



# Microscale characterization of rupture nucleation unravels precursors to faulting in rocks



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## ABSTRACT

Precursory signals, manifestations of microscale damage that precedes dynamic faulting, are key to earthquake forecasting and risk mitigation. Detections of precursors have primarily relied on measurements performed using sensors installed at some distance away from the rupture area in both field and laboratory experiments. Direct observations of continuous microscale damage accumulated during fault nucleation and propagation are scarce. Using an X-ray transparent triaxial deformation apparatus, we show the first quantitative high resolution three-dimensional (3D) information about damage evolution of rocks undergoing brittle failure. The dynamic microtomography images documented a spectrum of damage characteristics and different fault growth patterns. The interplay between various deformation mechanisms can result in either a positive, negative, or constant net volume change. Consequently, changes in rock density and acoustic wave velocities before faulting are expected to vary in different tectonics settings, hence making failure forecasting intrinsically dependent on rock type at depth.

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## 1. Introduction

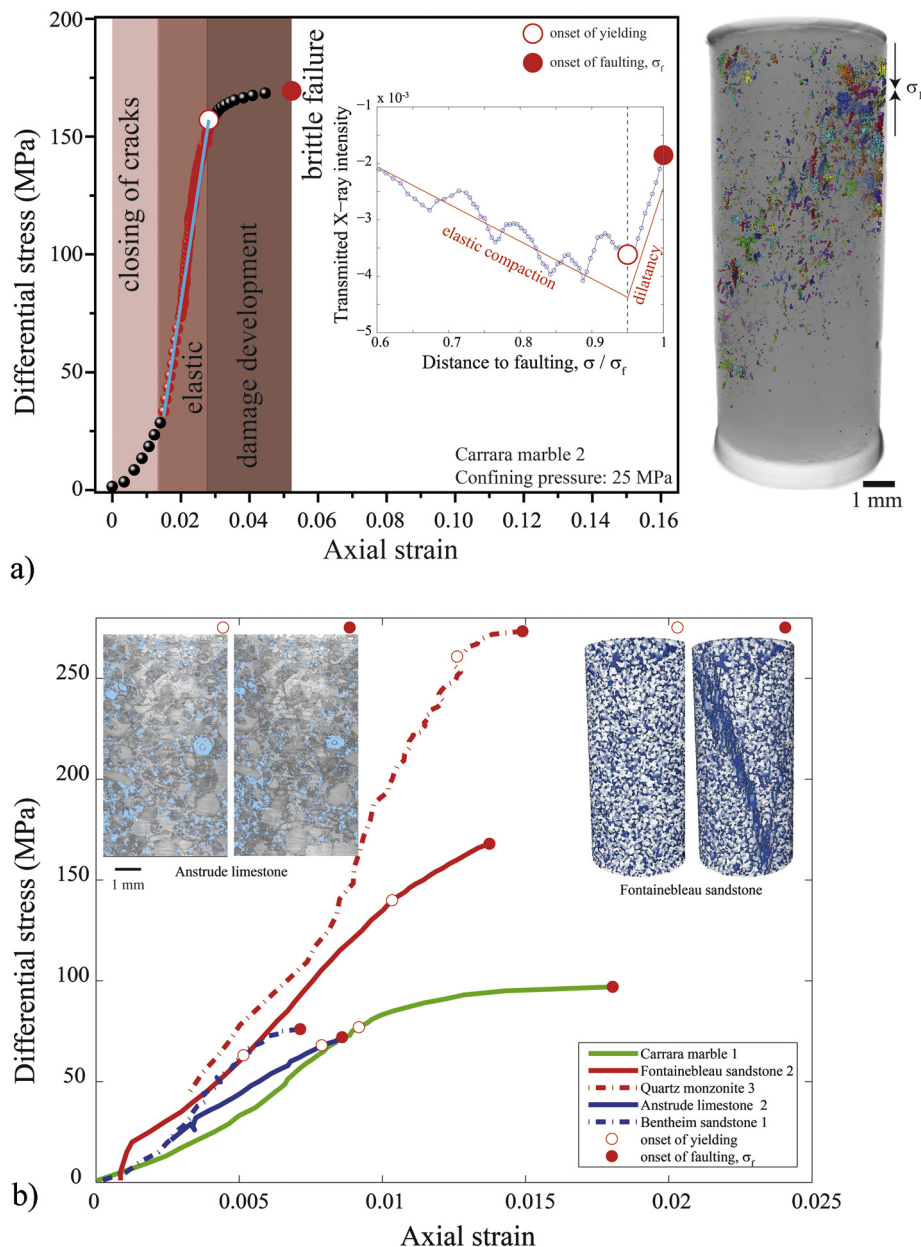
In the Earth's crust, faulting and fault rupture release a significant part of the elastic strain energy that accumulates due to tectonic loading, gravitational relaxation, and industrial activities such as underground fluid injection and extraction. The existence of precursory signals (Jones and Molnar, 1979; Ellsworth and Beroza, 1995; Bouchon et al., 2011; Kato et al., 2016) to such ruptures is a very old problem and it may provide the key to failure forecasting (de Arcangelis et al., 2016). Variations of geophysical or geochemical signals have been reported before major earthquakes (Ellsworth and Beroza, 1995; Bouchon et al., 2011), volcanic eruptions (Kato et al., 2015), and cliff collapses (Amitrano et al., 2005), however they are not ubiquitous and vary with geological settings (Bouchon et al., 2013). The occurrence of small seismic events weeks to hours before a major earthquake (Kato et al., 2016) has been interpreted in terms of small seismic or aseismic slips along the fault plane (Guglielmi et al., 2015). The distribution of microearthquake

magnitudes in the foreshock area may also vary before an earthquake or a volcanic eruption with a change in Gutenberg–Richter frequency–magnitude *b*-value (Sugan et al., 2014) interpreted as related to high stress concentration, dilatancy in the fault zone, and propagation of fractures. Geochemical proxies, such as the concentration of radon gas in soils (Hauksson, 1981), and sulfate and chloride anions in spring waters (Tsunogai and Wakita, 1995; Toutain et al., 1997) have been observed to increase days before an earthquake (Wakita, 1996). These events are thought to be caused by the opening of cracks preceding dynamic faulting that provide paths for the migration of these chemical species towards the surface. Even when such precursory signals have been detected, their amplitude varies spatially, their existence is not ubiquitous, and the physical processes that enable migration from depth to the surface cannot be observed directly. Here, we present experimental evidence of the nucleation and propagation of such precursory deformations at the microscale. We show how small variations of porosity self-organize prior to a catastrophic failure and how their dynamics varies between different rock types, allowing the identification of different paths to fault initiation.

Small deformations preceding a large rupture are detected in both field and laboratory studies. Field observations are per-

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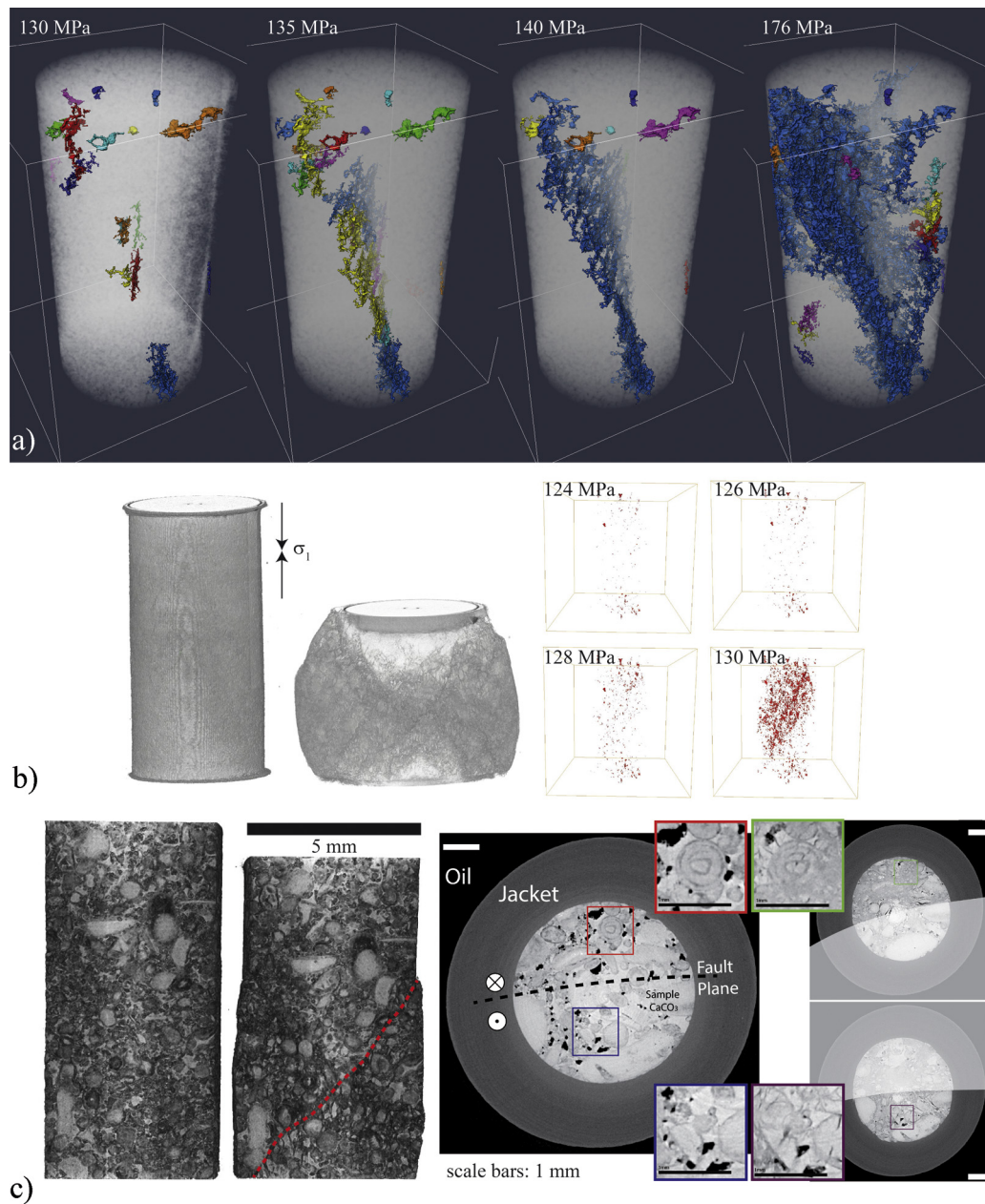
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**Fig. 1.** Stress–strain relationships and damage development prior to faulting. a) Stress–strain curve for a Carrara marble sample deformed at 25 MPa confining pressure. For each differential stress increment a 3D volume was imaged. At low stress, some microfractures initially present in the sample closed. Then, as the axial stress was increased, the sample deformed elastically with a more-or-less linear relationship between strain and stress. At the yield point (empty circle), irreversible deformation occurred, and the curve became non-linear, until faulting occurred (solid circle). The inset shows the corresponding X-ray absorption signal, with an increase of intensity as damage (i.e. porosity) developed towards faulting. On the right hand side, the sample is viewed in 3D with all individual damage events at the onset of faulting. b) Stress–strain curves of representative rocks deformed until faulting. Insets show 3D views of a Fontainebleau sandstone and 2D views in the middle of an Anstrude limestone at the onset of yielding and onset of faulting, respectively. Void spaces are shown in blue. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

formed using seismometer and GPS networks located at the surface of the Earth, several kilometers away from the earthquakes hypocenters. In laboratory, acoustic emissions of damage prior to failure has been recorded and analyzed (Lockner et al., 1991; Zang et al., 2000; Schubnel et al., 2007; Benson et al., 2008). However, a limitation of acoustic emission damage characterization comes from the low spatial resolution of source location, particularly in heterogeneous rocks. To date, few direct in-situ 3D images of such damage processes have been obtained at the scale of whole rock samples, and most have been obtained under shallow depth stress conditions (Lenoir et al., 2007; Hall, 2013; Zhu et al., 2016).

Using a state-of-the-art triaxial deformation apparatus (Renard et al., 2016) that is transparent to the high flux of X-rays produced by a synchrotron, we studied the microscale damage evolution in rocks as they were driven towards brittle failure by increasing the differential stress at constant pressure confining pressure. Because the adsorption of X-rays depends on the local density of the solid, the evolution of microscale damage in the forms of microfracturing and pore-collapse during deformation can be monitored in 3D in centimeter-size core samples with a spatial resolution of 6.5  $\mu\text{m}$ , as the differential stress is increased under stress conditions at depths of several kilometers (Fig. 1). The time-resolved 3D images document the interplay of a variety of deformation mechanisms and the



**Fig. 2.** Development of damage and faulting in various rocks visualized by in-situ X-ray microtomography. a) Development of a shear fracture into Fontainebleau sandstone with differential stress increasing by steps of 1 MPa from 130 MPa (left) to 176 MPa (right). The confining pressure was 10 MPa. The rock is shown in a translucent white color and the largest connected fractures are shown in various colors. b) Carrara marble at a confining pressure of 20 MPa before (left) and after (right) faulting. Dilatant behavior due to the pervasive nucleation and growth of microfractures (in red) initiated at the onset of yielding. This damage concentrated onto a band that evolved into a shear fault. c) Deformation of an Anstrude limestone at 20 MPa confining pressure until faulting. 3D view rendering before (left) and after (right) faulting, with the shear fault indicated by the dashed line. 2D slice images in the middle of the sample before (left) and after (right) faulting. Damage was mainly due to the collapse of pores prior to faulting.

corresponding microscale damage leading to faulting (Fig. 2, Video S4–S6). The style and amount of damage determine the variations of the bulk density and acoustic wave velocities of rocks as they approach faulting.

## 2. Material and methods

Several cylindrical cores, 4 or 5 mm in diameter and 10 mm in length, were taken from larger blocks of Carrara marble, Adamswiller sandstone, Fontainebleau sandstone, quartz-rich monzonite, Bentheim sandstone, and Anstrude limestone, with initial porosities in the range 0.5–19% and grain sizes in the range 0.1–0.7 mm. These rocks were chosen because they cover rock

types from compact crystalline to porous siliciclastic and carbonate rocks. Some of them have very homogeneous composition, e.g., almost pure calcium carbonate for the marble and limestone and almost pure quartz for the Fontainebleau sandstone. Most of them contain strong heterogeneities (i.e., polymineralic grains) and pores, one to two orders of magnitude smaller than the dimensions of the core samples.

Experiments were conducted using an X-ray transparent tri-axial deformation apparatus which enables the confining pressure (0–100 MPa), differential stress (0–200 MPa), temperature (25–250 °C), and fluid pressure (1–100 MPa) to be controlled independently (Fig. S1). The deformation apparatus, HADES (Renard et al., 2016), is installed on an X-ray microtomography rotation stage



**Table 1**

Rock sample characteristics and experimental conditions.  $\emptyset$ : sample diameter;  $P_c$ : confining pressure;  $Y$ : yield stress,  $\sigma_f$ : differential stress at faulting,  $E$ : Young's modulus,  $\phi_i$ : initial porosity. The number of 3D tomography volumes acquired during each experiment is given.

Sample #	$\emptyset$ (mm)	$P_c$ (MPa)	$Y$ (MPa)	$\sigma_f$ (MPa)	$E$ (GPa)	$\phi_i$	Nb. 3D scans
Quartz monzonite 3	4	20	261	273	22.6	0,13%	72
Fontainebleau sandstone 2	5	10	150	168	15.2	11%	47
Carrara marble 1	5	20	77	97	11.4	0,44%	45
Carrara marble 2	5	25	128	148	14.2	0,15%	97
Anstrude limestone 2	5	20	68	72	8.4	16%	41
Anstrude limestone 3	5	5	34	38	5.6	16%	26
Anstrude limestone 4	5	20	54	65	4.5	16%	55
Anstrude limestone 5	5	5	44	51	3.6	16%	27
Adamswiller sandstone 1	5	30	111	133	12.9	13%	57
Bentheim sandstone 1	5	5	63	76	16.5	19%	78

at beamline ID19 at the European Synchrotron Radiation Facility in Grenoble, France. During each deformation experiment, the apparatus is rotated over 180° and 1800 X-ray radiographs can be acquired with a voxel size of 6.5  $\mu\text{m}$  and estimated beam energy of 90 keV.

The experimental conditions are given in Table 1. All samples were deformed following the same procedure. First, a sample is compacted hydrostatically by increasing the axial stress and confining pressure equally. Once the hydrostatic confinement reaches a preset value ( $P_c$ , see Table 1), the first X-ray tomography scan was performed to obtain the initial state of the sample before deformation starts. Then, while keeping the confining pressure constant, the axial stress was increased by increments of 5 MPa at the beginning, and then by 2 or 1 MPa when the differential stress exceeds 50% of the shear strength of the sample. After each stress increment, a 3D X-ray microtomography scan was acquired at constant stress, until the sample failed by shear faulting. Each step of stress increase lasted for 1–2 min, and each tomography scan lasted for 3 minutes. The experiments were performed at room temperature and under nominally dry conditions. The reconstruction of the 3D volumes from the radiographs was performed at beamline ID19 at the ESRF, using both X-ray adsorption and phase contrast imaging (Mirone et al., 2014). Time resolved 3D volumes of the whole sample were acquired for each deforming rock.

The stress–strain curve was plotted for each sample by measuring, on the 3D microtomography images, the shortening of the rock core with increasing differential stress (Figs. 1b, S2). The 3D volumes were analyzed using the software Avizo™ to extract both the solid phase (grains) and the voids (porosity, microfractures) from the X-ray images obtained during each experiment. Because the gray levels of the pore space and of the solid grains were well separated (Fig. 3), only a simple procedure was needed to extract the void space. First, the 3D volumes were denoised based on a non-local averaging of all pixels in the image (non-local means filtering technique described in Buades et al. (2005)). Then, a gray level threshold was applied to separate the empty voids from the solid matrix. The same threshold was applied to all the 3D volumes of a given experiment and all individual voids were extracted. The processed data contained the position, volume, and surface area of each individual void (microfracture or pore). Consequently both changes in voids volume and surfaces area, as well as the creation of new voids can be determined after each stress increment. To test the effect of the choice of the threshold during the void segmentation procedure, several thresholds around the minimum of the histogram (a gray level of 7750 in Fig. 3), were used. The relationship between the damage index (see section 3.2 below) and the distance to faulting varied only moderately if the segmentation threshold was varied slightly, as Fig. 4 illustrates for the Bentheim sandstone.

This technique of high resolution in-situ imaging is novel and complement existing imaging techniques in rock physics such as

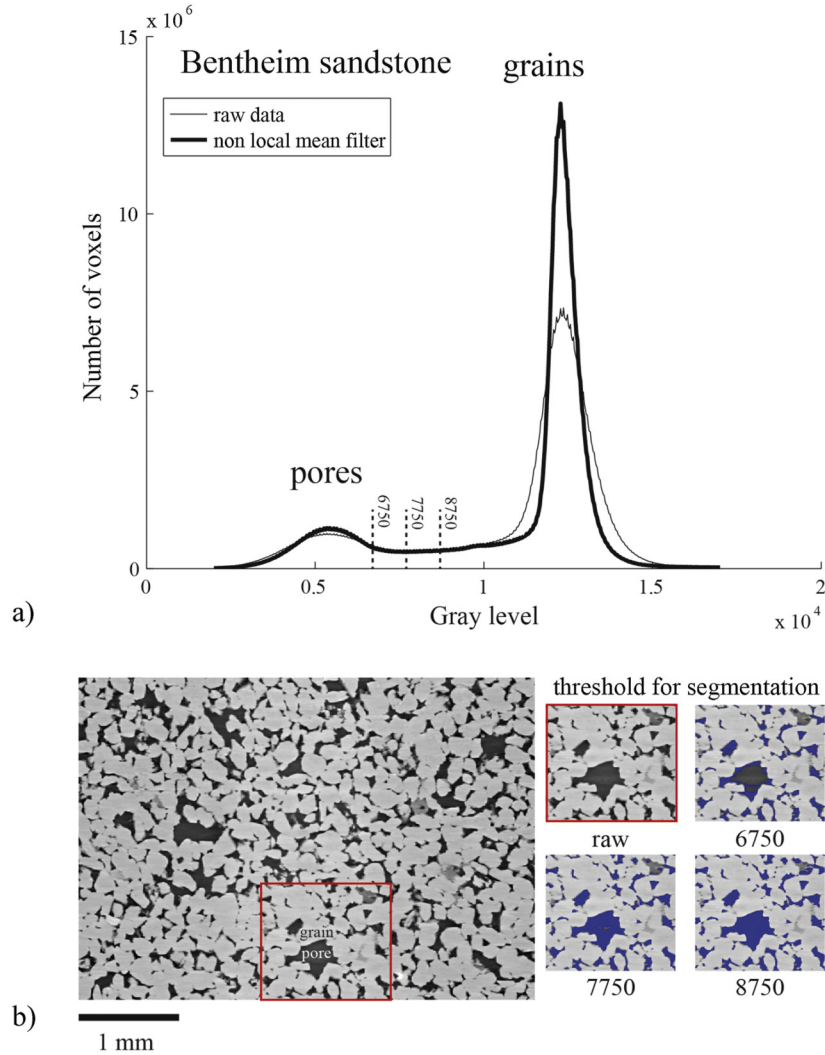
imaging from acoustic emission locations and ultrasonic velocities. With an acquisition time close to one minute, X-ray microtomography is still not quite fast enough to capture the very quick coalescence of microfractures observed by Lockner et al. (1991). However, the dynamic imaging presented here allows understanding 3D porosity development, crack anisotropy and the role of heterogeneities in general at the scale of a whole sample.

### 3. Results

The failure mode of rocks changes from brittle faulting in the seismogenic Earth's crust to mainly ductile flow at larger depths, as pressure and temperature increase (Paterson and Wong, 2005). In the brittle faulting regime, laboratory experiments have demonstrated that the deformation behavior preceding shear failure can be characterized by three stages: i) a non-linear regime at low stress related to the closing of pre-existing cracks or pores, ii) a linear elastic regime at moderate stress, followed by iii) a non-linear regime above a yield point related where irreversible deformations at scales smaller than that of the sample size (i.e., microscale damage) play an important role. During this last phase, damage increases and precursors can be detected in the tomography data (Fig. 1a). Then, the rock breaks at a failure threshold  $\sigma_f$  along a macroscopic fault that relaxes part of the remaining stress. This sequence of mechanical behaviors occurred for all the rocks deformed in this work (Figs. 1b, S2).

#### 3.1. Three modes of failure

Three modes of failure characterize the evolution of damage with increasing stress in the various rocks. In the first mode, observed in both the Fontainebleau sandstone (Figs. 1b inset, 2a), a porous siliciclastic rock, and the quartz monzonite, a compact crystalline rock, microfractures opened initially at grain boundaries or within grains. These microfractures initially opened as mode I cracks, parallel to the main compressive stress. They aligned predominantly along a well-defined plane with a mean angle of inclination at around 30° with respect to the direction of the maximum compressive stress,  $\sigma_1$  (Fig. 1). Linkage of these microfractures formed a finite size fault (Lockner et al., 1991; Zang et al., 2000). Near the fault tip, a high density of microfractures was observed within a small volume whose size is of the order of the grain size of the rock. This observation is consistent with the development of a finite-sized process zone (Bažant and Kazemi, 1990), also referred to as a damage zone or plastic zone. In the second mode of failure, represented by the Carrara marble, a rock with almost no porosity and composed of nearly 100% calcite, microfractures initially appeared indiscriminately and pervasively throughout the rock. Multiple parallel shears develop and spread across the sample, and at a late stage conjugate shears developed. As the sample approached failure, the microfractures clustered along a localized

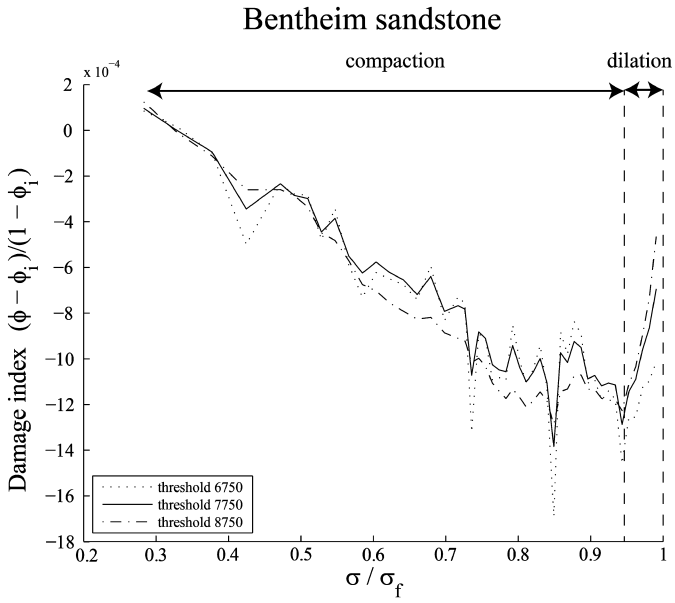


**Fig. 3.** a) Histogram of X-ray gray levels in a Bentheim sandstone sample with raw (thin line) and denoised (thick line) data. The two peaks correspond to pores and grains, respectively. The three thresholds used to perform the segmentation for the data of Fig. 4 are indicated. The minimum of the histogram corresponds to the gray level value of 7750. b) 2D slice of the Bentheim sandstone and effect of three different gray level thresholds on the segmentation of the pore space.

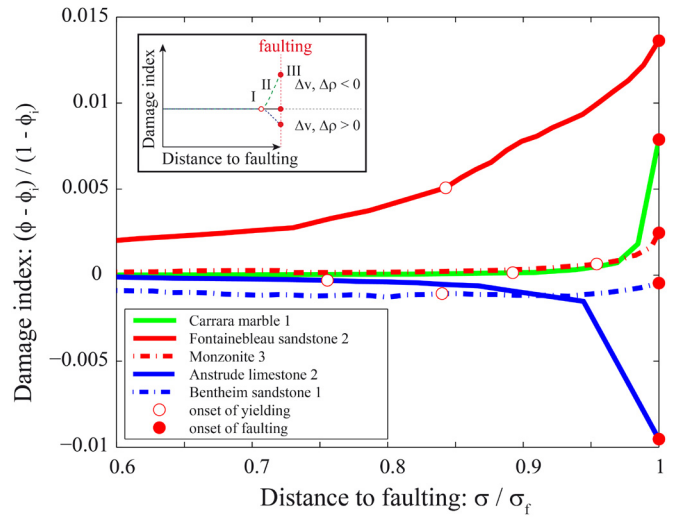
shear band oriented at around  $30^\circ$  with respect to  $\sigma_1$  that subsequently coalesced into a rupture plane (Figs. 1a, 2b). The sample failed by symmetric bulging in the middle by shearing on both sets of shear planes. This is classical cataclastic failure, and is typical of such ductile rocks as marble. The main difference between the first two modes of failure is that for the first one the damage extends at the fault tip only (Video S4), whereas for the second modes microfractures nucleate pervasively in the volume before localization of a fault (Video S5). The third mode of failure was observed in highly porous rocks, including Anstrude limestone (Figs. 1b inset, 2c, Video S6), and Adamswiller and Bentheim sandstones. At the onset of yield in these rocks, the microscale damage is controlled by the interplay between two competing processes: on the one hand microfractures cause dilatancy, on the other hand the closure of preexisting pores leads to compaction. As a result, a net volume decrease was observed before failure in both the Anstrude limestone (Fig. 5) and Bentheim sandstone, whereas no significant macroscopic density variation was measured for the Adamswiller sandstone (Fig. S3). This is the typical behavior of high porosity rocks (Zhu et al., 2010). At the field scale, shearing occurs by the formation of deformation bands, which are compaction features (Aydin and Johnson, 1978) rather than by dilatant cracks or faults. The deformation of such highly porous rocks in laboratory experiments differs as well (Mair et al., 2000).

### 3.2. Evolution of damage prior to failure

The three modes of failure presented above suggest that, for similar stress–strain relationships, the evolution of damage during fault nucleation and propagation can be markedly different even though the stress–strain relationships are similar. This can be quantified by defining a damage index  $(\phi - \phi_i)/(1 - \phi_i)$ , where  $\phi$  is the porosity of the sample at a given stress and  $\phi_i$  is the initial porosity of the undeformed sample. This index is positive for dilation and negative for compaction. It measures the magnitude of the porosity variations compared to the initial porosity. It can be calculated directly from the 3D microtomography data from which the voids can be extracted by a segmentation procedure (Figs. 3, 4). For some samples, the damage index increased as microfractures or a main fault nucleated and grew with increasing loading, for other samples it remained constant or even decreased when pore collapse occurred (Figs. 5, S3). When  $\sigma_f$ , the stress at faulting, was approached (Fig. 5), the damage index varied differently depending on the rock type. For Carrara marble, the acceleration of damage towards rupture followed a power-law singularity  $\frac{\phi - \phi_i}{1 - \phi_i} \sim (\frac{\sigma_f - \sigma}{\sigma_f})^{-\nu}$  with  $\nu \approx 2$  (Fig. 6), in line with the proposition that rock brittle failure and earthquakes could be related to the establishment of long range correlations in the stress field, and



**Fig. 4.** Evolution of the damage index towards faulting for a Bentheim sandstone sample. The deformation is characterized by compaction as the differential stress is increased, and then some dilation when approaching faulting. The three curves correspond to the three thresholds used for segmenting the pore space in Fig. 3 and show the same trend, independently on the choice of the threshold. The minimum of the histogram in the Fig. 3a corresponds to the gray level value 7750.

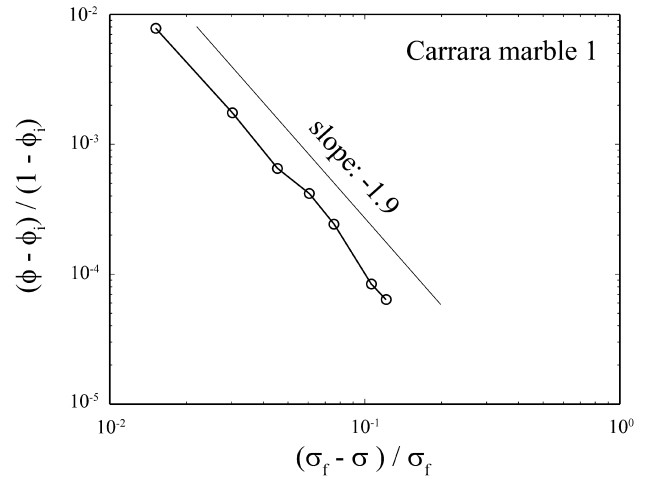


**Fig. 5.** Evolution of damage index as the stress is increased towards the faulting stress  $\sigma_f$ . The damage index can increase, decrease, or remain constant, depending on rock type. Inset: The damage index is the total void volume fraction  $\phi$  relative to the initial value  $\phi_0$  in the rock. When the damage index increases, the density  $\rho$  and seismic velocity  $v$  of the material decrease, and vice-versa. The sketch shows the onset of yielding (I), strain localization (II), and faulting (III).

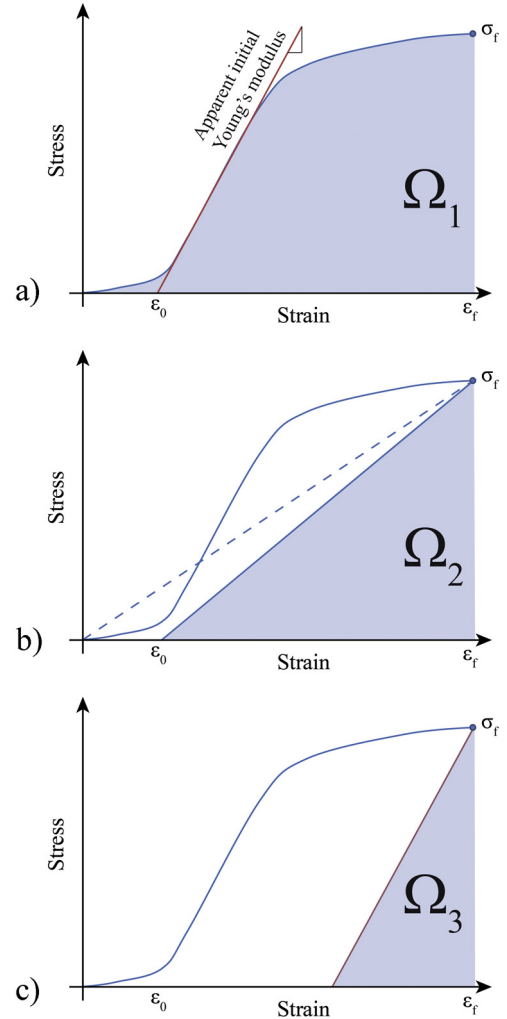
considered as critical phenomena (Jaumé and Lynn, 1999). For the other rocks, the damage index increased, remained constant, or decreased towards rupture (Figs. 6, S3).

### 3.3. Estimation of strain energy dissipation in low porosity rocks

We calculate the strain energy budget for experiments in which rocks with very low porosity (Carrara marble and quartz-monzonite) were loaded until failure. We consider  $E$ , the initial Young's modulus, and  $\varepsilon_0$  the “initial” strain in the absence of initial crack closure (Fig. 7a). We approximate the mechanical work



**Fig. 6.** Evolution of the damage index for the Carrara marble towards failure displayed on a log-log scale. The straight line corresponds to a power law  $\frac{\phi - \phi_i}{1 - \phi_i} \sim (\frac{\sigma_f - \sigma}{\sigma_f})^{-1.9}$  with an exponent of 1.9. Failure occurs when the normalized stress  $(\sigma_f - \sigma) / \sigma_f$  reaches zero. Each circle corresponds to a 3D volume acquired before failure.



**Fig. 7.** Strain energy during the loading phase of each sample. The surface  $\Omega_1$  corresponds to the mechanical work stored in the sample during loading and is the integral of the stress-strain curve. The surfaces  $\Omega_2$  and  $\Omega_3$  correspond to two extreme cases of the recovered elastic strain energy release upon unloading for a purely elastic damaged or a plastic solid, respectively.

**Table 2**

Top: Material parameters ( $E$ : Young's modulus,  $\sigma_f$ : axial stress at failure, SA: surface area of damage at failure,  $\gamma_0$ : surface energy of the rock;  $\varepsilon_0$ : strain when removing the initial crack closure;  $\varepsilon_f$ : strain at failure). Bottom: Estimation of the energy budget in the experiments for three samples (Carrara marble, quartz monzonite). The energy densities  $\Omega_1$ ,  $\Omega_2$ ,  $\Omega_3$  are defined in the Figure 7 and estimations of the ratios between damage due to surface energy and total strain energy due to the loading of the sample are given.

Sample #	$E$ GPa	$\varepsilon_0$	$\sigma_f$ MPa	$\varepsilon_f$	SA $\text{m}^2/\text{m}^3$	$\gamma_0$ $\text{J}/\text{m}^2$
Carrara marble 1	1,1E+01	2,2E−03	9,7E+01	1,9E−02	1,8E+03	5,0E+01
Carrara marble 2	1,4E+01	1,4E−02	1,5E+02	4,3E−02	2,6E+03	5,0E+01
Quartz monzonite 3	2,3E+01	2,0E−03	2,2E+02	1,1E−02	5,2E+02	5,0E+01

Sample #	$\Omega_1$ $\text{J}/\text{m}^3$	$\Omega_2, \varepsilon = 0$ $\text{J}/\text{m}^3$	$\Omega_2, \varepsilon = \varepsilon_0$ $\text{J}/\text{m}^3$	$\Omega_3$ $\text{J}/\text{m}^3$	$\Omega_1 - \Omega_2, \varepsilon = 0$ $\text{J}/\text{m}^3$	$\Omega_1 - \Omega_3$ $\text{J}/\text{m}^3$	$\gamma = \gamma_0 \times \text{SA}$ $\text{J}/\text{m}^3$	$\gamma / (\Omega_1 - \Omega_2)$	$\gamma / (\Omega_1 - \Omega_3)$
Carrara marble 1	1,1E+06	9,3E+05	8,2E+05	4,4E+05	1,9E+05	6,8E+05	8,9E+04	46%	13%
Carrara marble 2	4,1E+06	3,6E+06	2,4E+06	9,8E+05	4,6E+05	3,1E+06	1,3E+05	28%	4%
Quartz monzonite 3	1,3E+06	1,2E+06	1,0E+06	1,1E+06	8,7E+04	2,5E+05	2,6E+04	30%	10%

per unit volume  $\Omega_1$  done to the sample by the axial force up to the stress at failure  $\sigma_f$  by

$$\Omega_1 = \int_0^{\varepsilon_f} \sigma d\varepsilon,$$

where  $\sigma$  is the differential stress,  $\varepsilon$  is the axial strain, and  $\varepsilon_f$  the axial strain at failure. Note that this represents a lower limit of the work, as the diameter of the sample would change during loading and the radial strain would increase  $\Omega_1$  under these confining pressure conditions. To estimate the part of the work that is dissipated irreversibly during loading, two end-member hypotheses can be proposed for the unloading scenario.

In the first hypothesis, the elastic damage case, at  $\sigma_f$  the rock is considered to be a purely elastic but damaged solid, with a Young's modulus lower than the intact rock. As a consequence, upon unloading the strain would come back either to  $\varepsilon = 0$  or  $\varepsilon = \varepsilon_0$  if we neglect the initial crack closure process (Fig. 7b). These two options ( $\varepsilon = 0$  or  $\varepsilon = \varepsilon_0$ ) are only marginally different. To obtain the work converted into damage or heat before failure, one should remove the reversible elastic work  $\Omega_2 = \frac{1}{2}\sigma_f\varepsilon_f$ , or  $\Omega_2 = \frac{1}{2}\sigma_f(\varepsilon_f - \varepsilon_0)$ , from  $\Omega_1$ . The difference ( $\Omega_1 - \Omega_2$ ) corresponds to the irreversible strain energy into the sample from micro-damaging and other dissipation mechanisms.

In the second hypothesis, giving an upper limit on the amount of mechanical work dissipated during loading, we assume that the rock is a purely plastic material at the point of failure and that it acts as a linear elastic material when it is unloaded. Under these circumstances, one can consider an unloading path that would follow the initial Young's modulus  $E$  (Fig. 7c), i.e. the material is undamaged in the elastic sense (no effect on the elastic properties) but has undergone a purely plastic (irreversible) deformation  $\varepsilon_p = \varepsilon_f - \frac{\sigma_f}{E}$ . The associated recovered work  $\Omega_3 = \frac{1}{2}\frac{\sigma_f^2}{E}$  is necessarily smaller than  $\Omega_2$ , and so the dissipated energy ( $\Omega_1 - \Omega_3$ ) is larger. The reality for the dissipated strain energy prior to failure falls necessarily in between ( $\Omega_1 - \Omega_3$ ) (plastic hypothesis) and ( $\Omega_1 - \Omega_2$ ) (elastic damage hypothesis). These various energies for the Carrara marble and the quartz-monzonite, as well as the ratio between the surface energy due to the creation of microfractures and the damage strain energy are calculated in the Table 2.

Because each microfracture can be extracted in the 3D image, the surface area of each of them can be calculated. A cumulated created surface of  $\text{SA} = 2000 \text{ m}^2/\text{m}^3$  is calculated for the Carrara marble at the onset of failure. Considering a specific surface energy of  $\gamma_0 = 50 \text{ J}/\text{m}^2$  for marble (Friedman et al., 1972), a cumulated surface energy per unit volume of  $\approx 100000 \text{ J}/\text{m}^3$  is estimated. For the quartz monzonite, the created surface area is  $520 \text{ m}^2/\text{m}^3$ , the specific surface energy is taken similar to that

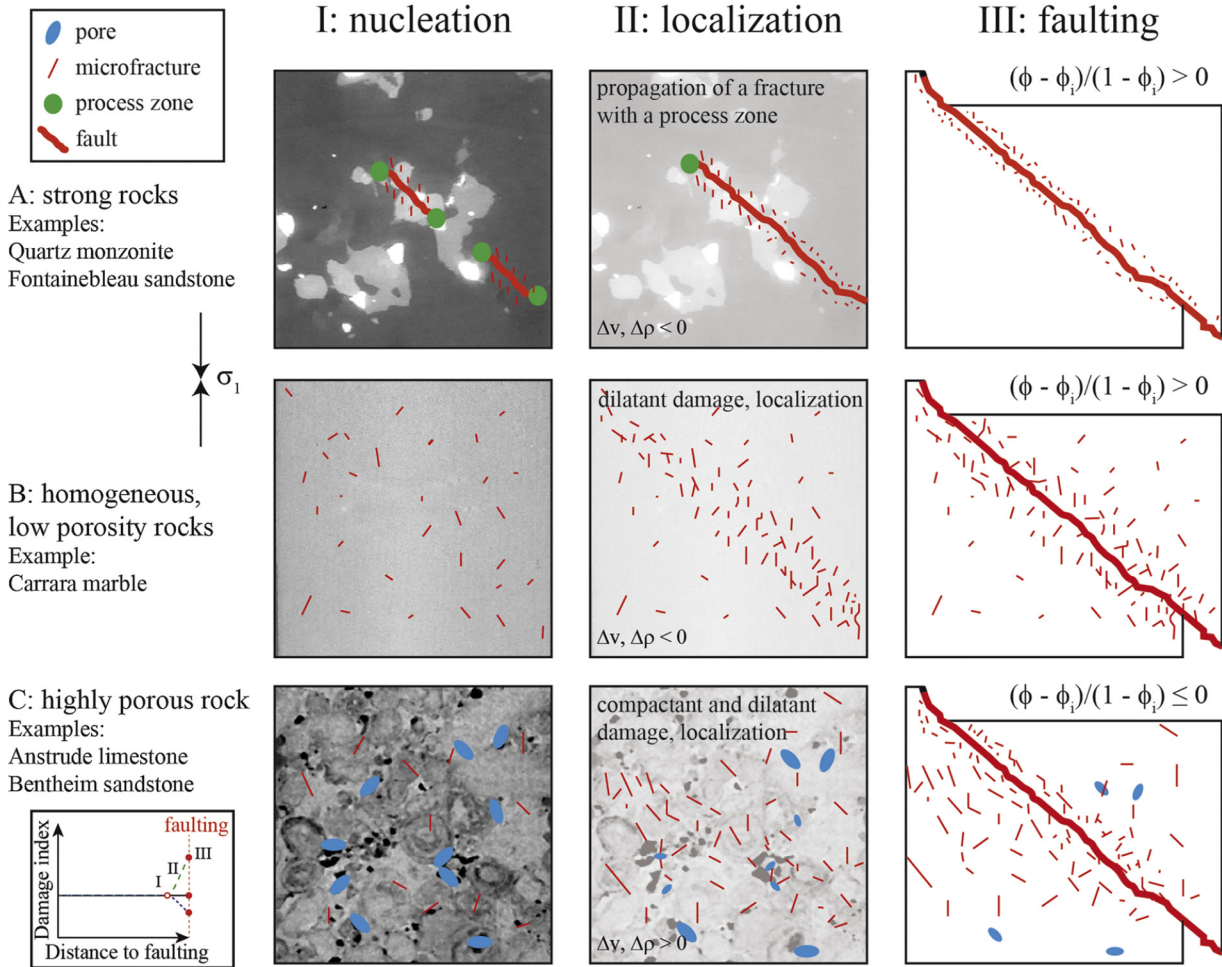
of granite  $\gamma_0 = 50 \text{ J}/\text{m}^2$  (Friedman et al., 1972), and the surface energy per unit volume is close to  $26000 \text{ J}/\text{m}^3$ . These values are always below the net amount of mechanical work converted into other forms of energy, as expected. However, they also mean that a significant percentage of the total dissipated energy ( $\sim 4\text{--}46\%$ ) corresponds to surface energy in the form of surfaces of the microfractures. Note that the estimated created surface area is a lower limit, because fractures with very small aperture widths or diameters may not be detected with a resolution (voxel size) of  $6.5 \mu\text{m}$ , and the diameters of microfractures may be underestimated because of their small aperture widths near their perimeters. The remaining fraction of the irreversible strain energy could be dissipated by damage at scales smaller than the resolution of the images, or by plastic strain, or by heat dissipation by frictional sliding along existing interfaces.

#### 4. Discussion and conclusion

Classical brittle failure criteria, such as the Coulomb's theory of faulting, ignore precursory phenomena, hence implicitly consider failure as a first order transition, in strong disagreement with the observations reported above. As shown in our experiments, the stress change during the microfracture nucleation to rupture transition (between the yield stress and the rupture stress) can be insignificant (e.g., Fig. 1b), and thus the precursory signals associated with microscale damage should be taken into account in failure prediction. In the field and laboratory experiments, acoustic recording of elastic waves produced by microfractures have shown an exponential (Schubnel et al., 2007) or power law acceleration (Jones and Molnar, 1979; de Arcangelis et al., 2016) of activity when rupture is approached. Such irreversible dilation, if it can be monitored during the evolution of a given rock body towards rupture, could explain the increasing flux of chemical species before faulting (Hauksson, 1981; Tsunogai and Wakita, 1995; Toutain et al., 1997).

The main difference between our experiments and a mature fault is the existence of a pre-existing fault gouge and fault core. These have substantially lower strengths than the less-damaged wall rocks. The precursors may well be concentrated on the fault zone itself, particularly within the gouge. In addition, the precursory damage, and the signals associated with it, that do occur prior to large earthquakes may be quite different from the damage and the signals associated with the initial shear failure that occurred far in the past. Conversely, fault healing results in a cohesive re-strengthening (Weiss et al., 2016), and under these conditions, the shear failure of intact rock samples does have important similarities with natural faulting. The dilation and associated enhanced fluid conductivity probably occurs within the faults zone and would depend on pre-existing flow pathways, which are activated as rupture conditions are approached.





**Fig. 8.** Variety of damage dynamics as stress is increased towards faulting. Phases I, II, and III correspond to the nucleation of damage at the onset of yielding, localization (during which rock density  $\rho$  and acoustic waves velocity  $v$  vary), and faulting, respectively. A) Growth of several fractures along a localized plane. At the tip of each fracture some damage develop in the form of vertical cracks. B) Pervasive damage (microfractures, shear bands) localizing onto a single shear plane. C) Interaction between dilatant damage (microfractures, in red) and compaction damage (collapse of pore, in blue) and strain localization along a shear fault. Typical microstructures are shown in the background (A: Quartz monzonite, B: Carrara marble, C: Anstrude limestone). Inset: same as in Fig. 5. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

In the three modes of damage development (Fig. 8), fractures are observed to form pervasively only for the Carrara marble (Fig. 8b) and in the process zone during the development of fractures in the quartz monzonite (Fig. 8a). However, in cases where compaction due to pore closure dominates (Fig. 8c), it is unlikely that new fractures and paths for fluids would form and produce similar precursor signals. Therefore, the type and intensity of precursory signals should depend on the nature of the rock at depth. Because of the complexity of these precursors, it is important to incorporate microscale damage into fracture mechanics models, which provide a framework for linking macroscopic failure phenomena to microscopic deformation mechanisms (Pijaudier-Cabot and Bažant, 1987; Kachanov, 2013; Lyakhovsky et al., 1997; Lyakhovsky et al., 2015).

Microfracturing creates surface area in the rock, and the variation of the corresponding surface energy prior to failure can be estimated. Cumulating over all the voids detected by our tomographic measurements, we calculated the increase of surface area per unit volume prior to failure to be in the order of  $500 \text{ m}^2/\text{m}^3$  for the monzonite and  $2000 \text{ m}^2/\text{m}^3$  for the Carrara marble, given the voxel size resolution of 6.5 micrometer. To relate this with the global energy budget, we calculated the total mechanical work done by the rig on the sample during loading up to failure stress. It falls in the range  $1\text{--}4 \text{ MJ}/\text{m}^3$  for these rocks, and of this

$0.25\text{--}3 \text{ MJ}/\text{m}^3$  is irreversibly dissipated (see Table 2). Indeed, prior to a macroscopic failure, part of the elastic strain energy is dissipated through various mechanisms. The creation of new surfaces from fractures nucleation and propagation represents between 4% and 46% of this energy dissipation. Other dissipation mechanisms such as heat production, plastic strain at the microfractures tips, and microfractures below the resolution of the imaging are also possible. The large amount of strain energy converted into fracture surface area is in favor of an elastic damage scenario in which the formation and propagation of microfractures are important precursors to failure.

The different ways in which damage evolves in different types of rock has implications for the evolution of the velocities of elastic waves in the vicinity of faults. The acoustic wave velocities were not measured directly during our experiments. However, the effect of damage on their amplitude variations can be estimated. Data of Figs. 3 and 5 show that the change in porosity increased as the increasing differential stress drove the rock towards failure, reaching a value of  $\Delta\phi = \pm 0.01$  for most samples at failure stress. Assuming a linear relationship between the compressive acoustic velocity  $V_p$  and porosity,  $V_p$  is equal to  $(V_{p0} - \alpha\phi)$ , where  $V_{p0}$  is the velocity at zero porosity, and  $\alpha$  varies between 3–10 km/s (Mavko et al., 2009). Considering a typical value for  $V_{p0}$  of around 5 km/s and an initial porosity of  $\phi_0 = 0.1$ , with  $\Delta V_p/V_p = -\alpha\Delta\phi/(V_{p0} - \alpha\phi_0)$ ,



the variation of acoustic velocity related to damage is about  $\pm 0.6\%$  at the onset of faulting. This variation represents a minimum because, due to the presence of microfractures oriented parallel to the main compressive stress,  $V_p$  anisotropy is expected to develop in the samples and larger acoustic waves velocities variations are expected (Schubnel and Guéguen, 2013). These variations of acoustic wave velocities are significant at the scale of the experiments. However, to be detected in nature they must occur in a rock volume large enough to be resolved by seismological inversion techniques.

Dynamic microtomography data reveal that rock density can either increase, remain constant, or decrease when shear faulting is approached. These results suggest that seismic, aseismic, and geochemical precursors to earthquakes or rock falls may vary significantly with the tectonic setting. Precursory signals to faulting, such as the amount and amplitude of microfractures, variations of acoustic wave velocity, and opening of fluid flow paths, strongly depend on the rock present at depth, where a competition between microscopic dilation and compaction processes at the grain scale plays an important role in the path to macroscopic failure. Furthermore, in porous rocks, both compaction and dilation precursory events were observed simultaneously at different locations. Scaled to the field, this indicates that, depending on the location of a geophysical or geochemical sensor at the Earth's surface, the nature and amplitude of precursors to faulting could vary spatially.

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## Author contributions

F.R. conceived the research, acquired and analyzed data, and wrote the paper. W.Z. and J.W. contributed to the discussion and manuscript preparation. B.C., M.K., and N.K. acquired and analyzed data.

## Appendix A. Supplementary material

Supplementary material related to this article can be found online at <http://dx.doi.org/10.1016/j.epsl.2017.08.002>.

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