

The dependence of planetary tectonics on mantle thermal state: Applications to early Earth evolution

Bradford J. Foley^{1,*}

¹Department of Geosciences, Pennsylvania State University,
University Park, PA, 16802

*Corresponding author. E-mail: bjf5382@psu.edu. Phone:
(814)-863-3591

Abstract

For plate tectonics to operate on a planet, mantle convective forces must be capable of forming weak, localized shear zones in the lithosphere that act as plate boundaries. Otherwise, a planet's mantle will convect in a stagnant lid regime, where subduction and plate motions are absent. Thus, when and how plate tectonics initiated on Earth is intrinsically tied to the ability of mantle convection to form plate boundaries; however, the physics behind this process are still uncertain. Most mantle convection models have employed a simple pseudoplastic model of the lithosphere, where the lithosphere "fails" and develops a mobile lid when stresses in the lithosphere reach the prescribed yield stress. With pseudoplasticity high mantle temperatures and high rates of internal heating, conditions relevant for the early Earth, impede plate boundary

formation by decreasing lithospheric stresses, and hence favor a stagnant lid for the early Earth. However, when a model for shear zone formation based on grain size reduction is used, early Earth thermal conditions do not favor a stagnant lid. While lithosphere stress drops with increasing mantle temperature or heat production rate, the deformational work, which drives grain size reduction, increases. Thus the ability of convection to form weak plate boundaries is not impeded by early Earth thermal conditions. However, mantle thermal state does change the style of subduction and lithosphere mobility; high mantle temperatures lead to a more sluggish, drip-like style of subduction. This “sluggish lid” convection may be able to explain many of the key observations of early Earth crust formation processes preserved in the geologic record. Moreover, this work highlights the importance of understanding the microphysics of plate boundary formation for assessing early Earth tectonics, as different plate boundary formation mechanisms are influenced by mantle thermal state in fundamentally different ways.

1 Introduction

Plate tectonics has fundamentally shaped the tectonic, thermal, and chemical evolution of the Earth, leaving our planet in sharp contrast to its neighbors in the solar system. However, despite the importance of plate tectonics for Earth’s history, when and how plate tectonics started on Earth is poorly constrained [e.g. *Condie and Kröner, 2008; van Hunen and Moyaen, 2012; Cawood et al., 2013; Korenaga, 2013*]. Few rocks from the Archean survive today, and those that exist are difficult to inter-

pret. For even earlier times, greater than 4 billion years ago, zircon grains are all that is available to constrain the dynamics of the very early Earth [Valley *et al.*, 2002; Harrison *et al.*, 2005; Kemp *et al.*, 2010]. Moreover, exactly what evidence would constitute clear proof for plate tectonics is still debated, as rocks formed by plate tectonic processes on the modern Earth can potentially be formed by non-plate-tectonic processes on the early Earth [Bédard, 2006; Johnson *et al.*, 2014; Sizova *et al.*, 2015], among other ambiguities. As a result, estimates for when plate tectonics began based on the geologic record span from > 4.0 Ga [Harrison *et al.*, 2005; Hopkins *et al.*, 2008] to < 1.0 Ga [Stern, 2005].

Determining how and when plate tectonics began on Earth is not only an important question for understanding the history of our own planet, but also for the more general question of what factors allow for the development of plate tectonics on any rocky planet. Earth is the only rocky planet or moon known to operate in a plate-tectonic regime; the other rocky bodies in the solar system are thought to operate in some form of stagnant lid regime [e.g. Breuer and Moore, 2007]. Interestingly, the icy satellite Europa potentially exhibits subduction, and possibly even full fledged plate tectonics, in its outer icy shell [Kattenhorn and Prockter, 2014]. However, more work is needed to determine whether potential subduction zones are spatially limited, akin to Venus as discussed below, or more widespread. In the stagnant lid regime, the surface exists as a single plate with mantle convection taking place beneath this plate, and there is no global network of subduction zones and mid-ocean ridges, or large-scale differential movement between different regions of the lithosphere [e.g. Ogawa *et al.*, 1991; Solomatov, 1995]. Stagnant lid planets

58 or satellites can still display volcanism and active tectonics, as seen on Mars [e.g.
59 *Neukum et al.*, 2004; *Robbins et al.*, 2011], Mercury [e.g. *Byrne et al.*, 2014], or Io
60 [e.g. *O'Reilly and Davies*, 1981; *Moore*, 2003]. In fact, Venus even shows evidence
61 for limited subduction in some regions, possibly due to burial of the lithosphere by
62 volcanism, and subsequent “peeling” away and sinking of this buried lithosphere [e.g.
63 *Sandwell and Schubert*, 1992; *Davaille et al.*, 2017], a process called “plume-induced”
64 subduction [*Gerya et al.*, 2015]. However, all of these planets and satellites clearly
65 lack the global system of mobile plates and plate boundaries that characterizes plate
66 tectonics on Earth.

67 Plate tectonics is also thought to play an important role in Earth’s ability to
68 maintain a surface environment suitable for life [e.g. *Kasting and Catling*, 2003; *Foley*
69 *and Driscoll*, 2016]. Plate tectonics helps power the geodynamo through efficient
70 cooling of the mantle and core [*Nimmo*, 2002; *Driscoll and Bercovici*, 2014], and
71 the resulting magnetic field helps to shield the planet from harmful radiation [e.g.
72 *Grieffmeier et al.*, 2005]. Moreover, plate tectonics facilitates carbon cycling between
73 the surface and interior, which helps to maintain temperate surface temperatures
74 on Earth thanks to a feedback between climate, silicate weathering, orogeny, and
75 volcanism [*Walker et al.*, 1981; *Tajika and Matsui*, 1992; *Franck et al.*, 1999; *Sleep and*
76 *Zahnle*, 2001; *Berner*, 2004; *Abbot et al.*, 2012; *Foley*, 2015]. Stagnant lid planets may
77 also be capable of establishing a carbon cycle that regulates climate [e.g. *Lenardic*
78 *et al.*, 2016; *Tosi et al.*, 2017; *Noack et al.*, 2017; *Foley and Smye*, 2018], though
79 current estimates still find that plate tectonics is the more favorable tectonic state
80 for long-term climate stability [*Foley and Smye*, 2018]. With the ongoing boom

81 in exoplanet discoveries now revealing that rocky planets are common in the galaxy
82 [[Batalha, 2014](#)], understanding the dynamical causes of plate tectonics has become an
83 increasingly important goal in astrobiology, in addition to earth science [e.g. [Valencia](#)
84 [et al., 2007](#); [O'Neill and Lenardic, 2007](#); [Kite et al., 2009](#); [Valencia and O'Connell,](#)
85 [2009](#); [Korenaga, 2010b](#); [Stamenkovic et al., 2011](#); [van Heck and Tackley, 2011](#); [Foley](#)
86 [et al., 2012](#); [Lenardic and Crowley, 2012](#); [Stein et al., 2013](#)].

87 While continued work in unraveling the Earth's early geologic record is essential
88 for answering the question of when plate tectonics began, theoretical studies on early
89 Earth mantle dynamics provide a key additional constraint, by demonstrating what
90 styles of mantle convection are geodynamically plausible. Theoretical studies can
91 also help in interpreting geologic observations by, for example, testing the feasibility
92 of different processes for generating Archean crust. Moreover, theoretical models
93 can also be readily extended to Venus, Mars, or Mercury, providing additional tests
94 on theories behind the origin of plate tectonics on Earth. That is, any theory must
95 be able to explain the presence of plate tectonics on Earth and its absence on the
96 other rocky planets in our solar system. In this paper I focus on the rheological
97 mechanisms necessary for generating plate like mantle convection, and the constraints
98 we can place on early Earth (specifically the Hadean and Archean) tectonics from
99 our understanding of these mechanisms. In particular, I highlight that attempting to
100 model the microphysics of plate boundary formation, in this case by modeling grain
101 size evolution, leads to new predictions about early Earth tectonics in comparison
102 to previous geodynamic models that treat the lithosphere as a plastic material. The
103 differences in the model results stem from fundamental differences in the physics

underlying the two plate generation mechanisms. As a result, in order to truly understand how and when plate tectonics began on Earth, and what factors are necessary for plate tectonics to begin on any rocky planet, we must understand the microphysics of shear localization and plate boundary formation.

1.1 Generating plate tectonics from mantle convection

The geodynamics behind the stagnant lid regime seen on planets such as Mars and Mercury has been well studied, and can be simply understood as a result of the strong temperature dependence of mantle rheology. Temperature dependent viscosity creates a strong, rigid lithosphere and thus confines convection to the warmer mantle interior where viscosity is lower [e.g. *Ogawa et al.*, 1991; *Solomatov*, 1995]. Plate tectonics then requires that some additional mechanism, that allows mantle convective forces to form narrow weak zones within the high viscosity lithosphere, such that plates can slide past each other and subduct beneath one another, be present. A strongly non-linear rheology, where regions of high stress or deformation become weaker than areas of low stress or deformation, has proven successful in forming plate boundaries and generating a “mobile lid” form of convection [e.g. *Weinstein and Olson*, 1992; *Moresi and Solomatov*, 1998; *Tackley*, 2000]. In this study I define the mobile lid regime as one where subduction of surface material into the mantle occurs and drives lithospheric mobility. Mobility of the lithosphere may be slow compared to typical fluid velocities in the mantle interior (a “sluggish lid” regime), exhibit varying degrees of episodicity, or fail to produce truly rigid plates. But as long as subduction of surface material that drives surface motion takes place,

126 convection is in the mobile lid regime. In fact, forming genuinely plate-like behav-
 127 ior is still a challenge today, as models typically fail to form strike-slip faults, truly
 128 rigid plates, or single-sided subduction [Bercovici *et al.*, 2015], though some of these
 129 features can be created in select cases [e.g. Gerya, 2010; Crameri *et al.*, 2012]. As
 130 a result, I will focus on the “mobile lid” regime (rather than the “plate-tectonic”
 131 regime) in contrast to the stagnant lid regime in this paper.

132 Although non-linear rheologies can generate mobile lid convection, the mechanism
 133 (or mechanisms) behind such rheological behavior are still not well understood [e.g.
 134 Bercovici *et al.*, 2015]. One commonly used mechanism is the pseudoplastic yield
 135 stress rheology [e.g. Fowler, 1993; Moresi and Solomatov, 1998; Tackley, 2000; Stein
 136 *et al.*, 2004; van Heck and Tackley, 2008; Lowman, 2011]. Here the lithosphere
 137 is assumed to have a finite strength, the yield stress, and fails when this stress is
 138 reached; failure of the lithosphere results in the formation of weak shear zones and
 139 mobility of the lithosphere. With the pseudoplastic rheology, the stress state in
 140 the lithosphere is critical for whether convection sits in a mobile lid or stagnant
 141 lid regime, as stresses in the lithosphere must reach the yield stress for weak plate
 142 boundaries to form.

143 While the pseudoplastic rheology is capable of producing plate-like mantle convec-
 144 tion, yield stress values far below that which are inferred from laboratory experiments
 145 [e.g. Mei *et al.*, 2010] or observations of lithospheric flexure [e.g. Zhong and Watts,
 146 2013], are typically needed to produce mobile lid convection [e.g. Moresi and Soloma-
 147 tov, 1998; Tackley, 2000; van Heck and Tackley, 2008; Solomatov, 2004; Korenaga,
 148 2010a]. It is thus unclear whether pseudoplasticity is capable of explaining the pres-

149 ence of plate tectonics on Earth; that is, additional weakening mechanisms may be
150 needed. One possible explanation is that hydration of old lithosphere could weaken
151 it, and make the effective strength low enough for yielding at subduction zones [*Ko-*
152 *renaga*, 2007]. It has also been proposed that channelized flow in the asthenosphere
153 enhances stresses, and may allow lithospheric yielding even without any weakening
154 via hydration [*Höink et al.*, 2012]. However, more work is needed to confirm whether
155 these hypotheses can fully reconcile the pseudoplastic yielding mechanism for gen-
156 erating plate tectonics with experimental and observational constraints of Earth’s
157 lithospheric strength.

158 Nevertheless the pseudoplastic rheology has been used in previous studies on
159 early Earth tectonics. A key feature of the Hadean and Archean Earth is that the
160 thermal state of the mantle was likely significantly different than at the present.
161 Rates of radiogenic heat production were higher [e.g. *Turcotte and Schubert*, 2002;
162 *Korenaga*, 2006] and the mantle interior was likely hotter as well. Mantle potential
163 temperatures could have been as high as ~ 2000 K just after planetary accretion
164 ended, and the putative magma ocean solidified [e.g. *Abe*, 1997; *Solomatov*, 2000],
165 though there is little physical evidence of the mantle thermal state at this early
166 stage of Earth’s history. In the Archean, petrological estimates indicate the mantle
167 was $\sim 100 - 200$ K hotter than the present day potential temperature of $\approx 1350^\circ$
168 C, and has gradually cooled since the Archean [e.g. *Herzberg et al.*, 2010; *Keller*
169 *and Schoene*, 2018]. However, high temperatures, similar to those inferred for the
170 Archean, may still prevail in some parts of the lower mantle, as evidenced by rocks,
171 thought to be sourced from a deep seated mantle plume, recording temperatures as

172 high as $\sim 1700^\circ \text{C}$ [*Trela et al., 2017*].

173 These generally warmer thermal conditions expected in the Hadean and Archean
174 mantle can change the lithospheric stress state, and thus influence the early Earth's
175 propensity for plate tectonics, at least as it would be generated with pseudoplastic
176 yielding. In particular, many studies have found that higher mantle temperatures
177 decrease the magnitude of stresses in the lithosphere, thus requiring lower yield stress
178 values for mobile lid convection; that is, stagnant lid convection becomes more likely
179 with increasing mantle temperature [e.g. *Stein et al., 2004*; *O'Neill et al., 2007*].
180 Moreover, the relative amounts of internal versus basal heating plays an important
181 role as well, as basal heating has been found to feature higher lithospheric stresses
182 than internally heated convection [e.g. *O'Neill et al., 2016*; *Weller and Lenardic,*
183 *2016*; *Korenaga, 2017*].

184 However, different mechanisms for generating plate tectonics from mantle convec-
185 tion have been proposed, and such mechanisms may respond differently to changes
186 in mantle thermal state. In particular, I focus here on grain size reduction as it is
187 commonly seen in exhumed lithospheric shear zones [*White et al., 1980*; *Drury et al.,*
188 *1991*; *Jin et al., 1998*; *Warren and Hirth, 2006*; *Skemer et al., 2010*], and viscosity
189 decreases with decreasing grain size when deformation is accommodated via diffusion
190 creep or grain boundary sliding [e.g. *Hirth and Kohlstedt, 2003*]. Whether grain size
191 reduction is a viable plate generation mechanism has been questioned, however, be-
192 cause grain size reduction by dynamic recrystallization takes place in the dislocation
193 creep regime, while grain size sensitive flow only occurs in the diffusion creep or grain
194 boundary sliding regimes [e.g. *Etheridge and Wilkie, 1979*; *De Bresser et al., 1998*;

195 [Karato and Wu, 1993](#)]. If grain size reduction cannot continue once deformation
196 has entered a grain size sensitive flow regime, only modest weakening can occur [e.g.
197 [De Bresser et al., 2001](#); [Montési, 2013](#)]. However, grain size reduction can continue
198 within the diffusion creep regime when a secondary phase (e.g. pyroxene) is dispersed
199 throughout the primary phase (e.g. olivine), because of the combined effects of dam-
200 age to the interface between phases and Zener pinning (where the secondary phase
201 blocks grain growth of the primary phase). Warping of the interface between phases
202 (or interface damage) itself drives grain size reduction, and such warping can occur
203 via any solid state creep mechanism [[Bercovici and Ricard, 2012](#)]. Recent experi-
204 mental studies confirm that the presence of secondary phases significantly enhances
205 grain size reduction, especially as phases begin to mix at high strain [[Bercovici and](#)
206 [Skemer, 2017](#); [Cross and Skemer, 2017](#); [Tasaka et al., 2017a, b](#)].

207 Grain size reduction has been shown to be an effective mechanism for generating
208 mobile lid convection on Earth, and explaining its absence on the other terrestrial
209 planets of our solar system [[Landuyt and Bercovici, 2009](#); [Foley et al., 2012](#)]. However
210 it should be noted that plate tectonics on Earth can only be explained with grain size
211 reduction for certain ranges of the key model parameters (specifically the damage
212 partitioning fraction and grain growth activation energy, defined below in §2.1), and
213 that these parameters are not well constrained experimentally. As a result, further
214 work constraining these parameters, as well as the theoretical formulation for grain
215 size evolution used in this and similar studies, is needed to test the viability of grain
216 size reduction as a mechanism for explaining the operation of plate tectonics on
217 Earth.

218 In this paper I show that a grain size reduction mechanism for generating plate
219 boundaries responds to changes in mantle temperature in a fundamentally different
220 way than pseudoplastic yielding. Specifically, new mantle convection calculations
221 are presented that demonstrate that deformational work, which drives grain size re-
222 duction in the lithosphere, increases with increasing internal heating rate, and con-
223 sequently increasing mantle temperature. Thus the situation is opposite that of the
224 pseudoplastic rheology, where higher internal heating rates or mantle temperatures
225 lead to lower stresses, thereby favoring a stagnant lid. As a result, a transition to the
226 stagnant lid regime at high mantle temperatures or high internal heating rates is not
227 seen when grain size reduction is considered. However, subduction and lithospheric
228 mobility does become more sluggish, and subduction becomes more episodic and
229 drip-like. These changes in subduction style have potentially important implications
230 for interpreting early Earth geological and geochemical observations, as discussed in
231 §4.2. The paper is structured as follows: the numerical model setup and governing
232 equations used in this study are described in §2; numerical results and scaling anal-
233 yses are presented in §3; the implications of the results are described in §4; and the
234 main conclusions and future directions needed to making progress on answering the
235 question of when plate tectonics started are summarized in §5 & §6, respectively.

2 Background Theory and Model Setup

2.1 Grain damage theory

I use a formulation for grain size evolution referred to as grain damage; it is based on energetics, as reducing grain size in a volume of rock is equivalent to increasing the surface energy in that volume [e.g. *Bercovici et al., 2001a, b; Bercovici and Karato, 2003; Austin and Evans, 2007; Landuyt et al., 2008; Bercovici and Ricard, 2012, 2013, 2014; Foley and Bercovici, 2014; Foley et al., 2014*]. The grain damage formulation used in this study is a simplified version of the theory for polyminerallic rocks from *Bercovici and Ricard [2012]*, which provides equations for the evolution of grain size in the different mineral phases and for the curvature of the interface between phases. *Bercovici and Ricard [2012]* shows that during deformation of a polyminerallic aggregate, a “pinned state” develops, where secondary phases dispersed through the primary phase “pin” grain boundaries, thereby slowing grain growth. Furthermore, in the pinned state the curvature of the interface between phases, or the interface roughness, controls the average grain size of the mineral phases; i.e. grain size becomes proportional to interface roughness in the pinned state. Assuming the pinned state prevails throughout the mantle thus simplifies the model, as the average grain size of a rock volume can now be tracked by one equation, rather than solving for both mineral phases and the interface roughness separately. That is, one can use the equation governing the interface roughness (equation 4d of *Bercovici and Ricard [2012]*) to solve for the grain size directly. I therefore assume the pinned state prevails throughout the mantle in this study.

258 An additional simplifying assumption I employ is that diffusion creep is the dom-
 259 inant deformation mechanism throughout the entire mantle, and dislocation creep,
 260 or any other deformation mechanism, can be neglected. Neglecting dislocation creep
 261 can potentially impact the results, as in reality the rheology will be controlled by
 262 whichever mechanism, diffusion creep or dislocation creep, can accommodate defor-
 263 mation the easiest [e.g. [Rozel et al., 2011](#)]. In particular, the typical grain size in the
 264 mantle interior could grow large enough at high mantle temperatures for dislocation
 265 creep to become the preferred deformation mechanism in this region. However, the
 266 results are unlikely to be significantly impacted by neglecting dislocation creep, as
 267 lid mobility is controlled by the effective rheology of shear zones in the lithosphere,
 268 where grains are small and diffusion creep dominates [[Foley and Bercovici, 2014](#)].
 269 Moreover, in the numerical models grain sizes in the mantle interior remain rela-
 270 tively small, typically lower than a few millimeters, even with high internal heating
 271 rates and thus high interior mantle temperatures (see §3.3). Dislocation creep would
 272 also cause viscous weakening in high stress regions, such as around downgoing slabs
 273 or beneath surface plates [e.g. [Jadamec and Billen, 2010](#)]. However, damage also
 274 leads to weakening in such locations (e.g. see §3.1), so this effect of neglecting dis-
 275 location creep is also unlikely to significantly influence the results. I also note that
 276 in the shallow lithosphere, additional creep mechanisms, such as low temperature
 277 plasticity, can become important [[Karato, 2008](#); [Kohlstedt and Mackwell, 2010](#); [Mei](#)
 278 [et al., 2010](#); [Thielmann, 2017](#)]. However, as explained above, diffusion creep is the
 279 dominant deformation mechanism in shear zones that have undergone significant
 280 grain size reduction. It is thus unclear if including low temperature plasticity would

281 significantly affect plate generation with grain damage.

282 Assuming the pinned state prevails also means that mineral phases are assumed
283 to always be well mixed, when in reality mixing occurs only after extensive defor-
284 mation [e.g. [Bercovici and Skemer, 2017](#); [Cross and Skemer, 2017](#); [Tasaka et al.,](#)
285 [2017a, b](#)]. Phase mixing is more efficient at small grain sizes, and thus damage also
286 becomes more effective at small grain sizes due to pinning and interface damage. As
287 a result, grain size itself influences the rate of grain size reduction, an effect that
288 is not captured in the models presented here. Including the effect of phase mixing
289 on grain size evolution is an important goal for future work, as it may improve the
290 plate-like nature of mobile lid convection produced via grain damage, by enhancing
291 shear localization [[Bercovici and Ricard, 2016](#)].

292 The above assumptions result in the following theoretical formulation of grain
293 damage used in this study. The mantle viscosity, μ , is a function of grain size and
294 temperature as expected for diffusion creep [e.g. [Hirth and Kohlstedt, 2003](#)]:

$$\mu = \mu_n \exp\left(\frac{E_v}{RT}\right) \left(\frac{A}{A_0}\right)^{-m}, \quad (1)$$

295 where μ_n is a constant, E_v is the activation energy for diffusion creep ($E_v = 300$ kJ
296 mol⁻¹ [[Karato and Wu, 1993](#)]), R is the universal gas constant, T is temperature, A is
297 fineness or inverse grain size, A_0 is a reference fineness, and m is a constant. A grain
298 size sensitivity exponent of $m = 2$ is used, the expected value for Nabarro-Herring
299 creep, or diffusion through the grain [e.g. [Hirth and Kohlstedt, 2003](#)].

300 The evolution of fineness follows

$$\frac{DA}{Dt} = \frac{f}{\gamma} \Psi - hA^p, \quad (2)$$

301 where t is time, f is the damage partitioning fraction, which can vary from zero
 302 to one, γ is the surface free energy, Ψ is the rate of deformational work, h is the
 303 healing rate, and p is a constant (I use $p = 4$, as estimated for polyminerallic rocks
 304 by *Bercovici and Ricard* [2012]). Deformational work rate is defined as $\Psi = \nabla \underline{v} : \underline{\tau}$,
 305 where $\underline{v}$ is velocity and $\underline{\tau}$ is the stress tensor. The first term on the right-hand
 306 side of (2) states that some fraction, f , of the deformational work partitions into
 307 surface energy, thereby reducing the grain size (or increasing fineness). The second
 308 term on the right-hand side of (2) represents normal grain growth, which acts to
 309 increase grain size (or reduce fineness). The healing rate constant, h , is a function
 310 of temperature with an Arrhenius form:

$$h = h_n \exp \left(-\frac{E_h}{RT} \right) \quad (3)$$

311 where h_n is a constant and E_h is the activation energy for grain growth. The value
 312 of E_h for polyminerallic rocks is not well known, because most grain growth exper-
 313 iments have been conducted on monominerallic samples. However, *Mulyukova and*
 314 *Bercovici* [2017] found that dynamic recrystallization experiments and observations
 315 from natural shear zones, where smaller grain sizes are found at lower temperatures,
 316 can be well fit with a grain growth activation energy of $E_h \approx 400$ kJ/mol. More-
 317 over, the damage partitioning fraction, f , could also be temperature-dependent, with

larger values of f found at lower temperatures [Rozel et al., 2011; Mulyukova and Bercovici, 2017]. However, with $E_h \approx 400$ kJ/mol, f is found to be nearly independent of temperature when grain damage theory is used to fit laboratory deformation experiments [Mulyukova and Bercovici, 2017; Foley, 2018]; as a result a constant f is used in this study.

The Arrhenius temperature-dependent laws for viscosity and healing, (1) & (3), are simplified in this study by using a Frank-Kamenetskii approximation, which gives the following modified equations for μ and h :

$$\mu = \mu_n \exp(\gamma_v T) \left(\frac{A}{A_0} \right)^{-m} \quad (4)$$

$$h = h_n \exp(-\gamma_h T). \quad (5)$$

(4) & (5) are then used, after non-dimensionalization (see §2.2), in the numerical models shown in this study. Here γ_v and γ_h describe the temperature-dependence of viscosity and healing, respectively. When non-dimensionalized these become the Frank-Kamenetskii parameters for viscosity and healing, and can be related to E_v and E_h as described in §2.2. The Frank-Kamenetskii approximation reduces the number of free parameters involved in the viscosity law after non-dimensionalization [see Korenaga, 2009], thus simplifying the modeling and analysis. The Frank-Kamenetskii approximation also results in lower viscosities at cold temperatures, i.e. in the lithosphere, than would be reached using the Arrhenius relation given by (1). However, the very large viscosity contrasts produced by the Arrhenius viscosity law with laboratory constrained activation energies are numerically challenging, and therefore

lower activation energies are typically used in modeling studies [e.g. [Tackley, 2000](#); [Foley et al., 2012](#); [O'Neill et al., 2016](#)]. The value of the Frank-Kamenetskii parameter chosen in this study results in viscosity variation that is consistent with other plate generation studies (see §3.1). A larger viscosity variation across the lithosphere would shift the boundary between stagnant lid and mobile lid convection, shown in Figure 1 below, to higher Frank-Kamenteskii parameters for healing, but is otherwise not expected to change the overall conclusions of this study.

2.2 Governing equations

The grain damage formulation is incorporated into a model of infinite Prandtl number, Boussinesq thermal convection. The damage formulation, (2), is non-dimensionalized using the following scales, where primes denote non-dimensional variables: $\underline{x} = \underline{x}'d$, where d is the depth of the mantle; $t = t'd^2/\kappa$, where κ is the thermal diffusivity; $\underline{v} = \underline{v}'\kappa/d$; $T = T'\Delta T + T_s$, where ΔT is the temperature difference across the mantle and T_s is the surface temperature; $A = A'A_0$; $\underline{\tau} = \underline{\tau}'\mu_m\kappa/d^2$, where μ_m is the reference viscosity defined at $T_m = \Delta T + T_s$ in the absence of damage (i.e. at $A = A_0$); and $\gamma_v = \theta_v/\Delta T$ and $\gamma_h = \theta_h/\Delta T$. θ_v and θ_h are the Frank-Kamenetskii parameters for viscosity and healing, respectively. The Frank-Kamenteskii parameter is related to the activation energy from the Arrhenius law as

$$\theta = \frac{E\Delta T}{R(T_s + \Delta T)^2}, \quad (6)$$

which gives θ_v for $E = E_v$ and θ_h for $E = E_h$.

357 Dropping the primes and continuing with non-dimensional variables, the resulting
 358 non-dimensional equation governing fineness evolution is:

$$\frac{DA}{Dt} = D\psi \exp(\theta_v(1-T))A^{-m} - H \exp(-\theta_h(1-T))A^p \quad (7)$$

359 where $\psi = \nabla \underline{v} : (\nabla \underline{v} + (\nabla \underline{v})^T)$, D is the non-dimensional damage number, and
 360 H is the non-dimensional healing number. These quantities are defined as $D =$
 361 $f\mu_m\kappa/(\gamma A_0 d^2)$ and $H = h_m A_0^{(p-1)} d^2/\kappa$ where $h_m = h(T_m)$.

362 The equations for conservation of mass, momentum, and energy, expressed in
 363 terms of non-dimensional variables using the same scales as above, are:

$$\nabla \cdot \underline{v} = 0 \quad (8)$$

364

$$0 = -\nabla P + \nabla \cdot (2\mu \underline{\underline{\varepsilon}}) + Ra_0 T \underline{\underline{\hat{z}}} \quad (9)$$

365

$$\frac{\partial T}{\partial t} + \underline{v} \cdot \nabla T = \nabla^2 T + Q \quad (10)$$

366 where P is the non-hydrostatic pressure, $\varepsilon_{ij} = (\partial v_i/\partial x_j + \partial v_j/\partial x_i)/2$ is the strain
 367 rate, $\underline{\underline{\hat{z}}}$ is the unit vector in the vertical direction, and Ra_0 is the reference Rayleigh
 368 number defined at the reference interior mantle viscosity and temperature; $Ra_0 =$
 369 $(\rho g \alpha \Delta T d^3)/(\kappa \mu_m)$ where ρ is density, α is thermal expansivity, and g is acceleration
 370 due to gravity. The non-dimensional internal heating rate, Q , is defined as $Q =$
 371 $H d^2/(\Delta T \kappa)$, where $H = H_v/(\rho C_p)$, H_v is the volumetric heating rate (with units of

372 Wm^{-3}), and C_p is the specific heat. The non-dimensional viscosity, μ , is defined as

$$\mu = \exp(\theta_v(1 - T))A^{-m}. \quad (11)$$

373 It is also helpful to define parameters to describe the variation of viscosity and
 374 healing across the mantle due to temperature dependence; μ_l/μ_m , the viscosity ratio
 375 in the absence of damage, and h_l/h_m , the healing ratio, where the subscript l denotes
 376 the value in the lithosphere (i.e. at $T = 0$ for all numerical models). The viscosity and
 377 healing ratios are therefore equivalent to the non-dimensional viscosity and healing,
 378 respectively, at the non-dimensional surface temperature of $T = 0$.

379 **2.3 Numerical Model Setup**

380 The models use free-slip top and bottom boundary conditions and periodic side
 381 boundaries. With periodic side boundaries, a uniform horizontal velocity can be
 382 added to the velocity solution while still satisfying the governing equations; in the
 383 numerical model this uniform horizontal velocity is set to be zero at each timestep.
 384 The temperature boundary conditions are $T = 0$ imposed at the surface and an
 385 insulating boundary condition at the base of the mantle; the models are therefore
 386 purely internally heated. Models have an aspect ratio of 4×1 and a resolution of
 387 512×128 . A finite-volume code, which was explained in [Foley and Bercovici \[2014\]](#),
 388 is used to solve equations (7)-(11). As the models are purely internally heated,
 389 the interior temperature that results when the system reaches steady-state can vary
 390 from the assumed value of T_m used in the non-dimensionalization scheme. Thus, T

391 in the mantle interior (T_i) can vary from 1. As the goal of this work is constraining
392 how mantle temperature affects plate boundary formation via grain damage, this
393 variation in T_i is the desired result of the modeling setup.

394 All numerical models are started with a mobile lid initial condition. In pseu-
395 doplastic models, whether the initial condition is mobile or stagnant lid has been
396 shown to influence the steady-state tectonic regime a model reaches [e.g. [Crowley](#)
397 [and O'Connell, 2012](#); [Weller and Lenardic, 2012](#); [Weller et al., 2015](#)]. Specifically,
398 it is harder to initiate plate tectonics from a stagnant lid state than it is to maintain
399 mobile lid convection once it has commenced. Thus, the choice of initial condition
400 for this study favors mobile lid convection as the final state reached in the models.
401 However, [Weller et al. \[2015\]](#) shows that increasing internal heating rate expands
402 the stagnant lid regime, and shrinks the mobile lid regime, for both mobile lid and
403 stagnant lid initial conditions, except at very low heat production rates where the
404 opposite trend is seen. Thus the trend of how internal heating rate affects the mode
405 of surface tectonics appears to hold independent of chosen initial condition. More-
406 over, [Foley et al. \[2014\]](#) found that mobile lid convection can readily develop from
407 an initially stagnant lid when grain damage is used, though a thorough study on the
408 effect of initial conditions on the final regime models with grain damage reach is still
409 needed.

410 A number of metrics and other quantities are calculated from the numerical
411 models as a post-processing step. The base of the lithosphere is determined from the
412 horizontally averaged temperature profile in the mantle. As pure internal heating
413 results in a temperature profile that increases with height from the base of the mantle

414 to the bottom of the lithosphere [e.g. [Moore, 2008](#)], I define the base of the lithosphere
 415 using the maximum of the horizontally averaged temperature profile, $\bar{T}_{\max}$; the base
 416 of the lithosphere is defined as $T_{\text{bl}} = 0.9\bar{T}_{\max}$. The total deformational work within
 417 the layer, Φ , is calculated by integrating $\tau_{ij}\dot{\epsilon}_{ij}$ over the whole model domain, and
 418 deformational work within the lithosphere (Φ_{lith}) and sub-lithospheric mantle (Φ_{man})
 419 are integrals over just the regions lying above and below the T_{bl} isotherm, respectively.
 420 I also define the interior mantle temperature, T_i , as the average temperature within
 421 the domain between the height where $\bar{T}_{\max}$ occurs and 0.1 units below this height.
 422 The average mantle velocity, v_{man} , is defined as the whole mantle RMS velocity, and
 423 the surface (or plate) velocity, v_{surf} , is defined as half the difference between the
 424 maximum and minimum horizontal surface velocities.

425 **3 Results**

426 **3.1 Regime diagram and convective planform**

427 A large suite of models varying internal heating rate, Q , and the Frank-Kamenetskii
 428 parameter for healing, θ_h , are run to map out the boundary between the mobile
 429 lid and stagnant lid regimes. The regime boundary is mapped out in terms of the
 430 variable θ_h for the following reasons. The damage to healing ratio in the lithosphere,
 431 $Dh_m/(Hh_l)$, exerts a major control on the boundary between the stagnant and mobile
 432 lid regimes [[Landuyt et al., 2008](#); [Foley et al., 2012](#)], and changing θ_h is a way to
 433 vary the damage to healing ratio. A lower θ_h results in more rapid grain growth
 434 in the lithosphere, i.e. increases h_l , as healing rate decreases less with decreasing

435 temperature than it would with a larger θ_h . Furthermore, a lower θ_h is a rough
 436 approximation of the effect of higher surface temperatures, which act to increase
 437 the temperature in the mid-lithosphere and thus increase grain growth rates in this
 438 region as well [*Landuyt and Bercovici, 2009; Foley et al., 2012; Bercovici and Ricard,*
 439 *2014*]. All models use $Ra_0 = 10^7$, $D = 10^{-2}$, $H = 1.5 \times 10^5$, and $\theta_v = 13.82$ (see
 440 Tables 1 & 2 for a compilation of all model parameters and results). The values of
 441 Ra_0 , D , and H are reasonable estimates for the modern day Earth [*Foley and Rizo,*
 442 *2017*], which these reference parameters are meant to represent, though it should
 443 be noted that uncertainty in these parameters, in particular for f , h_n , and γ_h , is
 444 high [see, e.g. *Mulyukova and Bercovici, 2017*]. The chosen θ_v results in 6 orders of
 445 magnitude viscosity variation across the lithosphere due to temperature dependence
 446 when $T_i = 1$, which is well within the stagnant lid regime in the absence of damage.
 447 As discussed in §2.1, θ_h is likely larger than θ_v for peridotite; however, here lower
 448 values of θ_h are used to find the boundary between mobile lid and stagnant lid
 449 regimes.

450 The regime diagram (Figure 1) shows two clear trends: at low Q , increasing Q
 451 requires larger θ_h for mobile lid convection; at higher Q (greater than $Q \approx 15$), the
 452 boundary between regimes is found to be largely insensitive to Q , and actually shows
 453 a gradual decrease in the θ_h value required for mobile lid convection as Q increases.
 454 The shape of the regime boundary at low Q implies that increasing internal heating
 455 rate impedes mobile lid convection, as a larger damage to healing ratio is required in
 456 order to produce lid mobility as Q increases. However, this effect is a result of low
 457 rates of internal heating leading to low viscosity ratios across the mantle; at low Q ,

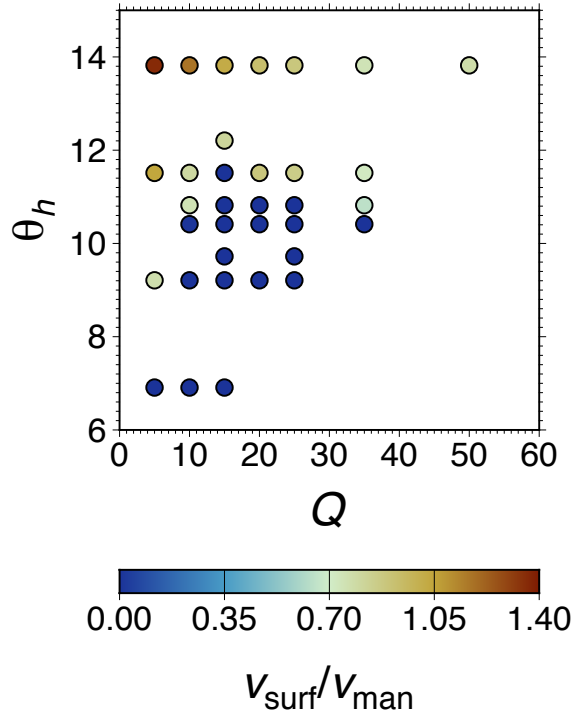


Figure 1: Regime diagram in θ_h - Q parameter space. Model results are colored by the ratio of surface velocity to whole mantle RMS velocity. Thus those colored dark blue, indicating surface velocities are negligibly small, are in the stagnant lid regime.

458 the viscosity variation between lithosphere and mantle interior is so low that only
 459 very modest levels of damage are needed to produce lithosphere mobility. Such a
 460 situation is not applicable to the early Earth, where mantle temperatures were high.
 461 Moreover, θ_v for mantle rock is higher than used in the convection models, as the
 462 very large viscosity variations that result from more realistic values of θ_v result in
 463 numerical convergence problems. The more relevant trend is that at higher Q , where
 464 the boundary between mobile and stagnant lid is approximately insensitive to Q .
 465 Thus, in contrast to the results from models with pseudoplastic yielding, increasing
 466 the internal heating rate or the interior mantle temperature (which increases with
 467 increasing Q in the models) does not lead to a transition to stagnant lid convection.

468 However, there are clear changes in the style of lithosphere mobility and subduc-
 469 tion that accompany higher rates of internal heating. Examining the planform of
 470 convection for mobile lid results with increasing Q (Figure 2) shows a trend towards
 471 increasing wavelength (e.g. plates are longer) and a more drip-like style of subduc-
 472 tion (example stagnant lid results are also shown in Figure 3). At high Q , the slab
 473 undergoes frequent necking, such that subduction takes place via a series of drips
 474 rather than with a continuous downgoing slab. An increased frequency of slab neck-
 475 ing events at higher mantle temperatures was also seen in regional scale subduction
 476 models [*van Hunen and van den Berg, 2008; Sizova et al., 2010*], and occurs for the
 477 same physical reasons as in the models shown here. At higher mantle temperatures
 478 the viscous resistance to slab sinking in the mantle interior is lower, so slabs sink
 479 faster. At the same time, the strength of the convergent boundary in the lithosphere
 480 is resisting slab sinking, and the combination of rapid sinking in the mantle interior

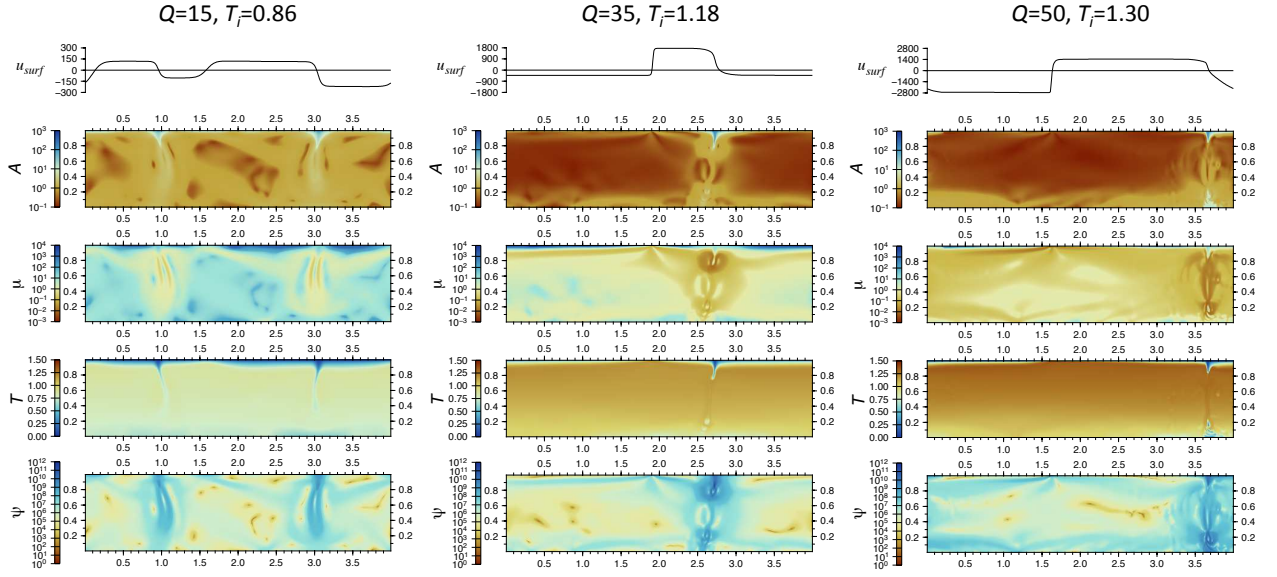


Figure 2: Planform of convection showing the horizontal surface velocity (u_{surf}), fineness field (A), viscosity field (μ), temperature field (T), and the deformational work rate (Ψ). Models with $\theta_h = 13.82$ and $Q = 15$, $Q = 35$, and $Q = 50$ are shown, which result in interior mantle temperatures of $T_i = 0.86$, $T_i = 1.18$, and $T_i = 1.30$, respectively. The perceptually-uniform color map “roma” is used in this study to prevent visual distortion of the data [Crameri, 2018a, b].

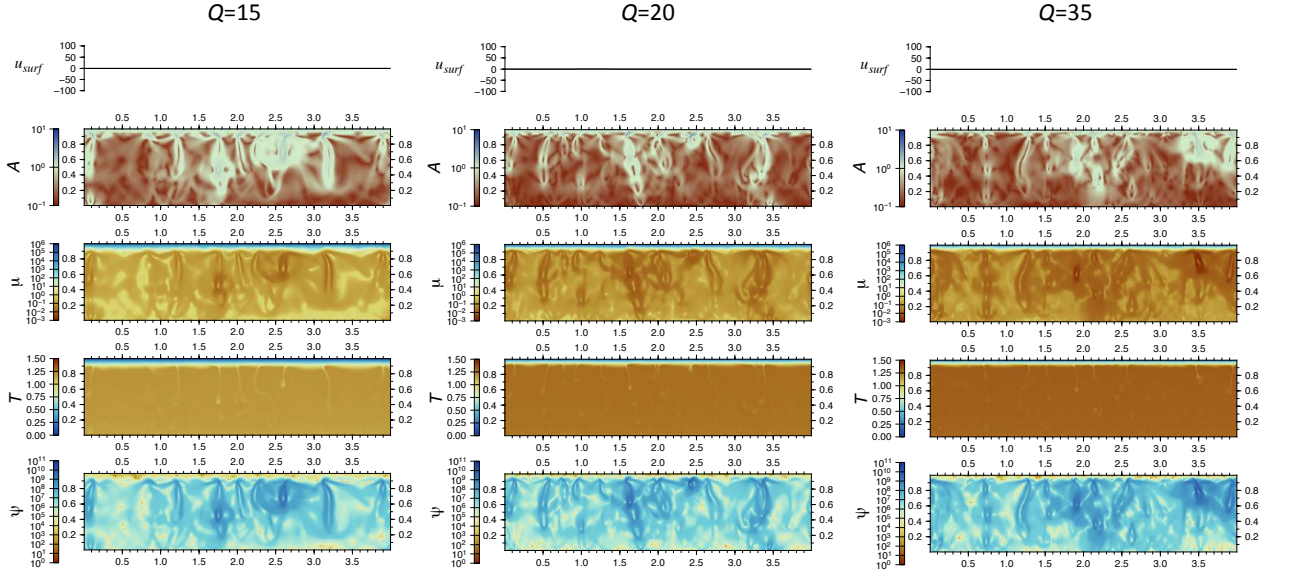


Figure 3: Planform of convection showing the horizontal surface velocity (u_{surf}), fineness field (A), viscosity field (μ), temperature field (T), and the deformational work rate (Ψ) for stagnant lid results. Models with $\theta_h = 10.414$ and $Q = 15$, $Q = 20$, and $Q = 35$ are shown.

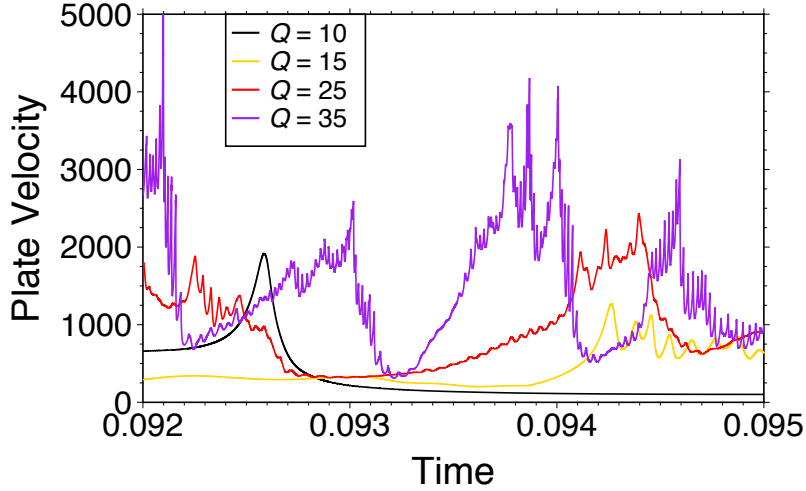


Figure 4: Surface (or plate) velocity as a function of time for models with $\theta_h = 13.82$ and $Q = 10$ (black line), $Q = 15$ (yellow line), $Q = 25$ (red line), and $Q = 35$ (purple line).

481 and resistance to sinking from the lithosphere leads to slab stretching and eventual
 482 tear-off. However, unlike what was commonly seen in subduction models, slab tear-
 483 off does not shutdown lithosphere mobility. Convergence in the lithosphere continues
 484 until a new slab forms, the new slab then tears off, and the cycle repeats.

485 The slab necking events lead to a distinct episodicity in surface velocity, which
 486 peaks as the slab forms and then decays when the slab breaks away, only to climb
 487 again as convergence continues and a new slab forms (Figure 4). Specifically, slab
 488 necking leads to a high frequency mode of surface velocity episodicity, which becomes
 489 prominent with increasing internal heating rate (e.g. it appears at $Q > \approx 25$ in
 490 the models shown here). As a result, the average time spacing between peaks in
 491 the surface velocity time series plot decreases from $\approx 3.3 \times 10^{-4}$ at $Q = 15$, to
 492 $\approx 6.1 \times 10^{-5}$ at $Q = 25$ and $\approx 2.2 \times 10^{-5}$ at $Q = 35$; in terms of dimensional

values these correspond to ≈ 89 , ≈ 16 , and ≈ 6 Myrs, respectively. I also note that there is clearly a range of frequencies of episodicity, in addition to the high frequency slab necking oscillations. Specifically, there is also a longer wavelength episodicity in surface velocity, likely reflecting reorganizations of the larger scale convection pattern in the mantle. Longer wavelength episodicity is present in the models at all values of Q , but the wavelength decreases with increasing Q as a result of a hotter mantle and more vigorous convection.

3.2 Scaling of deformational work rate during mantle convection

The numerical model results show that the boundary between mobile lid and stagnant lid convection has a different dependency on internal heating rate when grain damage is used than when pseudoplasticity is used. The reason for this difference stems from fundamental physical differences in the plate generation mechanisms. With pseudoplasticity, the stress in the lithosphere is the only factor that determines whether mobile lid convection can be produced, as stresses must be high enough to cause yielding deep into the lithosphere for lid mobility [e.g. [Wong and Solomatov, 2015](#)]. However, grain size reduction is driven by the deformational work done by mantle convection in the lithosphere, so it is the rate of deformational work, $\tau_{ij}\dot{\epsilon}_{ij}$, that is responsible for plate boundary formation with grain damage, rather than the stress state.

In steady-state (or statistical steady-state for time-dependent convection), the total deformational work in the convecting fluid must balance with surface heat loss

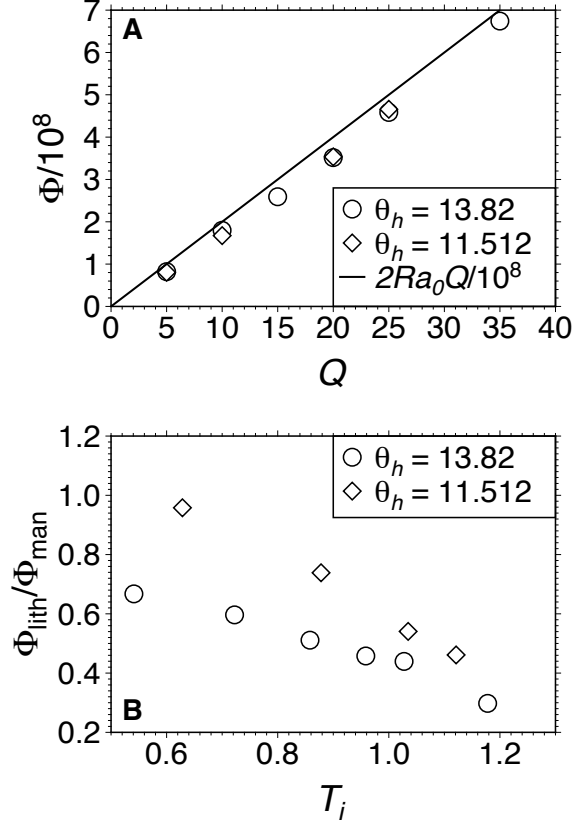


Figure 5: (A) Total deformational work within the convecting layer, Φ , as a function of internal heating rate, Q , and (B) ratio of total deformational work in the lithosphere (Φ_{lith}) to total deformational work in the sub-lithospheric mantle (Φ_{man}). Mobile lid models with $\theta_h = 13.82$ and $\theta_h = 11.512$ are shown. In Figure 5A the scaling law for total deformational work (13) is also plotted, with $L = 4$.

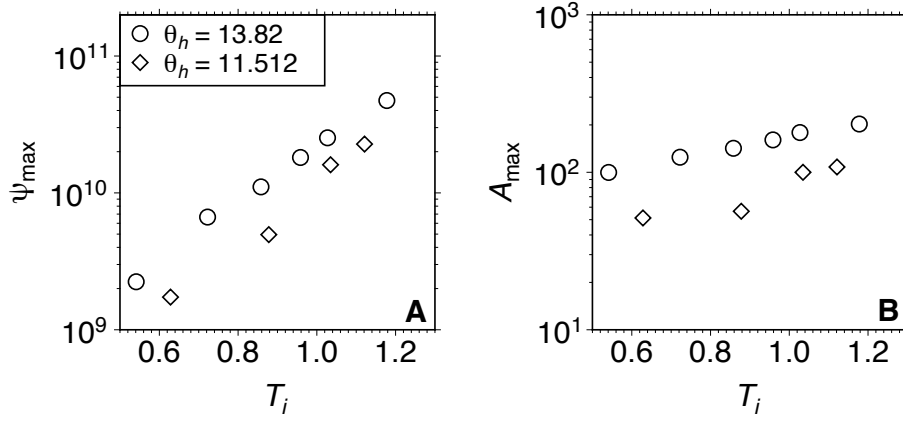


Figure 6: Maximum rate of deformational work in the lithosphere, $\Psi_{\max}$, as a function of interior mantle temperature, T_i for mobile lid models with $\theta_h = 13.82$ and $\theta_h = 11.512$ (A), and maximum lithospheric fineness, $A_{\max}$ as a function of T_i for the same models (B).

[e.g. [Hewitt et al., 1975](#); [Solomatov, 1995](#); [Crowley and O’Connell, 2012](#)], giving

$$\Phi = \int_V \tau_{ij} \dot{\epsilon}_{ij} dV = Ra_0 \left(Nu - \frac{Q}{2} \right) L \quad (12)$$

in the limit of large Nusselt number, Nu ; L in (12) is the aspect ratio of the convecting domain, so $L = 4$ for the models presented in this study. For two-dimensional Cartesian convection in thermal steady-state, $Nu \approx Q$, so

$$\Phi \approx Ra_0 Q L / 2. \quad (13)$$

The numerical models follow (13) (see Figure 5A), confirming that with increasing Q , the total deformational work increases. Thus the energy source for forming plate boundaries with grain damage actually increases with larger internal heating rates, in contrast to pseudoplastic yielding.

523 The rate of deformational work, Ψ , varies significantly in space throughout the
 524 convecting layer, but a substantial fraction occurs in the high viscosity lithosphere,
 525 concentrated in shear zones where the lithosphere converges and downwells (Figure
 526 2). The percentage of total deformational work in the lithosphere generally decreases
 527 with increasing mantle temperature, ranging from up to $\approx 50\%$ at low T_i to $\approx 15\%$
 528 $\%$ at high T_i (Figure 5B). The total lithospheric deformational work is dominated
 529 by work done in shear zones, such that the maximum value of Ψ in the lithosphere
 530 is always within convergent shear zones when convection is in a mobile lid regime.
 531 $\Psi_{\max}$, the maximum deformational work rate in the lithosphere, thus directly mea-
 532 sures the energy source available for grain size reduction in lithospheric shear zones.
 533 The numerical models show that $\Psi_{\max}$ increases with increasing mantle interior tem-
 534 perature, further demonstrating that the energy source for plate boundary formation
 535 with grain damage is enhanced at the mantle thermal conditions expected for the
 536 early Earth (Figure 6A). As a result, the maximum fineness in lithospheric shear
 537 zones, $A_{\max}$, also increases with increasing T_i (Figure 6B). Thus, when grain dam-
 538 age is used, high rates of internal heating do not cause a transition to stagnant lid
 539 convection, because the lithospheric deformational work rate increases with Q , and
 540 thus lithospheric shear zone fineness also increases.

541 Why stress and deformational work rate can scale in opposite ways with increas-
 542 ing mantle temperature or internal heating rate is a result of tradeoffs between how
 543 strain rate and viscosity change. Increasing mantle temperature generally decreases
 544 mantle viscosity, and in turn increases the typical mantle flow speeds, and thus the
 545 characteristic strain rate of mantle flow, as a result of higher thermal buoyancy forces

546 and a lower viscous resistance to flow. As the characteristic stress, $\tau = 2\mu\dot{\epsilon}$, where $\dot{\epsilon}$
 547 is the characteristic strain rate, increasing mantle temperature has competing effects
 548 on how stresses in the mantle and lithosphere will scale. Previous studies have found
 549 that the decrease in viscosity generally wins out over the increase in strain rate, cau-
 550 ing stress to drop as mantle temperature climbs [e.g. *O'Neill et al., 2007*]. However,
 551 as shown here, the energetics of convection require that the total deformational work
 552 increase with Nusselt number and internal heating rate. As a result, the rate of
 553 deformational work in lithospheric shear zones is positively correlated with mantle
 554 temperature (Figure 6A). As with the characteristic stress, the way the characteristic
 555 deformational work rate, $\Psi_c = 2\mu\dot{\epsilon}^2$, scales with mantle temperature is determined
 556 by the competing effects of mantle temperature on viscosity and strain rate. How-
 557 ever, in this case the strain rate squared term must win out over the decrease in
 558 viscosity to produce the observed trends in deformational work rate.

559 **3.3 Changes in subduction and lithosphere mobility style**

560 Although a transition to stagnant lid convection at high internal heating rates or
 561 high mantle temperatures is not seen, a hotter mantle does significantly change the
 562 style of subduction and lithosphere mobility. Lithospheric shear zones are weaker due
 563 to smaller grain sizes resulting from more effective damage, but the mantle interior
 564 also gets weaker with increasing temperature, and at a faster rate than lithospheric
 565 shear zones (Figure 7). As a result, the ratio of lithospheric shear zone viscosity
 566 to sub-lithospheric mantle viscosity increases with T_i (Figure 8A). Higher mantle
 567 temperatures also cause higher grain growth rates, and thus larger grain sizes in the

mantle interior. However, the effect of grain size in the ambient mantle interior, away from downwellings where damage causes localized zones of grain size reduction that significantly influence the rheology around downwellings, is small compared to viscosity temperature-dependence; average fineness in the mantle interior decreases by only a factor of ≈ 6 when going from $T_i \approx 0.5$ to $T_i \approx 1.2$ with $\theta_h = 13.82$, resulting in a factor of 36 increase in viscosity. Meanwhile temperature-dependence acts to decrease viscosity by over four orders of magnitude over the same temperature interval. The way mantle and lithosphere viscosities change with increasing mantle temperature also causes the ratio of surface velocity to average mantle velocity to decrease (Figure 8B). Convection therefore enters a “sluggish lid” regime at higher mantle temperatures, as defined by *Crowley and O’Connell [2012]*, where the lithosphere remains mobile and subduction active, but lithosphere velocities are much slower than interior mantle velocities. Lithosphere velocities can still be as large as modern Earth plate speeds, or larger, but as long as interior mantle velocities exceed surface plate velocities, then convection is considered to be in a sluggish lid regime.

The ratio of shear zone viscosity to mantle interior viscosity measures the strength of plate boundaries relative to the mantle, and the model results indicate this relative strength increases with T_i . In addition to causing the ratio of surface to mantle velocity to decrease with T_i , the increasing relative strength of plate boundaries also causes the change in subduction style from continuous, long-lived subduction, to drip-like subduction with frequent slab necking, as discussed in §3.1, and likely plays a role in the generally longer wavelength convection patterns seen at high heat production rates as well. As the relative strength of plate boundaries increases, thicker plates

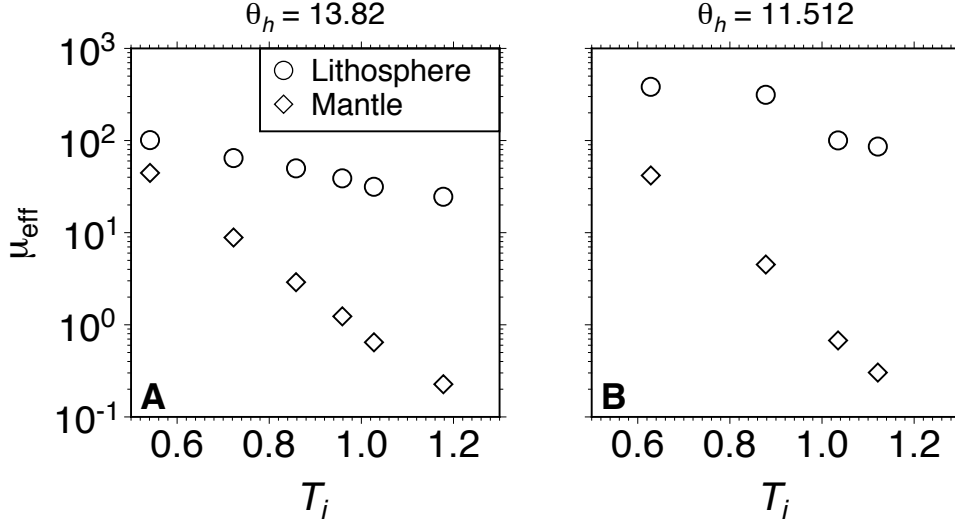


Figure 7: Effective viscosity of lithospheric shear zones (circles) and the mantle interior (diamonds) as a function of T_i , for mobile lid models with $\theta_h = 13.82$ (A) and $\theta_h = 11.512$ (B).

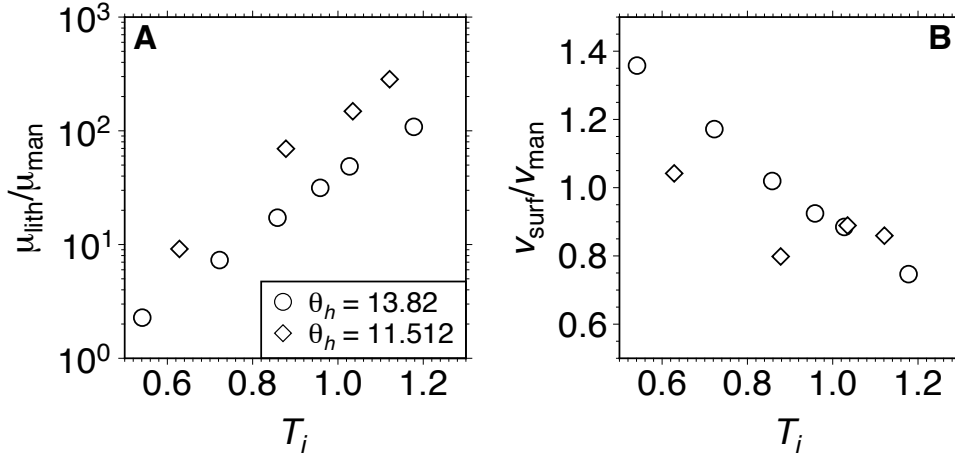


Figure 8: Ratio of the effective viscosity of lithospheric shear zones to the interior mantle viscosity as a function of T_i (A), and ratio of surface velocity to whole mantle RMS velocity (B), for mobile lid models with $\theta_h = 13.82$ and $\theta_h = 11.512$.

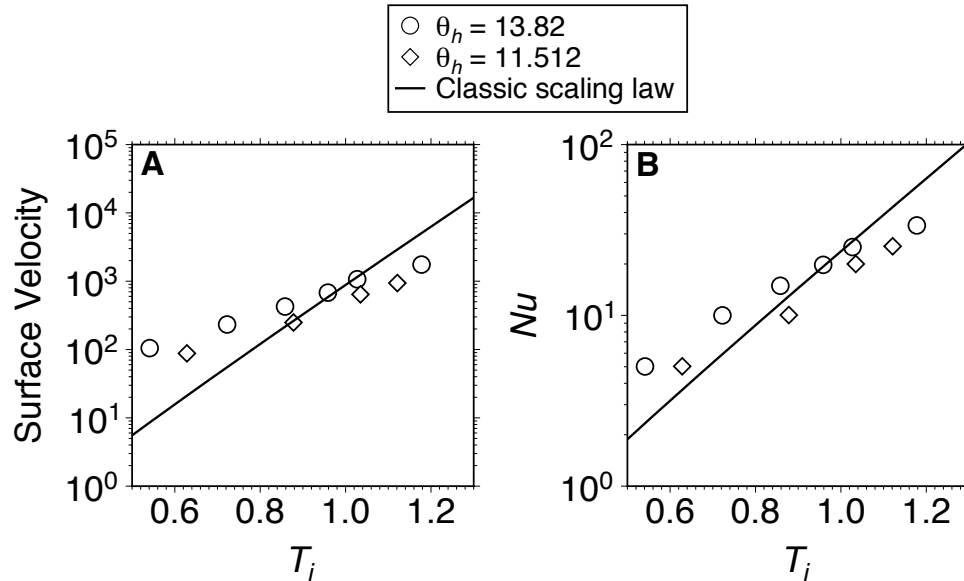


Figure 9: Surface velocity (A) and Nusselt number (B) as a function of T_i for mobile lid models with $\theta_h = 13.82$ and $\theta_h = 11.512$. Also plotted are the constant viscosity scaling laws for v_{surf} (16) and Nu (15). Scaling law constants b and a , from (16) and (15), respectively, are picked to fit the models with $\theta_h = 13.82$ at $T_i = 1$.

are required before subduction can occur, therefore resulting in longer wavelength convection [e.g. [McNamara and Zhong, 2005](#)]. Increasing internal heating rate also increases the sub-adiabatic temperature gradient in the mantle, where temperatures beneath the lithosphere are warmer than one would expect along an adiabat, and the deeper mantle is cooler; this temperature profile also favors long-wavelength convection patterns as a result of the depth-dependent viscosity profile that ensues [e.g. [Bunge et al., 1996](#); [Tackley, 1996](#); [Lenardic et al., 2006](#)].

Another important effect of how increasing mantle temperature influences mobile lid convection produced via grain damage, is that surface velocity and heat flux scale differently than classic scaling laws for mantle convection predict. These clas-

sic scaling laws are often used in thermal evolution models to estimate how plate
 tectonics would change at different mantle thermal conditions [e.g. [Davies, 2007](#)].
 The typical scaling law for surface heat flux from constant viscosity convection, or
 convection that can be approximated with a constant viscosity in the mantle interior,
 is $Nu = aRa_i^{1/3}$ [e.g. [Turcotte and Schubert, 2002](#); [Solomatov, 1995](#)], where Ra_i is
 the internal Rayleigh number, defined as

$$Ra_i = \frac{\rho g \alpha (T_i - T_s) d^3}{\kappa \mu (T_i)}. \quad (14)$$

Thus, Nusselt number scales as

$$Nu = a \left(\frac{Ra_0 T_i}{\exp(\theta_v(1 - T_i))} \right)^{1/3}, \quad (15)$$

when the Frank-Kamenetskii viscosity law is used. Likewise, the scaling law for
 surface velocity for constant viscosity convection is

$$v_{\text{surf}} = b \left(\frac{Ra_0 T_i}{\exp(\theta_v(1 - T_i))} \right)^{2/3}. \quad (16)$$

While the above scaling laws for Nu and v_{surf} strictly only apply to high Rayleigh
 number, constant viscosity convection, mobile lid convection with pseudoplasticity
 has been found to follow $Nu \sim Ra_i^{1/3}$ and $v_{\text{surf}} \sim Ra_i^{2/3}$ scaling relationships in previ-
 ous studies [[Moresi and Solomatov, 1998](#); [Korenaga, 2010a](#)], at least when additional
 complications, such as viscosity layering, are not present [[Crowley and O'Connell,](#)
[2012](#)]. Thus, these classic mantle convection scaling laws have been used to estimate

616 that the early Earth would experience rapid plate speeds and have a high convective
617 heat flux, if plate tectonics were operating at this time [e.g. [Davies, 2007](#)].

618 However, mobile lid convection produced with grain damage does not follow these
619 classic scaling laws, because: 1) the relative strength of lithospheric shear zones com-
620 pared to the underlying mantle increases with interior mantle temperature (Figure
621 8A); and, 2) the wavelength of convection shows clear changes with increasing tem-
622 perature, and hence Ra_i , an effect which is known to cause deviations from the
623 classic convection scaling laws [[Zhong, 2005](#)]. As a result, surface velocities at high
624 temperatures (e.g. above $T_i = 1$) are slower than would be expected if convection
625 followed the classic convection scaling law. Thus mobile lid convection, if it were
626 active on the early Earth, need not result in rapid plate speeds and high surface heat
627 fluxes, and instead may lie a sluggish lid regime as in the convection models shown
628 in this paper. The style of lithospheric mobility is important for interpreting a range
629 of geological and geochemical observations of early Earth evolution, as discussed in
630 more detail in §4.2. In fact, early Earth plate velocities could even be lower than
631 present day plate speeds, while still in a mobile lid regime. Higher mantle temper-
632 atures also enhance the effective grain growth rate in the lithosphere, an effect not
633 captured in the convection models presented here, which would cause plate speeds
634 to actually decrease with increasing mantle temperature as a result of strengthening
635 lithospheric shear zones [[Foley et al., 2014](#)]. A similar result has also been proposed
636 on the basis of dehydration stiffening of the mantle lithosphere during ridge melting
637 [[Korenaga, 2006](#)].

4 Discussion

A major implication of the results of this study is that mantle thermal state is overall less important for whether a planet shows mobile lid or stagnant lid tectonics than many previous studies have indicated. Instead, surface temperature and planet size may have a much stronger control over a planet’s style of tectonics. Specifically, low surface temperatures and larger planet sizes have been found to favor a mobile lid for convection with grain damage, a result that is also consistent with the planets in our solar system [Foley *et al.*, 2012]. Low surface temperatures suppress healing in the lithosphere, thereby enhancing damage and making mobile lid convection more likely [Landuyt and Bercovici, 2009; Foley *et al.*, 2012; Bercovici and Ricard, 2014], while deformational work rate increases with increasing planet size [Foley *et al.*, 2012]. That different mechanisms for generating plate boundaries produce different results for early Earth tectonics is not surprising, but does highlight the importance of the microphysics behind shear localization, as discussed more in the next section.

Furthermore, as early Earth thermal conditions do not impede the formation of weak plate boundaries with grain damage, no significant external factors or effects, beyond normal mantle convective forces, are needed to initiate and sustain a mobile lid. Foley *et al.* [2014] found that mobile lid convection can rapidly commence from an initial stagnant lid, solely as a result of Hadean mantle convection. Many authors have argued for additional mechanisms, beyond the forces from simple thermal convection, as the key for initiating plate tectonics; proposals include subduction induced by plumes [Gerya *et al.*, 2015], formation of early continents [Rey *et al.*, 2014], or meteorite impacts [O’Neill *et al.*, 2017]. Such extra mechanisms would

661 be necessary if, as results from using a pseudoplastic rheology, high temperatures
 662 or high heat production rates impede shear zone formation. However, the results
 663 presented here and in *Foley et al.* [2014] indicate that such external subduction ini-
 664 tiation mechanisms are not needed to start mobile lid tectonics on Earth, as weak
 665 plate boundaries can readily form from mantle convection at early Earth conditions.

666 4.1 Rheology and geodynamic predictions of planetary sur- 667 face tectonics

668 As illustrated in §3.2, the primary reason why models with pseudoplasticity and those
 669 with grain damage produce different predictions for early Earth tectonics stems from
 670 fundamental physical differences in how these mechanisms are formulated. This
 671 discrepancy highlights the importance of understanding the microphysics of shear
 672 localization and plate boundary formation for studying early Earth evolution; ulti-
 673 mately a thorough understanding of lithosphere rheology, and incorporation of this
 674 understanding into geodynamic models, is needed to determine how and why plate
 675 tectonics developed on Earth. For example, it has been argued that the pseudoplastic
 676 rheology can be thought of as an approximation of the more complicated microscale
 677 processes leading to lithospheric failure, such as grain size evolution and fabric de-
 678 velopment. In the case of grain size reduction, it is true that grain damage produces
 679 an effectively non-Newtonian stress-strain rate relationship, similar to pseudoplastic-
 680 ity, when grain size is given by (2) at steady-state [e.g *Foley et al.*, 2012; *Foley and*
 681 *Driscoll*, 2016]. However, this effective constitutive relationship is itself a function
 682 of mantle thermal state, among other factors, and these dependences are not cap-

683 tured by a simple pseudoplastic formulation. Thus, pseudoplasticity is not a good
684 approximation of processes such as grain size reduction, when trying to constrain
685 the physical factors that allow mobile lid convection to develop on a planet.

686 4.2 Sluggish lid convection and Archean tectonics

687 Sluggish lid convection in the Hadean and Archean can potentially explain geological
688 and geochemical observations of early Earth crust formation and tectonics. A number
689 of lines of evidence indicate that the style of tectonics was different from modern day
690 plate tectonics, or at least different from what simple models of plate tectonics on
691 a hotter Earth would predict. Many craton cores from the Eoarchean and Archean
692 are thought to have formed in ocean plateau settings rather than subduction zone
693 settings. Detailed studies of crustal geochemistry of the ≈ 4.0 Ga Acasta Gneiss
694 complex in Canada indicate this early section of felsic crust formed in a setting similar
695 to modern day Iceland [[Reimink et al., 2014](#); [Reimink et al., 2016](#)]. The “dome and
696 keel” structures of Archean felsic rocks in the Pilbara terrane in Australia, as well
697 as the geochemistry of this crust, also point towards formation in an ocean plateau-
698 like setting [e.g. [Pease et al., 2008](#); [Smithies et al., 2009](#); [Van Kranendonk, 2010](#);
699 [Van Kranendonk et al., 2015](#); [Johnson et al., 2017](#)]; in particular it’s not clear how
700 subduction could form the large spatial scale felsic “domes” seen in the Pilbara [e.g.
701 [Collins et al., 1998](#); [Thébaud and Rey, 2013](#); [François et al., 2014](#)]. There is also
702 geochemical evidence for episodes of subduction “failure” (i.e. slab breakoff), rather
703 than sustained subduction, seen in Archean greenstone belts [[Smithies et al., 2018](#)].

704 On a global scale, some studies argue for transitions in crust formation processes

705 in the Archean, around ~ 3.0 Ga, possibly indicating a change in Earth's tectonic
 706 mode. *Dhuime et al.* [2012] argues that the rate of continental crust growth changed
 707 at ≈ 3.0 Ga, possibly as a result of a changing style of mantle dynamics. How-
 708 ever, the history of continental crust growth is debated, and alternative scenarios
 709 with no change in crust growth rates in the Archean are also possible [*Korenaga*,
 710 2018; *Rosas and Korenaga*, 2018]. Studies from global geochemistry datasets indi-
 711 cate that the composition of the continental crust appears to have changed, from a
 712 more mafic composition prior to ~ 3.0 Ga to a more felsic composition after this
 713 time [e.g. *Keller and Schoene*, 2012; *Dhuime et al.*, 2015; *Tang et al.*, 2016]. This
 714 trend in crust composition has often been interpreted as representing the onset of
 715 plate tectonics, though not all studies agree; *Keller and Schoene* [2018] argue that
 716 the evolution of continental basaltic geochemistry over time actually represents plate
 717 tectonic processes throughout Earth history. Moreover, there are significant uncer-
 718 tainties in reconstructing the history of continental crust composition, and felsic early
 719 continents, potentially formed via plate tectonics, are still a viable possibility [e.g.
 720 *Greber et al.*, 2017].

721 Paired metamorphic belts (assemblages of low temperature, high pressure meta-
 722 morphic rocks and low pressure, high temperature rocks) are thought to be indicative
 723 of subduction, as they are formed in arc and back arc settings; these are notably ab-
 724 sent before ~ 3.0 Ga [*Brown*, 2014]. Similarly *Shirey and Richardson* [2011] argue
 725 that the appearance of eclogite inclusions in diamonds at ~ 3.0 Ga records the
 726 start of not only plate tectonics, but the full Wilson cycle. Finally, mantle chemi-
 727 cal heterogeneity formed during the first few hundred million years of Earth history

728 persists in the mantle for $\sim 1 - 2$ Gyrs [e.g. *Rizo et al.*, 2013; *Debaille et al.*, 2013].
 729 Such long mixing times are difficult to explain with simple models of early Earth
 730 plate tectonics, where a hot mantle is expected to result in vigorous convection and
 731 rapid mantle mixing [*Debaille et al.*, 2013; *O'Neill and Debaille*, 2014]. In fact early
 732 formed heterogeneity is even seen in modern rocks thought to be sourced from the
 733 large low shear velocity provinces (LLSVPs) in the lower mantle [*Rizo et al.*, 2016;
 734 *Mundl et al.*, 2017; *Horan et al.*, 2018; *Peters et al.*, 2018]. As the LLSVPs are
 735 typically hypothesized to be chemically dense, and thus resistant to mixing with the
 736 rest of the mantle [e.g. *Garnero and McNamara*, 2008], heterogeneity sourced from
 737 these regions probably does not constrain the efficiency of mantle mixing. However,
 738 the Archean rocks showing resolvable signatures of early formed heterogeneity do
 739 not show evidence of being sourced from LLSVPs, so they likely do constrain the
 740 efficiency of ancient mantle mixing.

741 On the other hand, there is also evidence for subduction in the Archean and
 742 Eoarchean, and possibly even the Hadean. Hadean zircons from the Jack Hills region
 743 of Australia have been used to argue for subduction on the Hadean Earth, based
 744 on the chemistry of their inclusions and pressure-temperature conditions where they
 745 formed [*Harrison et al.*, 2005; *Hopkins et al.*, 2008], though non-subduction formation
 746 scenarios for these zircons are also possible [*Kemp et al.*, 2010; *Nebel et al.*, 2014].
 747 Furthermore, evidence for subduction is seen in the 3.8 Ga Isua greenstone belt in
 748 Greenland [*Jenner et al.*, 2009; *Polat et al.*, 2011], the variably dated 4.4 – 3.8 Ga
 749 Nuvvuagittuq supracrustal belt in Canada [e.g. *Turner et al.*, 2014], the ≈ 3.6 Ga
 750 Acasta Gneiss Complex in Canada [*Koshida et al.*, 2016], and in Australia at ≈ 3.2

751 Ga [e.g. *Van Kranendonk, 2010*] and South Africa at ≈ 3.5 Ga [e.g. *Moyen et al.,*
752 *2007*]; see also *Moyen and Martin [2012]*. Thus early Earth tectonics likely featured
753 at least spatially limited, transient episodes of subduction.

754 A stagnant lid with short-lived episodic bursts of subduction has often been in-
755 voked to explain the above observations from the Hadean and Archean geologic record
756 [e.g. *Moore and Webb, 2013; Griffin et al., 2014; O'Neill et al., 2015; Bédard, 2018;*
757 *Condie, 2018*]. However, a sluggish lid, where subduction occurs more frequently
758 and on a locally confined scale as compared to the short-lived, global subduction
759 and resurfacing events seen during episodic overturns, may also be able to explain
760 early Earth geology. A sluggish lid, featuring subduction and lithospheric mobility,
761 can explain long-term preservation of early-formed mantle chemical heterogeneity, as
762 a sluggish lid also results in slow mixing [*Foley and Rizo, 2017*]. In fact, even plate-
763 tectonic style convection throughout the Hadean and Archean can allow early formed
764 heterogeneity to survive when variations in lower mantle mineralogy are taken into
765 account, as high viscosity, silica rich regions that are resistant to mixing tend to form
766 in the cores of convection cells [*Ballmer et al., 2017*]. Paleomagnetic reconstructions
767 of super-continent cycles show a trend of gradually increasing plate speeds over time,
768 rather than the decreasing trend one would expect from models based on the classic
769 mantle convection scaling laws discussed in §3.3 [*Condie et al., 2015*]. Such a trend
770 is also consistent with predictions from grain damage models that explicitly include
771 the effect of higher mantle temperatures on lithospheric grain growth rates [*Foley*
772 *et al., 2014*], an effect which is not included in the convection models shown in this
773 study (see §3.3).

Moreover, a sluggish lid regime would result in less efficient convective heat transport than modern style plate tectonics (see §3.3). Earth’s heat budget, where less than 50 % of Earth’s present day heat flow is thought to be derived from radiogenic heat production [e.g. *Jaupart et al.*, 2007], is difficult to reconcile with rapid plate speeds and a high heat flux on the early Earth; extrapolating back in time from modern day conditions results in a “thermal catastrophe,” where Earth is predicted to be in a molten state only ~ 1 Gyrs ago [*Korenaga*, 2003]. One possible solution to the “thermal catastrophe” problem is if heat flux does not increase strongly with mantle temperature, as this allows the modern Earth’s heat loss to be dominated by secular cooling without requiring mantle temperatures to increase sharply when extrapolated back in time [*Korenaga*, 2006]. Models of early Earth sluggish lid convection with grain damage indicate that heat flux is a weak function of mantle temperature, especially if the effect of mantle temperature on lithospheric grain growth rate is included [*Foley et al.*, 2014]. Thus sluggish lid convection may also work to reconcile Earth’s thermal history, though more detailed thermal evolution models are needed to demonstrate this robustly.

Inefficient heat transport on the early Earth may even explain the dominant crust formation processes thought to be operating at that time. Based on the estimates in *Foley et al.* [2014], sluggish lid convection at a mantle temperature of 2000-2100 K, representative of the Earth just after magma ocean solidification, would only result in ≈ 60 TW of convective heat flow, while radiogenic heat production would yield $\approx 75 - 100$ TW. Thus significant heat loss via mantle melting and volcanism is required to balance the heat budget, similar to, though less extreme, than the

797 heat-pipe volcanism proposed by *Moore and Webb* [2013] for the Hadean. As a re-
 798 sult, there would be extensive volcanism capable of creating thick ocean plateaus
 799 that could internally re-melt to form felsic crust, all while subduction is still active.
 800 If this extensive volcanism, which would occur largely as a result of passive mantle
 801 upwelling, produces significantly more felsic crust than any arc volcanism present
 802 at this time, then felsic crust production predominantly forming outside of subduc-
 803 tion zones can be explained without needing a stagnant lid. Stagnant lid convection
 804 would of course also result in felsic crust formation in non-subduction settings, since
 805 subduction is absent in this regime, but a sluggish lid allows for subduction without
 806 requiring sudden, global overturn events. In the sluggish lid conceptual model, man-
 807 tle upwelling volcanism will wane as the mantle cools and volcanic heat loss becomes
 808 less significant, leading to subduction zones then becoming the primary setting for
 809 continental crust production, an idea also proposed by *Van Kranendonk* [2010]. The
 810 above hypothesis is admittedly speculative at the present, and thus requires more
 811 detailed models of crust formation in a sluggish lid regime to be fully tested. How-
 812 ever, given the potential for reconciling a wide range of geological observations of the
 813 early Earth with a sluggish lid, this hypothesis is worth pursuing further.

814 **5 Conclusions**

815 Convection models with grain damage, a theoretical formulation for grain size evolu-
 816 tion that allows weak lithospheric shear zones to form via grain size reduction, show
 817 that the boundary between stagnant lid and mobile lid convection is only weakly sen-

sitive to mantle interior temperature or heat production rate. The near insensitivity of the mode of surface tectonics to mantle thermal state is in contrast to previous modeling studies performed with a pseudoplastic rheology; these studies found that increasing internal heating rate or mantle temperature decreases stresses in the lithosphere, therefore favoring a stagnant lid regime. The discrepancy in results stems from fundamental physical differences in the two mechanisms for generating weak plate boundaries. With grain damage, the work done by deformation in the lithosphere drives grain size reduction and subsequent plate boundary formation, while with pseudoplasticity the lithospheric stress state determines whether weak shear zones can form. The deformational work increases with increasing internal heating rate or mantle interior temperature, therefore allowing weak plate boundaries to form by grain size reduction at early Earth thermal conditions. Thus the question of early Earth geodynamics is intimately tied to lithosphere rheology. The microphysical processes that lead to shear localization in the lithosphere must be thoroughly understood, in order to constrain the geodynamics of the early Earth.

Although increasing mantle temperature towards early Earth conditions does not have a significant impact on the overall regime of mantle convection (stagnant or mobile lid) when grain damage is used, it does change the style of subduction and lithospheric mobility. Surface, or plate, motions become increasingly sluggish compared to flow velocities in the mantle interior as internal temperature increases. As a result, subduction becomes drip-like, and no longer features a coherent slab extending deep into the mantle. Drip-like subduction is a result of slabs constantly tearing-off as they form and sink into the mantle, which also leads to a distinct,

high frequency oscillation in plate speeds at the surface. This style of sluggish lid convection can potentially explain key observations of the early Earth geologic record, such as long-term preservation of early formed mantle heterogeneity, or changes in the rate of continental crust formation and average composition of the continental crust in the Archean. Sluggish lid convection leads to slow mantle mixing and hence long-term preservation of mantle chemical heterogeneity. Significant volcanism outside of normal ridge or arc settings would also be expected for a sluggish lid at early Earth thermal conditions, potentially allowing for crust formation in ocean plateau-like settings to be the dominant crust forming process. However, more detailed models combining geodynamics and petrology are needed to better test the hypothesis of early Earth sluggish lid convection, as outlined in the next section.

6 Future Directions

More work on lithospheric rheology, in particular the microphysics of plate boundary formation, is clearly needed to make significant progress on the question of early Earth evolution. However, another vital area of future work is integrating geodynamics, geochemistry, and petrology to better test models of early Earth tectonics. In particular, geodynamic models of early Earth tectonics need to track the conditions under which melting and crust formation would take place, so they can be compared with the geologic record. Such an approach is only recently being attempted [e.g. [Walzer and Hendel, 2008](#); [Gerya, 2011](#); [Johnson et al., 2014](#); [Sizova et al., 2015](#); [Rozel et al., 2017](#); [Walzer and Hendel, 2017](#)], and is a promising direction for progress in

the coming years. In addition to testing whether the tectonic modes produced in theoretical models are consistent with geological observations, systematic testing of different hypotheses for early Earth tectonics is also needed. In particular, working through the various key observations of early Earth crust formation to determine which styles of global tectonics are, or are not, consistent with these observations would be a major advance in our understanding of early Earth evolution. Presently it is still not clear which features of the Archean geologic record provide strong constraints on the style of tectonics, versus those that can be created by multiple different mechanisms and thus are compatible with multiple different modes of surface tectonics. With better integration of geodynamics, geochemistry, and petrology, and in particular systematic testing of different geodynamic scenarios against the ancient geologic record, progress on these critical questions can be achieved in the future.

7 Data Availability

The code used to produce the results shown in this paper can be accessed here: <https://github.com/bradfordjfoley/foley-convection-code>. Tables of the numerical model results, showing relevant parameters and key output are given in Tables 1 & 2.

880 **8 Acknowledgments**

881 This work was supported by NSF award number 1723057. I thank Jesse Reimink for
882 comments on an earlier version of the manuscript, and two anonymous reviewers for
883 their comments which greatly helped improve the manuscript.

Table 1: Table of mobile lid model results

Ra_0	θ_v	θ_h	D	H	Q	Resolution	Φ	v_{surf}	v_{man}	Ψ_{max}	A_{max}
10^7	13.82	13.82	10^{-2}	1.5×10^5	5	512×128	8.21×10^7	142.2	104.7	2.24×10^9	99.67
10^7	13.82	13.82	10^{-2}	1.5×10^5	10	512×128	1.80×10^8	272.4	232.5	6.66×10^9	124.7
10^7	13.82	13.82	10^{-2}	1.5×10^5	15	512×128	2.59×10^8	433.4	425.1	1.11×10^{10}	141.9
10^7	13.82	13.82	10^{-2}	1.5×10^5	20	512×128	3.52×10^8	630.1	681.7	1.81×10^{10}	160.6
10^7	13.82	13.82	10^{-2}	1.5×10^5	25	512×128	4.58×10^8	945.5	1068	2.52×10^{10}	178.8
10^7	13.82	13.82	10^{-2}	1.5×10^5	35	512×128	6.74×10^8	1308	1752	4.73×10^{10}	202.4
10^7	13.82	13.82	10^{-2}	1.5×10^5	50	512×128	6.82×10^8	2214	2849	6.36×10^{10}	212.6
10^7	13.82	12.206	10^{-2}	1.5×10^5	15	512×128	2.61×10^8	391.4	481.8	1.04×10^{10}	93.29
10^7	13.82	11.513	10^{-2}	1.5×10^5	5	512×128	8.07×10^7	91.53	87.85	1.73×10^9	51.26
10^7	13.82	11.513	10^{-2}	1.5×10^5	10	512×128	1.67×10^8	198.6	248.8	4.95×10^9	56.56
10^7	13.82	11.513	10^{-2}	1.5×10^5	20	512×128	3.53×10^8	570.1	641.2	1.60×10^{10}	100.0
10^7	13.82	11.513	10^{-2}	1.5×10^5	25	512×128	4.66×10^8	807.7	939.8	2.27×10^{10}	108.0
10^7	13.82	11.513	10^{-2}	1.5×10^5	35	512×128	5.98×10^8	1292	1797	2.61×10^{10}	109.6
10^7	13.82	10.82	10^{-2}	1.5×10^5	5	512×128	1.64×10^8	195.0	259.8	5.28×10^9	56.57
10^7	13.82	10.82	10^{-2}	1.5×10^5	35	512×128	5.59×10^8	1236	1906	2.36×10^{10}	91.61
10^7	13.82	9.21	10^{-2}	1.5×10^5	5	512×128	7.72×10^7	65.65	85.44	1.21×10^9	27.84

Table 2: Table of stagnant lid model results

Ra_0	θ_v	θ_h	D	H	Q	Resolution	v_{surf}	v_{man}
10^7	13.82	6.908	10^{-2}	1.5×10^5	5	512×128	0.074	272.9
10^7	13.82	6.908	10^{-2}	1.5×10^5	10	512×128	0.027	612.2
10^7	13.82	6.908	10^{-2}	1.5×10^5	15	512×128	0.033	614.4
10^7	13.82	9.21	10^{-2}	1.5×10^5	10	512×128	0.25	774.0
10^7	13.82	9.21	10^{-2}	1.5×10^5	15	512×128	0.20	1035
10^7	13.82	9.21	10^{-2}	1.5×10^5	20	512×128	0.070	1404
10^7	13.82	9.21	10^{-2}	1.5×10^5	25	512×128	0.055	1851
10^7	13.82	9.721	10^{-2}	1.5×10^5	15	512×128	0.67	600.6
10^7	13.82	9.721	10^{-2}	1.5×10^5	25	512×128	0.20	865.4
10^7	13.82	10.414	10^{-2}	1.5×10^5	10	512×128	3.07	416.1
10^7	13.82	10.414	10^{-2}	1.5×10^5	15	512×128	0.79	847.4
10^7	13.82	10.414	10^{-2}	1.5×10^5	20	512×128	0.20	1905
10^7	13.82	10.414	10^{-2}	1.5×10^5	25	512×128	0.27	1742
10^7	13.82	10.414	10^{-2}	1.5×10^5	35	512×128	0.17	2057
10^7	13.82	10.82	10^{-2}	1.5×10^5	15	512×128	1.84	583.0
10^7	13.82	10.82	10^{-2}	1.5×10^5	20	512×128	1.94	695.8
10^7	13.82	10.82	10^{-2}	1.5×10^5	25	512×128	0.36	1550
10^7	13.82	11.513	10^{-2}	1.5×10^5	15	512×128	4.52	1611

Notes: Stagnant lid models are not run all the way to statistical steady-state, and instead were stopped when it was clear that convection had entered a stagnant lid regime and would not return to a mobile lid. Velocities are averages over the model period when stagnant lid behavior began, but do not represent statistical steady-state velocities reached if the models were run longer.

References

- Abbot, D. S., N. B. Cowan, and F. J. Ciesla, Indication of Insensitivity of Planetary Weathering Behavior and Habitable Zone to Surface Land Fraction, *Astrophys. J.*, *756*, 178, doi:10.1088/0004-637X/756/2/178, 2012.
- Abe, Y., Thermal and chemical evolution of the terrestrial magma ocean, *Phys. Earth Planet. Inter.*, *100*, 27–39, doi:10.1016/S0031-9201(96)03229-3, 1997.
- Austin, N., and B. Evans, Paleowattmeters: A scaling relation for dynamically recrystallized grain size, *Geology*, *35*, 343–346, doi:10.1130/G23244A.1, 2007.
- Ballmer, M. D., C. Houser, J. W. Hernlund, R. M. Wentzcovitch, and K. Hirose, Persistence of strong silica-enriched domains in the Earth’s lower mantle, *Nature Geoscience*, *10*, 236–240, doi:10.1038/ngeo2898, 2017.
- Batalha, N. M., Exploring exoplanet populations with NASA’s Kepler Mission, *Proc. Natl. Acad. Sci.*, *111*, 12,647–12,654, doi:10.1073/pnas.1304196111, 2014.
- Bédard, J. H., A catalytic delamination-driven model for coupled genesis of Archaean crust and sub-continental lithospheric mantle, *Geochim. Cosmochim. Acta*, *70*, 1188–1214, doi:10.1016/j.gca.2005.11.008, 2006.
- Bédard, J. H., Stagnant lids and mantle overturns: implications for Archaean tectonics, magmagenesis, crustal growth, mantle evolution, and the start of plate tectonics, *Geoscience Frontiers*, *9*(1), 19–49, doi:10.1016/j.gsf.2017.01.005, 2018.

- 903 Bercovici, D., and S. Karato, Theoretical analysis of shear localization in the litho-
 904 sphere, in *Reviews in Mineralogy and Geochemistry: Plastic Deformation of Min-*
 905 *erals and Rocks*, vol. 51, edited by S. Karato and H. Wenk, chap. 13, pp. 387–420,
 906 Min. Soc. Am., Washington, DC, 2003.
- 907 Bercovici, D., and Y. Ricard, Mechanisms for the generation of plate tectonics by
 908 two-phase grain-damage and pinning, *Phys. Earth Planet. Inter.*, 202, 27–55, doi:
 909 10.1016/j.pepi.2012.05.003, 2012.
- 910 Bercovici, D., and Y. Ricard, Generation of plate tectonics with two-phase grain-
 911 damage and pinning: Source-sink model and toroidal flow, *Earth Planet. Sci.*
 912 *Lett.*, 365, 275–288, doi:10.1016/j.epsl.2013.02.002, 2013.
- 913 Bercovici, D., and Y. Ricard, Plate tectonics, damage, and inheritance, *Nature*,
 914 508(7497), 513–516, doi:10.1038/nature13072, 2014.
- 915 Bercovici, D., and Y. Ricard, Grain-damage hysteresis and plate tectonic states,
 916 *Phys. Earth Planet. Inter.*, 253, 31–47, doi:10.1016/j.pepi.2016.01.005, 2016.
- 917 Bercovici, D., and P. Skemer, Grain damage, phase mixing and plate-boundary for-
 918 mation, *Journal of Geodynamics*, 108, 40–55, doi:10.1016/j.jog.2017.05.002, 2017.
- 919 Bercovici, D., Y. Ricard, and G. Schubert, A two-phase model of compaction and
 920 damage, 1. general theory, *J. Geophys. Res.*, 106(B5), 8887–8906, doi:10.1029/
 921 2000JB900430, 2001a.
- 922 Bercovici, D., Y. Ricard, and G. Schubert, A two-phase model of compaction and

923 damage, 3. applications to shear localization and plate boundary formation, *J.*
924 *Geophys. Res.*, *106*(B5), 8925–8940, 2001b.

925 Bercovici, D., P. Tackley, and Y. Ricard, The generation of plate tectonics from
926 mantle dynamics, in *Treatise on Geophysics*, vol. 7, Mantle Dynamics, edited by
927 D. Bercovici and G. Schubert (chief editor), pp. 271–318, Elsevier, New York, 2015.

928 Berner, R., *The Phanerozoic carbon cycle*, Oxford University Press, 2004.

929 Breuer, D., and W. Moore, Dynamics and thermal history of the terrestrial planets,
930 the Moon, and Io, in *Treatise on Geophysics*, vol. 10, Planets and Moons, edited
931 by T. Spohn; G. Schubert (chief editor), pp. 299–348, Elsevier, New York, 2007.

932 Brown, M., The contribution of metamorphic petrology to understanding lithosphere
933 evolution and geodynamics, *Geoscience Frontiers*, *5*(4), 553–569, doi:10.1016/j.gsf.
934 2014.02.005, 2014.

935 Bunge, H., M. Richards, and J. Baumgardner, Effect of depth-dependent viscosity
936 on the planform of mantle-convection, *Nature*, *379*, 436–438, 1996.

937 Byrne, P. K., C. Klimczak, A. M. Celâl Şengör, S. C. Solomon, T. R. Watters, and
938 S. A. Hauck, II, Mercury’s global contraction much greater than earlier estimates,
939 *Nature Geoscience*, *7*, 301–307, doi:10.1038/ngeo2097, 2014.

940 Cawood, P. A., C. J. Hawkesworth, and B. Dhuime, The continental record and the
941 generation of continental crust, *Geological Society of America Bulletin*, *125*, 14–32,
942 doi:10.1130/B30722.1, 2013.

943 Collins, W. J., M. J. Van Kranendonk, and C. Teyssier, Partial convective overturn of
944 Archaean crust in the east Pilbara Craton, Western Australia: driving mechanisms
945 and tectonic implications, *Journal of Structural Geology*, *20*, 1405–1424, doi:10.
946 1016/S0191-8141(98)00073-X, 1998.

947 Condie, K., and A. Kröner, When did plate tectonics begin? Evidence from the
948 geologic record, in *When Did Plate Tectonics Begin?*, edited by K. Condie and
949 V. Pease, pp. 249–263, Geological Society of America, special Paper 440, 2008.

950 Condie, K., S. A. Pisarevsky, J. Korenaga, and S. Gardoll, Is the rate of super-
951 continent assembly changing with time?, *Precambrian Res.*, *259*, 278–289, doi:
952 10.1016/j.precamres.2014.07.015, 2015.

953 Condie, K. C., A planet in transition: The onset of plate tectonics on Earth between
954 3 and 2 Ga?, *Geoscience Frontiers*, *9*(1), 51 – 60, doi:10.1016/j.gsf.2016.09.001,
955 2018.

956 Crameri, F., Scientific colour maps (Version 3.0.0), *Zenodo*, doi:0.5281/zenodo.
957 1243863, 2018a.

958 Crameri, F., Geodynamic diagnostics, scientific visualisation and StagLab 3.0,
959 *Geosci. Model Dev. Discuss.*, doi:10.5194/gmd-2017-328, 2018b.

960 Crameri, F., P. J. Tackley, I. Meilick, T. V. Gerya, and B. J. P. Kaus, A free plate
961 surface and weak oceanic crust produce single-sided subduction on Earth, *Geophys.*
962 *Res. Lett.*, *39*, L03306, doi:10.1029/2011GL050046, 2012.

- 963 Cross, A. J., and P. Skemer, Ultramylonite generation via phase mixing in high-
964 strain experiments, *J. Geophys. Res. Solid Earth*, *122*, 1744–1759, doi:10.1002/
965 2016JB013801, 2017.
- 966 Crowley, J. W., and R. J. O’Connell, An analytic model of convection in a
967 system with layered viscosity and plates, *Geophys. J. Int.*, *188*, 61–78, doi:
968 10.1111/j.1365-246X.2011.05254.x, 2012.
- 969 Davaille, A., S. E. Smrekar, and S. Tomlinson, Experimental and observational ev-
970 idence for plume-induced subduction on Venus, *Nature Geoscience*, *10*, 349–355,
971 doi:10.1038/ngeo2928, 2017.
- 972 Davies, G. F., Thermal evolution of the mantle, in *Treatise on Geophysics*, vol. 9,
973 Evolution of the Earth, edited by D. Stevenson and G. Schubert (chief editor), pp.
974 197–216, Elsevier, New York, 2007.
- 975 De Bresser, J., C. Peach, J. Reijrs, and C. Spiers, On dynamic recrystallization during
976 solid state flow: effects of stress and temperature, *Geophys. Res. Lett.*, *25*, 3457–
977 3460, 1998.
- 978 De Bresser, J., J. ter Heege, and C. Spiers, Grain size reduction by dynamic recryst-
979 tallization: can it result in major rheological weakening?, *Intl. J. Earth Sci.*, *90*,
980 28–45, 2001.
- 981 Debaille, V., C. O’Neill, A. D. Brandon, P. Haenecour, Q.-Z. Yin, N. Mattielli, and
982 A. H. Treiman, Stagnant-lid tectonics in early Earth revealed by ^{142}Nd variations

983 in late Archean rocks, *Earth Planet. Sci. Lett.*, *373*, 83–92, doi:10.1016/j.epsl.2013.
 984 04.016, 2013.

985 Dhuime, B., C. J. Hawkesworth, P. A. Cawood, and C. D. Storey, A Change in the
 986 Geodynamics of Continental Growth 3 Billion Years Ago, *Science*, *335*, 1334–1336,
 987 doi:10.1126/science.1216066, 2012.

988 Dhuime, B., A. Wuestefeld, and C. J. Hawkesworth, Emergence of modern con-
 989 tinental crust about 3 billion years ago, *Nature Geoscience*, *8*, 552–555, doi:
 990 10.1038/ngeo2466, 2015.

991 Driscoll, P., and D. Bercovici, On the thermal and magnetic histories of Earth and
 992 Venus: Influences of melting, radioactivity, and conductivity, *Phys. Earth Planet.*
 993 *Inter.*, *236*, 36–51, doi:10.1016/j.pepi.2014.08.004, 2014.

994 Drury, M. R., R. L. M. Vissers, D. van der Wal, and E. H. Hoogerduijn Strating,
 995 Shear localisation in upper mantle peridotites, *Pure Appl. Geophys.*, *137*, 439–460,
 996 doi:10.1007/BF00879044, 1991.

997 Etheridge, M. A., and J. C. Wilkie, Grainsize reduction, grain boundary sliding
 998 and the flow strength of mylonites, *Tectonophysics*, *58*, 159–178, doi:10.1016/
 999 0040-1951(79)90327-5, 1979.

1000 Foley, B. J., The role of plate tectonic-climate coupling and exposed land area in
 1001 the development of habitable climates on rocky planets, *Astrophys. J.*, *812*, 36,
 1002 doi:10.1088/0004-637X/812/1/36, 2015.

1003 Foley, B. J., On the dynamics of coupled grain size evolution and shear heating in
1004 lithospheric shear zones, *Phys. Earth Planet Int.*, *in press*, doi:10.1016/j.pepi.2018.
1005 07.008, 2018.

1006 Foley, B. J., and D. Bercovici, Scaling laws for convection with temperature-
1007 dependent viscosity and grain-damage, *Geophys. J. Int.*, *199*(1), 580–603, doi:
1008 10.1093/gji/ggu275, 2014.

1009 Foley, B. J., and P. E. Driscoll, Whole planet coupling between climate, mantle, and
1010 core: Implications for rocky planet evolution, *Geochem., Geophys., Geosyst.*, *17*,
1011 doi:10.1002/2015GC006210, 2016.

1012 Foley, B. J., and H. Rizo, Long-term preservation of early formed mantle hetero-
1013 geneity by mobile lid convection: Importance of grainsize evolution, *Earth Planet.*
1014 *Sci. Lett.*, *475*, 94–105, doi:10.1016/j.epsl.2017.07.031, 2017.

1015 Foley, B. J., and A. J. Smye, Carbon cycling and habitability of Earth-size stagnant
1016 lid planets, *Astrobiology*, *18*(7), 873–896, doi:10.1089/ast.2017.1695, 2018.

1017 Foley, B. J., D. Bercovici, and W. Landuyt, The conditions for plate tectonics on
1018 super-earths: Inferences from convection models with damage, *Earth Planet. Sci.*
1019 *Lett.*, *331332*(0), 281 – 290, doi:10.1016/j.epsl.2012.03.028, 2012.

1020 Foley, B. J., D. Bercovici, and L. T. Elkins-Tanton, Initiation of plate tectonics from
1021 post-magma ocean thermochemical convection, *J. Geophys. Res. Solid Earth*, *119*,
1022 8538–8561, doi:10.1002/2014JB011121, 2014.

- 1023 Fowler, A. C., Boundary layer theory and subduction, *J. Geophys. Res.*, *98*, 21,997–
1024 22,005, doi:10.1029/93JB02040, 1993.
- 1025 François, C., P. Philippot, P. Rey, and D. Rubatto, Burial and exhumation during
1026 Archean sagduction in the East Pilbara Granite-Greenstone Terrane, *Earth Planet.*
1027 *Sci. Lett.*, *396*, 235–251, doi:10.1016/j.epsl.2014.04.025, 2014.
- 1028 Franck, S., K. Kossacki, and C. Bounama, Modelling the global carbon cycle for
1029 the past and future evolution of the earth system, *Chem. Geol.*, *159*(1), 305–317,
1030 1999.
- 1031 Garnero, E. J., and A. K. McNamara, Structure and Dynamics of Earth’s Lower
1032 Mantle, *Science*, *320*, 626, doi:10.1126/science.1148028, 2008.
- 1033 Gerya, T., Dynamical Instability Produces Transform Faults at Mid-Ocean Ridges,
1034 *Science*, *329*, 1047, doi:10.1126/science.1191349, 2010.
- 1035 Gerya, T., Future directions in subduction modeling, *Journal of Geodynamics*, *52*,
1036 344–378, doi:10.1016/j.jog.2011.06.005, 2011.
- 1037 Gerya, T., R. Stern, M. Baes, S. Sobolev, and S. Whattam, Plate tectonics on the
1038 Earth triggered by plume-induced subduction initiation, *Nature*, *527*(7577), 221–
1039 225, 2015.
- 1040 Greber, N. D., N. Dauphas, A. Bekker, M. P. Ptáček, I. N. Bindeman, and A. Hof-
1041 mann, Titanium isotopic evidence for felsic crust and plate tectonics 3.5 billion
1042 years ago, *Science*, *357*, 1271–1274, doi:10.1126/science.aan8086, 2017.

1043 Griebmeier, J.-M., A. Stadelmann, U. Motschmann, N. K. Belisheva, H. Lammer,
1044 and H. K. Biernat, Cosmic Ray Impact on Extrasolar Earth-Like Planets in Close-
1045 in Habitable Zones, *Astrobiology*, 5, 587–603, doi:10.1089/ast.2005.5.587, 2005.

1046 Griffin, W. L., E. A. Belousova, C. O’Neill, S. Y. O’Reilly, V. Malkovets, N. J.
1047 Pearson, S. Spetsius, and S. A. Wilde, The world turns over: Hadean-Archean
1048 crust-mantle evolution, *Lithos*, 189, 2–15, doi:10.1016/j.lithos.2013.08.018, 2014.

1049 Harrison, T. M., J. Blichert-Toft, W. Müller, F. Albarede, P. Holden, and S. J.
1050 Mojzsis, Heterogeneous Hadean Hafnium: Evidence of Continental Crust at 4.4 to
1051 4.5 Ga, *Science*, 310, 1947–1950, doi:10.1126/science.1117926, 2005.

1052 Herzberg, C., K. Condie, and J. Korenaga, Thermal history of the Earth and its
1053 petrological expression, *Earth and Planetary Science Letters*, 292, 79–88, doi:10.
1054 1016/j.epsl.2010.01.022, 2010.

1055 Hewitt, J. M., D. P. McKenzie, and N. O. Weiss, Dissipative heating in convective
1056 flows, *J. Fluid Mech.*, 68, 721–738, doi:10.1017/S002211207500119X, 1975.

1057 Hirth, G., and D. Kohlstedt, Rheology of the upper mantle and the mantle wedge: a
1058 view from the experimentalists, in *Subduction Factory Mongraph*, vol. 138, edited
1059 by J. Eiler, pp. 83–105, Am. Geophys. Union, Washington, DC, 2003.

1060 Höink, T., A. Lenardic, and M. Richards, Depth-dependent viscosity and mantle
1061 stress amplification: implications for the role of the asthenosphere in maintaining
1062 plate tectonics, *Geophys. J. Int.*, 191, 30–41, doi:10.1111/j.1365-246X.2012.05621.
1063 x, 2012.

- 1064 Hopkins, M., T. M. Harrison, and C. E. Manning, Low heat flow inferred from >
 1065 4Gyr zircons suggests Hadean plate boundary interactions, *Nature*, *456*, 493–496,
 1066 doi:10.1038/nature07465, 2008.
- 1067 Horan, M. F., R. W. Carlson, R. J. Walker, M. Jackson, M. Garçon, and M. Norman,
 1068 Tracking Hadean processes in modern basalts with 142-Neodymium, *Earth Planet.*
 1069 *Sci. Lett.*, *484*, 184–191, doi:10.1016/j.epsl.2017.12.017, 2018.
- 1070 Jadamec, M. A., and M. I. Billen, Reconciling surface plate motions with rapid three-
 1071 dimensional mantle flow around a slab edge, *Nature*, *465*, 338–341, doi:10.1038/
 1072 nature09053, 2010.
- 1073 Jaupart, C., S. Labrosse, and J. C. Mareschal, Temperatures, heat and energy in the
 1074 mantle of the earth, in *Treatise on Geophysics*, vol. 7 Mantle Dynamics, edited by
 1075 D. Bercovici, chap. 6, pp. 253–305, Elsevier, 2007.
- 1076 Jenner, F., V. Bennett, A. Nutman, C. R. Friend, M. Norman, and G. Yaxley,
 1077 Evidence for subduction at 3.8 Ga: geochemistry of arc-like metabasalts from the
 1078 southern edge of the Isua Supracrustal Belt, *Chem. Geol.*, *261*(1), 83–98, 2009.
- 1079 Jin, D., S. Karato, and M. Obata, Mechanisms of shear localization in the continental
 1080 lithosphere: Inference from the deformation microstructures of peridotites from the
 1081 Ivrea zone, northwestern Italy, *J. Struct. Geol.*, *20*, 195–209, 1998.
- 1082 Johnson, T. E., M. Brown, B. J. P. Kaus, and J. A. Vantongeren, Delamination
 1083 and recycling of Archaean crust caused by gravitational instabilities, *Nature Geo-*
 1084 *science*, *7*, 47–52, doi:10.1038/ngeo2019, 2014.

- 1085 Johnson, T. E., M. Brown, N. J. Gardiner, C. L. Kirkland, and R. H. Smithies,
1086 Earth’s first stable continents did not form by subduction, *Nature*, *543*, 239–242,
1087 doi:10.1038/nature21383, 2017.
- 1088 Karato, S., *Deformation of Earth Materials: An Introduction to the Rheology of the*
1089 *Solid Earth*, Cambridge University Press, New York, 2008.
- 1090 Karato, S., and P. Wu, Rheology of the Upper Mantle: A Synthesis, *Science*,
1091 *260*(5109), 771–778, doi:10.1126/science.260.5109.771, 1993.
- 1092 Kasting, J. F., and D. Catling, Evolution of a Habitable Planet, *Annu. Rev. Astron.*
1093 *Astrophys.*, *41*, 429–463, doi:10.1146/annurev.astro.41.071601.170049, 2003.
- 1094 Kattenhorn, S. A., and L. M. Prockter, Evidence for subduction in the ice shell of
1095 Europa, *Nature Geoscience*, *7*, 762–767, doi:10.1038/ngeo2245, 2014.
- 1096 Keller, B., and B. Schoene, Plate tectonics and continental basaltic geochemistry
1097 throughout Earth history, *Earth Planet. Sci. Lett.*, *481*, 290–304, doi:10.1016/j.
1098 epsl.2017.10.031, 2018.
- 1099 Keller, C. B., and B. Schoene, Statistical geochemistry reveals disruption in secu-
1100 lar lithospheric evolution about 2.5 Gyr ago, *Nature*, *485*, 490–493, doi:10.1038/
1101 nature11024, 2012.
- 1102 Kemp, A. I. S., S. A. Wilde, C. J. Hawkesworth, C. D. Coath, A. Nemchin, R. T.
1103 Pidgeon, J. D. Vervoort, and S. A. DuFrane, Hadean crustal evolution revisited:
1104 New constraints from Pb-Hf isotope systematics of the Jack Hills zircons, *Earth*
1105 *Planet. Sci. Lett.*, *296*, 45–56, doi:10.1016/j.epsl.2010.04.043, 2010.

- 1106 Kite, E. S., M. Manga, and E. Gaidos, Geodynamics and Rate of Volcanism on Mas-
 1107 sive Earth-like Planets, *Astrophys. J.*, *700*, 1732–1749, doi:10.1088/0004-637X/
 1108 700/2/1732, 2009.
- 1109 Kohlstedt, D., and S. Mackwell, Strength and deformation of planetary lithospheres,
 1110 in *Planetary Tectonics*, edited by T. Waters and R. Schultz, pp. 397–456, Cam-
 1111 bridge Univ. Press, Cambridge, UK, 2010.
- 1112 Korenaga, J., Energetics of mantle convection and the fate of fossil heat, *Geophys.*
 1113 *Res. Lett.*, *30*(8), 1437, 2003.
- 1114 Korenaga, J., Archean geodynamics and the thermal evolution of earth, in *Archean*
 1115 *Geodynamics and Environments*, vol. 164, edited by K. Benn, J.-C. Mareschal,
 1116 and K. Condie, pp. 7–32, AGU Geophysical Monograph Series, 2006.
- 1117 Korenaga, J., Thermal cracking and the deep hydration of oceanic litho-
 1118 sphere: A key to the generation of plate tectonics?, *J. Geophys. Res.*, *112*,
 1119 doi:10.1029/2006JB004502, 2007.
- 1120 Korenaga, J., Scaling of stagnant-lid convection with Arrhenius rheology and the
 1121 effects of mantle melting, *Geophys. J. Int.*, *179*, 154–170, doi:10.1111/j.1365-246X.
 1122 2009.04272.x, 2009.
- 1123 Korenaga, J., Scaling of plate tectonic convection with pseudoplastic rheology, *J.*
 1124 *Geophys. Res.*, *115*, B11,405, doi:doi:10.1029/2010JB007670, 2010a.
- 1125 Korenaga, J., On the likelihood of plate tectonics on super-earths: Does size matter?,
 1126 *Astrophys. J.*, *725*(1), L43, 2010b.

- 1127 Korenaga, J., Initiation and Evolution of Plate Tectonics on Earth: Theories
1128 and Observations, *Annu. Rev. Earth Planet. Sci.*, *41*, 117–151, doi:10.1146/
1129 annurev-earth-050212-124208, 2013.
- 1130 Korenaga, J., Pitfalls in modeling mantle convection with internal heat production,
1131 *J. Geophys. Res. Solid Earth*, *122*, 4064–4085, doi:10.1002/2016JB013850, 2017.
- 1132 Korenaga, J., Estimating the formation age distribution of continental crust by un-
1133 mixing zircon ages, *Earth Planet. Sci. Lett.*, *482*, 388–395, doi:10.1016/j.epsl.2017.
1134 11.039, 2018.
- 1135 Koshida, K., A. Ishikawa, H. Iwamori, and T. Komiya, Petrology and geochemistry
1136 of mafic rocks in the Acasta Gneiss Complex: Implications for the oldest mafic
1137 rocks and their origin, *Precambrian Res.*, *283*, 190–207, 2016.
- 1138 Landuyt, W., and D. Bercovici, Variations in planetary convection via the effect of
1139 climate on damage, *Earth and Planetary Science Letters*, *277*(1-2), 29–37, 2009.
- 1140 Landuyt, W., D. Bercovici, and Y. Ricard, Plate generation and two-phase damage
1141 theory in a model of mantle convection, *Geophys. J. Int.*, *174*, 1065–1080, doi:
1142 10.1111/j.1365-246X.2008.03844.x, 2008.
- 1143 Lenardic, A., and J. W. Crowley, On the Notion of Well-defined Tectonic Regimes
1144 for Terrestrial Planets in this Solar System and Others, *Astrophys. J. Lett.*, *755*,
1145 132, doi:10.1088/0004-637X/755/2/132, 2012.
- 1146 Lenardic, A., M. A. Richards, and F. H. Busse, Depth-dependent rheology and the

1147 horizontal length scale of mantle convection, *J. Geophys. Res.*, *111*, B07404, doi:
 1148 10.1029/2005JB003639, 2006.

1149 Lenardic, A., A. Jellinek, B. Foley, C. O'Neill, and W. Moore, Climate-tectonic
 1150 coupling: Variations in the mean, variations about the mean, and variations in
 1151 mode, *J. Geophys. Res. Planets*, *121*(10), 1831–1864, 2016.

1152 Lowman, J. P., Mantle convection models featuring plate tectonic behavior: An
 1153 overview of methods and progress, *Tectonophysics*, *510*, 1–16, doi:10.1016/j.tecto.
 1154 2011.04.015, 2011.

1155 McNamara, A. K., and S. Zhong, Degree-one mantle convection: Dependence on
 1156 internal heating and temperature-dependent rheology, *Geophys. Res. Lett.*, *32*,
 1157 L01301, doi:10.1029/2004GL021082, 2005.

1158 Mei, S., A. M. Suzuki, D. L. Kohlstedt, N. A. Dixon, and W. B. Durham, Exper-
 1159 imental constraints on the strength of the lithospheric mantle, *J. Geophys. Res.*
 1160 *Solid Earth*, *115*, B08204, doi:10.1029/2009JB006873, 2010.

1161 Montési, L. G. J., Fabric development as the key for forming ductile shear zones and
 1162 enabling plate tectonics, *Journal of Structural Geology*, *50*, 254–266, doi:10.1016/
 1163 j.jsg.2012.12.011, 2013.

1164 Moore, W. B., Tidal heating and convection in Io, *J. Geophys. Res. Planets*, *108*,
 1165 5096, doi:10.1029/2002JE001943, 2003.

1166 Moore, W. B., Heat transport in a convecting layer heated from within and below,
 1167 *J. Geophys. Res.*, *113*(B12), B11407, doi:10.1029/2006JB004778, 2008.

- 1168 Moore, W. B., and A. A. G. Webb, Heat-pipe Earth, *Nature*, 501(7468), 501–505,
1169 doi:10.1038/nature12473, 2013.
- 1170 Moresi, L., and V. Solomatov, Mantle convection with a brittle lithosphere: Thoughts
1171 on the global tectonic style of the earth and venus, *Geophys. J. Int.*, 133, 669–682,
1172 doi:10.1046/j.1365-246X.1998.00521.x, 1998.
- 1173 Moyen, J.-F., and H. Martin, Forty years of TTG research, *Lithos*, 148, 312–336,
1174 2012.
- 1175 Moyen, J.-F., G. Stevens, A. F. Kisters, and R. W. Belcher, Chapter 5.6: TTG Plu-
1176 tons of the Barberton Granitoid-Greenstone Terrain, South Africa, *Developments*
1177 *in Precambrian Geology*, 15, 607–667, 2007.
- 1178 Mulyukova, E., and D. Bercovici, Formation of lithospheric shear zones: Ef-
1179 fect of temperature on two-phase grain damage, *Phys. Earth Planet. Inter.*,
1180 270(Supplement C), 195 – 212, doi:https://doi.org/10.1016/j.pepi.2017.07.011,
1181 2017.
- 1182 Mundl, A., M. Touboul, M. G. Jackson, J. M. D. Day, M. D. Kurz, V. Lekic, R. T.
1183 Helz, and R. J. Walker, Tungsten-182 heterogeneity in modern ocean island basalts,
1184 *Science*, 356, 66–69, doi:10.1126/science.aal4179, 2017.
- 1185 Nebel, O., R. P. Rapp, and G. M. Yaxley, The role of detrital zircons in Hadean
1186 crustal research, *Lithos*, 190, 313–327, doi:10.1016/j.lithos.2013.12.010, 2014.
- 1187 Neukum, G., et al., Recent and episodic volcanic and glacial activity on Mars

1188 revealed by the High Resolution Stereo Camera, *Nature*, *432*, 971–979, doi:
 1189 10.1038/nature03231, 2004.

1190 Nimmo, F., Why does venus lack a magnetic field?, *Geology*, *30*(11), 987–990, 2002.

1191 Noack, L., A. Rivoldini, and T. Van Hoolst, Volcanism and outgassing of stagnant-lid
 1192 planets: Implications for the habitable zone, *Phys. Earth Planet. Int.*, *269*, 40–57,
 1193 doi:10.1016/j.pepi.2017.05.010, 2017.

1194 Ogawa, M., G. Schubert, and A. Zebib, Numerical simulations of three-dimensional
 1195 thermal convection in a fluid with strongly temperature-dependent viscosity, *J.*
 1196 *Fluid Mech.*, *233*, 299–328, 1991.

1197 O’Neill, C., and V. Debaille, The evolution of Hadean-Eoarchaeon geodynamics,
 1198 *Earth Planet. Sci. Lett.*, *406*, 49–58, doi:10.1016/j.epsl.2014.08.034, 2014.

1199 O’Neill, C., and A. Lenardic, Geological consequences of super-sized Earths, *Geophys.*
 1200 *Res. Lett.*, *34*, 19,204–19,208, doi:10.1029/2007GL030598, 2007.

1201 O’Neill, C., A. Lenardic, L. Moresi, T. Torsvik, and C.-T. Lee, Episodic precambrian
 1202 subduction, *Earth Planet. Sci. Lett.*, *262*(3-4), 552 – 562, doi:10.1016/j.epsl.2007.
 1203 04.056, 2007.

1204 O’Neill, C., A. Lenardic, and K. C. Condie, Earth’s punctuated tectonic evolution:
 1205 cause and effect, *Geological Society of London Special Publications*, *389*, 17–40,
 1206 doi:10.1144/SP389.4, 2015.

- 1207 O'Neill, C., A. Lenardic, M. Weller, L. Moresi, S. Quenette, and S. Zhang, A win-
1208 dow for plate tectonics in terrestrial planet evolution?, *Physics of the Earth and*
1209 *Planetary Interiors*, 255, 80–92, doi:10.1016/j.pepi.2016.04.002, 2016.
- 1210 O'Neill, C., S. Marchi, S. Zhang, and W. Bottke, Impact-driven subduction on the
1211 Hadean Earth, *Nature Geoscience*, 10, 793–797, doi:10.1038/ngeo3029, 2017.
- 1212 O'Reilly, T. C., and G. F. Davies, Magma transport of heat on Io - A mecha-
1213 nism allowing a thick lithosphere, *Geophys. Res. Lett.*, 8, 313–316, doi:10.1029/
1214 GL008i004p00313, 1981.
- 1215 Pease, V., J. Percival, H. Smithies, G. Stevens, and M. Van Kranendonk, When did
1216 plate tectonics begin? evidence from the orogenic record, *Geological Society of*
1217 *America Special Papers*, 440, 199–228, 2008.
- 1218 Peters, B. J., R. W. Carlson, J. M. D. Day, and M. F. Horan, Hadean silicate
1219 differentiation preserved by anomalous $^{142}\text{Nd}/^{144}\text{Nd}$ ratios in the Réunion hotspot
1220 source, *Nature*, 555, 89–93, doi:10.1038/nature25754, 2018.
- 1221 Polat, A., P. W. Appel, and B. J. Fryer, An overview of the geochemistry of
1222 Eoarchean to Mesoarchean ultramafic to mafic volcanic rocks, SW Greenland:
1223 Implications for mantle depletion and petrogenetic processes at subduction zones
1224 in the early Earth, *Gondwana Res.*, 20(2), 255–283, 2011.
- 1225 Reimink, J. R., T. Chacko, R. A. Stern, and L. M. Heaman, Earth's earliest evolved
1226 crust generated in an Iceland-like setting, *Nature Geoscience*, 7, 529–533, doi:
1227 10.1038/ngeo2170, 2014.

- 1228 Reimink, J. R., T. Chacko, R. A. Stern, and L. M. Heaman, The birth of a cratonic
1229 nucleus: lithogeochemical evolution of the 4.02–2.94 Ga Acasta Gneiss Complex,
1230 *Precambrian Res.*, *281*, 453–472, 2016.
- 1231 Rey, P. F., N. Coltice, and N. Flament, Spreading continents kick-started plate
1232 tectonics, *Nature*, *513*, 405–408, doi:10.1038/nature13728, 2014.
- 1233 Rizo, H., M. Boyet, J. Blichert-Toft, and M. T. Rosing, Early mantle dynamics
1234 inferred from ^{142}Nd variations in Archean rocks from southwest Greenland, *Earth*
1235 *Planet. Sci. Lett.*, *377*, 324–335, doi:10.1016/j.epsl.2013.07.012, 2013.
- 1236 Rizo, H., R. J. Walker, R. W. Carlson, M. F. Horan, S. Mukhopadhyay, V. Manthos,
1237 D. Francis, and M. G. Jackson, Preservation of earth-forming events in the tung-
1238 sten isotopic composition of modern flood basalts, *Science*, *352*(6287), 809–812,
1239 doi:10.1126/science.aad8563, 2016.
- 1240 Robbins, S. J., G. di Achille, and B. M. Hynek, The volcanic history of Mars: High-
1241 resolution crater-based studies of the calderas of 20 volcanoes, *Icarus*, *211*, 1179–
1242 1203, doi:10.1016/j.icarus.2010.11.012, 2011.
- 1243 Rosas, J. C., and J. Korenaga, Rapid crustal growth and efficient crustal recycling in
1244 the early Earth: Implications for Hadean and Archean geodynamics, *Earth Planet.*
1245 *Sci. Lett.*, *494*, 42–49, doi:10.1016/j.epsl.2018.04.051, 2018.
- 1246 Rozel, A., Y. Ricard, and D. Bercovici, A thermodynamically self-consistent damage
1247 equation for grain size evolution during dynamic recrystallization, *Geophys. J.*
1248 *Intl.*, *184*, 719–728, doi:10.1111/j.1365-246X.2010.04875.x, 2011.

- 1249 Rozel, A. B., G. J. Golabek, C. Jain, P. J. Tackley, and T. Gerya, Continental
1250 crust formation on early Earth controlled by intrusive magmatism, *Nature*, *545*,
1251 332–335, doi:10.1038/nature22042, 2017.
- 1252 Sandwell, D. T., and G. Schubert, Flexural ridges, trenches, and outer rises around
1253 coronae on Venus, *J. Geophys. Res.*, *97*, 16,069, doi:10.1029/92JE01274, 1992.
- 1254 Shirey, S. B., and S. H. Richardson, Start of the Wilson Cycle at 3 Ga Shown
1255 by Diamonds from Subcontinental Mantle, *Science*, *333*, 434–436, doi:10.1126/
1256 science.1206275, 2011.
- 1257 Sizova, E., T. Gerya, M. Brown, and L. L. Perchuk, Subduction styles in the
1258 Precambrian: Insight from numerical experiments, *Lithos*, *116*, 209–229, doi:
1259 10.1016/j.lithos.2009.05.028, 2010.
- 1260 Sizova, E., T. Gerya, K. Stüwe, and M. Brown, Generation of felsic crust in the
1261 archaean: A geodynamic modeling perspective, *Precambrian Res.*, *271*, 198–224,
1262 2015.
- 1263 Skemer, P., J. M. Warren, and P. B. Kelemen, Microstructural and rheological evo-
1264 lution of a mantle shear zone, *J. Petrol.*, *51*(1-2), 43–53, doi:10.1093/petrology/
1265 egp057, 2010.
- 1266 Sleep, N., and K. Zahnle, Carbon dioxide cycling and implications for climate on
1267 ancient earth, *Journal of Geophysical Research*, *106*(E1), 1–373, 2001.
- 1268 Smithies, R. H., D. C. Champion, and M. J. Van Kranendonk, Formation of Pale-

1269 oarchean continental crust through infracrustal melting of enriched basalt, *Earth*
1270 *Planet. Sci. Lett.*, *281*, 298–306, doi:10.1016/j.epsl.2009.03.003, 2009.

1271 Smithies, R. H., T. J. Ivanic, J. R. Lowrey, P. A. Morris, S. J. Barnes, S. Wyche,
1272 and Y.-J. Lu, Two distinct origins for Archean greenstone belts, *Earth Planet. Sci.*
1273 *Lett.*, *487*, 106–116, doi:10.1016/j.epsl.2018.01.034, 2018.

1274 Solomatov, V., Scaling of temperature- and stress-dependent viscosity convection,
1275 *Phys. Fluids*, *7*, 266–274, doi:10.1063/1.868624, 1995.

1276 Solomatov, V., Fluid dynamics of a terrestrial magma ocean, in *Origin of the Earth*
1277 *and Moon*, edited by R. Canup and K. Righter, p. 555, University of Arizona Press,
1278 Tucson, 2000.

1279 Solomatov, V. S., Initiation of subduction by small-scale convection, *J. Geophys.*
1280 *Res.*, *109*(B18), B01,412, doi:10.1029/2003JB002628, 2004.

1281 Stamenkovic, V., D. Breuer, and T. Spohn, Thermal and transport properties of
1282 mantle rock at high pressure: Applications to super-earths, *Icarus*, *216*(2), 572 –
1283 596, doi:10.1016/j.icarus.2011.09.030, 2011.

1284 Stein, C., J. Schmalzl, and U. Hansen, The effect of rheological parameters on plate
1285 behaviour in a self-consistent model of mantle convection, *Phys. Earth Planet.*
1286 *Int.*, *142*, 225–255, 2004.

1287 Stein, C., J. P. Lowman, and U. Hansen, The influence of mantle internal heating
1288 on lithospheric mobility: Implications for super-Earths, *Earth Planet. Sci. Lett.*,
1289 *361*, 448–459, doi:10.1016/j.epsl.2012.11.011, 2013.

- 1290 Stern, R. J., Evidence from ophiolites, blueschists, and ultrahigh-pressure metamor-
 1291 phic terranes that the modern episode of subduction tectonics began in Neopro-
 1292 terozoic time, *Geology*, *33*, 557, doi:10.1130/G21365.1, 2005.
- 1293 Tackley, P., On the ability of phase transitions and viscosity layering to induce long-
 1294 wavelength heterogeneity in the mantle, *Geophys. Res. Lett.*, *23*, 1985–1988, 1996.
- 1295 Tackley, P., Self-consistent generation of tectonic plates in time-dependent, three-
 1296 dimensional mantle convection simulations, 1. Pseudoplastic yielding, *Geochem.*
 1297 *Geophys. Geosyst.* (G^3), *1*, doi:2000GC000036, 2000.
- 1298 Tajika, E., and T. Matsui, Evolution of terrestrial proto-co₂ atmosphere coupled
 1299 with thermal history of the earth, *Earth and planetary science letters*, *113*(1-2),
 1300 251–266, 1992.
- 1301 Tang, M., K. Chen, and R. L. Rudnick, Archean upper crust transition from mafic
 1302 to felsic marks the onset of plate tectonics, *Science*, *351*, 372–375, doi:10.1126/
 1303 science.aad5513, 2016.
- 1304 Tasaka, M., M. E. Zimmerman, and D. L. Kohlstedt, Rheological weakening of olivine
 1305 + orthopyroxene aggregates due to phase mixing: 1. Mechanical behavior, *J. Geo-*
 1306 *phys. Res. Solid Earth*, *122*(10), 7584–7596, doi:10.1002/2017JB014333, 2017a.
- 1307 Tasaka, M., M. E. Zimmerman, D. L. Kohlstedt, H. Stünitz, and R. Heilbronner,
 1308 Rheological weakening of olivine + orthopyroxene aggregates due to phase mixing:
 1309 Part 2. Microstructural development, *J. Geophys. Res. Solid Earth*, *122*(10), 7597–
 1310 7612, doi:10.1002/2017JB014311, 2017b.

- 1311 Thébaud, N., and P. F. Rey, Archean gravity-driven tectonics on hot and flooded
1312 continents: Controls on long-lived mineralised hydrothermal systems away from
1313 continental margins, *Precambrian Research*, *229*, 93–104, doi:10.1016/j.precamres.
1314 2012.03.001, 2013.
- 1315 Thielmann, M., Grain size assisted thermal runaway as a nucleation mechanism for
1316 continental mantle earthquakes: Impact of complex rheologies, *Tectonophysics*,
1317 doi:10.1016/j.tecto.2017.08.038, 2017.
- 1318 Tosi, N., et al., The habitability of a stagnant-lid Earth, *Astron. Astrophys.*, *605*,
1319 A71, doi:10.1051/0004-6361/201730728, 2017.
- 1320 Trela, J., E. Gazel, A. V. Sobolev, L. Moore, M. Bizimis, B. Jicha, and V. G.
1321 Batanova, The hottest lavas of the Phanerozoic and the survival of deep Archaean
1322 reservoirs, *Nature Geoscience*, *10*, 451–456, doi:10.1038/ngeo2954, 2017.
- 1323 Turcotte, D., and G. Schubert, *Geodynamics*, 2nd ed., Cambridge Univ. Press, New
1324 York, 2002.
- 1325 Turner, S., T. Rushmer, M. Reagan, and J.-F. Moyen, Heading down early on? Start
1326 of subduction on Earth, *Geology*, *42*, 139–142, doi:10.1130/G34886.1, 2014.
- 1327 Valencia, D., and R. J. O’Connell, Convection scaling and subduction on Earth and
1328 super-Earths, *Earth Planet. Sci. Letts.*, *286*, 492–502, doi:10.1016/j.epsl.2009.07.
1329 015, 2009.
- 1330 Valencia, D., R. J. O’Connell, and D. D. Sasselov, Inevitability of Plate Tectonics
1331 on Super-Earths, *Astrophys. J.*, *670*, L45–L48, doi:10.1086/524012, 2007.

- 1332 Valley, J. W., W. H. Peck, E. M. King, and S. A. Wilde, A cool early Earth, *Geology*,
1333 30, 351, doi:10.1130/0091-7613(2002)030<0351:ACEE>2.0.CO;2, 2002.
- 1334 van Heck, H., and P. Tackley, Planforms of self-consistently generated plates
1335 in 3d spherical geometry, *Geophys. Res. Lett.*, 35, L19,312, doi:doi:10.1029/
1336 2008GL035190, 2008.
- 1337 van Heck, H. J., and P. J. Tackley, Plate tectonics on super-Earths: Equally or more
1338 likely than on Earth, *Earth Planet. Sci. Lett.*, 310, 252–261, doi:10.1016/j.epsl.
1339 2011.07.029, 2011.
- 1340 van Hunen, J., and J.-F. Moyen, Archean Subduction: Fact or Fiction?, *Annu. Rev.*
1341 *Earth Planet. Sci.*, 40, 195–219, doi:10.1146/annurev-earth-042711-105255, 2012.
- 1342 van Hunen, J., and A. P. van den Berg, Plate tectonics on the early Earth: Limi-
1343 tations imposed by strength and buoyancy of subducted lithosphere, *Lithos*, 103,
1344 217–235, doi:10.1016/j.lithos.2007.09.016, 2008.
- 1345 Van Kranendonk, M. J., Two types of Archean continental crust: Plume and plate
1346 tectonics on early Earth, *Am. J. Sci.*, 310(10), 1187–1209, 2010.
- 1347 Van Kranendonk, M. J., R. H. Smithies, W. L. Griffin, D. L. Huston, A. H. Hick-
1348 man, D. C. Champion, C. R. Anhaeusser, and F. Pirajno, Making it thick: a vol-
1349 canic plateau origin of Palaeoarchean continental lithosphere of the Pilbara and
1350 Kaapvaal cratons, *Geological Society of London Special Publications*, 389, 83–111,
1351 doi:10.1144/SP389.12, 2015.

- 1352 Walker, J., P. Hayes, and J. Kasting, A negative feedback mechanism for the long-
 1353 term stabilization of Earth’s surface temperature, *J. Geophys. Res.*, *86*, 9776–9782,
 1354 doi:10.1029/JC086iC10p09776, 1981.
- 1355 Walzer, U., and R. Hendel, Mantle convection and evolution with growing continents,
 1356 *J. Geophys. Res. Solid Earth*, *113*, B09405, doi:10.1029/2007JB005459, 2008.
- 1357 Walzer, U., and R. Hendel, Continental crust formation: Numerical modelling of
 1358 chemical evolution and geological implications, *Lithos*, *278*, 215–228, doi:10.1016/
 1359 j.lithos.2016.12.014, 2017.
- 1360 Warren, J. M., and G. Hirth, Grain size sensitive deformation mechanisms in nat-
 1361 urally deformed peridotites, *Earth Planet. Sci. Letts.*, *248*(1-2), 438 – 450, doi:
 1362 10.1016/j.epsl.2006.06.006, 2006.
- 1363 Weinstein, S., and P. Olson, Thermal convection with non-newtonian plates, *Geo-*
 1364 *phys. J. Int.*, *111*, 515–530, doi:10.1111/j.1365-246X.1992.tb02109.x, 1992.
- 1365 Weller, M. B., and A. Lenardic, Hysteresis in mantle convection: Plate tectonics
 1366 systems, *Geophys. Res. Lett.*, *39*, L10202, doi:10.1029/2012GL051232, 2012.
- 1367 Weller, M. B., and A. Lenardic, The energetics and convective vigor of mixed-mode
 1368 heating: Velocity scalings and implications for the tectonics of exoplanets, *Geo-*
 1369 *phys. Res. Lett.*, *43*(18), 9469–9474, doi:10.1002/2016GL069927, 2016.
- 1370 Weller, M. B., A. Lenardic, and C. O’Neill, The effects of internal heating and large
 1371 scale climate variations on tectonic bi-stability in terrestrial planets, *Earth Planet.*
 1372 *Sci. Lett.*, *420*, 85–94, doi:10.1016/j.epsl.2015.03.021, 2015.

- 1373 White, S., S. Burrows, J. Carreras, N. Shaw, and F. Humphreys, On mylonites in
1374 ductile shear zones, *J. Struct. Geol.*, *2*, 175–187, 1980.
- 1375 Wong, T., and V. S. Solomatov, Towards scaling laws for subduction initiation on
1376 terrestrial planets: constraints from two-dimensional steady-state convection sim-
1377 ulations, *Prog. Earth Planet. Sci.*, *2*, 18, doi:10.1186/s40645-015-0041-x, 2015.
- 1378 Zhong, S., Dynamics of thermal plumes in three-dimensional isoviscous thermal
1379 convection, *Geophy. J. Int.*, *162*, 289–300, doi:10.1111/j.1365-246X.2005.02633.x,
1380 2005.
- 1381 Zhong, S., and A. B. Watts, Lithospheric deformation induced by loading of the
1382 Hawaiian Islands and its implications for mantle rheology, *J. Geophys. Res. Solid*
1383 *Earth*, *118*, 6025–6048, doi:10.1002/2013JB010408, 2013.