



# First Measurement of the Hubble Constant from a Dark Standard Siren using the Dark Energy Survey Galaxies and the LIGO/Virgo Binary–Black-hole Merger GW170814

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## Abstract

We present a multi-messenger measurement of the Hubble constant  $H_0$  using the binary–black-hole merger GW170814 as a standard siren, combined with a photometric redshift catalog from the Dark Energy Survey (DES). The luminosity distance is obtained from the gravitational wave signal detected by the Laser Interferometer Gravitational-Wave Observatory (LIGO)/Virgo Collaboration (LVC) on 2017 August 14, and the redshift information is provided by the DES Year 3 data. Black hole mergers such as GW170814 are expected to lack bright electromagnetic emission to uniquely identify their host galaxies and build an object-by-object Hubble diagram. However, they are suitable for a statistical measurement, provided that a galaxy catalog of adequate depth and redshift completion is available. Here we present the first Hubble parameter measurement using a black hole merger. Our analysis results in  $H_0 = 75^{+40}_{-32} \text{ km s}^{-1} \text{ Mpc}^{-1}$ , which is consistent with both SN Ia and cosmic microwave background measurements of the Hubble constant. The quoted 68% credible region comprises 60% of the uniform prior range  $[20, 140] \text{ km s}^{-1} \text{ Mpc}^{-1}$ , and it depends on the assumed prior range. If we take a broader prior of  $[10, 220] \text{ km s}^{-1} \text{ Mpc}^{-1}$ , we find  $H_0 = 78^{+96}_{-24} \text{ km s}^{-1} \text{ Mpc}^{-1}$  (57% of the prior range). Although a weak constraint on the Hubble constant from a single event is expected using the dark siren method, a multifold increase in the LVC event rate is anticipated in the coming years and combinations of many sirens will lead to improved constraints on  $H_0$ .

*Key words:* catalogs – cosmology: observations – gravitational waves – surveys

## 1. Introduction

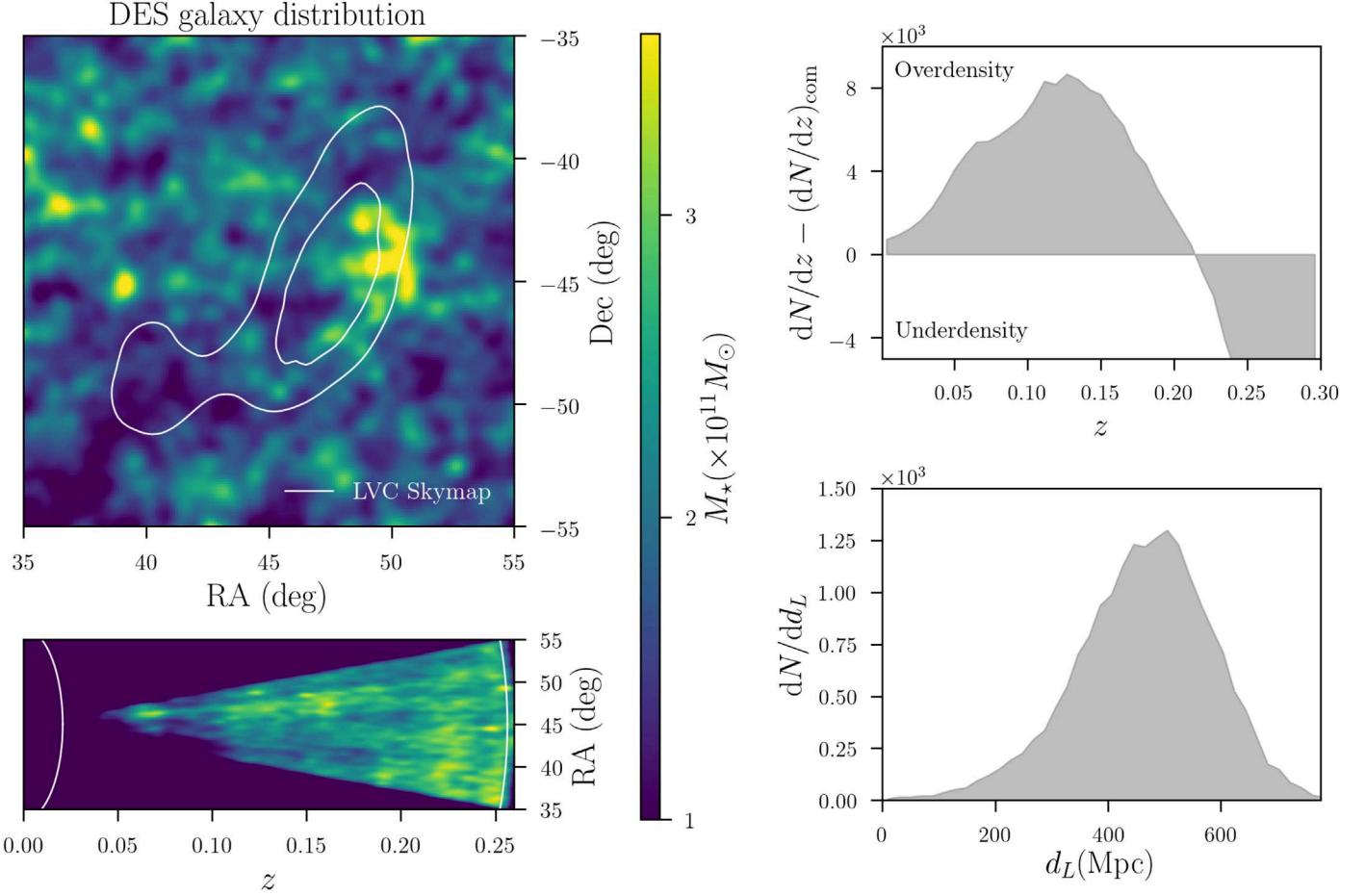
Unlike most extragalactic distance observables, mergers of neutron star and black hole binary systems are absolute distance indicators. Often referred to as “standard sirens,” they emit gravitational waves (GWs) from which the luminosity distance can be inferred without relying on any calibration with respect to another source: the rate of change in frequency gives the system’s size and thus the intrinsic amplitude, which is compared against the observed signal amplitude to obtain the distance to the source. If redshifts are associated with those sirens (in the simplest case, the host galaxy is identified and its redshift is obtained via spectroscopic follow up), a measurement of the present rate of expansion of the universe  $H_0$  can be achieved via the distance-redshift relation. The use of GW sources as cosmological probes was first proposed by Schutz (1986), and recently revisited in several works (e.g., Holz & Hughes 2005).

For dark energy research, the possibility of measuring  $H_0$  directly and independently from other methods is of great interest. Local measurements obtained from SN Ia and other distance indicators, as well as the predicted value inferred from the cosmic microwave background (CMB) at  $z \sim 1100$ , have achieved remarkable precision of 1%–2.5% (e.g., Planck Collaboration et al. 2018; Riess et al. 2018). They disagree, however, by more than  $3\sigma$  and interpreting this tension as evidence for beyond- $\Lambda$ CDM dark energy or new physics at the early universe requires new measurements of great precision and accuracy (Freedman 2017; Mörtsell & Dhawan 2018). Those measurements are one of the greatest challenges faced by current experiments in cosmology because the observables are subject to correlated systematic effects arising from their complex astrophysics. As estimates become more precise, this challenge becomes more severe and the need for novel independent methods becomes more pressing. Those methods, however, are few and hard to come by. One possibility is standard sirens, which remained elusive for almost 30 yr, until the detection of the first GW event (GW150914; Abbott et al. 2016). The first standard siren-based  $H_0$  measurement (Abbott et al. 2017a) came with the discovery of the binary–neutron-star (BNS) merger GW170817 (Abbott et al. 2017) and its associated electromagnetic counterpart (Arcavi et al. 2017; Coulter et al. 2017; LIGO Scientific Collaboration et al. 2017; Lipunov et al. 2017; Soares-Santos et al. 2017; Tanvir et al. 2017; Valenti et al. 2017). Several studies have developed

methodologies to infer cosmological parameters from standard sirens and establish their constraining power (Schutz 1986; Holz & Hughes 2005; MacLeod & Hogan 2008; Nisanke et al. 2010, 2013; Del Pozzo 2012; Nishizawa 2017; Chen et al. 2018; Feeney et al. 2019; Mortlock et al. 2018; Vitale & Chen 2018). Chen et al. (2018) predicted that we will be able to constrain  $H_0$  with 2% precision within 5 yr with standard sirens detected by the Laser Interferometer Gravitational-Wave Observatory (LIGO)/Virgo, while Nair et al. (2018) predicted a ~7% measurement with just 25 binary–black-hole (BBH) events from the Einstein telescope.

Anticipating that the LIGO/Virgo Collaboration (LVC) network of GW detectors would eventually achieve sensitivity sufficient to enable standard siren-based measurements, the Dark Energy Survey (DES) collaboration and external collaborators launched in 2015 the DES gravitational waves (DESGW) program. DESGW uses the Dark Energy Camera (DECam) to search for optical emission associated with LVC-detected mergers and pursues cosmological measurements with standard sirens. In particular, the multi-messenger shared discovery of the neutron-star merger GW170817, and of its optical kilonova, resulted in a measurement of  $H_0$  (Abbott et al. 2017a) that inaugurated the era of siren-based cosmology. We have also performed the most comprehensive searches for optical emission to black hole events, including GW150914 (Soares-Santos et al. 2016), GW151226 (Cowperthwaite et al. 2016), and GW170814 (Doctor et al. 2018). These events are expected to be dark, although the possibility of optical emission has yet to be observationally excluded.

Dark sirens can also be used for cosmology using a statistical method, as first proposed in Schutz (1986). Provided a catalog of potential host galaxies within the event localization region, their redshifts will contribute in a probabilistic way to the measurement of  $H_0$ , depending on the galaxies’ distance and sky position. This approach has been developed within a Bayesian framework by Del Pozzo (2012) and Chen et al. (2018) and implemented in Fishbach et al. (2019) using GW170817, which produced results consistent with the first measurement (Abbott et al. 2017a) where the identified host galaxy, NGC 4993 (e.g., Palmese et al. 2017), was used. Eventually, a large sample of events will enable precise cosmological measurements using the dark siren approach.



**Figure 1.** Left: stellar mass distribution of the DES galaxies used in this analysis (color map) and the GW170814 localization region at 50% and 90% CL (white contours). The region in redshift space is valid for the prior range  $20 < H_0 < 140 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . The stellar mass map has been smoothed with a Gaussian filter of width  $0.3^\circ$ . The bottom panel shows the galaxies' stellar mass distribution in R.A. and redshift, projected over the decl. Right: distributions of the DES galaxy redshifts within the region of interest (top) and the luminosity distance in HEALPIX pixels from the LVC distance likelihood, as given in the sky map (bottom). The histograms are obtained from a Monte-Carlo (MC) sampling the galaxies' redshift probability distribution function (PDF) and the luminosity distance likelihood in each pixel. The redshift distribution has been subtracted by a uniform distribution in comoving volume ( $dN/dz$ )<sub>com</sub>, obtained assuming  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , and containing the same total number of galaxies to highlight the overdensity of galaxies in the region.

In this work, we measure  $H_0$  using the GW event GW170814 (Abbott et al. 2017b) as a dark siren. GW170814 resulted from the inspiral and merger of a BBH system at a luminosity distance of  $540^{+130}_{-210} \text{ Mpc}$  (median value with 90% credible interval). The masses of the black holes were  $30.5^{+5.7}_{-3.0}$  and  $25.3^{+2.8}_{-4.2} M_\odot$ , respectively. GW170814 is the first BBH detected by a triple network (including LIGO Hanford and Livingston, plus Virgo), and it has the smallest localization volume of any of the BBH events detected by LVC thus far. Therefore, the number of potential host galaxies is lower compared to other events, making GW170814 the most appropriate event for this measurement. Additionally, the event localization region falls within the DES footprint, making DES galaxy catalogs a prime sample for measurement of  $H_0$ . With this one event, our goal is to provide a proof of principle measurement, addressing the challenges that are specific to the dark siren method, and establishing its potential to yield precision cosmology results in the near future.

A key component of the measurement is crafting the appropriate galaxy catalog: completeness, as well as precise and accurate photometric redshifts (photo- $z$ 's), throughout the entire volume probed are required. The overlap of GW170814's area with DES allows us to employ galaxy catalogs produced from the

first three years of the survey (DES Y3; Abbott et al. 2018). This first dark siren measurement is a step toward incorporating this new cosmological probe into the portfolio of cosmic surveys for dark energy.

A detailed description of the data used in this analysis is provided in Section 2, followed by a description of our implementation of the method in Section 3. We present our results and discussion in Section 4, and our conclusions in Section 5. Throughout this Letter we assume a flat  $\Lambda$ CDM cosmology with  $\Omega_m = 0.3$  and  $H_0$  values in the  $20\text{--}140 \text{ km s}^{-1} \text{ Mpc}^{-1}$  range. All quoted error bars represent the 68% confidence level (CL), unless otherwise stated.

## 2. Data

### 2.1. The LVC Sky Map

The sky map used in this work is the publicly available LALInference map (LIGO Scientific Collaboration & Virgo Collaboration 2017),<sup>230</sup> provided in HEALPIX (Górski et al. 2005) pixels. The luminosity distance probability distribution is approximated with a Gaussian in each pixel.

<sup>230</sup> <https://dcc.ligo.org/LIGO-T1700453/public>

The region of interest, enclosing 90% of the localization probability, is  $61.66 \text{ deg}^2$ . The projected sky map and the distribution of luminosity distance mean values from the LVC distance likelihood in each pixel within the region of interest are shown in Figure 1. The probability peak is located at R.A., decl. =  $(47^\circ 523, -44^\circ 856)$ . At the peak location, the luminosity distance is 504.7 Mpc and the Gaussian width is 91.9 Mpc. Using the limiting values of our  $H_0$  prior range ( $[20, 140] \text{ km s}^{-1} \text{ Mpc}^{-1}$ ) we can convert the 90% and 99.7% distance range into a redshift range ( $0.02 < z < 0.26$  and  $z < 0.3$ , respectively) for this analysis.

## 2.2. The DES Galaxy Catalog

The DES<sup>231</sup> (The Dark Energy Survey Collaboration 2005; Dark Energy Survey Collaboration et al. 2016) is an optical-near-infrared survey that images  $5000 \text{ deg}^2$  of the South Galactic Cap in the *grizY* bands. The survey is being carried out using a  $\sim 3 \text{ deg}^2$  charge-coupled device (CCD) camera (the DECam, see Flaugher et al. 2015) mounted on the Blanco 4 m telescope at the Cerro Tololo Inter-American Observatory (CTIO) in Chile. The data used here are from the first 3 yr of observations (2013 September–2016 February; Abbott et al. 2018).

The DES Data Management (DESDM) pipeline was used for data reduction (Morganson et al. 2018). The process includes calibration of the single-epoch images, which are co-added after background subtraction and then cut into tiles. The source catalog was created using SOURCE EXTRACTOR (SEXTRACTOR; Bertin & Arnouts 1996) to detect objects on the *riz* co-added images. The median  $10\sigma$  limiting magnitudes of Y3 data for galaxies are  $g = 24.33$ ,  $r = 24.08$ ,  $i = 23.44$ ,  $z = 22.69$ , and  $Y = 21.44$  mag (Abbott et al. 2018). The photometry used in this work is part of a value-added Y3 catalog not released with the first data release (DR1), and is the result of the Multi-Object Fitting (MOF) pipeline that uses the *ngmix* code.<sup>232</sup> Following a procedure similar to Drlica-Wagner et al. (2017) for Year 1 data, the DES collaboration made further selections to produce a high-quality object catalog called the Y3 “gold” catalog. For this sample, redshifts have been computed using the Directional Neighborhood Fitting (DNF; De Vicente et al. 2016), and they are not included in DR1.

The DNF method applied to Y3 data provides redshift information for each galaxy in the form of a probability distribution function (PDF), from which a mean redshift, and half of the central 68th percentile width, are computed. The width of the PDF can be over or underestimated due to the sampling of the training set and algorithmic details of DNF. This issue is particularly relevant for the redshift range used in this work, which is low compared to that exploited in weak lensing and large-scale structure cosmology, for which the DNF method was optimized. We find that the typical uncertainty below redshift  $z \sim 0.1$  is underestimated by a factor of 10 when compared to the typical scatter found for the subset of the galaxies with available spectroscopic redshifts (where the standard deviation is  $\sigma \gtrsim 0.015$ ). Thus, we add a minimum uncertainty of 0.015 for these low- $z$  galaxies. At  $0.1 < z < 0.3$ , the uncertainty is well behaved and the average value follows  $\bar{\sigma}_z(z) \simeq 0.013 (1 + z)^3$ , as we find using an empirical fit.

We produce alternative photo- $z$  estimates with another machine-learning code, ANNz2 (Sadeh et al. 2016). This allows us to test the impact of the correction applied to the DNF errors on the posterior of the Hubble constant. Photo- $z$  with ANNz2 have previously been validated for cosmological analyses using DES Science Verification data (Abbott et al. 2016; Bonnett et al. 2016; Leistedt et al. 2016) and for the Kilo-Degree Survey (KiDS; Bilicki et al. 2018), and are produced as part of the DES photo- $z$  pipeline (Gschwend et al. 2018). In particular, it provides error estimates through a  $k$ -nearest neighbor ( $k$ NN) method, and dedicated redshifts for the purposes of this analysis. We additionally employ a reweighting technique (Lima et al. 2008) specifically for our galaxy sample to further tune our redshifts. We run ANNz2 in randomized regression mode with 50 Boosted Decision Trees, using a spectroscopic sample of 245,458 matching Y3 galaxies out to redshift  $z \gtrsim 1$ , randomly split into subsamples for training, testing, and validation. The training and the reweighting use *griz* MOF magnitudes. We find that the typical error roughly follows  $\sim 0.02 (1 + z)^3$  in the redshift range of interest. The two algorithms, DNF and ANNz2, gave similar results; see Section 4.

These redshifts, together with publicly available spectroscopic redshifts from 2dF, 6dF, and SPT-GMOS (Colless et al. 2001; Jones et al. 2009; Bayliss et al. 2016) and the DES MOF photometry, are used to estimate galaxy properties (including stellar mass and absolute magnitude) of this sample. This is achieved through a broadband spectral energy distribution (SED) fitting of galaxy magnitudes with LEPHARE (Arnouts et al. 1999, Ilbert et al. 2006). Estimates of the galaxy properties used here from DES data alone have been tested and studied in several DES works (Palmese et al. 2016; Etherington et al. 2017; Palmese et al. 2019). We add a 0.05 systematic uncertainty in quadrature to the magnitudes, to account for systematic uncertainties in magnitude estimation and model variance.<sup>233</sup> The simple stellar population templates used for the fitting are Bruzual & Charlot (2003), with three metallicities ( $0.2 Z_\odot$ ,  $Z_\odot$  and  $2.5 Z_\odot$ ), a Chabrier (2003) initial mass function and a Milky Way (Allen 1976) extinction law with five different values between 0 and 0.5 for the  $E(B - V)$  reddening. The star formation history chosen is exponentially declining as  $e^{-t/\tau}$  with  $\tau = 0.1, 0.3, 1, 2, 3, 5, 10, 15$ , and 30 Gyr.

The source list of the Y3 gold catalog is 95% complete for galaxies within our apparent magnitude limit,  $r < 23.35$  (Abbott et al. 2018). This value is computed through the recovery rate of sources from the deeper Canada-France-Hawaii Telescope Lensing Survey (CFHTLenS; Erben et al. 2013), and thus includes the correct distribution of surface brightnesses. Nevertheless, extended, low surface brightness galaxies near our flux limit may be preferentially missed by the detection pipeline. We therefore provide an approximate completeness of sources throughout the redshift range of interest. Using DNF mean redshifts, we convert the source completeness to  $r < 23.35$  from Abbott et al. (2018, their Figure 12) into a completeness in redshift intervals,  $\Delta z = 0.02$ . By taking the peak of the magnitude distribution in each bin as roughly our observed magnitude limit at that redshift, we find our sample is  $> 93\%$  complete across the range  $0 < z < 0.26$ . We further determined that the fraction of low-redshift,

<sup>231</sup> [www.darkenergysurvey.org](http://www.darkenergysurvey.org)

<sup>232</sup> <https://github.com/esheldon/ngmix>

<sup>233</sup> This is a regularization to compensate for the synthetic model set grid and the fact that many SED fitting codes do not include a model error function. The value chosen is based on past experience of what gives stable results.

extended galaxies missed by the DES Y3 pipeline is  $\sim 1\%$ , when compared with the Two Micron All-Sky Survey (2MASS) extended source catalog (Huchra et al. 2012). For the purpose of this Letter, we choose to ignore those ultra-low- $z$  sources as most of them are at  $z < 0.02$  and are not relevant for the present analysis.

The DES Y3 gold catalog, is nonetheless, an observed magnitude-limited sample. This analysis requires a volume-limited sample, which we obtain by applying a luminosity cut. In order to determine the appropriate cut to create a volume-limited sample, we compute the completeness limits in terms of absolute quantities (luminosity and stellar mass). We follow the method outlined in Pozzetti et al. (2010) and Hartley et al. (2013). We identify galaxies with observed magnitudes that are bright enough to be complete and representative of the real galaxy population within redshift bins. To compute the 95% completeness limit in (rest-frame) luminosity, we scale the luminosities of this sample to that which they would have if their observed magnitude were equal to the survey completeness limit, and take the 95th percentile of the resulting luminosity distribution. This value corresponds to  $-17.2$  in  $r$ -band absolute magnitude and  $\sim 3.8 \times 10^8 M_\odot$  in stellar mass for the redshift range of interest. We cut the DES catalog at the specific absolute luminosity value mentioned above. We conclude that our volume-limited galaxy sample is complete within the redshift range of interest for galaxies down to stellar masses of  $\sim 3.8 \times 10^8 M_\odot$ . In other words, our galaxy catalog contains  $\sim 77\%$  of the total stellar mass in the volume considered by assuming that the galaxies follow a Schechter stellar mass function with the best-fit values from Weigel et al. (2016).

The final galaxy stellar mass and redshift distributions of galaxies are shown in Figure 1. The stellar mass map clearly shows the presence of large-scale structure, including clusters, voids, and filaments. We recognize a number of well-known clusters within the volume of interest, including several Abell clusters. A uniform distribution of galaxies in comoving volume ( $dN/dz$ )<sub>com</sub> has been subtracted from the observed galaxies' redshift distribution in Figure 1 to highlight the overdensities. The ( $dN/dz$ )<sub>com</sub> distribution has been obtained by assuming  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$  and it contains the same total number of galaxies as the observed  $dN/dz$  over the redshift range shown. We are able to identify a “wall”-like structure around  $z \sim 0.06$  spanning most of the area between  $35 < \text{R.A.} < 55$  and  $-55 < \text{decl.} < -35$ , which is spectroscopically confirmed by 2dF, LCRS, (Shectman et al. 1996), and especially 6dF. A broader galaxy overdensity is found around  $z \sim 0.12$  (also seen in LCRS and 2dF, and composed of several Abell galaxy clusters). This broad peak is also identified in redshift distributions by other photo- $z$  codes, including a template-based code, the Bayesian Photometric Redshift (Benéz 2000). We have further verified that overdensities at the lowest redshifts ( $z \sim 0.06$ ) are also present in spectroscopic samples outside of the region of interest. This is expected at these low redshifts, where large-scale structure projects onto vast areas of the sky. In summary, there are 77,092 galaxies within the 90% LIGO/Virgo probability volume, and 105,011 when 99.7% of the distance probability is considered, of which  $\sim 6000$  have spectroscopic redshifts.

### 3. Method

In order to estimate the posterior probability of  $H_0$  given GW data  $d_{\text{GW}}$  from a single event detection, and electromagnetic (EM) data from a galaxy survey, we follow Chen et al. (2018). By applying Bayes' theorem, one can write the posterior as

$$p(H_0|d_{\text{GW}}, d_{\text{EM}}) \propto p(d_{\text{GW}}, d_{\text{EM}}|H_0)p(H_0). \quad (1)$$

We assume that all cosmological parameters except for  $H_0$  are fixed (flat  $\Lambda$ CDM cosmology with  $\Omega_m = 0.3$  and  $\Omega_\Lambda = 0.7$ ). We treat the joint GW and EM likelihood  $p(d_{\text{GW}}, d_{\text{EM}}|H_0)$  as the product of two individual likelihoods (as the processes involved in producing the data from the two experiments are independent) marginalized over all variables except for the true luminosity distance  $d_L$  and solid angle  $\hat{\Omega}_{\text{GW}}$  of the GW source, and for the true host galaxy redshift  $z_i$  and solid angle  $\hat{\Omega}_i$ . Note that the solid angles  $\hat{\Omega}$  are vectors with the angular position of the source/galaxy as direction, and they all subtend the same area ( $\sim 3 \times 10^{-3} \text{ deg}^2$ ) as the sky is pixelized with HEALPix maps in this work. If we assume that the event happened in one of the observed galaxies  $i$ , then  $\hat{\Omega}_{\text{GW}}$  and  $\hat{\Omega}_i$  are related, and so are  $d_L$  and  $z_i$  through the cosmology (in this case,  $H_0$ ). By marginalizing also over the choice of galaxy  $i$ , the joint marginal likelihood can be written as

$$\begin{aligned} & p(d_{\text{GW}}, d_{\text{EM}}|z_j, \hat{\Omega}_j, H_0) \\ & \propto \sum_i w_i \int dd_L d\hat{\Omega}_{\text{GW}} p(d_{\text{GW}}|d_L, \hat{\Omega}_{\text{GW}}) \\ & \quad \times p(d_{\text{EM}}|z_j, \hat{\Omega}_j) \delta_D(d_L - d_L(z_i, H_0)) \delta_D(\hat{\Omega}_{\text{GW}} - \hat{\Omega}_i), \end{aligned} \quad (2)$$

where  $\delta_D$  is the Dirac delta function,  $w_i$  are weights that represent the relative probability that different galaxies host a GW source, and  $\{z_j, \hat{\Omega}_j\}$  represents all the galaxies' redshift and solid angle. These weights could be based on some galaxy properties, such as luminosity or star formation rate, but here we assume they are uniform across all galaxies given our lack of knowledge of GW host galaxy properties.

We also need to marginalize over the galaxies' redshifts and sky positions, with a reasonable choice of prior  $p(z_i, \hat{\Omega}_i)$ . If one assumes that the galaxies are uniformly distributed in comoving volume  $V$ , and volume-limited within  $V_{\text{max}}$ ,

$$p(z_i, \hat{\Omega}_i) dz_i d\hat{\Omega}_i \propto \frac{1}{V_{\text{max}}} \frac{d^2 V}{dz_i d\hat{\Omega}_i} dz_i d\hat{\Omega}_i \propto \frac{1}{V_{\text{max}}} \frac{r^2(z_i)}{H(z_i)} dz_i d\hat{\Omega} \quad (3)$$

where  $r$  is the comoving distance to the galaxy. While this assumption holds on average over sufficiently large volumes, it is possible that future precision cosmology analyses will require taking into account the real clustering of galaxies in this formalism.

Assuming that we precisely know the galaxies' positions  $\{\hat{\Omega}_j\}$  (which is realistic especially in the limit in which spatial probabilities are considered within HEALPix pixels), we can integrate over the galaxies' positions as delta functions about the observed values. The marginal EM likelihood reduces to  $p(d_{\text{EM}}|z_j)$ , which we approximate for simplicity by a product of Gaussian distributions,  $\mathcal{N}$ , for each galaxy, centered around the observed redshift values  $z_{\text{obs},i}$  with a width given by the

redshift's uncertainty  $\sigma_{z,i}$  for each galaxy  $i$ :

$$p(d_{\text{EM}}|\{z_j\}) = \prod_i p(z_{\text{obs},i}|z_i) = \prod_i \mathcal{N}(z_{\text{obs},i}, \sigma_{z,i}; z_i). \quad (4)$$

The marginal GW likelihood  $p(d_{\text{GW}}|d_L, \Omega)$  can be computed as prescribed in Singer et al. (2016):

$$p(d_{\text{GW}}|d_L, \hat{\Omega}) \propto p(\hat{\Omega}) \frac{1}{\sqrt{2\pi}\sigma(\hat{\Omega})} \exp\left[-\frac{(d_L - \mu(\hat{\Omega}))^2}{2\sigma^2(\hat{\Omega})}\right] N(\hat{\Omega}), \quad (5)$$

where the position probability, location, normalization, and scale (PROB  $p(\hat{\Omega})$ , DISTMU  $\mu$ , DISTNORM  $N$ , and DISTSTD  $\sigma$ , respectively) of the luminosity distance at each position are provided in the sky map.

We now consider the selection effects of GW events and galaxies introduced by the experiments' sensitivities and detection pipelines. We follow the approach of Chen et al. (2018) and Mandel et al. (2019), and include a  $[\beta(H_0)]^{-1}$  factor that normalizes the likelihood over all possible GW and EM data. Given that our galaxy catalog is volume-limited out to larger distances than the maximum observable distance for the GW events, this term reduces to

$$\beta(H_0) = \frac{V[d_{L,\text{GW}}^{\max}(H_0)]}{V_{\max}(H_0)}, \quad (6)$$

where  $V[d_{L,\text{GW}}^{\max}(H_0)]$  is the maximum observable volume for the GW events considered.

Finally, Equation (1) becomes

$$p(H_0|d_{\text{GW}}, d_{\text{EM}}) \propto \frac{p(H_0)}{V[d_{L,\text{GW}}^{\max}(H_0)]} \sum_i \frac{1}{\mathcal{Z}_i} \times \int dz_i p(d_{\text{GW}}|d_L(z_i, H_0), \hat{\Omega}_i) p(d_{\text{EM}}|z_i) \frac{r^2(z_i)}{H(z_i)}, \quad (7)$$

where  $\mathcal{Z}_i = \int p(d_{\text{EM}}|z_i) r^2(z_i)/H(z_i) dz_i$  are evidence terms that arise from integrating out the other galaxy redshifts in each term of the sum. This formalism can be extended to combine data  $\{d_{\text{GW},j}\}$  and  $d_{\text{EM}}$  from a sample of multiple events  $j$ , assuming that the GW events are independent and that the galaxy catalog is fixed for all events:

$$p(H_0|\{d_{\text{GW},j}\}, d_{\text{EM}}) \propto p(H_0) \int d^N z_k d^N \hat{\Omega}_k p(z_k, \hat{\Omega}_k) \times p(d_{\text{EM}}|\{z_k, \hat{\Omega}_k\}) \left[ \prod_j p(d_{\text{GW},j}|z_k, \hat{\Omega}_k) \right]. \quad (8)$$

In the following, we assume a flat prior on  $H_0$  within  $[20, 140]$   $\text{km s}^{-1} \text{Mpc}^{-1}$ , unless otherwise stated. This is a very broad prior, covering a range that is much larger than current estimates of  $H_0$ . This choice was made as a compromise between the following aspects: (i) a result that is mostly informed by the LVC and DES data rather than by external constraints, (ii) a result that can be compared with the first standard siren estimate, and (iii) a complete galaxy sample that contains most of the stellar mass within the localization volume, to minimize the chance of missing the real host galaxy. As explained in more detail in Section 4, the redshift cut is related to the  $H_0$  prior range, and in order to explore higher values of  $H_0$ , one needs to include higher redshift galaxies, and make a higher luminosity cut to preserve the volume-limited sample.

A blinded analysis has been performed when estimating the  $H_0$  posterior from the data to avoid confirmation bias. The values of the Hubble constant have been randomly displaced by an unknown amount, and we unblinded after our pipeline was able to reliably reproduce the input cosmology on simulation tests.

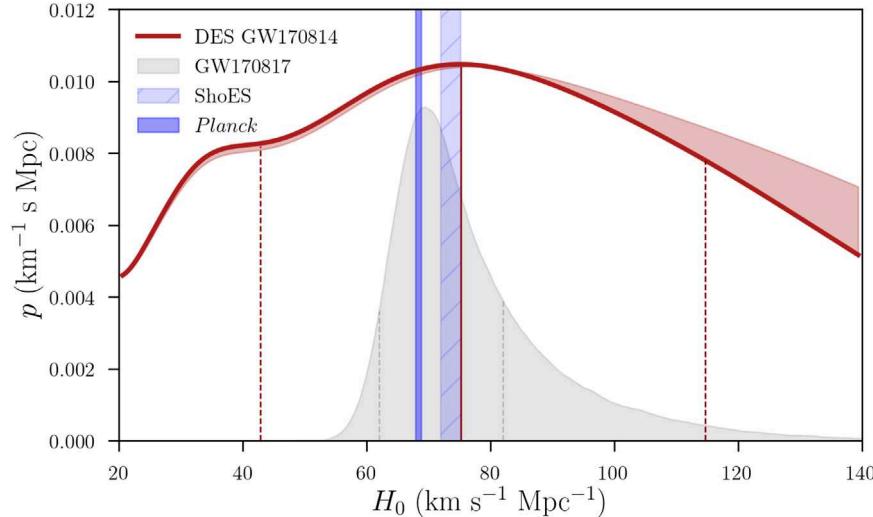
## 4. Results and Discussion

We apply the described methodology to the DES galaxies' redshifts and the GW170814 LIGO/Virgo sky map to produce a posterior distribution for the Hubble constant. We find that changes in the  $H_0$  estimate and its uncertainty between using the corrected DNF photo- $z$ 's or the ANN2 outputs are below the percent level. This agreement is expected, because the two methods produce redshift distributions that are consistent with similar uncertainties. We also add a 0.001 systematic redshift error in quadrature (corresponding to a typical peculiar velocity of  $\sim 300 \text{ km s}^{-1}$ ). The effect of this correction on the posterior is negligible because only a few percent of the galaxies have a spectroscopic redshift, and the effect of peculiar velocities on the remaining galaxies is more than an order of magnitude below their typical photo- $z$  error.

Our maximum a posteriori estimate of the Hubble constant is  $H_0 = 75^{+40}_{-32} \text{ km s}^{-1} \text{ Mpc}^{-1}$  using a flat prior between 20 and 140  $\text{km s}^{-1} \text{ Mpc}^{-1}$ . The full posterior distribution is shown in Figure 2, and Table 1 summarizes our findings. The presence of a main, though broad, peak, is expected given the large-scale structure seen in the observed volume.

As described in Section 2.1, the galaxy sample used in these results is selected as described in Section 2, and covers the LIGO/Virgo 90% credible localization volume. The distance cut is translated into a redshift cut (made on the mean photo- $z$  value of each galaxy) for a given  $H_0$  prior. This cut ensures that the galaxy catalog is as complete as possible throughout the whole redshift range of interest for the cosmological parameters used, and includes the fainter galaxies observable for a volume-limited sample defined as in Section 2. In fact, in order to include more distant galaxies, the luminosity cut needs to be brighter to ensure that the sample is still volume limited, with the risk of missing the true host galaxy. We have explored the impact of the redshift cut on the  $H_0$  posterior, while keeping the angular selection to be within the 90% credible localization area. The effect of including galaxies out to 99.7% of the distance localization (corresponding to  $z \lesssim 0.3$ ) is most pronounced at high  $H_0$  values, as shown by the shaded red region in Figure 2. With this less restrictive cut, the credible region shifts to  $H_0 = 77^{+41}_{-33} \text{ km s}^{-1} \text{ Mpc}^{-1}$ , showing a  $\sim 2\%$  change of the maximum. The effect described here arises from tens of thousand of galaxies at the higher redshifts included with the more relaxed distance cut and the ansatz of Gaussianity of the luminosity distance posterior. In fact, these galaxies contribute with a non-negligible probability to the posterior because of the high  $d_L$  tail shown in the bottom-right panel of Figure 1, and they contribute more significantly at high  $H_0$  values. This few percent effect is insignificant at the current levels of precision, but will need to be explored in the future using a more realistic luminosity distance posterior.

Our result agrees well (as expected, due to the large uncertainty) with the latest CMB estimate of the Hubble constant by the *Planck* Collaboration ( $67.36 \pm 0.54 \text{ km s}^{-1} \text{ Mpc}^{-1}$  from TT,TE,EE+lowP+lensing; Planck Collaboration et al. 2018), and with results using distance ladder methods by ShoES



**Figure 2.** Hubble constant posterior distribution obtained by marginalizing over  $\sim 77,000$  possible host galaxies (red line), showing the maximum value (solid vertical line). The maximum a posteriori and its 68% confidence level is  $H_0 = 75^{+40}_{-32} \text{ km s}^{-1} \text{ Mpc}^{-1}$  for a flat prior in the range  $[20, 140] \text{ km s}^{-1} \text{ Mpc}^{-1}$ . The shaded region represents the change in the posterior when different fractions of the localization volume are considered (from 90% to 99.7% of the LIGO/Virgo luminosity distance posterior). The PDF computed from the larger volume has been renormalized to have the same value of the 90% localization volume  $H_0$  posterior at the maximum, to highlight differences below and beyond the main peak. The posterior obtained by Abbott et al. (2017a) for the bright standard siren event GW170817, associated to one galaxy, is shown in gray. The prior used in that work was flat-in-log over a narrower range ( $[50, 140] \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), and the posterior has been rescaled by a factor 0.2 for visualization purposes. The 68% CL of both PDFs is shown by the dashed lines. Constraints from *Planck* (Planck Collaboration et al. 2018) and Supernovae and  $H_0$  for the Equation of State (SHoES; Riess et al. 2016, 2018) at  $1\sigma$  are shown in purple boxes.

**Table 1**  
Hubble Constant Estimate from this Work

Prior	$H_0$	$+ \sigma_{H_0}$	$- \sigma_{H_0}$	$\sigma_{H_0}/H_0$	$\sigma_{H_0}/H_0$ prior
$[20, 140]$	75	40	32	47.8%	54.3%

**Note.** All  $H_0$  values and errors are in  $\text{km s}^{-1} \text{ Mpc}^{-1}$ . The uncertainty from the flat prior only is derived by assuming the same  $H_0$  maximum found in the analysis. Quoted uncertainties represent 68% confidence level around the maximum of the posterior, and they are statistical only. The last column quantity ( $\sigma_{H_0}/H_0$  prior) corresponds to 68% times the prior width divided by  $H_0$ .

( $73.52 \pm 1.62 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ; Riess et al. 2016) and by DES ( $67.77 \pm 1.30 \text{ km s}^{-1} \text{ Mpc}^{-1}$  from SN+BAO; Macaulay et al. 2019).

For the bright standard siren measurement using GW170817 and its electromagnetic counterpart, Abbott et al. (2017a) found  $H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$  at 68% credible interval. Without an EM counterpart leading to a unique host galaxy redshift, we would have recovered a broader  $H_0$  posterior because we average over all possible host galaxies in the localization volume. For example, Fishbach et al. (2019) applied the statistical standard siren method to GW170817 and found a larger uncertainty than the counterpart standard siren result:  $H_0 = 76^{+48}_{-23} \text{ km s}^{-1} \text{ Mpc}^{-1}$  for a uniform prior over the range  $[10, 220] \text{ km s}^{-1} \text{ Mpc}^{-1}$ . For a BBH standard siren measurement, as in this work, the combination of the larger localization volume (implying a significantly greater number of potential host galaxies) and the large photometric redshift uncertainty for each galaxy results in an even broader  $H_0$  posterior. Therefore, while applying the statistical standard siren method to GW170817 yields a 68% credible region on  $H_0$  comprising 34% of the prior range (Fishbach et al. 2019), in this work we obtain a 68% credible region on  $H_0$  that is 60% of the prior range. We note that the prior used in Fishbach et al. (2018) is 1.75 times broader than the prior used in this work; if we adopt

the same broader prior of  $[10, 220]$  for our analysis of GW170814, we find  $H_0 = 78^{+96}_{-24} \text{ km s}^{-1} \text{ Mpc}^{-1}$ . The dependence of the width of the  $H_0$  posterior on the prior width is a consequence of the fact that the GW observation, which provides only a luminosity distance estimate, is consistent with arbitrarily large  $H_0$ 's, if there are galaxies at sufficiently large redshifts. If the galaxy catalog extends to some redshift,  $z_{\max}$ , the posterior would fall off around  $H_0 \approx c z_{\max} / d_L$ , where  $d_L$  is the typical luminosity distance from the GW posterior. However, this fall off is artificial as there are galaxies at greater redshifts that are not included in the catalog. These may be accounted for using catalog incompleteness corrections. We chose the prior range for this analysis rather than a larger one such that we did not need to include such corrections, which simplifies the analysis. However, dark siren measurements will become particularly interesting when multiple events can be combined and this effect becomes irrelevant (Chen et al. 2018).

The analysis in Fishbach et al. (2019) for GW170817 used the Galaxy List for the Advanced Detector Era (GLADE) galaxy catalog (Dálya et al. 2018), and accounted for incompleteness at the distance of GW170817. GLADE becomes significantly incomplete at the distance to GW170814. As GW detectors improve in sensitivity, the majority of dark standard sirens will be detected at even greater distances and with larger localization volumes, well beyond the reach of spectroscopic galaxy catalogs. This highlights the need for reliable and complete photometric galaxy catalogs. Surveys such as DES, Pan-STARRS1 (Chambers et al. 2016), and the Large Synoptic Survey Telescope (LSST) are therefore likely to play an important role in future constraints from BBH standard sirens.

The assumption throughout this work is that even if the event occurred in a galaxy below our luminosity threshold, large-scale structure predicts that fainter galaxies follow the clustering pattern of the more luminous galaxies in our sample. We have verified in our simulations that a threshold up to 1 mag brighter than the limit used here to place events has a

negligible impact over a sample of 100 events, provided that the catalog is volume limited for the range of redshifts relevant to the measurement.

Galaxies are biased tracers of the universe’s dark matter, therefore some theories predict that the origin of the black holes involved in these GW events is primordial, constituting part or all of the dark matter (Bird et al. 2016; Clesse & García-Bellido 2017, 2018; García-Bellido 2017). In that case, GW events follow exactly the underlying dark matter distribution (presenting an unbiased tracer). Because of the stellar mass to dark matter halo connection (see Wechsler & Tinker 2018, and references therein) it is reasonable to weight galaxies by their stellar mass in Equation (2) as  $w_i \propto M_*$ . The impact of this scaling with stellar mass or star formation rate has been explored in Fishbach et al. (2019). We find that the stellar mass weighting has a negligible effect on the posterior. This is due to the large volume analyzed (over which the stellar masses tend to be averaged out) and to the precision level of this measurement. In other theories, these black hole binaries are produced in very-low-metallicity galaxies (e.g., Cao et al. 2018; Mapelli et al. 2018), biased relative to the dark matter distribution differently than the luminous galaxies in our catalog. J. Annis et al. (2019, in preparation) explore the effect of the tracer bias assumptions on the  $H_0$  posterior for future analyses aiming at precision measurements.

Another assumption of our analysis that needs attention concerns the redshift likelihood. As anticipated above for the GW likelihood, this will not, in general, be well approximated by a Gaussian. In the future, we plan to explore the impact of realistic photometric redshift PDFs on the  $H_0$  posterior, in order to enable precision cosmology with BBH events. An analysis with the full, asymmetric, GW likelihood will also be required. While an estimate of those effects is needed, tests on off-source lines of sight show that our constraint is likely not strongly impacted by the photo- $z$  training sample or systematic failures.

In the past two LVC observing seasons, black hole mergers outnumbered neutron star events at a rate of approximately 10–1. Uncertainties on the expected detection rate are large, but conservative estimates predict  $\sim 1$  event per week for the upcoming observing campaign (scheduled to start in 2019 April). The majority of these events will have larger localization volumes than GW170814 (Chen & Holz 2016 estimated that  $\lesssim 1\%$  of BBHs will be localized to better than  $10^4$  Mpc $^3$ ), and hence provide poorer constraints than those reported here. However, given the high expected event rate for dark sirens, larger event samples will be available in the future. Chen et al. (2018) provided forecasts using a distribution of realistic localization area, finding that the dark siren method will reach  $\sim 10\%$  statistical precision on  $H_0$  by 2026 from BBH mergers only, and 5%–10% precision from BNS mergers if none of them have EM counterparts.

## 5. Conclusions

In this Letter, we have performed the first measurement of the Hubble constant using a GW detection of a BBH merger as a dark standard siren and the DES galaxies as a sample of potential host galaxies. Our analysis was blinded to avoid confirmation bias. Our main results, discussed in Section 4, include a measurement of  $H_0 = 75^{+40}_{-32}$  km s $^{-1}$  Mpc $^{-1}$  for a flat prior within [20,140] km s $^{-1}$  Mpc $^{-1}$ , which is consistent with previous measurements of  $H_0$ . The 68% confidence interval

quoted here is 60% of the uniform prior range, and it depends on the width of the prior. For example, with a broader prior of [10,220] km s $^{-1}$  Mpc $^{-1}$ , we find  $H_0 = 78^{+96}_{-24}$  km s $^{-1}$  Mpc $^{-1}$ . Albeit weak, this measurement is not uninformative and the method becomes more powerful when we combine large numbers of dark sirens (Chen et al. 2018).

Future dark siren measurements will require complete galaxy catalogs. A wide field galaxy catalog with a DES-like depth is currently available only for  $\sim$ one-eighth of the sky. However, DES can be complemented with other data sets taken with DECam (such as the Blanco Imaging of the Southern Sky, BLISS, and the Dark Energy Camera Legacy Survey (DECaLS)), to cover the whole Southern sky to a good depth ( $r \sim 23.4$ ,  $5\sigma$  depth). An even deeper survey with more precise photo- $z$ ’s, such as the LSST (LSST Dark Energy Science Collaboration 2012), would be of great value for further improving these constraints.

At the expected level of precision from hundreds of events (<10%), systematics will play an important role. In future work, we plan to incorporate systematic uncertainties in our simulated data studies, in order to prepare for precision cosmology analyses on real data. We anticipate that some of the main sources of systematics will be photo- $z$  biases and catastrophic outliers, photo- $z$  training sample variance, galaxy catalog cuts, and galaxy catalog completeness. In order to achieve the full potential of statistical standard siren cosmology, wide and deep galaxy surveys such as DES and LSST are necessary. Overall, our findings show that the synergy between GW black hole merger detections and new-generation large galaxy surveys will establish a new powerful probe for precision cosmology.

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## References

- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2016, *PhRvL*, **116**, 061102  
 Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017, *PhRvL*, **119**, 161101  
 Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017a, *Natur*, **551**, 85  
 Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017b, *PhRvL*, **119**, 141101  
 Abbott, T., Abdalla, F. B., Allam, S., et al. 2016, *PhRvD*, **94**, 022001  
 Abbott, T. M. C., Abdalla, F. B., Allam, S., et al. 2018, arXiv:1801.03181  
 Allen, D. A. 1976, *MNRAS*, **174**, 29P  
 Arcavi, I., Hosseinzadeh, G., Howell, D. A., et al. 2017, *Natur*, **551**, 64  
 Arnouts, S., Cristiani, S., Moscardini, L., et al. 1999, *MNRAS*, **310**, 540  
 Bayliss, M. B., Ruel, J., Stubbs, C. W., et al. 2016, *ApJS*, **227**, 3  
 Benéz, N. 2000, *Apl*, **536**, 571  
 Bertin, E., & Arnouts, S. 1996, *A&AS*, **117**, 393  
 Bilicki, M., Hoekstra, H., Brown, M. J. I., et al. 2018, *A&A*, **616**, A69  
 Bird, S., Cholis, I., Muñoz, J. B., et al. 2016, *PhRvL*, **116**, 201301  
 Bonnett, C., Troxel, M. A., Hartley, W., et al. 2016, *PhRvD*, **94**, 042005  
 Brzuza, G., & Charlton, S. 2003, *MNRAS*, **344**, 1000  
 Cao, L., Lu, Y., & Zhao, Y. 2018, *MNRAS*, **474**, 4997  
 Chabrier, G. 2003, *PASP*, **115**, 763  
 Chambers, K. C., Magnier, E. A., Metcalfe, N., et al. 2016, arXiv:1612.05560  
 Chen, H.-Y., Fishbach, M., & Holz, D. E. 2018, *Natur*, **562**, 545  
 Chen, H.-Y., & Holz, D. E. 2016, arXiv:1612.01471  
 Clesse, S., & García-Bellido, J. 2017, *PDU*, **15**, 142  
 Clesse, S., & García-Bellido, J. 2018, *PDU*, **22**, 137  
 Colless, M., Dalton, G., Maddox, S., et al. 2001, *MNRAS*, **328**, 1039  
 Coulter, D. A., Foley, R. J., Kilpatrick, C. D., et al. 2017, *Sci*, **358**, 1556  
 Cowperthwaite, P. S., Berger, E., Soares-Santos, M., et al. 2016, *ApJL*, **826**, L29  
 Dálya, G., Galgócz, G., Dobos, L., et al. 2018, *MNRAS*, **479**, 2374  
 Dark Energy Survey Collaboration, Abbott, T., Abdalla, F. B., et al. 2016, *MNRAS*, **460**, 1270  
 Del Pozzo, W. 2012, *PhRvD*, **86**, 043011  
 De Vicente, J., Sánchez, E., & Sevilla-Noarbe, I. 2016, *MNRAS*, **459**, 3078  
 Doctor, Z., Kessler, R., Herner, K., et al. 2018, arXiv:1812.01579  
 Drlica-Wagner, A., Sevilla-Noarbe, I., Rykoff, E. S., et al. 2017, *PhRvD*, submitted  
 Erben, T., Hildebrandt, H., Miller, L., et al. 2013, *MNRAS*, **433**, 2545  
 Etherington, J., Thomas, D., Maraston, C., et al. 2017, *MNRAS*, **466**, 228  
 Feeney, S. M., Peiris, H. V., Williamson, A. R., et al. 2019, *PhRvL*, **122**, 061105  
 Fishbach, M., Gray, R., Magaña Hernandez, I., et al. 2019, *ApJL*, **871**, L13  
 Flaugher, B., Diehl, H. T., Honscheid, K., et al. 2015, *AJ*, **150**, 150  
 Freedman, W. L. 2017, *NatAs*, **1**, 0169  
 García-Bellido, J. 2017, *JPhCS*, **840**, 012032  
 Górski, K. M., Hivon, E., Banday, A. J., et al. 2005, *Apl*, **622**, 759  
 Gschwend, J., Rossel, A. C., Ogando, R. L. C., et al. 2018, *A&C*, **25**, 58  
 Hartley, W. G., Almaini, O., Mortlock, A., et al. 2013, *MNRAS*, **431**, 3045  
 Holz, D. E., & Hughes, S. A. 2005, *ApJ*, **629**, 15  
 Huchra, J. P., Macri, L. M., Masters, K. L., et al. 2012, *ApJS*, **199**, 26  
 Ilbert, O., Arnouts, S., McCracken, H. J., et al. 2006, *A&A*, **457**, 841  
 Jones, D. H., Read, M. A., Saunders, W., et al. 2009, *MNRAS*, **399**, 683  
 Leistedt, B., Peiris, H. V., Elsner, F., et al. 2016, *ApJS*, **226**, 24  
 LIGO Scientific CollaborationVirgo Collaboration, GBM, F., et al. 2017, arXiv:1710.05833  
 LIGO Scientific CollaborationVirgo Collaboration 2017, *GCN*, **21934**, 1  
 Lima, M., Cunha, C. E., Oyaizu, H., et al. 2008, *MNRAS*, **390**, 118  
 Lipunov, V. M., Gorbovskoy, E., Kornilov, V. G., et al. 2017, *ApJL*, **850**, L1  
 LSST Dark Energy Science Collaboration 2012, arXiv:1211.0310  
 Macaulay, E., Nichol, R. C., Bacon, D., et al. 2019, *MNRAS*, **486**, 2184  
 MacLeod, C. L., & Hogan, C. J. 2008, *PhRvD*, **77**, 043512  
 Mandel, I., Farr, W. M., & Gair, J. R. 2019, *MNRAS*, **486**, 1086  
 Mapelli, M., Giacobbo, N., Toffano, M., et al. 2018, *MNRAS*, **481**, 5324  
 Morganson, E., Gruendl, R. A., Menanteau, F., et al. 2018, *PASP*, **130**, 074501  
 Mortlock, D. J., Feeney, S. M., Peiris, H. V., Williamson, A. R., & Nisanke, S. M. 2018, arXiv:1811.11723  
 Mörtsell, E., & Dhawan, S. 2018, *JCAP*, **9**, 025  
 Nair, R., Bose, S., & Deep Saini, T. 2018, *PhRvD*, **98**, 023502  
 Nishizawa, A. 2017, *PhRvD*, **96**, 101303  
 Nisanke, S., Holz, D. E., Dalal, N., et al. 2013, arXiv:1307.2638  
 Nisanke, S., Holz, D. E., Hughes, S. A., Dalal, N., & Sievers, J. L. 2010, *ApJ*, **725**, 496  
 Palmese, A., Annis, J., Burgad, J., et al. 2019, *MNRAS*, submitted  
 Palmese, A., Hartley, W., Tarsitano, F., et al. 2017, *ApJL*, **849**, L34  
 Palmese, A., Lahav, O., Banerji, M., et al. 2016, *MNRAS*, **463**, 1486  
 Planck Collaboration, Aghanim, N., Akrami, Y., et al. 2018, arXiv:1807.06209

- Pozzetti, L., Bolzonella, M., Zucca, E., et al. 2010, *A&A*, **523**, A13  
 Riess, A. G., Casertano, S., Yuan, W., et al. 2018, *ApJ*, **861**, 126  
 Riess, A. G., Macri, L. M., Hoffmann, S. L., et al. 2016, *ApJ*, **826**, 56  
 Sadeh, I., Abdalla, F. B., & Lahav, O. 2016, *PASP*, **128**, 104502  
 Schutz, B. F. 1986, *Natur*, **323**, 310  
 Shectman, S. A., Landy, S. D., Oemler, A., et al. 1996, *ApJ*, **470**, 172  
 Singer, L. P., Chen, H.-Y., Holz, D. E., et al. 2016, *ApJS*, **226**, 10  
 Soares-Santos, M., Holz, D. E., Annis, J., et al. 2017, arXiv:[1710.05459](https://arxiv.org/abs/1710.05459)  
 Soares-Santos, M., Kessler, R., Berger, E., et al. 2016, *ApJL*, **823**, L33  
 Tanvir, N. R., Levan, A. J., González-Fernández, C., et al. 2017, *ApJL*, **848**, L27  
 The Dark Energy Survey Collaboration 2005, arXiv:[astro-ph/0510346](https://arxiv.org/abs/astro-ph/0510346)  
 Valenti, S., Sand, D. J., Yang, S., et al. 2017, *ApJL*, **848**, L24  
 Vitale, S., & Chen, H.-Y. 2018, *PhRvL*, **121**, 021303  
 Wechsler, R. H., & Tinker, J. L. 2018, *ARA&A*, **56**, 435  
 Weigel, A. K., Schawinski, K., & Bruderer, C. 2016, *MNRAS*, **459**, 2150