

# Band-to-band transitions and critical points in the near-infrared to vacuum ultraviolet dielectric functions of single crystal urania and thoria

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## ABSTRACT

Band-to-band transition energy parameters for single-crystal actinide samples of uranium oxide and thorium oxide were determined and compared using spectroscopic ellipsometry and critical-point dielectric function analyses. Spectroscopic ellipsometry measurements from the near-infrared to the vacuum ultraviolet spectral region were used to determine the dielectric functions of uranium oxide and thorium oxide. The critical-point structure is similar between  $\text{UO}_2$  and  $\text{ThO}_2$  but strongly blue shifted for  $\text{ThO}_2$ . We find bandgap energies of 2.1 eV and 5.4 eV for  $\text{UO}_2$  and  $\text{ThO}_2$ , respectively.

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Uranium dioxide (urania),  $\text{UO}_2$ , and thorium dioxide (thoria),  $\text{ThO}_2$ , have garnered interest recently as semiconductors suitable for neutron detection.<sup>1,2</sup> Present knowledge of the electronic and optical properties of  $\text{ThO}_2$  is scarce. Knowledge for  $\text{UO}_2$  is also not exhaustive. Until recently, experimental studies of optical and electronic properties of  $\text{UO}_2$  and  $\text{ThO}_2$  have been limited due to the nonavailability of single-crystal samples of optical quality. Our previous research on these samples indicates high-quality ordered structures of near stoichiometric  $\text{UO}_2$  as indicated by core level photoemission

spectroscopy and other techniques<sup>3–7</sup> and compared to previous measurements of growth by other processes.<sup>8</sup> This study is a continuation of the previous work given that we have evidence that we have near-stoichiometric  $\text{UO}_2$ <sup>3,5,9,10</sup> and  $\text{ThO}_2$ <sup>6,7,9</sup> permitting detailed analysis of their optical properties.

Few measurements of optical properties in the near-infrared to ultraviolet spectral region exist for  $\text{UO}_2$ : Schoenes studied reflectance from  $\text{UO}_2$  single crystals in the range of 0.03 eV–13 eV and determined the complex-valued dielectric function,  $\epsilon = \epsilon_1 + i\epsilon_2$ , from

numerical Kramers–Kronig integral calculations.<sup>8</sup> Meek *et al.* measured transmission of  $\text{UO}_2$  thin films and determined the absorption properties.<sup>11</sup> He *et al.* used spectroscopic ellipsometry and density functional theory to explore the bandgap of uranium oxide thin films with various compositions.<sup>12</sup> Siekhaus and Crowhurst<sup>13</sup> and Dugan *et al.*<sup>3</sup> used spectroscopic ellipsometry to determine the critical-point structures in  $\epsilon$ . Critical-point structures are associated with singularities in the joint density of states and caused by electronic band-to-band transitions.<sup>14</sup> Critical-point features have different shapes corresponding to the type of the band structure singularities and can be characterized by critical-point transition energy, broadening, and amplitude parameters. For  $\text{UO}_2$ , significant shifts were observed previously in the optical critical-point features obtained by reflectivity<sup>9</sup> and by ellipsometry.<sup>3,13</sup> No measurements of optical properties have been reported thus far for  $\text{ThO}_2$ .

Both uranium and thorium are similar with 6 valence electrons in uranium (electron configuration  $[\text{Rn}] 5f3 6d1 7s2$ ) and 4 valence electrons in thorium ( $[\text{Rn}] 6d2 7s2$ ). Their oxides are equivalent in structure, fluorite (cubic), and similar in unit cell dimensions. A comparison of the dielectric functions of single-crystal  $\text{UO}_2$  and  $\text{ThO}_2$  is now possible from analysis of spectroscopic ellipsometry measurements from the near-infrared to vacuum ultraviolet spectral region. We performed a critical-point analysis on the dielectric functions and compared the band-to-band transition parameters obtained from the analysis for the two actinide oxides.

In order to obtain meaningful physical information from spectroscopic ellipsometric data, appropriate physical models must be utilized for data analysis.<sup>15</sup>  $\text{UO}_2$  and  $\text{ThO}_2$  are both optically isotropic, and hence, it is assumed here that no polarization mode conversion between parallel (*p*) and perpendicular (*s*) occurs upon reflection of the light from the surfaces of the single crystals. The substrate–ambient boundary condition approximation was chosen, where the single-crystal actinides are considered as optically thick, quasihalf-infinite substrates.<sup>16</sup> Finite roughness at the single crystal–ambient interface affects the spectroscopic ellipsometry data and must be accounted for. Specifically, mechanically polished single crystal surfaces contain residual surface defect regions. An effective medium approximation was used to mimic the effects of physical surface roughness by an effective over-layer with effective dielectric function values and with effective thicknesses much smaller than the wavelengths.<sup>16</sup> Typically, the surface roughness layer thickness corresponds to the average physical roughness surface height variation.<sup>17</sup> Here, the dielectric function of the surface roughness layer was calculated by averaging  $\epsilon$  of the actinide single crystal with void ( $\epsilon = 1$ ) with a variable volume ratio. The remaining model parameters are then the thickness of the surface roughness layer and the real and the imaginary parts of  $\epsilon$  for every wavelength. Thus, a wavelength-by-wavelength regression analysis was utilized to determine all unknown parameters.

The optical critical-point features govern the spectral shape of the dielectric function of materials in the band-to-band transition spectral region. Critical-point structures can be rendered by model dielectric function approaches. The critical-point features are accounted for by 5 Gaussian-broadened oscillators, to render the imaginary part for each of their critical-point contribution,  $n$ ,

$$\epsilon_2(E) = \sum_{n=1}^N A_n \left[ e^{-\left(\frac{E-E_n}{\sigma_n}\right)^2} - e^{-\left(\frac{E+E_n}{\sigma_n}\right)^2} \right], \quad (1)$$

where

$$\sigma_n = \frac{B_n}{2\sqrt{\ln(2)}}, \quad (2)$$

and the real part of  $\epsilon$  is obtained from Kramers–Kronig integration

$$\epsilon_1(E) = \epsilon_\infty + \frac{2}{\pi} P \int_0^\infty \frac{\xi \epsilon_2(\xi)}{\xi^2 - E^2} d\xi. \quad (3)$$

Here,  $A_n$ ,  $E_n$ , and  $B_n$  denote the  $n$ th-critical-point amplitude, transition energy, and transition broadening parameters, respectively.  $E$  is the photon energy, and  $\epsilon_\infty$  is the static contribution to the dielectric function.<sup>3,18</sup>

The hydrothermal synthesis technique was used to grow  $\text{ThO}_2$  and  $\text{UO}_2$  single crystals for this study. Growth procedures for  $\text{ThO}_2$  and  $\text{UO}_2$  were quite similar in temperature, pressure, and mineralizer solution. The mineralizer solution for both growth reactions was a 6 M cesium fluoride solution (Alfa Aesar, 99.99%). Growth reactions were contained in sealed silver ampoules (99.95% Ag, Refining Systems Inc.) to minimize impurities that could be leached from the walls of the Inconel autoclave. These were sealed at either end via welding. For the  $\text{ThO}_2$  sample, a seed crystal of  $\text{ThO}_2$  was suspended in the upper portion of the silver tube on a silver seed rack. A charge of  $\text{ThO}_2$  nutrient/feedstock (99.99% thorium oxide, International Bio-analytical Laboratories) was placed in the lower portion of the tube with a porous silver baffle separating the feedstock and the seed crystal. The baffle limits thermal mixing and ensures two distinct temperature regions in the tube. Once fully assembled, the silver tubes were placed in a 250 ml Inconel autoclave. Counter-pressure water was added to 80%–85% of the remaining volume to prevent the silver tube from rupturing due to pressure from the mineralizer solution.

Band heaters were placed on the autoclave to form two temperature zones that correspond to the feedstock and seed crystal zones. The cesium fluoride solution dissolves the feedstock at the higher temperature (dissolution) zone and forms a saturated solution. By adjusting the seed crystal (crystallization zone) to a lower temperature, a natural convective flow was established, thereby circulating the saturated solution to the cooler region. The lower temperature results in a supersaturated solution and  $\text{ThO}_2$  is precipitated from solution onto the seed crystal. For  $\text{ThO}_2$ , the dissolution zone temperature was 650 °C and the crystallization zone was 600 °C, which generated a pressure of 172 MPa. These conditions were maintained for 90 days. Upon cooling, the  $\text{ThO}_2$  seed crystal was extracted from the silver tube and rinsed to remove the residual cesium fluoride mineralizer. The  $\text{UO}_2$  sample was also grown on a  $\text{ThO}_2$  seed crystal, as no large  $\text{UO}_2$  substrates/seeds were available. The mineralizer solution, temperatures, and pressures were exactly the same for the  $\text{UO}_2$  (99.998% uranium oxide, International Bio-analytical Laboratories) growth procedure, although the growth was only maintained for 50 days.

Both samples were ground flat along the (100) crystallographic plane and polished. The samples were sonicated in both acetone and de-ionized water to remove residual crystal bond and loose particulates.

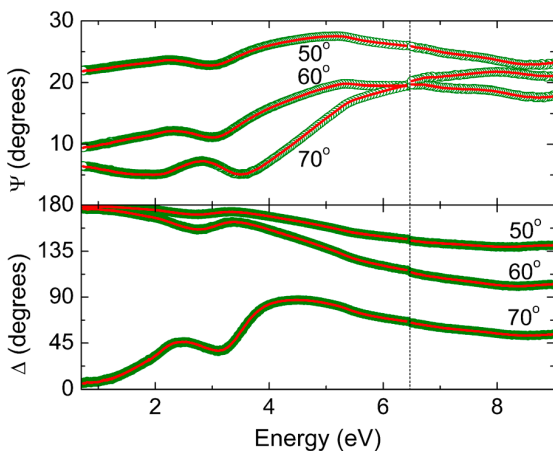
Lattice parameters for  $\text{ThO}_2$  and  $\text{UO}_2$  were obtained via single crystal X-ray diffraction (XtaLAB mini, Rigaku). Due to the excessive size of the  $\text{ThO}_2$  and  $\text{UO}_2$  crystals used in the ellipsometry measurements, lattice parameters could not be determined directly from these samples. Smaller spontaneously nucleated crystals of  $\text{ThO}_2$  and  $\text{UO}_2$

grown under similar conditions were used to measure the representative lattice parameters. For  $\text{ThO}_2$ , the lattice parameter was  $(5.6070 \pm 0.0006)$  Å, which is consistent with the expected value of  $a = 559.7$  pm.<sup>19</sup> The lattice parameters of  $\text{UO}_2$  were observed in previous publications as  $(5.4703 \pm 0.0006)$  Å corresponding to a stoichiometry of  $\text{UO}_{2.003}$ .<sup>20,21</sup> Further discussion and evidence supporting stoichiometric nature of these samples can be found in the [supplementary material](#).

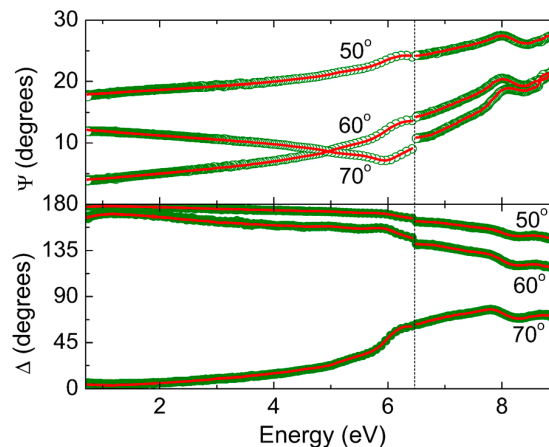
Spectroscopic ellipsometry data were collected from 0.75 eV to 6.4 eV with a dual-rotating compensator ellipsometer (RC2, J. A. Woollam Co., Inc.) as shown in Figs. 1 and 2. Data were acquired at seven angles of incidence ( $\Phi_a = 45^\circ, 50^\circ, 55^\circ, 60^\circ, 65^\circ, 70^\circ$ , and  $75^\circ$ ); however, while all are used in the data analysis, only three are shown for clarity. The spectral resolution from this instrument is 1 nm.

In the spectral range from 5 eV to 9 eV, data were collected with a nitrogen-purged rotating analyzer ellipsometer (VUV-VASE, J. A. Woollam Co., Inc.). In this region, data were acquired at three angles of incidence ( $\Phi_a = 50^\circ, 60^\circ$ , and  $70^\circ$ ). The resolution for this measurement was chosen to be 0.02 eV. Note also that although there is a significant overlap in the acquired data range, we show only data from 6.5 eV and above in Figs. 1 and 2 for clarity, with a dashed vertical line indicating the switch.

Figures 1 and 2 show experimental (symbols) and best-match model calculated (solid lines) spectroscopic ellipsometry data from multiple angles of incidence for the  $\text{UO}_2$  and  $\text{ThO}_2$  single crystals, respectively. We note excellent agreement between experimental data and model simulation data. The model simulation data were obtained by wavelength-by-wavelength determining  $\epsilon$  and the surface roughness effective layer thickness. For the  $\text{UO}_2$  crystal, we obtain a roughness effective layer thickness of approximately 4 nm, assuming that the roughness effective layer is formed from a 50:50 volume ratio of void and  $\text{UO}_2$  material (dielectric function). For  $\text{ThO}_2$ , we obtain a roughness effective layer with a 10:90 volume ratio of void and  $\text{ThO}_2$ , with effective roughness layer thickness values of approximately 10 nm and 20 nm, differing between the VUV and RC2 measurements,

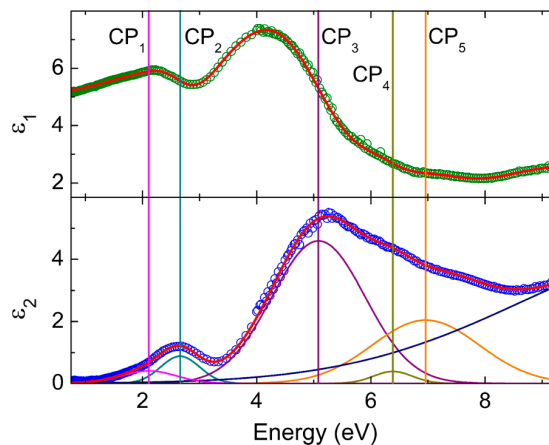


**FIG. 1.** Experimental (open symbols:  $\Psi$ , closed symbols:  $\Delta$ ) and best-match model calculated spectroscopic ellipsometry data (solid lines) for spectroscopic ellipsometry data measured at multiple angles of incidence for the  $\text{UO}_2$  single crystal sample. The dashed vertical line indicates instrument switch at 6.5 eV.



**FIG. 2.** Same as Fig. 1 for the  $\text{ThO}_2$  single-crystal sample.

respectively, which we identify as caused by surface effects due to the crystal polishing processes. The submicroscopic surface roughness also causes an angular spread of the reflected measurement beams, which enter the model analysis by considering the apertures of the two instruments. This modification of the model analysis consists of the consideration of a reflected beam with a spread over the angle of incidence which corresponds to the entrance pupil of the detector. This entrance is larger for the VUV instrument (approximately  $8^\circ$ ) than for the near-IR-VIS instrument (approximately  $3^\circ$ ). As a result, for the  $\text{ThO}_2$  sample, a small offset is seen for the ellipsometry data across the spectral transition between the two instruments (Fig. 2). Note that this offset is purely instrumental and due to surface roughness, and both effects are thereby removed numerically as shown in the resulting dielectric function for  $\text{ThO}_2$  in Fig. 4. Figures 3 and 4 depict the real



**FIG. 3.** Real (green symbols) and imaginary parts (blue symbols) of  $\epsilon$  for the  $\text{UO}_2$  single-crystal sample obtained from the wavelength-by-wavelength spectroscopic ellipsometry data analysis. Shown in comparison are the individual (solid lines) and total (red lines) critical-point transition contributions. Vertical lines indicate the individual critical-point transition energy parameters.

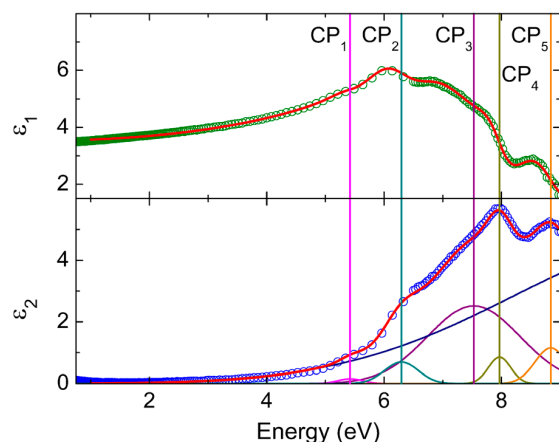


FIG. 4. Same as Fig. 3 for the ThO<sub>2</sub> single-crystal sample.

and imaginary parts of  $\epsilon$  for UO<sub>2</sub> and ThO<sub>2</sub>, respectively, obtained from our data analyses (symbols). For both samples, we observe a vanishing imaginary part of the dielectric response toward the near-infrared spectral range, indicative of a semiconductor material with nonvanishing bandgap energy. We observe a long tail-like feature in the ThO<sub>2</sub> dielectric function below the bandgap, indicative of the existence of crystalline defects within the ThO<sub>2</sub> sample.

Figures 3 and 4 also show the best-match model calculated critical-point contributions identified within our critical-point model analysis (solid lines). The individual critical-point contributions and their corresponding band-to-band transition center energy parameters are shown in the imaginary part of the dielectric functions with color coordinated vertical lines, in Figs. 3 and 4, thereby identifying the center energy,  $E_n$ , of each Gaussian oscillator rendering as close as possible the wavelength-by-wavelength determined functions  $\epsilon$  for UO<sub>2</sub> and ThO<sub>2</sub>, respectively. Table I and Table II list all critical-point parameter values within the investigated spectral range for the UO<sub>2</sub> single-crystal sample and for the ThO<sub>2</sub> single-crystal sample, respectively. We observe a large tail in the imaginary part of the dielectric function of ThO<sub>2</sub> below the bandgap which we model with a very broad Gaussian oscillator centered at higher energy outside the investigated spectral range. This oscillator also accounts for all higher energy transitions which contribute to the dielectric function and a similar oscillator

TABLE I. Critical-point parameters: amplitude ( $A_n$ ), transition energy ( $E_n$ ), and broadening ( $B_n$ ) for the UO<sub>2</sub> dielectric function within the investigated spectral region. Digits in parentheses indicate the 90% confidence interval obtained from numerical best-match model analysis. A static contribution to the dielectric function near unity  $1.02 \pm 0.02$  was found for the real part of the dielectric function of UO<sub>2</sub>.

$n$	$A_n$ (eV)	$E_n$ (eV)	$B_n$ (eV)
1	0.4 (0)	2. (1)	1. (1)
2	0. (8)	2.6 (6)	0.8 (0)
3	4.5 (9)	5.0 (8)	1.9 (3)
4	0.3 (9)	6.3 (9)	0.8 (1)
5	2.0 (4)	6.9 (6)	2.2 (1)

TABLE II. Same as Table I for ThO<sub>2</sub>. A static contribution to the dielectric function of  $1.01 \pm 0.01$  was determined for the real part of the dielectric function of ThO<sub>2</sub>.

$n$	$A_n$ (eV)	$E_n$ (eV)	$B_n$ (eV)
1	0.1 (2)	5.4 (4)	0.4 (3)
2	0.6 (7)	6.3 (5)	0.6 (6)
3	2.2 (3)	7.5 (0)	1.6 (3)
4	1.1 (8)	7.96 (5)	0.4 (5)
5	0.9 (9)	8.82 (6)	0.5 (9)

centered at higher energy was used in the UO<sub>2</sub> critical-point analysis as well.

The five distinct critical-point features in the optical response of both actinide oxides are enumerated on the order of ascending transition energy ( $n = 1, 2, 3, 4$ , and  $5$ ). These features are plotted using the same color codes in Figs. 3 and 4. In both cases, the 3rd ( $n = 3$ ) critical-point features are the strongest contributions to the respective dielectric functions. As noted at the outset, while uranium and thorium have quite distinct configurations of valence electrons (uranium: [Rn]  $5f^3 6d^1 7s^2$ ; thorium: [Rn]  $6d^2 7s^2$ ), UO<sub>2</sub> and ThO<sub>2</sub> have many similarities, as is also evident from this work. Uranium's  $5f$  electrons are not expected to participate in bonding and hence both actinide oxides crystallize in the same cubic fluorite structure, with only a slightly higher lattice constant for ThO<sub>2</sub>.

The lowest critical-point transition energies,  $E_{\text{UO}_2,1} = 2.1$  eV and  $E_{\text{ThO}_2,1} = 5.4$  eV, are the fundamental band-to-band transition energy (bandgap energy) of the respective oxide. In spite of many similarities, it is clear that the critical-point features are sharper and more closely spaced for the wider bandgap material (ThO<sub>2</sub>). This is expected for a wide bandgap oxide. In the case of UO<sub>2</sub>, this experimentally determined lowest critical-point transition energy shows excellent agreement with the previously published results of band structure calculations, which predicted a bandgap energy of 2.19 eV.<sup>3</sup> Several studies have been conducted of the band structure of ThO<sub>2</sub>.<sup>22–24</sup> The calculated values of the bandgap span a broad range of 3.3–6.9 eV. Our experimental value of 5.4 eV falls somewhere in the middle of this broad range but does not seem to match any specific published values.

In summary, high-quality, single-crystal actinide oxide samples of uranium oxide and thorium oxide were synthesized and investigated by structural and optical methods. A spectroscopic ellipsometry analysis determined the dielectric functions for both oxides, which reflect critical-point structures similar in appearance but shifted in photon energy. Five critical-point structures are observed in both materials, where the lowest bandgap energies of 2.1 eV are found for UO<sub>2</sub> and 5.4 eV for ThO<sub>2</sub>. A strong blue shift by approximately 2–3 eV is obtained for all band-to-band transitions in ThO<sub>2</sub> with respect to UO<sub>2</sub>.

See the [supplementary material](#) for details related to thorium and uranium sample quality, stoichiometry, and electronic structure.

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