

Power Allocation for Energy Efficiency and Secrecy of Wireless Interference Networks

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Abstract—Considering a multi-user interference network with an eavesdropper, this paper aims at the power allocation to optimize the worst secrecy throughput among the network links or the secure energy efficiency in terms of achieved secrecy throughput per Joule under link security requirements. Three scenarios for the access of channel state information are considered: the perfect channel state information; partial channel state information with channels from the transmitters to the eavesdropper exponentially distributed; and not perfectly known channels between the transmitters and the users with exponentially distributed errors. The paper develops various path-following procedures of low complexity and rapid convergence for the optimal power allocation. Their effectiveness and viability are illustrated through numerical examples. The power allocation schemes are shown to achieve both high secrecy throughput and energy efficiency.

Index Terms—Interference network, secure communication, energy-efficient communication, power allocation, path-following algorithms.

I. INTRODUCTION

THE broadcast nature of the wireless medium exhibits different challenges in ensuring secure communications in the presence of adversarial users [1], [2]. In particular, it is difficult to protect the transmitted signals from unintended recipients, who may improperly extract information from an ongoing transmission without being detected [3], [4]. Physical layer security [5], [6] has been proposed as a solution to provide security in wireless networks and researchers with a goal being to optimize the secure throughput of a wireless

network in the presence of eavesdroppers (EVs), which is the difference between the desired user throughput and eavesdroppers' throughput [2]. Beyond secure throughput, significant interest has recently been put on optimizing the secure energy efficiency (SEE), which is the ratio of the secure throughput to the total network power consumption, measured in terms of bits per Joule per Hertz [7], [8].

There has been considerable recent research on physical layer security in wireless communication systems. For example, assuming the availability of full channel state information (CSI), secrecy optimization has been studied for cooperative relaying networks in [9]–[11]. Energy efficiency (EE) of wireless networks has also drawn attention. For examples, resource allocation algorithms for the optimization of spectral efficiency as well as EE have been established in [12]. Keeping EE maximization as an objective, the authors in [13] proposed a precoder design for multi-input-multi-output (MIMO) two-way relay networks. EE maximization for cooperative spectrum sensing in cognitive sensor networks is studied in [14].

The critical topic of SEE has also been explored very recently [7], [8], [15]–[20]. Specifically, power control algorithms for SEE maximization in decode-and-forward (DF) and amplify-and-forward (AF) relaying networks have been considered in [15] and [7], respectively. In [16], the authors developed a distributed power control algorithm for SEE maximization in DF relaying. The same resource allocation problem for SEE maximization assuming full-duplex relaying is considered in [17]. Recently, the authors in [18] and [19] also derived the trade-off between SEE and secure spectral efficiency in cognitive radio networks, while the authors in [21] considered similar problems for ultra-dense small cells underlaid on macro cells. All these works have assumed the perfect CSI knowledge at the transmitter end, which is not always possible.

It is commonly known that time or frequency resources are generally limited in wireless networks and thus have to be shared among multiple users. This can result in interference among users in the network and thus one has to opt for careful resource allocation or interference alignment schemes [22]. Considering a multiuser MIMO interference network, [20] used the costly interference alignment technique to cancel both information leakage and interference and then Dinkelbach's method of fractional programming is adopted to optimize EE. As shown in [8], both zero-forcing and interference alignment are not efficient in optimizing the network SEE.

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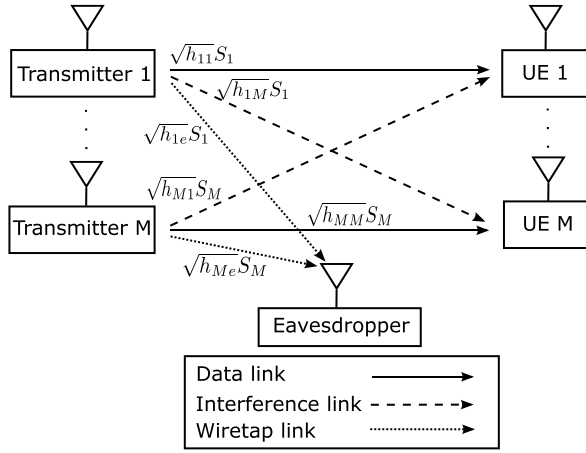


Fig. 1. System model.

In this paper, we propose novel and efficient resource allocation algorithms for both worst-case secure throughput and worst secure energy efficiency maximization of a highly interference-limited multi-user wireless network. Unlike many previous works, we do not assume perfect CSI knowledge at the transmitters. In fact, our transmitters only carry channel distribution knowledge for the eavesdropper and imperfect CSI for the users. Particularly, we consider three optimization scenarios to gradually build our algorithms. We start with the “perfect CSI” scenario. Next, we consider a “partial CSI” setup where the channel between the transmitters and the eavesdropper is exponentially distributed and only that channel distribution knowledge is available at the transmitters. Finally, we solve for the hardest “robust optimization” scenario, where in addition to the assumption of only channel distribution knowledge about eavesdroppers, we also assume uncertain channels between the transmitters and the users with exponentially distributed errors. We develop various path-following procedures of low complexity and rapid convergence for the optimal power allocation. Our extensive simulation results illustrate their effectiveness and viability.

The rest of the paper is organized as follows. Section II, Sections III and IV are devoted to optimizing the links’ worst secrecy throughput and the network secure energy efficiency under the perfect CSI, partial CSI and imperfectly known CSI, respectively. The simulation is provided in Section V to show the efficiency of the theoretical developments in the previous section. Appendices provide fundamental rate outage inequalities and approximations, which are the mathematical base of the theoretical sections II-IV.

II. INTERFERENCE NETWORKS UNDER PERFECT CSI

We consider a cooperative network consisting of M single-antenna transmitters and M single-antenna users as depicted in Figure 1, where each transmitter i intends to send the information s_i to user i . The information s_i is normalized, i.e. $\mathbb{E}(x_i^2) = 1$. Let $\mathbf{p}_i$ be the transmit power allocated to transmitter i and $\mathbf{p} = (\mathbf{p}_1, \dots, \mathbf{p}_M)^T$. Furthermore, denote by $\sqrt{h_{ji}}$ the path gain from transmitter j to user i . The received

signal at user i is

$$y_i = \sqrt{h_{ii}\mathbf{p}_i}s_i + \sum_{j \neq i}^M \sqrt{h_{ji}\mathbf{p}_j}s_j + n_i,$$

where $n_i \in \mathcal{CN}(0, \sigma_i^2)$ is additive noise.

Suppose that there is an eavesdropper, which is also equipped with a single antenna. Denoting by $\sqrt{h_{ie}}$ the path gain from transmitter i to the EV, the received signal at the EV is

$$y_e = \sum_{i=1}^M \sqrt{h_{ie}\mathbf{p}_i}s_i + n_e,$$

where $n_e \in \mathcal{CN}(0, \sigma_e^2)$ is additive noise.

Under the perfect CSI at the transmitters, the information throughput at user i is

$$f_i(\mathbf{p}) \triangleq \ln \left(1 + \frac{h_{ii}\mathbf{p}_i}{\sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2} \right). \quad (1)$$

With the EV considered as part of the legitimate network, the path gain $\sqrt{h_{ie}}$ can also be assumed known [23]. The wiretapped throughput for user i at the EV is

$$g_i(\mathbf{p}) \triangleq \ln \left(1 + \frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2} \right). \quad (2)$$

The secrecy throughput in transmitting information s_i to user i while keeping it confidential from the eavesdropper is defined as

$$\max\{f_i(\mathbf{p}) - g_i(\mathbf{p}), 0\}. \quad (3)$$

We consider the following fundamental optimization problems in a such network: the maximin secrecy throughput optimization

$$\max_{\mathbf{p}} \Phi_{\text{sp}}(\mathbf{p}) \triangleq \min_{i=1, \dots, M} [f_i(\mathbf{p}) - g_i(\mathbf{p})] \quad (4a)$$

$$\text{s.t. } 0 < \mathbf{p}_i \leq P_i, \quad i = 1, \dots, M, \quad (4b)$$

and the network SEE maximization under users’ secrecy throughput quality-of-service (QoS) requirements

$$\max_{\mathbf{p}} \Phi_{\text{ee}}(\mathbf{p}) \triangleq \frac{\sum_{i=1}^M [f_i(\mathbf{p}) - g_i(\mathbf{p})]}{\zeta \sum_{i=1}^M \mathbf{p}_i + P_c} \quad (5a)$$

$$\text{s.t. } (4b), \quad f_i(\mathbf{p}) - g_i(\mathbf{p}) \geq c_i, \quad i = 1, \dots, M, \quad (5b)$$

or the maximin transmitter EE optimization under users’ secrecy throughput QoS requirements

$$\max_{\mathbf{p}} \min_{i=1, \dots, M} \frac{f_i(\mathbf{p}) - g_i(\mathbf{p})}{\zeta \mathbf{p}_i + P_c^i} \quad \text{s.t. } (4b), (5b). \quad (6)$$

Here ζ is the reciprocal of the drain efficiency of the power amplifier, P_c^i is the circuit power at transmitter i and $P_c = \sum_{i=1}^M P_c^i$. As the numerator in the objective function in (5) is the sum secrecy throughput while the denominator is the network power consumption, the objective function in (5) expresses the network SEE in terms of nats/s/Joule. Similarly,

each subfunction in (6) expresses the SEE in for transmitting the information s_i . Moreover, the constraint (5b) for given thresholds c_i sets the QoS for the users in terms of the secrecy throughput. This constraint is nonconvex, which is in contrast to the throughput constraint

$$f_i(\mathbf{p}) \geq \tilde{c}_i, \quad i = 1, \dots, M,$$

which is equivalent to the linear constraint

$$h_{ii}\mathbf{p}_i \geq (e^{\tilde{c}_i} - 1) \left(\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2 \right), \quad i = 1, \dots, M.$$

A popular now approach [24] is to treat $f_i - g_i$ in (4) as a d.c. (difference of two concave functions) function [25]: $f_i(\mathbf{p}) - g_i(\mathbf{p}) = \tilde{f}_i(\mathbf{p}) - \tilde{g}_i(\mathbf{p})$ with $\tilde{f}_i(\mathbf{p}) = \ln(\sum_{j=1}^M h_{ji}\mathbf{p}_j + \sigma_i^2) + \ln(\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2)$ and $\tilde{g}_i(\mathbf{p}) = \ln(\sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2) + \ln(\sum_{j=1}^M h_{je}\mathbf{p}_j + \sigma_e^2)$ which are concave. Then at each iteration, $\tilde{f}_i$ is linearized while $\tilde{g}_i$ is innerly approximated by a concave quadratic function for a lower approximation of $\tilde{f}_i - \tilde{g}_i$ [26], [27]. As a result, each iteration invokes solution of a simple convex quadratic optimization problem with the logarithmic function optimization of high computational complexity avoided.

Our next subsections are devoted to efficient computational approach to solving each of (4), (5) and (6) without d.c. representation.

A. Max-Min Secrecy Throughput Optimization

At every $p^{(\kappa)} \in R_+^M \triangleq \{(x_1, \dots, x_M)^T : x_k > 0, k = 1, \dots, M\}$, applying inequality (72) in the Appendix II for $x = 1/h_{ii}\mathbf{p}_i$, $y = \sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2$ and $\bar{x} = 1/h_{ii}p_i^{(\kappa)}$, $\bar{y} = \sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2$ yields

$$f_i(\mathbf{p}) \geq f_i^{(\kappa)}(\mathbf{p}) \quad (7)$$

for

$$f_i^{(\kappa)}(\mathbf{p}) \triangleq \ln(1 + x_i^{(\kappa)}) + \frac{x_i^{(\kappa)}}{1 + x_i^{(\kappa)}} \times \left(2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2}{\sum_{j \neq i} h_{ji}p_j^{(\kappa)} + \sigma_i^2} \right). \quad (8)$$

On the other hand, applying inequality (75) in the Appendix II for $x = h_{ie}\mathbf{p}_i$, $y = \sum_{j \neq i}^M h_{je}\mathbf{p}_j$ and $\bar{x} = h_{ie}p_i^{(\kappa)}$, $\bar{y} = \sum_{j \neq i}^M h_{je}p_j^{(\kappa)}$ yields

$$g_i(\mathbf{p}) \leq g_i^{(\kappa)}(\mathbf{p}), \quad (9)$$

for

$$g_i^{(\kappa)}(\mathbf{p}) = \ln(1 + x_{e,i}^{(\kappa)}) + \frac{1}{1 + x_{e,i}^{(\kappa)}} \times \left(\frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2} - x_{e,i}^{(\kappa)} \right). \quad (10)$$

Initialized by a feasible $p^{(0)}$ for the convex constraint (4b), at the κ -th iteration we solve the convex optimization problem

$$\max_{\mathbf{p}} \Phi_{\text{sp}}^{(\kappa)}(\mathbf{p}) \triangleq \min_{i=1, \dots, M} [f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p})] \quad \text{s.t. (4b)} \quad (11)$$

to generate the next iterative point $p^{(\kappa+1)}$. As (11) involves M decision variables and M linear constraints, its computational complexity is $\mathcal{O}(M^2M^{2.5} + M^{3.5})$.

One can see that $\Phi_{\text{sp}}(\mathbf{p}) \geq F_{\text{sp}}^{(\kappa)}(\mathbf{p}) \quad \forall \mathbf{p} \in \mathbb{R}_+^M$ and $\Phi_{\text{sp}}(p^{(\kappa)}) = F_{\text{sp}}^{(\kappa)}(p^{(\kappa)})$. Furthermore, $\Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa+1)}) > \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa)})$ if $p^{(\kappa+1)} \neq p^{(\kappa)}$ because the former is the optimal solution of (11) while the latter is its feasible point. Therefore,

$$\Phi_{\text{sp}}(p^{(\kappa+1)}) \geq \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa+1)}) > \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa)}) = \Phi_{\text{sp}}(p^{(\kappa)}), \quad (12)$$

i.e. $p^{(\kappa+1)}$ is better than $p^{(\kappa)}$; as such $\{p^{(\kappa)}\}$ is a sequence of improved points that converges at least to a locally optimal solution of (4) satisfying the first order necessary optimality condition [28, Proposition 1]. In summary, we propose in Algorithm 1 a path-following computational procedure for the maximin secrecy throughput optimization problem (4).

Algorithm 1 Path-Following Algorithm for Maximin Secrecy Throughput Optimization

Initialization: Set $\kappa = 0$. Choose an initial feasible point $p^{(0)}$ for the convex constraints (4b). Calculate $R_{\min}^{(0)}$ as the value of the objective in (4) at $p^{(0)}$.

repeat

- Set $\kappa = \kappa + 1$.
- Solve the convex optimization problem (11) to obtain the solution $p^{(\kappa)}$.
- Calculate $R_{\min}^{(\kappa)}$ as the value of the objective in (4) at $p^{(\kappa)}$.

until $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$.

B. Secure Energy Efficient Maximization

Define

$$\pi(\mathbf{p}) = \zeta \sum_{i=1}^M \mathbf{p}_i + P_c.$$

Applying the inequality (73) in Appendix II for $x = 1/h_{ii}\mathbf{p}_i$, $y = \sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2$, $t = \pi(\mathbf{p})$, and $\bar{x} = 1/h_{ii}p_i^{(\kappa)}$, $\bar{y} = \sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2$, $\bar{t} = \pi(p^{(\kappa)})$ yields

$$\frac{f_i(\mathbf{p})}{\pi(\mathbf{p})} \geq F_i^{(\kappa)}(\mathbf{p}) \quad (13)$$

for

$$F_i^{(\kappa)}(\mathbf{p}) \triangleq \frac{2 \ln(1 + x_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + x_i^{(\kappa)})} \times \left(2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2}{\sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2} \right) - \frac{\ln(1 + x_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}). \quad (14)$$

On the other hand, applying inequality (75) in Appendix II for $\alpha = 1 + \ln(2)$, $x = h_{ie}\mathbf{p}_i / (\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2)$, $t = \pi(\mathbf{p})$ and

$\bar{x} \triangleq h_{ie}p_i^{(\kappa)} / (\sum_{j \neq i} h_{je}p_j^{(\kappa)} + \sigma_e^2)$, $\bar{t} = \pi(p^{(\kappa)})$ yields

$$\begin{aligned} \frac{-g_i(\mathbf{p})}{\pi(\mathbf{p})} \geq & 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \\ & - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} \\ & - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}, \end{aligned} \quad (15)$$

which together with (76) in Appendix II yield

$$\frac{f_i(\mathbf{p}) - g_i(\mathbf{p})}{\pi(\mathbf{p})} \geq G_i^{(\kappa)}(\mathbf{p}) \quad (16)$$

for the concave function

$$\begin{aligned} G_i^{(\kappa)}(\mathbf{p}) \triangleq & 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \\ & - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} \\ & - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}. \end{aligned} \quad (17)$$

Initialized by a feasible point $p^{(0)}$ for (5), we solve the following convex optimization problem at the κ -th iteration to generate the next iterative point $p^{(\kappa+1)}$:

$$\max_{\mathbf{p}} \Phi_{ee}^{(\kappa)}(\mathbf{p}) \triangleq \sum_{i=1}^M [F_i^{(\kappa)}(\mathbf{p}) + G_i^{(\kappa)}(\mathbf{p})] \quad (18a)$$

$$\text{s.t. (4b), } f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p}) \geq c_i, \quad i = 1, \dots, M. \quad (18b)$$

The computational complexity of (18) is $\mathcal{O}(M^2(2M)^{2.5} + (2M)^{3.5})$.

Due to (7) and (9), the nonconvex constraint (5b) in (5) is implied by the convex constraint (18b) in (18). Similarly to (12), we can show that $\Phi_{ee}(p^{(\kappa+1)}) > \Phi_{ee}(p^{(\kappa)})$ whenever $p^{(\kappa+1)} \neq p^{(\kappa)}$; as such the computational procedure that invokes the convex program (18) to generate the next iterative point, is path-following for (5), which at least converges to its locally optimal solution satisfying the Karush-Kuh-Tucker (KKT) conditions of optimality.

Recalling the definition (9) and (10) of functions $f_i^{(\kappa)}$ and $g_i^{(\kappa)}$, initialized by any feasible point $\tilde{p}^{(0)}$ for the convex constraint (4b), we generate $\tilde{p}^{(\kappa+1)}$, $\kappa = 0, \dots$, as the optimal solution of the convex optimization problem

$$\max_{\mathbf{p}} \min_{i=1, \dots, M} \frac{f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p})}{c_i} \quad \text{s.t. (4b)} \quad (19)$$

until $\tilde{p}^{(\kappa+1)}$ such that $\min_{i=1, \dots, M} (f_i(p^{(\kappa+1)}) - g_i(p^{(\kappa+1)}))/c_i \geq 1$ is found and thus $p^{(0)} = \tilde{p}^{(\kappa+1)}$ is feasible for (5) that is needed for the initial step.

Analogously, to address the maximin secure energy efficient optimization problem (6) define

$$\pi_i(\mathbf{p}_i) = \zeta \mathbf{p}_i + P_c^i.$$

Similarly to (13) and (16) the following inequalities can be obtained:

$$\frac{f_i(\mathbf{p})}{\pi_i(\mathbf{p}_i)} \geq \tilde{F}_i^{(\kappa)}(\mathbf{p}_i) \quad (20)$$

$$\frac{-g_i(\mathbf{p})}{\pi_i(\mathbf{p}_i)} \geq \tilde{G}_i^{(\kappa)}(\mathbf{p}_i) \quad (21)$$

for

$$\begin{aligned} \tilde{F}_i^{(\kappa)}(\mathbf{p}_i) \triangleq & \frac{2 \ln(1 + x_i^{(\kappa)})}{\pi_i(p_i^{(\kappa)})} + \frac{x_i^{(\kappa)}}{\pi_i(p_i^{(\kappa)})(1 + x_i^{(\kappa)})} \\ & \times \left(2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2}{\sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2} \right) \\ & - \frac{\ln(1 + x_i^{(\kappa)})}{\pi_i^2(p_i^{(\kappa)})} \pi_i(\mathbf{p}_i) \end{aligned} \quad (22)$$

$$\begin{aligned} \tilde{G}_i^{(\kappa)}(\mathbf{p}_i) \triangleq & 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi_i(p_i^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi_i(p_i^{(\kappa)})} \\ & - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi_i(p_i^{(\kappa)})} \frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} \\ & - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi_i^2(p_i^{(\kappa)})} \pi_i(\mathbf{p}_i) - \frac{\alpha}{\pi_i(\mathbf{p}_i)}. \end{aligned} \quad (23)$$

Initialized a feasible point $p^{(0)}$ for (6), which is found by using the generation (19), the following convex optimization problem at the κ -th iteration is proposed to generate the next iterative point $p^{(\kappa+1)}$:

$$\begin{aligned} \max_{\mathbf{p}} \min_{i=1, \dots, M} [\tilde{F}_i^{(\kappa)}(\mathbf{p}) + \tilde{G}_i^{(\kappa)}(\mathbf{p})] \\ \text{s.t. (4b), } f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p}) \geq c_i, \quad i = 1, \dots, M. \end{aligned} \quad (24)$$

The computational complexity of (24) is similar to that of (18).

The computational procedure that invokes the convex program (24) to generate the next iterative point, is path-following for (6), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

III. INTERFERENCE NETWORKS UNDER PARTIAL WIRETAP CSI

When the EV is not part of the legitimate network, it is almost impossible to estimate channels h_{ie} from the transmitters to it. It is common to assume that $h_{ie} = \bar{h}_{ie}\chi_{ie}$, where χ_{ie} is an exponential distribution with the unit mean and $\bar{h}_{ie}$ is a known deterministic quantity. Accordingly, instead of (2), the wiretapped throughput for user i at the EV is defined via the following throughput outage [29]–[33]:

$$\begin{aligned} g_{i,o}(\mathbf{p}) \triangleq & \max \{ \ln(1 + \mathbf{r}_i) : \\ & \text{Prob} \left(\frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} < \mathbf{r}_i \right) \leq \epsilon_{EV} \} \end{aligned} \quad (25)$$

for $\epsilon_{EV} > 0$. Using (63) in Appendix I, it follows that

$$g_{i,o}(\mathbf{p}) = \ln(1 + \mathbf{r}_i)$$

where

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 \mathbf{p}_i + \bar{h}_{ie} \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) = 0, \quad i = 1, \dots, M. \quad (26)$$

Therefore, the problem of maximin secrecy throughput optimization can be formulated as

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)] \quad (27a)$$

$$\text{s.t. (4b), (26), } \mathbf{r}_i > 0, \quad i = 1, \dots, M. \quad (27b)$$

The following result unravels the computationally intractable nonlinear equality constraints in (26).

Proposition 1: The problem (27) is equivalent to the following problem

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)] \quad (28a)$$

$$\text{s.t. (4b), (27b), } \mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \times \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) \geq 0, \quad i = 1, \dots, M. \quad (28b)$$

Proof: Since the equality constraint (26) implies the inequality constraint (28b), it is true that

the optimal value of (27) $\leq$ the optimal value of (28).

We now show that there is an optimal solution of (28) satisfies the equality constraint (26) and thus

the optimal value of (28) $\leq$ the optimal value of (27),

showing the equivalence between (28) and (27). Indeed, suppose that at the optimality,

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) > 0$$

for some $i = 1, \dots, M$. Then there is $0 < \gamma_i < 1$ such that

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + (\gamma \mathbf{r}_i) \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \times \sum_{j \neq i}^M \ln \left(1 + \frac{\gamma \mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) = 0,$$

that yields

$$f_i(\mathbf{p}) - \ln(1 + \gamma \mathbf{r}_i) > f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i),$$

so $\gamma \mathbf{r}_i$ is also the optimal solution of (28), which satisfies the equality constraint (26). $\square$

To address problem (28), note that a lower bounding function for the first term in (28a) is $f_i^{(\kappa)}(\mathbf{p})$ defined by (8), while an upper bounding function for the second term in (28a) is the following linear function

$$a_i^{(\kappa)}(\mathbf{r}_i) = \ln(1 + r_i^{(\kappa)}) - \frac{r_i^{(\kappa)}}{r_i^{(\kappa)} + 1} + \frac{\mathbf{r}_i}{r_i^{(\kappa)} + 1}. \quad (29)$$

The main difficulty now is to develop a lower bounding approximation for the function in the left hand side (LHS) of constraint (28b). Applying inequality (72) in Appendix II

for $x = 1/\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j$, $y = \bar{h}_{ie} \mathbf{p}_i$ and $\bar{x} = 1/r_i^{(\kappa)} \bar{h}_{je} p_j^{(\kappa)}$, $\bar{y} = \bar{h}_{ie} p_i^{(\kappa)}$ yields

$$\ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) \geq \lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \quad (30)$$

for

$$\lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \triangleq \ln(1 + x_{ij}^{(\kappa)}) + y_{ij}^{(\kappa)} \times \left(2 - \frac{r_i^{(\kappa)} p_j^{(\kappa)}}{\mathbf{r}_i \mathbf{p}_j} - \frac{\mathbf{p}_i}{p_i^{(\kappa)}} \right) \quad (31)$$

with $x_{ij}^{(\kappa)} \triangleq r_i^{(\kappa)} \bar{h}_{je} p_j^{(\kappa)} / \bar{h}_{ie} p_i^{(\kappa)}$ and $y_{ij}^{(\kappa)} \triangleq x_{ij}^{(\kappa)} / (x_{ij}^{(\kappa)} + 1)$. Therefore, over the trust region

$$\lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \geq 0, \quad 2.5 - \frac{\mathbf{r}_i}{r_i^{(\kappa)}} - \frac{\mathbf{p}_j}{p_j^{(\kappa)}} \geq 0 \quad (32)$$

it is true that

$$\begin{aligned} & \mathbf{p}_i \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) \\ & \geq \mathbf{p}_i \ln(1 + x_{ij}^{(\kappa)}) + y_{ij}^{(\kappa)} \left(2\mathbf{p}_i - \frac{r_i^{(\kappa)} p_j^{(\kappa)} \mathbf{p}_i}{\mathbf{r}_i \mathbf{p}_j} - \frac{\mathbf{p}_i^2}{p_i^{(\kappa)}} \right) \\ & = \left(\ln(1 + x_{ij}^{(\kappa)}) + 2y_{ij}^{(\kappa)} \right) \mathbf{p}_i \\ & \quad - 0.5y_{ij}^{(\kappa)} \left[2 \frac{\mathbf{p}_i^2}{p_i^{(\kappa)}} + \left(\frac{\sqrt{2}\mathbf{p}_i}{\sqrt{p_i^{(\kappa)}}} + \frac{\sqrt{p_i^{(\kappa)} r_i^{(\kappa)} p_j^{(\kappa)}}}{\sqrt{2}\mathbf{r}_i \mathbf{p}_j} \right)^2 - \frac{2\mathbf{p}_i^2}{p_i^{(\kappa)}} \right. \\ & \quad \left. - \frac{p_i^{(\kappa)} (r_i^{(\kappa)} p_j^{(\kappa)})^2}{2\mathbf{r}_i^2 \mathbf{p}_j^2} \right] \\ & \geq \Lambda_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \end{aligned} \quad (33)$$

for

$$\begin{aligned} \Lambda_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) &= \left(\ln(1 + x_{ij}^{(\kappa)}) + 2y_{ij}^{(\kappa)} \right) \mathbf{p}_i \\ & \quad - 0.5y_{ij}^{(\kappa)} \left(\frac{\sqrt{2}\mathbf{p}_i}{\sqrt{p_i^{(\kappa)}}} + \frac{\sqrt{p_i^{(\kappa)} r_i^{(\kappa)} p_j^{(\kappa)}}}{\sqrt{2}\mathbf{r}_i \mathbf{p}_j} \right)^2 \\ & \quad - 0.5y_{ij}^{(\kappa)} p_i^{(\kappa)} \left(\frac{\mathbf{r}_i}{r_i^{(\kappa)}} + \frac{\mathbf{p}_j}{p_j^{(\kappa)}} - 2.5 \right). \end{aligned}$$

Note that in obtaining (33) we also used the fact that function $\nu(\mathbf{r}_i, \mathbf{p}_j) \triangleq 1/\mathbf{r}_i^2 \mathbf{p}_j^2$ is convex in the domain $\{\mathbf{r}_i > 0, \mathbf{p}_j > 0\}$ and accordingly [25] $1/\mathbf{r}_i^2 \mathbf{p}_j^2 \geq \nu(r_i^{(\kappa)}, p_j^{(\kappa)}) + \langle \nabla \nu(r_i^{(\kappa)}, p_j^{(\kappa)}), (\mathbf{r}_i, \mathbf{p}_j) - (r_i^{(\kappa)}, p_j^{(\kappa)}) \rangle = [5 - 2(\mathbf{r}_i/r_i^{(\kappa)} + \mathbf{p}_j/p_j^{(\kappa)})]/(r_i^{(\kappa)} p_j^{(\kappa)})^2$.

Initialized from a feasible point $(p^{(0)}, r^{(0)})$ for (28) we solve the following convex program at the κ -th iteration to

generate $(p^{(\kappa+1)}, r_u^{(\kappa+1)})$:

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i^{(\kappa)}(\mathbf{p}) - a_i^{(\kappa)}(\mathbf{r}_i)] \quad (34a)$$

$$\text{s.t. (4b), (27b), (32), } \mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \sigma_e^2 \mathbf{r}_i + \bar{h}_{ie} \sum_{j \neq i}^M \Lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \geq 0, \quad i = 1, \dots, M. \quad (34b)$$

The computational complexity of (34) is $\mathcal{O}((2M)^2(5M)^{2.5} + (5M)^{2.5})$ because it involves $2M$ decision variables and $5M$ linear and quadratic constraints.

Then $r_i^{(\kappa+1)}$ is found from solving

$$0 = \psi_i(\mathbf{r}_i) \triangleq p_i^{(\kappa+1)} \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + p_i^{(\kappa+1)} \bar{h}_{ie} \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} p_j^{(\kappa+1)}}{\bar{h}_{ie} p_i^{(\kappa+1)}} \right), \quad i = 1, \dots, M, \quad (35)$$

by bisection on $[0, r_{u,i}^{(\kappa+1)}]$ such that

$$0 \leq \psi_i(r_i^{(\kappa+1)}) \leq \epsilon_b \quad (\text{tolerance}). \quad (36)$$

A bisection on $[r_l, r_u]$ for solving $\psi_i(\mathbf{r}_i) = 0$ where ψ_i increases in $\mathbf{r}_i > 0$ is implemented as follows:

- Define $r_i = (r_l + r_u)/2$. Reset $r_l = r_i$ if $\psi_i(r_i) < 0$. Otherwise reset $r_u = r_i$.
- Terminate until $0 \leq \psi_i(r_i) \leq \epsilon_b$.

In summary, we propose in Algorithm 2 a path-following computational procedure for the maximin secrecy throughput optimization problem (28), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

Algorithm 2 Path-Following Algorithm for Maximin Secrecy Throughput Optimization

Initialization: Set $\kappa = 0$. Choose an initial feasible point $(p^{(0)}, r^{(0)})$ for (28) and calculate $R_{\min}^{(0)}$ as the value of the objective function in (28) at $(p^{(0)}, r^{(0)})$.

repeat

- Set $\kappa = \kappa + 1$.
- Solve the convex optimization problem (34) to obtain the solution $(p^{(\kappa)}, r_u^{(\kappa)})$.
- Solve the nonlinear equations (35) to obtain the roots $r_i^{(\kappa)}$.
- Calculate $R_{\min}^{(\kappa)}$ as the value of the objective function in (28) at $(p^{(\kappa)}, r^{(\kappa)})$.

until $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$.

A feasible $(p^{(0)}, r^{(0)})$ is found as follows: taking $p^{(0)}$ feasible to the power constraint (4b) and finding $r^{(0)}$ from solving

$$0 = \psi_i(\mathbf{r}_i) \triangleq p_i^{(0)} \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \bar{h}_{ie} p_i^{(0)} \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} p_j^{(0)}}{\bar{h}_{ie} p_i^{(0)}} \right) \quad i = 1, \dots, M,$$

by bisection on $[0, r_{u,i}^{(0)}]$ with $\psi_i(r_{u,i}) > 0$. Such $r_{u,i}^{(0)}$ can be easily found: from any $r_{u,i} > 0$, if $\psi_i(r_{u,i}) \geq 0$ then we are done. Otherwise reset $r_{u,i} \leftarrow 2r_{u,i}$ and check $\psi_i(r_{u,i})$. Stop when $\psi_i(r_{u,i}) > 0$. Intuitively, taking $r_{u,i}^{(0)} = \bar{h}_{ie} p_i^{(0)} / \sigma_e^2$ will work.

Furthermore, the problem of SEE maximization can be formulated as

$$\max_{\mathbf{p}, \mathbf{r}} \frac{\sum_{i=1}^M (f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i))}{\pi(\mathbf{p})} \quad (37a)$$

$$\text{s.t. (4b), (27b), (28b)} \quad f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i) \geq c_i, \quad i = 1, \dots, M. \quad (37b)$$

Using the inequality (74) in Appendix II leads to

$$\frac{-\ln(1 + \mathbf{r}_i)}{\pi(\mathbf{p})} \geq \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p})$$

for

$$\begin{aligned} \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}) &\triangleq 2 \frac{\alpha - \ln(1 + r_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{r_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + r_i^{(\kappa)})} \\ &\quad - \frac{\mathbf{r}_i}{\pi(p^{(\kappa)})(1 + r_i^{(\kappa)})} \\ &\quad - \frac{\alpha - \ln(1 + r_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}. \end{aligned} \quad (38)$$

Initialized by a feasible $(p^{(0)}, r^{(0)})$, the following convex program is solved to generate $(p^{(\kappa+1)}, r^{(\kappa+1)})$ at the κ iteration:

$$\max_{\mathbf{p}, \mathbf{r}} \sum_{i=1}^M [F_i^{(\kappa)}(\mathbf{p}) + \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p})] \quad (39a)$$

$$\text{s.t. (4b), (27b), (32), (34b),} \quad (39b)$$

$$f_i^{(\kappa)}(\mathbf{p}) - a_i^{(\kappa)}(\mathbf{r}_i) \geq c_i, \quad i = 1, \dots, M. \quad (39c)$$

The computational complexity of (34) is $\mathcal{O}((2M)^2(6M)^{2.5} + (6M)^{2.5})$.

It can be shown that the computational procedure that invokes the convex program (39) to generate the next iterative point, is path-following for (37), which at least converges to its locally optimal solution satisfying the KKT conditions.

A point $(p^{(0)}, r^{(0)})$ is feasible for (37) if and only if $\min_{i=1, \dots, M} [f_i(p^{(0)}) - \ln(1 + r_i^{(0)})] / c_i \geq 1$ and thus can be easily located by adapting Algorithm 2.

Similarly, a path-following procedure for the following maximin SEE optimization problem can be proposed

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} \frac{f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)}{\pi_i(\mathbf{p})} \quad (40a)$$

$$\text{s.t. (4b), (27b), (28b), (37b).} \quad (40b)$$

IV. ROBUST OPTIMIZATION

Beside assuming that $h_{ie} = \bar{h}_{ie} \chi_{ie}$ with an exponential distribution χ_{ie} with the unit mean and deterministic $\bar{h}_{ie}$, we also assume that CSI of h_{ji} is not known perfectly in the form $h_{ji} = \bar{h}_{ji}(1 + \delta \chi_{ji})$ with deterministic $\bar{h}_{ji}$ and δ , and random χ_{ji} , which is an independent exponential distribution

of the unit mean. Instead of (1), the throughput at user i is defined via the following outage probability

$$f_{i,o}(\mathbf{p}) \triangleq \max\{\ln(1 + \mathbf{R}_i): \text{Prob}\left(\frac{h_{ii}\mathbf{p}_i}{\sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2} < \mathbf{R}_i\right) \leq \epsilon_c\} \quad (41)$$

for $0 < \epsilon_c \ll 1$.

Using (67) in Appendix II, it follows that

$$f_{i,o}(\mathbf{p}) = \ln(1 + \mathbf{R}_i), \quad i = 1, \dots, M, \quad (42)$$

where

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) = 0, \quad i = 1, \dots, M. \end{aligned} \quad (43)$$

Therefore, the problem of maximin secrecy throughput robust optimization is defined by

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \min_{i=1, \dots, M} [\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i)] \quad (44a)$$

$$\text{s.t. (4b), (27b), (28b), (43),} \quad (44b)$$

$$\mathbf{R}_i > 0, \quad i = 1, \dots, M. \quad (44c)$$

The following result unravels the computationally intractable nonlinear equality constraints in (43):

Proposition 2: Problem (44) is equivalent to the following problem

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \min_{i=1, \dots, M} [\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i)] \quad (45a)$$

$$\text{s.t. (4b), (28b), (27b), (44c)} \quad (45b)$$

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) \leq 0, \\ & i = 1, \dots, M. \end{aligned} \quad (45c)$$

Proof: Again, it is obvious that the optimal value of (44) is not more than the optimal value of (45). Furthermore, at an optimal solution of (45), if

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) < 0, \end{aligned}$$

for some i then there is $\gamma > 1$ such that

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + (\gamma \mathbf{R}_i) (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} (\gamma \mathbf{R}_i) \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) = 0, \end{aligned}$$

which results in $\ln(1 + \gamma \mathbf{R}_i) > \ln(1 + \mathbf{R}_i)$, implying that $\gamma \mathbf{R}_i$ is also an optimal solution of (45). We thus have proved

that there is always an optimal solution of (45) to satisfy the equality constraints in (43), so the optimal value of (45) is not more than the optimal value of (44), completing the proof of Proposition 2. $\square$

To address problem (45), firstly we provide a lower bounding approximation for the first term in the objective function in (45b) as follows

$$\begin{aligned} \ln(1 + \mathbf{R}_i) & \geq A_i^{(\kappa)}(\mathbf{R}_i) \\ & \triangleq \ln(1 + R_i^{(\kappa)}) + \frac{R_i^{(\kappa)}}{R_i^{(\kappa)} + 1} - \frac{(R_i^{(\kappa)})^2}{R_i^{(\kappa)} + 1} \frac{1}{\mathbf{R}_i}. \end{aligned}$$

Next, to obtain an upper bounding approximation for the function in the left hand side of (45c) and thus to provide an inner approximation for constraint (45c), we use the following inequality

$$\begin{aligned} \mathbf{R}_i \mathbf{p}_j & = 0.5(\mathbf{R}_i + \mathbf{p}_j)^2 - 0.5\mathbf{R}_i^2 - 0.5\mathbf{p}_j^2 \\ & \leq \Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) \\ & \triangleq 0.5(\mathbf{R}_i + \mathbf{p}_j)^2 - R_i^{(\kappa)}\mathbf{R}_i + 0.5(R_i^{(\kappa)})^2 \\ & \quad - p_j^{(\kappa)}\mathbf{p}_j + 0.5(p_j^{(\kappa)})^2, \end{aligned} \quad (46)$$

over the trust region

$$2\mathbf{R}_i \geq R_i^{(\kappa)}, 2\mathbf{p}_j \geq p_j^{(\kappa)}. \quad (47)$$

Then

$$\begin{aligned} & \mathbf{p}_i \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) \\ & \leq \mathbf{p}_i \left[\ln \left(1 + \frac{\bar{h}_{ji} R_i^{(\kappa)} p_j^{(\kappa)}}{\bar{h}_{ii} p_i^{(\kappa)}} \right) \right. \\ & \quad \left. + \frac{1}{\frac{\bar{h}_{ii}}{\bar{h}_{ji}} + \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}}} \left(\frac{\mathbf{R}_i \mathbf{p}_j}{\mathbf{p}_i} - \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}} \right) \right] \\ & \leq \Phi_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j, \mathbf{p}_i) \\ & \triangleq \mathbf{p}_i \ln \left(1 + \frac{\bar{h}_{ji} R_i^{(\kappa)} p_j^{(\kappa)}}{\bar{h}_{ii} p_i^{(\kappa)}} \right) \\ & \quad + \frac{1}{\frac{\bar{h}_{ii}}{\bar{h}_{ji}} + \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}}} \left(\Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) - \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}} \mathbf{p}_i \right). \end{aligned} \quad (48)$$

Initialized from a feasible $(p^{(0)}, R^{(0)}, r^{(0)})$ for (45) we solve the following convex program at the κ -th iteration to generate the next iterative point $(p^{(\kappa+1)}, R^{(\kappa+1)}, r^{(\kappa+1)})$:

$$\max_{\mathbf{w}, \mathbf{r}} \min_{i=1, \dots, M} [A_i^{(\kappa)}(\mathbf{R}_i) - a_i^{(\kappa)}(\mathbf{r}_i)] \quad (49a)$$

$$\text{s.t. (4b), (27b), (32), (34b), (44c), (47)} \quad (49b)$$

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \sigma_i^2 \mathbf{R}_i + \sum_{j \neq i} \bar{h}_{ji} \Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \sum_{j \neq i}^M \Phi_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j, \mathbf{p}_i) \leq 0, \quad i = 1, \dots, M. \end{aligned} \quad (49c)$$

The computational complexity of (49) is $\mathcal{O}((3M)^2(9M)^{2.5} + (9M)^{2.5})$.

At the same κ -th iteration, $r_i^{(\kappa+1)}$ is found from solving (35) by bisection on $[0, r_{u,i}^{(\kappa+1)}]$ such that (36), while $R_i^{(\kappa+1)}$ is found from solving

$$\zeta_i(\mathbf{R}_i) = 0, \quad i = 1, \dots, M, \quad (50)$$

for the increasing function

$$\begin{aligned} \zeta_i(\mathbf{R}_i) \triangleq & \delta \ln(1 - \epsilon_c) - 1 + \frac{\mathbf{R}_i(\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} p_j^{(\kappa+1)})}{\bar{h}_{ii} p_i^{(\kappa+1)}} \\ & + \delta \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i p_j^{(\kappa+1)}}{\bar{h}_{ii} p_i^{(\kappa+1)}} \right), \end{aligned}$$

by bisection on $[R_{l,i}^{(\kappa+1)}, R_{u,i}]$ with $\zeta_i(R_{u,i}) > 0$ such that

$$-\epsilon_b \leq g_i(R_i^{(\kappa+1)}) \leq 0. \quad (51)$$

$R_{u,i}$ can be easily located: initialized by $R_i = 2R_{l,i}^{(\kappa+1)}$ and check $\zeta_i(R_i)$. If $\zeta_i(R_i) > 0$ then we are done. Otherwise reset $R_i \leftarrow 2R_i$ until $\zeta_i(R_i) > 0$. Intuitively, taking $R_{u,i} = 2\bar{h}_{ii} p_i^{(\kappa+1)} / (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} p_j^{(\kappa+1)})$ will work.

In summary, we propose in Algorithm 3 a path-following computational procedure for the maximin secrecy throughput optimization problem (45), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

Algorithm 3 Path-Following Algorithm for Maximin Secrecy Throughput Optimization

Initialization: Set $\kappa = 0$. Choose an initial feasible point $(p^{(0)}, R^{(0)}, r^{(0)})$ for (45) and calculate $R_{\min}^{(0)}$ as the value of the objective function in (45) at $(p^{(0)}, R^{(0)}, r^{(0)})$.

repeat

- Set $\kappa = \kappa + 1$.
- Solve the convex optimization problem (49) to obtain the solution $(p^{(\kappa)}, R_i^{(\kappa)}, r_u^{(\kappa)})$.
- Solve the nonlinear equations (35) to obtain the roots $r_i^{(\kappa)}$.
- Solve the nonlinear equations (50) to obtain the roots $R_i^{(\kappa)}$.
- Calculate $R_{\min}^{(\kappa)}$ as the value of the objective function in (45) at $(p^{(\kappa)}, R^{(\kappa)}, r^{(\kappa)})$.

until $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$.

An initial feasible $(p^{(0)}, R^{(0)}, r^{(0)})$ can be easily found as follows: taking any $p^{(0)}$ feasible to the power constraint (4b) to find $R^{(0)}$ and $r^{(0)}$ from solving

$$\begin{aligned} \zeta_i(\mathbf{R}_i) \triangleq & \delta \ln(1 - \epsilon_c) - 1 + \frac{\mathbf{R}_i(\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} p_j^{(0)})}{\bar{h}_{ii} p_i^{(0)}} \\ & + \delta \sum_{j \neq i}^M \ln \left(1 + \frac{\bar{h}_{ji} \mathbf{R}_i p_j^{(0)}}{\bar{h}_{ii} p_i^{(0)}} \right) = 0, \quad i = 1, \dots, M, \end{aligned}$$

by bisection on $[0, 2\bar{h}_{ii} p_i^{(0)} / (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} p_j^{(0)})]$, and $r^{(0)}$ is found from solving

$$\ln(1 - \epsilon_c) + \frac{\mathbf{r}_i \sigma_e^2}{\bar{h}_{ie} p_i^{(0)}} + \sum_{j \neq i}^M \ln \left(1 + \frac{\mathbf{r}_i \bar{h}_{je} p_j^{(0)}}{\bar{h}_{ie} p_i^{(0)}} \right) = 0, \quad i = 1, \dots, M,$$

by bisection on $[0, \bar{h}_{ie} p_i^{(0)} / \sigma_e^2]$.

Lastly, the network secure energy efficiency problem is now formulated by

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \frac{\sum_{i=1}^M (\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i))}{\pi(\mathbf{p})} \quad (52a)$$

$$\text{s.t. (4b), (27b), (28b), (43), (44c),} \quad (52b)$$

$$\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i) \geq c_i, \quad i = 1, \dots, M. \quad (52c)$$

To this end, we use inequality (73) in Appendix II to obtain

$$\begin{aligned} \frac{\ln(1 + \mathbf{R}_i)}{\pi(\mathbf{p})} & \geq \tilde{A}_i^{(\kappa)}(\mathbf{R}_i, \mathbf{p}) \\ & \triangleq \frac{2 \ln(1 + R_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{R_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + R_i^{(\kappa)})} \\ & \quad \times \left(1 - \frac{R_i^{(\kappa)}}{\mathbf{R}_i} \right) - \frac{\ln(1 + R_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}). \end{aligned} \quad (53)$$

Initialized by a feasible point $(R^{(0)}, r^{(0)}, p^{(0)})$, at the κ -th iteration, the following convex program is solved to generate $(R^{(\kappa+1)}, r^{(\kappa+1)}, p^{(\kappa+1)})$

$$\max_{\mathbf{w}, \mathbf{r}} \sum_{i=1}^M \left[\tilde{A}_i^{(\kappa)}(\mathbf{R}_i, \mathbf{p}) + \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}) \right] \quad (54a)$$

$$\text{s.t. (4b), (27b), (32), (34b), (44c), (47), (49c),} \quad (54b)$$

$$A_i^{(\kappa)}(\mathbf{R}_i) - a_i^{(\kappa)}(\mathbf{r}_i) \geq c_i, \quad i = 1, \dots, M. \quad (54c)$$

The computational complexity of (49) is $\mathcal{O}((3M)^2(10M)^{2.5} + (10M)^{2.5})$.

It can be shown that the computational procedure that invokes the convex program (54) to generate the next iterative point, is path-following for (52), which at least converges to its locally optimal solution satisfying the KKT conditions.

A point $(p^{(0)}, R^{(0)}, r^{(0)})$ is feasible for (52) if and only if $\min_{i=1, \dots, M} [f_i(R_i^{(0)}) - \ln(1 + r_i^{(0)})] / c_i \geq 1$ and thus can be easily located by adapting Algorithm 3.

Similarly, a path-following procedure for the following maximin SEE optimization problem can be proposed

$$\begin{aligned} \max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} \frac{f_i(\mathbf{R}_i) - \ln(1 + \mathbf{r}_i)}{\pi_i(\mathbf{p})} \\ \text{s.t. (4b), (27b), (28b), (43), (44c), (52c).} \end{aligned} \quad (55)$$

V. SIMULATION

This section evaluates the performance of the proposed algorithms through extensive simulation. Considered in all simulation studies is a wireless network with $M = 10$ transmitter-user communication pairs and noise variance $\sigma_e^2 = \sigma_e^2 = 1$ mW [34]. All channels among each pair are i.i.d. complex normal random variable with zero mean and unit

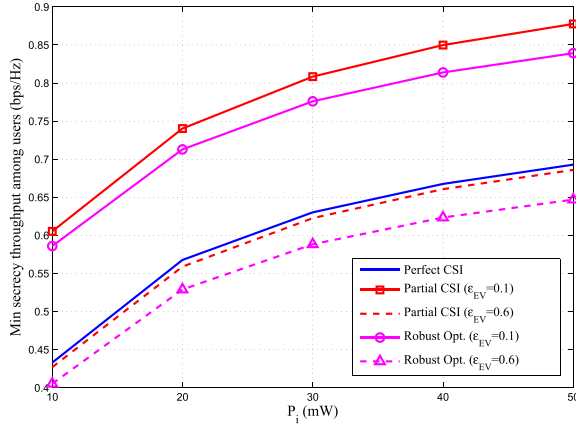


Fig. 2. Min secrecy throughput among users versus the transmit power budget.

variance. The drain efficiency of power amplifier $1/\zeta$ is set to be 40% and the circuit power of each transmitter is $P_c^i = 5$ mW. Besides, we set $\epsilon_c = 0.1$ and $\epsilon_{EV} \in \{0.1, 0.6\}$ and $\delta = 0.1$. The computation tolerance for terminating all proposed Algorithms is $\epsilon_{tol} = 10^{-4}$. We divide the obtained information throughput results by $\ln(2)$ to arrive at the unit of bps/Hz (in throughput) and bits/J/Hz (in energy efficiency).

A. Maximin Secrecy Throughput Optimization

This subsection analyzes the secrecy throughput in the presence of eavesdropper. In what follows, we consider five cases, including “Perfect CSI”, “Partial CSI ($\epsilon_{EV} = 0.1$)”, “Partial CSI ($\epsilon_{EV} = 0.6$)”, “Robust Opt. ($\epsilon_{EV} = 0.1$ $\epsilon_c = 0.1$)” and “Robust Opt. ($\epsilon_{EV} = 0.6$ $\epsilon_c = 0.1$)”. The terms “Perfect CSI”, “Partial CSI” and “Robust Opt.” correspond to the scenarios discussed in Sections III, IV and V, respectively. Fig. 2 plots the minimum secrecy throughput versus the transmit power budget P_i varying from 10 to 50 mW. As expected, it is seen that the secrecy throughput increase with the transmitted power budget P_i . It is also observed that the secrecy throughput of “Partial CSI” with $\epsilon_{EV} = 0.1$ is always better than the secrecy throughputs of others. For $\epsilon_{EV} = 0.1$, “Partial CSI” and “Robust Opt.” clearly and significantly outperform “Perfect CSI”. However, the secrecy throughput of “Perfect CSI” is superior to the secrecy throughputs of “Partial CSI” and “Robust Opt.” with $\epsilon_{EV} = 0.6$. This is not a surprise because according to the wiretapped throughput defined by (2) and the throughput outage defined by (25)-(26), the former is seen higher than the later for small ϵ_{EV} .

Table I provides the average number of iterations required to solve maximin secrecy throughput optimization for the above three cases. As can be observed, our proposed algorithm converges in less than 14 iterations, on average, for all considered cases.

B. Energy Efficiency Maximization

In this subsection, we first examine the performance of EE maximization algorithm versus the QoS constraint. The transmitted power P_i is fixed at 20 mW and QoS constraint c_i varies from 0.1 to 0.5 bps/Hz. It can be observed from Fig. 3 that the

TABLE I
AVERAGE NUMBER OF ITERATIONS FOR MAXIMIN SECURE THROUGHPUT OPTIMIZATION

P_i (mW)	10	20	30	40	50
Perfect CSI	8.12	7.63	7.61	7.71	8.56
Partial CSI ($\epsilon_{EV} = 0.1$)	11.25	10.87	10.73	10.40	10.31
Partial CSI ($\epsilon_{EV} = 0.6$)	13.12	12.18	14.92	12.60	11.68
Robust Opt. ($\epsilon_{EV} = 0.1$)	4.20	4.33	4.20	3.52	3.35
Robust Opt. ($\epsilon_{EV} = 0.6$)	5.18	4.96	4.82	4.14	4.90

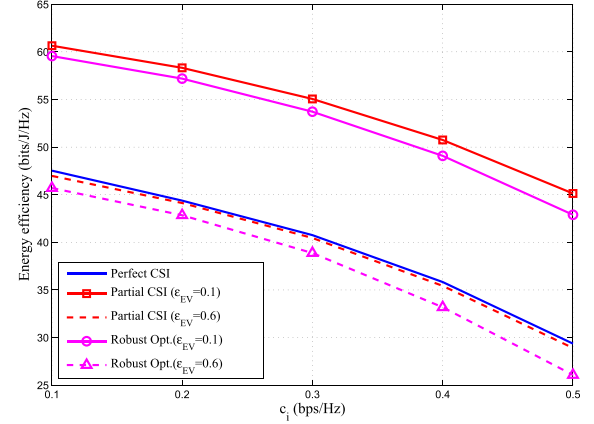


Fig. 3. Energy efficiency versus QoS constraint.

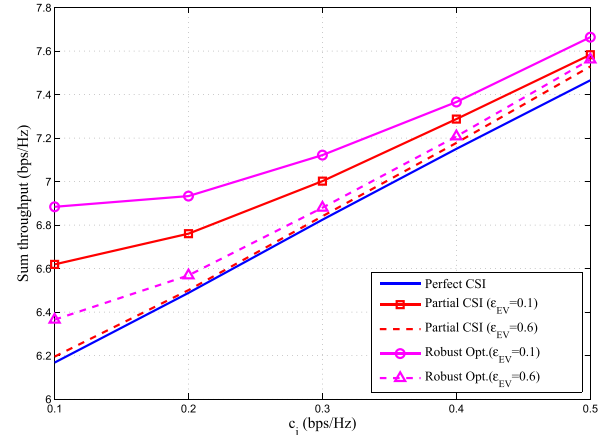


Fig. 4. Sum throughput versus QoS constraint.

EE performance degrades as the QoS constraint c_i increases. Moreover, “Partial CSI” with $\epsilon_{EV} = 0.1$ outperforms others in terms of EE performance. To find out the impact on the sum throughput and total power consumption in EE maximization algorithm, the achieved sum throughput and the total power consumed are illustrated in Fig. 4 and 5, respectively. It can be seen that the total power consumption increases faster than the sum throughput, which explains why EE degrades as c_i increases in Fig. 3. Although the sum throughput of “Robust Opt.” is slightly better than “Partial CSI”, “Partial CSI” consumes less power than “Robust Opt.”. Table II shows that our proposed EE maximization algorithm converges in less than 35 iterations, on average, in all considered cases.

Next, we further investigate the performance of EE versus the transmit power budget. The QoS constraint c_i is fixed at

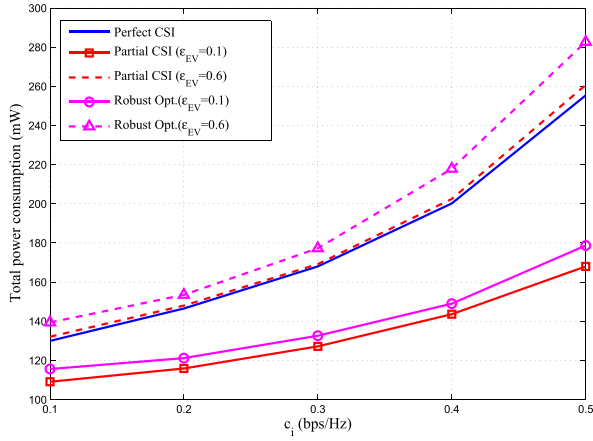


Fig. 5. Total power consumption versus QoS constraint.

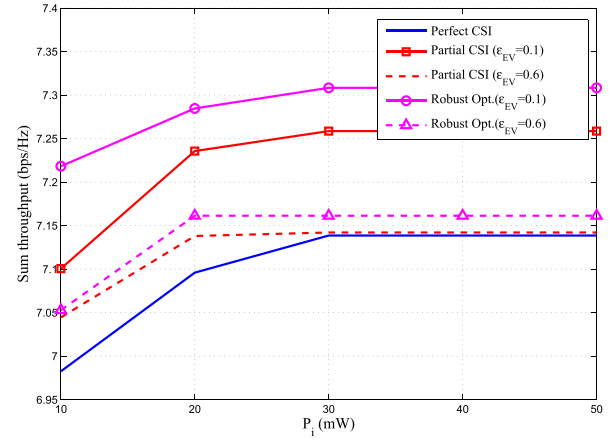


Fig. 7. Sum throughput versus the transmit power budget.

TABLE II
AVERAGE NUMBER OF ITERATIONS FOR ENERGY
EFFICIENCY MAXIMIZATION

c_i (bps/Hz)	0.1	0.2	0.3	0.4	0.5
Perfect CSI	32.21	29.62	24.26	21.23	15.33
Partial CSI ($\epsilon_{EV} = 0.1$)	33.73	33.12	28.75	25.74	23.25
Partial CSI ($\epsilon_{EV} = 0.6$)	35.82	30.56	34.22	22.26	18.34
Robust Opt. ($\epsilon_{EV} = 0.1$)	24.25	27.41	25.53	30.06	31.75
Robust Opt. ($\epsilon_{EV} = 0.6$)	29.02	23.76	26.80	29.32	23.46

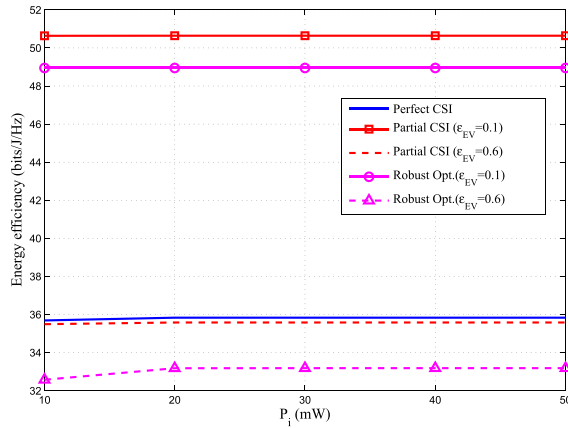


Fig. 6. Energy efficiency versus the transmit power budget.

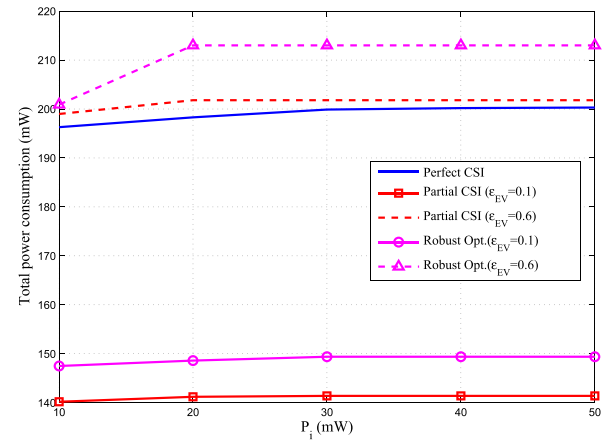


Fig. 8. Total power consumption versus the transmit power budget.

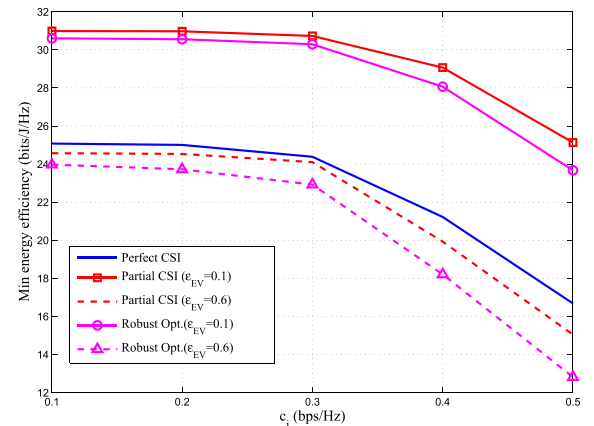


Fig. 9. Minimum energy efficiency versus the QoS constraint.

0.4 bps/Hz and P_i varies from 10 to 50 mW. As shown in Fig. 6, we observe that the EE performance of “Partial CSI” with $\epsilon_{EV} = 0.1$ clearly and significantly outperforms the optimized EE of other cases. Furthermore, it can be seen that the EE performances saturate when the transmit power budget exceeds the threshold. That is because for small transmit power budget, the denominator of EE is dominated by the circuit power and the EE is maximized by maximization of the sum throughput in the numerator. However, for larger transmit power budget, the denominator of EE is dominated by the actual transmit power. When the total power consumption saturates in Fig. 8, both the EE and the sum throughput accordingly saturate in Figs. 6 and 7.

C. Maxmin Energy Efficiency Optimization

In this subsection, we aim to maximize the minimum EE performance. Firstly, Fig. 9 plots the maximized minimum EE versus QoS constraint. The transmitted power P_i is fixed at 20 mW and QoS constraint c_i varies from 0.1 to 0.5 bps/Hz. It can be seen that the optimized minimum EE decreases with increasing c_i and the EE performance of “Partial CSI”

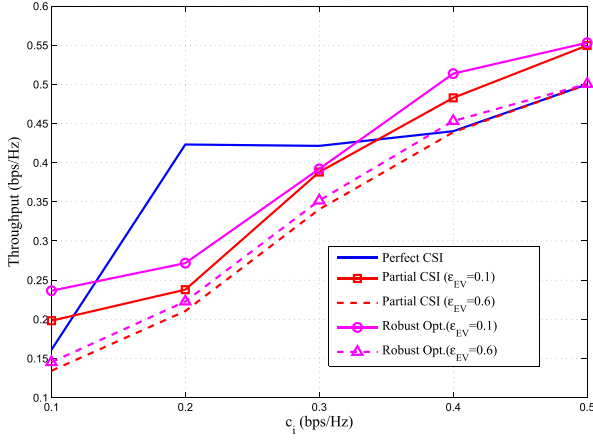


Fig. 10. Throughput versus the QoS constraint.

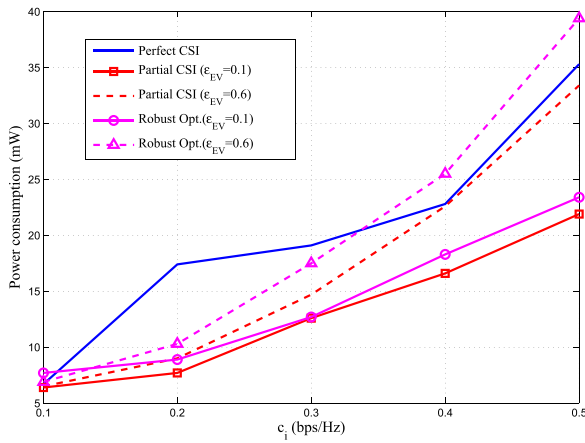


Fig. 11. Power consumption versus the QoS constraint.

TABLE III
AVERAGE NUMBER OF ITERATIONS FOR MAXIMIN ENERGY EFFICIENCY OPTIMIZATION

c_i (bps/Hz)	0.1	0.2	0.3	0.4	0.5
Perfect CSI	32.42	30.35	31.61	29.23	22.25
Partial CSI ($\epsilon_{EV} = 0.1$)	21.86	22.13	20.42	20.82	30.23
Partial CSI ($\epsilon_{EV} = 0.6$)	23.66	25.02	22.68	33.30	29.34
Robust Opt. ($\epsilon_{EV} = 0.1$)	16.05	23.27	23.36	31.15	18.62
Robust Opt. ($\epsilon_{EV} = 0.6$)	20.78	26.12	31.24	27.46	23.92

with $\epsilon_{EV} = 0.1$ is always better than the optimized EE of other cases. Furthermore, it is also observed that for $\epsilon_{EV} = 0.1$ “Partial CSI” and “Robust Opt.” outperform “Perfect CSI” in terms of EE performance, while “Perfect CSI” is superior to “Partial CSI” and “Robust Opt.” for $\epsilon_{EV} = 0.6$. The corresponding throughput and power consumption are plotted in Fig. 10 and 11, respectively. Table III shows that maximin EE optimization converges in less than 33 iterations, on average, in all considered cases.

Next, we investigate the maximin EE performance versus the transmit power budget. The QoS constraint c_i is fixed at 0.4 bps/Hz and P_i varies from 10 to 50 mW. The minimum EE performance versus the transmit power budget is illustrated in Fig. 12. Again, we observe that the optimized minimum EE saturates when the transmit power is larger than some threshold. This is due to the fact that under small transmit

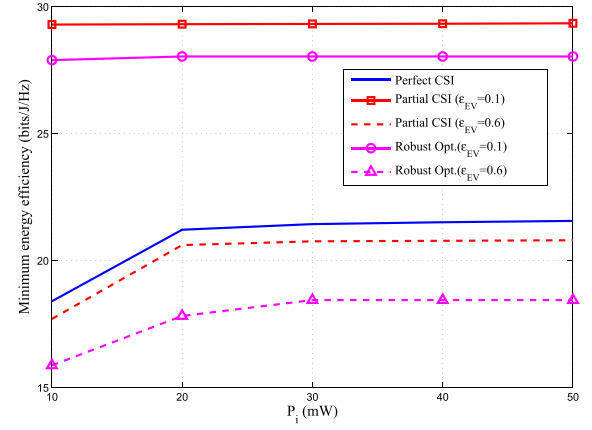


Fig. 12. Minimum energy efficiency versus the transmit power budget.

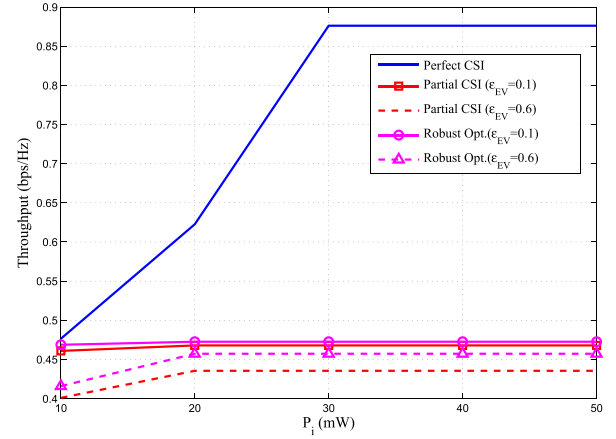


Fig. 13. Throughput versus the transmit power budget.

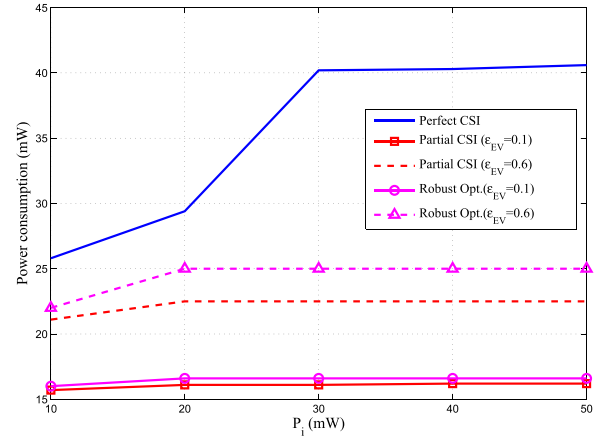


Fig. 14. Power consumption versus the transmit power budget.

power regime, the EE is maximized by maximizing the throughput in the numerator. When the transmit power is large enough to obtain the optimized EE, both throughput and power consumption accordingly saturate in Figs. 13 and 14.

VI. CONCLUSION

We have considered the problem of power allocation to maximize the worst links’s secrecy throughput or the network’s secure energy efficiency under various scenarios of

available channel state information. We have further proposed path-following algorithms tailored for each of the considered scenarios. Finally, we have provided simulations to show the efficiency of the proposed algorithms. Extensions to beamforming in multi-input single-output (MISO) interference networks with multiple eavesdroppers are under current investigation.

APPENDIX I OUTAGE PROBABILITY FUNDAMENTAL

Recall a probability distribution χ is called an *exponential distribution* if its probability density function (pdf) is in form $\lambda e^{-\lambda x}$ with $\lambda > 0$. It is immediate to check that $\text{Prob}(\chi \geq t) = e^{-\lambda t}$ and $\mathbb{E}[\chi] = 1/\lambda$. Recall the following result [29, (15)].

Theorem 1: Suppose $z_1, \dots, z_n$ are independent exponentially distributed random variables with $\mathbb{E}(z_i) = 1/\lambda_i$. Then for deterministic $p_i > 0$, $i = 1, \dots, n$:

$$\text{Prob}(p_1 z_1 \leq \sum_{i=2}^n p_i z_i) = 1 - \prod_{i=2}^n \frac{1}{1 + (\lambda_1/p_1)/(\lambda_i/p_i)}. \quad (56)$$

It follows from (56) that

$$\begin{aligned} \text{Prob}(p_1 z_1 > c + \sum_{i=2}^n p_i z_i) \\ = e^{-\lambda_1 c/p_1} \prod_{i=2}^n \frac{1}{1 + (\lambda_1/p_1)/(\lambda_i/p_i)} \end{aligned} \quad (57)$$

and

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma} > \gamma\right) \\ = \text{Prob}(p_1 z_1 > \sum_{i=2}^n \gamma p_i z_i + \gamma \sigma) \\ = e^{-\lambda_1 \gamma \sigma/p_1} \prod_{i=2}^n \frac{1}{1 + \gamma(\lambda_1/p_1)/(\lambda_i/p_i)}. \end{aligned} \quad (58)$$

Sometimes, it is also more convenient to write (56), (57) and (58) in terms of means $\bar{\lambda}_i = 1/\lambda_i$ of z_i as

$$\text{Prob}(p_1 z_1 \leq \sum_{i=2}^n p_i z_i) = 1 - \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + p_i \bar{\lambda}_i}, \quad (59)$$

$$\begin{aligned} \text{Prob}(p_1 z_1 > c + \sum_{i=2}^n p_i z_i) \\ = e^{-c/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + p_i \bar{\lambda}_i}, \end{aligned} \quad (60)$$

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma} > \gamma\right) \\ = e^{-\gamma \sigma/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + \gamma p_i \bar{\lambda}_i} \end{aligned} \quad (61)$$

Theorem 2: For given $\varepsilon > 0$, define

$$r_{\max} \triangleq \max\{r : \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2}\right) < r\} \leq \varepsilon\} \quad (62)$$

Then $r_{\max}$ is the unique positive root of the nonlinear equation

$$\ln(1 - \varepsilon) + \frac{r \sigma^2}{p_1 \bar{\lambda}_1} + \sum_{i=2}^n \ln\left(1 + \frac{r p_i \bar{\lambda}_i}{p_1 \bar{\lambda}_1}\right) = 0. \quad (63)$$

Proof: Applying (60) yields

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2} < r\right) \\ = \text{Prob}(p_1 z_1 < r(\sum_{i=2}^n p_i z_i + \sigma^2)) \\ = 1 - e^{-r \sigma^2/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + r p_i \bar{\lambda}_i}. \end{aligned} \quad (64)$$

Therefore,

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2} < r\right) \leq \varepsilon \\ \Leftrightarrow 1 - e^{-r \sigma^2/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + r p_i \bar{\lambda}_i} \leq \varepsilon \\ \Leftrightarrow \ln(1 - \varepsilon) + \frac{r \sigma^2}{p_1 \bar{\lambda}_1} + \sum_{i=2}^n \ln\left(1 + \frac{r p_i \bar{\lambda}_i}{p_1 \bar{\lambda}_1}\right) \leq 0. \end{aligned} \quad (65)$$

By noticing that the function in the LHS of (65) is increasing in r , we arrive at (63). $\square$

Theorem 3: Suppose $\bar{z}_i > 0$, $p_i > 0$, $\delta > 0$ and $\sigma > 0$ are deterministic values, while $\bar{z}_i$ are independent exponential distributions. For $\varepsilon > 0$, define

$$r_p \triangleq \max\{r : \text{Prob}\left(\frac{p_1 \bar{z}_1(1 + \delta \bar{z}_1)}{\sum_{i=2}^n p_i \bar{z}_i(1 + \delta \bar{z}_i) + \sigma^2} < r\right) \leq \varepsilon\}. \quad (66)$$

Then r_p is the unique positive root of the nonlinear equation

$$\begin{aligned} \delta \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} \\ + \delta \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) = 0. \end{aligned} \quad (67)$$

Proof: Using (65) yields

$$\begin{aligned} \text{Prob}\left(\frac{p_1 \bar{z}_1(1 + \delta \bar{z}_1)}{\sum_{i=2}^n p_i \bar{z}_i(1 + \delta \bar{z}_i) + \sigma^2} < r\right) \leq \varepsilon \\ \Leftrightarrow \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1 \delta} \\ + \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) \leq 0 \end{aligned} \quad (68)$$

$$\begin{aligned} \Leftrightarrow \delta \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} \\ + \delta \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) \leq 0. \end{aligned} \quad (69)$$

Again, by noticing that the function in the LHS of (69) is increasing in r we arrive at (67). $\square$

One can see that for $\delta \rightarrow 0$ (less uncertainty), (69) becomes

$$\begin{aligned} \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} &\leq 0 \\ \Leftrightarrow r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1 &\leq 0 \\ \Leftrightarrow r &\leq \frac{p_1 \bar{z}_1}{\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i}, \end{aligned}$$

so r_p is the standard ratio

$$\frac{p_1 \bar{z}_1}{\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i}.$$

APPENDIX II FUNDAMENTAL INEQUALITIES

Lemma 1: It is true that

$$\ln(1 + 1/t) \geq 1/(t+1) \quad \forall t > 0 \quad (70)$$

Proof: One can easily check $(t+1) \ln(1 + 1/t) \geq 1 \quad \forall t > 0$ by plotting the graph of function $(t+1) \ln(1 + 1/t)$ over $(0, +\infty)$. $\square$

Theorem 4: The function $f(x, y, t) \triangleq \ln(1 + 1/xy)^{1/t}$ is convex in the domain $\{x > 0, y > 0, t > 0\}$.

Proof: Writing $f(x, y, t) = (1/t)(\ln(xy+1) - \ln x - \ln y)$, it is ease to see that the Hessian $\nabla^2 f(x, y, t)$ is

$$\begin{aligned} \nabla^2 f(x, y, t) &= \begin{bmatrix} \frac{2xy+1}{x^2(xy+1)^2t} & \frac{1}{(xy+1)^2t} & \frac{1}{t^2(xy+1)x} \\ \frac{1}{(xy+1)^2t} & \frac{1}{y^2(xy+1)^2t} & \frac{1}{t^2(xy+1)y} \\ \frac{1}{t^2(xy+1)x} & \frac{1}{t^2(xy+1)y} & \frac{2 \ln(1 + 1/xy)}{t^3} \end{bmatrix} \\ &\succeq (x^2 y^2 (xy+1)^2 t^3)^{-1} \\ &\quad \cdot \begin{bmatrix} (xy+1)y^2 t^2 & x^2 y^2 t^2 & t(xy+1)xy^2 \\ x^2 y^2 t^2 & (xy+1)x^2 t^2 & t(xy+1)x^2 y \\ t(xy+1)xy^2 & t(xy+1)x^2 y & 2(xy+1)x^2 y^2 \end{bmatrix}, \end{aligned} \quad (71)$$

where the inequality (70) has been applied to the $(3, 3)$ -th entry of $\nabla^2 f(x, y, t)$ to arrive the matrix inequality in (71). Here and after, $\mathcal{A} \succeq \mathcal{B}$ for matrices $\mathcal{A}$ and $\mathcal{B}$ means that $\mathcal{A} - \mathcal{B}$ is a positive definite matrix. Then, calculating the subdeterminants of matrix in the right hand side (RHS) of (71) yields $(xy+1)y^2 t^2 > 0$,

$$\begin{vmatrix} \frac{1}{x^2(xy+1)t} & \frac{1}{(xy+1)^2t} \\ \frac{1}{(xy+1)^2t} & \frac{1}{y^2(xy+1)t} \end{vmatrix} = x^2 y^2 t^4 (2xy+1) > 0$$

and

$$\begin{vmatrix} (xy+1)y^2 t^2 & x^2 y^2 t^2 & t(xy+1)xy^2 \\ x^2 y^2 t^2 & (xy+1)x^2 t^2 & t(xy+1)x^2 y \\ t(xy+1)xy^2 & t(xy+1)x^2 y & 2(xy+1)x^2 y^2 \end{vmatrix} = x^4 y^4 t^4 (xy+1)[(xy+1)^3 - 1] > 0.$$

Therefore the matrix in the RHS of (71) is positive definite, implying that the Hessian $\nabla^2 f(x, y, t)$ is positive definite,

which is the necessary and sufficient condition for the convexity of f [25]. $\square$

As the function $f(x, y) \triangleq \ln(1 + 1/xy)$ is convex in the domain $\{x > 0, y > 0\}$ it follows that [25] for every $x > 0$, $y > 0$, $\bar{x} > 0$ and $\bar{y} > 0$,

$$\begin{aligned} \ln(1 + 1/xy) &= f(x, y) \\ &\geq f(\bar{x}, \bar{y}) + \langle \nabla f(\bar{x}, \bar{y}), (x, y) - (\bar{x}, \bar{y}) \rangle \\ &= \ln(1 + 1/\bar{x}\bar{y}) \\ &\quad + \frac{1/\bar{x}\bar{y}}{1 + 1/\bar{x}\bar{y}}(2 - x/\bar{x} - y/\bar{y}). \end{aligned} \quad (72)$$

Similarly, for the convex function $f(x, y, t) \triangleq \ln(1 + 1/xy)^{1/t}$, one has the following inequality for every $x > 0$, $y > 0$, $t > 0$, $\bar{x} > 0$, $\bar{y} > 0$ and $\bar{t} > 0$,

$$\begin{aligned} \frac{\ln(1 + 1/xy)}{t} &= f(x, y, t) \\ &\geq f(\bar{x}, \bar{y}, \bar{t}) + \langle \nabla f(\bar{x}, \bar{y}, \bar{t}), (x, y, t) - (\bar{x}, \bar{y}, \bar{t}) \rangle \\ &= \frac{2 \ln(1 + 1/\bar{x}\bar{y})}{\bar{t}} + \frac{1/\bar{x}\bar{y}}{\bar{t}(1 + 1/\bar{x}\bar{y})}(2 - x/\bar{x} - y/\bar{y}) - \frac{\ln(1 + 1/\bar{x}\bar{y})}{\bar{t}^2}t \end{aligned} \quad (73)$$

Analogously, the inequality

$$\begin{aligned} \frac{-\ln(1+x)}{t} &\geq 2 \frac{\alpha - \ln(1+\bar{x})}{\bar{t}} + \frac{\bar{x}}{\bar{t}(1+\bar{x})} \\ &\quad - \frac{x}{\bar{t}(1+\bar{x})} - \frac{\alpha - \ln(1+\bar{x})}{\bar{t}^2}t - \frac{\alpha}{t} \\ &\quad \forall 0 \leq x \leq M, \quad \alpha \geq \ln(1+M) + 0.5 \end{aligned} \quad (74)$$

follows from the convexity of function $\frac{\alpha - \ln(1+x)}{t}$ over the trust region $0 \leq x \leq M$.

Lastly, the inequality

$$\begin{aligned} \ln(1 + x/y) &\leq \ln(1 + \bar{x}/\bar{y}) + \frac{1}{1 + \bar{x}/\bar{y}} \\ &\quad \times (0.5(x^2/\bar{x} + \bar{x})/y - \bar{x}/\bar{y}) \end{aligned} \quad (75)$$

follows from the concavity of function $\ln(1+z)$ and then the inequality

$$\begin{aligned} x &= 0.5(x^2/\bar{x} + \bar{x}) - 0.5(x - \bar{x})^2/\bar{x} \\ &\leq 0.5(x^2/\bar{x} + \bar{x}) \quad \forall x > 0, \quad \bar{x} > 0. \end{aligned} \quad (76)$$

REFERENCES

- [1] A. G. Fragkiadakis, E. Z. Tragos, and I. G. Askoxylakis, "A survey on security threats and detection techniques in cognitive radio networks," *IEEE Commun. Surveys Tuts.*, vol. 15, no. 1, pp. 428–445, 1st Quart., 2013.
- [2] A. Mukherjee, S. A. A. Fakoorian, J. Huang, and A. L. Swindlehurst, "Principles of physical layer security in multiuser wireless networks: A survey," *IEEE Commun. Surveys Tuts.*, vol. 16, no. 3, pp. 1550–1573, 3rd Quart., 2014.
- [3] Y. Liang, H. V. Poor, and S. Shamai, "Secure communication over fading channels," *IEEE Trans. Inf. Theory*, vol. 54, no. 6, pp. 2470–2492, Jun. 2008.
- [4] R. Bassily *et al.*, "Cooperative security at the physical layer: A summary of recent advances," *IEEE Signal Process. Mag.*, vol. 30, no. 5, pp. 16–28, Sep. 2013.
- [5] H. V. Poor, "Information and inference in the wireless physical layer," *IEEE Wireless Commun.*, vol. 19, no. 1, pp. 40–47, Feb. 2012.

- [6] H. V. Poor and R. F. Schaefer, "Wireless physical layer security," *Proc. Nat. Acad. Sci. USA*, vol. 114, pp. 19–26, Jan. 2017.
- [7] D. Wang, B. Bai, W. Chen, and Z. Han, "Achieving high energy efficiency and physical-layer security in AF relaying," *IEEE Trans. Wireless Commun.*, vol. 15, no. 1, pp. 740–752, Jan. 2016.
- [8] N. T. Nghia, H. D. Tuan, T. Q. Duong, and H. V. Poor, "MIMO beamforming for secure and energy-efficient wireless communication," *IEEE Signal Process. Lett.*, vol. 24, no. 2, pp. 236–239, Feb. 2017.
- [9] L. Dong, Z. Han, A. P. Petropulu, and H. V. Poor, "Improving wireless physical layer security via cooperating relays," *IEEE Trans. Signal Process.*, vol. 58, no. 3, pp. 1875–1888, Mar. 2010.
- [10] J. Li, A. P. Petropulu, and S. Weber, "On cooperative relaying schemes for wireless physical layer security," *IEEE Trans. Signal Process.*, vol. 59, no. 10, pp. 4985–4997, Oct. 2011.
- [11] T. M. Hoang, T. Q. Duong, H. A. Suraweera, C. Tellambura, and H. V. Poor, "Cooperative beamforming and user selection for improving the security of relay-aided systems," *IEEE Trans. Commun.*, vol. 63, no. 12, pp. 5039–5051, Dec. 2015.
- [12] Y. Li, M. Sheng, C. Yang, and X. Wang, "Energy efficiency and spectral efficiency tradeoff in interference-limited wireless networks," *IEEE Commun. Lett.*, vol. 17, no. 10, pp. 1924–1927, Oct. 2013.
- [13] J. Rostampoor, S. M. Razavizadeh, and I. Lee, "Energy efficiency maximization precoding design for SWIPT in MIMO two-way relay networks," *IEEE Trans. Veh. Technol.*, vol. 66, no. 99, pp. 7888–7896, Sep. 2017.
- [14] M. Zheng, L. Chen, W. Liang, H. Yu, and J. Wu, "Energy-efficiency maximization for cooperative spectrum sensing in cognitive sensor networks," *IEEE Trans. Green Commun. Netw.*, vol. 1, no. 1, pp. 29–39, Mar. 2017.
- [15] D. Wang, B. Bai, W. Chen, and Z. Han, "Energy efficient secure communication over decode-and-forward relay channels," *IEEE Trans. Commun.*, vol. 63, no. 3, pp. 892–905, Mar. 2015.
- [16] J. Farhat, G. Brante, R. D. Souza, and J. L. Rebelatto, "Secure energy efficiency of selective decode and forward with distributed power allocation," in *Proc. IEEE Int. Symp. Wireless Commun. Syst. (ISWCS)*, Aug. 2015, pp. 701–705.
- [17] Y. Chen, L. Wang, M. Ma, and B. Jiao, "Power allocation for full-duplex relay networks: Secure energy efficiency optimization," in *Proc. IEEE Globecom*, Dec. 2016, pp. 1–6.
- [18] X. Xu, W. Yang, Y. Cai, and S. Jin, "On the secure spectral-energy efficiency tradeoff in random cognitive radio networks," *IEEE J. Sel. Areas Commun.*, vol. 34, no. 10, pp. 2706–2722, Oct. 2016.
- [19] J. Ouyang, M. Lin, Y. Zou, W. P. Zhu, and D. Massicotte, "Secrecy energy efficiency maximization in cognitive radio networks," *IEEE Access*, vol. 5, pp. 2641–2650, 2017.
- [20] T. T. Vu, H. H. Kha, and H. D. Tuan, "Transceiver design for optimizing the energy efficiency in multiuser MIMO channels," *IEEE Commun. Lett.*, vol. 20, no. 8, pp. 1507–1510, Aug. 2016.
- [21] J. Zheng, Y. Wu, N. Zhang, H. Zhou, Y. Cai, and X. Shen, "Optimal power control in ultra-dense small cell networks: A game-theoretic approach," *IEEE Trans. Wireless Commun.*, vol. 16, no. 7, pp. 4139–4150, Jul. 2017.
- [22] G. Zheng, I. Krikidis, C. Masouros, S. Timotheou, D.-A. Toumpakaris, and Z. Ding, "Rethinking the role of interference in wireless networks," *IEEE Commun. Mag.*, vol. 52, no. 11, pp. 152–158, Nov. 2014.
- [23] A. Chorti, S. M. Perlaza, Z. Han, and H. V. Poor, "On the resilience of wireless multiuser networks to passive and active eavesdroppers," *IEEE J. Sel. Areas Commun.*, vol. 31, no. 9, pp. 1850–1863, Sep. 2013.
- [24] H. H. Kha, H. D. Tuan, and H. H. Nguyen, "Fast global optimal power allocation in wireless networks by local D.C. programming," *IEEE Trans. Wireless Commun.*, vol. 11, no. 2, pp. 510–515, Feb. 2012.
- [25] H. Tuy, *Convex Analysis and Global Optimization*, 2nd ed. New York, NY, USA: Springer, 2016.
- [26] A. A. Nasir, H. D. Tuan, T. Q. Duong, and H. V. Poor, "Secrecy rate beamforming for multicell networks with information and energy harvesting," *IEEE Trans. Signal Process.*, vol. 65, no. 3, pp. 677–689, Feb. 2017.
- [27] H. H. M. Tam, H. D. Tuan, D. T. Ngo, T. Q. Duong, and H. V. Poor, "Joint load balancing and interference management for small-cell heterogeneous networks with limited backhaul capacity," *IEEE Trans. Wireless Commun.*, vol. 16, no. 2, pp. 872–884, Feb. 2017.
- [28] B. R. Marks and G. P. Wright, "A general inner approximation algorithm for nonconvex mathematical programs," *Oper. Res.*, vol. 26, no. 4, pp. 681–683, 1978.
- [29] S. Kandukuri and S. Boyd, "Optimal power control in interference-limited fading wireless channels with outage-probability specifications," *IEEE Trans. Wireless Commun.*, vol. 1, no. 1, pp. 46–55, Jan. 2002.
- [30] S. Ghosh, B. D. Rao, and J. R. Zeidler, "Outage-efficient strategies for multiuser MIMO networks with channel distribution information," *IEEE Trans. Signal Process.*, vol. 58, no. 12, pp. 6312–6324, Dec. 2010.
- [31] W. Li, T.-H. Chang, C. Lin, and C.-Y. Chi, "Coordinated beamforming for multiuser MISO interference channel under rate outage constraints," *IEEE Trans. Signal Process.*, vol. 61, no. 5, pp. 1087–1103, Mar. 2013.
- [32] W. Li, T. Chang, and C. Chi, "Multicell coordinated beamforming with rate outage constraint—Part I: Complexity analysis," *IEEE Trans. Signal Process.*, vol. 63, no. 11, pp. 2749–2762, Jun. 2015.
- [33] W. Li, T. Chang, and C. Chi, "Multicell coordinated beamforming with rate outage constraint—Part II: Efficient approximation algorithms," *IEEE Trans. Signal Process.*, vol. 63, no. 11, pp. 2763–2778, Jun. 2015.
- [34] C. Wang, H.-M. Wang, D. W. K. Ng, X.-G. Xia, and C. Liu, "Joint beamforming and power allocation for secrecy in peer-to-peer relay networks," *IEEE Trans. Wireless Commun.*, vol. 14, no. 6, pp. 3280–3293, Jun. 2015.



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