



18 **Abstract**

19 Magnetospheric substorms represent key explosive processes in the interaction of the Earth's  
20 magnetosphere with the solar wind, and their understanding and modeling is critical for space  
21 weather forecasting. During substorms, the magnetic field on the night side is first stretched in  
22 the anti-sunward direction and then it rapidly contracts earthward bringing hot plasmas from the  
23 distant space regions into the inner magnetosphere, where they contribute to geomagnetic storms  
24 and Joule dissipation in the polar ionosphere, causing impressive splashes of aurora. Here we  
25 show for the first time, that mining millions of spaceborne magnetometer data records from  
26 multiple missions allows one to reconstruct the global 3-D picture of these stretching and  
27 dipolarization processes. Stretching results in the formation of a thin (less than the Earth's  
28 radius) and strong (up to  $\sim 6 \text{ nA/ m}^2$ ) current sheet, which is diverted into the ionosphere during  
29 dipolarization. In the meantime, the dipolarization signal propagates further into the inner  
30 magnetosphere resulting in the accumulation of a longer-lived current there ( $\sim 2 \text{ nA/ m}^2$  with a  
31 total strength of  $\sim 2 \text{ MA}$ ), giving rise to a proto-geomagnetic storm. The global 3-D structure of  
32 the corresponding substorm currents including the substorm current wedge is reconstructed from  
33 data.

34 **Plain Language Summary**

35 Using several millions of historical magnetometer records and data mining techniques we form  
36 virtual spacecraft constellations of tens of thousands of spacecraft to reconstruct the global shape  
37 of the terrestrial magnetosphere at the moments of its most dramatic reconfigurations responsible  
38 for major space weather disturbances.

39 **1 Introduction**

40 The magnetic field generated by Earth's core creates a cocoon around our planet called  
41 the magnetosphere, which shields life from the hazardous flow of high-energy particles  
42 emanating from the Sun and carried via the solar wind (McComas et al., 2011). Magnetospheric  
43 plasmas are virtually collisionless, and as a result, the fundamental processes that govern their  
44 evolution, such as magnetic reconnection, may involve microscopic scales comparable to the  
45 electron gyroradius (Burch et al., 2016), which makes their global first-principle description  
46 difficult. At the same time, with the multiple missions that have explored our planet's  
47 neighborhood in the space era, an opportunity arises to create a comprehensive empirical  
48 description of the magnetosphere, and in particular its magnetic field (Tsyganenko, 2013). The  
49 empirical models combine general expansions of the magnetospheric current systems with  
50 physics-based constraints on the global shape of the magnetosphere and the localization of its  
51 main currents. So far, such an approach has been successful for one class of major disturbances,  
52 magnetic storms (Tsyganenko & Sitnov, 2007; Sitnov et al., 2008, 2010, 2018; Stephens et al.,  
53 2016). Storms occur when the interplanetary magnetic field (IMF) orients southward (anti-  
54 parallel to the dayside terrestrial magnetic field) and persists for many hours. The resulting  
55 reconnection between the IMF and the magnetospheric magnetic field directly drives  
56 magnetospheric convection enhancing the near-Earth "ring" current, which is observed using  
57 magnetometers on the surface of the Earth, from which the geomagnetic indices are calculated,  
58 such as the low-latitude *Sym-H* index (Iyemori, 1990). As a result, mining spacecraft  
59 magnetometer data with similar values of *Sym-H* and its trends allows one to reconstruct the  
60 storm picture (Sitnov et al., 2008, 2010, 2018; Stephens et al., 2016).

Unlike storms, substorms were first recognized due to their high-latitude auroral manifestations (Akasofu, 1964) and the corresponding magnetic field disturbances reflected by auroral indices such as the *AL* index (Davis & Sugiura, 1966). They represent another class of space weather phenomena associated with the global reconfiguration of the magnetosphere (Angelopoulos et al., 2008, 2013). Substorms are more transient and less predictable than storms and they may cause substantial damage to satellites (Connors et al., 2011) and ground-based systems (Boteler, 2001). They also inject the seed populations of energetic radiation belt particles that are further accelerated during storms (Reeves et al., 2003; Turner et al., 2015; Baker et al., 2016). Since the beginning of space era, substorms were considered as building blocks of storms (Chapman, 1962; Kamide, 1992; Kamide et al., 1998; Sharma et al. 2013). However, quantitative description of that substorm-to-storm assembling process has remained an unsolved problem for more than half a century.

Even after several recent multi-probe missions aimed to understand substorm mechanisms, such as THEMIS (Angelopoulos et al., 2008) and MMS (Burch et al., 2016), a global quantitative picture of the reconfiguration of the geomagnetic field and underlying electric currents is still missing. Several case studies with fortunate conjunctions of multiple probes (Sergeev, Angelopoulos, et al., 2011; Petrukovich et al., 2013; Artemyev et al., 2016) suggest that substorms often begin with a 30–50-minute period (termed the “growth” phase) where the nightside magnetic field stretches in the anti-sunward direction and the tail current sheet (CS) becomes strong ( $J \sim 10 \text{ nA/m}^2$ ) and thin, with the thickness of a fraction of the Earth radius  $R_E$ , comparable to the thermal ion gyroradius (Runov et al., 2006; Sergeev, Angelopoulos, et al., 2011). Moreover, the thinning process is multi-scale because the thin current sheet (TCS) forms inside of another, much thicker CS. Observations also suggest that during the most active and transient “expansion” phase, the stretched magnetic field becomes more dipolar, which is interpreted as an addition of a downward flowing equatorial current in the near-Earth magnetotail forming a part of a new current system, termed the “substorm current wedge” (SCW) (McPherron et al., 1973). It connects the tail CS with the ionosphere via earthward (downward) field-aligned currents (FACs) on the eastern side of the wedge and tailward (upward) FACs on the western side. This current system, is similar in sense to higher-latitude currents connecting the ionosphere with the distant parts of the magnetosphere and its boundaries, coined region-1 FACs (Iijima & Potemra, 1976) or R1. But it is opposite to the FACs (henceforth called R2) connecting the ionosphere with the westward storm-time current on the night side also known as the partial ring current or PRC (Fukushima & Kamide, 1973). Later, based on magnetohydrodynamic (MHD) simulations (Birn et al., 1999) and observations (Sergeev, Tsyganenko, et al., 2011; Sergeev et al., 2014) it was suggested that the structure of substorm current systems is more complex, and it also includes an additional R2-sense system. Whether the latter becomes a part of the PRC could not be resolved, because MHD models do not describe energy-dependent particle drifts that control storm currents. So far, the empirical reconstruction of substorms was limited to a number of custom-tailored descriptions of the corresponding current systems, such as ad hoc TCS models of the growth phase (Pulkkinen et al., 1991; Kubyshkina et al., 1999) and wire-type SCW models (Tsyganenko, 1997, Sergeev, Tsyganenko, et al., 2011; Sergeev et al., 2014). Thus, the global structure of substorm currents, which is key for understanding their mechanisms (Angelopoulos et al., 2008, 2013), remained a mystery.

Below we present results of an empirical reconstruction of the substorm current systems covering all key phases of this phenomenon within the same data-analysis framework, based on

107 the largest ever set of Earth magnetospheric magnetometer data, a detailed description of  
 108 currents, and advanced data mining algorithms. For the first time, we infer from data the global  
 109 structure and evolution of key substorm elements, the TCS and SCW, as well as a part of the ring  
 110 current accumulated after each substorm that persists in time lengths nearing storm-scales.

111 The following section describes the basic methodology of the empirical reconstruction of  
 112 the substorm magnetic field, including the model structure, data mining procedure, database,  
 113 fitting, and optimization details. In section 3 we present the main results of the reconstruction,  
 114 including thinning and dipolarization of the magnetotail, the evolution of the TCS and  
 115 complementary thick CS, the 3-D SCW, as well as storm-scale currents associated with thick CS.  
 116 The results are summarized and further discussed in section 4.

## 117 2 Empirical reconstruction of the geomagnetic field

118 The complexity of substorms along with the large volumes of data accumulated during  
 119 the space era has motivated us to model substorms by mining data within a system science  
 120 approach (Vassiliadis, 2006), in which their global description, characterized by the *Sym-H* and  
 121 *AL* indices, is used to bin the database of spacecraft magnetic field measurements. The different  
 122 stages of substorm evolution, such as the growth and recovery phases, is reflected in the time  
 123 derivatives of these indices. To capture the spatial structure of the magnetic field, an empirical  
 124 model is employed, whose coefficients are adjusted by fitting the model to data.

125 A fundamental tradeoff when developing an empirical model is balancing model  
 126 complexity with data availability. For instance, a model with too many degrees of freedom will  
 127 be subject to overfitting, whereas an underfit model will not fully capture the breadth of  
 128 information contained in the data. With this tradeoff in mind, a new class of empirical magnetic  
 129 field models was developed (Tsyganenko and Sitnov, 2007, Sitnov et al., 2008) (henceforth  
 130 termed the TS07D model). The idea was to develop a malleable (as opposed to rigid and hand-  
 131 tailored) model and dynamically bin and fit a subset of the measured magnetic field vectors from  
 132 the database (as opposed to having one universal fit of the model, each moment in time is binned  
 133 and fit separately), thus enabling the reconstruction of the dynamics of the magnetosphere be  
 134 dictated by the data.

135 Below, we first report the model architecture followed by the description of the  
 136 magnetometer database. After this, the dynamical data mining technique is detailed. In particular,  
 137 we will demonstrate how the architecture and data mining have been upgraded to allow for  
 138 empirical reconstruction of substorm current systems and their dynamics.

### 139 2.1 Model Architecture

140 The total magnetic field as measured by spacecraft within the magnetosphere, can be  
 141 decomposed into two primary components, the field due to the Earth itself (internal), and the  
 142 field created by electric currents flowing in space (external):  $\mathbf{B}_{tot} = \mathbf{B}_{int.} + \mathbf{B}_{ext.}$ . The most  
 143 commonly used internal field model in the space physics community is the IGRF model  
 144 (Thébault et al., 2015), and in the context of this work is assumed to be perfectly accurate. The  
 145 goal here is to model the external field. It is further decomposed into different constituents owing  
 146 to the primary magnetospheric current systems, in this model the equatorial, field aligned, and  
 147 magnetopause currents  $\mathbf{B}_{ext.} = \mathbf{B}_{eq.} + \mathbf{B}_{FAC} + \mathbf{B}_{MP}$ .

## 148 2.1.1 Equatorial Field Description

149 The description of the equatorial currents follows the formulation originally developed for  
 150 the TS07D empirical magnetic field model (Tsyganenko & Sitnov, 2007; Sitnov et al., 2008).  
 151 This model diverged from earlier models, where the approach is to describe each equatorial  
 152 current system (symmetric ring current, partial ring current, and tail current) individually using a  
 153 predefined analytical description. In TS07D, these individual modules are replaced by an  
 154 expansion of orthogonal basis functions.

$$\mathbf{B}^{(eq)}(\rho, \phi, z; D) = \sum_{n=1}^N a_n^{(s)} \mathbf{B}_n^{(s)} + \sum_{m=1}^M \sum_{n=1}^N \left( a_{mn}^{(o)} \mathbf{B}_{mn}^{(o)} + a_{mn}^{(e)} \mathbf{B}_{mn}^{(e)} \right) \#(1)$$

155  
 156 The form of these functions comes about as the magnetic vector potential solution to Laplace's  
 157 equation for a thin current sheet, i.e. given  $\mathbf{j}^{(eq)}(\rho, \phi, z) = (j_\rho \hat{\mathbf{p}} + j_\phi \hat{\mathbf{\Phi}}) \delta(z)$  derive  $\mathbf{A}(\rho, \phi, z)$ .  
 158 Using separation of variables, the solution ends up using a combination of sines and cosines for  
 159 the azimuthal dependence, Bessel functions for the radial dependence, and an exponential decay  
 160 function for the  $Z$ -dependence. The magnetic field components can be computed by taking the  
 161 curl of the magnetic vector potential solution. This procedure ensures a divergenceless magnetic  
 162 field. To introduce a thickness to the current sheet, the  $Z$ -coordinate is replaced with  $\zeta =$   
 163  $\sqrt{z^2 + D^2}$ . This broadens the delta profile in height and introduces a characteristic half-thickness  
 164 parameter  $D$ .

165 During the substorm growth phase, a thin current sheet (TCS) develops within the thicker  
 166 magnetotail plasma current sheet (CS), resulting in a magnetotail with two different  
 167 characteristic half-thicknesses. To describe such a configuration, the idea was simply to double  
 168 the aforescribed solution:

$$\mathbf{B}^{(eq)}(\rho, \phi, z) = \mathbf{B}^{(eq)}(\rho, \phi, z; D) + \mathbf{B}^{(eq)}(\rho, \phi, z; D_{TCS}) \#(2)$$

169  
 170 In this expansion the thickness of the main (presumably thick) CS can be arbitrary and it is only  
 171 restricted by the data-fitting procedure, while the TCS thickness has an ad hoc upper limit  $D_{TCS} <$   
 172  $D_0$ , which is taken to be equal to  $2 R_E$  in view of observations (Runov et al., 2006; Sergeev,  
 173 Angelopoulos, et al., 2011) showing that  $D_{TCS}$  is of the order of the thermal ion gyroradius, that  
 174 is,  $D_{TCS} < 2R_E$ .

175 The solar wind compresses the magnetosphere, and its dynamic pressure ( $P_{dyn} = \rho V^2$ ) has  
 176 long been known to correlate with the magnitude of the equatorial magnetic field (Siscoe et al.,  
 177 1968). The first effect is directly built into the model in the construction of the magnetopause  
 178 currents (described below). The latter is accounted for by representing each expansion  
 179 coefficient as a binomial  $a_{mn} \rightarrow a_{mn,0} + a_{mn,1} \sqrt{P_{dyn}}$ , where the square root of the dynamic  
 180 pressure was chosen as the functional dependence.

181 The magnetotail orients its configuration along the Sun-Earth line motivating the use of the  
 182 Geocentric Solar Magnetospheric (GSM) coordinate system. However, closer to the Earth, where  
 183 the field is still approximately dipolar, the field aligns with the dipole axis, prompting the use of  
 184 the Solar Magnetic (SM) coordinate system (Laundal & Richmond, 2017). These two  
 185 coordinates differ by a single Euler angle rotation, which has been termed the dipole tilt angle.  
 186 Thus, to model the magnetic field and the associated magnetospheric current systems, they must  
 187 transition from one to the other. This is accomplished by formulating the current systems  
 188 assuming no dipole tilt as described above and then applying the deformation technique

189 formulated in (Tsyganenko, 1998). This reflects the hinging of the magnetotail, as well as its  
 190 warping and twisting, as described in detail in (Tsyganenko, 1998, 2002). The corresponding  
 191 hinging, warping, and twisting coefficients are free parameters of the model to be obtained from  
 192 the data-fitting procedure. We note, these deformations warp the magnetic equator so that it no  
 193 longer lies in a plane. This can make direct comparisons between different times complex, as  
 194 both the current systems and their dipole tilt deformations change with time. For this reason,  
 195 when plotting the 2-D equatorial panels in equatorial and 3 D distributions described below, the  
 196 deformation has been turned off by setting the hinging, warping, and twisting effects to zero.  
 197 This also aligns the magnetic equator with the equatorial plane.

### 198 2.1.2 Field Aligned Currents

199 The cartoon representation of the FACs describes them as two concentric dawn-dusk  
 200 antisymmetric conical currents flowing into and out of Earth, where the higher and lower latitude  
 201 systems have been termed R1 and R2 respectively. The actual structure inferred from data is  
 202 much more complex even during quiet times (Iijima & Potemra, 1976) and especially during  
 203 substorms (Zou et al., 2009; Murphy et al., 2013). In particular, the Harang discontinuity  
 204 (Harang, 1946) and the SCW, require higher order descriptions to effectively model them. Thus,  
 205 this substorm model utilizes the more flexible FAC module detailed in (Sitnov et al., 2017). The  
 206 local time (azimuthal) dependence of the current density is determined using the first four terms  
 207 of a Fourier series, where the amplitude coefficients are determined when the model is fit to  
 208 magnetometer data. It is noted that the first term ( $A \sin(\phi)$ ) corresponds to the primary dawn-  
 209 dusk antisymmetry, while the second term ( $B \cos(\phi)$ ) introduces a rotation as seen by the  
 210 trigonometric relation:  $A \sin(\phi) + B \cos(\phi) = \sqrt{A^2 + B^2} \sin(\phi + \Delta\phi)$ . The second two terms  
 211 are higher order modes and allow for finer scale local time structure.

$$j(\phi) = A \sin(\phi) + B \cos(\phi) + C \sin(2\phi) + D \cos(2\phi) \#(3)$$

212 The latitudinal dependence is determined by solving the magnetic vector potential  
 213 representation of a thin conical current sheet:  $\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}$  using separation of variables. The  
 214 solution is of the form  $A_r(\phi, \theta) = \sum_{m=1}^N B_m T^{(m)} \sin m\phi$ . The functions  $T^{(m)}$  were found in  
 215 (Tsyganenko, 1991). However, this solution is rather rigid, so a linear combination of these  
 216 modules can be used while still being a solution to the above equation. Two such modules are  
 217 used for both FAC regions that half overlap. The result is a total of sixteen linear coefficients  
 218 (four azimuthal multiplied by four latitudinal) that determine the FAC structure, which is capable  
 219 of reconstructing the Harang discontinuity.

220 To this point, the FACs are described as cones emanating from the origin, so a deformation  
 221 is applied that bends the current sheets along approximately dipolar field lines. An additional  
 222 deformation accounts for the day-night asymmetry, the dipole tilt angle, and a global rescaling of  
 223 the FAC system (Tsyganenko, 2002). The global rescaling parameter allows the FAC currents to  
 224 shift to different latitudes and introduces two additional free non-linear parameters (for R1 and  
 225 R2) that are fit as described below.

### 226 2.1.3 Magnetopause Currents

227 Each magnetospheric current system in the empirical description has its supplementary  
 228 magnetopause (so-called Chapman-Ferraro) current system, which minimizes the internal  
 229 magnetic field outside the magnetopause (Tsyganenko & Sitnov, 2007). The model assumes a  
 230 closed magnetosphere, i.e. the magnetic field does not penetrate the magnetopause. This is

231 accomplished by adding to each of the above fields and the Earth's internal field a  
 232 complementary shielding field  $\mathbf{B}_{sh}$ , which satisfies the condition  $(\mathbf{B} + \mathbf{B}_{sh}) \cdot \mathbf{n}|_s = 0$ , where the  
 233 surface is the modeled magnetopause. The general idea is based on the fact that the  
 234 magnetopause currents do not penetrate inside the magnetosphere. Hence, their magnetic field is  
 235 curl free there and can be derived as a solution of Laplace's equation  $\nabla^2 U = 0$ . The general  
 236 solution can be found from separation of variables and becomes a linear expansion in the chosen  
 237 coordinate system. The coefficients of this linear expansion can be solved by sampling the  
 238 magnetopause surface and then minimizing the r.m.s. normal component of the total field. The  
 239 magnetopause boundary is represented by an analytical function whose form was shown in  
 240 (Tsyganenko, 1995). This functional form was fit to the empirically derived magnetopause  
 241 computed in (Shue et al., 1998).

242 For example, each equatorial expansion was shielded with a cylindrical harmonic  
 243 expansion, see eq. 20 of (Tsyganenko & Sitnov, 2007). The Earth's internal field is a bit more  
 244 complicated, owing to the strong dependence of the dipole tilt. This is solved by splitting the  
 245 scalar potential  $U$  into two independent scalar potentials for the portions of the field parallel and  
 246 perpendicular to the  $X$ -axis:  $U = U_{\parallel} \sin \Psi + U_{\perp} \cos \Psi$ , where the solution for  $U_{\parallel}$  and  $U_{\perp}$  are  
 247 solved using Cartesian coordinates. The FAC is shielded using a similar combination of  
 248 Cartesian solutions, except owing to the even more complicated structure, additional terms are  
 249 necessary to reduce the residuals (eq. 34 of (Tsyganenko, 1995)). Finally, the changes in the  
 250 solar wind dynamic pressure cause the magnetopause to expand and contract in a self-similar  
 251 way (Shue et al., 1998). This effect can be replicated in the shielding currents by scaling the  
 252 position by  $\mathbf{r}'(P_{dyn}) = \left(\frac{P_{dyn}}{P_{dyn,0}}\right)^{\epsilon} \mathbf{r}$ . Here  $\epsilon$  is taken to be 0.155 based on the analysis in (Shue et  
 253 al., 1998).

## 254 2.2 Data Mining Procedure

255 To mine magnetometer records for magnetic field reconstruction, which are most relevant to  
 256 the moment of interest we employ the nearest-neighbor (NN) approach (Mitchell, 1997;  
 257 Vassiliadis, 2006; Wu et al., 2008; Sitnov et al., 2008, 2012). In this approach, the global state of  
 258 the magnetosphere is filled with data records that fall into a small number of  $M$  global  
 259 parameters. These are either derived from geomagnetic indices that reflect specific phases of  
 260 magnetic storms and substorms or from solar wind measurements that act as a driver of the  
 261 magnetospheric dynamics. Then a subset of the historical database to be used to reconstruct the  
 262 magnetic field is determined as a small vicinity around the query point in the  $M$ -dimensional  
 263 space of global parameters.

264 Geomagnetic indices were developed to measure different aspects of geomagnetic activity.  
 265 In this study, the *Sym-H* and *AL* indices are utilized as they are widely considered to be metrics  
 266 of storm and substorm activity respectively (Rostoker, 1972). During storms, charged particles  
 267 become trapped in orbits that encircle the Earth, leading to a predominantly westward flowing  
 268 symmetric ring current. Magnetometers situated at low and mid-latitudes on the surface of the  
 269 Earth observe this current as a magnetic field that is opposite in direction of the main dipole field  
 270 (called the horizontal component or *H*). The *Sym-H* index (Iyemori, 1990) averages six *H*-  
 271 component measurements from mid-latitude magnetometer stations at 1-minute cadence. It is  
 272 analogous with the 1-hour cadence *Dst* index (Rostoker, 1972). However, the magnetopause  
 273 currents also significantly impact the value of the magnetic field at the surface of the Earth  
 274 (Burton et al., 1975). To account for this, the 'pressure-corrected' index is computed to remove

275 the contributions from the magnetopause currents:  $Sym-H^* = A \cdot Sym-H - B \cdot (P_{dyn})^{1/2}$ ,  
 276 where the values of A and B are taken to be 0.8 and 13.0 respectively (Tsyganenko, 1996).  
 277 During the substorm expansion phase, a westward substorm electrojet forms in the ionosphere,  
 278 which translates into a decrease in the observed H-component in magnetometers located along  
 279 the auroral zone in the northern hemisphere. Then the  $AL$  index is derived as the lower envelope  
 280 of these geomagnetic variations at selected (10–13) observatories along the auroral zone. Since  
 281 the substorm electrojet is the dominant ionospheric current during the expansion phase, the  $AL$   
 282 index reflects the level of substorm activity. More discussions on the use of  $AL$  and other  
 283 geomagnetic indices in the global characterization of substorms can be found in (Rostoker, 1972;  
 284 Partamies et al., 2013; McPherron & Chu, 2017).

285 Solar wind quantities have also long been known to correlate with geomagnetic activity  
 286 (Newell et al., 2007, and references therein). Of particular interest is the value of  $vB_{south}^{IMF}$ . Here  
 287  $-v$  is the X-component of the solar wind bulk flow velocity in the GSM coordinate system and  
 288  $B_{south}^{IMF}$  is the southward component of the IMF ( $B_{south}^{IMF} = -B_z^{IMF}$  when  $B_z^{IMF} < 0$  and  $B_{south}^{IMF} =$   
 289 0 otherwise). The quantity  $vB_{south}^{IMF}$  has been shown to be the major driver of storms (Burton et  
 290 al., 1975) and highly correlated with substorms (Blanchard & McPherron, 1995).

291 The storm state of the magnetosphere is determined by smoothing the pressure-corrected  
 292  $Sym-H$  index using a weighted moving average where the weights are defined by a half-cosine  
 293 window function (Sitnov et al., 2012)

$$G_1(t) = \langle Sym-H^* |(t) \propto \int_{-\Pi/2}^0 Sym-H^*(t + \tau) \cos(\pi\tau/\Pi) d\tau \#(4)$$

294  
 295 and its smoothed time derivative is defined as

$$G_2(t) = D\langle Sym-H^* | / D t \propto \int_{-\Pi/2}^0 Sym-H^*(t + \tau) \sin(2\pi\tau/\Pi) d\tau \#(5)$$

296  
 297 which is necessary, in particular, to distinguish between the main and recovery storm phases.  
 298 The averaging constant  $\Pi = \Pi_{st} = 12$  hours (Sitnov et al., 2008) is chosen to eliminate the effects on  
 299 shorter (e.g., substorm) time scales. The notation  $\langle \dots |$  is used to indicate that the window function  
 300 only averages over past data, which prevents the smoothed parameter from being influenced by  
 301 future data, and the notation  $D\langle \dots | / D t$  to reflect that it is not equal to the true time derivative.

302 Similarly, the substorm state of the magnetosphere is determined by the smoothed  $AL$  index

$$G_3(t) = \langle AL | \propto \int_{-\Pi/2}^0 AL(t + \tau) \cos(\pi\tau/\Pi) d\tau \#(6)$$

303  
 304 and its smoothed time derivative

$$G_4(t) = D\langle AL | / D t \propto \int_{-\Pi/2}^0 AL(t + \tau) \sin(2\pi\tau/\Pi) d\tau \#(7)$$

305  
 306 which should distinguish between the growth, expansion, and recovery phases of substorms. The  
 307 corresponding averaging time scale is now  $\Pi = \Pi_{sst} = 2.0$  hours reflecting the typical duration of a  
 308 substorm (Partamies et al., 2013).

309 To take into account the solar wind and IMF input we introduce a fifth global parameter

$$G_5(t) = \langle vB_{south}^{IMF} \rangle \propto \int_0^{\tau_\infty} vB_{south}^{IMF}(t - \tau_\infty + \tau) \exp[(\tau - \tau_\infty)/\tau_0] d\tau \#(8)$$

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311  
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with an e-folding time of  $\tau_0=0.5$  hours, based on the duration of a typical substorm growth phase (Partamies et al., 2013). The integration limit is  $\tau_\infty=6\tau$  corresponding to six e-foldings. Thus, the dimension of the binning space is  $M=5$ . Smoothing the parameters serves to eliminate higher frequency oscillations that may be caused by noise and magnetospheric structures on time-scales smaller than substorm time-scales.

316 Then the NN vicinity of the query point  $\mathbf{G}^{(q)}=\{G_1^{(q)}, \dots, G_5^{(q)}\}$  is determined by the distance  
317  $R=|\mathbf{G}^{(i)} - \mathbf{G}^{(q)}|$  of the NN points  $\mathbf{G}^{(i)}$ ,  $i=1, \dots, K_{NN}$ , in the 5-dimensional Euclidean space with the  
318 metric:

$$R = \left( \sum_{j=1}^M \delta_j \left( \frac{G_j}{\sigma_{G_j}} \right)^2 \right)^{\frac{1}{2}} \#(9)$$

319 where  $\sigma_{G_j}$  is the standard deviation of the component  $G_j$  (additional factors  $\delta_j$  are implemented to  
320 balance statistical weights of storm and substorm parameters; for example, putting them zero for  
321  $G_1$  and  $G_2$  excludes storm effects from the binning procedure). In this study, all dimensions are  
322 weighted equally, i.e.  $\delta_j=1$ . The number  $K_{NN}$  is chosen to have a sufficiently dense distribution of  
323 measurements for the reconstruction of the spatial structure of the geomagnetic field. On the  
324 other hand, it should be much less than the whole size  $K_{DB}$  of the model database to provide a  
325 sufficient selectivity of the NN method (for example, to distinguish between main and recovery  
326 phases of storms). The number of NNs used so far was  $K_{NN} \sim 10^4 \ll K_{DB}$ . Thus, the binning  
327 procedure based on the NN-approach represents a reasonable trade-off between past statistical  
328 models with  $K_{NN}=K_{DB}$  (Tsyganenko & Sitnov, 2005, and refs. therein) and event-oriented  
329 models with  $K_{NN} \sim 1$  (Kubyshkina et al., 1999).

330 The source of the geomagnetic indices and solar wind data are the 5-minute cadence  
331 datafiles from the OMNI database ([https://omniweb.gsfc.nasa.gov/ow\\_min.html](https://omniweb.gsfc.nasa.gov/ow_min.html)). As such, the  
332 cadence of the magnetic field reconstructions presented below is also 5-minutes.

333

### 2.3 Magnetometer Database

334 The original TS07D model was comprised of data from the Geotail, Cluster, Polar,  
335 Geostationary Operational Environmental Satellite (GOES) 8, 9, 10, and 12, and the  
336 Interplanetary Monitoring Platform (IMP) 8 missions (Tsyganenko & Sitnov, 2007). This set was  
337 chosen as it matches the beginning of continuous solar wind monitoring with the launch of the  
338 WIND spacecraft in late 1994 and included data through 2005. However, in the decade since that  
339 database was developed, Geotail, Cluster, and GOES continued to operate, and new missions  
340 launched, including five Time History of Events and Macroscale Interactions during Substorms  
341 (THEMIS) probes and the pair of Van Allen Probes spacecraft.

342 In constructing the new database, Cluster (2001–2016) and Polar (1996–2006) were  
343 reprocessed and included the newly collected data. In the original database, the four Cluster  
344 spacecraft were averaged into a single data source, but in the new reprocessing, they were treated  
345 as individual spacecraft. IMP-8, Geotail, and GOES 8, 9, 10, and 12 were left unchanged, even  
346 though some of them do have additional data. Incorporating these new data will take place in the  
347 future. The five THEMIS probes, launched in 2007, whose primary science objective is to  
348 resolve the timing, dynamics, and spatial scales of substorms, provided an extremely valuable set

349 of magnetometer data in the magnetotail. In 2010, two of the THEMIS probes, began to change  
350 their orbit eventually becoming Lunar orbiters, thereby becoming the ARTEMIS mission. To  
351 filter out the transition period, the THEMIS data was filtered to exclude data for  $r > 31 R_E$ , which  
352 matches the largest apogee of the THEMIS mission and the primary apogee of the Geotail  
353 mission. This filter was also applied to the IMP-8 and Geotail datasets, as occasionally, the  
354 sparse amount of data beyond  $31 R_E$ , results in anomalous results, presumed to be caused by  
355 overfitting or Gibbs phenomena. The twin Van Allen Probe spacecraft, launched in 2012, have a  
356 perigee of a few hundred kilometers and an apogee of  $5.8 R_E$ , and thus its data populate the  
357 equatorial inner-magnetosphere region that was missing in the original database.

358 Of the original set, only Polar and Cluster had perigees closer than Geosynchronous orbit,  
359 and only Polar had a perigee below  $4 R_E$ . However, due to the large magnitude of the total field,  
360 there was a concern that small attitude errors would make it difficult to distinguish between the  
361 external and internal field and Polar data below  $3.2 R_E$  were filtered. This concern was found to  
362 be overly conservative for equatorial spacecraft, as long as special attention was given to remove  
363 anomalous data points, and the new lower bound was changed to  $1.5 R_E$  for equatorial spacecraft  
364 (Van Allen Probes and THEMIS). However, the  $3.2 R_E$  was maintained for polar orbiting  
365 spacecraft (Polar and Cluster), not because of the attitude concern, but rather because of the large  
366 magnitude of the deviation in the field for the low-altitude FACs.

367 The magnetometer database is summarized in Table 1 ( $K_{DB} = 3,589,288$ ). It is also  
368 described and available on the Space Physics Data Facility at the following URL:  
369 [https://spdf.sci.gsfc.nasa.gov/pub/data/aaa\\_special-purpose-datasets/empirical-magnetic-field-370 modeling-database-with-TS07D-coefficients/](https://spdf.sci.gsfc.nasa.gov/pub/data/aaa_special-purpose-datasets/empirical-magnetic-field-modeling-database-with-TS07D-coefficients/). This study represents the first application of this  
371 new database.

372 **Table 1.**

373 Magnetospheric data of the extended set proposed as a basis of this study.

Spacecraft	Number	Period
Cluster 1	288,550	2001—2015
Cluster 2	289,725	2001—2015
Cluster 3	286,787	2001—2015
Cluster 4	225,048	2001—2015
Geotail	131,409	1994—2005
Polar	358,227	1996—2006
Imp8	3,160	1995—2000
Goes-08	233,674	1995—2003
Goes-09	84,951	1995—1998
Goes-10	213,295	1999—2005
Goes-12	79,569	2003—2005
Themis-A	286,382	2008—2015
Themis-B	26,580	2008—2010
Themis-C	42,863	2008—2010
Themis-D	286,592	2008—2015
Themis-E	290,104	2008—2015
Van Allen A	231,965	2012—2016
Van Allen B	230,407	2012—2016

374

375

## 2.4 Fitting the Model and Optimizing its Resolution

376 Now that the model has been formulated and the appropriate magnetometer data selected,  
 377 the next step is to use the data to choose the value of the model's parameters. The model contains  
 378 both linear coefficients and non-linear parameters. The first are found using the standard singular  
 379 value decomposition method for linear regression (Press et al., 1992), the latter, including the  
 380 scaling parameters of the FAC system, hinging, warping and twisting effects of the tail CS, as  
 381 well as its thickness parameters  $D$  and  $D_{TCS}$ , are adjusted using the standard Nelder-Mead  
 382 downhill simplex method, as described in more detail in (Press et al., 1992).

383 Additionally, another complication is that the spatial density of the data is largely non-  
 384 uniform, potentially biasing the fit toward regions of the magnetosphere with a higher density of  
 385 magnetometer data points, such as geosynchronous orbit, where the GOES satellites are located.  
 386 A weighting scheme (Tsyganenko & Sitnov, 2007) is used that lowers.raises the weights in  
 387 high/low density regions. The data is binned by  $0.5 R_E$  radial bins, e.g. one bin is the spherical  
 388 shell consisting of  $5.0 R_E \leq r < 5.5 R_E$ . Each spacecraft contained in the bin is assigned a  
 389 weight,  $w_i = \frac{\langle \Delta N \rangle}{\max(\frac{\langle N \rangle}{5}, \Delta N_i)} \frac{\langle B \rangle}{\langle B_i \rangle}$ . The first part is inversely proportional to the number of data points  
 390 per bin ( $\Delta N_i$ ). The max function caps the maximum weight by preventing extremely  
 391 underpopulated bins from getting a huge weight. The second part is inversely proportional to the  
 392 average field of the points in that bin. This gives higher weights to bins (such as in the tail)  
 393 where the external magnetic field is relatively small, and in unweighted least squares regression  
 394 would have little impact in the target function. Together, these two factors help give the tail more  
 395 influence in the fit than it would otherwise have in unweighted least squares regression.

396 There are several model configuration parameters that can be adjusted. Important are the  
 397 number of equatorial expansions and the number of NNs to be used. In all previous iterations of  
 398 the model reported in the literature (Tsyganenko & Sitnov, 2007; Sitnov et al., 2008, 2010, 2018;  
 399 Sitnov, Stephens, et al., 2017; Stephens et al., 2013, 2016), the number of NNs was set to  
 400  $K_{NN}=8,000$ . This number was rather arbitrarily chosen by assuming that approximate size of the  
 401 modeled magnetosphere is  $20 R_E \times 20 R_E \times 20 R_E = 8,000 R_E^3$ , so approximately one NN per  
 402 cubic Earth Radii. Related to this is the number of azimuthal and radial expansions used in  
 403 modeling the equatorial currents. Adding more expansions increases the potential resolution, but  
 404 if the data density is too low, it risks introducing unphysical artifacts from overfitting or Gibbs  
 405 phenomena. The original expansions were set to  $(M,N)=(4,5)$ . The model was later customized  
 406 by incorporating spacecraft data from the inner magnetosphere (Stephens et al., 2016), allowing  
 407 for an increase in the number of expansions  $(M,N)=(6,20)$ , but the analysis in the study was  
 408 limited to  $r \leq 7 R_E$ .

409 In this study, the original choice of  $K_{NN}$  was revisited. Choosing the number of NNs is a  
 410 tradeoff. A smaller number of NNs ( $K_{NN} \sim 1$ ), leans the fitting towards event-oriented modeling,  
 411 while a large number tends to statistical averaging. Specifically, a challenge here arose in that  
 412 there is a significant decrease in the number of magnetic field measurements beyond  $r \sim 12 R_E$ ,  
 413 which was the apogee for some of the THEMIS spacecraft for the most part of the mission. In  
 414 the model validation presented in below Figure 1, the configuration matched that of (Stephens et  
 415 al., 2016), as the THEMIS-E spacecraft's apogee was  $12 R_E$ , thus enabling a higher resolution.  
 416 But, in order to effectively describe the morphology throughout most of the inner magnetotail,  
 417 i.e. when  $r \leq 20 R_E$ , changes were made to eliminate overfitting in  $12 R_E \leq r \leq 20 R_E$ . First, the  
 418 number of NNs was increased fourfold (8,000 to 32,000), and the number of expansions in the  
 419 equatorial expansion was decreased to  $((M,N)=(6,8))$ . The magnetotail reconstructions presented

420 throughout the rest of the study use this configuration, with the exception of the comparison of  
 421 THEMIS-E magnetometer data with the original and new substorm models presented in  
 422 Figure 1. Here, the density of data located within  $r \leq 12 R_E$  allows for a greater number of  
 423 expansions (M,N)=(6,20) with less NNs  $K_{NN} = 8,000$ .

424 **3 Structure and evolution of substorm current systems**

425 3.1 Thinning and dipolarization reproduced with the new data mining approach and  
 426 compared with in situ observations

427 Figure 1 demonstrates the results of the model application (configured using  $K_{NN} = 8,000$   
 428 and (M,N)=(6,20)) to a large group of substorms during the March 2008 magnetic storm. The  
 429 comparison of the substorm model (red lines) with the baseline storm model TS07D (blue lines)  
 430 shows that, unlike the latter, the new model captures the increase of the magnetic field  $|B_x|$   
 431 measured by the THEMIS-E probe (black lines) that is responsible for the stretching of the  
 432 magnetic field in the growth phase (Figure 1a). Also, it reproduces substorm dipolarization  
 433 signatures seen as sharp positive spikes of the  $B_z$  field (Figure 1c) correlated with the dips of the  
 434  $AL$  index (Figure 1f). Thus, one can expect that the new model will reproduce the main substorm  
 435 current systems and their evolution.

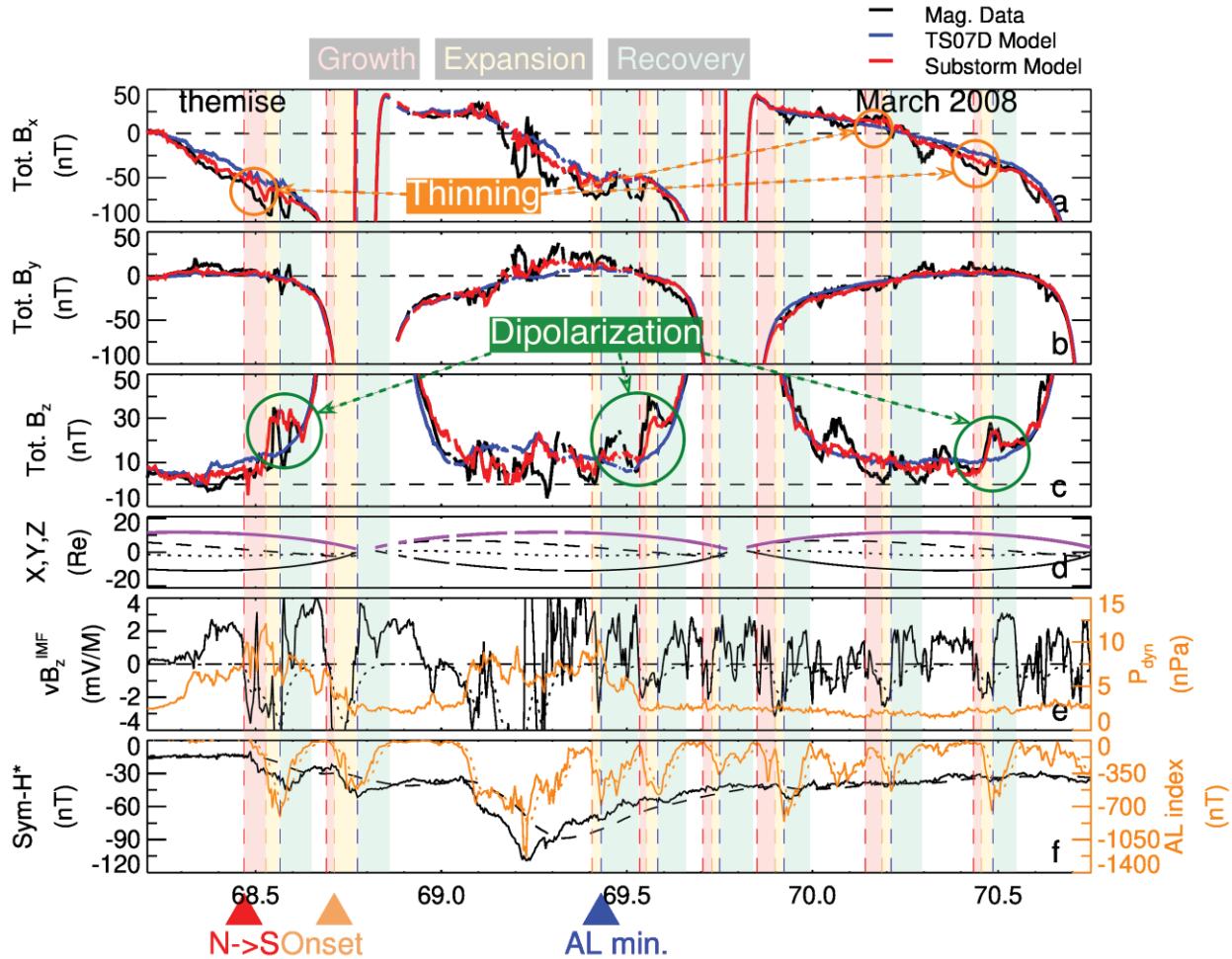
436 For this study, the first point in time prior to the substorm with a southward solar wind  
 437 ( $B_z^{IMF} < 0$ ) defines the start of the growth phase (dashed vertical red line). Substorm onset time  
 438 (dashed vertical yellow line), i.e. the start of the expansion phase, is determined from the  
 439 substorm onset time lists derived from the *SML* index (Newell & Gjerloev, 2011a, 2011b;  
 440 Gjerloev, 2012) and the *MPB* index (McPherron & Chu, 2017). However, these two lists often  
 441 differed substantially or entirely missed substorms observed from visual inspection of the *AL*  
 442 index. For these cases, the onset times are determined by inspection of the SuperMag ground  
 443 magnetometer vector plots. The start of the recovery phase is defined as the minimum of the *AL*  
 444 index denoted by the dashed vertical blue line and the end of the recovery phase is defined when  
 445 the *AL* index either returns to the baseline level ( $AL > -25$  nT) or the next growth phase begins.

446 The definition of storm phases described above may differ from other substorm  
 447 definitions, and in particular, the original notion of the auroral substorm (Akasofu, 1964), as  
 448 discussed, for example in (McPherron, 2016, and refs. Therein). Here we use it mainly to place  
 449 the discussion of our results into the context of the already known history of substorm studies.  
 450 The definition of substorm phases does not affect in any way our data mining and fitting  
 451 procedures. On the other hand, one can expect that the output of the present study can be used to  
 452 improve the definitions of substorm phases and to make them more consistent.

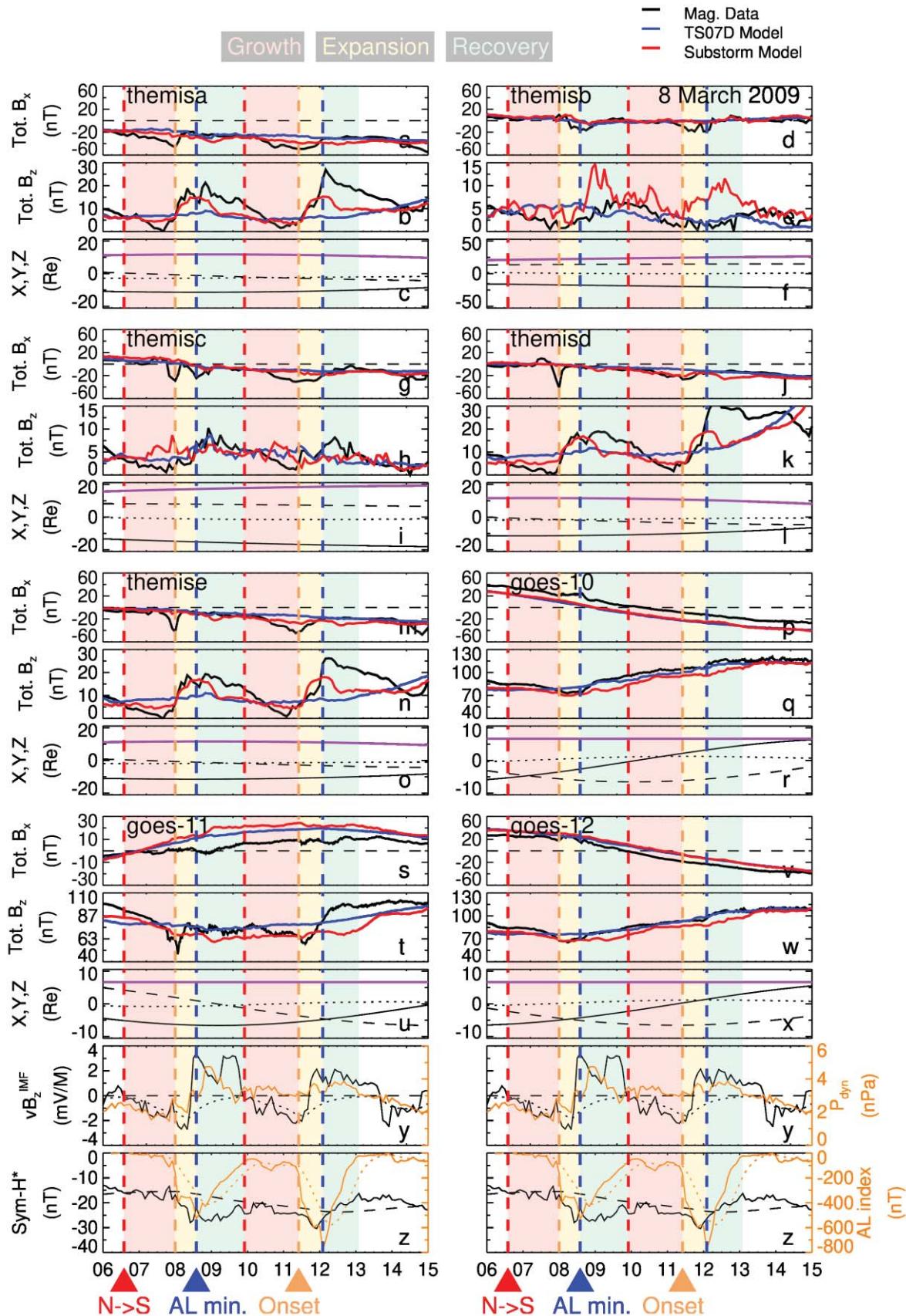
453 The reconstruction accuracy of thinning and dipolarization processes shown in Figure 1 is  
 454 reduced in the midst of the storms, near the *Sym-H* minimum (DOY=69–69.5). The most likely  
 455 reason of this reduction is the significant effects of storm variations expressed by the *Sym-H*  
 456 index in the data mining process, which extends now over the whole 5-D space equations (4)–(8)  
 457 where the distribution of data with the selected  $K_{NN}$  becomes relatively scarce. However, away  
 458 from the *Sym-H* minimum, the use of storm parameters in the binning space is important because  
 459 it allows to separate substorms with different levels of the storm background, and in particular, to  
 460 separate between storm-time and non-storm-time substorms.

461 Figure 2 shows another example of validation using the lower spatial resolution in the  
 462 equatorial plane (M,N)=(6,8), and at the same time, the larger number of NNs in the binning sets

463  $K_{NN} = 32,000$ . In spite of the fact that such changes worsen the validation results (they reduce  $B_z$   
464 dipolarization peaks; thinning in this case is hard to evaluate because the probes are located  
465 relatively close to the plasma sheet), they allow for the use of more virtual probes for the spatial  
466 reconstruction to reveal the generic picture of substorms, which is discussed in the next section.  
467 Figure 2 still clearly shows that the new method reproduces dipolarizations observed by  
468 THEMIS probes A, D, and E (panels (b), (k), and (n)). Validation results for GOES-10 and  
469 GOES-12 shown in panels (p)–(r) and (v)–(x) suggest that the new empirical reconstruction  
470 works well at geosynchronous orbit, although the TS07D model does track  $B_z$  more accurately.  
471 This may not be entirely unexpected, as the TS07D database was comprised of a larger  
472 percentage of GOES data and only included storm-time parameters in the binning procedure. At  
473 the same time, panels (s) and (t) reveal substantial differences with GOES-11 data particularly  
474 during the second dipolarization. The reconstruction of  $B_z$  is reasonable during the growth phase  
475 but is underestimated during the expansion and recovery phases. In regards to THEMIS-B and  
476 THEMIS-C, these spacecraft map to  $r > 20 R_E$  for much of this interval and particularly for the  
477 second substorm, as can be seen in Figures S1–S3. Because these spacecraft were in this  
478 configuration for only about two years before becoming the Acceleration, Reconnection,  
479 Turbulence and Electrodynamics of the Moon’s Interaction with the Sun (ARTEMIS) mission  
480 there is a lack of data in this region. As described above, the model resolution and  $K_{NN}$  number  
481 were chosen to optimize reconstruction in the region  $r \leq 20 R_E$ , thus these spacecraft are largely  
482 beyond the range that the model is expected to perform optimally.  
483



484 **Figure 1.** Key substorm signatures captured by the new data mining technique using a fleet of  $\sim 11,000$  virtual  
 485 spacecraft. Comparison of THEMIS-E magnetometer data with the original and new substorm data mining  
 486 technique for a group of substorms during March 2008 magnetic storm. (a, b, and c) The  $X$ ,  $Y$ , and  $Z$  components of  
 487 the in situ magnetic field measured by the THEMIS-E magnetometer (black line) compared with the model  
 488 evaluated at the spacecraft location, showing the original version of the model (blue line, configured with  
 489  $(M,N)=(6,8)$  and  $K_{NN} = 32,000$ ) and the newly constructed substorm version of the model (red line, configured with  
 490  $(M,N)=(6,20)$  and  $K_{NN} = 8,000$ ). The coordinate system used throughout this paper is GSM. (d) The ephemeris of the  
 491 THEMIS spacecraft where the  $X$ ,  $Y$ ,  $Z$ , and  $R$  components correspond to the solid, dashed, dotted, and purple lines  
 492 respectively. (e) Solar wind measurements; the electric field parameter  $vB_z^{IMF}$  and the smoothed  $vB_s^{IMF}$  parameter in  
 493 solid and dotted black respectively, and the dynamic pressure in orange. (f) Geomagnetic indices; the pressure-  
 494 corrected storm index ( $Sym-H^*$ ) and its smoothed value in solid and dashed black respectively, and the substorm  
 495 index ( $AL$ ) and its smoothed value in solid and dotted orange respectively. The time cadence for these panels and for  
 496 all subsequent plots is 5-minutes.



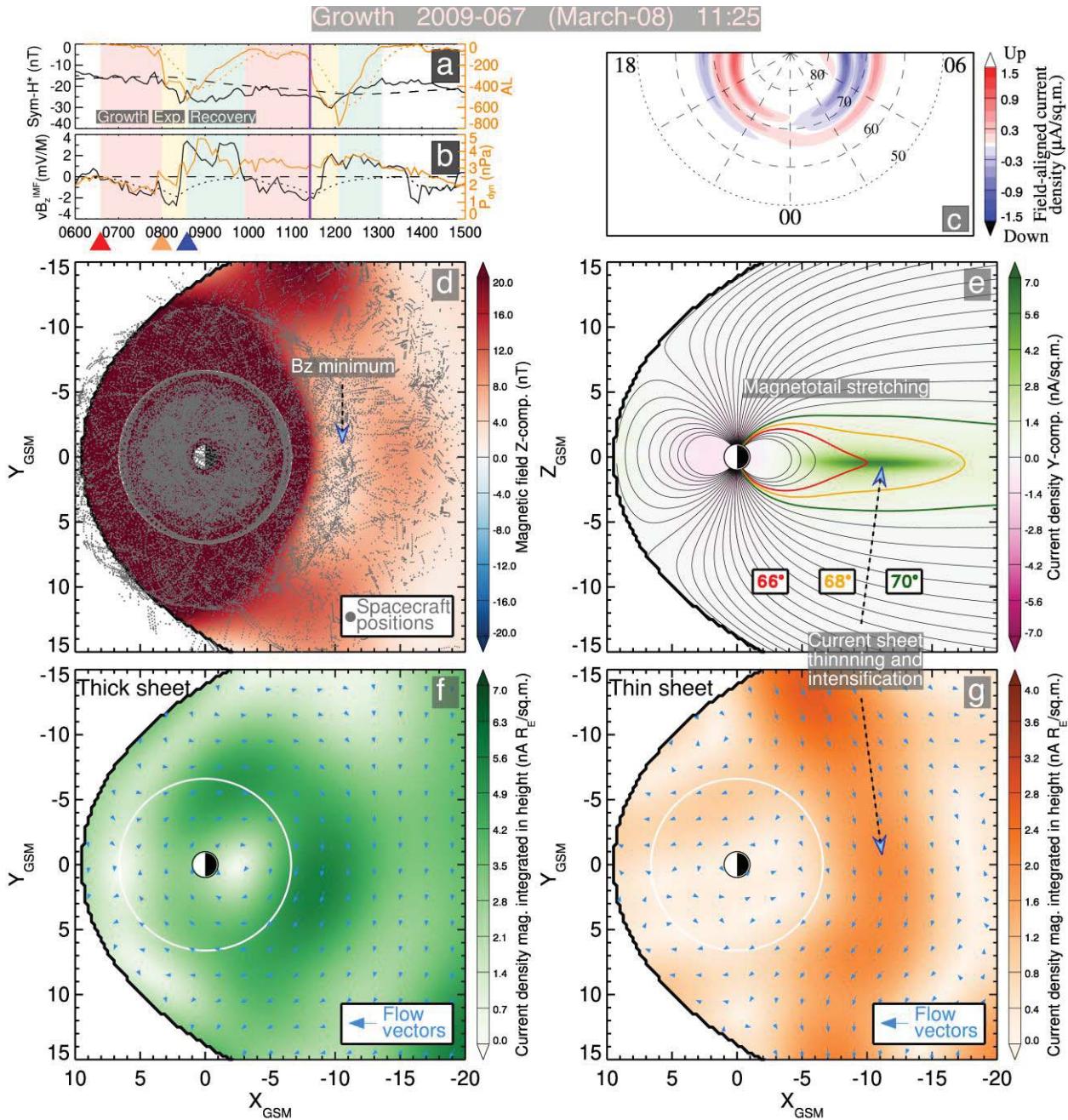
498 **Figure 2.** Comparison of THEMIS and GOES magnetometer data with the original and new substorm data mining  
499 technique for the March 8, 2009 substorms. (a and b) The  $X$  and  $Z$  components of the in situ magnetic field  
500 measured by the THEMIS-A magnetometer (black line) compared with the model evaluated at the spacecraft  
501 location, showing the original version of the model (blue line, configured with  $(M,N)=(6,8)$  and  $K_{NN} = 32,000$ ) and  
502 the newly constructed substorm version of the model (red line, configured with  $(M,N)=(6,8)$  and  $K_{NN} = 32,000$ ). (c)  
503 The ephemeris of the THEMIS spacecraft where the  $X$ ,  $Y$ ,  $Z$ , and  $R$  components correspond to the solid, dashed,  
504 dotted, and purple lines respectively. (d–x) Matches a, b, and c, except for the four other THEMIS spacecraft and the  
505 three GOES spacecraft. (y and z) Solar wind measurements and Geomagnetic indices respectively; similar to panels  
506 (e) and (f) in Figure 1 respectively. Note that in this run, compared to the set of March 2008 substorms shown in  
507 Figure 1, the following parameters have been changed to avoid overfitting in the key region  $12 R_E \leq r \leq 20 R_E$ :  $K_{NN}$   
508 was increased fourfold (8,000 to 32,000), and the number of expansions in the equatorial expansion was decreased  
509 ( $(M,N)=(6,8)$ ).

## 510            3.2 Global distributions of the magnetic field and current in different substorm phases

511            We now focus on the reconstructions of a pair of non-storm substorms, which occurred  
512 on 8 March 2009. The substorm (marked by the *AL* dip in Figure 3a) started after an hour of the  
513 solar wind loading with  $vB_z^{(IMF)} < 0$  (Figure 3b). Its late growth phase is characterized by  
514 formation of a deep ( $\sim 4$  nT) minimum of the  $B_z$  field (Figure 3d), which was derived recently  
515 from particle precipitation characteristics (Sergeev et al., 2018), and a large and strong ( $\sim 6$  nA/  
516  $m^2$ ) TCS providing a stretched tail configuration (Figure 3e). Figures 3f and 3g show the height  
517 integrated current density from the thick CS and the TCS part, respectively. It is seen that while  
518 the TCS occupies the broad local time region outside geosynchronous orbit ( $r \sim 6.6 R_E$ ) and  
519 inside  $r \sim 15 R_E$ , the thick CS is located closer to Earth and in a wider local time region, including  
520 the day side sector. While the traditional picture of magnetospheric currents treats the ring  
521 current and tail current as spatially separated, however, Figure 3f and 3g shows that they form a  
522 single system, whose artificial separation in ad hoc models was rather misleading. The low-  
523 altitude FAC distribution in Figure 3c has the expected spiral pattern.

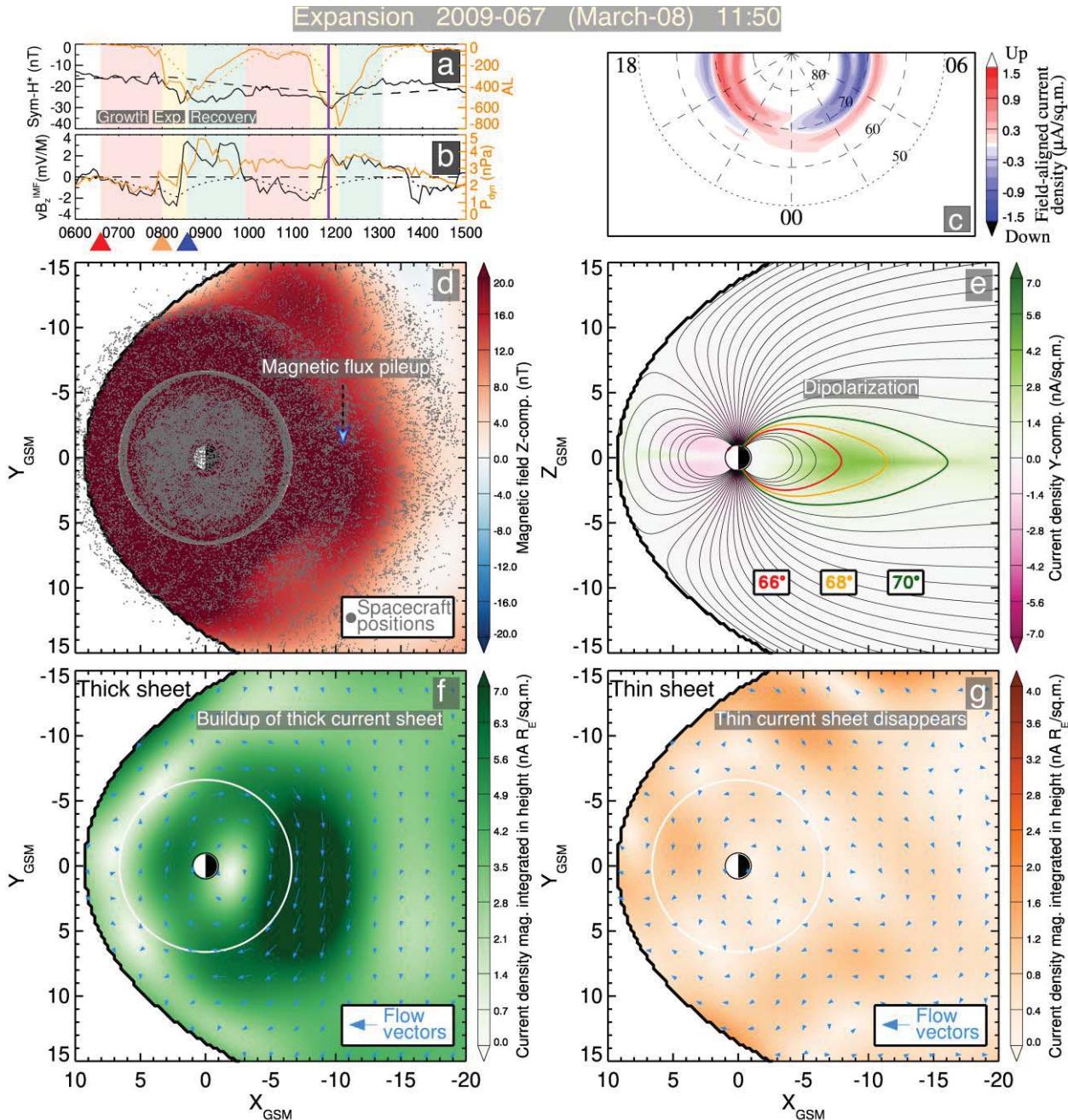
524            In the expansion phase, marked by the rapid decrease of the *AL* index in Figure 4a, the  $B_z$   
525 minimum is replaced by a flux pileup region (Figure 4d), while the TCS disappears (Figure 4g)  
526 or even changes its direction to downward, resulting in the bifurcated structure of the meridional  
527 CS distribution near the neutral plane (Figure 4e,  $X \approx -5 R_E$ ), and providing a substantial  
528 dipolarization of the tail magnetic field highlighted by colored field lines. The  $70^\circ$  field line, that  
529 was open during the growth phase, is now closed indicating a shrinking of the polar cap  
530 boundary on the ionosphere. At the same time, the thick CS becomes greatly enhanced,  
531 particularly in the region  $4 R_E \leq r \leq 12 R_E$  (Figure 4f) occupying a  $\sim 70^\circ$  sector centered about  
532 local midnight. The comparison of Figure 4c with Figure 3c reveals strong enhancement of the  
533 FAC system (both R1 and R2-sense currents), particularly equatorward of the  $70^\circ$  latitude.

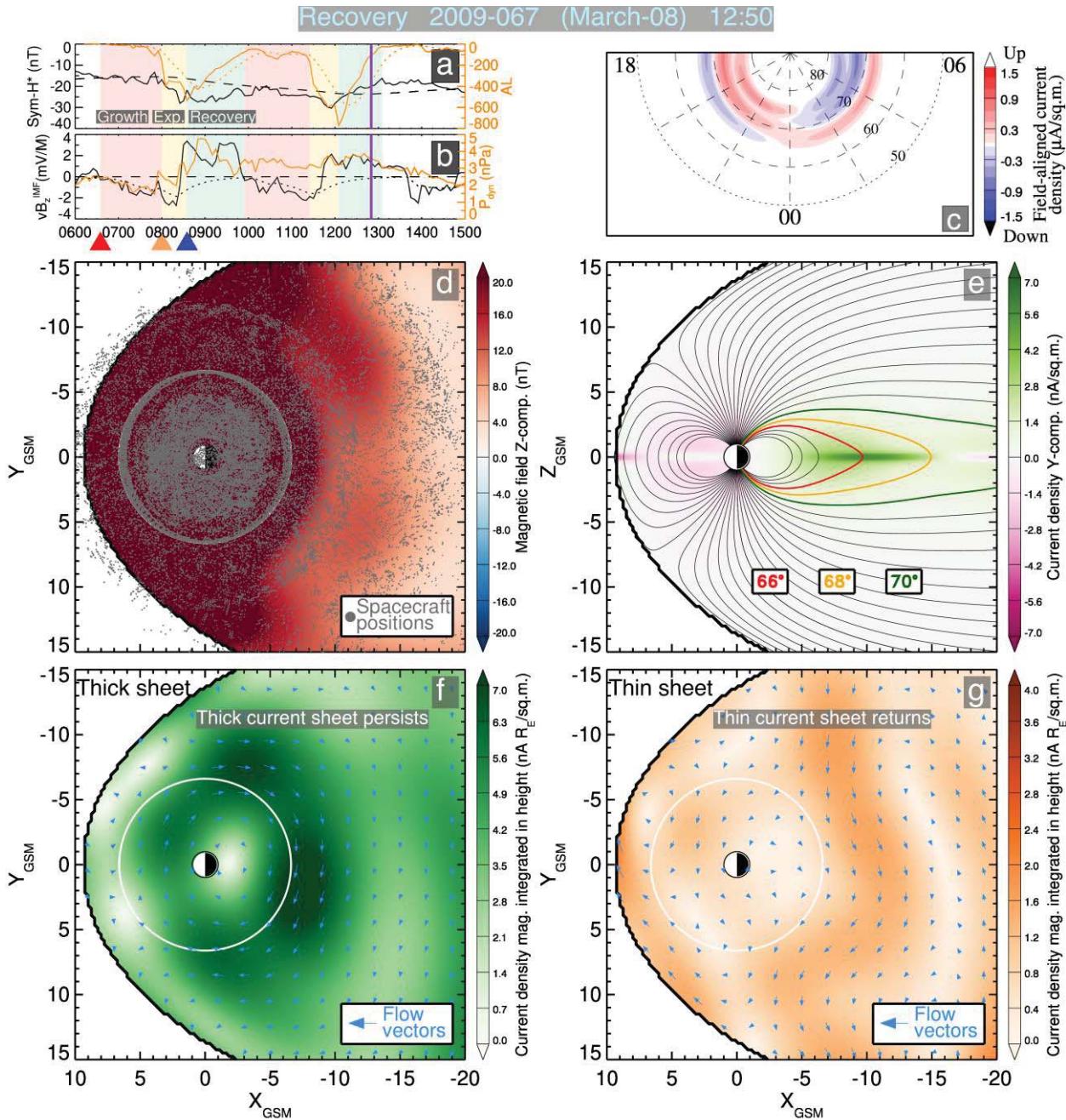
534            In the recovery phase (Figure 5), when the *AL* index increases approaching its base zero  
535 level (Figure 5a), the  $B_z$  field remains enhanced on the night side (Figure 5d) in spite of the  
536 rebuilding of the TCS (Figures 5e and 5g). The most interesting new feature in the empirical  
537 picture of this phase is the persistence of a strong thick CS penetrating deeply inside the  
538 geosynchronous region (Figure 5f).



539 **Figure 3.** Reconstruction of the late growth phase of the March 8, 2009 substorm. Configured with  $(M, N) = (6, 8)$  and  
 540  $K_{NN} = 32,000$  corresponding to  $\sim 5 \cdot 10^4$  virtual spacecraft (a and b) Geomagnetic indices and solar wind  
 541 measurements respectively; similar to panels (f) and (e) in Figure 1 respectively. The vertical purple lines represent  
 542 the moment in time. (c) The FACs flowing into and out of the ionosphere in blue and red respectively. (d) The  
 543 equatorial slice of the total magnetic field with grey circles overplotted representing the locations of the  
 544 magnetometers used to fit this moment. For the equatorial plots, the magnetic equator is forced to be coincident with  
 545 this plane by setting the twisting and warping terms in the model zero. (e) The meridional slice of the  $Y$ -component  
 546 of the current density, green indicates current flowing out of the page and purple into the page. Magnetic field lines  
 547 are overplotted and start from the ionosphere at  $60^\circ$  with  $2^\circ$  step in latitude and with three of the field lines being  
 548 highlighted. (f and g) The equatorial slice of the height integrated magnitude of the current density for the thick  
 549 current sheet (CS) and thin current sheet (TCS) respectively (thick CS is integrated over  $0 \leq Z \leq 5 R_E$  and TCS is

550 integrated over  $0 \leq Z \leq 1 R_E$ ) with arrows overplotted showing the direction and magnitude of the current density  
551 vectors.





555  
 556 **Figure 5.** Reconstruction of the recovery phase of the March 8, 2009 substorm. Featuring the return of the TCS  
 557 (panels (e) and (g)) and persistence of the thick CS (panel (f)). The panels are the same as in Figure 3 but except for

## 558        3.3 Quantitative analysis of substorm currents and magnetic field variations

559 Further analysis of the March 2009 substorms presented in Figure 6 reveals the enhancement of  
 560 all FAC components in both substorms (Figures 6c and 6d). They show the square roots of the  
 561 sum of the squared amplitude coefficients  $(\sum_{m=1}^N C_m^2)^{1/2}$  for the eight higher latitude and eight  
 562 lower latitude modules. It should be noted that they are labeled as R1 and R2 based solely on  
 563 their latitude. Since the modules overlap in latitude and possesses higher order modes, which of  
 564 the coefficients contribute to the sense of the R1 and R2 current flow remains to be further  
 565 investigated. The comparison between Figures 6c and 6d shows that while both R1 and R2  
 566 components are enhanced after the onset, the low-latitude R2 components dominate in the  
 567 expansion phase. The corresponding equatorward shift of the FAC system is seen from the  
 568 comparison of Figures 3c and 4c and is consistent with the results of in situ observations of  
 569 substorm FACs using the Active Magnetosphere and Planetary Electrodynamics Response  
 570 Experiment (AMPERE) and from ground-based magnetometer and optical instrumentation from  
 571 the Canadian Array for Realtime Investigations of Magnetic Activity (CARISMA), as well as  
 572 from THEMIS magnetometer arrays reported by Murphy et al. (2013).

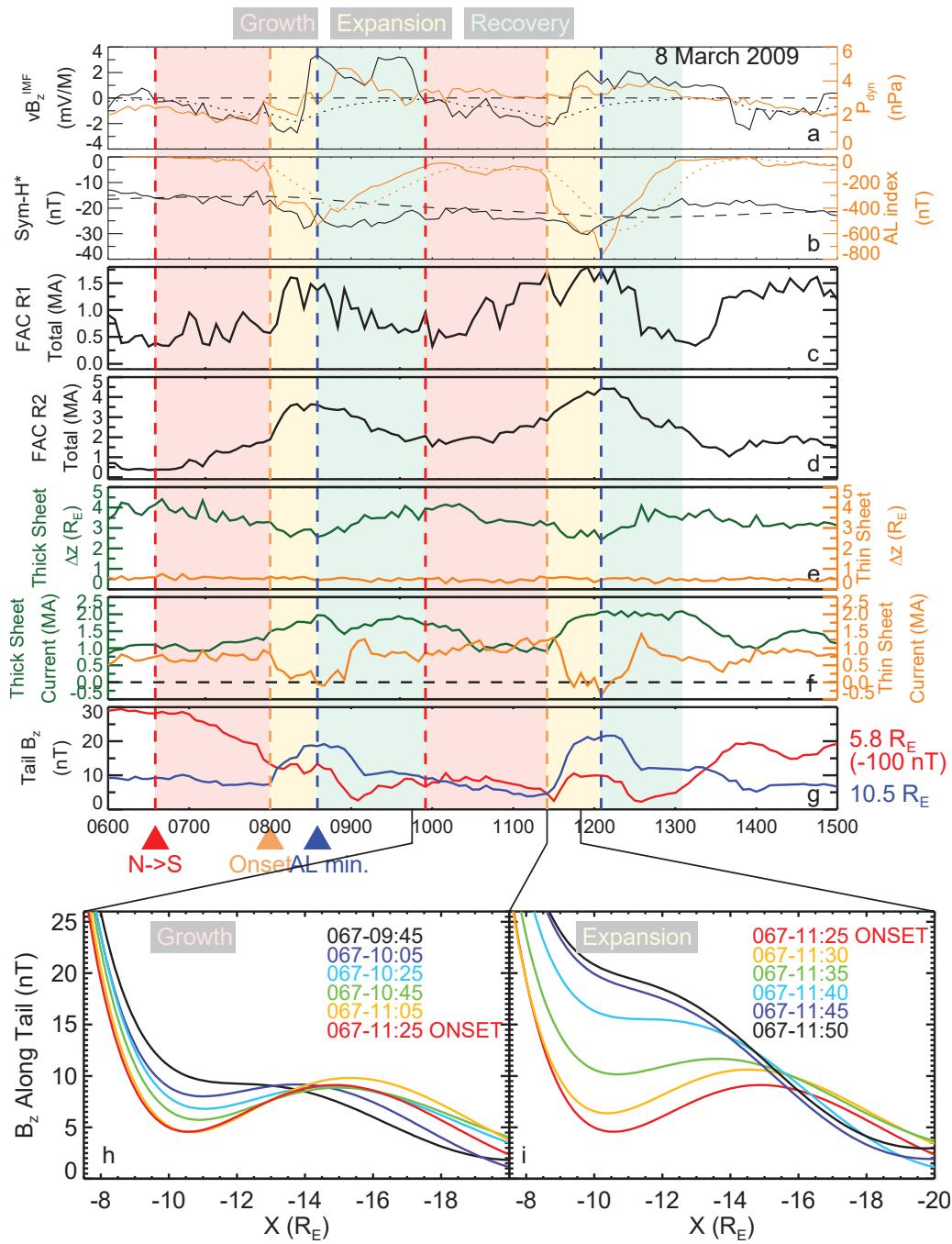
573        These FAC amplitude variations anti-correlate with the evolution of the thick CS thickness  
 574 (dark green line in Figure 6e). The evolution of the strength of the TCS and thick CS is plotted in  
 575 Figure 6f. The thick CS resembles the conventional ring current (Figures 3f–5f), meanwhile the  
 576 TCS contributes mainly to the magnetotail current (Figures 3g–5g). The strength of the TCS in  
 577 Figure 6 is quantified as the amount of cross tail current flowing in the magnetotail and is  
 578 computed by integrating the westward-flowing current density using a rectangular area integral:  
 579  $I^{(thin)} = \int_{-1}^{+1} \int_{-16}^{-6} j_y^{(thin)} dx dz$ . Only the TCS module is activated during this computation and  
 580 dipole tilt effects are ignored by setting it to zero. Meanwhile, the thick CS current is instead  
 581 computed by evaluating the integral on the noon meridian from the surface of the Earth to  
 582 Geosynchronous orbit  $I^{(thick)} = \int_{-5}^{+5} \int_{+1}^{+GEO} j_y^{(thick)} dx dz$ , and is thus a measure of the  
 583 conventional ring current.

584        According to Figures 6f and 6g, the most rapidly varying parameters are the TCS current  
 585 and the equatorial magnetic field  $B_z$ . The TCS current gradually increases during the growth  
 586 phase (from  $I \approx 0.8$  MA to  $I \approx 1.3$  MA for the second substorm) and then rapidly decreases  
 587 during the expansion phase, even reaching negative values indicating an eastward TCS and  
 588 reducing the total current, which results in the bifurcated current structure mentioned above, as  
 589 confirmed by in situ multi-probe analysis (e.g. Fig. 4II in (Runov et al., 2006)). Meanwhile,  $B_z$   
 590 rapidly increases (from  $\sim 4$  nT to  $\sim 21$  nT for the second substorm) in the expansion phase after  
 591 the preceding gradual decrease (from  $\sim 10$  nT to  $\sim 4$  nT) in the growth phase, in agreement with  
 592 fortuitous in situ multi-probe observations (Sergeev, Angelopoulos, et al., 2011). The  
 593 corresponding profiles in the growth and expansion phases, presented in two insets in Figure 6,  
 594 show the magnetic field stretching and dipolarization over the whole tail, thus providing key  
 595 information, which cannot be obtained in the foreseeable future by any real constellation mission  
 596 (e.g., Petrukovich et al., 2013; Ohtani and Motoba, 2017).

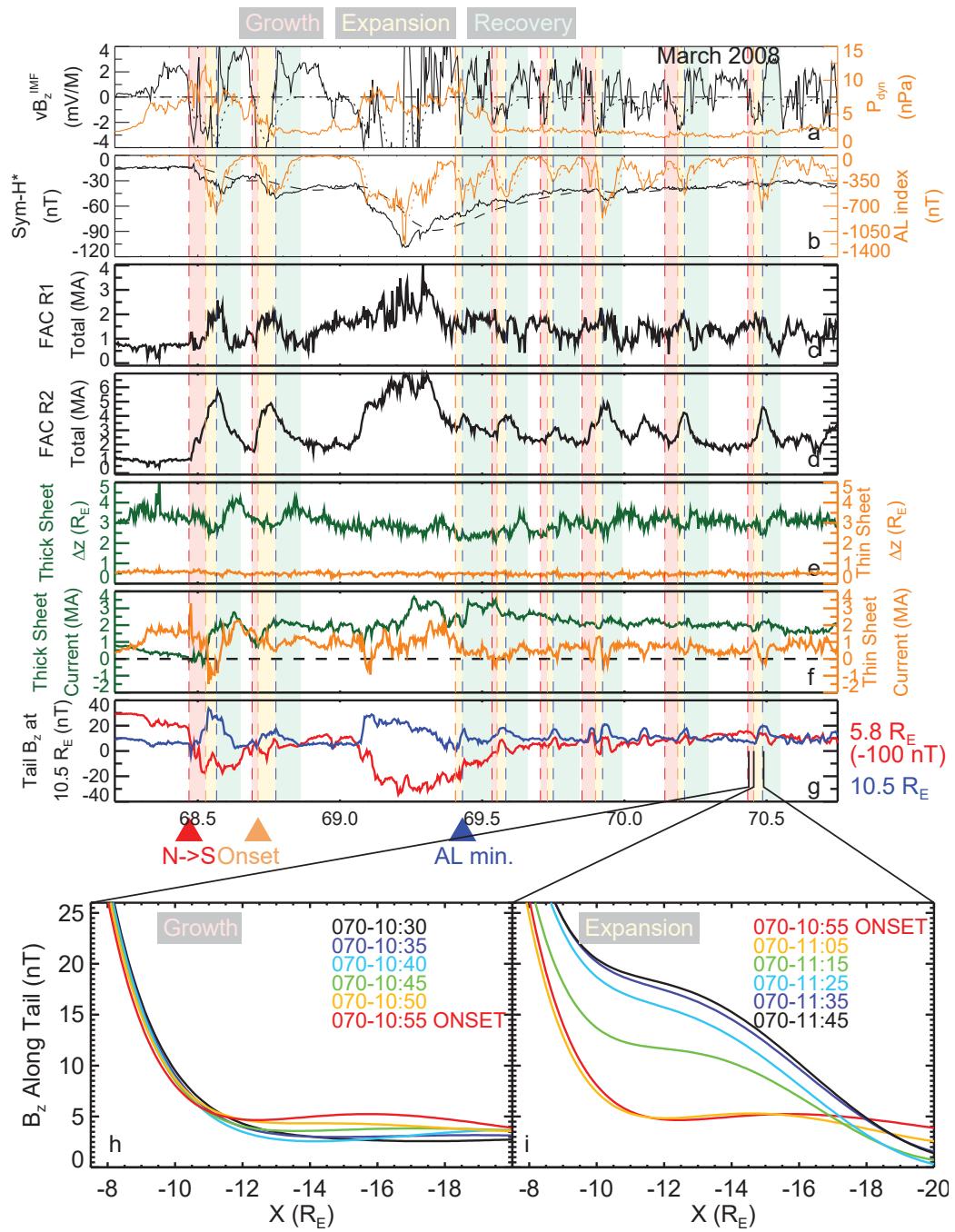
597        Meanwhile the thick CS evolution (Figure 6f) proceeds on longer time scales. Its  
 598 magnitude starts increasing during the expansion phase and stays enhanced at least an hour into  
 599 the recovery phase. The time scales and radial location of the thick CS suggest that it describes  
 600 the seed ring current responsible for storm dynamics of the magnetosphere. This hypothesis is

601 supported by another group of substorms in the March 2008 storm (Figure 7). In particular,  
602 Figure 7f shows that the thick CS magnitude elevates during the first substorm in the March  
603 2008 storm series and then remains elevated throughout the whole storm. We conclude that, in  
604 contrast to the TCS, which is an inherently substorm feature, the complementary thick CS should  
605 rather be characterized as a “proto-ring current” describing the contribution of substorms to the  
606 buildup of geomagnetic storms.

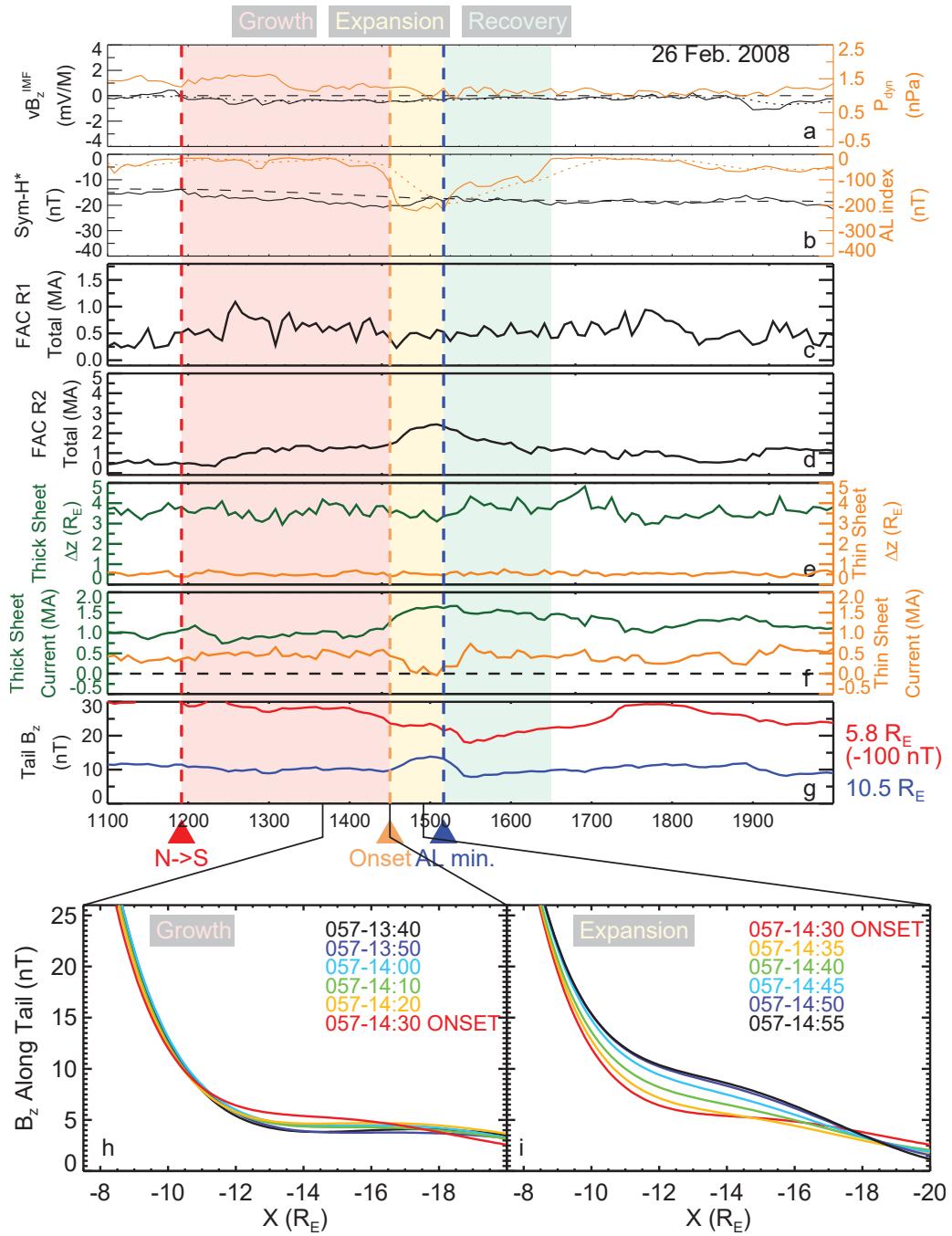
607 Other interesting features of the March 2008 main and early recovery phase (DOY=69–  
608 69.5) substorms (as seen in Figure 7) are overall elevated FAC amplitudes, which exceed their  
609 non-storm values (Figure 7c and 7d), and a strong dipolarization ( $B_z$  increase) at  $\mathbf{r} = (-10.5 R_E, 0,$   
610  $0)$  accompanied by a reduction of  $B_z$  in the inner magnetosphere near the Van Allen Probes  
611 apogee ( $\mathbf{r} = (-5.8 R_E, 0, 0)$ ) representing most likely combined substorm and storm effects. At the  
612 same time, according to Figure 7h, the substorm in the recovery phase of this storm reveals the  
613 same formation of the  $B_z$  hump at  $X \approx -16 R_E$  and the tailward  $B_z$  gradient earthward of it in the  
614 late growth phase of the substorm, which was seen for the March 8, 2009 substorm (Figures 3d  
615 and 6h). The formation of regions with a tailward  $B_z$  gradient has recently been recognized as a  
616 key feature of magnetotail destabilization mechanisms, including tearing (Sitnov & Schindler,  
617 2010; Merkin et al., 2015; Merkin & Sitnov, 2016; Sitnov, Merkin, et al., 2017; Birn et al.,  
618 2018), ballooning/interchange (Pritchett and Coroniti, 2013), and flapping (Erkaev et al., 2007)  
619 instabilities. Thus, the new data mining approach advances earlier multi-probe measurements  
620 (Petrukovich et al., 2013; Ohtani and Motoba, 2017) and machine-learning analysis (Yue et al.,  
621 2015), because it resolves the tailward  $B_z$  gradient effect. Note that this finding is consistent with  
622 the earlier statistical studies (Wang et al., 2004, Fig. 9b) and the statistical visualization of  
623 substorms (Machida et al., Fig. 2c), as well as the most recent results obtained by remote sensing  
624 methods (Sergeev et al., 2018).



625  
626 **Figure 6.** Analysis of the March 8, 2009 substorm current system evolution. (a and b) Solar wind measurements and  
627 Geomagnetic indices respectively; similar to panels (e) and (f) in Figure 1 respectively. (c and d) The square root of  
628 the sum of the squared amplitude coefficients for the R1 and R2 FAC modules respectively (Sitnov, Stephens, et al.,  
629 2017). (e) The equatorial CS half thickness parameter for the thick CS in green and the TCS in orange. (f) The  
630 westward current from the thick CS module passing through the dayside rectangle:  $1.0 R_E \leq X \leq 6.616 R_E$  and  $-5.0$   
631  $R_E \leq Z \leq 5.0 R_E$  in green and the westward current from the TCS module passing through the magnetotail rectangle:  
632  $-16 R_E \leq X \leq -6 R_E$  and  $-1.0 R_E \leq Z \leq 1.0 R_E$  in orange. (g) Total modeled  $B_z$  sampled at  $r = (-5.8 R_E, 0, 0)$  in red and  
633  $r = (-10.5 R_E, 0, 0)$  in blue. (h and i) The total modeled  $B_z$  sampled along the line  $(-20 R_E \leq X \leq -7.5 R_E, 0, 0)$  during  
the growth and expansion phase respectively.

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635

**Figure 7** Analysis of the March 2008 storm containing substorms, substorm current system evolution. The panels are the same as in Figure 6 but except for a different event.



638        The analysis of a relatively weak non-storm substorm, which occurred 26 February 2008,  
 639 is presented in Figure 8 (the corresponding validation results are provided in Figure S4). It  
 640 confirms the general nature of some key substorm features that have been conjectured before but  
 641 are now seen with statistical significance for a range of different types of substorms. These  
 642 include the rapid disappearance of the TCS in the expansion phase (Figure 8f, orange line)  
 643 accompanied by the more gradual and long-lasting increase and accumulation of the thick CS  
 644 (Figure 8f, green line),  $B_z$  dipolarization at  $10.5 R_E$  correlated with a signal at  $5.8 R_E$ , which  
 645 however may not have the similar form (compare Figure 8g and the first event in Figure 6g with  
 646 the second event in the same figure as well as in Figure 7g). The generic nature of thinning and  
 647 dipolarization processes, including the evolution of TCS and thick CS components, is confirmed  
 648 by supplementary Figures S5–S10, which show analogs of Figures 3–5 for 10 March and 26  
 649 February 2008 substorms.

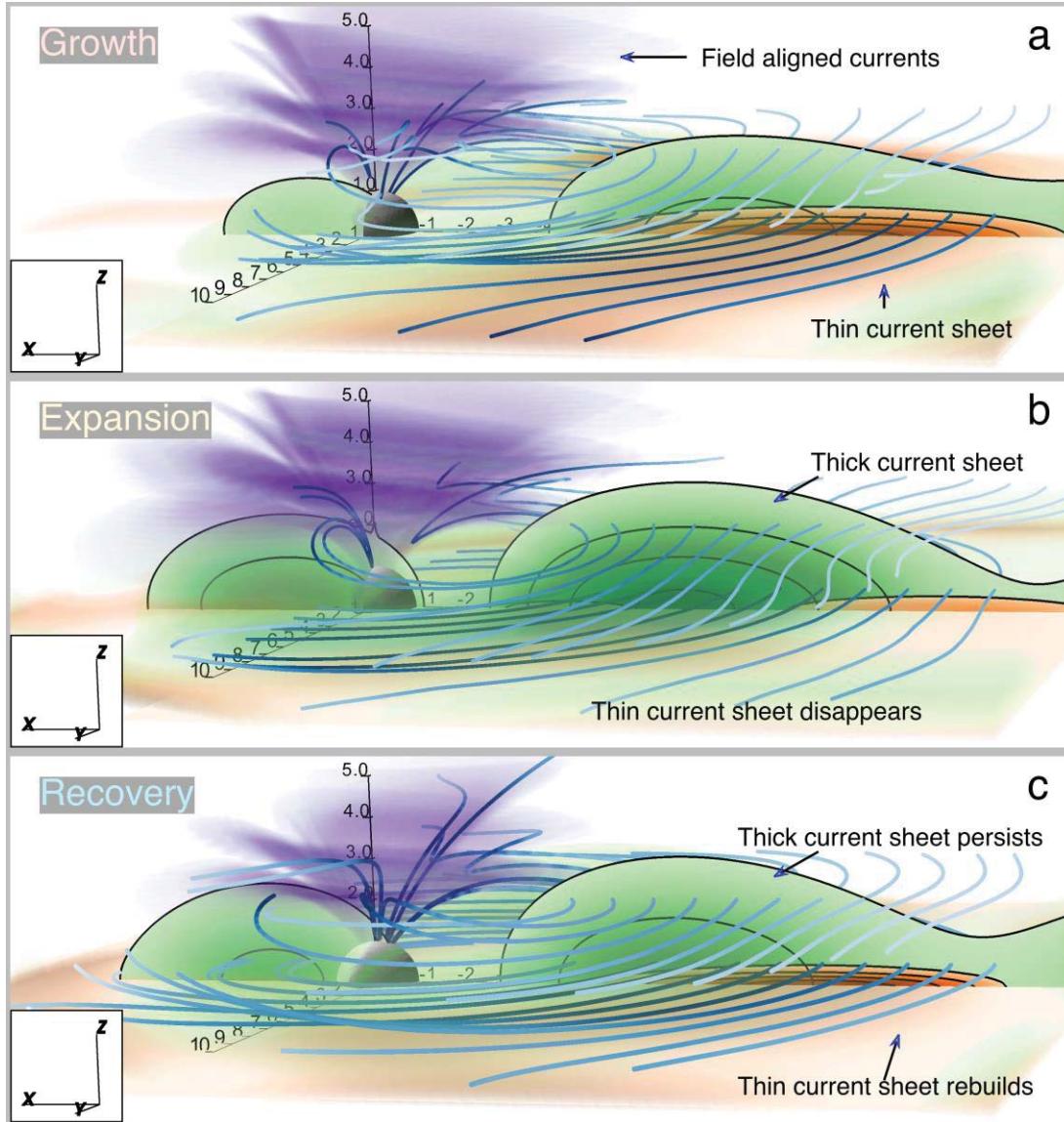
650        At the same time, Figure 8h, in contrast to Figures 6h and 7h, does not show the  
 651 formation of a  $B_z$  hump in the late growth phase. One can suggest that it is either forming earlier  
 652 (black line) or further away from the Earth, where the empirical reconstruction is less robust  
 653 because of the lack of data. Also,  $vB_z^{IMF}$  is relatively weak prior to the substorm, so it is possible  
 654 that the growth phase of this particular substorm is not fully captured by the parameter derived  
 655 from  $vB_z^{IMF}$  described in equation (8). The specific conditions favorable for the hump formation  
 656 and determining its location in the tail are still to be investigated.

657        A common feature for all events considered here is the increase of the FAC R2  
 658 magnitude, first in the growth phase and then a more rapid enhancement in the expansion phase.  
 659 It is not accompanied by the corresponding enhancement of the higher-latitude R1 current part  
 660 for the weak storm shown in Figure 8c. For stronger storms shown in Figures 6c and 7c the  
 661 concurrent R1 is present, but its shape is not so similar to the substorm variation expressed in  
 662 terms of the  $AL$  index. One should stress here that the amplitudes R1 and R2 shown in panels  
 663 Figures 6c–8c only reflect the strength of the corresponding high- and low-latitude currents, but  
 664 not their R1/R2sense. The detailed structure of these currents, including their 3-D features will  
 665 be described in the next section.

### 666        3.4 3-D picture of substorm currents and the substorm current wedge

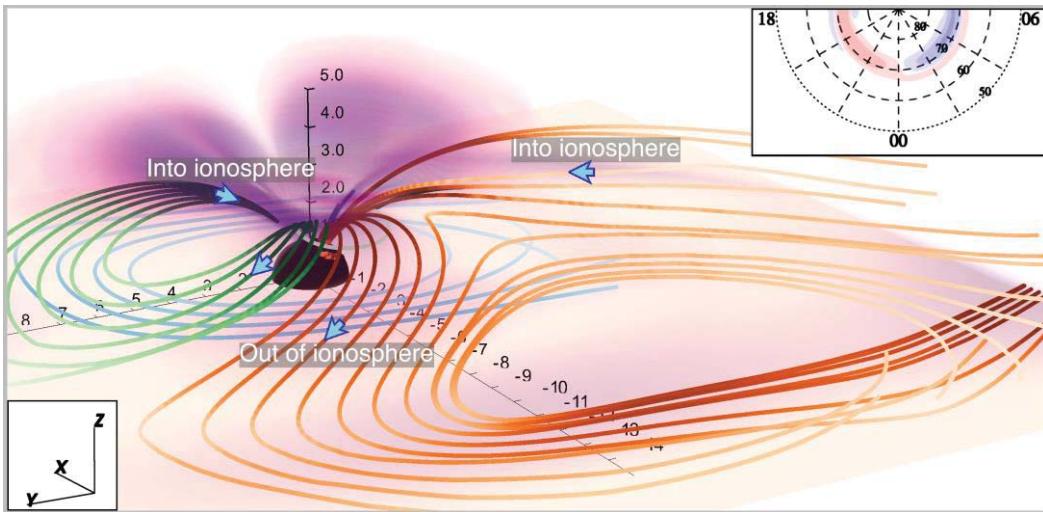
667        Figure 9 provides 3-D distributions of magnetospheric currents in different phases of the  
 668 March 2009 substorm, corresponding to Figures 3, 4, and 5, whereas Figure 10 provides the  
 669 reconstruction of the current systems associated with the substorm expansion.

670        Figures 9a–9c confirm the TCS buildup, decay and rebuilding shown by an orange  
 671 volume rendering and reflected by 2-D slices in Figures 3–5. The evolution of the thick CS  
 672 shown by the meridional cut of the corresponding contribution to the total current density is  
 673 different from the TCS evolution, and of particular interest is the persistence of the thick CS in  
 674 the recovery phase. Mapping of selected 3-D current loops in Figure 9b (see also Figure 5d)  
 675 shows that the thick CS is closed through the ionosphere via R2-type FAC system similar to the  
 676 storm-time PRC.



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**Figure 9.** 3-D reconstruction of major current systems for the March 8, 2009 substorm. (a) growth phase; (b) expansion phase; (c) recovery phase. An orange volume rendering shows the 3-D distribution of the TCS and a violet volume rendering shows the FAC distribution. The 3-D distribution of the thick CS is shown by a 3-D green volume rendering and it is complemented by the 2-D distribution of the current along the midnight meridian. Blue contours show selected current lines and their intensity reflects the current strength.



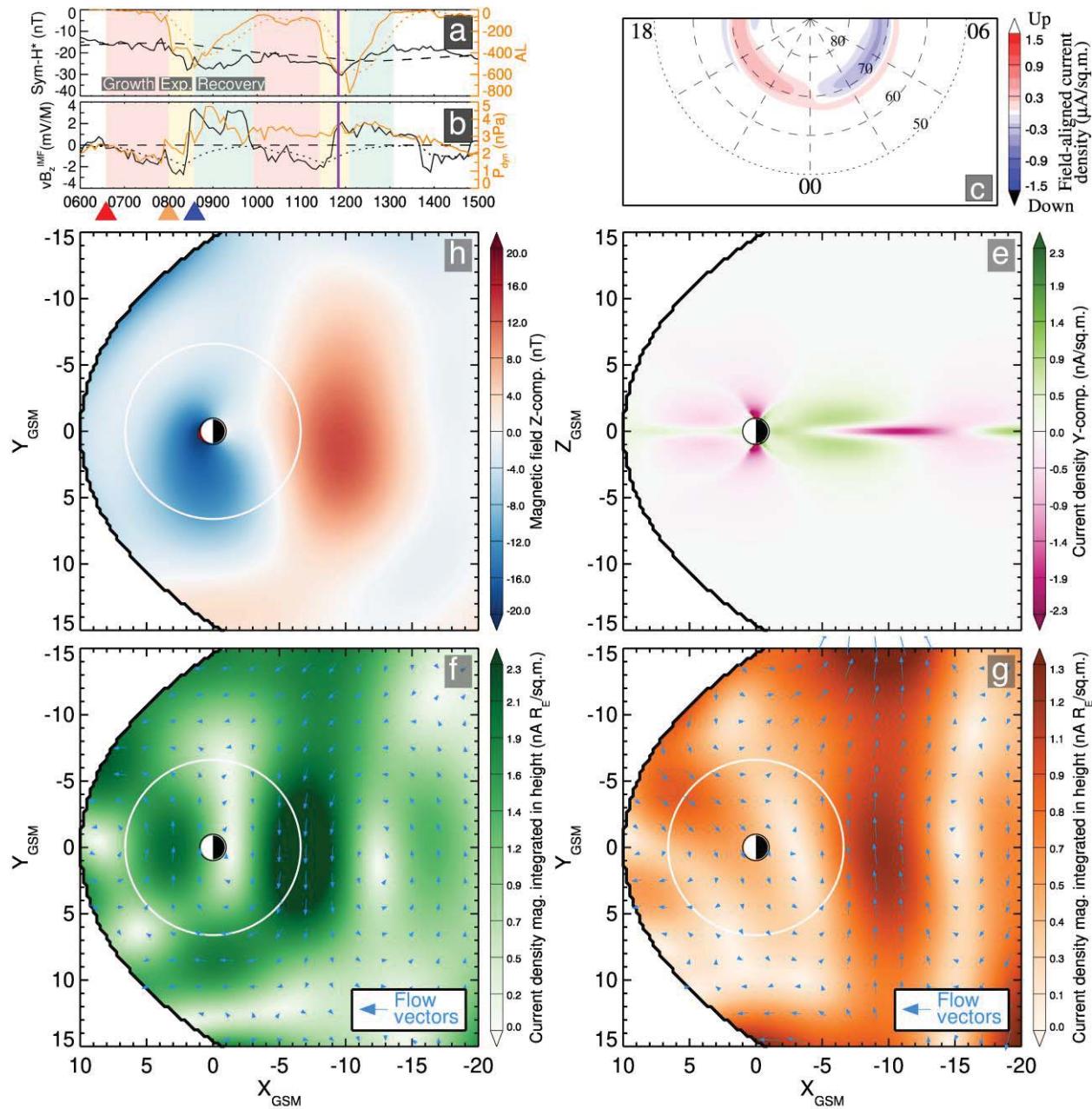
682 **Figure 10.** 3-D reconstruction of SCW for the March 8, 2009 substorm. Currents present are obtained by taking the  
 683 curl of the difference between the magnetic fields in the expansion and growth phase currents. A violet volume  
 684 rendering shows the 3-D distribution of the currents, while selected current lines feature the classical SCW (dark  
 685 orange lines), R2 currents similar to the PRC storm-time current (green lines), and symmetric ring current (blue  
 686 lines). The inset in the format of Figure 3c displays the FAC distribution of 3-D currents, and in particular, the low-  
 687 altitude portion of the SCW.

688 The distinctive features of the substorm current system reconfigurations are presented in  
 689 Figure 10, which shows 3-D currents obtained from the difference between the magnetic field in  
 690 the expansion phase (Figure 4) and the growth phase (Figure 3). Currents in Figure 10 are  
 691 computed by applying Ampere's law to the difference between the expansion (11:50) and growth  
 692 phase (11:25). In order to simplify this picture, the growth phase used in this difference  
 693 calculation was fit in a different manner. The non-linear parameters were not fit but were instead  
 694 set to be identical to the expansion phase. For example, this forces the FAC distributions from  
 695 the growth and expansion phases to coalign, making for a simpler picture when the difference is  
 696 computed. Additionally, for simplicity the dipole tilt deformations are turned off by setting the  
 697 parameters that control this deformation (hinging, warping, and twisting parameters) to zero.  
 698 This aligns the magnetic equator in the equatorial plane.

699 The inset in Figure 10 shows that the low-altitude FAC system has the spiral pattern  
 700 similar to that of the total field in each phase. However, this spiral is shifted to low latitudes,  
 701 compared to the growth phase pattern (Figure 3c). Figure 10, together with Figure 11, show that  
 702 the spiral pattern is a set of foot points of the R1-sense SCW loop (orange lines), which had been  
 703 conjectured (Crooker & McPherron, 1972; Fukushima & Kamide, 1973; McPherron et al., 1973)  
 704 based on a limited number of ground-based and spaceborne observations. Figure 10 also  
 705 confirms the appearance of closed near-equatorial SCW loops predicted based on MHD  
 706 simulations of magnetotail dipolarizations (loop #3 in Plate 4 in (Birn et al., 1999) further  
 707 generalized to a combination of loops #3 and 4 in Fig. 5 in (Kepko et al., 2015)). Although the  
 708 earthward propagation of the dipolarization signal deep into the geosynchronous region is clearly  
 709 seen from data (compare black and red lines in Figure 6g), Figure 10 does not show a separate  
 710 R2 current system earthward of the SCW, which was predicted as a precursor of dipolarizing  
 711 flux tubes based on MHD and kinetic simulations (Birn et al., 1999; Yang et al., 2011). This may  
 712 be caused by either yet insufficient spatial resolution of our empirical picture or by transient  
 713 nature of R2 FAC precursors on the time scales smaller than those of substorms. At the same  
 714 time, Figure 10 reveals two large-scale current systems apparently associated with the buildup of

715 the storm-time currents: the R2 loop located right clockwise of the SCW (green lines) resembling  
 716 the PRC, and another current loop encircling the Earth and similar to the symmetric ring current  
 717 (SRC).

## Substorm current wedge 2009-067 (March-08)



718 **Figure 11.** 2-D reconstruction of the substorm expansion currents of the March 8, 2009 substorm (2-D analog of  
 719 Figure 6). The panels are similar to Figures 3–5 but except now are the difference between the expansion phase and  
 720 the growth phase. The ionospheric closure of the SCW in panel (c) is shown centered about midnight and flows in  
 721 the same sense as a R1 FAC. The equatorial slice of the differenced magnetic field in panel (d), reflects the magnetic  
 722 flux buildup region centered in the premidnight sector and at  $X \sim -10 R_E$ . Also seen, is a decrease in the magnetic  
 723 field from pre-noon through the post-dusk sector within Geosynchronous orbit caused by the buildup of a westward

724 ring current. Panel (e) shows the meridional slice of the  $Y$ -component of the differenced current density. The  
725 equatorial portion of the SCW can be seen in this panel as the eastward TCS centered at  $X \sim -10 R_E$ . It partially  
726 closes through the westward thick CS shown in the same panel and also partially closes through the ionosphere as is  
727 shown in Figure 10. On the dayside within Geosynchronous orbit, the thick CS is westward, indicating a ring  
728 current. Panels (f) and (g) show the equatorial slice of the height integrated magnitude of the differenced current  
729 density for the thick and thin CSs. The equatorial portion of the SCW shown in panel (g) is flowing eastward and is  
730 centered in the premidnight sector at  $X \sim -10 R_E$ . Meanwhile a westward thick CS shown in panel (f), is enhanced in  
731 the region centered about midnight at  $X \sim -7 R_E$ . Part of this enhancement is seen to be the closure of the SCW in  
732 Figure 10, while part of it flows out to the pre-dusk magnetopause. Yet additional current flows around to the  
733 dayside, forming a symmetric ring current part. There is an additional smaller dusk enhancement at  $Y \sim 8 R_E$ . As was  
734 shown in Figure 10, this partially closes through the ionosphere, forming a PRC.

735 The qualitative picture of substorms and storms, including the SCW, PRC and SRC  
736 systems, was conjectured almost half a century ago based largely on ground-based observations  
737 of the magnetic field by Crooker and McPherron (1972) as well as Kamide & Fukushima (1972)  
738 (see in particular, Figs. 22 and 23 in (Fukushima & Kamide, 1973)). However, only now the  
739 quantitative reconstruction of the 3-D structure of all these currents and their evolution directly  
740 from spaceborne magnetometer data has become possible. The generic nature of the obtained  
741 substorm features shown here for the March 2009 event is confirmed by similar results obtained  
742 for the March 2008 storm-time substorms (Figures 1, 7 and S5–S7) and a much weaker substorm  
743 that occurred on 26 February 2008 (Figures 8 and S8–S10). Also noteworthy, is that the  
744 magnetic field dipolarization in the expansion phase clearly shows that the magnetic flux is  
745 redistributed earthward (seen from the comparison between Figures 3d and 3e, on the one hand,  
746 and 4d and 4e, on the other, as well from the comparison of panels (h) and (i) in Figures 6–8),  
747 which is consistent with in situ observations by multi-probe missions (Ohtani, 1998;  
748 Angelopoulos et al., 2008) and confirms the statistical significance of the corresponding  
749 fortuitous substorm case studies. For example, as is seen from Figure 6g, during the second event  
750 of the March 2009 substorms, the beginning of the dipolarization is observed at  $10.5 R_E$  in the  
751 tail tens of minutes before it is seen to begin at  $5.8 R_E$  (approximately the apogee of the Van  
752 Allen spacecraft). In the first weaker substorm, the dipolarization never reaches  $5.8 R_E$  and the  
753 field there actually continues to thin. The analysis of March and February 2008 substorms  
754 (Figures 7 and 8) confirm that finding.

#### 755 4 Discussion and Conclusions

756 We conclude that by data mining more than two decades of multi-mission magnetometer  
757 data the global picture of major 3-D current systems that constitute the phenomenon of  
758 magnetospheric substorms, as defined by the auroral index  $AL$ , can be reconstructed. Their  
759 evolution is not limited to the stretching and dipolarization of the night-side magnetic field, but  
760 also includes the formation and persistence of currents pertinent to magnetic storms. The data-  
761 mining approach employed in our study is based on the NN method, which generalizes earlier  
762 multi-probe event-oriented reconstructions as well as custom-made statistical models, revealing  
763 both the generic thinning/dipolarization signatures and also the individual features of the event of  
764 interest. It should be stressed that in this paper we do not introduce another “fully cooked”  
765 geomagnetic field model, like T89, TS05 and other classical Tsyganenko models (e.g.,  
766 Tsyganenko, 2013, and refs. therein). We rather introduce a method of the empirical analysis of  
767 the magnetospheric configuration during substorms, and we provide the first proof-of-principle  
768 demonstration that this method works.

769 This approach assumes the state of the magnetosphere during substorms can be  
770 determined by the 5-D state vector defined by equations (4)–(8) and locates magnetometer data  
771 from the historical database from events closest to the moment of interest using a Euclidean  
772 distance metric represented by equation (9). Thus, the data-mining approach lies in between  
773 event based studies that use simultaneous in situ measurements to infer substorm dynamics and  
774 large statistical studies that average over all the available substorms. As this study shows, the  
775 approach is capable of distinguishing substorm phases, identifying the mixed nature of storm-  
776 time substorms, and distinguishes between strong (8 March 2009) and weaker (26 February  
777 2008) substorms. This technique is still limited in reproducing some details of individual events,  
778 as is seen from our validation tests (Figures 1, 2, and S4). In particular, the magnitude of both the  
779 current sheet thinning signatures in  $B_x$  and the dipolarization signatures in  $B_z$  are often

underestimated in the reconstructions as compared to the in situ magnetometer data. This may be the result of averaging over numerous substorms and thus spreads these signatures over a larger local time. Additionally, the  $AL$  index contains little information about the local time location and extent of the dipolarization and associated substorm current wedge. This may explain the discrepancy between the reconstructed  $B_z$  component of the magnetic field and the GOES-11 magnetometer data during the expansion phase of the 8 March 2009 event (Figure 2t). GOES-11 is located at  $\sim 3$  MLT, however, Figure 4d and 4f indicate the reconstructed dipolarization does not penetrate that far downward. Another contributing factor may be a result of the dimensionality of the NN parameter space. By minimizing the distance in a 5-D parameter space, the sensitivity of any single parameter is decreased. For example, the second substorm on 8 March 2009 has a minimum value of smoothed  $AL$  of  $-576$  nT, while the average of the NNs selected for this reconstruction is only  $-423$  nT. This can be mitigated by increasing the corresponding weight factor of any given parameter in the distance metric in equation (9), but as of now this investigation has not been done. There is also perhaps a shortcoming in the use of the smoothed  $vB_s^{IMF}$  parameter to identify the growth phase. Of the three growth phase tail  $B_z$  profiles plotted in Figures 6–8h, only Figure 6h had a strongly defined tailward  $B_z$  gradient, which of the three, had strongest smoothed  $vB_s^{IMF}$  profile (Figure 6a dotted black dotted line). In comparison, the growth phase represented in Figure 6h only lasted for 25 minutes as determined by  $vB_s^{IMF}$  and the 26 February, while long, was much weaker ( $vB_s^{IMF} < 0.4$  mV/M). Neither of these later types of growth phases will be well captured by equation (8).

This study is limited to relatively conventional isolated substorms with characteristic loading-unloading cycle durations of about 2 hours, consistent with the selected NN parameters (4)–(6). However, the magnetospheric activity reflected by the auroral indices, such as the  $AL$  index, is not limited to substorms. It also includes longer time-scale phenomena, such as steady magnetospheric convection events (SMC) that represent a mode where this conversion process is quasi-steady and the dayside reconnection rate is assumed to be in balance with the nightside rate. Like substorms, this class of events is frequently defined from auroral indices, often a stable and continuous level of  $AL$  activity, and they are sustained by stably southward IMF (Sergeev, Pellinen et al. 1996). As such, there is overlap between substorms and SMC based purely on  $AL$  and solar wind parameters such as  $vB_s^{IMF}$ . This demonstrates the importance of including the time derivatives of the parameters in the NN approach. SMC events were previously analyzed with the TS07D model (Stephens et al., 2013), and in particular it was found these events possessed a tailward  $B_z$  gradient. However, the  $B_z(x)$  profiles were found to differ substantially. The early part of the SMC event possessed a deep  $B_z$  minimum (similar to the onset profile in Figure 6h), but as the SMC event progressed the  $B_z$  minimum became shallower and moved earthward. The advancements presented here may be useful in discerning the variety of magnetotail configurations that exist in these different convection modes and how they relate to one another. However, due to the long duration and relatively rarity of SMCs compared with substorms (O'Brien et al., 2002), the DM technique may be customized for SMCs by adding longer duration  $AL$  parameters similar to those in equations (6) and (7) but with a smoothing timescale on the order of SMC intervals.

At the same time, the present analysis averaged over many interesting substorm phenomena on the scales smaller than those of the global magnetospheric reconfiguration during a substorm. They include bursty bulk flows, dipolarization fronts, ballooning/interchange, and flapping motions of the plasma sheet, as well as wedgelets (e.g., Sergeev et al., 2006; Runov et al., 2012; Liu et al., 2013; Kepko et al., 2015, and refs. therein) and their ionospheric

826 manifestations (Keiling et al., 2013; Henderson, 2013). These phenomena are very important to  
 827 understand substorm mechanisms (e.g., Sergeev, Pulkkinen et al., 1996), but they are hard to  
 828 reconstruct using any global empirical reconstruction of the magnetic field. They can be  
 829 investigated, however, using local observations (Sergeev, Angelopoulos et al., 2011), global  
 830 MHD (Wiltberger et al., 2000; Raeder et al., 2008), and local kinetic (Yang et al., 2011; Sitnov,  
 831 Merkin et al., 2017) simulations of the magnetosphere. It is interesting that the latter reveal the  
 832 importance of the global structure of the magnetosphere (for instance, through the flux tube  
 833 volume parameter) for substorm plasma instabilities (Sitnov, Merkin et al., 2017; Birn et al.,  
 834 2018).

835 Thus, the obtained empirical picture of substorms may be decisive for understanding their  
 836 underlying physical mechanisms and for interpreting similar substorm-like phenomena on other  
 837 planets (Mitchell et al., 2009; Slavin et al., 2010), in the solar corona (Reeves et al., 2008), and  
 838 on other astrophysical objects (Osten et al., 2016) where such a comprehensive coverage in space  
 839 and time is impossible.

840

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 852 SPDF website ([https://spdf.gsfc.nasa.gov/pub/data/aaa\\_special-purpose-datasets/empirical-magnetic-field-modeling-database-with-TS07D-coefficients/](https://spdf.gsfc.nasa.gov/pub/data/aaa_special-purpose-datasets/empirical-magnetic-field-modeling-database-with-TS07D-coefficients/)). The model output is available on  
 853 request and will be archived.

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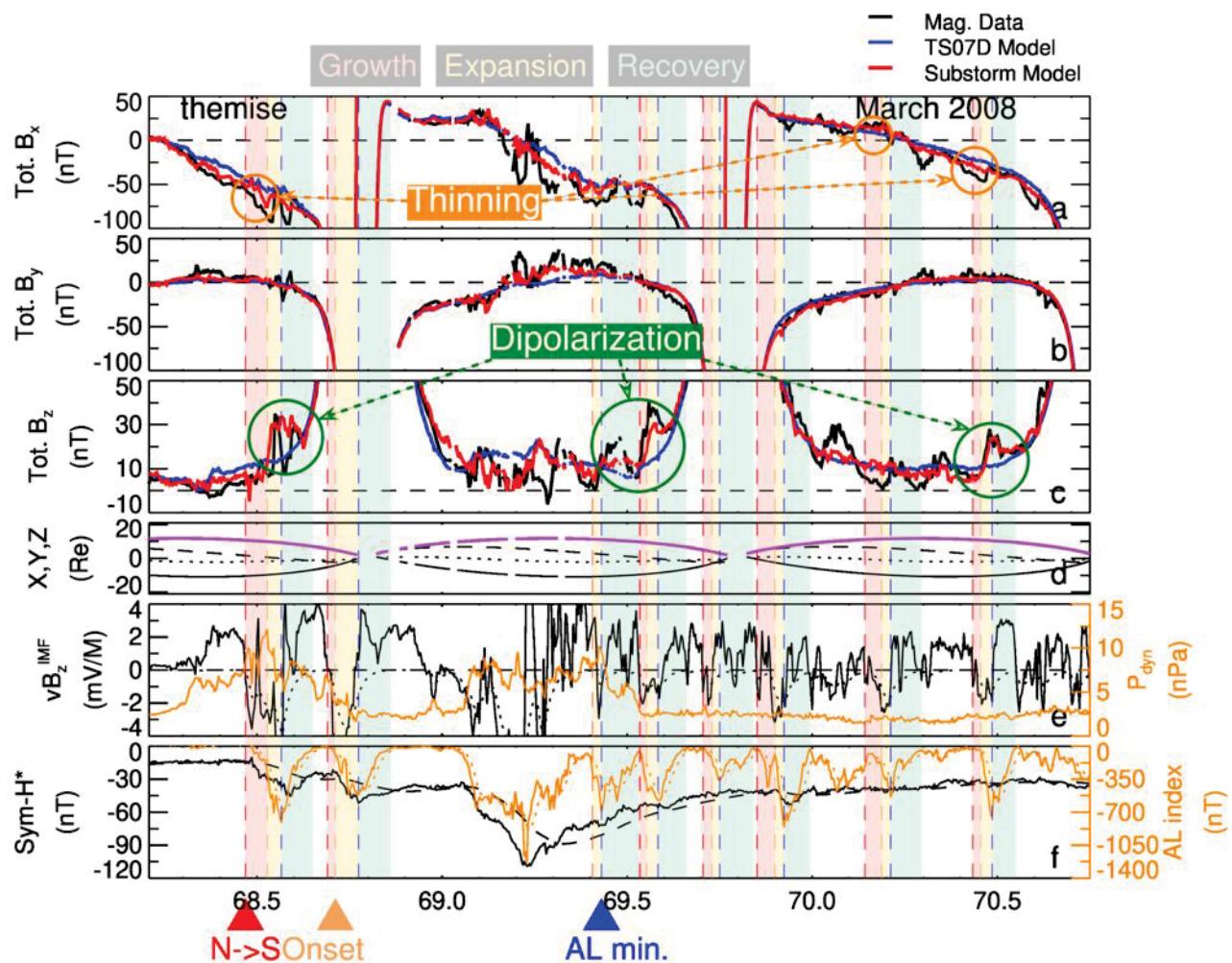
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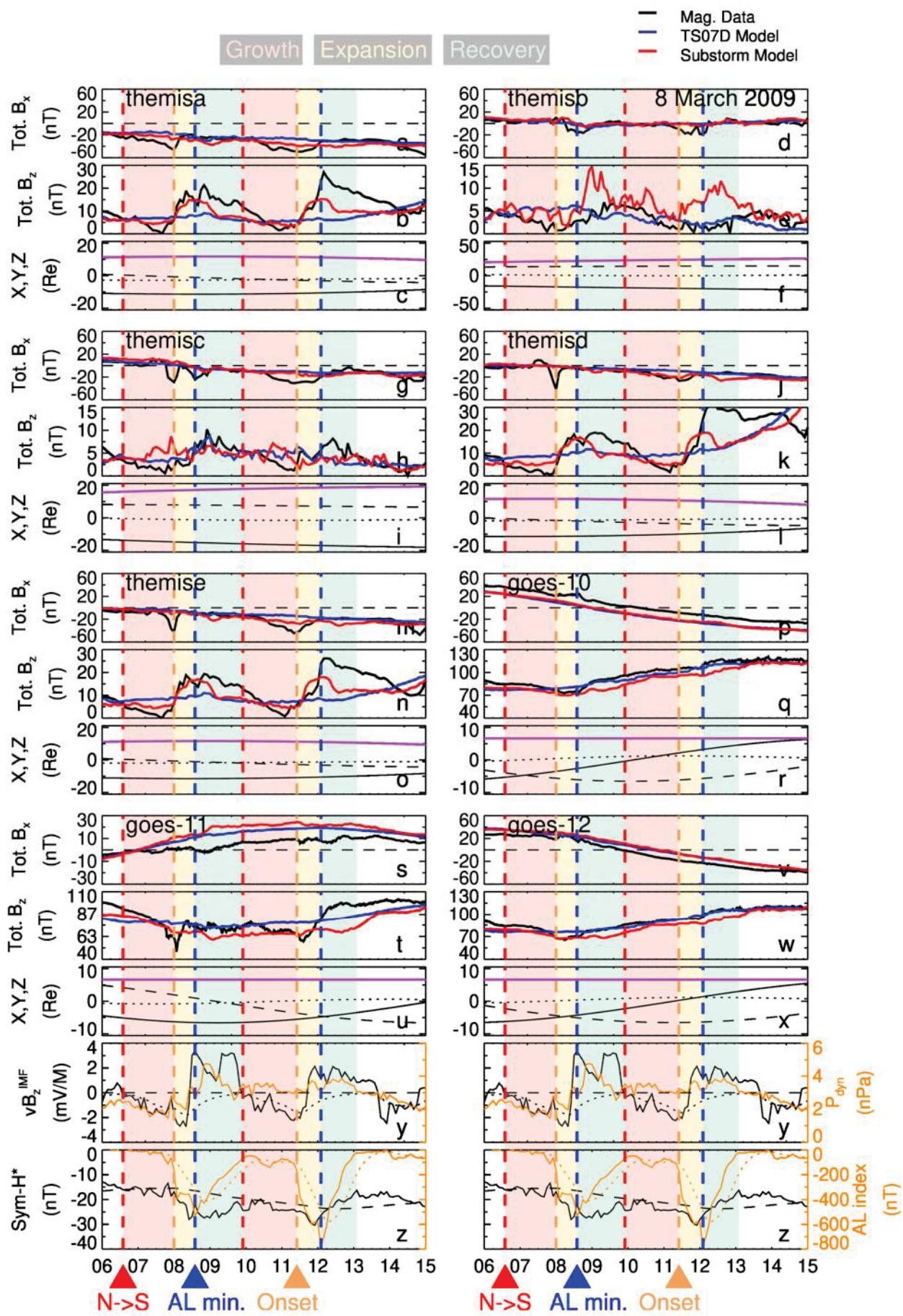
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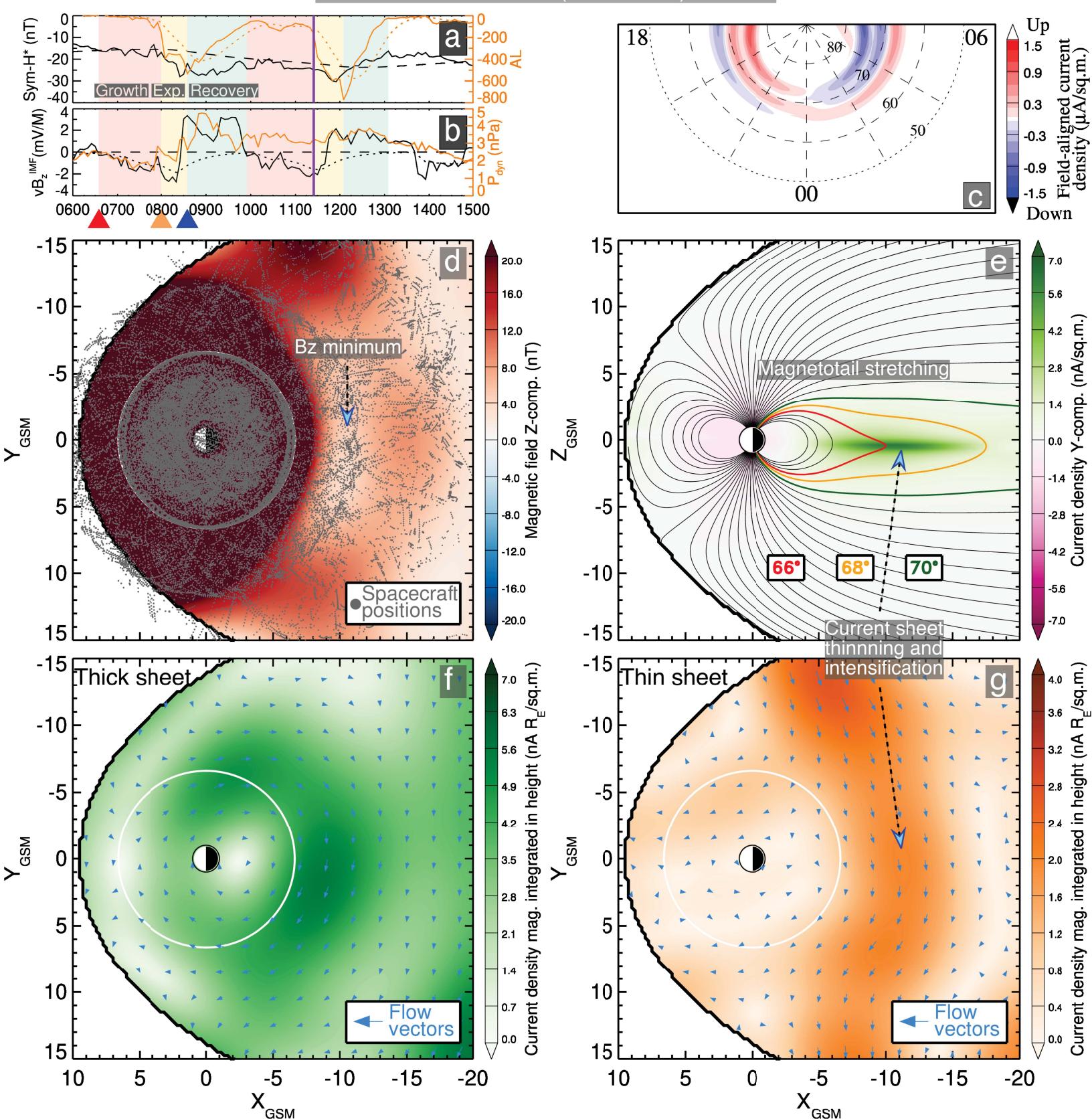


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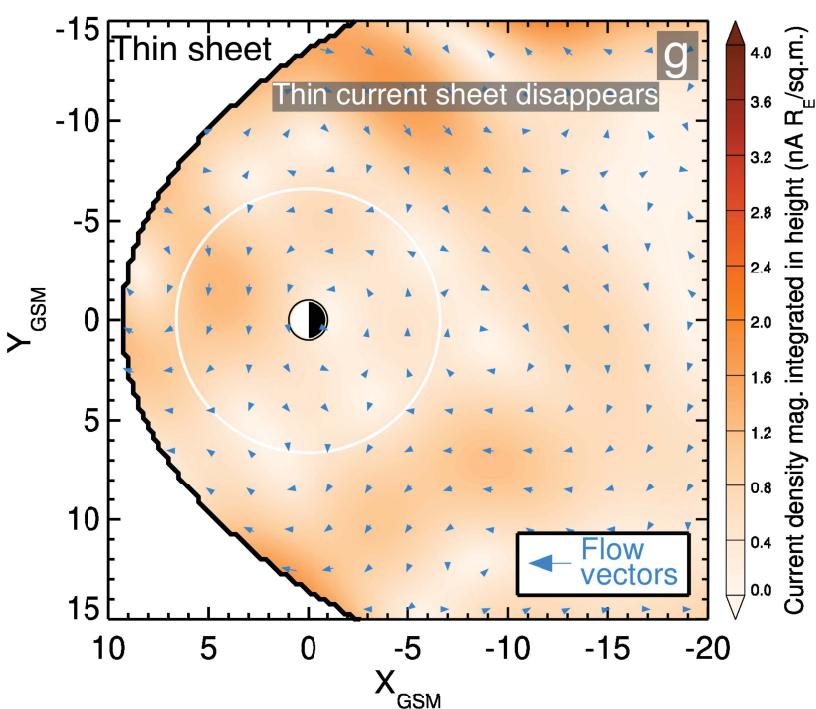
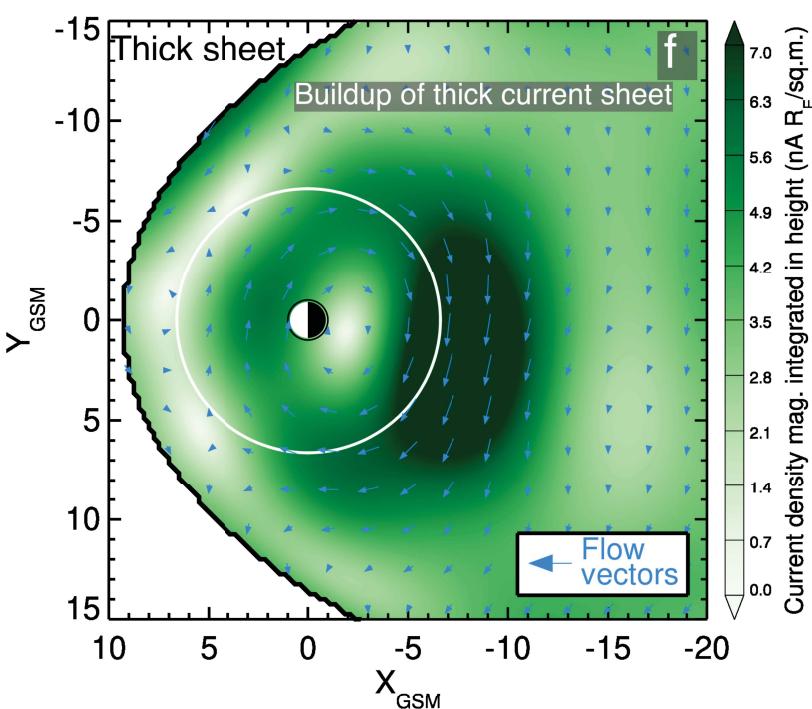
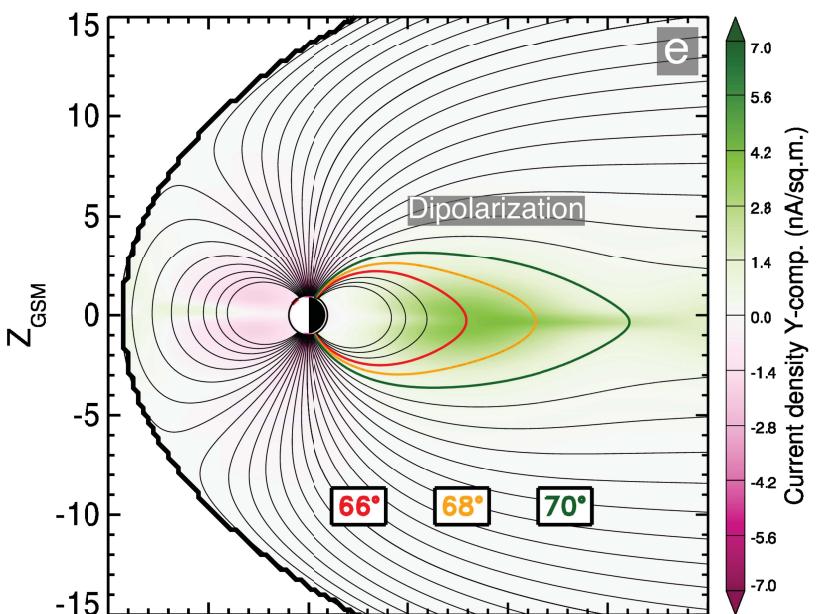
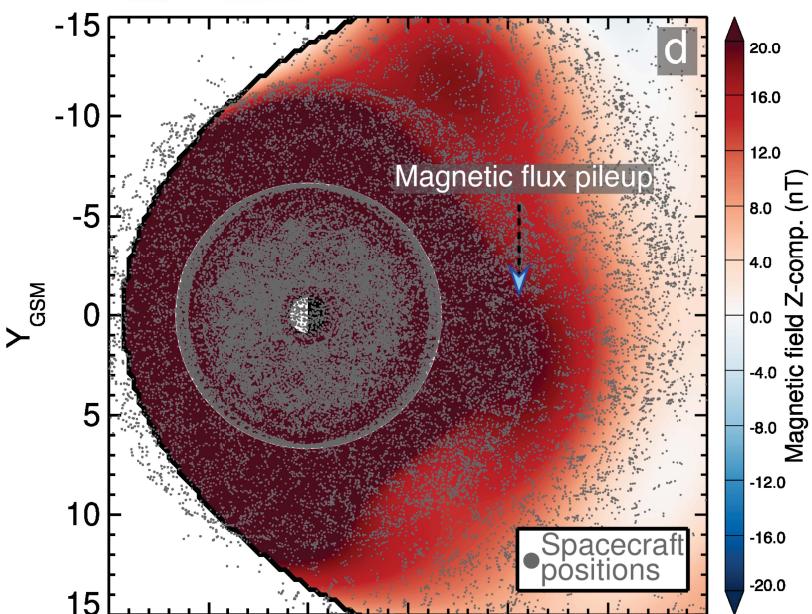
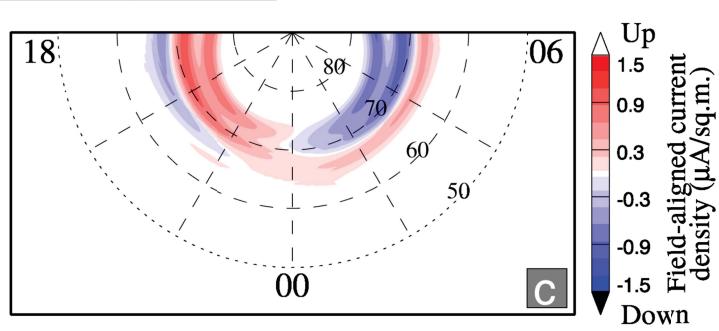
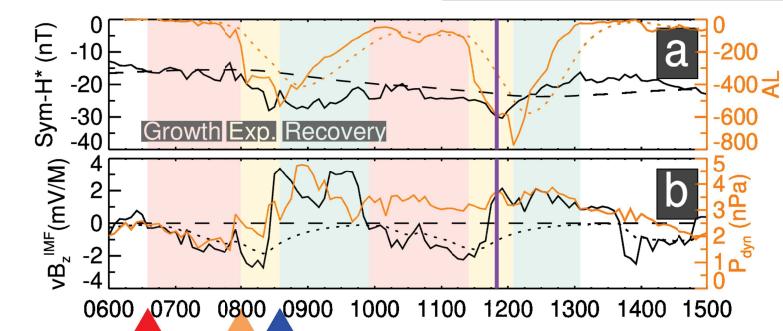
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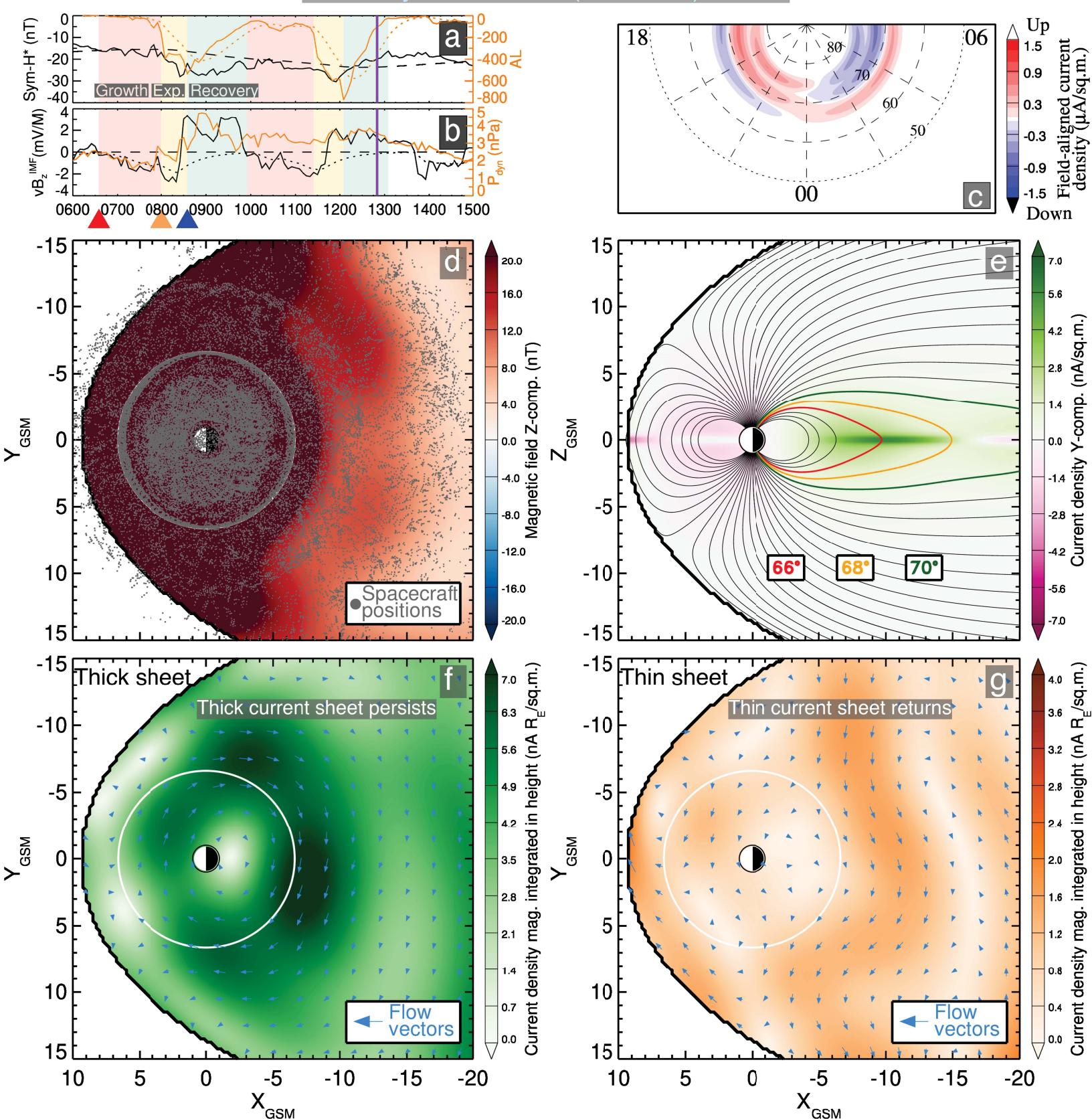
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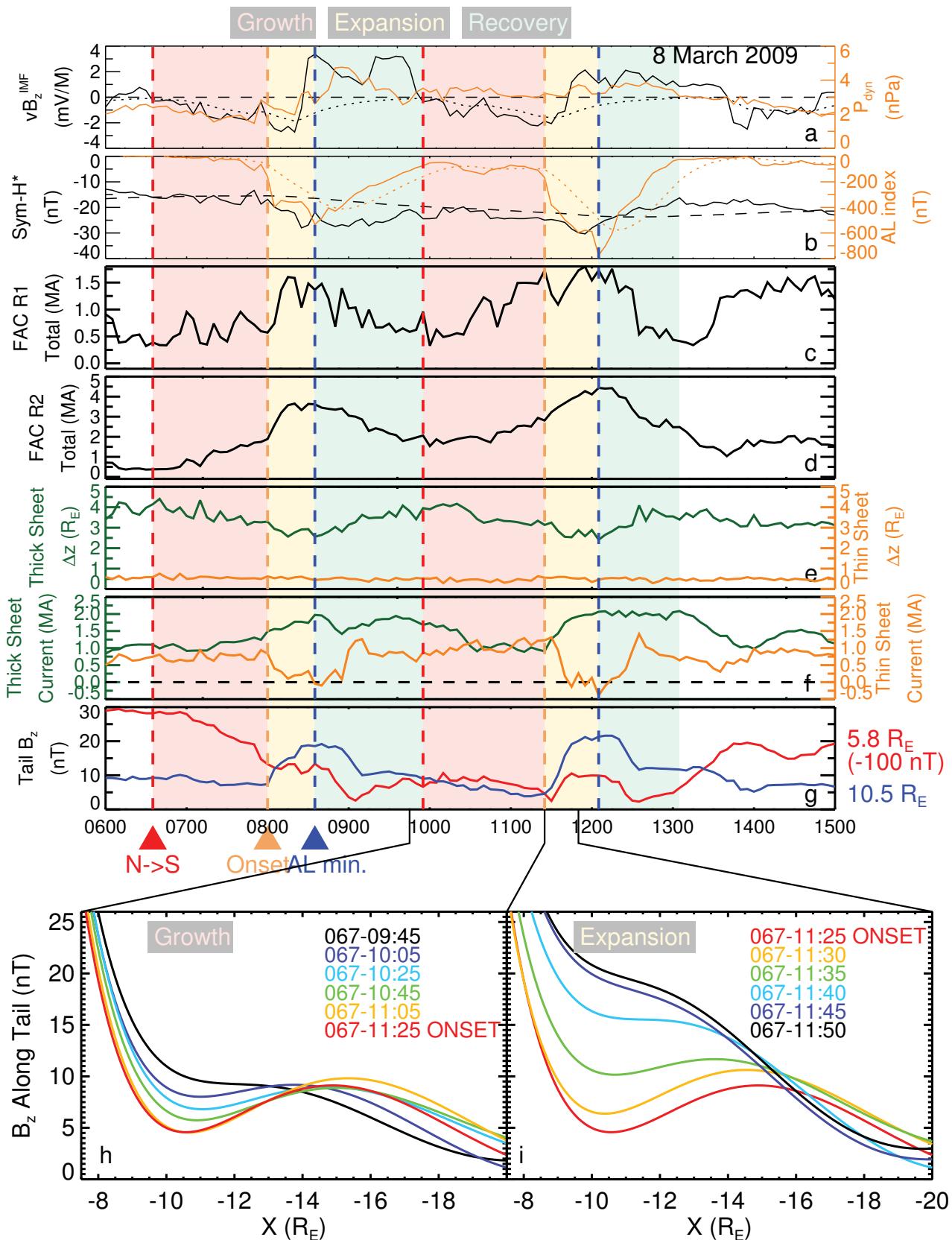


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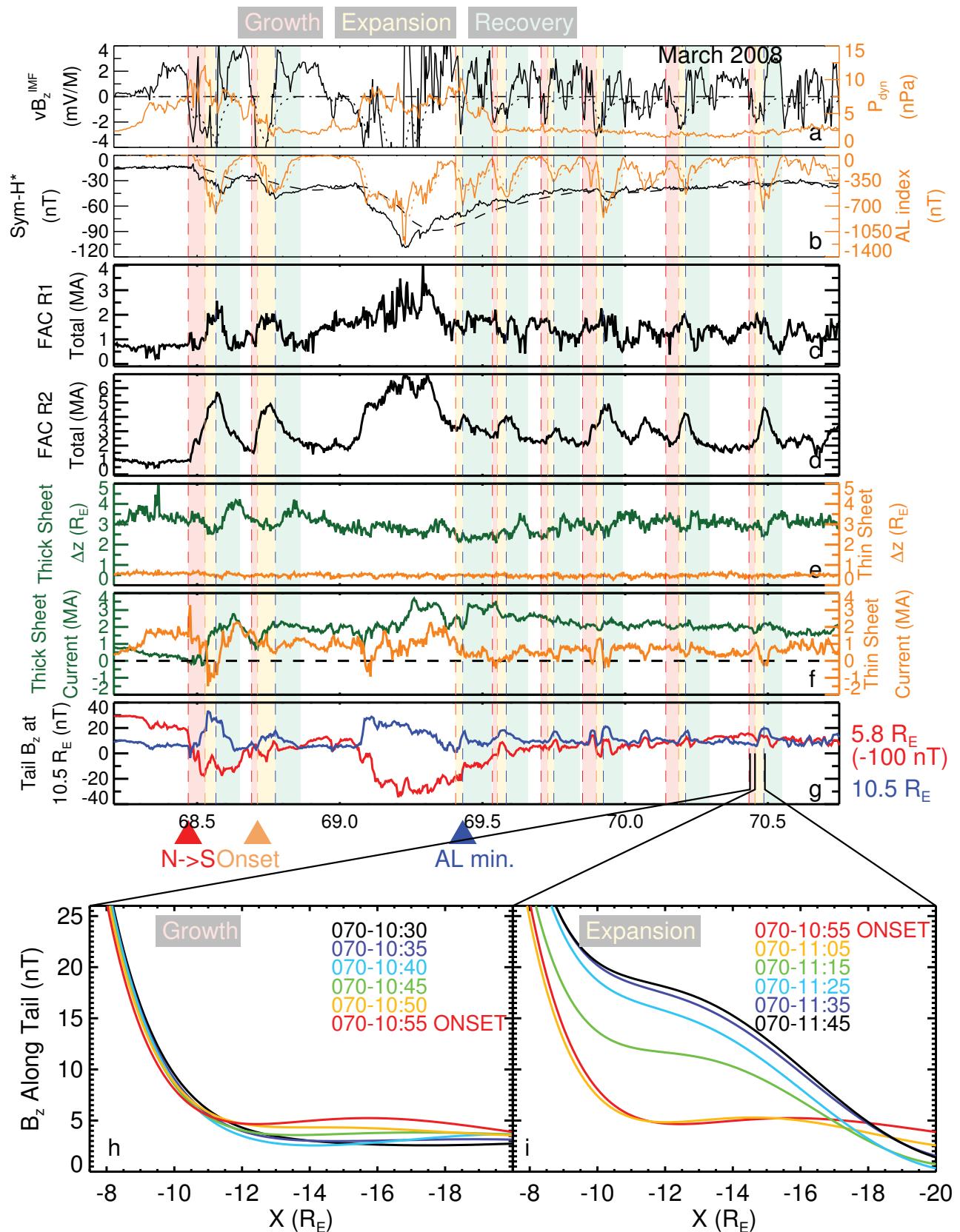
### Recovery 2009-067 (March-08) 12:50



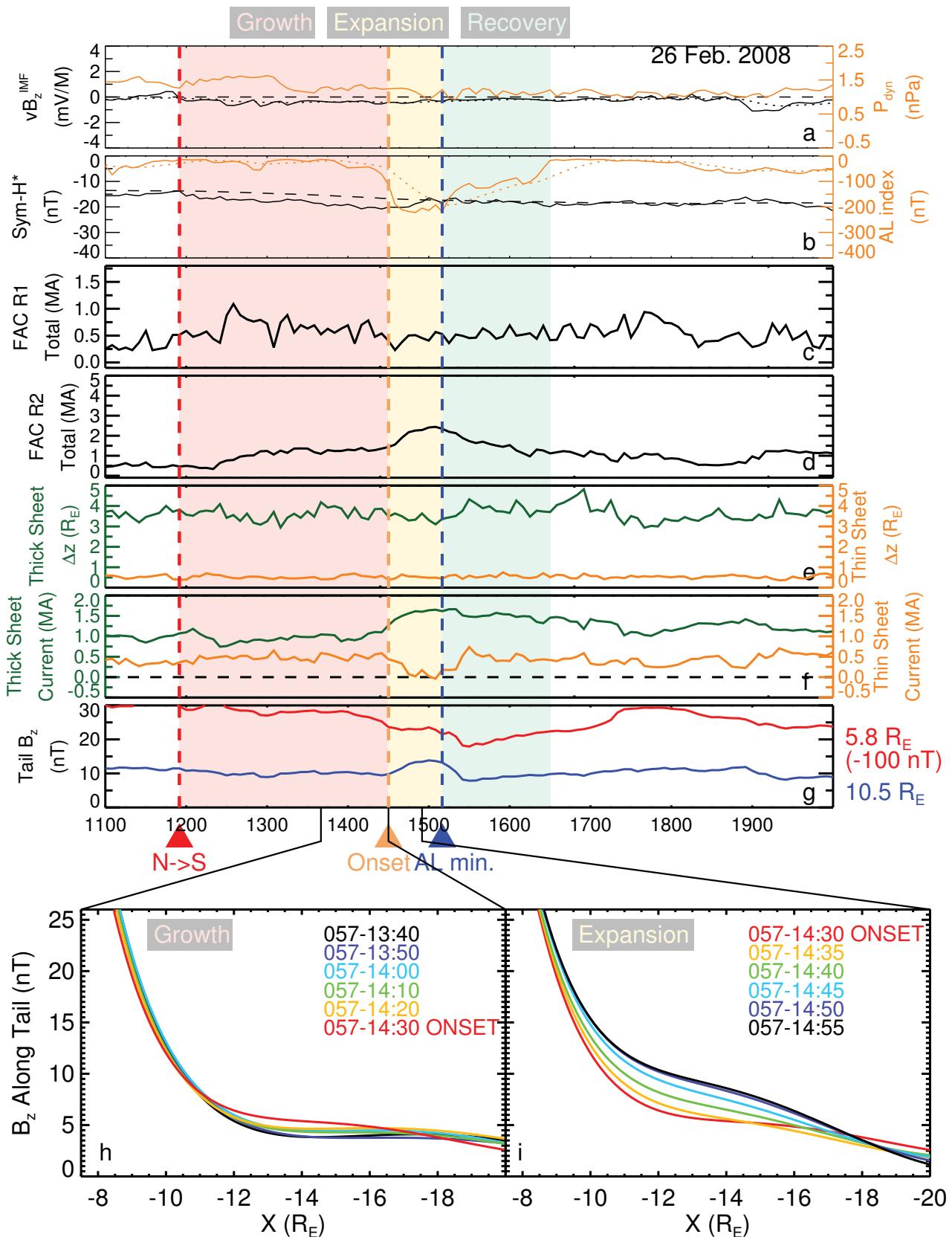




F07.

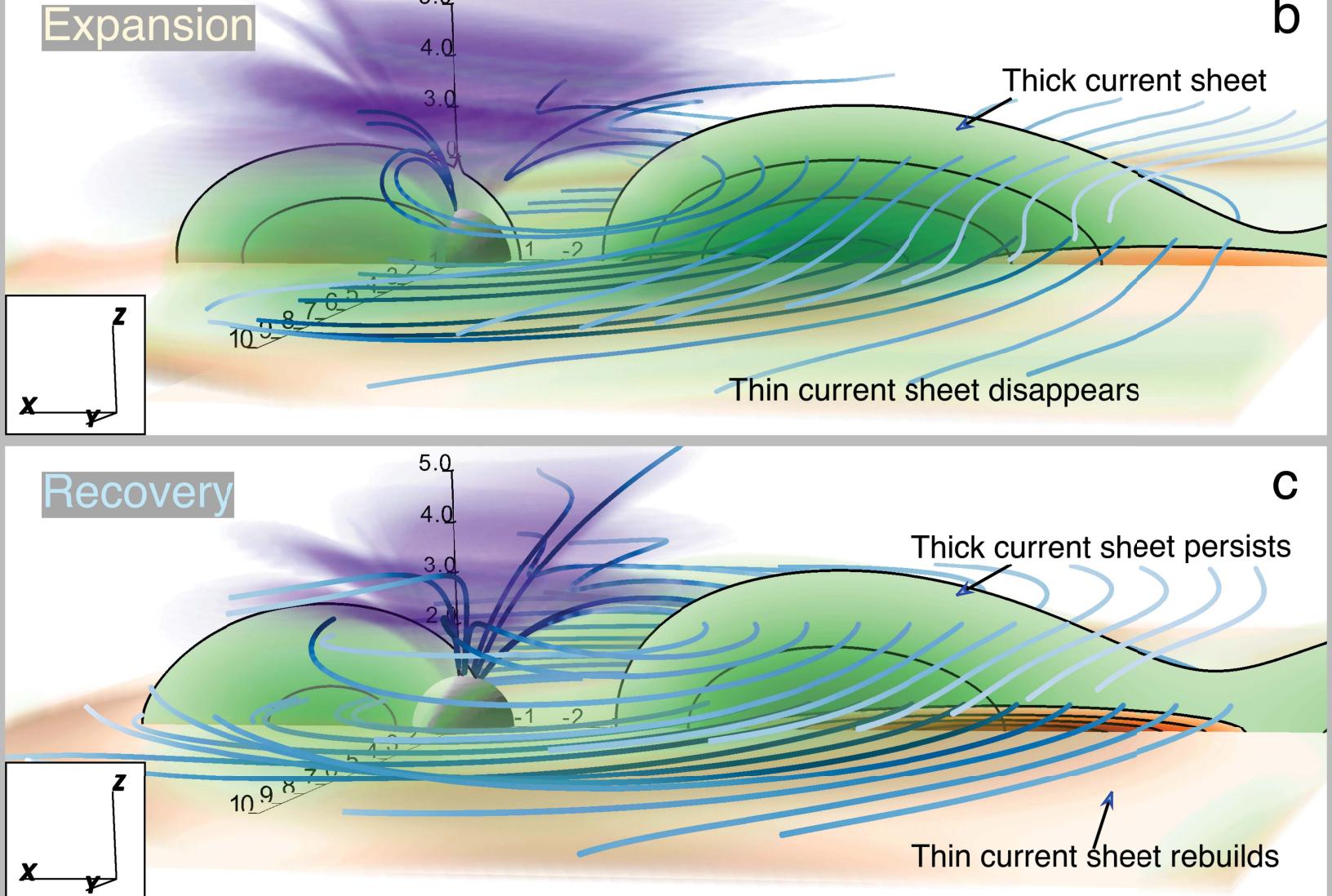




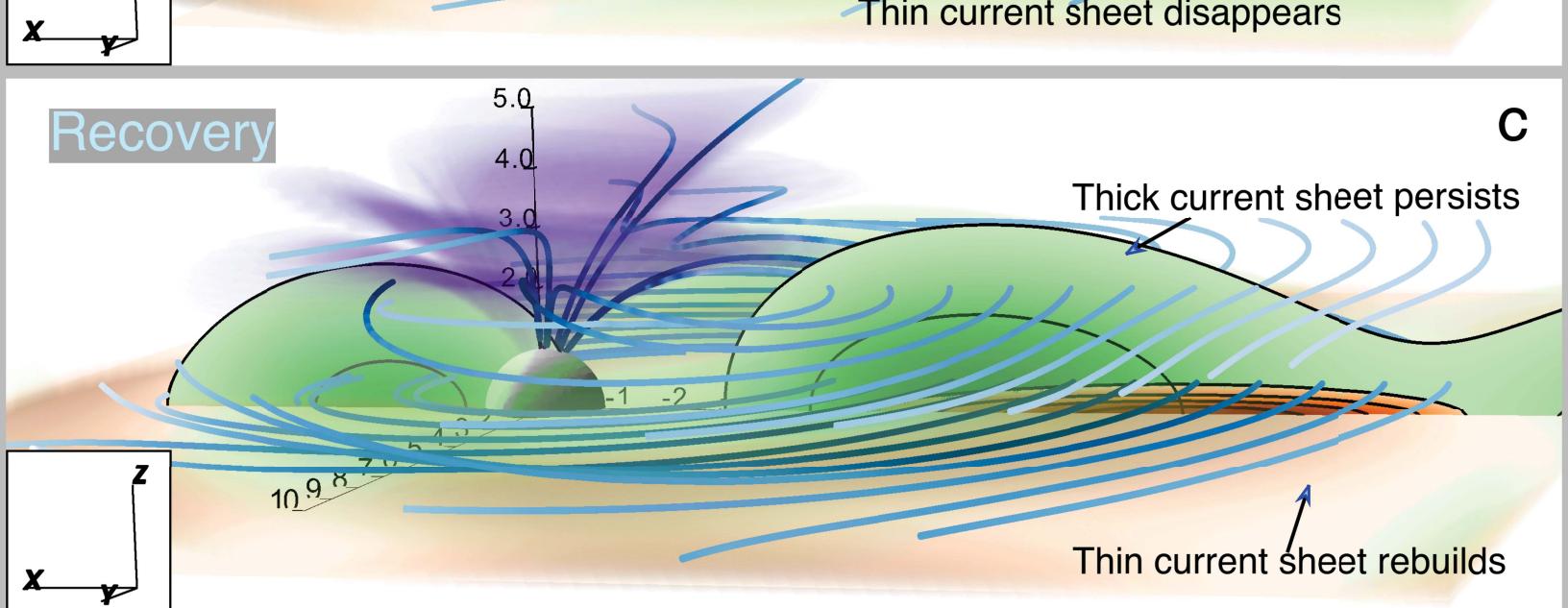


F09.

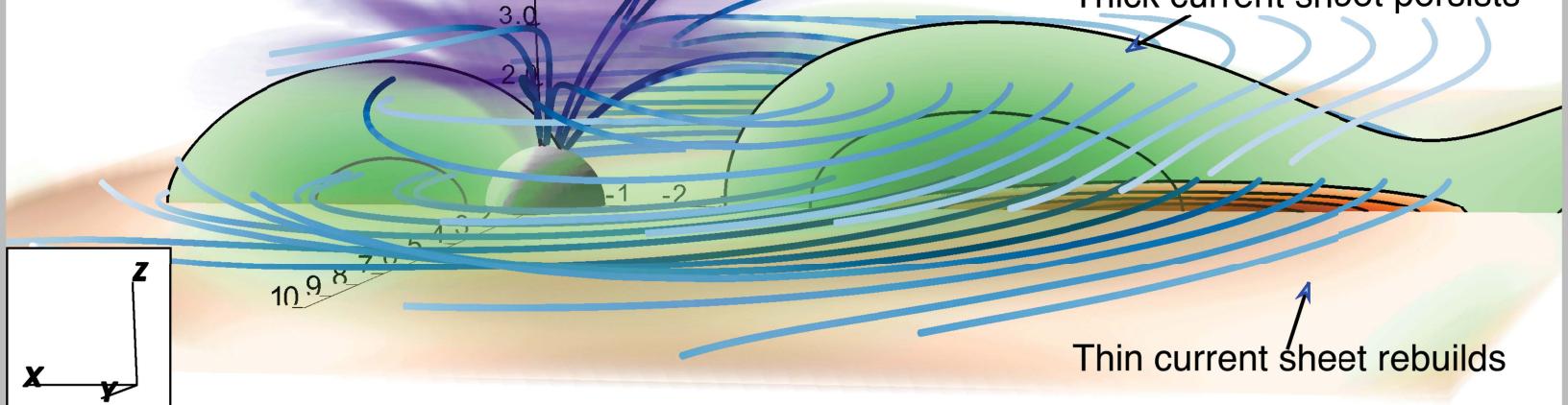
## Growth



## Expansion



## Recovery

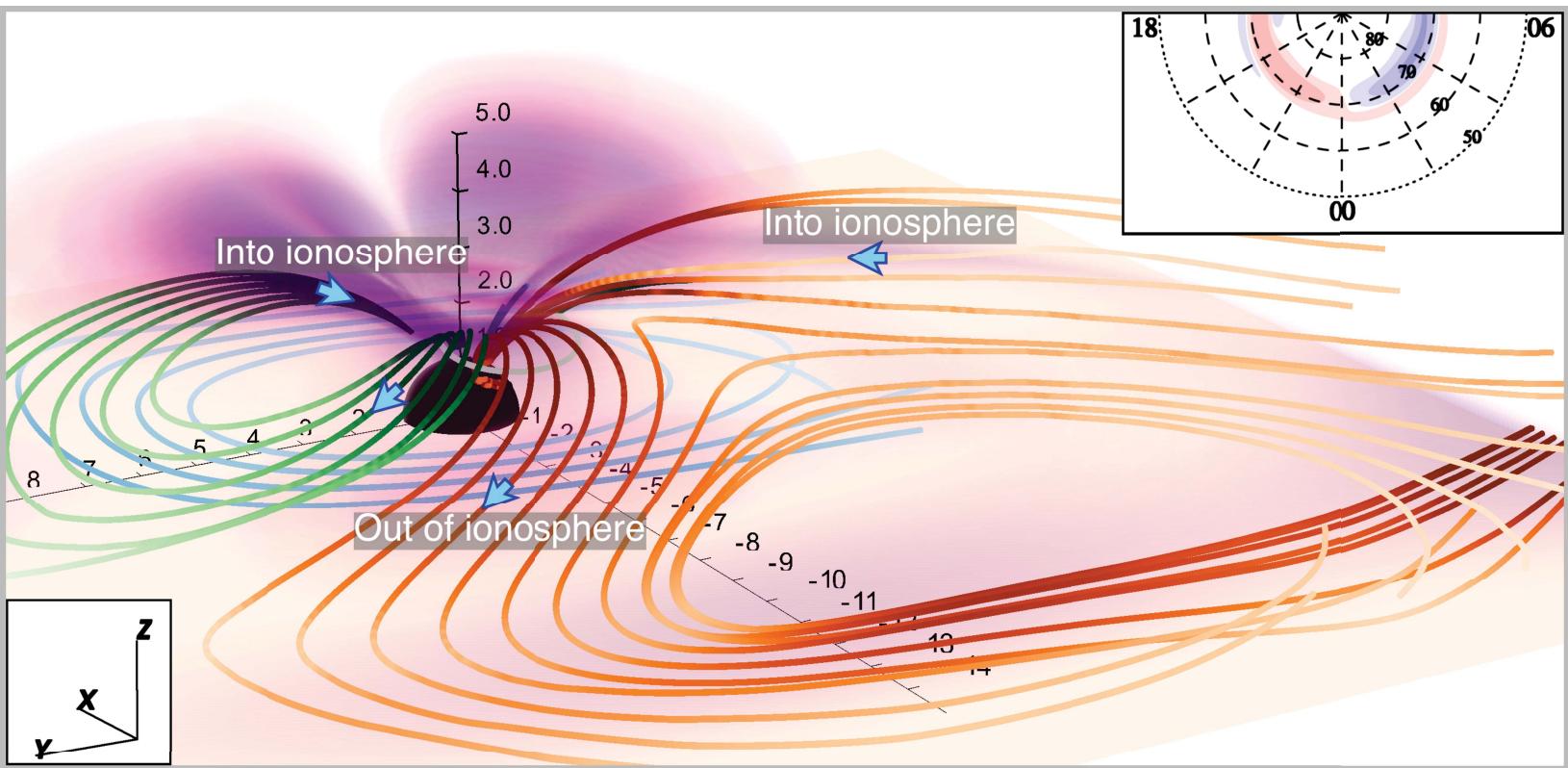


a

b

c

F01.





# Substorm current wedge

2009-067 (March-08)

