

# Crucial Physical Dependencies of the Core-Collapse Supernova Mechanism

A. Burrows<sup>1</sup> · D. Vartanyan<sup>1</sup> · J.C. Dolence<sup>2</sup> ·  
M.A. Skinner<sup>3</sup> · D. Radice<sup>4</sup>

Received: 25 October 2017 / Accepted: 19 November 2017

© The Author(s) 2018. This article is published with open access at Springerlink.com

**Abstract** We explore with self-consistent 2D FORNAX simulations the dependence of the outcome of collapse on many-body corrections to neutrino-nucleon cross sections, the nucleon-nucleon bremsstrahlung rate, electron capture on heavy nuclei, pre-collapse seed perturbations, and inelastic neutrino-electron and neutrino-nucleon scattering. Importantly, proximity to criticality amplifies the role of even small changes in the neutrino-matter couplings, and such changes can together add to produce outsized effects. When close to the critical condition the cumulative result of a few small effects (including seeds) that individually have only modest consequence can convert an anemic into a robust explosion, or even a dud into a blast. Such sensitivity is not seen in one dimension and may explain the apparent heterogeneity in the outcomes of detailed simulations performed internationally. A natural conclusion is that the different groups collectively are closer to a realistic understanding of the mechanism of core-collapse supernovae than might have seemed apparent.

---

Supernovae

Edited by Andrei Bykov, Roger Chevalier, John Raymond, Friedrich-Karl Thielemann, Maurizio Falanga and Rudolf von Steiger

---

✉ A. Burrows  
[burrows@astro.princeton.edu](mailto:burrows@astro.princeton.edu)

D. Vartanyan  
[dvartany@astro.princeton.edu](mailto:dvartany@astro.princeton.edu)

J.C. Dolence  
[jdoelnce@lanl.gov](mailto:jdoelnce@lanl.gov)

M.A. Skinner  
[skinner15@llnl.gov](mailto:skinner15@llnl.gov)

D. Radice  
[dradice@astro.princeton.edu](mailto:dradice@astro.princeton.edu)

<sup>1</sup> Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544, USA

<sup>2</sup> CCS-2, Los Alamos National Laboratory, P.O. Box 1663, Los Alamos, NM 87545, USA

<sup>3</sup> Livermore National Laboratory, 7000 East Ave., Livermore, CA 94550-9234, USA

<sup>4</sup> Schmidt Fellow, Institute for Advanced Study, 1 Einstein Drive, Princeton, NJ 08540, USA

**Keywords** Supernova theory · Neutrino physics · Multi-dimensional radiation/hydrodynamics

## 1 Introduction

A goal of core-collapse supernova theory is to explain the mechanism of explosion. It is an accepted truism of the field that a necessary condition for this is that complicated multi-dimensional simulation codes incorporating the requisite neutrino, nuclear, and gravitational physics reproduce such explosions robustly, yielding at the very least the requisite asymptotic energies, residual neutron star masses, and nucleosynthesis. A simple analytic explanation has not been forthcoming and, given the manifest complexities of the process, would not be deemed credible. It is thought that one litmus test of success would be such a demonstration for a non-rotating model between  $\sim 8$  and  $\sim 20$   $M_{\odot}$ , the progenitor ZAMS (Zero-Age Main-Sequence) mass regime that must provide the lion's share of core-collapse supernova events.

However, to date the various groups engaged in such efforts around the world have failed to agree on the outcomes of the collapse of otherwise similar progenitor massive star cores. This is despite claims to have embedded the necessary physics and microphysics into the simulations. In fact, the numerical algorithms, resolutions, and input physics all differ, and even when the physics is deemed similar, the implementations and approximations surely differ. The ORNL group (Bruenn et al. 2013, 2016), with their CHIMERA code, uses multi-group flux-limited diffusion (MGFLD) neutrino transport (Bruenn 1985), the VH-1 Newtonian hydrodynamics package, a monopole correction for general relativity (GR) (Marek et al. 2006), but multiple one-dimensional solves for multi-dimensional transport using the so-called “ray-by-ray+” approach (Buras et al. 2003; Burrows et al. 1995). Such a dimensional reduction for the transport, particularly manifest in 2D, ignores lateral, non-radial radiative transport, which has been shown to be of quantitative (Ott et al. 2008; Brandt et al. 2011; Burrows 2013; Dolence et al. 2015; Sumiyoshi et al. 2015) and qualitative (Skinner et al. 2016) importance. To the point, Skinner et al. (2016) have shown that the ray-by-ray anomalies in the angular distribution of the radiation field and corresponding neutrino heating rates can reinforce the axial sloshing motions in 2D and push the shock into explosion.<sup>1</sup> Bruenn et al. (2013, 2016) find explosions in 2D (axially symmetry) for all the progenitors they studied (the 12-, 15-, 20-, and 25- $M_{\odot}$  models of Woosley and Heger 2007), but the models all explode at about the same post-bounce time ( $\sim 100$  milliseconds) and the shock radii never decrease in value. When performed in 3D for the 15- $M_{\odot}$  model of Woosley and Heger (2007), Lentz et al. (2015) obtain a weaker explosion delayed in its onset by an extra  $\sim 100$  milliseconds.

Müller et al. (2012a, 2012b), using the conformally-flat CoCoNuT hydrodynamics code in combination with the VERTEX transport solver and the ray-by-ray+ approach, find that models explode in 2D, but explode with lower energies and at post-bounce explosion times that differ significantly from those found by the ORNL group. In addition, their shock radii generally decrease from a peak occurring near a time  $\sim 200$  ms after bounce, before increasing just prior to explosion hundreds of milliseconds later (and all at different post-bounce times). Using the VERTEX-PROMETHEUS code, the Garching group obtained weak explosions in 2D for a 11.2- $M_{\odot}$  progenitor (Buras et al. 2006) and for a rotating 15- $M_{\odot}$  progenitor (Marek and Janka 2009), though the outcomes when proper correction is made for

<sup>1</sup> However, the general absence in 3D of either an axial effect or the pronounced sloshing seen in 2D may be rendering 3D simulations performed with the ray-by-ray approach less problematic. This has yet to be tested.

the corresponding mantle binding energies were not clear. More recently, the Garching group (Summa et al. 2016, 2018) obtained explosions in 2D for a broad range of Woosley and Heger (2007) progenitors from 11 to 28  $M_{\odot}$ , but these calculations as well did not comport with those of the ORNL group in the timescales and energies seen. The Garching group has also used for all their multi-D VERTEX supernova simulations a variant of the problematic ray-by-ray+ dimensionally-reduced transport approach.

However, Murphy et al. (2013) and Couch and Ott (2015), and originally Burrows et al. (1995), highlight the importance of turbulent pressure behind the shock as an aid to explosion, but note that such a pressure is larger (artificially) in 2D than in 3D. Turbulent pressure is also (possibly) more anisotropic in 2D, favoring the radial stress component, further enhancing the prospects (again, artificially) for overcoming the accretion ram pressure. Hence, the current explosions in 2D may in part, or at times, be numerical artifacts.

Importantly, though Hanke et al. (2012) have speculated that the sloshing motion oftentimes associated in 2D with the SASI (standing accretion shock instability) may be crucial to explosion, the recent non-rotating default VERTEX-PROMETHEUS calculations in 3D by that same Garching group (that at times manifest the SASI) do not explode (Hanke et al. 2013; Tamborra et al. 2014), even though the corresponding 2D simulations did. As an aside, Burrows et al. (2012) note that such a pronounced axial sloshing motion is rarely in evidence in 3D. However, with altered microphysics, in particular with a change in the axial-vector coupling constant ( $g_A$ ) due to a speculative enhanced effect on the nucleon spin of the strange quark, Melson et al. (2015) do obtain a weak explosion in 3D of the Woosley and Heger (2007) 20- $M_{\odot}$  in 3D. The difference in outcome is due to the consequent decrease in the neutrino-neutron neutral-current scattering cross section in the neutron-rich envelope of the proto-neutron star bounded by the stalled shock and the resultant increase in the electron-neutrino luminosity and average energy that are instrumental in heating this envelope. However, the magnitude of the strangeness correction employed by Melson et al. may be larger than experiment allows (Ahmed et al. 2012; Green et al. 2017). Furthermore, it is not clear that all these currently published under-powered 3D explosions will actually succeed as an explosion after traversing the entire star and after the mass cut between ejecta and residual core is determined hydrodynamically. An exception is the recent work of Müller et al. (2017), who perform 3D multi-group simulations using their simpler FMT method (Müller and Janka 2015) for an 18- $M_{\odot}$  progenitor model evolved in 3D to collapse. Such a 3D progenitor naturally manifests seed perturbations that Müller et al. (2017) show are instrumental in leading to an explosion with a respectable energy.

The calculations of Burrows et al. (2006a, 2006b, 2007a) and Ott et al. (2008), using the VULCAN/2D code, and Dolence et al. (2015), using the CASTRO code (Zhang et al. 2011, 2013) employed multi-dimensional transport, and not ray-by-ray+, but in neither of these 2D studies did the authors see explosions by the neutrino mechanism. VULCAN/2D did not have all the terms to order  $v/c$  in the transport, but CASTRO did, and the results were similar (Dolence et al. 2015). Importantly, neither VULCAN/2D nor CASTRO made corrections for the effects of general relativity, and this could explain in part the different outcome. However, since other self-consistent calculations (summarized previously) that obtained explosions in 2D used the ray-by-ray scheme, while the VULCAN/2D and CASTRO studies did not, one is tempted to suggest that the ray-by-ray approach may in 2D be yielding qualitatively incorrect results.

Suwa et al. (2010) obtain an explosion in 2D of a 13- $M_{\odot}$  progenitor, while Takiwaki et al. (2012) obtain an explosion for an 11.2- $M_{\odot}$  progenitor in both 2D and 3D. Both these efforts, however, neglect  $\nu_{\mu}$  and  $\nu_{\tau}$  neutrinos, which constitute roughly 50% of the total neutrino losses after bounce, and use the IDSA (Liebendörfer et al. 2009) and ray-by-ray

approximations for the transport. Suwa et al. (2016) continued their explorations in 2D with a large suite of progenitor simulations, but continue to neglect  $\nu_\mu$  and  $\nu_\tau$  neutrinos and use the IDSA plus ray-by-ray+ transport methods. They highlight a possible role in the explosion systematics of transitions in the mass accretion rate. Ott et al. (2013) perform fully general-relativistic 3D simulations, employing a leakage scheme for all the neutrinos. Their goal was to explore the relative role of the SASI and neutrino-driven convection, and they found for their simulation of the  $27\text{-M}_\odot$  progenitor of Woosley et al. (2002) that neutrino-driven convection dominated once it started. Roberts et al. (2016), using full GR hydrodynamics and an M1 transport scheme (Sect. 2) roughly similar to ours (but without the velocity-dependent terms in the transport, inelastic scattering, or many-body effects), emphasize the importance of spatial resolution in determining whether and how the same  $27\text{-M}_\odot$  model explodes, as well as the different outcomes for octant and full  $4\pi$  steradian simulations. Kuroda et al. (2016) have achieved a fully general-relativistic 3D code, also using the M1 transport closure, but have yet to simulate progenitor models beyond a few tens of milliseconds post-bounce. Pan et al. (2016) have constructed a 2D non-relativistic (Newtonian) neutrino radiation/hydrodynamic scheme using the IDSA transport approach for the  $\nu_e$  and  $\bar{\nu}_e$  neutrinos and a leakage scheme for the  $\nu_\mu$  neutrinos. Importantly, they do not use the ray-by-ray+ approach, but follow the transport of  $\nu_e$  and  $\bar{\nu}_e$  neutrinos multi-dimensionally. They obtain explosions for all the progenitor models studied.

Suwa et al. (2010) and Nakamura et al. (2014) found that rotation aided explosion, mostly by rotationally expanding the size of the gain region and increasing the mass it contained. Iwakami et al. (2014) and Takiwaki et al. (2016) highlight the rotational excitation of  $m = 1$  spiral-arm modes and find a role for non-axisymmetric rotational instabilities. Iwakami et al. (2014) used a light-bulb neutrino scheme, and neglected “ $\nu_\mu$ ” neutrinos. Both Nakamura et al. (2014) and Takiwaki et al. (2016) observed equatorial explosions in the rapidly-rotating context. Recently, Janka et al. (2016) and Summa et al. (2018) published a rapidly-rotating 3D model that exploded and highlighted the potential role of an “ $m = 1$ ” structure in the gain region. Earlier, Fryer and Heger (2000) used SPH for the hydrodynamics and a simplified gray scheme for the neutrino transport to explore the role of rapid rotation. Moreover, in all of these studies the initial rotation rate was not only high in the mantle, but was high in the core. Such rapid initial spins (periods of a few seconds) and final spins (periods of  $\sim 2\text{--}10$  milliseconds) seem not to be consistent with inferred pulsar spin periods at birth (crudely,  $\sim 300 \pm 200$  milliseconds; Emmering and Chevalier 1989; Faucher-Giguere and Kaspi 2006; Popov and Turolla 2012; Noutsos et al. 2013) and may be associated only with hypernovae (Burrows et al. 2007c) and/or gamma-ray bursts (MacFadyen and Woosley 1999).

In this paper, we explore, with self-consistent 2D FORNAX (Sect. 2) simulations, the dependence of the outcome of collapse (most notably whether the model explodes) on neutrino-nucleon scattering rates (via modifications of in-medium response corrections due to many-body effects), pre-collapse convective perturbations, inelastic neutrino-electron scattering, and inelastic neutrino-nucleon scattering. We also continue our study, started in Skinner et al. (2016), of the issues raised by the use of the ray-by-ray+ method. What we find is that when the proto-neutron star bounded by a stalled shock is close to the critical condition for explosion (Burrows and Goshy 1993), as it easily can be in the turbulent multi-D context, the sensitivity to explosion of small changes in the physical inputs is amplified. The magnitude of such changes might be only  $\sim 20\%$ , but the result can be qualitatively different, in particular whether the model explodes. In the 1D (spherical) case, the core is not sensitive to comparable changes (“Mazurek’s Law”), but in the multi-D turbulent (and chaotic) context, small changes in the physics can have a qualitative effect on explodability. This may explain why the various groups around the world simulating core-collapse supernovae

can witness very different outcomes, despite the fact that they ostensibly are incorporating almost the same microphysics and similar computational approaches. Small differences are amplified near criticality in this chaotic context. The availability of a new generation of fast, but accurate, simulation codes, such as FORNAX (Sect. 2), and significant supercomputer resources enable rapid multi-parameter investigations in the multi-dimensional (in particular 2D), multi-physics context. Such wide-ranging explorations reveal patterns not easily discerned when one (or only a few) simulations are the focus of a paper and its (or their) results solely are mined.

## 2 Numerical Method and Computational Setup

We have developed an entirely new multi-dimensional, multi-group radiation/hydrodynamic code, FORNAX, for the study of core-collapse supernovae. This code is described in detail in an upcoming paper (in preparation). For the purposes of this paper, we note that it employs spherical coordinates in one and two spatial dimensions, solves the comoving-frame, multi-group, two-moment, velocity-dependent transport equations to  $O(v/c)$ , and uses the M1 tensor closure for the second and third moments of the radiation fields (Dubroca and Feugeas 1999; Vaytet et al. 2011). Three species of neutrino ( $\nu_e$ ,  $\bar{\nu}_e$ , and “ $\nu_\mu$ ” [ $\nu_\mu$ ,  $\bar{\nu}_\mu$ ,  $\nu_\tau$ , and  $\bar{\nu}_\tau$  lumped together]) are followed using an explicit Godunov characteristic method applied to the radiation transport operators, but an implicit solver for the radiation source terms.

The hydrodynamics in FORNAX is based on a directionally-unsplit Godunov-type finite-volume method. Fluxes at cell faces are computed with the fast and accurate HLLC approximate Riemann solver based on left and right states reconstructed from the underlying volume-averaged states. In the interior, to alleviate Courant limits due to converging angular zones, the code can deresolve in angle with decreasing radius, conserving hydrodynamic and radiative fluxes in a manner similar to the method employed in AMR codes at refinement boundaries. Gravity is handled in 2D and 3D with a monopole or a multipole solver (Müller and Steinmetz 1995). When using the latter, we generally set the maximum spherical harmonic order necessary equal to twelve. The monopole gravitational term is altered to accommodate approximate general-relativistic gravity (Marek et al. 2006), and we employ the metric terms,  $g_{rr}$  and  $g_{tt}$ , derived from this potential to incorporate general relativistic redshift effects in the neutrino transport equations (in the manner of Rampp and Janka 2002). In 2D, rotation and a third component of the velocity vector can be included in the hydrodynamics. We use the SFHo equation of state (EOS) by default (Steiner et al. 2013), but in this paper do compare with results using the DD2 EOS (Banik et al. 2014).<sup>2</sup>

For these simulations, we follow twenty energy ( $\varepsilon_\nu$ ) groups for each of the  $\nu_e$ ,  $\bar{\nu}_e$ , and “ $\nu_\mu$ ” species (again, the four species,  $\nu_\mu$ ,  $\bar{\nu}_\mu$ ,  $\nu_\tau$ , and  $\bar{\nu}_\tau$  lumped together.) For the  $\nu_e$  types, the neutrino energy  $\varepsilon_\nu$  varies logarithmically from 1 MeV to 300 MeV, while it varies from 1 MeV to 100 MeV for the  $\bar{\nu}_e$  s and  $\nu_\mu$  s. We have performed calculations with forty energy groups and found little difference in the results. The radial coordinate,  $r$ , runs from 0 to 20,000 kilometers (km) in 608 zones. The radial grid smoothly transitions from uniform spacing with  $\Delta r = 0.5$  km in the interior to logarithmic spacing, with a transition radius near  $\sim 100$  km. The polar angular grid spacing covers the full  $180^\circ$  and varies smoothly from  $\approx 0.95^\circ$  at the poles to  $\approx 0.65^\circ$  at the equator in 256 zones.

<sup>2</sup>In a earlier version of this paper, we used the  $K = 220$  MeV Lattimer-Swesty equation of state (Lattimer and Swesty 1991) for all our simulations, but since this EOS has been shown to be inconsistent with recent measurements we redid the models and paper using EOSes still consistent with what is known.

A comprehensive set of neutrino-matter interactions are followed in FORNAX, and these are described in Burrows et al. (2006a, 2006b). Inelastic neutrino-nucleon scattering is handled using a modified version of the Thompson et al. (2003) approach (Sect. 4). Our neutrino microphysics is more comprehensively listed in our upcoming code paper.

### 3 Many-Body Neutrino Response Corrections

Melson et al. (2015) invoked a modification in the axial-vector coupling constant ( $g_A$ ) due to a possible strangeness contribution to the nucleon spin of  $g_A^s = -0.2$ . This results in an approximate decrease in the neutrino-nucleon scattering rate of  $\sim 20\%$  and in Melson et al. the consequence was an explosion in 3D, even though they did not witness an explosion in 3D when using their default microphysical suite. Curiously, without their strangeness correction, the same model exploded in 2D. However, the value of the correction,  $g_A^s$ , they employed in their 3D model is likely too large and  $g_A^s$  may be closer to zero (Ahmed et al. 2012; Green et al. 2017).

Many-body corrections to neutral-current and charged-current neutrino-nucleon interactions have been discussed in the past (Burrows and Sawyer 1998, 1999; Hannestad and Raffelt 1998; Reddy et al. 1999; Roberts et al. 2012) in the context of proto-neutron stars and supernovae, and have been known to affect the neutrino-matter reaction rates. Burrows and Sawyer (1998) in particular suggested that many-body corrections to the axial-vector and vector structure factors for neutrino-nucleon scattering could be of a magnitude sufficient to be of relevance to the viability of the neutrino-driven mechanism of core-collapse supernovae, but did not provide a robust estimate of the magnitude of this diminution much below nuclear densities.

The effect of the many-body correction to neutral-current neutrino-nucleon scattering in the supernova context is mostly due to the increase in the  $\nu_\mu$  luminosity occasioned by the decrease in the associated  $\nu_\mu + (n, p) \rightarrow \nu_\mu + (n, p)$  scattering cross section for densities above  $\sim 10^{12} \text{ g cm}^{-3}$ ; this causes a further compression in the core. Such a compression, similar to the effect of GR, raises the temperatures near the  $\nu_e$  and  $\bar{\nu}_e$  neutrinospheres, thereby raising their associated luminosities and average emergent neutrino energies. These changes increase the neutrino-matter heating rates in the gain region and, hence, facilitate explosion. Since the super-allowed charged-current absorption reactions still dominate the  $\nu_e/\bar{\nu}_e$ -matter interaction rates, the direct effect of this structure factor correction to the axial-vector term in the neutrino-nucleon scattering rate on the  $\nu_e$  and  $\bar{\nu}_e$  luminosities is slight.

A many-body structure factor ( $S_A$ ) correction to the axial-vector term in the neutrino-nucleon scattering rate due to the neutrino response to nuclear matter at (low) densities below  $\sim 10^{13} \text{ g cm}^{-3}$  was recently derived by Horowitz et al. (2017) using a virial approach. These authors derive a fit:

$$S_A = \frac{1}{1 + A(1 + Be^{-C})}, \quad (1)$$

where

$$A = A_0 \frac{n(1 - Y_e + Y_e^2)}{T^{1.22}} \quad (2)$$

$$B = \frac{B_0}{T^{0.75}} \quad (3)$$

$$C = C_0 \frac{nY_e(1 - Y_e)}{T^{0.5}} + D_0 \frac{n^4}{T^6}. \quad (4)$$

In these equations,  $T$  is the temperature in MeV,  $Y_e$  is the electron fraction,  $n$  is the baryon density in  $\text{fm}^{-3}$ ,  $A_0 = 920$ ,  $B_0 = 3.05$ ,  $C_0 = 6140$ , and  $D_0 = 1.5 \times 10^{13}$ . Horowitz et al. (2017) join their fit to Burrows and Sawyer (1998) for the higher densities, but were most careful fitting their formula for temperatures between 5 and 10 MeV. Nevertheless, though Horowitz et al. (2017) intended their fit to apply at all densities, temperatures, and  $Y_e$  s, (and we use it in this paper at all thermodynamic points), one should be aware that no current approach to this physics is likely to be correct at the highest densities above  $\sim 10^{14} \text{ g cm}^{-3}$ . Therefore, use of this formula in supernova and proto-neutron-star cores should be considered provisional. Fortunately, since such densities are too high to affect the evolution during the first second post bounce, and are most relevant during the later proto-neutron-star cooling phase, the values of the Horowitz correction at the highest densities are not germane to the conclusions of this paper.

However, many-body effects in the charged-current sector and on absorption may be comparable (Burrows and Sawyer 1999; Roberts et al. 2012; Fischer 2016), but have not yet been factored in. Therefore, neglected is the effect of final-state nucleon blocking for charged-current absorption reactions. Blocking is important only at high densities, where many-body interaction effects are likely to be even larger. Therefore, we have postponed their inclusion until such corrections, which must for self-consistency be done with the same interaction model that informed the equation of state employed, are available.

The fit derived by Horowitz et al. (2017) to the structure factor applied to  $g_A^2$  translates into a decrease in the neutrino-nucleon scattering cross section in the crucial region at and deeper than the various neutrinospheres of  $\sim 5\%$  to  $\sim 35\%$ . This effect is a function of density, temperature, and electron fraction ( $Y_e$ ). Horowitz et al. (2017) state that the corresponding structure factor for the vector current is likely greater than one, but since the vector contribution to neutrino-nucleon scattering is small, this is likely to be subdominant. The upshot is a potentially important, and physically plausible, decrease in the neutrino-matter scattering rates that translates into an increase in the driving  $\nu_e$  and  $\bar{\nu}_e$  luminosities and average energies, thereby increasing the heating rate in the gain region.

We note that the corresponding many-body correction for charged-current interactions may be in the same direction (Fischer 2016; Burrows and Sawyer 1999, although see Roberts et al. 2012) and could also be important (Sect. 5.3). The correction would be small at low densities in the gain region, but higher deeper inside, where the neutrinospheres reside. If the rates are suppressed, this could increase the  $\nu_e$  and  $\bar{\nu}_e$  luminosities, while simultaneously not decreasing the heating in the gain region and is not like a uniform correction at all radii. Such behavior, if it obtains, would be near optimal for aiding the explosion.

## 4 Inelastic Scattering

Neutrino-electron scattering rates and cross sections are much smaller than those for neutrino-nucleon scattering, which themselves are smaller still than those for super-allowed charged-current reactions such as  $\nu_e + n \rightarrow p + e^-$ . For  $\varepsilon_\nu = 10 \text{ MeV}$ , this deficit is approximately two orders of magnitude. However, due to the small mass of the electron, the energy transfer to the matter during a “Compton-like” neutrino-electron scattering is on average quite large, while, due to the large mass of the nucleon, the corresponding average energy transfer during neutrino-nucleon scattering is rather small. Therefore, the large cross section for neutrino-nucleon scattering multiplied by the small associated energy transfer can be comparable to the product of the small neutrino-electron cross section with the large per-interaction energy transfer and depend upon temperature, density, and neutrino energy

(Janka et al. 1996; Thompson et al. 2000). The upshot is that inelastic scattering off both electrons and nucleons can modify thermal profiles and heating rates exterior to the neutrinospheres and in the gain region and contribute to explosion by the neutrino heating mechanism. Moreover, Müller et al. (2012b) make the point that heating by  $\nu_\mu$ -nucleon inelastic energy transfer can boost the temperatures near the  $\nu_e$  and  $\bar{\nu}_e$  neutrinospheres and results in slightly higher  $\nu_e$  and  $\bar{\nu}_e$  energy luminosities, which in turn enhance heating behind the shock correspondingly.

The detailed theory of the structure functions and redistribution kernels for such inelastic scattering, including the effects of final-state blocking and the thermal spectrum of the targets, can be found in Burrows et al. (2006a, 2006b), Reddy et al. (1999), Thompson et al. (2003), and Thompson et al. (2000). Pioneering work on inelastic scattering off electrons in the core-collapse context can be found in Bruenn (1985) and Mezzacappa and Bruenn (1993). However, those latter papers were focussed on the downscattering effect due to inelastic  $\nu_e - e^-$  scattering on the electron neutrinos produced during infall and the consequent decrease in the trapped lepton fraction. Since a larger trapped lepton fraction could help facilitate immediate post-bounce explosions (Burrows and Lattimer 1983), this quantity was more relevant when the prompt hydrodynamic supernova mechanism still seemed viable. However, with the emergence of the delayed, neutrino-driven mechanism (Bethe and Wilson 1985), and the conclusion that the prompt mechanism could not work due to catastrophic neutrino losses at and around shock breakout, the value of the trapped lepton fraction, and its precise value, receded in significance.

Nevertheless, heating behind the stalled shock due to inelastic energy transfer from neutrinos to both electrons and nucleons, or boosting the  $\nu_e$  and  $\bar{\nu}_e$  luminosities by  $\nu_\mu$  down-scattering near their neutrinospheres (Müller et al. 2012b), may help achieve the critical condition for explosion, particularly when in concert with the inclusion of the in-medium neutrino response (Horowitz et al. 2017; Sect. 3) and the slightly net positive influence of GR. Heating by inelastic neutrino-electron scattering is still sub-dominant with respect to that due to charged-current  $\nu_e$  and  $\bar{\nu}_e$  absorption, and in 1D (spherical) simulations there is almost no hydrodynamic consequence of its inclusion (Thompson et al. 2003). The same can be said of inelastic neutrino-nucleon scattering (Janka et al. 1996; Burrows and Sawyer 1998, 1999; Thompson et al. 2000). However, in the realistic multi-D context of the core-collapse phenomenon, the cumulative effect of the addition of a few sub-dominant heating mechanisms, compression due to enhanced  $\nu_\mu$  neutrino losses and consequent  $\nu_e$  and  $\bar{\nu}_e$  neutrinosphere heating,<sup>3</sup> and greater proximity to the critical condition due to multi-D effects<sup>4</sup> amplifies the leverage of even small additions to the gain-region heating power over their effects individually and can convert an anemic explosion into a robust explosion, or even a dud into a blast. One recalls that the original delayed mechanism of Wilson required for explosion only a modest enhancement of  $\sim 25\%$  in the neutrino luminosity.<sup>5</sup>

From the work of Thompson et al. (2000) and Tubbs (1979), we find that the crossover energy between upscattering and downscattering is nearer  $6k_B T$  (not  $3k_B T$ , as in Müller and Janka 2015), where  $k_B$  is Boltzmann's constant and  $T$  is the temperature, around densities of  $\sim 10^{11} \text{ g cm}^{-3}$  to  $\sim 10^{13} \text{ g cm}^{-3}$  and so our approximate redistribution rate for  $\nu_\mu$  s is

<sup>3</sup> as in neutrino-electron scattering and many-body scattering rate suppression

<sup>4</sup> Examples include the enhancement of the stress behind the shock due to turbulent pressure (Burrows et al. 1995; Murphy et al. 2013; Janka 2012; Burrows 2013) and the modest increase in the dwell time in the gain region of the post-shock matter (Murphy and Burrows 2008; Dolence et al. 2013)

<sup>5</sup> In that case, it was due to “neutron-finger convection,” subsequently later shown not to occur (Bruenn and Dineva 1996; Dessart et al. 2006).

proportional to  $\kappa_{scat}(\varepsilon_\mu - 6k_B T)/m_n c^2$ , where  $\kappa_{scat}$  is the  $\nu_\mu$  scattering opacity and  $m_n$  is the neutron mass.

Inelastic scattering off nucleons lowers the  $\nu_\mu$  luminosity, while the corresponding quantities for the  $\nu_e$  and  $\bar{\nu}_e$  are slightly increased (Müller et al. 2012b). The latter responses explain the positive effect on explodability of the inclusion of inelastic scattering off nucleons. The direct effect of such inelasticity is in the core, and the effect in the shocked mantle is indirect.

## 5 Microphysical Dependencies of the 2D Explosion Models

For a set of 4 fiducial models (with progenitor masses of 13, 15, 16, and 20  $M_\odot$ ), we performed a parameter study of input physics highlighting the role of small changes in promoting (or preventing) explosion. We refer the reader to the upcoming paper by Vartanyan et al. (2018, submitted) for a more detailed description of these simulations. When models explode, the time to explosion can vary significantly with inputs. The relative time of explosion can help one gauge the role of the inputs in question.<sup>6</sup> While there are many combinatoric possibilities, we settled on just a few comparisons to demonstrate the effects we see universally. We employ the notation IES, INS, MB, pert, and rbrp to indicate “inelastic neutrino-electron,” “inelastic neutrino-nucleon,” “many-body,” “perturbations,”, and “ray-by-ray+,” respectively.

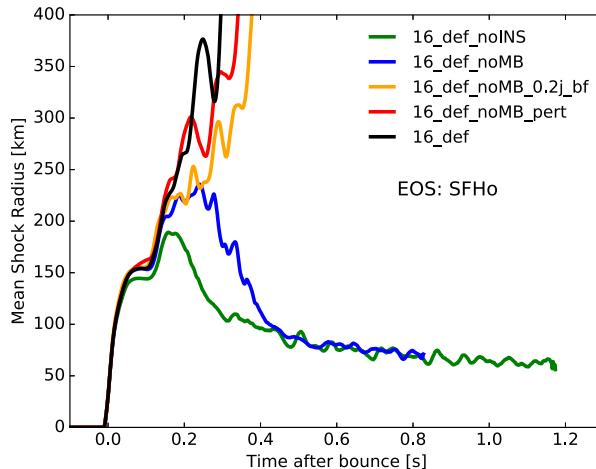
### 5.1 Inelastic Scattering

Models with only inelastic scattering off electrons (IES), inelastic scattering off both electrons and nucleons (IES\_INS), and additionally with the many-body effect (IES\_INS\_MB) can illuminate the respective roles of each.<sup>7</sup> Figure 1 compares outcomes for the 16- $M_\odot$  progenitor. We toggled the role of inelastic scattering off electrons and nucleons as well as the many-body effect for the 16  $M_\odot$  progenitor of Woosley and Heger (2007), which we found to explode early at  $\sim 300$  ms using the default setup IES\_INS\_MB. However, performing the simulation with any of these components removed prevents explosion.

Figure 2 depicts the role of IES, INS, and MB on the emergent spectra at two different times after bounce. One of the central results that can be gleaned is the time of explosion. This quantity can help one gauge the relative role of the inputs in question. The default model (def) here does explode. Prior to explosion, both inelastic scattering off electrons and off nucleons and the many-body correction led to higher spectral fluxes. After the default model explodes, the flux spectrum diminishes relative to that of the non-exploding model 16\_def\_noMB. The slight increase in the heating in the gain region prior to explosion due to the inclusion of inelastic neutrino-electron and neutrino-nucleon scattering has certainly helped the core achieve the critical explosion condition. Figure 3 compares the emergent

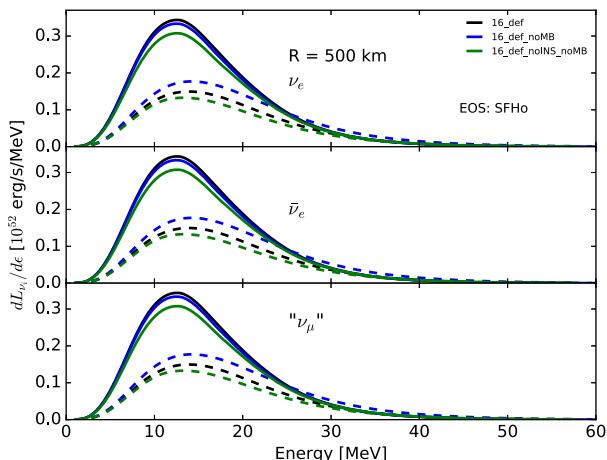
<sup>6</sup>The “time of explosion” is sometimes defined as the time the mean shock radius achieves 400 km. We think this definition somewhat arbitrary, but acknowledge some degree of arbitrariness in any definition, however useful. We here define the time of explosion as the approximate time at which the curve of the mean shock radius versus time is inflected upwards. All our models that inflect in this way explode and all these models have been continued to at least one second after bounce. The mean shock radii of these exploding models all achieve radii beyond 5000 kilometers by the end of the simulation.

<sup>7</sup>In a previous version of this paper, we had employed an opacity file that was compromised by a compiler bug. The net result of this error was a slightly enhanced magnitude of the neutral-current many-body effect. This error has now been fixed.

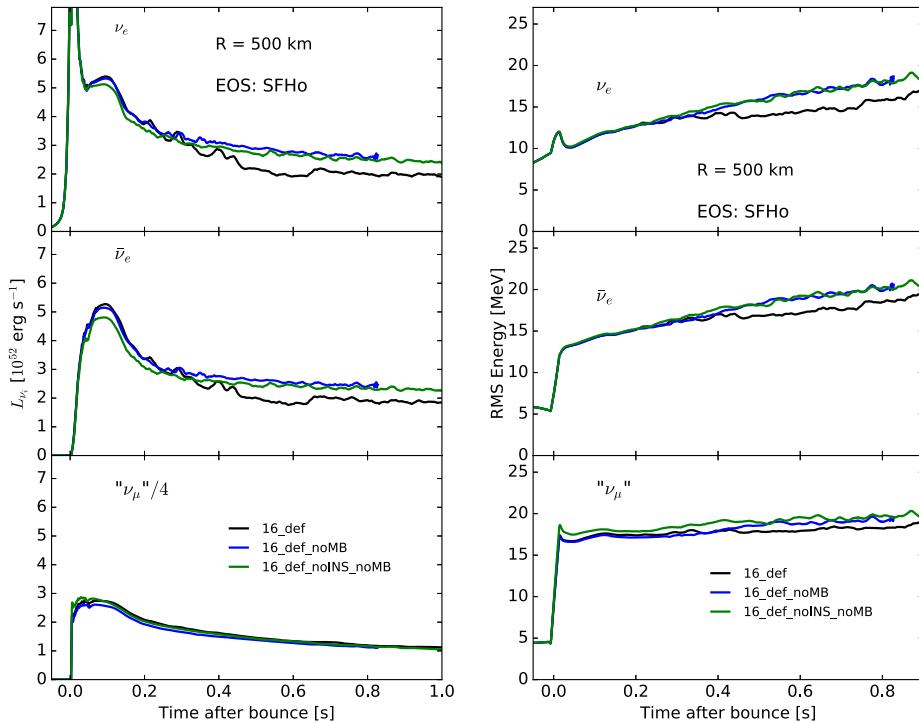


**Fig. 1** Shock radii (in km) versus time post-bounce (in s) for variations on the default  $16 M_{\odot}$  progenitor. In all figures, default model “def” refers to inclusion of inelastic scattering off both electrons (IES) and nucleons (INS), as well as the inclusion of the Horowitz et al. (2017) many-body correction (MB). This model explodes at  $\sim 250$  ms post-bounce. We then remove and add certain inputs, denoted by a subscript with “def”. Removing either the many-body correction (blue, “16\_def\_noMB”) or inelastic scattering off nucleons (green, “16\_def\_noINS”) leads to a dud. However, even without the many-body correction (noMB), adding either perturbations (red) (“\_pert”; Sect. 6) or modifying the opacity table to include Fischer’s (2016) correction to the nucleon-nucleon bremsstrahlung rate (“bf”) and only 20% of the electron capture rate (Juodagalvis et al. 2010) on heavy nuclei (orange, “0.2j”), leads to an explosion  $\sim 50$  and  $\sim 100$  ms, respectively, after our default model. This helps illustrate the sensitive dependence of the outcome—explosion or dud—on the microphysical inputs when near criticality

**Fig. 2** The role of inelastic scattering off electrons and nucleons and the neutral-current many-body correction on the emergent spectra (in  $10^{52}$  erg/s/MeV) at 500 km at 100 (solid) and 400 (dashed) ms post-bounce. At early times, prior to explosion, both inelastic scattering off electrons and nucleons and the many-body correction lead to upscattering. At 400 ms, the default model has exploded and hence has a diminished spectrum vis-à-vis the non-exploding model 16\_def\_noMB



neutrino luminosities (left panel) and root-mean-square (rms) neutrino energies (right) for three models. The boosting in the  $\nu_{\mu}$  luminosity and rms energy is clearly manifest, as are the corresponding boosts in those quantities for the  $\nu_e$  and  $\bar{\nu}_e$  neutrinos. While one may have speculated that enhanced neutrino losses, particularly due to  $\nu_{\mu}$  s that are almost ineffectual in heating the shocked mantle, would have had a negative effect on explodability, the converse is true. Greater losses lead to a further compaction of the core with an increase in the



**Fig. 3** Modification due to inelastic scattering off electrons and nucleons of the luminosities (*left*) and RMS energies (*right*) of neutrinos at 500 km, redshifted to the lab frame. Including inelastic scattering off nucleons decreases the  $\nu_\mu$  luminosities and RMS energies by  $\sim 10\%$ , as in Müller et al. (2012b), while slightly increasing the  $\nu_e$  and  $\bar{\nu}_e$  luminosities. RMS energies of the latter are mostly unaffected by inelastic scattering. The default model (*black*, with many-body corrections and both inelastic scatterings) shows a dip in luminosity and RMS energy after 300 ms post-bounce, the time of its explosion

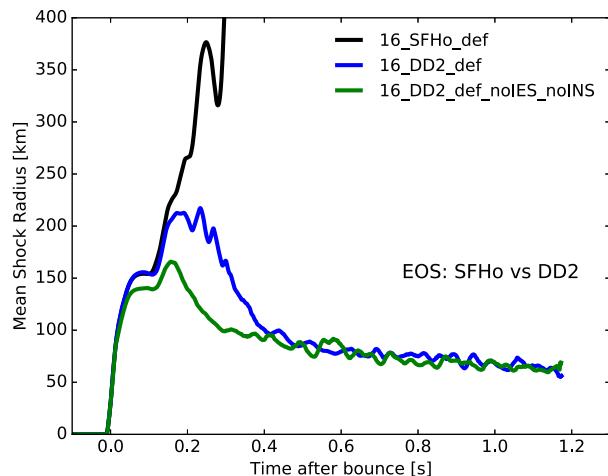
matter temperatures near the  $\nu_e$  and  $\bar{\nu}_e$  neutrinospheres. The result is similar in effect to that of GR, whereby such core heating enhances the driving  $\nu_e$  and  $\bar{\nu}_e$  luminosities and the average neutrino energies, which in turn enhance the heating power in the gain region. Since it is this power deposition that ultimately drives explosions, the net effect is quite supportive of explosion.

However, the actual magnitude and form of the correction to the axial-vector coupling term in the expression for the neutrino-nucleon scattering rate may be different from that derived by Horowitz et al. (2017) and this still needs to be verified. Moreover, the effects of similar many-body corrections to the absorption rates need to be incorporated, as do those for the vector coupling strengths. One prediction of the consequence of the structure-factor correction we have employed is the enhanced  $\nu_\mu$  luminosities and average energies seen in Fig. 3. It is noteworthy that, as it stands, the effect on the outcome of core-collapse of many-body rate suppressions (Burrows and Sawyer 1998, 1999) might be large.

## 5.2 Equation of State

Through its control of the pressure for a given temperature, density, and  $Y_e$ , the equation of state of hot, lepton-rich nuclear matter will determine the structure of the proto-neutron

**Fig. 4** Shock radii (km) versus time after bounce (s) for the SFHo and DD2 EOS for the  $16 M_{\odot}$  WH07 progenitor as a function of time after bounce. Only the former (our default model) explodes. We also plot for comparison a model with the DD2 EOS, but without any inelastic scattering off electrons or nucleons. Though neither DD2 model explodes, including inelastic scattering increases the stalled shock radius by  $\sim 70$  km



star and its evolution after bounce. The stiffer the EOS, the more extended the core. On the one hand, a stiff EOS will resist the quick increase in temperature near the  $\nu_e$  and  $\bar{\nu}_e$  neutrinospheres, and the consequent enhancement of the neutrino heating rate in the gain region, seen both in the comparison of GR and Newtonian models and in the increase in the  $\nu_{\mu}$  losses due to the many-body effect. On the other, a stiffer EOS will provide a more stable inner platform that won't as easily (by its inward motion with time after bounce) send out weakening rarefactions to the outer bounce shock that could inhibit explosion. Figure 4 indicates (at least for this  $16 M_{\odot}$  model) that the first effect seems to win, since the DD2 EOS model does not explode, while the SFHo model (the softer of the two at high densities) does. On this figure we also show that, though the DD2 model didn't explode, the behavior of the shock with time was significantly less vigorous when the inelastic scattering effects were turned off, reiterating the conclusions of Sect. 4 and Sect. 5.1. We also note that since the shock in the default DD2 model achieved a large mean shock radius ( $\sim 200$  km) before subsiding, this model was nevertheless very close to exploding.

### 5.3 Nucleon-Nucleon Bremsstrahlung and Electron-Capture on Heavies

On Fig. 1, we also provide a model that drops the many-body correction to neutrino-nucleon scattering, as derived by Horowitz et al. (2017), but substitutes in the Fischer (2016) correction to the nucleon-nucleon bremsstrahlung rate (“bf”) and divides the electron capture rate on heavy nuclei derived for the SFHo EOS by Jodagalvis et al. (2010) by five (“0.2j”). The former effect lowers the bremsstrahlung production rate of  $\nu_{\mu}$  neutrinos, as well as the inverse bremsstrahlung absorption. The latter effect slightly retards the infall rate, thereby decreasing the mass accretion rate post-bounce at a given time. Decreasing this rate can facilitate explosion. As the figure suggests, these microphysical changes can compensate for ignoring the many-body effect to result in a similarly-aided explosion. Clearly, such modest alterations in the microphysics of relevance, still within the envelope of our ignorance, could play a positive role. In Fig. 5 below, we see a similar positive effect of these potential changes in the default microphysics for a  $13 M_{\odot}$  model. Together with the model in Fig. 1, this suggests that a more extensive exploration of such physics would be fruitful.

## 6 Progenitor Perturbations

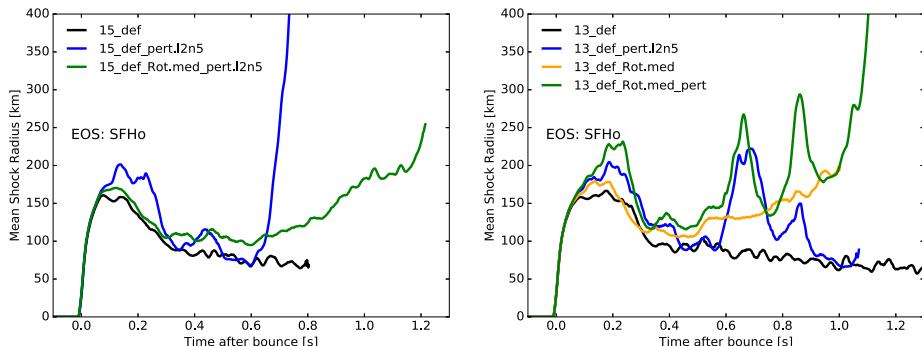
Performing the last stages of stellar evolution before collapse hydrodynamically in 2D and 3D has been shown to alter, perhaps in significant ways, the compositional, entropy, and density profiles of the core (Meakin et al. 2011; Couch et al. 2015; Chatzopoulos et al. 2016; Müller et al. 2016; Abdikamalov et al. 2016; Müller et al. 2017), and it has long been known that progenitor density profiles have an impact on the outcome of collapse. This is implicit in the critical curve analysis of Burrows and Gosh (1993), where  $\dot{M}$  and the accretion ram pressure play central roles. It is also a factor in discussions of the compactness parameter (O'Connor and Ott 2011) and its extensions (Ertl et al. 2015). In this vein, one notes that at least three groups (Kitaura et al. 2006; Burrows et al. 2007b; Radice et al. 2017) have already demonstrated that the  $8.8\text{-M}_\odot$  “electron-capture” supernova progenitor of Nomoto and Hashimoto (1988), with its extremely steep density ledge, can explode in 1D by the neutrino-driven wind mechanism, though the explosion energy is low ( $\sim 1\text{--}2 \times 10^{50}$  ergs).

However, when spherical progenitor models do not readily lead to explosion, the initial perturbation spectrum in the progenitor’s convective silicon and oxygen zones could certainly affect the timescales for the generation of turbulence behind the stalled shock and be a factor in the onset of explosion (Couch and Ott 2013; Müller and Janka 2015; Couch et al. 2015; Abdikamalov et al. 2016; Müller et al. 2017). Specifically, the magnitude, character, and spectra of seed perturbations will affect how quickly turbulence reaches the non-linear regime and, perhaps, whether turbulence grows to non-linearity at all during the finite time the accreta are in the unstable gain region.

Therefore, introducing physically-motivated seed perturbations that originate from and reflect the three-dimensional character of the convective core of an actual massive star at its terminal stage of evolution is a topic of some interest. However, most calculations done to date do not start with true 3D convective structures, but with 1D models from the literature, and impose either ad hoc perturbations in density or velocity randomly at the grid level or allow grid asphericities (such as obtained when using a Cartesian grid) or truncation errors to act as seeds. Neither of these approaches is physical, and the resulting initial perturbation spectra lead to early growth rates in the linear regime that reflect not the multi-D progenitor perturbation structure, but the numerical development of convenient artificial power spectra. This will affect how quickly turbulence reaches the non-linear regime and, perhaps, whether turbulence grows to non-linearity at all during the finite time the accreta are in the unstable gain region. In addition, this may have a bearing on the post-bounce delay to a turbulence-aided explosion, with the consequent effect on the time and energy of that explosion.

Therefore, the seed perturbations that arise during oxygen and silicon burning prior to collapse might be key inputs into core-collapse supernova theory, and Couch and Ott (2013), Müller and Janka (2015), Couch et al. (2015), Müller (2016), and Müller et al. (2017) have begun to explore this. However, mixing-length theory, though inadequate as a comprehensive theory, still provides a measure of the magnitude of velocity perturbations at the onset of collapse (Müller et al. 2016), and they are only a few hundred to  $\sim 500 \text{ km s}^{-1}$ , with Mach numbers bounded by  $\sim 0.08$  (Woosley and Heger 2007). This is not large.

In this section, we provide a quick glimpse at the possible relative role of significant perturbations on the timing and character of explosion in light of the other physics. To this end, we employ the methodology of Müller and Janka (2015). These authors impose a vector velocity perturbation map on their progenitor that is more realistic than many past approaches and renders a perturbation field that is independent of grid resolution. This (surprisingly) was rarely attempted in the past and provides a specific context for future comparison. We set the maximum perturbation speed on the grid to  $1000 \text{ km s}^{-1}$ , which as indicated earlier



**Fig. 5** Shock radius (in km) versus time after bounce (in s) for the 15 (left) and 13 (right)  $M_{\odot}$  Woosley and Heger (2007) models, showcasing the effect of significant perturbations and moderate rotation. We follow Müller and Janka (2015) prescription in implementing perturbations to radial velocities on infall over three regions with the maximal radial velocity ( $1000 \text{ km s}^{-1}$ ),  $n$  (number of radial convective cells), and  $l$  (number of angular convective cells) as parameters. The interior region spans 1000 to 2000 km, outside the nascent core, the middle region 2100 to 4000 km, and the outer region 4100 to 6000 km, truncated roughly where accretion ends after the first second for our simulations. All regions have  $l = 2$ ,  $n = 5$  and maximum radial velocity of  $1000 \text{ km s}^{-1}$ . See text for a discussion

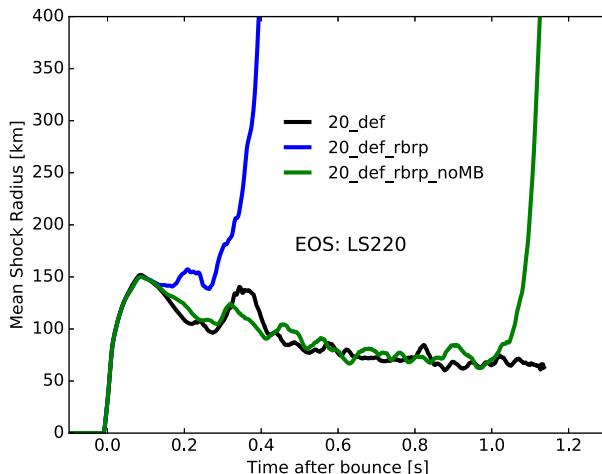
may be near or beyond the expected upper end of the range, a spherical harmonic index  $\ell$  of 2, and a radial “quantum number”  $n$  of 5. Both  $\ell$  and  $n$  are parameters in the Müller and Janka (2015) formulation. With this parameter set, we simulate in 2D the self-consistent multi-group evolution of 13- and 15- $M_{\odot}$  progenitors and compare the result to a default model for which the initial perturbations are much smaller and arose numerically from grid noise.

Figure 5 portrays the evolution of the mean shock radii, with and without progenitor perturbations. The left panel shows that the imposed perturbations converted failure into success for the 15- $M_{\odot}$ . We also provide on this panel a model including the effect of a modest rotation rate, along with the perturbation. Including the latter resulted in an explosion, though later. Our rotational study has revealed that the effect of rotation is not monotonic with initial internal rotational speed or spatial profile. On the right panel of Fig. 5, we show the corresponding behavior for the 13- $M_{\odot}$  progenitor, which does not explode in our study for the default microphysics. It does, however, explode when similar perturbations are imposed and when a similar rotational profile is assumed. In this case, rotation promotes explosion, highlighting its non-monotonic effect upon outcome.

We note that the initial perturbations we imposed have an amplitude that is somewhat larger than expected (Müller et al. 2016) and that their character is still rather artificial. The magnitude of the initial perturbations may well be lower, but their character and magnitude will certainly vary from progenitor to progenitor. Therefore, a much more thorough study with 3D progenitors and 3D collapse models is called for.

## 7 Ray-by-Ray+ Anomalies

As shown by Skinner et al. (2016), the ray-by-ray+ approach to neutrino transport, whereby multi-D transport is replaced by multiple 1D transport calculations with corrections for matter advection, but not lateral transport, can introduce systematic errors in the heating rates along the poles in axisymmetric 2D simulations. Such enhancements, when in proximity to



**Fig. 6** Shock radius (km) versus time after bounce (s) for the  $20 M_{\odot}$  WH07 progenitor using the LS220 EOS, with and without the ray-by-ray-plus (rbrp) approximation to neutrino transport. All models include inelastic scattering off electrons and nucleons. We see that including ray-by-ray+ (rbrp) leads to an explosion when otherwise there was none. The model with ray-by-ray+ and without many-body (green) explodes as well, though 700 ms after the model with ray-by-ray+ and many-body, suggesting that the ray-by-ray+, though artificial, is more significant to explosion than the physical inclusion of the many-body correction

criticality, may be producing explosions artificially. At the very least, the time to explosion is artificially shortened, perhaps significantly. Since there is little or no accumulation of explosion energy prior to global instability (Burrows et al. 1995),<sup>8</sup> an earlier explosion may make more of the emitted neutrinos available for explosive driving.

Figure 6 compares three  $20 M_{\odot}$  models, using this time the LS220 EOS. Here, the default model does not explode, but the one employing the ray-by-ray+ simplification does. Note that, for both ray-by-ray+ models, the model without the many-body (MB) correction explodes much later (by 700 ms) than the model with MB. Our results suggest, for this progenitor, that the artificial ray-by-ray+ approximation is more significant to explosion than the physical many-body effect. One is left to speculate whether 2D simulations in the literature that employ ray-by-ray+ would indeed explode if they used more realistic transport. This is all the more relevant in 3D, given that extant published models that do explode in 2D have more difficulty exploding in 3D, a context in which it is not clear that the ray-by-ray+ method introduces as great an artifact as in 2D. It is true that the turbulent pressure spectra in 2D and 3D are different, with the turbulent cascade in 2D resulting in enhanced stresses on larger scales, and that the turbulent-stress boost to explodability may be smaller in 3D. This could also be a factor in the more anemic outcomes in published 3D models. Nevertheless, it may be that the more problematic nature of published 3D models vis-à-vis 2D models is a consequence of some combination of the use of ray-by-ray+ and the reduced turbulent stress in 3D.

We conclude this section by noting that the calculations of Skinner et al. (2016) did not include various physical effects (such as inelasticities and the many-body correction) that we highlight here. In Skinner et al., we obtained explosions using ray-by-ray+ for some models that did not explode otherwise, and when they exploded they did so late.

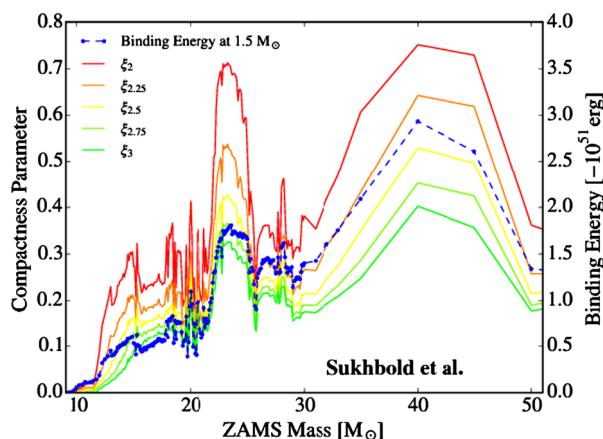
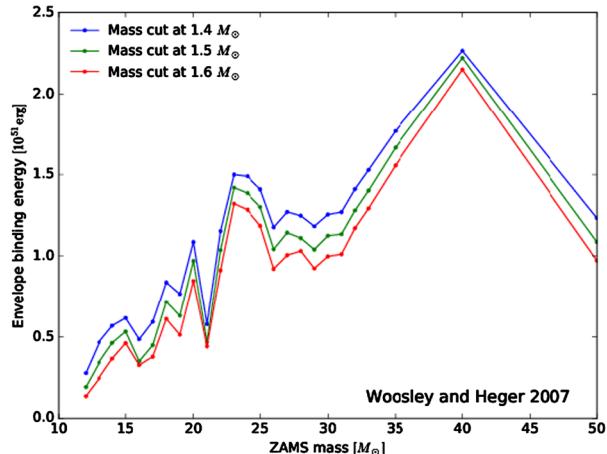
<sup>8</sup>Only those neutrinos emitted after the onset of the explosion contribute to the asymptotic explosion energy.

## 8 Compactness

Finally, we conclude that although the compactness parameter (O'Connor and Ott 2011, 2013; Pejcha and Thompson 2015), defined at bounce for a given mass interior ( $M$ ) at a given radius ( $R$ ) as  $\xi \equiv M/M_{\odot}(1000 \text{ km}/R)$ , is one measure of the important density structure of the progenitor, it is not necessarily predictive of explosion, at least during the first second after bounce. We find that, depending upon the neutrino physics employed, the temporal order in which models with different compactness parameters explode after bounce varies. If time of explosion is a fit measure of explodability, then this alone would challenge the usefulness of the compactness concept vis à vis explodability. Nevertheless, though the compactness parameter is large for the  $21\text{-}M_{\odot}$  model and small for the  $12\text{-}M_{\odot}$ , we found that the former can be more explodable. One might have thought that if compactness were the sole predictor the details of the neutrino-matter interaction would have mattered little in this regard. However, we see that the time to explosion does not necessarily correlate well with compactness. Models with dense envelopes have larger accretion and total neutrino luminosities after bounce, and it is these luminosities that drive explosion. In addition, models with dense envelopes and higher compactness have a greater optical depth to neutrinos in the gain region. Since the neutrino power deposition goes approximately as the product of this depth and the luminosities, high-compactness progenitors have an advantage. Therefore, it is feasible that more massive models might be more explosive, and this trend has been seen by other modelers (Summa et al. 2016, 2018; Bruenn et al. 2016). In fact, in the Summa et al. and Bruenn et al. papers for the Woosley and Heger (2007) models, the post-bounce explosion times increase in the sequence  $20, 25, 15$ , and  $12\text{-}M_{\odot}$ , which is clearly not monotonic with compactness. This behavior is the reverse of what might be expected if low compactness signaled greater explodability. Finally, the work of Nakamura et al. (2015) suggests that though they see a weak correlation, it is not monotonic with compactness. In fact, many of their plots versus compactness resemble scatter plots.

A critical issue is whether these more massive models with shallower density profiles that explode early can maintain explosion during the traversal of the shock through the outer stellar mantle. The binding energy penalty of the outer envelope generally increases with progenitor mass and might be too steep a price to pay during subsequent evolution for those more massive cores that explode earlier and, perhaps, more energetically. As previously stated, for most of the relevant mass function, the envelope binding energy exterior to a given interior mass is an increasing function of progenitor mass. It is this "barrier" that may set the limit to the range of massive stars that can explode and leave behind neutron stars, although it cannot be excluded that the progenitor mass range that yields neutron stars, and not black holes, may be discontinuous (Sukhbold et al. 2016). Figure 7 portrays various exterior binding energies and Fig. 8 follows with a depiction of the close correspondence between the compactness and the envelope binding energy exterior to a baryonic mass cut of  $1.5\text{-}M_{\odot}$ . Therefore, we contend that whatever significance there may be to the compactness parameter is likely due to its correspondence with the binding energy of the outer envelope exterior to a given mass cut and that compactness need not correlate with the apparent explodability during the first second after core bounce. Importantly, the ultimate outcome will depend upon the progress of the shock at post-bounce times that generally exceed those to which most core-collapse simulations currently go.

**Fig. 7** The outer envelope binding energies (in Bethes [ $\equiv 10^{51}$  erg]) for baryon mass cuts of 1.4, 1.5, and  $1.6 M_{\odot}$  versus ZAMS mass ( $M_{\odot}$ ) for the Woosley and Heger (2007) progenitor models



**Fig. 8** This plot depicts the dependence of the compactness parameter (O'Connor and Ott 2011, 2013), calculated at various interior masses, versus progenitor ZAMS mass, as well as the corresponding envelope binding energy (blue dots; in Bethes [ $10^{51}$  ergs]) for a baryon mass cut of  $1.5 M_{\odot}$  (see Fig. 7). The progenitor models of Sukhbold and Woosley (2014) (also in Sukhbold et al. 2016) are used. As this figure shows, whatever the position at which compactness is defined, it correlates extremely well with envelope binding energy. It is our contention that it is the latter quantity that is more germane to the outcome of core collapse

## 9 Conclusions

In this paper, we have generated and explored detailed 2D (axisymmetric) approximate GR models of core-collapse supernovae using the new code FORNAX, treating all the relevant physics to determine the dependence of the mechanism of explosion and its timing on the physical and numerical inputs and assumptions. These include inelastic neutrino-electron and neutrino-nucleon scattering, many-body/structure-factor corrections to the neutrino-nucleon scattering rates, nucleon-nucleon bremsstrahlung, electron capture on heavies, and physically-motivated initial perturbations. We have also reexamined in brief the effect of using the ray-by-ray+ simplification to neutrino transport. We found that much of the wide variation between the results obtained by different groups around the world simulating stel-

lar collapse (as well as whether the core explodes at all) might be explained by slight variations at the  $\sim 10\text{--}30\%$  level in the microphysical inputs when the models are near the critical condition for explosion. In the process, we gauged the relative importance of otherwise sub-dominant neutrino physics processes to the outcome of collapse. Proximity to criticality amplifies the dependence upon small changes in the neutrino sector that translate into slight, but crucial, changes in the emergent luminosities and average neutrino energies and the consequent post-shock heating rates; such sensitivity is not manifest in 1D simulations for which the core is (most often) far from explosive.

Thus, “Mazurek’s Law” of severe feedback under variations in neutrino cross sections and rates is overturned due to the proximity to instability possible in the realistic multi-D turbulent context. While alterations in the neutrino coupling rates have little effect in 1D, in multi-D the hydrodynamic response to even small changes and/or corrections to neutrino interaction rates can be more substantial due to greater proximity to the critical curve.

The upshot is that small variations between the methods, microphysics, and resolutions used by groups who ostensibly are incorporating the “same” inputs translates naturally into post-bounce explosion time differences that can range by many hundreds of milliseconds, and in some cases can turn a dud into an explosion (or vice versa). We suggest that this thereby explains in large measure the apparent heterogeneity in the outcomes of detailed simulations performed internationally. A natural conclusion is that, viewed correctly, the different groups are collectively closer to a realistic understanding of the neutrino-driven mechanism of supernova explosion than might have seemed apparent and that a push to rationalize approaches and understand microphysical details in the neutrino-matter interaction sector and the nuclear equation of state could bring a resolution to the decades-long quest for a predictive model of core-collapse supernova explosions.

We have found that many-body corrections to neutrino-matter interaction rates, even at sub-nuclear densities, can have similar effects as general relativity, progenitor perturbations, or inelastic neutrino-electron and neutrino-nucleon scattering. However, we caution that the actual magnitude and functional form of all the various many-body corrections to the neutrino-matter rates (both neutral- and charged-current), however important they seem from our current simulations, still need to be explored and verified.

We performed a test using the ray-by-ray+ approximation to neutrino transport in a manner similar to that employed by Skinner et al. (2016) to gauge its effect on the outcome of collapse when a full physics suite is employed. In Skinner et al. (2016), it was shown that ray-by-ray+ artificially enhanced heating along the poles in synchrony with the axial sloshing seen in 2D simulations and thereby made models more explosive. The shift in the explosion times can be as large as the full range currently witnessed by the various supernova simulation groups for a given progenitor. One can speculate that had groups that use the ray-by-ray+ simplification used real multi-D transport their 2D models would have exploded later, perhaps much later or not at all. Speculating further, one wonders whether the fact that 3D models explode later than the corresponding 2D models (Lentz et al. 2015) or not at all (Melson et al. 2015, if without their strangeness fix) may be connected with their use of ray-by-ray+, since non-rotating 3D simulations seldom manifest the axial sloshing seen in 2D. In short, without ray-by-ray+, it is not clear that 2D would explode much earlier than 3D. However, the differences between the 2D and 3D convective cascades may be equally in play here and the associated simulations still need to be performed to assess this.

The possible role of initial perturbations as seeds to the growth of convective instability in and around the gain region has been a subject of recent focus. Clearly, allowing grid noise, truncation error, or other numerical noise to initiate linear growth to the non-linear phase, or imposing artificial initial perturbations, is less than satisfactory. This is particularly true

given that seeds have a finite time to grow after accreting through the shock before leaving the unstable region and given that the time to instability and explosion is germane to which phase of the neutrino light curve is driving explosion. Inaugurating the non-linear convective phase early and maintaining it until explosion may be important, and the magnitude and timing of convective seeding is therefore of interest. Though we have deferred until later a more comprehensive study of this subject, we tested the effect of adding to the progenitor velocity perturbations whose magnitude was informed by mixing-length theory (Müller et al. 2016). In fact, we allowed the maximum perturbation speed to be  $1000 \text{ km s}^{-1}$ , with a Mach number as high as  $\sim 0.12$ , which is a bit larger than found in 1D progenitor models (cf. Woosley and Heger 2007). Indeed, we found that large imposed perturbations of this sort could enable explosion, though the magnitude of the imposed perturbation seems large. Clearly, it will be important to determine their character, and the many 3D-progenitor studies now in process promise to do just that.

Many-body corrections to scattering rates, inelastic scattering, decreases in nucleon-nucleon bremsstrahlung rates and in electron capture rates on heavy nuclei, and initial seed perturbations all boost “explodability” and shorten the time to explosion. In fact, these effects add synergistically and non-linearly to aide explosion, despite the fact that they individually amount to effects at the  $\sim 10\text{--}30\%$  level. This is due to the proximity of multi-D models to criticality, and is not seen in 1D simulations.

Furthermore, the turbulence behind the shock that has been shown to aid explosion in the realistic multi-D context naturally introduces indeterminacy in detail. Even the same progenitor star, but with different random seed perturbations and rotational structures at collapse, should yield a range of explosion energies, nucleosynthesis,  $^{56}\text{Ni}$  yields, pulsar kicks, and explosion morphologies. Therefore, it is expected that Nature provides distribution functions, and not one-to-one maps, in all signatures of explosion. In the long run, theory will need to come to grips with this, but in the short run one should not expect that in the chaotic context of turbulent convection and pre-collapse structures the best models will correspond in detail. This is the physical and natural consequence of turbulence and chaos, and will be paralleled in comparison verification studies.

The next stage is to explore the same issues in three dimensions, and one expects there to be important differences (Takiwaki et al. 2014; Lentz et al. 2015; Müller 2015; Müller et al. 2017). It is only after performing such simulations, and their subsequent verification, that a robust resolution to the core-collapse supernova problem can be claimed. Nevertheless, there has been significant progress of late in unraveling this central mystery in astrophysics, in demonstrating the viability of the neutrino-driven mechanism of explosion, and in illuminating its component physics.

**Acknowledgements** The authors acknowledge the help of Evan O’Connor with the Lattimer-Swesty equation of state and of Todd Thompson, who was instrumental in developing the inelastic scattering tables and schema. In addition, they thank Chuck Horowitz for early conversations concerning the neutrino response in nuclear matter at low densities, his insights into neutrino-matter interaction physics, and for an advanced look at his recent paper on these topics. Finally, they would like to thank Yukiya Saito and Junichiro Iwasawa for help scrutinizing the various progenitor model sets in the literature and Sean Couch for stimulating conversations on a variety of core-collapse topics. Support was provided by the Max-Planck/Princeton Center (MPPC) for Plasma Physics (NSF PHY-1144374) and NSF grant AST-1714267. The authors employed computational resources provided by the TIGRESS high performance computer center at Princeton University, which is jointly supported by the Princeton Institute for Computational Science and Engineering (PICSciE) and the Princeton University Office of Information Technology, and by the National Energy Research Scientific Computing Center (NERSC), which is supported by the Office of Science of the US Department of Energy (DOE) under contract DE-AC03-76SF00098. The authors express their gratitude to Ted Barnes of the DOE Office of Nuclear Physics for facilitating their use of NERSC. This work was originally part of the “Three Dimensional Modeling of Core-Collapse Supernovae” PRAC allocation support by the National Science Foundation

(award number ACI-1440032) and was part of the Blue Waters sustained-petascale computing project, which is supported by the National Science Foundation (awards OCI-0725070 and ACI-1238993) and the state of Illinois. Blue Waters is a joint effort of the University of Illinois at Urbana-Champaign and its National Center for Supercomputing Applications. This paper has been assigned a LANL preprint # LA-UR-16-28849.

**Open Access** This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (<http://creativecommons.org/licenses/by/4.0/>), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

## References

E. Abdikamalov, A. Zhaksylykov, D. Radice, S. Berdibek, *Mon. Not. R. Astron. Soc.* **461**, 3864 (2016)

Z. Ahmed et al., *Phys. Rev. Lett.* **108**, 102001 (2012)

S. Banik, M. Hempel, D. Bandyopadhyay, *Astrophys. J. Suppl. Ser.* **214**, 22–37 (2014). [arXiv:1404.6173](https://arxiv.org/abs/1404.6173)

H. Bethe, J.R. Wilson, *Astrophys. J.* **295**, 14 (1985)

T.D. Brandt, A. Burrows, C.D. Ott, E. Livne, *Astrophys. J.* **728**, 8 (2011)

S.W. Bruenn, *Astrophys. J. Suppl. Ser.* **58**, 771 (1985)

S.W. Bruenn, T. Dineva, *Astrophys. J. Lett.* **458**, L71 (1996)

S.W. Bruenn, A. Mezzacappa, W.R. Hix et al., *Astrophys. J. Lett.* **767**, L6 (2013)

S.W. Bruenn, E.J. Lentz, W.R. Hix et al., *Astrophys. J.* **818**, 123 (2016)

R. Buras, M. Rampp, H.-T. Janka, K. Kifonidis, *Phys. Rev. Lett.* **90**, 241101 (2003)

R. Buras, H.-T. Janka, M. Rampp, K. Kifonidis, *Astron. Astrophys.* **457**, 281 (2006)

A. Burrows, *Rev. Mod. Phys.* **85**, 245 (2013)

A. Burrows, J. Goshy, *Astrophys. J. Lett.* **416**, L75 (1993)

A. Burrows, J.M. Lattimer, *Astrophys. J.* **270**, 735 (1983)

A. Burrows, R.F. Sawyer, *Phys. Rev. C* **58**, 554 (1998)

A. Burrows, R.F. Sawyer, *Phys. Rev. C* **59**, 510 (1999)

A. Burrows, J. Hayes, B.A. Fryxell, *Astrophys. J.* **450**, 830 (1995)

A. Burrows, S. Reddy, T.A. Thompson, *Nucl. Phys. A* **777**, 356 (2006a)

A. Burrows, E. Livne, L. Dessart, C.D. Ott, J. Murphy, *Astrophys. J.* **640**, 878 (2006b)

A. Burrows, L. Dessart, E. Livne, C.D. Ott, J. Murphy, *Astrophys. J.* **655**, 416 (2007a)

A. Burrows, L. Dessart, E. Livne, The multi-dimensional character and mechanisms of core-collapse supernovae, in *The Proceedings of the Conference “SUPERNOVA 1987A: 20 YEARS AFTER; Supernovae and Gamma-Ray Bursters”*. AIP Proceedings Series, vol. 937 (2007b), pp. 370–380. Held in Aspen, CO, February 19–23

A. Burrows, L. Dessart, E. Livne, C.D. Ott, J. Murphy, *Astrophys. J.* **664**, 416 (2007c)

A. Burrows, J.C. Dolence, J. Murphy, *Astrophys. J.* **759**, 5 (2012)

E. Chatzopoulos, S.M. Couch, W.D. Arnett, F.X. Timmes, *Astrophys. J.* **822**, 61 (2016)

S.M. Couch, C.D. Ott, *Astrophys. J. Lett.* **778**, L7 (2013)

S.M. Couch, C.D. Ott, *Astrophys. J.* **799**, 5 (2015). [arXiv:1408.1399](https://arxiv.org/abs/1408.1399)

S.M. Couch, E. Chatzopoulos, W.D. Arnett, F.X. Timmes, *Astrophys. J. Lett.* **808**, L21 (2015). [arXiv:1503.02199](https://arxiv.org/abs/1503.02199)

L. Dessart, A. Burrows, E. Livne, C.D. Ott, *Astrophys. J.* **645**, 534 (2006)

J.C. Dolence, A. Burrows, J. Murphy, J. Nordhaus, *Astrophys. J.* **765**, 110 (2013)

J.C. Dolence, A. Burrows, W. Zhang, *Astrophys. J.* **800**, 10 (2015). [arXiv:1403.6115](https://arxiv.org/abs/1403.6115)

B. Dubroca, J.L. Feugeas, C. R. Acad. Sci. **329**, 915 (1999)

R.T. Emmering, R.A. Chevalier, *Astrophys. J.* **345**, 931 (1989)

T. Ertl, H.T. Janka, S.E. Woosley, T. Sukhbold, M. Ugliano, *Astrophys. J.* **818**, 124 (2015). [arXiv:1503.07522](https://arxiv.org/abs/1503.07522)

C.-A. Faucher-Giguere, V. Kaspi, *Astrophys. J.* **643**, 355 (2006)

T. Fischer, *Astron. Astrophys.* **593**, 103 (2016). [arXiv:1608.05004](https://arxiv.org/abs/1608.05004)

C.L. Fryer, A. Heger, *Astrophys. J.* **541**, 1033 (2000)

J. Green, N. Hasan, S. Meinel, M. Engelhardt, S. Krieg, J. Laeuchli, J. Negele, K. Orginos, A. Pochinsky, S. Syritsyn, *Phys. Rev. D* **95**, 114502 (2017). [arXiv:1703.06703](https://arxiv.org/abs/1703.06703)

F. Hanke, A. Marek, B. Müller, H.-T. Janka, *Astrophys. J.* **755**, 138 (2012)

F. Hanke, B. Müller, A. Wongwathanarat, A. Marek, H.-T. Janka, *Astrophys. J.* **770**, 66 (2013)

S. Hannestad, G. Raffelt, *Astrophys. J.* **507**, 339 (1998)

C.J. Horowitz, O.L. Caballero, Z. Lin, E. O’Connor, A. Schwenk, *Phys. Rev. C* **95**, 025801 (2017). [arXiv:1611.05140](https://arxiv.org/abs/1611.05140)

W. Iwakami, H. Nagakura, S. Yamada, *Astrophys. J.* **793**, 5 (2014). [arXiv:1404.2646](https://arxiv.org/abs/1404.2646)

H.-T. Janka, *Annu. Rev. Nucl. Part. Sci.* **62**, 407 (2012)

H.-T. Janka, W. Keil, G. Raffelt, D. Seckel, *Phys. Rev. Lett.* **76**, 2621 (1996)

H.-T. Janka, T. Melson, A. Summa, *Annu. Rev. Astron. Astrophys.* **66**, 341 (2016). [arXiv:1602.05576](https://arxiv.org/abs/1602.05576)

A. Juodagalvis, K. Langanke, W.R. Hix, G. Martínez-Pinedo, J. Sampaio, *Nucl. Phys.* **848**, 454 (2010)

F.S. Kitaura, H.-T. Janka, W. Hillebrandt, *Astron. Astrophys.* **450**, 345 (2006)

T. Kuroda, T. Takiwaki, K. Kotake, *Astrophys. J. Suppl. Ser.* **222**, 20 (2016)

J.M. Lattimer, F.D. Swesty, *Nucl. Phys. A* **535**, 331 (1991)

E.J. Lentz, S.W. Bruenn, W.R. Hix, A. Mezzacappa, O.E.B. Messer, E. Endeve, J.M. Blondin, J.A. Harris, P. Marronetti, K.N. Yakunin, *Astrophys. J. Lett.* **807**, 31 (2015). [arXiv:1505.05110](https://arxiv.org/abs/1505.05110)

M. Liebendörfer, S.C. Whitehouse, T. Fischer, *Astrophys. J.* **698**, 1174 (2009)

A. MacFadyen, S.E. Woosley, *Astrophys. J.* **524**, 262 (1999)

A. Marek, H.-T. Janka, *Astrophys. J.* **694**, 664 (2009)

A. Marek, H. Dimmelmeier, H.-T. Janka, E. Müller, R. Buras, *Astron. Astrophys.* **445**, 273 (2006)

C.A. Meakin, T. Sukhbold, W.D. Arnett, *Astrophys. Space Sci.* **336**, 123 (2011)

T. Melson, H.-T. Janka, R. Bollig et al., *Astrophys. J. Lett.* **808**, 42 (2015). [arXiv:1504.07631](https://arxiv.org/abs/1504.07631)

A. Mezzacappa, S.W. Bruenn, *Astrophys. J.* **405**, 637 (1993)

B. Müller, *Mon. Not. R. Astron. Soc.* **453**, 287 (2015). [arXiv:1506.05139](https://arxiv.org/abs/1506.05139)

B. Müller, *Publ. Astron. Soc. Aust.* **33**, 048 (2016). [arXiv:1608.03274](https://arxiv.org/abs/1608.03274)

B. Müller, H.-T. Janka, *Mon. Not. R. Astron. Soc.* **448**, 2141 (2015). [arXiv:1409.4783](https://arxiv.org/abs/1409.4783)

E. Müller, M. Steinmetz, *Comput. Phys. Commun.* **89**, 45 (1995)

B. Müller, H.-T. Janka, A. Heger, *Astrophys. J.* **761**, 72 (2012a)

B. Müller, H.-T. Janka, A. Marek, *Astrophys. J.* **756**, 84 (2012b)

B. Müller, M. Viallet, A. Heger, H.-T. Janka, *Astrophys. J.* **833**, 124 (2016). [arXiv:1605.01393](https://arxiv.org/abs/1605.01393)

B. Müller, T. Melson, A. Heger, H.-T. Janka, *Mon. Not. R. Astron. Soc.* **472**, 491 (2017). [arXiv:1705.00620](https://arxiv.org/abs/1705.00620)

J. Murphy, A. Burrows, *Astrophys. J.* **688**, 1159 (2008)

J. Murphy, J.C. Dolence, A. Burrows, *Astrophys. J.* **771**, 52 (2013)

K. Nakamura, T. Kuroda, T. Takiwaki, K. Kotake, *Astrophys. J.* **793**, 45 (2014). [arXiv:1403.7290](https://arxiv.org/abs/1403.7290)

K. Nakamura, T. Takiwaki, T. Kuroda, K. Kotake, *Publ. Astron. Soc. Jpn.* **67**, 107 (2015). [arXiv:1406.2415](https://arxiv.org/abs/1406.2415)

K. Nomoto, M. Hashimoto, *Phys. Rep.* **163**, 13 (1988)

A. Noutsos, D.H.F.M. Schnitzeler, E.F. Keane, M. Kramer, S. Johnston, *Mon. Not. R. Astron. Soc.* **430**, 2281 (2013)

E. O'Connor, C.D. Ott, *Astrophys. J.* **730**, 70 (2011)

E. O'Connor, C.D. Ott, *Astrophys. J.* **762**, 126 (2013)

C.D. Ott, A. Burrows, L. Dessart, E. Livne, *Astrophys. J.* **685**, 1069 (2008)

C.D. Ott, E. Abdikamalov, P. Mösta, R. Haas, S. Drasco, E. O'Connor, C. Reisswig, C.A. Meakin, E. Schnetter, *Astrophys. J.* **768**, 115 (2013). [arXiv:1210.6674](https://arxiv.org/abs/1210.6674)

K.-C. Pan, M. Liebendörfer, M. Hempel, F.-K. Thielemann, *Astrophys. J.* **817**, 72 (2016)

O. Pejcha, T.A. Thompson, *Astrophys. J.* **801**, 90 (2015)

S.B. Popov, R. Turolla, *Astrophys. Space Sci.* **341**, 457 (2012)

D. Radice, A. Burrows, D. Vartanyan, M.A. Skinner, J.C. Dolence, *Astrophys. J.* **850**, 43 (2017). [arXiv:1702.03927](https://arxiv.org/abs/1702.03927)

M. Rampp, H.-T. Janka, *Astron. Astrophys.* **396**, 361 (2002)

S. Reddy, M. Prakash, J.M. Lattimer, J.A. Pons, *Phys. Rev. C* **59**, 2888 (1999)

L.F. Roberts, S. Reddy, G. Shen, *Phys. Rev. C* **86**, 065803 (2012). [arXiv:1205.4066](https://arxiv.org/abs/1205.4066)

L.F. Roberts, C.D. Ott, R. Haas, E. O'Connor, P. Diener, E. Schnetter, *Astrophys. J.* **831**, 98 (2016)

M.A. Skinner, A. Burrows, J.C. Dolence, *Astrophys. J.* **831**, 81 (2016). [arXiv:1512.00113](https://arxiv.org/abs/1512.00113)

A.W. Steiner, M. Hempel, T. Fischer, *Astrophys. J.* **774**, 17 (2013)

T. Sukhbold, S.E. Woosley, *Astrophys. J.* **783**, 10 (2014)

T. Sukhbold, T. Ertl, S.E. Woosley, J.M. Brown, H.-T. Janka, *Astrophys. J.* **821**, 38 (2016)

K. Sumiyoshi, T. Takiwaki, H. Matsufuru, S. Yamada, *Astrophys. J. Suppl. Ser.* **216**, 37 (2015). [arXiv:1403.4476](https://arxiv.org/abs/1403.4476)

A. Summa, F. Hanke, H.-T. Janka, T. Melson, A. Marek, B. Müller, *Astrophys. J.* **825**, 6 (2016). [arXiv:1511.07871](https://arxiv.org/abs/1511.07871)

A. Summa, H.-T. Janka, T. Melson, A. Marek, *Astrophys. J.* **852**, 28 (2018). [arXiv:1708.04154](https://arxiv.org/abs/1708.04154)

Y. Suwa, K. Kotake, T. Takiwaki, S.C. Whitehouse, M. Liebendörfer, K. Sato, *Publ. Astron. Soc. Jpn.* **62**, L49 (2010)

Y. Suwa, S. Yamada, T. Takiwaki, K. Kotake, *Astrophys. J.* **816**, 16 (2016). [arXiv:1406.6414](https://arxiv.org/abs/1406.6414)

T. Takiwaki, K. Kotake, Y. Suwa, *Astrophys. J.* **749**, 98 (2012). [arXiv:1108.3989](https://arxiv.org/abs/1108.3989)

T. Takiwaki, K. Kotake, Y. Suwa, *Astrophys. J.* **786**, 83 (2014). [arXiv:1308.5755](https://arxiv.org/abs/1308.5755)

T. Takiwaki, K. Kotake, Y. Suwa, *Mon. Not. R. Astron. Soc.* **461**, L112 (2016). [arXiv:1602.06759](https://arxiv.org/abs/1602.06759)

I. Tamborra, F. Hanke, H.-T. Janka, B. Mueller, G. Raffelt, A. Marek, *Astrophys. J.* **792**, 96 (2014). [arXiv:1402.5418](https://arxiv.org/abs/1402.5418)

T.A. Thompson, A. Burrows, J.E. Horvath, *Phys. Rev. C* **62**, 035802 (2000)

T.A. Thompson, A. Burrows, P. Pinto, *Astrophys. J.* **592**, 434 (2003)

D.L. Tubbs, *Astrophys. J.* **231**, 846 (1979)

N.M.H. Vaytet, E. Audit, B. Dubroca, F. Delahaye, J. Quant. Spectrosc. Radiat. Transf. **112**, 1323 (2011)

D. Vartanyan, A. Burrows, D. Radice, M.A. Skinner, J. Dolence, *Astrophys. J.* (2018, submitted)

S.E. Woosley, A. Heger, *Phys. Rep.* **442**, 269 (2007)

S.E. Woosley, A. Heger, T.A. Weaver, *Rev. Mod. Phys.* **74**, 1015 (2002)

W. Zhang, L. Howell, A. Almgren, A. Burrows, J. Bell, *Astrophys. J. Suppl. Ser.* **196**, 20 (2011)

W. Zhang, L. Howell, A. Almgren, A. Burrows, J.C. Dolence, J. Bell, *Astrophys. J. Suppl. Ser.* **204**, 7 (2013)