

# Optimal design of structures using cyber-physical wind tunnel experiments with mechatronic models

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ABSTRACT: This paper explores the use of a cyber-physical systems (CPS) approach to optimize the design of rigid, low-rise structures subjected to wind loading, with the intent of producing a foundational method to study more complex structures through future research. The CPS approach combines the accuracy of physical wind tunnel testing with the ability to efficiently explore a solution space using numerical optimization algorithms. The approach is fully automated, with experiments executed in a boundary layer wind tunnel (BLWT), sensor feedback monitored by a computer, and actuators used to bring about physical changes to a mechatronic structural model. Because the model is undergoing physical change as it approaches the optimal solution, this approach is given the name "loop-in-the-model" optimization.

Proof-of-concept was demonstrated for a low-rise structure with a parapet wall of variable height. Parapet walls alter the location of the roof corner vortices, reducing suction loads on the windward facing roof corners and edges and setting up an interesting optimal design problem. In the BLWT, the parapet height was adjusted using servo-motors to achieve a particular design. Experiments were conducted at the University of Florida Experimental Facility (UFEF) of the National Science Foundation's (NSF) Natural Hazard Engineering Research Infrastructure (NHERI) program.

KEYWORDS: cyber-physical systems; mechatronic; optimization; boundary-layer wind tunnel; parapet; UFEF; NHERI

## 1 INTRODUCTION

Boundary layer wind tunnels (BLWT) are the primary tool in wind engineering to characterize surface pressures on bluff bodies. BLWT modeling is valuable when studying new structures for which the simplified provisions of ASCE 7 are inadequate or too conservative [1]. While BLWT modeling has remained a standard for decades, it has not benefited from recent advances in computationally-based optimization techniques for structural design. These techniques are now efficient enough to be applied during live testing if the structure has the ability to morph, e.g., change aerodynamic shape. Meta-heuristic algorithms such as particle swarm and genetic

42 algorithms are problem-independent algorithms that efficiently explore a complex solution  
 43 space, providing new opportunities to study multi-variate and multi-objective optimization  
 44 problems. These optimization algorithms have promise for delivering cost-effective design  
 45 solutions for wind-sensitive structures. Moreover, the accuracy of the numerical optimization  
 46 process can be improved by combining it with an experimental method such as BLWT modeling.

47 The goal of the study is to explore the use of cyber-physical systems (CPS) for optimal  
 48 design in wind engineering. We demonstrate proof-of-concept for cyberinfrastructure-augmented  
 49 BLWT modeling that produces optimal designs faster than purely experimental methods and  
 50 with a higher degree of realism than purely computational methods. The approach is fully  
 51 automated, with experiments executed in a BLWT, sensor feedback monitored and analyzed by a  
 52 coordinating computer, and optimization techniques used to bring about physical changes to the  
 53 structural model in the BLWT (see Figure 1). Because the model is undergoing physical change  
 54 as it approaches the optimal solution, this approach is given the name "loop-in-the-model"  
 55 testing.

56 The building selected for the proof-of-concept was a low-rise structure with a parapet  
 57 wall of variable height. The windward roof edges on low-rise structures cause a separation of the  
 58 boundary layer and generate vortex flow with large suction loading that is particularly severe for  
 59 oblique approaching wind angles. Changing the parapet height has a significant effect on these  
 60 wind suction loads because it alters the location of the roof corner vortex, which mitigates  
 61 extreme corner and edge suction loads with the tradeoff of increasing the downward roof loads in  
 62 certain cases [2-5]. In this study, the model parapet height was adjusted automatically using  
 63 servo-motors to create a particular design that is a "candidate" in the optimization framework.  
 64 The building envelope was instrumented with pressure taps to measure the envelope pressure  
 65 loading. The taps were densely spaced on the roof to provide sufficient resolution to capture the  
 66 change in roof corner vortex formation. A modified particle swarm optimization (PSO)  
 67 algorithm was implemented to achieve optimum parapet height which minimized suction on the  
 68 roof and parapet surfaces. Experiments were conducted in the BLWT located at the University of  
 69 Florida Experimental Facility (UFEF) of the National Science Foundation's (NSF) Natural  
 70 Hazard Engineering Research Infrastructure (NHERI) program.

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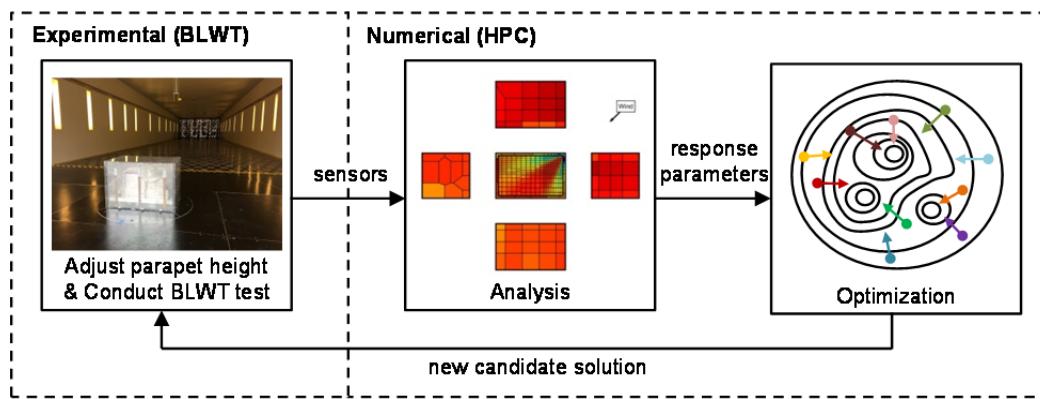


Figure 1. Diagram of CPS framework for optimal design under wind loading

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## 2 CPS OPTIMIZATION FRAMEWORK

73 CPSs link the real world with the cyber world, leveraging the capabilities of computers to  
 74 monitor and control physical attributes [6]. Common components of CPSs include sensing,  
 75 actuation, and communication systems for interfacing, computation for executing numerical  
 76 models or algorithms, and a physical phenomenon of interest. The applications for CPS in civil  
 77 engineering are diverse, including hybrid simulation [7-9], online health monitoring and model  
 78 updating [10], and decision-making frameworks [11]. In civil engineering, experimental testing  
 79 is essential to capture complex behavior for which numerical models are insufficient, e.g., strong  
 80 nonlinearities, new devices and materials, and complex loads such as wind loads on bluff bodies.  
 81 Physical models that capture these behaviors can be linked to numerical algorithms to create a  
 82 versatile cyber-physical framework. Experimental testing has experienced a revolution through  
 83 the use of CPS. Applications including the substructuring of physical systems and the  
 84 substructuring of optimization algorithms are explored below.

85 In civil engineering, the first use of CPS as an experimental method began in earthquake  
 86 engineering with what is now known as hybrid simulation [7,12,13]. Hybrid simulation is a type  
 87 of hardware-in-the-loop (HIL) test where the structural system is separated into numerical and  
 88 experimental components that are linked together through a loop of action and reaction using  
 89 actuators and sensors. In this way, the entire structural system is evaluated with a cost savings in  
 90 the numerical components and enhanced realism in the experimental components. Hybrid  
 91 simulation traditionally uses an extended time-scale for the experimental components, capturing  
 92 the quasi-static nonlinear behavior of the specimen while modeling damping and inertia  
 93 numerically. The development of rate-dependent structural control devices such as base isolation  
 94 bearings and fluid dampers spurred interest in expanding hybrid simulation to run both  
 95 experimental and numerical components in real time. The first modern real-time hybrid  
 96 simulation (RTHS) was conducted by Nakashima et al. on a SDOF system [14].

97 Figure 2 shows an incomplete set of applications of CPS in civil engineering with a focus  
 98 on experimental testing in earthquake and wind engineering. HIL testing has been developed for  
 99 earthquake engineering in the form of hybrid simulation and RTHS. Similar HIL frameworks can  
 100 be developed for wind engineering to study complex problems such as progressive failure and  
 101 fluid-structure interaction, represented by the dashed boxes with X's under the *Hardware-in-the-Loop Testing*  
 102 group in Figure 2.

103 Another opportunity for CPS in civil engineering is a substructuring of the optimization  
 104 process, shown in the *Cyber-Physical Optimization Group* in Figure 2. Key to this framework is  
 105 the numerical exploration of the design space coupled with the experimental creation and  
 106 evaluation of a candidate designs. Experimental evaluation can take the form of either traditional  
 107 testing methods (e.g., BLWT) or HIL methods (e.g., RTHS). The former is explored in this paper  
 108 using a mechatronic specimen to explore candidate designs subject to accurate wind loading  
 109 created using a BLWT. This application is termed "loop-in-the-model" optimization (LIMO)  
 110 because the model is iteratively adapting toward an optimal configuration. The name is  
 111 complementary to "model-in-the-loop" or "hardware-in-the-loop" testing where instead of  
 112 substructuring a physical system, a physical system's properties are iteratively adjusted through  
 113 optimization. Additional possibilities for cyber-physical optimization are identified with dashed  
 114 boxes and X's in Figure 2, for example, hardware-in-the-loop optimization (HILO), which  
 115 combines HIL testing with LIMO.

116 There are many opportunities for developing new cyber-physical experimental techniques  
 117 across civil engineering as identified in Figure 2. This study takes a new approach, namely the  
 118 substructuring of the optimization process, to create a new family of experimental methods with  
 119 rich possibilities for improving structural design.

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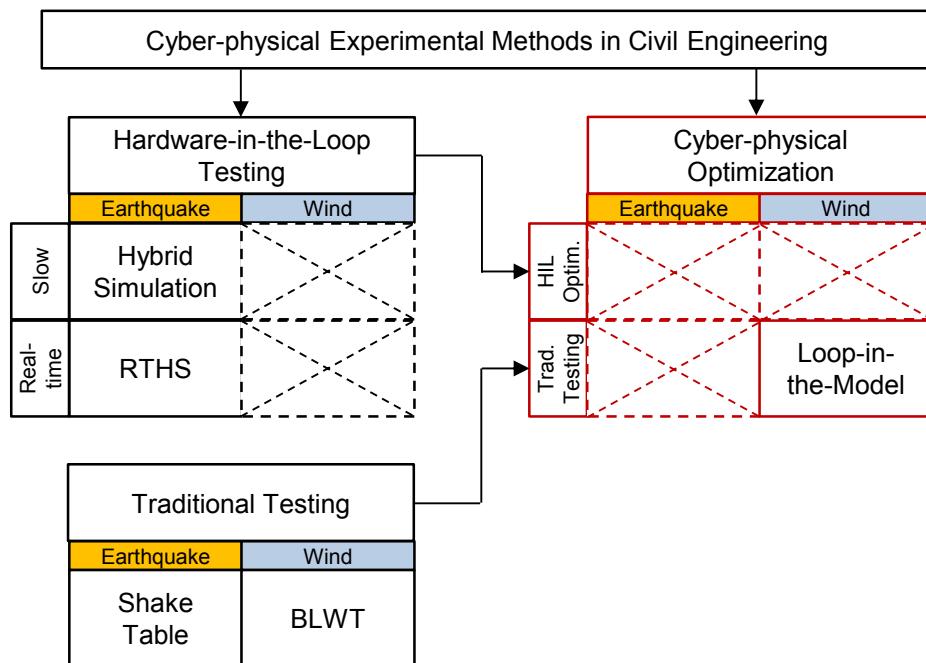
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Figure 2. CPS experimental methods in earthquake and wind engineering.

## 123 3 OPTIMIZATION ALGORITHMS

124 A cyber-physical optimization framework (e.g. LIMO) can be built around any optimization  
 125 algorithm by replacing the evaluation of a numerical model with physical testing. Popular  
 126 optimization algorithms are broadly categorized as gradient-based or metaheuristic.  
 127 Metaheuristic algorithms are problem independent and better suited for solving multi-objective  
 128 and constrained problems without the need for gradient information [15-16]. These algorithms  
 129 broadly explore candidate solutions within a search space to avoid premature or local  
 130 convergence, which can lead to non-intuitive solutions for complex optimization problems. At  
 131 the same time, metaheuristics are stochastic in nature, and therefore there is no guarantee that a  
 132 global optimal solution, or even bounded solution, will be found [17].

133 Particle swarm optimization (PSO) is the metaheuristic algorithm selected for the proof-  
 134 of-concept in this study. PSO mimics social behavior where a population of individuals (swarm)  
 135 adapts to its environment by discovering and jointly exploring promising regions. This swarm  
 136 intelligence method is based on the simulation of social interactions of members of a species,  
 137 such as the movement of flocks of birds, schools of fish, and swarm of bees. Its development was  
 138 inspired by evolutionary programming, genetic algorithms, and evolution strategies and shares  
 139 similarities with genetic algorithms and evolutionary algorithms.

140 In the context of structural engineering, the swarm represents a group of candidate design  
 141 solutions. Each particle within the swarm is a candidate design which consists of an  $N$ -  
 142 dimensional finite position and velocity. The position refers to the values of  $N$  design parameters  
 143 (e.g., parapet height of the structure) while the velocity refers to the change in the design  
 144 parameters from one iteration to the next. The position of the particles is often initially randomly  
 145 distributed throughout the design space. The swarm of particles then iteratively moves  
 146 throughout the search space seeking better positions with the goal of discovering the global best

147 solution. At each iteration, the particles' historic best costs and the swarm's historic best cost are  
 148 updated and used to determine the next particle positions. This process is repeated either for a  
 149 predetermined number of design iterations, or until user-defined convergence is reached.

150 The process for updating the position of each particle is  
 151

$$x_{j+1}^i = x_j^i + v_{j+1}^i \Delta t \quad (2.1)$$

152 where  $x_{j+1}^i$  is the position of particle  $i$  at iteration  $j + 1$ ,  $v_{j+1}^i$  is the corresponding velocity  
 153 vector of the particle, and  $\Delta t$  is the time step value.

154 The procedure for determining the velocity vector of each particle in the swarm depends  
 155 on the particular PSO algorithm. The equation commonly used for updating the velocity vector  
 156 was first introduced by Shi and Eberhart as  
 157

$$v_{j+1}^i = w v_j^i + c_1 r_1 \frac{(p_j^i - x_j^i)}{\Delta t} + c_2 r_2 \frac{(p_j^g - x_j^i)}{\Delta t} \quad (2.2)$$

158 where  $r_1$  and  $r_2$  are independent random numbers in the range  $[0,1]$ ,  $p_j^i$  is the best known  
 159 position of particle  $i$  considering iterations 1 through  $j$ ,  $p_j^g$  is the best known position of all  
 160 particles considering iterations 1 through  $j$ , and  $\Delta t$  is the time step value [18]. A unit time step  
 161 of one iteration is often used for  $\Delta t$ . In Equation 2.2, there are three problem-dependent  
 162 parameters that influence every particle's velocity: the inertia of the particle,  $w$  and two trust  
 163 parameters,  $c_1$  and  $c_2$ . The inertia controls the algorithm's exploration properties; a larger  
 164 inertia enables a more global search of the design space because particles are more inclined to  
 165 continue on their previous trajectory. The trust parameters indicate how much confidence the  
 166 current particle has in itself,  $c_1$  and in the swarm,  $c_2$  and will draw the particle to these  
 167 respective best positions. The selection of inertia and trust weights are problem dependent and  
 168 their values must be determined case-by-case. A poor selection of parameters may lead to  
 169 premature convergence to a solution that is not globally optimal, or at the other extreme, a  
 170 solution that takes an excessive number of iterations to converge. Parameter selection can be  
 171 made through trial and error or deduction and personal judgment.

## 172 4 PROOF-OF-CONCEPT MODEL DEVELOPMENT

173 Proof-of-concept for the CPS optimization framework is demonstrated for a low-rise building  
 174 with a parapet wall of variable height. The parapet height was controlled using linear stepper  
 175 motors. A single controllable design variable is sufficient for proof-of-concept and by limiting  
 176 the study to a single design variable, unnecessary mechanical complexity was avoided and focus  
 177 was instead placed on the optimization framework. While linear mechanical actuation was used  
 178 herein, other mechanical and material solutions can actuate more complex models. For example,  
 179 inflatable bladders or soft actuators can create controllable smooth geometries, smart materials  
 180 can create discrete changes in envelope features, and stiffness and damping changes can alter the  
 181 dynamic behavior of aeroelastic specimens. This CPS approach inherently loses some of the  
 182 flexibility of numerical modeling by requiring physical changes; however it produces realistic  
 183 loading on a structure through BLWT modeling.

184 In general, this CPS approach can be applied if the design parameter of interest can be  
185 controlled using a mechatronic specimen. For example, Elshaer et al. [19] explored the  
186 performance enhancement of tall buildings by optimizing the corner geometries using  
187 computational fluid dynamics (CFD). This problem can be recreated in a BLWT using a model  
188 with expandable bladders capable of creating a range of corner geometries. It is important when  
189 using this CPS approach to consider the search space for the optimization problem when  
190 designing the specimen. This approach can only consider changes which are physically possible.

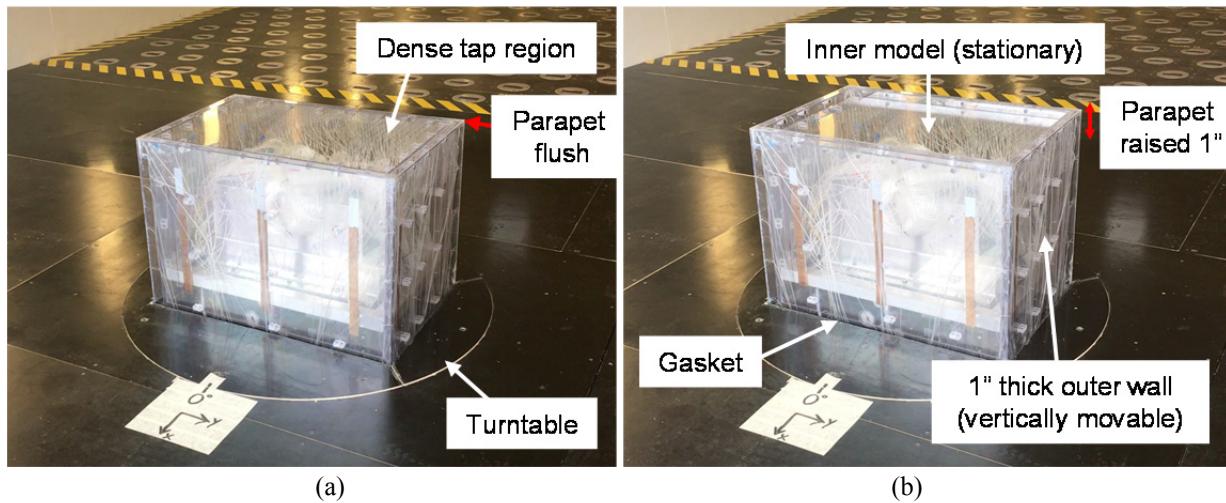
191 *4.1 Effects of wind on low-rise buildings with parapets*

192 Architectural detailing has a large influence on the distribution of pressures over a roof surface in  
193 magnitude, direction, and correlation. Wind approaching at oblique angles to a building with a  
194 flat roof produces strong vortices near the upwind corner and edges of the roof [20]. These  
195 vortices are similar to the vortices that are produced at the leading edge of delta type wings and,  
196 as such, are also known as delta wing vortices. These vortices create an area of high suction on  
197 the surface of the roof near the corner [21]. Parapet walls reduce these suction loads, preventing  
198 roof gravel and other loose material from becoming wind-borne debris that can damage a  
199 building's envelope and lead to wind and rain intrusion. Solid, continuous perimetric parapets  
200 taller than 1 m act to reduce both the mean and peak pressure coefficients most notably in the  
201 corner region of these buildings [22]. Most research regarding parapets has focused on  
202 characterizing the local pressure distributions on the roof surface, specifically for components  
203 and cladding. Some studies propose the use of parapets with non-uniform or modified geometries  
204 to reduce the extreme suction loads caused by the corner vortices [2]. Additionally, a few studies  
205 consider the effect of parapets on the underlying structural members [3, 23]. Recent studies  
206 reveal that it is essential to have a high density of pressure taps in the upwind corner region to  
207 ensure that the peak suction pressures are captured [2, 3, 20].

208 Most building codes, such as ASCE 7-10, allow for a pressure reduction over different  
209 regions of a roof in the presence of parapets; however there has not been extensive research  
210 conducted regarding accurate regions of reduction based upon the geometry of the building and  
211 parapet or on the optimal height of a parapet for a given low-rise building [1]. Additionally,  
212 research has primarily focused on the corner zones of roofs with limited research focusing on the  
213 edge and interior zones. The research regarding the edge and interior zones has mainly focused  
214 on mitigating local loading through the use of alternative geometries and not much regarding the  
215 effect of different heights of solid, perimetric parapets or on the optimal height of solid  
216 perimetric parapets [5].

217 *4.2 Model actuation*

218 The design parameter selected is the parapet wall height of a low-rise building. Candidate design  
219 solutions must be physically created in the BLWT such that their envelope wind loads are  
220 accurately measured. The outer wall of the model was actuated by four stepper motors, one at  
221 each corner of the model. The inner core of the model remained stationary, maintaining a  
222 constant building height. As the outer wall rose above the inner model, a parapet wall was  
223 created. Strips made from polytetrafluoroethylene (PTFE) were used between the inner model  
224 and outer wall to assist in achieving smooth linear actuation. A foam gasket was used between  
225 the outer wall and the turntable to allow the outer wall to move while preventing air from leaking  
226 around the model. The model is shown in Figure 3, including the inner model (stationary) and  
227 outer wall (vertically movable).

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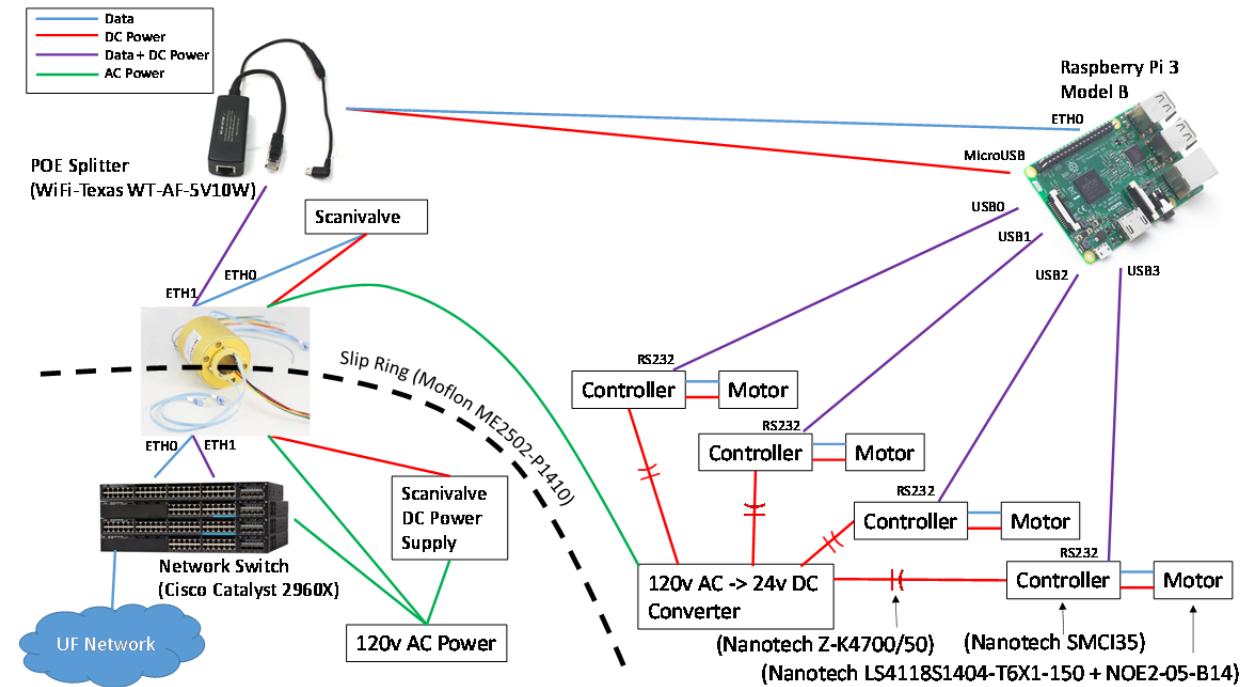
230 Figure 3. (a) Building model with a 0 inch parapet wall and (b) a 1 inch parapet wall

231 Nanotec stepper motors with a captured lead screw raised and lowered the outer wall  
 232 around the inner core of the model to change the eave height. The motors connected to the outer  
 233 wall using polycarbonate triangular supports installed in the bottom corners. A PVC pipe  
 234 installed around the drive shaft of the stepper motor protected the shaft from coming into contact  
 235 with any urethane pressure tap tubing during actuation. The stepper motor and its installation are  
 236 shown in Figure 4. The setup for controlling the stepper motors is given in Figure 5. Data (i.e.,  
 237 commands from the coordinating computer on the UF network) and power passed through a slip  
 238 ring on the BLWT turntable. A Raspberry Pi 3 was mounted within the turntable to take  
 239 commands from the coordinating computer and send to each of the four stepper motor  
 240 controllers, which in turn actuated the stepper motors. Encoders on the stepper motors provided  
 241 feedback to ensure the desired displacement was reached.

242



Figure 4. (a) Stepper motor and (b) stepper motor installed in corner of parapet wall with PVC shield



243

244

Figure 5. Wiring diagram for stepper motor control

245 

### 4.3 Model Geometry

246 The low-rise building was modeled after a two-story office building. A length-to-width ratio of  
 247 1.5 was selected to create a rectangular building shape. Model dimensions were selected as 29.25  
 248 inches  $\times$  19.50 inches in plan with a height of 20 inches. By actuating the outer wall, a parapet  
 249 wall of up to 4.5 inches model-scale was created. Urethane tubing and pressure taps were  
 250 installed on the outer and inner sides of the parapet wall. A total thickness of the model parapet  
 251 wall (and thus outer wall) of at least 1 inch was required to accommodate the thickness of  
 252 polycarbonate sheets, metal tubulation, and minimum bend radius for the urethane tubing. The  
 253 pressure taps on the outer and inner parapet walls were staggered to permit a thinner model  
 254 parapet wall.

255 Based on the model dimensions and target design of a two-story office building, a 1:18  
 256 model-scale was selected. This corresponds to a building with full-scale dimensions of 29.6 feet  
 257  $\times$  44.4 feet in plan, 30 feet tall, and a 1.5 foot thick parapet. According to the Building Code  
 258 Requirements for Masonry Structures, parapet walls should have a thickness of at least 8 inches  
 259 [24]. The building model represents a realistic two-story full-scale building with a two by three  
 260 bay steel frame.

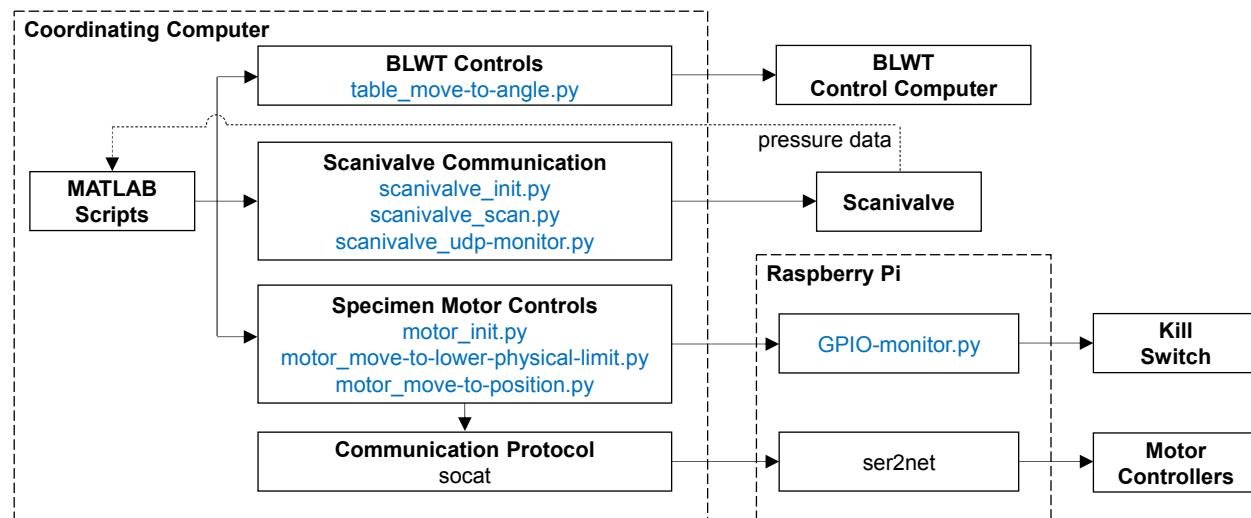
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## 5 CYBER-PHYSICAL EXPERIMENTAL SETUP

262 In the proof-of-concept developed for this paper, the loop-in-the-model optimization was driven  
 263 by a numerical optimization algorithm executed in MATLAB on a coordinating computer [25].  
 264 The algorithm determined which candidate designs to evaluate, after which the cyber-  
 265 infrastructure actuated the specimen to physically create these designs in the BLWT. The  
 266 pressures on the model building surfaces were measured using pressure scanners and metadata  
 267 was recorded for the atmospheric pressure, reference wind velocity, and humidity. Tests were

268 repeated over all desired wind angles. The data and metadata were accessed by the coordinating  
 269 computer where a MATLAB script evaluated the objective function for each candidate design.  
 270 The optimization algorithm used the results for each candidate design within an iteration to  
 271 determine the candidate designs for the next iteration. After testing, data and metadata were  
 272 stored in the data repository of the NHERI DesignSafe web portal for later access by researchers  
 273 [26].

274 The communication framework between the cyber and physical components is shown in  
 275 Figure 6, a complement to the wiring diagram of Figure 5. The coordinating computer runs the  
 276 basic MATLAB scripts for the duration of the optimization. The MATLAB scripts execute  
 277 python scripts to interface with external systems, including the UFEF's BLWT Control  
 278 Computer to change the specimen angle, Scanivalve for data acquisition, and Raspberry Pi for  
 279 motor control.



280  
 281 Figure 6. Links between cyber-physical components

## 282 5.1 Experimental equipment

283 Experiments were conducted in the BLWT located at the University of Florida Natural Hazard  
 284 Engineering Research Infrastructure (NHERI) Experimental Facility. The BLWT is 6.1 m wide  
 285 with a 1 m turntable centered along the 6.1 m width 31.75 m downwind of 8 fans. The fans were  
 286 kept at 1050 RPM for all testing, which corresponds to a reference height velocity of  
 287 approximately 14 m/s. The pressures on the model building surfaces were measured using  
 288 Scanivalve ZOC33 [27]. The model building installed in the BLWT is shown in Figure 7.



289

290

Figure 7. Boundary layer wind tunnel with model low-rise building, upwind view

291 *5.2 Tap tributary areas*

292 The pressure measured at each pressure tap was assumed to act over a unique and non-  
293 overlapping tap tributary area on the model surface. In this model, tap locations were variable  
294 due to the moving outer wall. Based on the parapet wall height, exposed tap locations and  
295 surface areas were calculated. Then, tap tributary areas were calculated using Voronoi diagrams  
296 derived from Delaunay triangulation [28]. This process is both reproducible and automated,  
297 which was particularly important because the geometry of the building changes with every  
298 candidate solution. The taps and tributary areas for the model with a parapet wall of 5 inches are  
299 depicted in the flattened view of Figure 8. The walls of the building are given by Surfaces 1 to 4.  
300 As the walls extended above the roof (from actuation), Surfaces 1 to 4 also formed the outer  
301 parapet walls. The inner parapet walls are given by Surfaces 6 to 9. The edges that join the outer  
302 walls (Surfaces 1 to 4) and the inner parapet walls (Surfaces 6 to 9) in Figure 8 are at the same  
303 height in the model. Surfaces 5 and 10 are the top of the parapet wall and the roof, respectively.  
304 As the parapet height increased, the tributary areas for both the outer wall and inner parapet  
305 walls increased while the tributary areas for the top of the parapet wall and the roof remained  
306 constant.  
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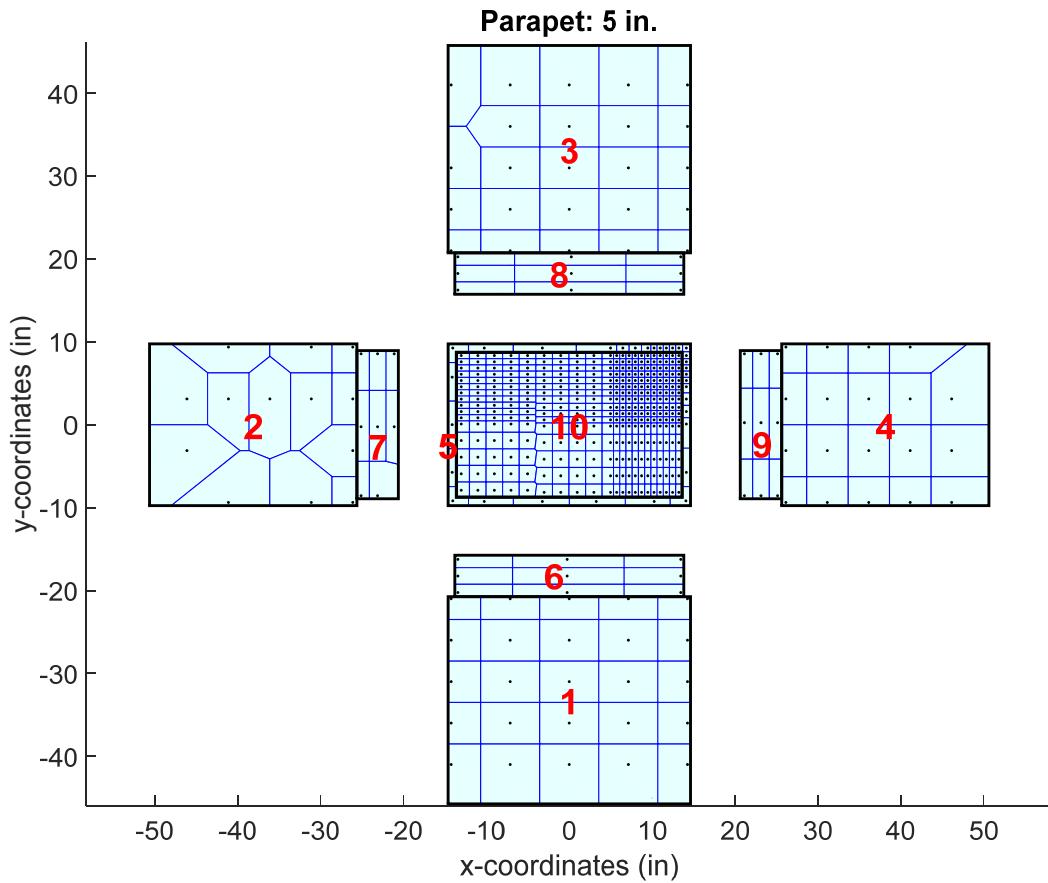


Figure 8. Tap locations and tributary areas on a flattened representation of the model with a parapet of 5 inches

308 5.3 Wind simulation

309 Simulation of upwind terrain roughness was performed via the Terraformer, an automated  
 310 roughness element grid that rapidly reconfigures the height and orientation of 1116 roughness  
 311 elements in a  $62 \times 18$  grid to achieve desired upwind terrain conditions [29]. The grid has a fetch  
 312 length of 18.3 m. Dimensions of the elements are 5 cm by 10 cm, and they are spaced 30 cm  
 313 apart in a staggered pattern. Height and orientation can be varied from 0-160 mm and 0-360  
 314 degrees, respectively. For this study, the Terraformer was configured to simulate open terrain for  
 315 the given geometric scale (1:18).

316 Prior to placing the model in the tunnel, flow measurements were taken at the center of  
 317 the test section using an automated gantry system instrumented with four Turbulent Flow  
 318 Instrumentation Cobra pressure probes that measure  $u$ ,  $v$ , and  $w$  velocity components and static  
 319 pressure. For this study, roughness elements were raised to 20 mm and oriented with the wide  
 320 edge perpendicular to the flow. Figure 9 includes the mean velocity profile and the measured  
 321 longitudinal turbulence spectra at a height of 610 mm. The mean velocity profile was normalized  
 322 by the reference mean wind velocity  $U_{\text{ref}}$  measured at a height  $z_{\text{ref}} = 1.48$  m. A roughness length  
 323 estimate of 1.59 mm was obtained from a non-linear least-squares fit of the log law in the  
 324 inertial-sublayer (ISL) region ( $z \sim 150\text{-}900$  mm), following the curve-fitting method in  
 325 Karimpour et al. [30]. This results in an equivalent full-scale roughness length of 0.029 m, which

326 is within the range of open terrain as defined in ASCE 7-10. The measured spectra was  
 327 compared with the power spectra model in ESDU [31], and first derived by von Kármán for  
 328 isotropic turbulence [32]. The measured longitudinal integral length scale ( $L_u^x$ ) in the tunnel at  $z$   
 329 = 610 mm was 1.06 m. For a 1:18 simulation, this results in a full-scale  $L_u^x = 18$  m ( $z \sim 11$  m),  
 330 which is ~16% of the expected  $L_u^x$  for open terrain – e.g., for  $z_0 = 0.03$  m and  $z = 10$  m,  $L_u^x$   
 331 = 110 m [33]. The challenges associated with achieving sufficient length scales of turbulence in  
 332 the BLWT for large models (e.g., low-rise buildings) are well established [34, 35]. The  
 333 discrepancy in  $L_u^x$  (model versus full-scale) arises from the absence of large-scale turbulence in  
 334 the BLWT. Recent methods, such as partial turbulence simulation [36], have been successful in  
 335 compensating for a lack of large-scale turbulence. Nevertheless, the mismatch in integral lengths  
 336 does not detract from the fundamental objective of applying CPS approaches in the BLWT.  
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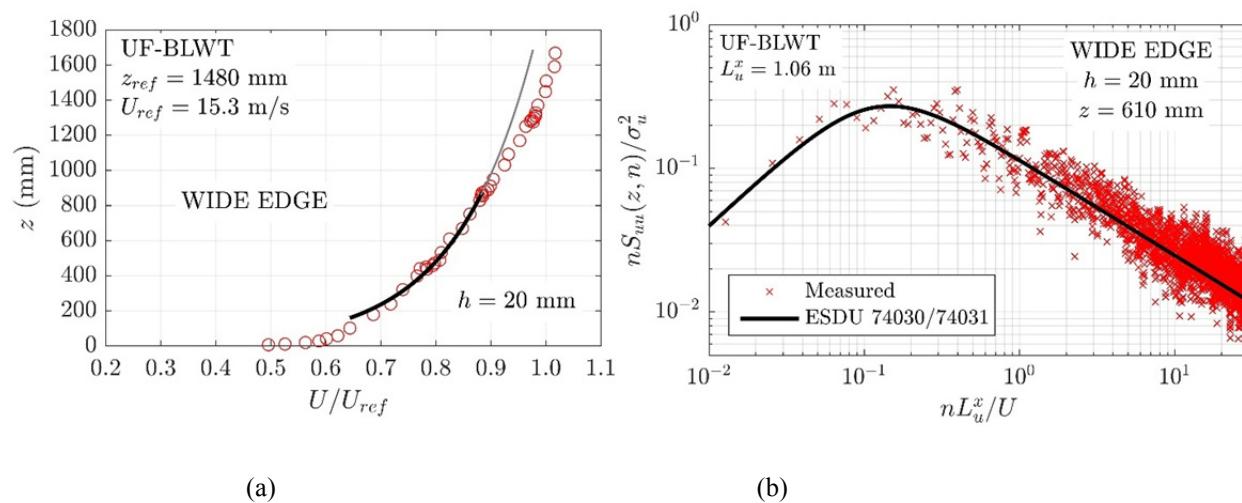


Figure 9. (a) Mean velocity profile and (b) longitudinal turbulence spectra ( $z = 610$  mm) measured at the center of the test section for  $h = 20$  mm and a wide edge windward element orientation.

### 338 5.4 Pressure coefficients

339 Differential pressures from 512 taps were measured simultaneously and sampled at 625 Hz. Data  
 340 was collected for 120 seconds, corresponding to approximately 660 seconds full-scale assuming  
 341 a basic wind speed of 40 m/s at reference height. Pressure coefficients were referenced to the  
 342 velocity pressure at the model eave height. This velocity pressure was obtained indirectly by  
 343 applying a reduction factor to pitot tube measurements at the freestream ( $z = 1.48$  m). Maximum  
 344 and minimum pressure coefficients were estimated from each tap pressure time history using a  
 345 Fisher-Tippett Type I (Gumbel) distribution [37]. The  $C_p$  time history was truncated into 50  
 346 segments of equal length. The peak maximum and minimum pressure coefficients from each  
 347 segment were then taken, and the 78<sup>th</sup> percentile is then used to estimate the maximum and  
 348 minimum  $C_p$  values.

## 349 6 OPTIMIZATION

350 The optimization problem was physically constrained by the model-scale minimum and  
 351 maximum parapet height of 0 and 4.5 inches, respectively. The lower and upper physical bounds  
 352 were chosen such that the optimal solution would confidently be located within the search space.  
 353 Considering the time limits on experimental resources, a balance was needed between sufficient  
 354 particles to create the PSO swarm effect and sufficient iterations to converge. Based on an  
 355 estimated two minutes per BLWT run, one minute to set up the BLWT run, and a day of testing,  
 356 five particles were selected.

357 The objective function was selected as a minimization of the suction on the roof, inner  
 358 parapet walls, and top of the parapet considering all wind angles (Surfaces 5-10) in Figure 8. As  
 359 the parapet height increased, the suction decreased for the roof surface and top of the parapet  
 360 wall and increased for the inner parapet wall surfaces. Critical minimum  $C_p$  values were  
 361 observed for the roof, inner parapet wall, and top of parapet at approach wind angles of 45° and  
 362 90° (Figures 10 and 11). To minimize the number of BLWT runs, each candidate solution was  
 363 only evaluated at 45° and 90° with the dense roof taps upwind.

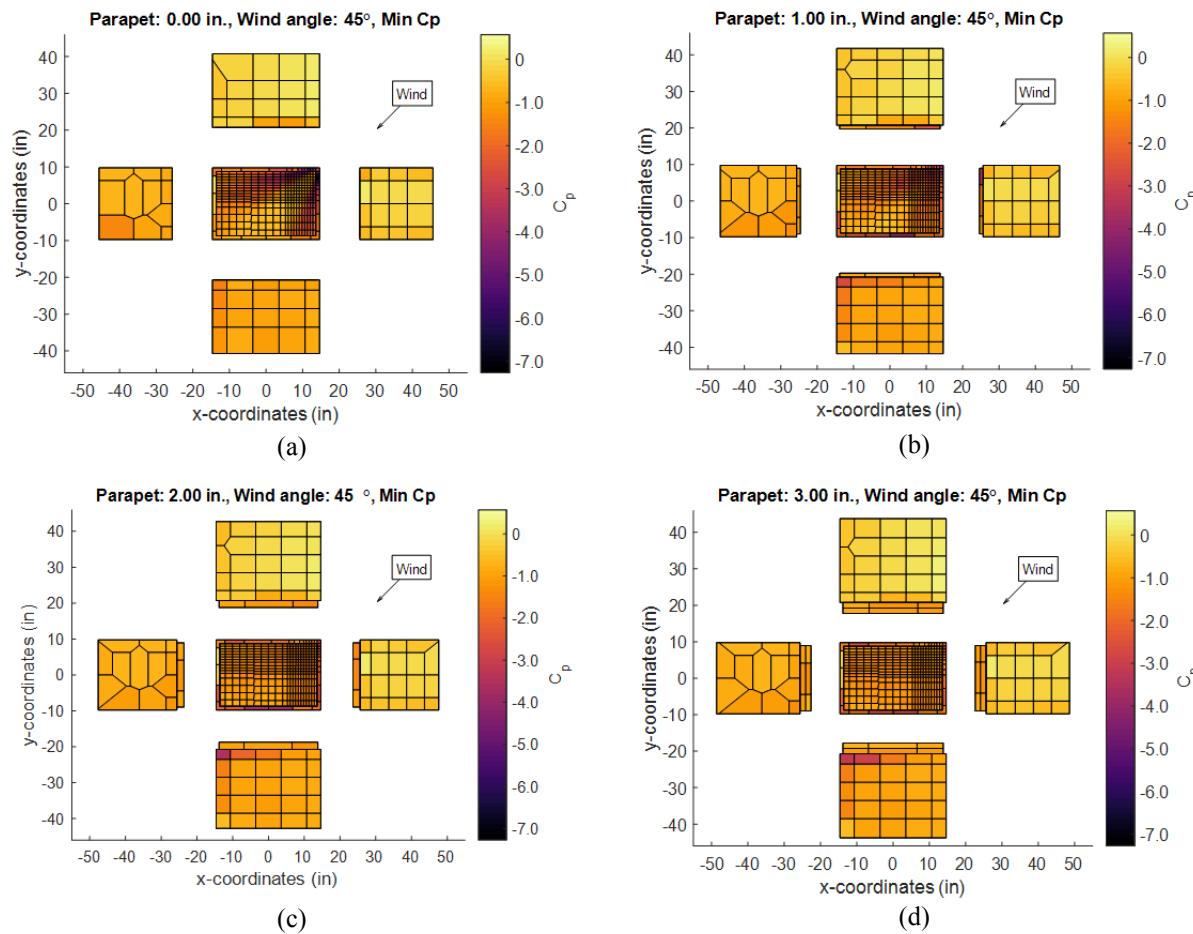


Figure 10. Minimum  $C_p$  for 45°, (a) 0 inch parapet, (b) 1 inch parapet, (c) 2 inch parapet, and (d) 3 inch parapet

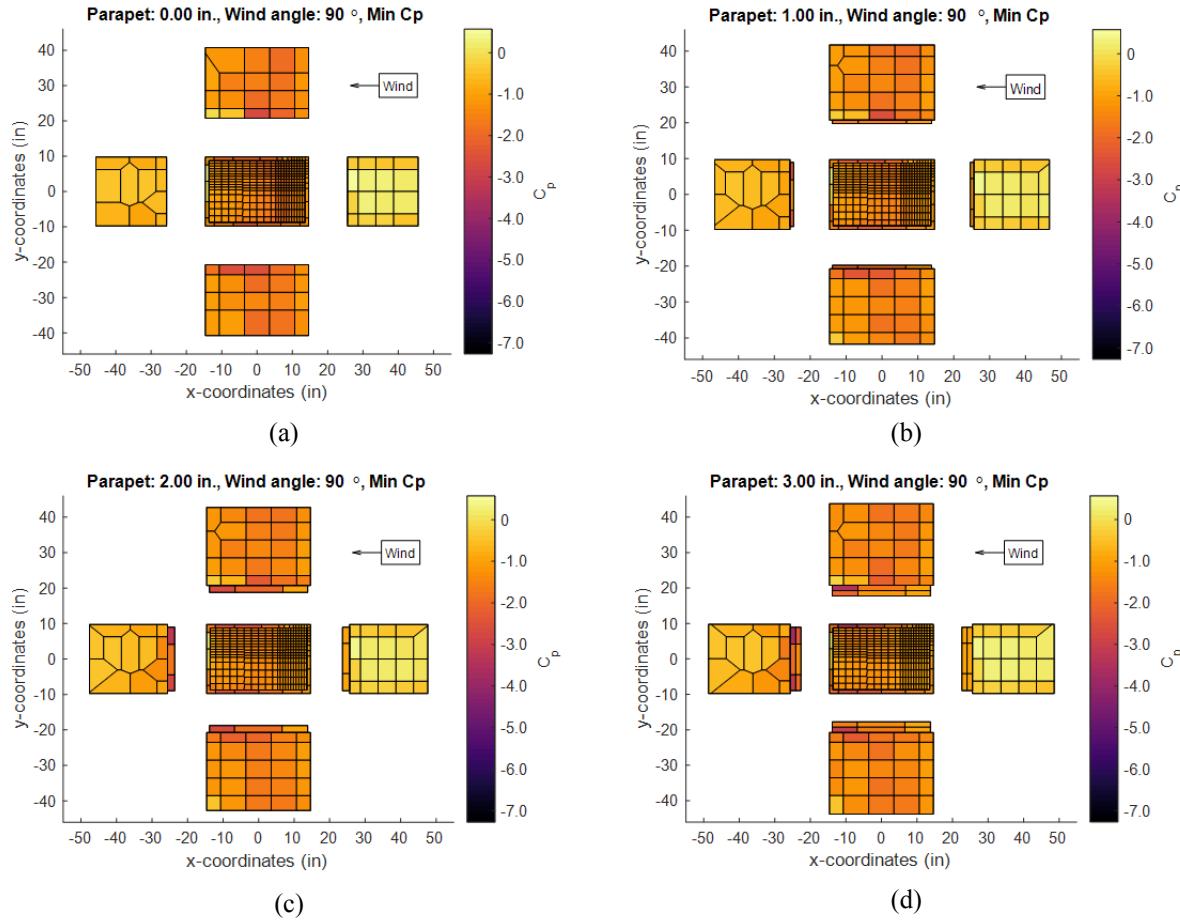


Figure 11. Minimum  $C_p$  for 90°, (a) 0 inch parapet, (b) 1 inch parapet, (c) 2 inch parapet, and (d) 3 inch parapet

The experiments were driven by a modified PSO algorithm. Modifications were made to increase the computational efficiency and reduce the number of experiments required. Traditional PSO does not address particles which violate design constraints. Thus, constrained optimization was introduced to address this problem through the use of a fly-back mechanism. In the traditional fly-back mechanism, a particle that would violate a design constraint is prevented from moving for that iteration. The algorithm proceeds as normal for the next iteration. The global minima (or maxima, depending on objective) of design problems are often close to the boundaries of the feasible search space [38]. The traditional fly-back mechanism will exploit solutions around the boundaries. In this study, the solution is not expected to be near the boundaries. Therefore, in addition to preventing the particle from moving beyond the boundary, the direction of the velocity is reversed (i.e., the velocity now points away from the boundary). This modification enables better exploration of the interior of the search space.

The cyber-physical optimization approach specialized for PSO, a predetermined set of evaluation wind angles, and the proof-of-concept parapet model is shown in Figure 12. Loops over all angles, all particles, and all iterations are highlighted to clearly illustrate the experimental timeline.

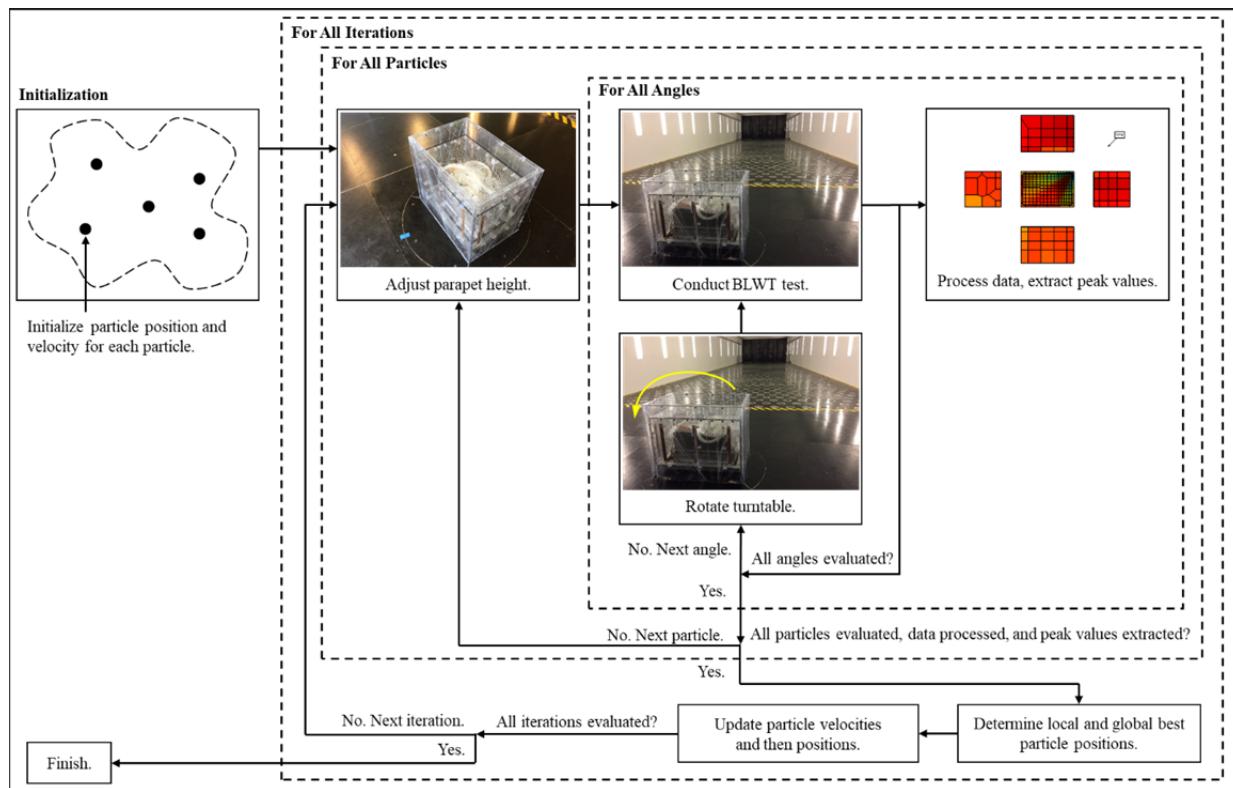


Figure 12. Cyber-physical optimization approach as implemented with PSO

380  
381

## 382 7 OPTIMIZATION RESULTS AND ANALYSIS: CASE 1

383 The problem-specific PSO parameters of  $w$ ,  $c_1$ , and  $c_2$  are all selected as 0.5. These values  
 384 produced favorable convergence for a simulated (offline) optimization run using a pre-recorded  
 385 test matrix of wind angles and parapet heights. To initialize the (online) optimization run, the  
 386 position of the particles was uniformly distributed across the range of positions. A total of 13  
 387 design iterations were conducted for the 5 particles. The convergence of the particles towards the  
 388 optimum height of 2.69 inches is shown in Figure 13a. Four of the five particles converged to the  
 389 global best cost. The one particle that did not converge is likely due to the particle being attracted  
 390 to both its personal best cost (achieved at iteration 1) and the global best cost. Methods to avoid  
 391 particles becoming stuck will be considered in Section 8. The global best cost for each iteration  
 392 is shown in Figure 13b. Points with both particle number and cost identified represent an update  
 393 to the global best cost. Figures 14 and 15 depict the envelope plot of the minimum  $C_p$  for the  
 394 optimal parapet height at 45° and 90° respectively. This illustrates the balance in minimum  $C_p$  on  
 395 the roof and top of the parapet wall (Figure 14) and inner parapet wall surfaces (Figure 15). This  
 396 balance is expected because the suction on the roof, top of the parapet, and inner parapet walls  
 397 were given equal weight in the objective function.

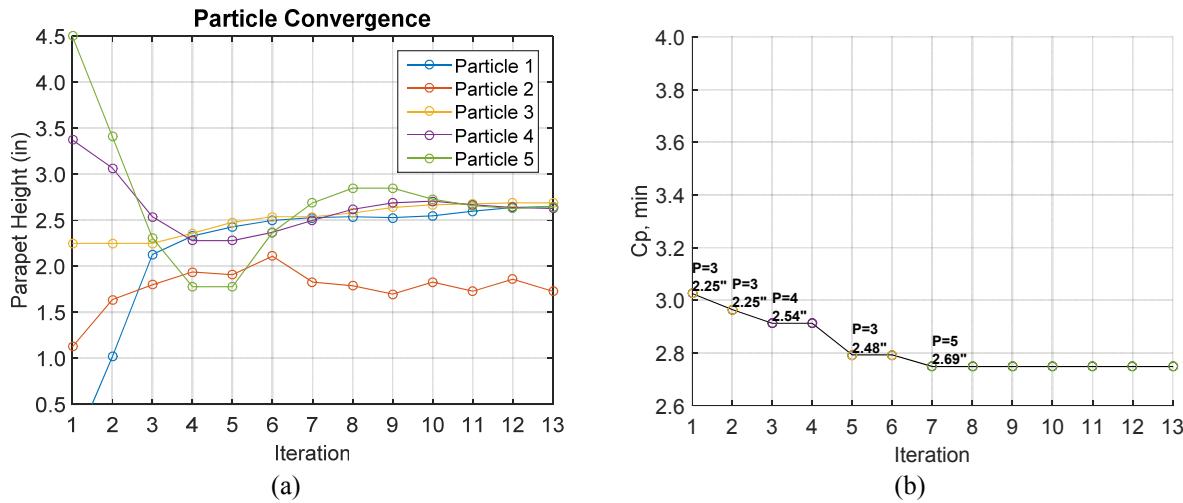
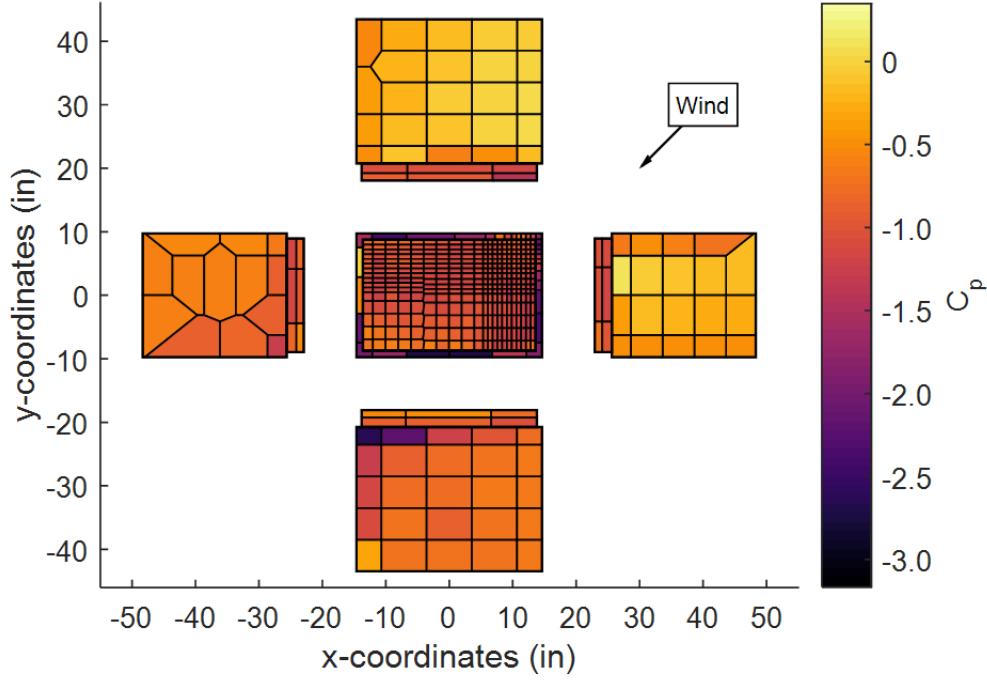
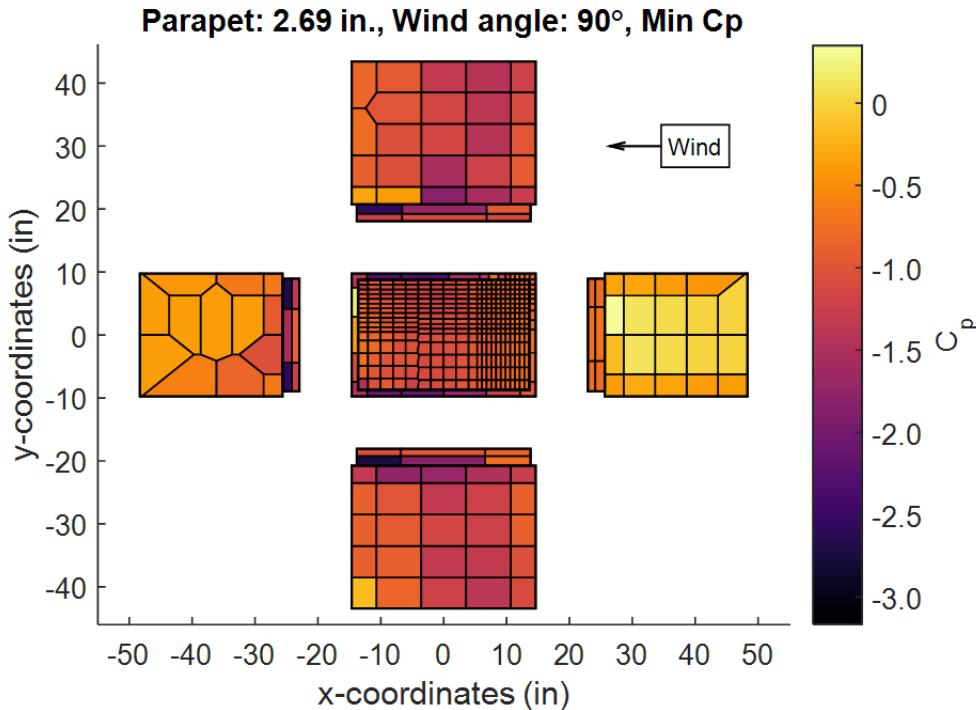


Figure 13. (a) Particle convergence at each iteration and (b) Iteration history of global best cost

398 The optimal result corresponds to a full-scale parapet height of 4.04 feet, an otherwise  
 399 non-intuitive design. This parapet height simultaneously minimizes suction on the roof and inner  
 400 parapet walls. According to the Building Code Requirements for Masonry Structures, the height  
 401 of structural parapets should not exceed 3 times their thickness [24]. The optimal height found  
 402 satisfies this limit of 4.5 feet as applied to the current building.

**Parapet: 2.69 in., Wind angle: 45°, Min Cp**Figure 14. Minimum  $C_p$  for optimal parapet height, 45° wind angle shown

Figure 15. Minimum  $C_p$  for optimal parapet height, 90° wind angle shown

## 403 8 OPTIMIZATION RESULTS AND ANALYSIS: CASE 2

404 Two additional PSO modifications are proposed to improve the accuracy of the cyber-physical  
 405 approach to optimization by addressing issues which arise with both the cyber and physical  
 406 components. The issues of premature convergence (cyber) and sensitivity to outliers (physical)  
 407 are identified and modifications are introduced for evaluation in a second optimization run.

408 8.1 *Smartest particle: avoid premature convergence*

409 PSO can prematurely converge to solutions found in early iterations if not properly calibrated  
 410 [39]. Recalling Equation 2.2, the calculation of the velocity vector for each particle at iteration  $j$   
 411 depends on the best known position of all particles considering iterations 1 through  $j$ . If the  
 412 global best position corresponds to a local optimum, then premature convergence may occur as  
 413 all particles are attracted to this solution. If weight is placed on the position of the particle which  
 414 found the global best position, rather than the global best position itself, then premature  
 415 convergence can be avoided. This particle, the "smartest" particle, will encourage continued  
 416 exploration by avoiding stagnation of the  $p_j^g$  term.

417 Following the current position of the global best particle rather than its global best  
 418 positions leads to a new definition for velocity updates

419

$$v_{j+1}^i = w v_j^i + c_1 r_1 \frac{(p_j^i - x_j^i)}{\Delta t} + c_2 r_2 \frac{(x_j^g - x_j^i)}{\Delta t} \quad (8.1)$$

420 where  $r_1$  and  $r_2$  are independent random numbers in the range  $[0,1]$ ,  $w$  is the inertia of the  
 421 particle,  $c_1$  and  $c_2$  are two trust parameters indicating a particle's trust in itself and trust in the  
 422 swarm respectively,  $p_j^i$  is the best known position of particle  $i$  considering iterations 1 through  
 423  $j$ ,  $x_j^g$  is the position at iteration  $j$  of the particle  $g$  which determined the best known position  
 424 of all particles considering iterations 1 through  $j$ , and  $\Delta t$  is the time step value.

425 *8.2 Forgetting function: avoid sensitivity to outliers*

426 BLWT testing is subject to experimental error; results will vary from experiment to experiment,  
 427 even for the same specimen configuration. Data may be associated with a specimen  
 428 configuration that is not truly representative of that configuration. With regard to PSO, outlier  
 429 data can affect both a particle's local best solution and the swarm's global best solution. Even if  
 430 the results are not repeatable, they may be retained as the local or global best solution for the  
 431 remainder of the optimization. Outliers can potentially cause convergence to a position that does  
 432 not accurately represent the global best position. To address the variability of wind tunnel  
 433 testing, a modification to the PSO algorithm is proposed.

434 A "forgetting function" is introduced to the swarm so that particles within the swarm  
 435 suffer a partial loss of memory and "forget" both global and local best solutions. In evaluating  
 436 global and local best costs, the modified PSO algorithm will only consider solutions that have  
 437 been created within a specified number of previous iterations. The corresponding positions for  
 438 this limited horizon will become the new global and local best particle positions. If the solution  
 439 of a particular parapet height was the result of an outlier experiment, then it will eventually be  
 440 forgotten, and the global and local best particle positions would be updated in its absence. With  
 441 the forgetting function, the convergence to the global solution may no longer be monotonic.

442 After offline simulations using Case 1 test data, the number of iterations to consider for  
 443 global and local best calculations is selected to be 5 (i.e., the current iteration and 4 previous  
 444 iterations).

445 *8.3 Optimization results and analysis*

446 The problem-specific parameters of  $w, c_1$ , and  $c_2$  are selected to be 0.5, 1.0, and 1.0  
 447 respectively so that an equal weight would be placed on the particle's inertia, trust in itself, and  
 448 trust in the swarm by giving the products of  $c_1 r_1$  and  $c_2 r_2$  each a mean of 0.5. The position of  
 449 the particles was initially randomly distributed across the range of positions. A total of 15 design  
 450 iterations were conducted for the 5 particles. The convergence of the particles towards the  
 451 optimum height of 2.70 inches is shown in Figure 16a. The global best cost for each iteration is  
 452 shown in Figure 16b, and the results are similar to those of Figure 13b. Figures 17 and 18 depict  
 453 the envelope plot of the minimum  $C_p$  for the optimal parapet height at  $45^\circ$  and  $90^\circ$  respectively,  
 454 and the results are similar to those of Figures 14 and 15. The optimal result corresponds to a full-  
 455 scale parapet height of 4.05 feet, an otherwise non-intuitive design which satisfies the limit of 4.5  
 456 feet according to the Building Code Requirements for Masonry Structures as applied to the  
 457 current building [24].

458 In comparison to the modified PSO used in Case 1 which had four of five particles  
 459 converge to the global best cost (Figure 13a), all five particles converged to the global best cost  
 460 with the incorporation of the smartest particle (Figure 15a). The loss of diversity of individuals

461 within a population is a symptom of premature convergence because of the loss of the  
 462 exploration capabilities of the individuals. This loss of diversity can be seen in Figure 13a as  
 463 multiple particles are close to one another in position and follow similar search paths, whereas  
 464 the particles in Figure 16a retain their diversity.

465 In comparison to the modified PSO used in Case 1 which had a monotonically  
 466 converging global best cost, the global best cost non-monotonically converges with the  
 467 incorporation of the forgetting function. The global best position determined at iteration 10 of  
 468 2.68 inches attracts all particles to this height. Despite repeated testing of this particular position  
 469 after it is found to be the global best position, the position of 2.70 inches is found to produce a  
 470 better cost once the particular test at iteration 10 is forgotten. This suggests that the solution  
 471 found to be the global best at iteration 10 was not representative of the height of 2.68 inches and  
 472 can be considered an outlier. Similarly, the solution at 2.70 inches may be an outlier, which  
 473 would be revealed by continued testing.

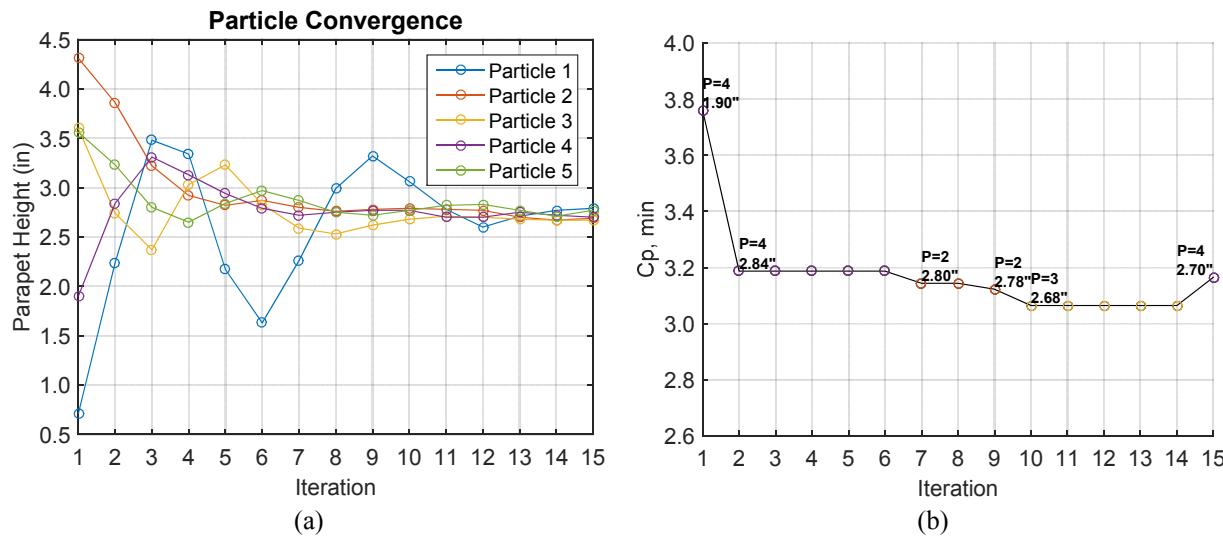
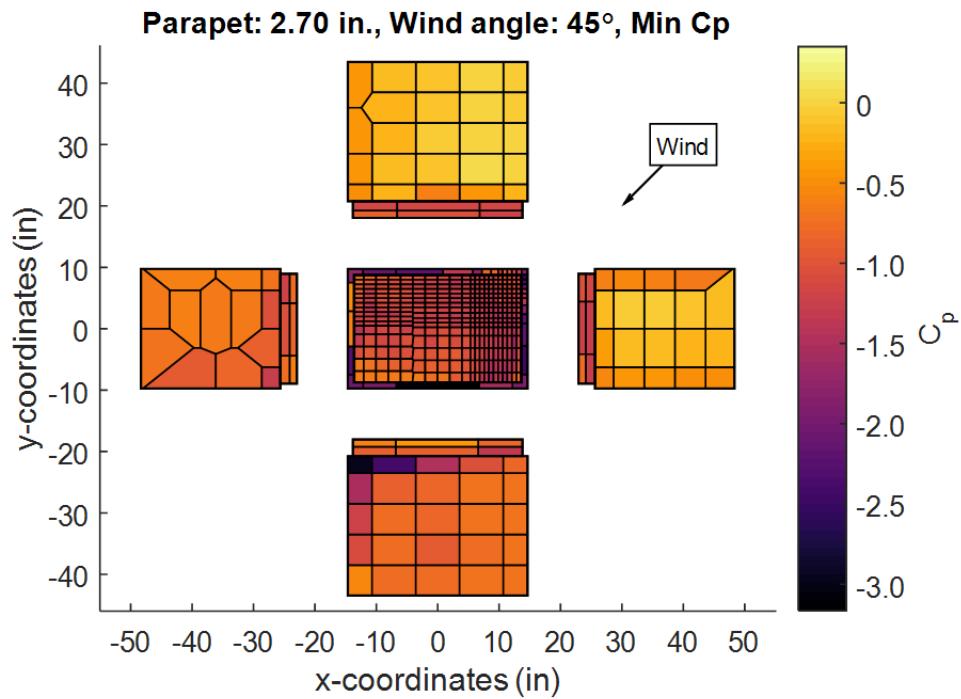
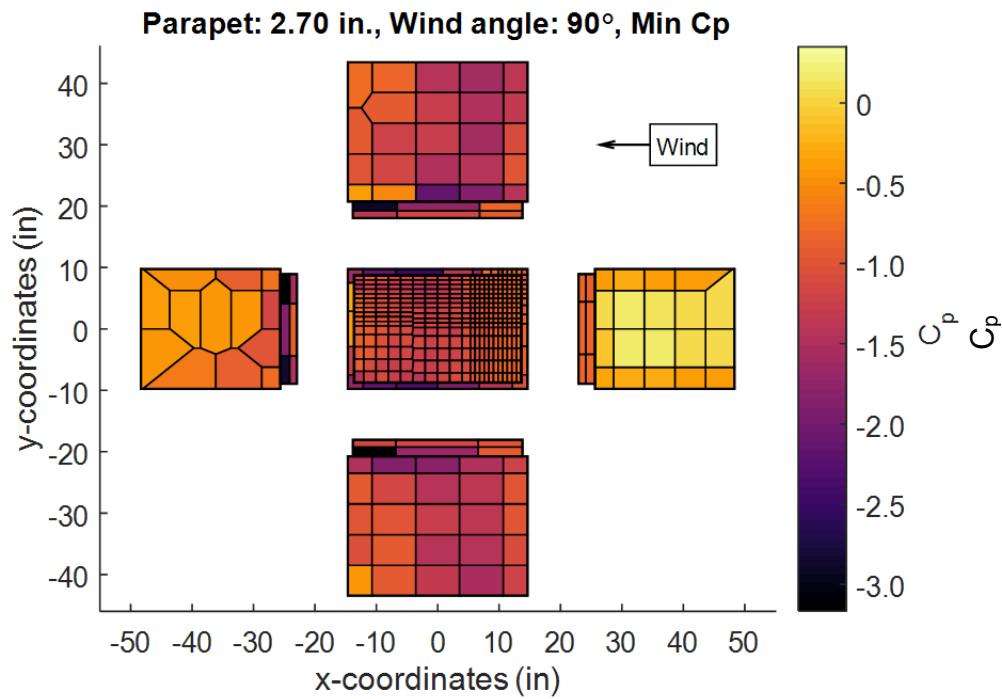


Figure 16. (a) Particle convergence at each iteration and (b) Iteration history of global best cost

Figure 17. Minimum  $C_p$  for optimal parapet height, 45° wind angle shownFigure 18. Minimum  $C_p$  for optimal parapet height, 90° wind angle shown

## 474 9 CONCLUSIONS

475 This study explores a cyber-physical system (CPS) approach to the optimal design of structures  
476 subject to wind loading. The optimization process is substructured into cyber and physical  
477 components, creating a new loop-in-the-model optimization (LIMO) framework. The analysis of  
478 data, calculation of objective functions, and determination of new candidate designs is done  
479 numerically. The creation and evaluation of candidate designs is completed physically in a  
480 boundary layer wind tunnel (BLWT) using a mechatronic specimen. The framework was  
481 demonstrated to automatically guide the physical structure to an optimal state based on user-  
482 defined objectives and constraints. The LIMO framework enables the optimal solution to be  
483 found quicker than brute force methods, in particular for complex structures with many design  
484 variables. The integration of metaheuristic search algorithms will enable the discovery of new  
485 and non-intuitive designs, all while placing the burden of design iteration on an accurate and  
486 automated system. Successful implementation will simplify and enhance the design workflow  
487 and ultimately advance our capability to build stronger and more resilient structures.

488 As proof-of-concept, this study investigated the effect of wind loads on low-rise  
489 buildings with a solid parapet of variable height, creating an optimization problem with a single  
490 design variable that has a non-monotonic influence on the envelope wind load. This study  
491 focuses on envelope load effects, seeking the parapet height that minimizes roof and parapet wall  
492 suction loading. The optimization algorithm selected was particle swarm optimization (PSO);  
493 however the framework is flexible and could be guided by any gradient-based (i.e., using finite  
494 differences) or metaheuristic algorithms. Based on the objective function and constraints chosen,  
495 optimal parapet heights of 2.69 inches model-scale and 4.04 feet full-scale (Case 1) and 2.70  
496 inches model-scale and 4.05 feet full-scale (Case 2) were found for the low-rise structure studied  
497 using the modified PSO algorithms. The findings are potentially significant for more complex  
498 structures where the optimal solution may not be obvious and cannot be easily determined with  
499 traditional experimental or computational methods.

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