photovoltaic conversion efficiency of GaAs solar cells and photodetectors,^{41,42} although its importance for high-efficiency perovskite-based solar cells has been the subject of recent controversy.^{43–45}

In this work, we performed a detailed time- and spectrally resolved investigation of waveguide-assisted photon selfabsorption-re-emission in single-crystal CsPbBr₃ microwires synthesized via a one-step, solution-processing method. We took advantage of two-photon excitation to avoid surfacerelated PL quenching and moisture-induced artifacts.^{46,47} We directly tracked the evolution of PL signals as a function of the lateral separation between excitation and collection spots along the microwire to the distances exceeding 100 μ m. We observed appearance of the delayed rises in PL kinetics, accompanied by continuous spectral redistribution of the PL signal, initially centered at 525 nm, toward lower energy, concentrating the emission intensity in a well-defined peak at 545 nm. To explain salient features of the position-dependent PL dynamics, we numerically analyzed a model of the evolution of charge carrier density that accounts for radiation trapping in one-dimensional waveguides. The model establishes a quantitative framework that accommodates well the observed PL kinetics and unambiguously points to the importance of photon recycling effects. Moreover, it indicates that internal radiative efficiency of the CsPbBr₃ microwires is close to unity, thus providing the necessary foundation for the usage of CsPbBr₃ perovskite materials in light-emitting applications.

Sample Preparation and Structural Characterization of CsPbBr₃ Microwires. We synthesized CsPbBr3 microwires using a customized cast-capping crystallization⁴⁸ process. Several drops of CsPbBr3 precursor solution were dropped on a glass substrate, while a second glass was used as the capping substrate to confine the solution. The two glasses were heated at 100 °C for 3-5 days to let the crystals grow to the desired sizes. The resulting arrays of microwires were characterized using optical spectroscopy, scanning electron microscopy (SEM), X-ray diffraction (XRD), transmission electron microscopy (TEM), selected area electron diffraction (SAED), and energy dispersive X-ray spectroscopy (EDX) techniques (Figures 1 and S1), which demonstrate nearly ideal crystal structure, stoichiometric composition, and shape uniformity, making microwires ideally suited for light trapping and waveguiding.

Bulk optical absorption and PL emission measurements show the onset of the optical band gap at ~510 nm and main PL peak at ~525 nm, with a full-width half-maximum (fwhm) of 21 nm when the CsPbBr₃ microwires are excited at 400 nm (Figure 1b). The structural analysis confirms the crystalline nature of the microwires. Figure 1c shows the top-view SEM image of as-synthesized microwires. The microwires present several different lengths, from a few to hundreds of micrometers, according to the synthesis protocol, with a uniform width and thickness of $5-7 \mu$ m. The XRD spectrum of the assynthesized microwires shows two sharp peaks at 15° and 30°,



Figure 1. Synthesis and characterization of CsPbBr₃ microwires. (a) Schematic drawing of cast-capping method for growing the CsPbBr₃ microwires. (b) Normalized absorption and photoluminescence spectra of CsPbBr₃ microwire crystals grown by cast-capping method. (c) SEM top view of a single CsPbBr₃ microwire with a scale bar of 30 μ m. (d) XRD spectra of asgrown CsPbBr₃ microwires. (e) TEM image of a single microwire with a scale bar of 500 nm. The inset shows the high-resolution SAED results of a single CsPbBr₃ microwire with a scale bar of 2 nm⁻¹.

in good agreement with the orthorhombic CsPbBr₃ phase, indicating the preferential orientation of the crystallization process. Furthermore, TEM and SAED patterns confirm the crystalline nature of the wires and the orthorhombic symmetry (Figure 1e). Finally, EDX analysis probed the elemental uniformity of as-synthesized microwires with a homogeneous distribution of Cs/Pb/Br (~1/1/3) matching well the stoichiometry of CsPbBr₃ (Figure S1). All these results collectively confirmed that high-quality single-crystalline CsPbBr₃ microwires with preferential orientation were obtained through our customized cast-capping technique.

Photon Waveguiding and Absorption-Re-emission. The primary parameters that govern photon recycling are extinction coefficient (α) and radiative efficiency within individual microwires.⁴⁹ When absorption length $(l = 1/\alpha)$ is much smaller than the size of the sample, the light's propagation between the excitation and detection regions will allow for many absorption-re-emission events, thus influencing the spectrum shape and modifying the observed lifetime. Selfabsorption is assisted by total internal reflection (TIR) that keeps a substantial fraction of photons from escaping the structure and guides light over longer distances in the waveguide. Bulk absorption measurements are not representative of the absorption within individual microwires due to the noncontinuous microwires' coverage on the glass substrate. To alleviate this problem, we performed linear absorption measurements on individual microwires using confocal double-objective geometry, as shown in the left part of the inset in Figure 2a. An objective with a lower numerical aperture $(NA \sim 0.5)$ has been used to couple broadband white light



Figure 2. (a) Linear absorption spectrum of an individual microwire. Inset: Left part, schematics of linear absorption measurements using white light; right part, variable length excitation-collection measurements using the same pair of objectives, with the bottom one translated along the microwire. (b) PL spectra as a function of separation s. Spectra are normalized at the maximum emission intensity. Excitation power 20 μ W. Inset: PL emission intensity at the 530 nm peak as a function of separation distance s.



Figure 3. (a) Normalized PL dynamics of the CsPbBr₃ perovskite microwires as a function of separation between excitation and collection spots measured at main emission peak of 530 nm. (b) Expanded view of the early times, presented on a linear scale. Fitted curves are shown.

(WL) through the top facet of the microwire (from the air side), while a higher-NA objective positioned below the glass substrate was used for light collection. The thickness of the microwires (as seen in SEM imaging) has been consistently found in the \sim 5 um range, thus allowing us to estimate the absorption coefficient. The use of a low-NA objective largely avoids the problem of WL coupling into the waveguiding modes and thus escaping detection (NA = 0.5 corresponds to 30° coupling half angle, while the index of refraction $n \sim 2.3$ of the CsPbBr₃ material corresponds to a TIR critical angle of θ_{cr} $\sim 27^{\circ}$). Figure 2a indicates that optical density (OD) of individual microwires ranges from 0.1 to 0.15 OD at the main exciton peak and approximately between 0.05 and 0.075 at the PL emission wavelengths of 525-530 nm. The corresponding absorption length, l_i is on the order of 20-40 μ m, and the extinction coefficient, α , is in the range of $\sim 2.5-5 \times 10^2$ cm⁻¹. The extinction values obtained in our work point to the potential contribution of the TIR-assisted waveguiding to photon recycling in microwires.

PL Spectra Indicating Photon Recycling. Figure 2b presents PL spectra for several values of the spatial separation *s* between the excitation and collection volumes along the individual microwire. The same excitation–collection arrangement (right side of the inset in Figure 2a) has been used, whereas excitation light is from a 800 nm laser source positioned in the middle of the microwire and the PL collection spot is scanned along the microwire's bottom surface, with separation distance *s* in excess of 100 μ m. The relative weight of the main emission peak at

~530 nm at first shifts toward longer emission wavelength (for $s = 0-30 \ \mu m$ separations, indicated by arrows). This initial shift is attributed to the primary (i.e., PL emission that is produced by direct laser excitation) photon reabsorption at shorter wavelengths and correspondingly larger PL contribution at longer wavelength due to spectral filtering within the perovskite material as previously described.⁵⁰ However, at longer separation distances, we observe the appearance and relative growth of a well-defined peak at the lower energy, which is continuously evolving to ~545 nm as separation distance exceeds 100 μ m. It is clearly seen that while the overall intensity of the emission is dropping off sharply (inset to Figure 2b), the re-emission peak is taking over the primary PL emission. A similar behavior of PL spectra has been recently observed in ref 32. This behavior is indicative of repetitive PL self-absorptionre-emission mechanism under conditions of inhomogeneous broadening that is shifting emission down in energy (following sharp cutoff in absorption profile) and points toward multistep photon recycling in CsPbBr₃ perovskites.

Quantitative Description of Photon Recycling Using PL Dynamics. Quantitative interpretation of the PL emission spectra is complicated by the specifics of light propagation within the microwire. Visual appearance and intensity of PL peaks are often related to the presence of macroscopic surface defects that strongly influence the amount of the collected PL light (Figure S2). At the same time, PL lifetime measurements are affected by only the intrinsic factors such as pumping of the perovskite by the two-photon excitation pulse at short separation distances and pumping via PL absorption-reemission events at longer separations. Using an 800 nm laser for two-photon excitation allows us to mostly avoid excitation of the surface-related states that typically manifest themselves in very short initial PL lifetime components (some examples are shown in the Supporting Information).⁴⁹ Figure 3a shows that, as the separation is increased, we observe an appearance of delayed rise components, indicating the influx of excitations to the distant regions of the microwire. To properly analyze and represent the dynamics in a noise-free format, we consistently fitted PL decays with 2-3 exponentials, fully accounting for the observed rise and fall dynamics. Figure 3b shows an expanded view of the fitted kinetics at different separation distances for shorter delay times. The data illustrate the gradual evolution of the rise time components in the PL dynamics at longer separations. This behavior is a clear signature of the delayed energy influx into the remote regions of the microwire.

In general, there could be two mechanisms generating excitations in the remote parts of the microwire away from the original laser excitation spot. One is the photon recycling, and the other is carrier diffusion, where charge carriers generated by the laser pulse diffuse within the wire and recombine at a later time, giving rise to the delayed PL emission.⁵¹ To clarify this issue, we performed independent carrier mobility measurements in individual microwires using two-dimensional space charge limited current (2D-SCLC) and field effect transistor (FET) methods (more details are in provided in Experimental Section in the Supporting Information, Figures S3 and S4). The results indicate that the hole mobilities are in the range of μ = 0.01–0.02 cm²/(Vs), which is in a good agreement with the value reported by Huo et al.⁵² Considering PL lifetime of the carriers to be around 400 ns (Figure 3a), the estimated roomtemperature diffusion length, $L_{\rm D} \sim 0.1~\mu{\rm m}$. Hence, the observed evolution of PL decay dynamics at separation distances of tens of micrometers cannot be a result of charge carrier diffusion. The fitted PL rise time values (shown in the Supporting Information, Table S1) indicate the nearly linear dependence of the rise time constants with the separation distance along the microwire as will be appropriate for a stepby-step, radiative energy-transfer process. Taken together, spectral and dynamics data point to photon recycling, assisted by waveguiding in CsPbBr₃ perovskite microwires.

For such a scenario to occur, microwire samples must have sufficiently high PL emission quantum yield that would allow for a number of sequential absorption-re-emission events. However, the PLQY of an individual microwire cannot be reliably deduced from the bulk QY measurements. In a bulk sample, the emitted PL photons are waveguided within the microwires and experience multiple absorption-emissionscattering steps, greatly reducing their probability to escape toward detection. Standard measurements with an integrating sphere provide PLQY of the microwires on the order of 5-8%, in agreement with bulk CsPbBr3 single crystals, but clearly too small to explain the observed experimental data within the scope of photon recycling model. Furthermore, it is well-known that PLQY in perovskite materials is fluence-dependent.53 Measurements using an integrating sphere operate at low fluence conditions where monomolecular (trap-assisted) recombination regime results in lower PLQY values. In contrast, photon recycling necessarily involves higher excitation fluences to generate enough photons to be recorded at the remote locations along the wire. Light propagation inside the microwire is governed by the TIR light confinement factor, T.

Following the calculations presented by Shurcliff and Jones⁵⁴ for light from an isotropic emitter trapped within the rectangular waveguide of the index $n_{\rm per} \sim 2.3$ with five sides facing air ($n_{\rm air} = 1$) and one side facing the glass substrate ($n_{\rm q} = 1.5$), the confinement factor is estimated as $T \sim 0.63$. (i.e., once generated, 63% of the photons will forever propagate inside via TIR if no reabsorption is taking place.) Hence, in the process of photon recycling that involves multiple absorption—re-emission steps, confinement plays a major role in retaining photons within the waveguide and maintaining sufficiently high re-excitation fluence.

In order to rationalize the observed experimental behavior of separation-dependent PL kinetics as observed in Figure 3, we analyze here an *effective* one-dimensional model, appropriately modified from the one found in the kinetic theory of semiconductors:⁵⁵

$$\frac{\partial n(x, t)}{\partial t} = D \frac{\partial^2 n(x, t)}{\partial x^2} - \frac{n(x, t)}{\tau_{tr}} - Bn^2(x, t) + qB \int dx' K(|x - x'|) n^2(x', t)$$
(1)

The validity of the one-dimensional model here is based on the overall geometrical shape of the excited region of the microwires. The initial excitation takes place via a two-photon absorption whose linear absorption length is much larger than the lateral dimension of the wire. The initial excitation region is therefore practically uniformly distributed across the microwire. This uniformity is then of course preserved in the process of the diffusion, making the latter a function of only coordinate xalong the microwire (in full similarity with textbook treatments of the diffusion from uniformly excited surface). Equation 1 thus describes the spatial-temporal evolution n(x, t) of the charge carriers' density along the microwire from the initial profile n(x, 0) for the equal populations of photoexcited electrons, n, and holes, p. In addition to single-particle processes of carrier diffusion (coefficient D) and trap-assisted decay (lifetime τ_{tr}), eq 1 incorporates bimolecular (electronhole, $np = n^2$) radiative recombination (coefficient *B*) responsible for PL emission.^{54,56} The last term in eq 1 is representative of photon recycling and describes carrier generation at point x due to reabsorption of the light emitted as a result of radiative bimolecular recombination at point x'(kernel K(|x - x'|)). As the two PL-related terms are both proportionate to $n^2(x, t)$, their role in the overall dynamics increases for higher excitation densities. Because bimolecular recombination can also involve a nonradiative channel, the dimensionless parameter 0 < q < 1 in eq 1 defines its radiative quantum yield: at q = 1, all electron-hole recombination events result in photon emission.

To experimentally validate the bimolecular dependence of PL ~ n^2 on density n, we recorded initial PL intensity as a function of the laser excitation power, P. Because of the two-photon excitation method used in this work, the light absorption itself is also proportional to the square of the laser power, leading to the fourth-power dependence of the observed PL, ~ P^4 , for the bimolecular recombination emission. Figure 4 shows the total PL emission, integrated along the microwire as a function of the applied 800 nm laser power. The calculation method as well as representative PL kinetics are shown in Figure S5. The observed PL signal dependence of the rate of



Figure 4. Initial PL intensity integrated along the microwire as a function of the applied laser power. Dots, experimental points; colored lines, proportionality to different powers of *P*.

radiative processes on the density n (which is different from the linear dependence, expected in the case of exciton density⁵⁷).

The simulations resulting from the numerical solutions to the model of eq 1 are exemplified in Figure 5 for a set of



Figure 5. Model PL decay curves for several separation distances calculated with eq 1 and distinguished by curve colors. Compared are results with bimolecular radiative efficiency q = 0.25 (dashed lines) and q = 1 (solid lines). For this computational example, the maximum initial carrier density $n_{\text{max}} = 3/B\tau_{\text{tr}}$ was used, and other parameters are defined in the text. Reduced time is shown in the units of the charge carrier lifetime.

representative parameter values. If all emitted photons were reflected from the microwire sidewalls, the spatial kernel would behave as $K(x) = \alpha \int_{1}^{\infty} e^{-\alpha |x| u} du/2u$ and would satisfy the conservation condition, $\int_{-\infty}^{\infty} K(x) dx = 1.5^{7}$ We correspondingly modify the kernel to account for photons escaping through the sidewalls (and actually contributing to the observed PL); in the computational example of Figure 5, the kernel satisfies $\int_{-\infty}^{\infty} K(x) dx \approx 0.69$. This number is very close to the previously estimated TIR light confinement factor $T \sim$ 0.63, while the linear absorption length is $1/\alpha = 40 \ \mu m$. (Note that this length is also much larger than the lateral size of the wire.) The model PL decay curves in Figure 5 were simulated starting from the initial excitation profile extracted from the experimental data for Figure 3. In our simulations, we purposefully used a substantially increased (with respect to the experimentally inferred) value of the single-carrier diffusion length $L_{\rm D} = \sqrt{D\tau_{\rm tr}} = 1 \ \mu {\rm m}$ and observed that, even with this value, such diffusion cannot account for the experimentally observed time-dependent spreading of the initial profile. Moreover, the observed pattern of position-dependent PL decay could not be simulated with low to moderate values of the bimolecular radiative efficiency parameter q (dashed lines in Figure 5 show simulation results for q = 0.25). Only for high radiative efficiency, simulation results in Figure 5 (only q = 1

data shown by solid lines) compare favorably with experimental data in Figure 3, reflecting both faster PL decays at the early times at shorter spatial separations (associated with $n^2(x, t)$ term) and appearance of the delayed PL risetimes due to photon recycling at longer separations.

Prior studies performed with Methylammonium-based Perovskite (MAP) perovskites have indicated that the efficiencies of bimolecular recombination span a wide range of values, from <10% percent to close to unity, and could be strongly influenced by trap-assisted Auger recombination.^{8–11} Consequently, this mechanism would be more relevant to polycrystalline MAP films than for single-crystal materials as the latter generally have lower defect densities. Hence, our findings that bimolecular recombination efficiency in CsPbBr₃ crystalline microwires is close to unity in elementary electron– hole recombination events is in line with those models.

Our model calculations also account for competition with single-particle recombination (lifetime τ_{tr}), their interplay being dependent on the carrier density. In our experiments, as the initial excitation profile spreads in space and decays in time, this density keeps decreasing so that eventually the single-particle recombination becomes the dominant mechanism wherever the density is low enough. Concomitantly, transient analysis reflects distance-dependent changes in the PL emission kinetics, influenced by initial carrier density and photon recycling. The high value of the radiative efficiency of the intrinsic elementary electron-hole recombination steps that is inferred from our data on the CsPbBr₃ microwires should thus not be confused with standard bulk measurements of the quantum yield that could result in significantly reduced, and intensity-dependent, values both due to single-particle trapping and multiple reabsorption-emission steps.

We investigated PL evolution and emission dynamics in individual CsPbBr3 microwires using two-photon excitation and double-objective excitation-collection microscopy. Our results show propagation of the PL emission within individual microwires to distances in excess of a 100 μ m from the excitation location. We found that PL spectral content and PL kinetics strongly depend on the propagation distance along the microwire. As the separation distance increases, the PL emission spectrally redistributes toward the lower energy while PL kinetics develop delayed emission rises, with rise time components scaling with the separation distance. We applied the one-dimensional model of spatiotemporal evolution of the charge carrier density that accounts for monomolecular and bimolecular recombination and waveguide-assisted photon self-absorption-re-emission. Simulated PL dynamics clearly show that the low PLOY values found by the bulk sample measurements are incompatible with the experimental data whenever the material experiences strong photon recycling. The model reveals internal recombination efficiency of the microwires to be close to unity. These findings show the influence of photon recycling on the emission properties of CsPbBr₃ perovskites and underscore its significance for rational design of cesium halide perovskite materials for light-emitting and photon conversion applications.

ASSOCIATED CONTENT

Supporting Information

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Experimental section, EDX results, optical images of microwires, fitted PL kinetics, and mobility measurements (SCLC and FET) (PDF)

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Notes

The authors declare no competing financial interest.

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