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## Layer- and substrate-dependent charge density wave criticality in 1T–TiSe<sub>2</sub>

To cite this article: Sadhu Kolekar *et al* 2018 *2D Mater.* **5** 015006

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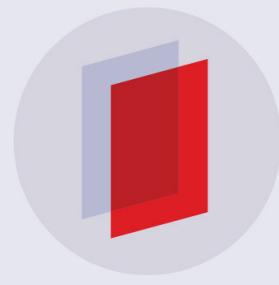
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## 2D Materials



### PAPER

# Layer- and substrate-dependent charge density wave criticality in 1T-TiSe<sub>2</sub>

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Keywords: TiSe<sub>2</sub>, exciton condensate, monolayer, scanning tunneling spectroscopy, exciton insulator

### Abstract

TiSe<sub>2</sub> exhibits an unconventional charge density wave (CDW) that has been associated with an excitonic insulator transition. Here we investigate how the CDW transition is changed for single to few layers compared to bulk TiSe<sub>2</sub>. TiSe<sub>2</sub> grown by molecular beam epitaxy on HOPG- or MoS<sub>2</sub>-substrates is characterized by variable temperature scanning tunneling microscopy and spectroscopy. We show that the CDW state persists for the monolayer but the transition temperature  $T_{\text{CDW}}$  is significantly increased compared to the bulk. Furthermore,  $T_{\text{CDW}}$  is strongly dependent on the substrate material. Within the model of an excitonic insulator phase for TiSe<sub>2</sub>, the substrate dependence may be associated with variations of the excitonic binding energies by the dielectric properties of the substrate. Interestingly, for single layer TiSe<sub>2</sub> on HOPG we also observe peaks in the tunneling spectra below 50 K, which are tentatively assigned to coherence peaks of an excitonic condensate. The peaks are observed below  $T_{\text{CDW}}$  of  $\sim 230$  K, suggesting that an excitonic insulator induced CDW can exist without a phase coherent state.

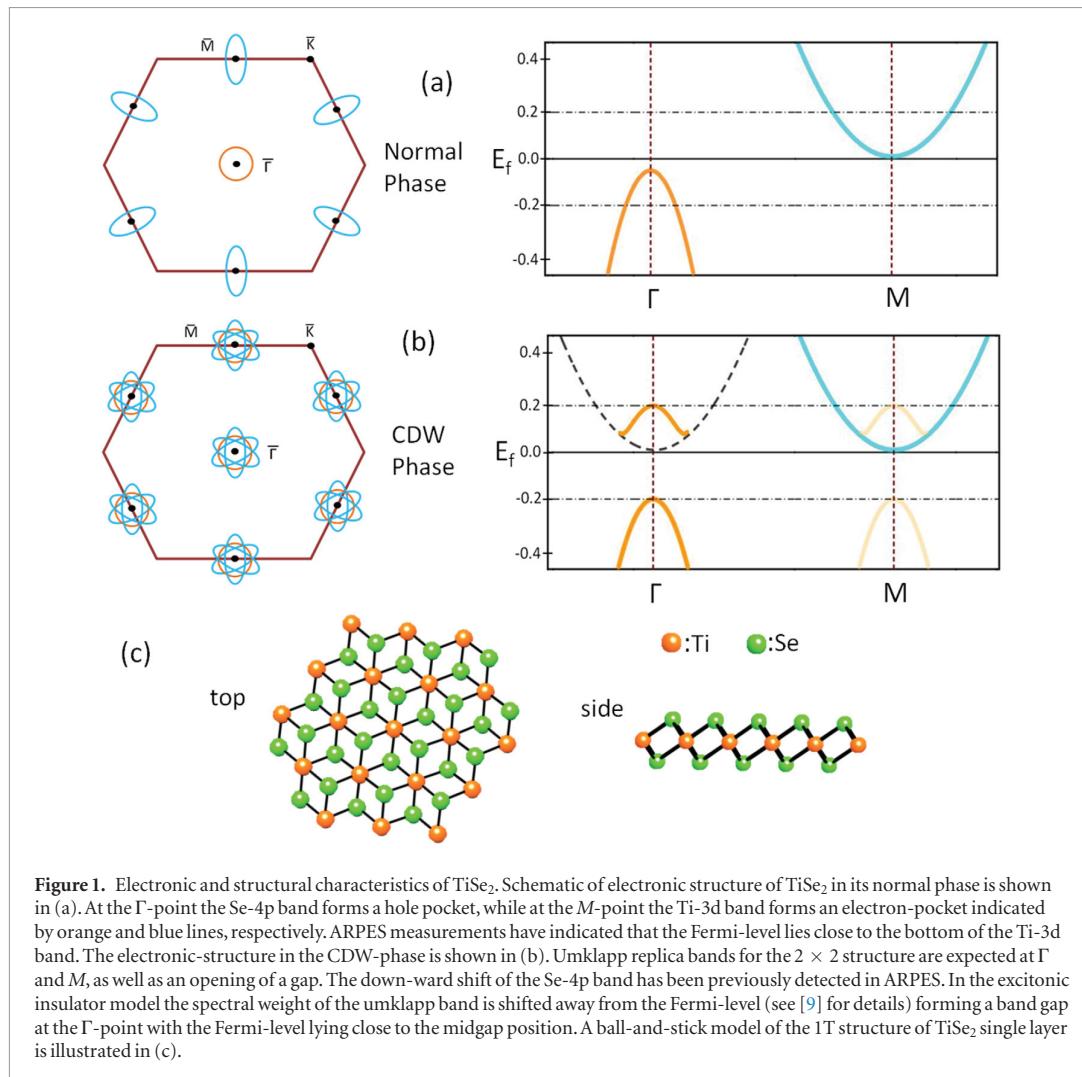
It has been demonstrated that reducing the dimensions to a single-layer enables modifications of conventional charge density waves (CDW) in metallic transition metal dichalcogenides (TMDCs) [1, 2]. For TiSe<sub>2</sub>, however, traditional explanations for CDW formation, based on Fermi surface nesting, fail [3]. Instead, an unconventional excitonic mechanism has been invoked [4, 5]. This implies a CDW dependence on the number of layers because the exciton binding energy is increased in single layer TMDCs compared to bulk [6].

Bulk TiSe<sub>2</sub> forms a commensurate  $2 \times 2 \times 2$  CDW with a transition temperature around 200 K. In view of Fermi wave-vector nesting failing to explain CDW in TiSe<sub>2</sub>, the CDW transition has been proposed to be related to a Jahn–Teller like lattice distortion [7, 8], the formation of an excitonic condensate [9–12], or a combination of these effects [13]. The interest in TiSe<sub>2</sub> has also been fueled by recent discoveries that showed that superconductivity can be induced by copper doping [14] or field-effect doping of few-layer TiSe<sub>2</sub> [15]. In both cases the suppression of the CDW [16] is considered essential in order to achieve superconductivity.

The basic electronic structure of TiSe<sub>2</sub> consists of strongly dispersing Se-4p derived valence bands (three bands have been identified in ARPES) at the

$\Gamma$ -point and Ti-3d derived electron-pockets at the  $M$ -points of the Brillouin zone (BZ) boundary. There is increasing evidence that the Se-4p and Ti-3d states do not overlap even in the normal state and instead exhibit an energy gap of  $\sim 50$  meV. Upon formation of  $2 \times 2 (\times 2)$  CDW, strong ‘umklapp’ shadow bands are formed. The electronic structure in the normal- and the  $2 \times 2$  CDW-phase are schematically shown in figure 1. Recent ARPES studies on single-layer samples indicate a similar valence band structure to bulk samples, with some increase in the binding energy of the valence band maximum [17, 18]. Generally, ARPES also agrees for both single layer as well as bulk samples that the bottom of the Ti-3d band is occupied at the  $M$ -point. However, while the Se-4p band shows strong spectral weight at the  $M$ -point in the CDW phase, no intensity of the Ti-3d states at the  $\Gamma$ -point are observed in ARPES [12, 17, 18]. The vanishing spectral weight of such a Ti-3d umklapp-band at  $\Gamma$  has been explained in the picture of an excitonic insulator [9]. In this model, the Fermi-level should lie close-to mid-gap for the band gap of the excitonic insulator phase at  $\Gamma$ , as illustrated in figure 1.

The band structure of TiSe<sub>2</sub> makes it potentially susceptible to formation of an excitonic condensate as the basic mechanism for formation of the CDW. This mechanism was first predicted in the 1960s and

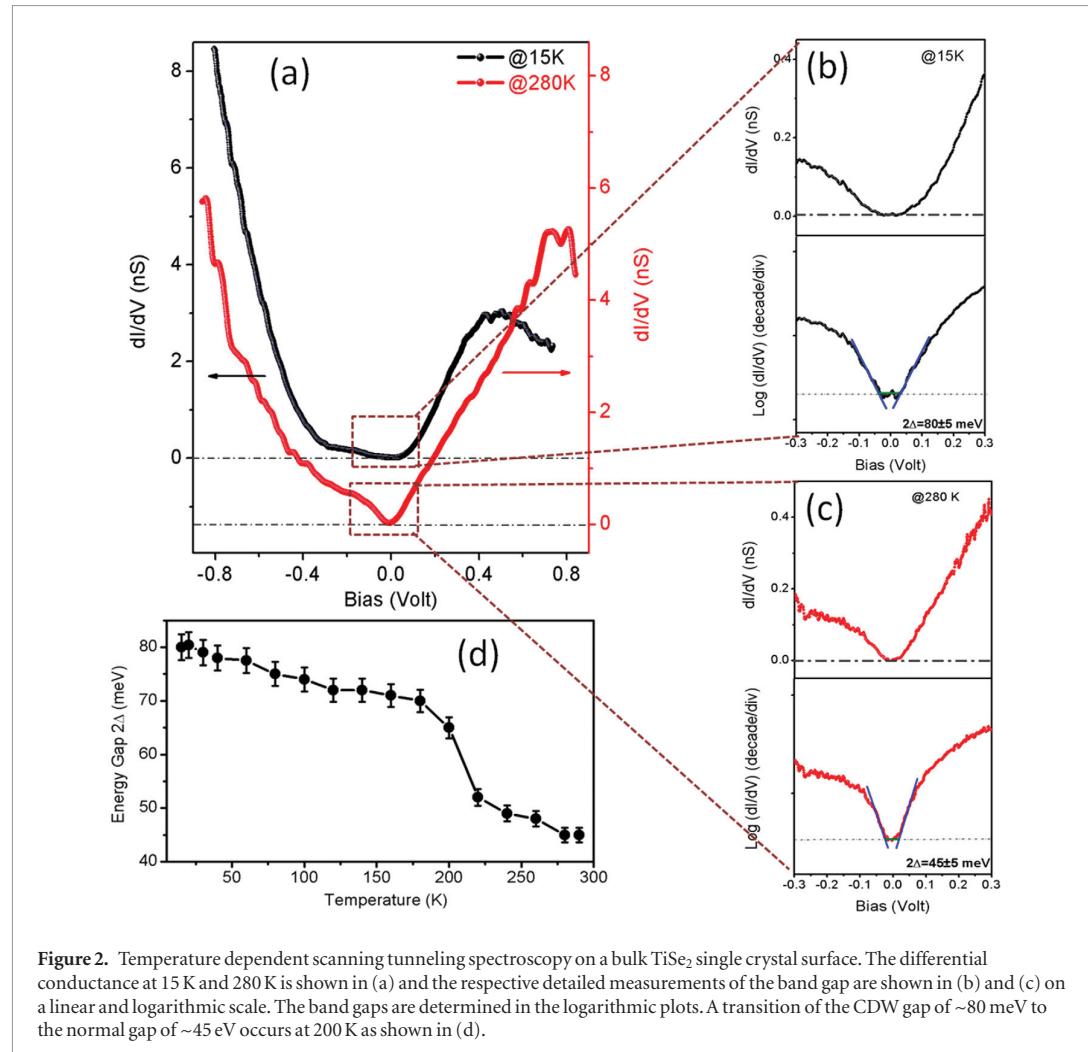


**Figure 1.** Electronic and structural characteristics of  $\text{TiSe}_2$ . Schematic of electronic structure of  $\text{TiSe}_2$  in its normal phase is shown in (a). At the  $\Gamma$ -point the Se-4p band forms a hole pocket, while at the  $M$ -point the Ti-3d band forms an electron-pocket indicated by orange and blue lines, respectively. ARPES measurements have indicated that the Fermi-level lies close to the bottom of the Ti-3d band. The electronic-structure in the CDW-phase is shown in (b). Umklapp replica bands for the  $2 \times 2$  structure are expected at  $\Gamma$  and  $M$ , as well as an opening of a gap. The down-ward shift of the Se-4p band has been previously detected in ARPES. In the excitonic insulator model the spectral weight of the umklapp band is shifted away from the Fermi-level (see [9] for details) forming a band gap at the  $\Gamma$ -point with the Fermi-level lying close to the midgap position. A ball-and-stick model of the 1T structure of  $\text{TiSe}_2$  single layer is illustrated in (c).

may be expected for a material with the valence band and conduction band offset in  $k$ -space with either a small energy overlap or gap [19, 20]. In such a material spontaneous excitation of electrons from the valence band into the conduction band could become energetically favorable if the electron–hole pair (exciton) binding energy is larger than the energy cost for promoting electrons to the conduction band, i.e. the band gap energy. In this scenario, the exciton binding energy is related to the order parameter in a BCS like description of the CDW phase transition, implying that the transition temperature should be related to the exciton binding energy. Generally, the exciton binding energy is a material property and cannot be easily modified. For TMDCs, however, the exciton binding energy has been demonstrated to increase markedly with the decrease of number of layers. Consequently, if the excitonic insulator model for the CDW in  $\text{TiSe}_2$  is valid, the increased exciton binding energy for monolayers is expected to result in a larger CDW-gap and an increased transition temperature for monolayers compared to bulk  $\text{TiSe}_2$  may be predicted. Moreover, the excitonic binding energy for a monolayer is tuned by

the dielectric properties of the material surrounding the monolayer [21, 22]. Consequently, the CDW transition may depend on dielectric properties of the substrate material the  $\text{TiSe}_2$  monolayer is supported on.

Here we investigate the properties of  $\text{TiSe}_2$  with variable temperature scanning tunneling spectroscopy (STS). STS enables measuring the opening of a gap between valence and conduction band and thus makes it a valuable tool for characterizing many body phenomena [23]. However, STS does not provide momentum resolved information and STS mainly probes states around  $\Gamma$ -point, specifically for 2D materials. We observe a band gap opening that is significantly larger for the single layer than the few layer materials. Moreover, the band gap strongly depends on the substrate material. Using variable temperature STS we can determine the transition temperature by fitting of the band gap to a mean field theory expression. Interestingly, we also observe pronounced peaks close to the band edges in the differential conductance for  $\text{TiSe}_2$ /HOPG at below 50 K. We tentatively assign these pronounced peaks to phase coherence peaks expected to exist in an isotropic Bose–Einstein condensate of excitons.



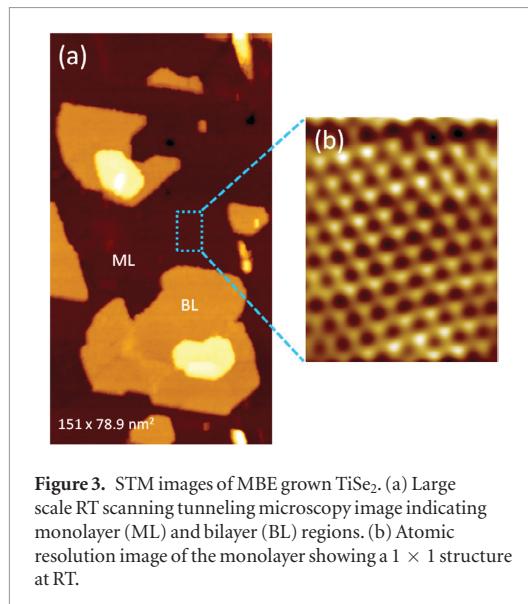
**Figure 2.** Temperature dependent scanning tunneling spectroscopy on a bulk  $\text{TiSe}_2$  single crystal surface. The differential conductance at 15 K and 280 K is shown in (a) and the respective detailed measurements of the band gap are shown in (b) and (c) on a linear and logarithmic scale. The band gaps are determined in the logarithmic plots. A transition of the CDW gap of  $\sim 80$  meV to the normal gap of  $\sim 45$  meV occurs at 200 K as shown in (d).

## Results

Before addressing monolayer samples, we discuss measurements on bulk  $\text{TiSe}_2$  to provide a comparison to the few and monolayer samples. Figure 2 shows STS measurements on a single crystal  $\text{TiSe}_2$  sample with our spectra being consistent with previously reported data on bulk samples [24]. We are extracting the band gap as a function of temperature by plotting differential conductance  $dI/dV$  and finding the valence band maximum and conduction band minimum by extrapolating the respective band edges to zero. With this approach, we find a small gap of  $\sim 45$  meV for the normal state at RT and a slightly larger gap of  $\sim 80$  meV at 15 K. The dependence of the measured gap on temperature is displayed in figure 2(d). A transition from the lower to the larger band gap value occurs at  $\sim 200$  K, consistent with the reported CDW transition of  $\text{TiSe}_2$ . These measurements give a value for  $2\Delta/(k_B T_c) = 80$  meV/( $k_B$  200 K) = 4.64, i.e. a slightly larger value than the prediction of conventional BCS theory of 3.65. The larger value is explained by stronger quasiparticle coupling.

$\text{TiSe}_2$  thin films grown by MBE enable the investigation of the dependence of the CDW band gap as

a function of the number of  $\text{TiSe}_2$  layers. Figure 3 shows room temperature STM images of typical  $\text{TiSe}_2$  films. The large-scale image shows the formation of extended monolayer terraces with some bilayer islands. Atomic scale images of the terraces show good quality similar to previously reported MBE-grown  $\text{TiSe}_2$  [25]. For further spectroscopic characterization the MBE grown samples were transferred in a vacuum suitcase to a dedicated variable temperature STM. In order to characterize the dependence of the electronic structure on the number of layers we choose a sample-region that exhibits non-uniform film thickness, possibly at a growth spiral. The band gap measurement at 15 K, i.e. in CDW phase, is shown in figure 4 as a function of layers determined from the step height separating the individual terraces. For only 3 layers the band gap measurement is, to within the experimental uncertainty, the same as the band gap of bulk surfaces. For one- and two-layer thick samples the band gap is significantly larger and we measure  $\sim 180$  meV for the monolayer film. Moreover, the differential conductance for the monolayer exhibits prominent peaks that are not present in bulk  $\text{TiSe}_2$ . For the monolayer  $\text{TiSe}_2$ , these peaks appear at energies below the valence band maximum and above the conduction band minimum.



Comparison with two independent ARPES measurements for monolayer TiSe<sub>2</sub> [17,18], shows that the energy of the peaks corresponds closely to the band maximum of the Se-4p band. All the measurements have been reproduced on three independent samples and at several spots on these samples.

In order to demonstrate that these peaks are associated with a 2 × 2 charge density wave in the monolayer, we performed dI/dV mapping with set-points below (120 mV) and at (200 mV) the peak position. Figures 4(d) and (e) shows the dI/dV maps. For 120 mV set-point only weak modulations are observed while at 200 mV a clear 2 × 2 intensity modulation is observed corresponding to the CDW periodicity. This illustrates that even for the monolayer a 2 × 2 charge modulation is observed and the pronounced peaks in the differential conductance measurement are related to this CDW modulation.

In further investigations, we characterize the band gap measured in STS as a function of sample temperature, as shown in figure 5(a). The first observation is that the pronounced peaks become strongly suppressed and vanish completely at ~50 K (figures 5(c) and (d)), while the STS-band gap remains unaltered. The disappearance of the peaks in differential conductance indicates that they are associated with a thermally driven transition. The fact that this transition is below  $T_{CDW}$  shows that the CDW can form independent of the observation of the pronounced peaks in differential conductance. Further increase in sample temperature leads eventually to a reduced band gap and the band gap reaches the same value as for the normal phase in bulk TiSe<sub>2</sub>. This demonstrates that the band gap opening is entirely a consequence of the CDW transition. As expected an increased band gap for single layer also translates into an increase in  $T_{CDW}$  from ~200 K to ~230 K. A similar increase in  $T_{CDW}$  for monolayer TiSe<sub>2</sub> on graphene has recently been deduced from photoemission measurements [18].

A possible explanation for the strongly increased CDW-gap in single-layer materials is the increased exciton binding energy in single-layer TMDCs compared to bulk materials leading to a larger magnitude of the order parameter in an excitonic insulator driven CDW transition [9]. A test for the correlation between CDW in TiSe<sub>2</sub> and the excitonic binding energy is to vary the excitonic binding energy. Ordinarily the excitonic binding energy of a material is a material property. However, in monolayers TMDCs the surrounding dielectric material influences the Coulomb screening of electron–hole pairs. Replacing the HOPG substrate with a wide band gap semiconducting van der Waals material is expected to reduce charge screening and thus increase the exciton binding energy. Here we choose MoS<sub>2</sub> as such a material. Figure 5(b) shows STS spectra for monolayer TiSe<sub>2</sub> on MoS<sub>2</sub> as a function of temperature. In agreement with the excitonic picture, the band gap in the CDW phase and  $T_c$  is significantly increased for TiSe<sub>2</sub>/MoS<sub>2</sub> system compared to TiSe<sub>2</sub> on HOPG. Interestingly, contrary to TiSe<sub>2</sub>/HOPG no pronounced peaks in the differential conductance are observed down to lowest accessible temperature of 15 K.

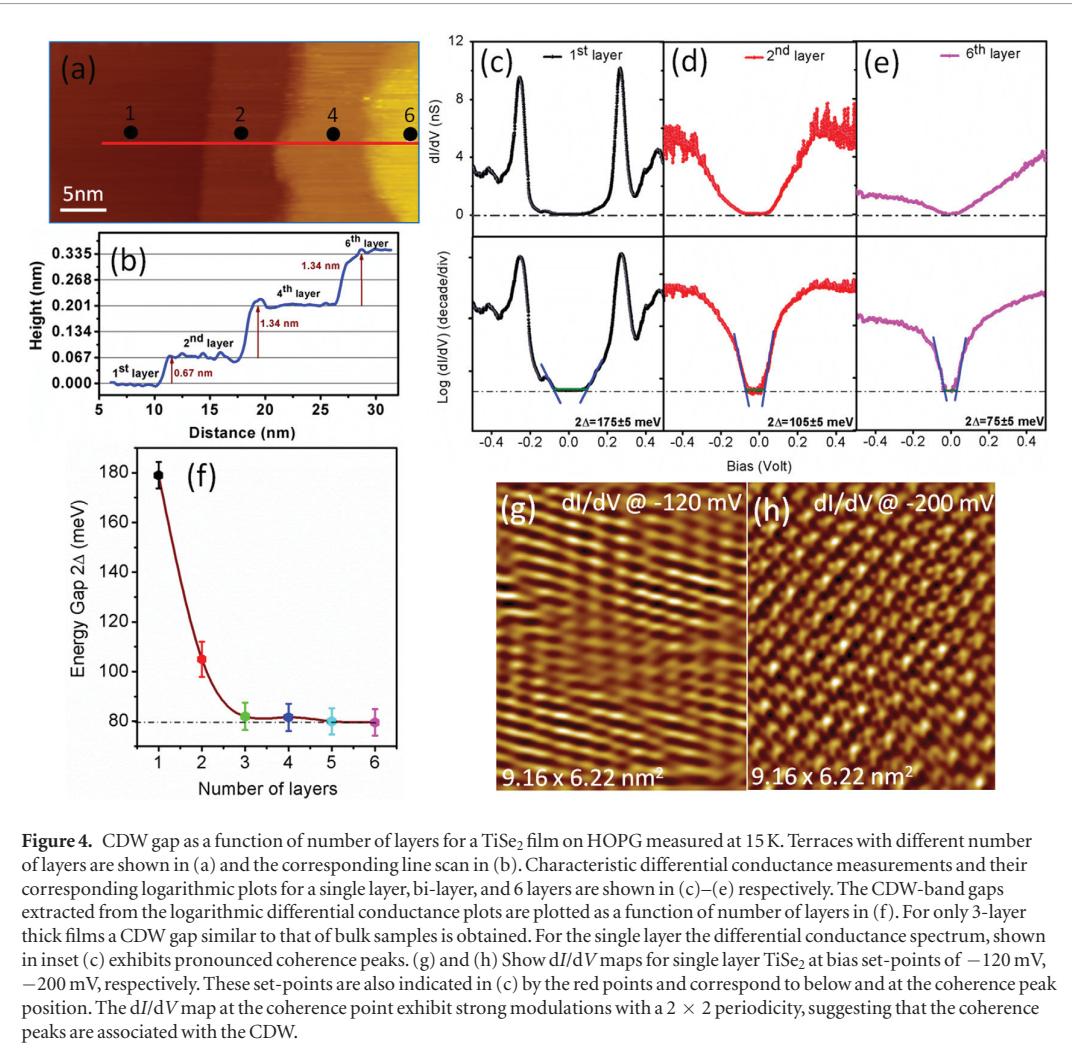
## Discussion

The variation of the STS band gaps for bulk TiSe<sub>2</sub> as well as for single layer TiSe<sub>2</sub> on HOPG and MoS<sub>2</sub> substrates follow an expected mean field theory temperature dependence as shown in figure 6. The data are fit based on the mean-field theory expression [18]:

$$\Delta^2(T) - \Delta^2(T_{CDW}) \sim \tanh^2 \left( A \sqrt{\frac{T_{CDW}}{T} - 1} \right), \quad (1)$$

where  $A = 2.1$  is a proportionality constant, and  $\Delta(T)$  and  $\Delta(T_{CDW})$  is the energy gap at temperature  $T$ , and the constant value for the energy gap above the critical temperature  $T_{CDW}$ , respectively. The Transition temperature derived from this fitting agrees with the generally accepted  $T_c$  for bulk TiSe<sub>2</sub> of ~200 K and shows an increase to 230 K and 280 K for monolayers on HOPG and MoS<sub>2</sub>, respectively. This increase in CDW transition temperature for monolayer TiSe<sub>2</sub> from HOPG to MoS<sub>2</sub> substrate is consistent with the measured large energy gaps. A larger exciton binding energy for single layer TiSe<sub>2</sub> supported on the semi-conducting MoS<sub>2</sub> compared to the semi-metallic graphite is expected. Consequently, the trend of an increased  $T_{CDW}$  for monolayer TiSe<sub>2</sub> on MoS<sub>2</sub> compared to HOPG, is also consistent within the model of an excitonic insulator phase which suggests a scaling of the transition temperature with the excitonic binding energy.

It is important to compare our STS work with previously reported ARPES studies both on bulk [5, 9, 12] and monolayer TiSe<sub>2</sub> samples [17, 18]. In ARPES measurements an opening of a gap below the Fermi-level is observed with the Ti-3d state at the Fermi-level remaining at the *M*-point. Only a down ward shift of



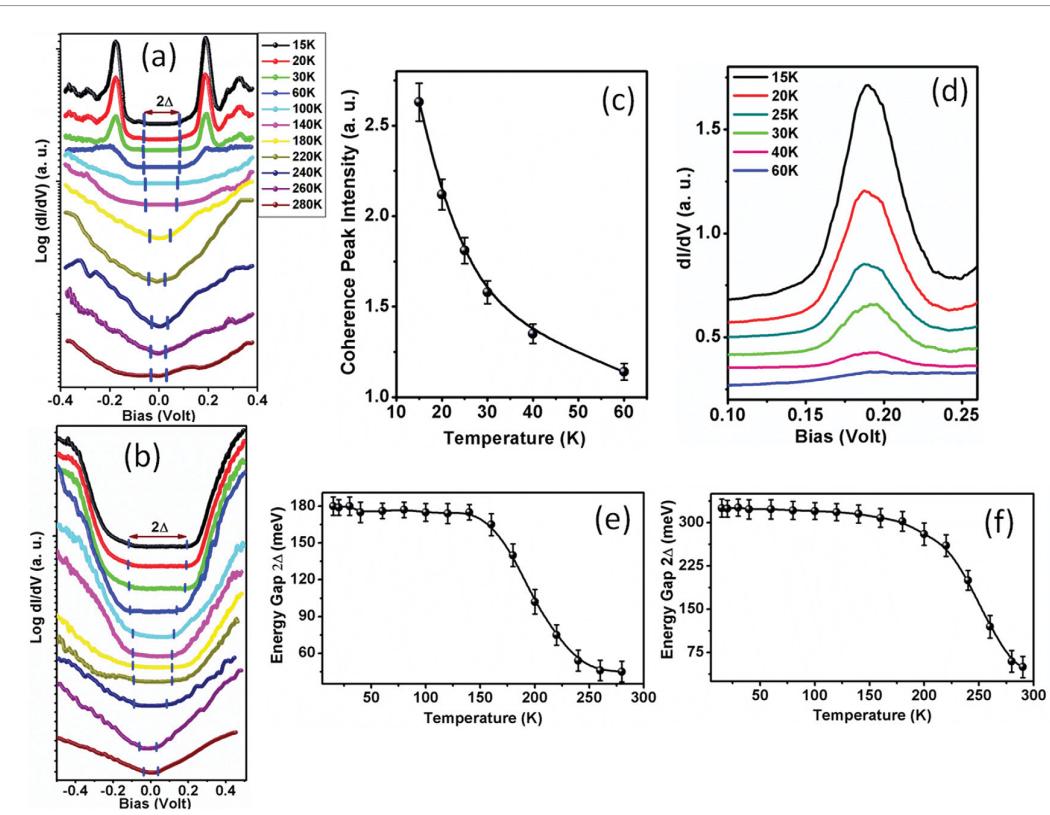
**Figure 4.** CDW gap as a function of number of layers for a  $\text{TiSe}_2$  film on HOPG measured at 15 K. Terraces with different number of layers are shown in (a) and the corresponding line scan in (b). Characteristic differential conductance measurements and their corresponding logarithmic plots for a single layer, bi-layer, and 6 layers are shown in (c)–(e) respectively. The CDW-band gaps extracted from the logarithmic differential conductance plots are plotted as a function of number of layers in (f). For only 3-layer thick films a CDW gap similar to that of bulk samples is obtained. For the single layer the differential conductance spectrum, shown in inset (c) exhibits pronounced coherence peaks. (g) and (h) Show  $dI/dV$  maps for single layer  $\text{TiSe}_2$  at bias set-points of  $-120$  mV,  $-200$  mV, respectively. These set-points are also indicated in (c) by the red points and correspond to below and at the coherence peak position. The  $dI/dV$  map at the coherence point exhibit strong modulations with a  $2 \times 2$  periodicity, suggesting that the coherence peaks are associated with the CDW.

the Se-4p states is observed in ARPES for temperatures below the CDW transition. We may compare the ARPES Se-4p band maximum as a function of temperature for monolayer  $\text{TiSe}_2$  on grapheme [17, 18] with our STS data. It is apparent that the pronounced peak in the differential conductance at low temperature coincides with the Se-4p band maximum in ARPES data and thus this feature should be assigned to the band maximum of Se-4p. However, no further states are observed in ARPES between the Se-4p band maximum and the Ti-3d conduction band and thus we currently cannot explain the small intensity observed in STS above the Se-4p state. Nevertheless, we use this onset for plotting the band gap versus temperature because it is the only reliable feature at elevated temperatures or for enabling comparison with  $\text{TiSe}_2$  on  $\text{MoS}_2$  substrates.

While ARPES cannot measure the conduction band, a partially occupied Ti-3d band at the  $M$ -point is consistently observed in ARPES indicating that the Fermi-level lies very close to the bottom of the Ti-3d band. On the other hand, while the umklapp Se-4p band is observed in ARPES at the ‘original’  $M$ -point of the BZ, no indication of an equivalent umklapp Ti-3d band at the  $\Gamma$ -point is observed in ARPES studies [17].

Such a negligible spectral weight of an umklapp Ti-3d state has been explained theoretically for an excitonic insulator phase [9]. Thus our STS data can be reconciled with the ARPES data, because in STS we are most sensitive to states at the  $\Gamma$ -point. This is in particularly true for 2D materials. In general, it is established that the tunneling current is dominated by states with a large velocity component normal to the surface and consequently states with in-plane momenta are contributing less to the tunneling signal, which has been referred to the ‘tunneling cone’ [26]. Thus we propose that the observed STS-gap reflects only the magnitude of the gap at the  $\Gamma$ -point, while the metallic Ti-3d states at the  $M$ -point are of negligible intensity in our STS data. Furthermore, we also expect the Fermi-level to lie close to mid-gap in the excitonic insulator phase at the  $\Gamma$ -point, as sketched in figure 1. Moreover, the excitonic condensate state has been predicted at  $\sim 150$  meV above the Fermi-level for an order parameter of 100 meV [9] similar to the observed position of the peak in differential conductance.

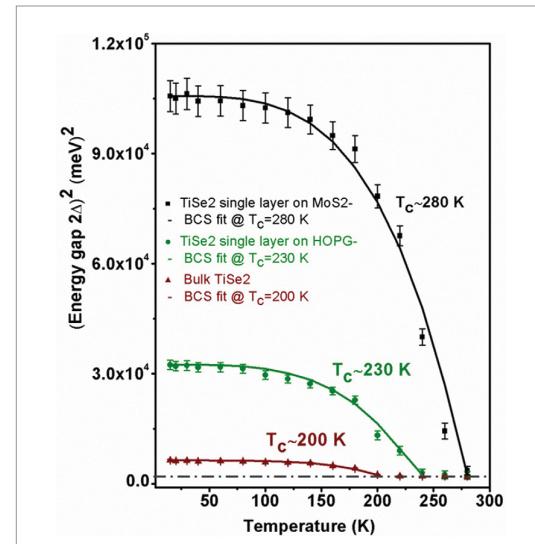
The strong and reproducible peaks in the differential conductance for single layer  $\text{TiSe}_2$  on HOPG and their well-defined temperature dependence require some explanation. Their appearance is similar to



**Figure 5.** Temperature dependent differential conductance spectra for single layer TiSe<sub>2</sub> on HOPG- and MoS<sub>2</sub>-substrates. The differential conductance of TiSe<sub>2</sub> on HOPG is shown in (a) and for TiSe<sub>2</sub> on MoS<sub>2</sub> in (b). The change of the coherence peak as a function of T is shown in (c) and (d). The band edges are marked in (a) and (b) by short lines and the band gap is plotted in (e) for TiSe<sub>2</sub> on HOPG and in (f) for TiSe<sub>2</sub> on MoS<sub>2</sub>.

coherence peaks in superconductors below  $T_c$ , albeit the larger energy gap observed for the CDW in TiSe<sub>2</sub>. If an excitonic condensate is formed the excitons are expected to also form a phase coherent state and this should be observed in STS as coherence peaks. To the best of our knowledge, no such peaks have ever been reported for TiSe<sub>2</sub>, nor do we observe it for any other material than single layer TiSe<sub>2</sub> on HOPG. Moreover, it is only observed below 50 K, i.e. significantly below  $T_{CDW}$ . Thus, the absence of these peaks in certain materials would suggest that an excitonic insulator phase may form without long range phase coherence.

The lack of coherence-peaks for monolayer-TiSe<sub>2</sub>/MoS<sub>2</sub> also suggests that phase coherence can be easily destroyed by, for example, stronger scattering mechanisms in such heterostructures compared to TiSe<sub>2</sub>/HOPG samples. Scattering may be related to a stronger interlayer coupling because of interlayer hybridization of frontier orbitals in TMDC heterostructures [27]. Electronic interlayer coupling give rise to stronger scattering or even interlayer excitons as observed in semiconducting van der Waals TMDC-heterostructures [28, 29]. Thus, we predict that the coherent state may only be observed in weakly coupled heterostructures, such as observed for TiSe<sub>2</sub>/HOPG, or truly freestanding single layer TiSe<sub>2</sub>. Clearly, further studies are required to verify the assignment of the pronounced



**Figure 6.** Mean field theory fitting of the band gap versus temperature for CDW transitions. Data for TiSe<sub>2</sub> single layer on HOPG- and MoS<sub>2</sub>-substrates as well as for bulk TiSe<sub>2</sub> are shown. The mean-field theory is best fit with transition temperatures of 200 K, 230 K, and 280 K for bulk TiSe<sub>2</sub>, single layer on HOPG, and single layer on MoS<sub>2</sub>, respectively.

peaks in STS to coherence peaks. For a start, contactless measurements for TiSe<sub>2</sub>/HOPG by for example ARPES would be important.

## Conclusions

In conclusion, the CDW transition temperature in single layer is increased compared to bulk  $\text{TiSe}_2$  and can be further controlled by the choice of support. The increase in the gap can be understood by variations in the excitonic binding energy in TMDCs and thus is consistent with an excitonic origin for the CDW in  $\text{TiSe}_2$ . Interestingly, pronounced peaks in the differential conductance for  $\text{TiSe}_2$  monolayers on HOPG are observed which we tentatively attribute to the formation of a phase coherent state in an excitonic condensate. In general, this study shows that new insight in many body physics of layered TMDCs can be gleaned from studying monolayers and their interfaces. Moreover, we demonstrated the potential for tuning many body physics in these materials by growing van der Waals heterostructures.

## Methods

Mono- to few-layer  $\text{TiSe}_2$  was grown on HOPG or  $\text{MoS}_2$  substrates by e-beam evaporation of Ti and simultaneous deposition of atomic Se from a hot wall Se-cracker source. The substrates were cleaved in air and immediately introduced into the vacuum chamber. The substrates were subsequently annealed in UHV at 300 °C for 5 h prior to film growth.  $\text{TiSe}_2$  was grown at a substrate temperature of 200 °C and at a growth rate of 0.56 ml min<sup>-1</sup>. After growth, the samples were characterized by XPS and room temperature STM before transferring them in a vacuum suitcase to a variable temperature STM. This STM is a commercial Pan-style RHK STM. A closed cycle cryostat allowed cooling of the sample to a minimum of 15 K and the sample could be heated in the cryostat to various target temperatures. STM and STS was taken with a cut PtIr-tip. For  $dI/dV$  spectroscopy a lock-in amplifier with a modulation voltage of 7 mV and reference frequency 995 Hz was used. For reference, we also conducted spectra on bulk  $\text{TiSe}_2$  single crystals. STS measurements on  $\text{TiSe}_2$  single crystals were previously published and our data are in good agreement with such studies confirming consistency of our data with those in different groups.

## Acknowledgement

The authors acknowledge support from the National Science Foundation under grant DMR-1701390.

## Notes

The authors declare no competing financial interests.

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