Measurement of charm and bottom production from semileptonic hadron decays in $p+p$ collisions at $\sqrt{s} = 200$ GeV

C. Aidala,[40] Y. Akiba,[52, 53, *] M. Alfred,[23] V. Andrieux,[40] N. Apadula,[28] H. Asano,[33, 52] B. Azmoun,[7] V. Babintsev,[24] N.S. Bandara,[39] K.N. Barish,[8] S. Bathe,[5, 53] A. Bazilevsky,[7] M. Beaumier,[8] R. Belmont,[12, 46] A. Berdnikov,[55] Y. Berdnikov,[55] D.S. Blau,[32, 43] J.S. Bok,[45] M.L. Brooks,[35] J. Bryslawskyj,[5, 8] V. Bumazhnov,[24] S. Campbell,[13] V. Canoa Roman,[58] R. Cervantes,[58] C.Y. Chi,[13] M. Chiu,[7] I.J. Choi,[25] J.B. Choi,[10, †] Z. Citron,[63] M. Connors,[21, 53] N. Cronin,[58] M. Csanád,[16] T. Csörgő,[17, 64] T.W. Danley,[47] M.S. Daugherity,[1] G. David,[7, 15, 58] K. DeBlasio,[44] K. Dehmelt,[58] A. Denisov,[24] A. Deshpande,[7, 53, 58] E.J. Desmond,[7] A. Dion,[58] D. Dixit,[58] J.H. Do,[65] A. Drees,[58] K.A. Drees,[6] J.M. Durham,[35] A. Durum,[24] A. Enokizono,[52, 54] H. En'yo,[52] S. Esumi,[61] B. Fadem,[41] W. Fan,[58] N. Feege,[58] D.E. Fields,[44] M. Finger,[9] M. Finger, Jr.,[9] S.L. Fokin,[32] J.E. Frantz,[47] A. Franz,[7] A.D. Frawley,[20] Y. Fukuda,[61] C. Gal,[58] P. Gallus,[14] E.A. Gamez,[40] P. Garg,[3, 58] H. Ge,[58] F. Giordano,[25] Y. Goto,[52, 53] N. Grau,[2] S.V. Greene,[62] M. Grosse Perdekamp,[25] T. Gunji,[11] H. Guragain,[21] T. Hachiya,[42, 52, 53] J.S. Haggerty,[7] K.I. Hahn,[18] H. Hamagaki,[11] H.F. Hamilton,[1] S.Y. Han,[18, 52] J. Hanks,[58] S. Hasegawa,[29] T.O.S. Haseler,[21] X. He,[21] T.K. Hemmick,[58] J.C. Hill,[28] K. Hill,[12] A. Hodges,[21] R.S. Hollis,[8] K. Homma,[22] B. Hong,[31] T. Hoshino,[22] N. Hotvedt,[28] J. Huang,[7] S. Huang,[62] K. Imai,[29] M. Inaba,[61] A. Iordanova,[8] D. Isenhower,[1] S. Ishimaru,[42] D. Ivanishchev,[51] B.V. Jacak,[58] M. Jezghani,[21] Z. Ji,[58] X. Jiang,[35] B.M. Johnson,[7, 21] D. Jouan,[49] D.S. Jumper,[25] J.H. Kang,[65] D. Kapukchyan,[8] S. Karthas,[58] D. Kawall,[39] A.V. Kazantsev,[32] V. Khachatryan,[58] A. Khanzadeev,[51] C. Kim,[8, 31] E.-J. Kim,[10] M. Kim,[52, 56] D. Kincses,[16] E. Kistenev,[7] J. Klatsky,[20] P. Kline,[58] T. Koblesky,[12] D. Kotov,[51, 55] S. Kudo,[61] B. Kurgyis,[16] K. Kurita,[54] Y. Kwon,[65] J.G. Lajoie,[28] A. Lebedev,[28] S. Lee,[65] S.H. Lee,[28, 58] M.J. Leitch,[35] Y.H. Leung,[58] N.A. Lewis,[40] X. Li,[35] S.H. Lim,[35, 65] M.X. Liu,[35] V.-R. Loggins,[25] S. Lökös,[16, 17] K. Lovasz,[15] D. Lynch,[7] T. Majoros,[15] Y.I. Makdisi,[6] M. Makek,[66] V.I. Manko,[32] E. Mannel,[7] M. McCumber,[35] P.L. McGaughey,[35] D. McGlinchey,[12, 35] C. McKinney,[25] M. Mendoza,[8] W.J. Metzger,[17] A.C. Mignerey,[38] A. Milov,[63] D.K. Mishra,[4] J.T. Mitchell,[7] Iu. Mitrankov,[55] G. Mitsuka,[30, 52, 53] S. Miyasaka,[52, 60] S. Mizuno,[52, 61] P. Montuenga,[25] T. Moon,[65] D.P. Morrison,[7] S.I. Morrow,[62] T. Murakami,[33, 52] J. Murata,[52, 54] K. Nagai,[60] K. Nagashima,[22, 52] T. Nagashima,[54] J.L. Nagle,[12] M.I. Nagy,[16] I. Nakagawa,[52, 53] K. Nakano,[52, 60] C. Nattrass,[59] S. Nelson,[19] T. Niida,[61] R. Nishitani,[42] R. Nouicer,[7, 53] T. Novák,[17, 64] N. Novitzky,[58] A.S. Nyanin,[32] E. O'Brien,[7] C.A. Ogilvie,[28] J.D. Orjuela Koop,[12] J.D. Osborn,[40] A. Oskarsson,[36] G.J. Ottino,[44] K. Ozawa,[30, 61] V. Pantuev,[26] V. Papavassiliou,[45] J.S. Park,[56] S. Park,[52, 56, 58] S.F. Pate,[45] M. Patel,[28] W. Peng,[62] D.V. Perepelitsa,[7, 12] G.D.N. Perera,[45] D.Yu. Peressounko,[32] C.E. PerezLara,[58] J. Perry,[28] R. Petti,[7] M. Phipps,[7, 25] C. Pinkenburg,[7] R.P. Pisani,[7] A. Pun,[47] M.L. Purschke,[7] P.V. Radzevich,[55] K.F. Read,[48, 59] D. Reynolds,[57] V. Riabov,[43, 51] Y. Riabov,[51, 55] D. Richford,[5] T. Rinn,[28] S.D. Rolnick,[8] M. Rosati,[28] Z. Rowan,[5] J. Runchey,[28] A.S. Safonov,[55] T. Sakaguchi,[7] H. Sako,[29] V. Samsonov,[43, 51] M. Sarsour,[21] S. Sato,[29] C.Y. Scarlett,[19] B. Schaefer,[62] B.K. Schmoll,[59] K. Sedgwick,[8] R. Seidl,[52, 53] A. Sen,[28, 59] R. Seto,[8] A. Sexton,[38] D. Sharma,[58] I. Shein,[24] T.-A. Shibata,[52, 60] K. Shigaki,[22] M. Shimomura,[28, 42] T. Shioya,[61] P. Shukla,[4] A. Sickles,[25] C.L. Silva,[35] D. Silvermyr,[36] B.K. Singh,[3] C.P. Singh,[3] V. Singh,[3] M.J. Skoby,[40] M. Slunečka,[9] K.L. Smith,[20] M. Snowball,[35] R.A. Soltz,[34] W.E. Sondheim,[35] S.P. Sorensen,[59] I.V. Sourikova,[7] P.W. Stankus,[48] S.P. Stoll,[7] T. Sugitate,[22] A. Sukhanov,[7] T. Sumita,[52] J. Sun,[58] Z. Sun,[15] S. Suzuki,[42] J. Sziklai,[64] K. Tanida,[29, 53, 56] M.J. Tannenbaum,[7] S. Tarafdar,[62, 63] A. Taranenko,[43] G. Tarnai,[15] R. Tieulent,[21, 37] A. Timilsina,[28] T. Todoroki,[53, 61] M. Tomášek,[14] C.L. Towell,[1] R.S. Towell,[1] I. Tserruya,[63] Y. Ueda,[22] B. Ujvari,[15] H.W. van Hecke,[35] J. Velkovska,[62] M. Virius,[14] V. Vrba,[14, 27] N. Vukman,[66] X.R. Wang,[45, 53] Z. Wang,[5] Y.S. Watanabe,[11] C.P. Wong,[21] C.L. Woody,[7] C. Xu,[45] Q. Xu,[62] L. Xue,[21] S. Yalcin,[58] Y.L. Yamaguchi,[53, 58] H. Yamamoto,[61] A. Yanovich,[24] J.H. Yoo,[31, 53] I. Yoon,[56] H. Yu,[45, 50] I.E. Yushmanov,[32] W.A. Zajc,[13] A. Zelenski,[6] Y. Zhai,[28] S. Zharko,[55] and L. Zou[8]

(PHENIX Collaboration)

[1] Abilene Christian University, Abilene, Texas 79699, USA
[2] Department of Physics, Augustana University, Sioux Falls, South Dakota 57197, USA
[3] Department of Physics, Banaras Hindu University, Varanasi 221005, India
[4] Bhabha Atomic Research Centre, Bombay 400 085, India
[5] Baruch College, City University of New York, New York, New York, 10010 USA
[6] Collider-Accelerator Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA
[7] Physics Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA
[8] University of California-Riverside, Riverside, California 92521, USA
[9] Charles University, Ovocný trh 5, Praha 1, 116 36, Prague, Czech Republic
[10] Chonbuk National University, Jeonju, 561-756, Korea
[11] Center for Nuclear Study, Graduate School of Science, University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 113-0033, Japan

[12] *University of Colorado, Boulder, Colorado 80309, USA*
[13] *Columbia University, New York, New York 10027 and Nevis Laboratories, Irvington, New York 10533, USA*
[14] *Czech Technical University, Zikova 4, 166 36 Prague 6, Czech Republic*
[15] *Debrecen University, H-4010 Debrecen, Egyetem tér 1, Hungary*
[16] *ELTE, Eötvös Loránd University, H-1117 Budapest, Pázmány P. s. 1/A, Hungary*
[17] *Eszterházy Károly University, Károly Róbert Campus, H-3200 Gyöngyös, Mátrai út 36, Hungary*
[18] *Ewha Womans University, Seoul 120-750, Korea*
[19] *Florida A&M University, Tallahassee, FL 32307, USA*
[20] *Florida State University, Tallahassee, Florida 32306, USA*
[21] *Georgia State University, Atlanta, Georgia 30303, USA*
[22] *Hiroshima University, Kagamiyama, Higashi-Hiroshima 739-8526, Japan*
[23] *Department of Physics and Astronomy, Howard University, Washington, DC 20059, USA*
[24] *IHEP Protvino, State Research Center of Russian Federation, Institute for High Energy Physics, Protvino, 142281, Russia*
[25] *University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA*
[26] *Institute for Nuclear Research of the Russian Academy of Sciences, prospekt 60-letiya Oktyabrya 7a, Moscow 117312, Russia*
[27] *Institute of Physics, Academy of Sciences of the Czech Republic, Na Slovance 2, 182 21 Prague 8, Czech Republic*
[28] *Iowa State University, Ames, Iowa 50011, USA*
[29] *Advanced Science Research Center, Japan Atomic Energy Agency, 2-4*
Shirakata Shirane, Tokai-mura, Naka-gun, Ibaraki-ken 319-1195, Japan
[30] *KEK, High Energy Accelerator Research Organization, Tsukuba, Ibaraki 305-0801, Japan*
[31] *Korea University, Seoul, 02841*
[32] *National Research Center "Kurchatov Institute", Moscow, 123098 Russia*
[33] *Kyoto University, Kyoto 606-8502, Japan*
[34] *Lawrence Livermore National Laboratory, Livermore, California 94550, USA*
[35] *Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA*
[36] *Department of Physics, Lund University, Box 118, SE-221 00 Lund, Sweden*
[37] *IPNL, CNRS/IN2P3, Univ Lyon, Universt Lyon 1, F-69622, Villeurbanne, France*
[38] *University of Maryland, College Park, Maryland 20742, USA*
[39] *Department of Physics, University of Massachusetts, Amherst, Massachusetts 01003-9337, USA*
[40] *Department of Physics, University of Michigan, Ann Arbor, Michigan 48109-1040, USA*
[41] *Muhlenberg College, Allentown, Pennsylvania 18104-5586, USA*
[42] *Nara Women's University, Kita-uoya Nishi-machi Nara 630-8506, Japan*
[43] *National Research Nuclear University, MEPhI, Moscow Engineering Physics Institute, Moscow, 115409, Russia*
[44] *University of New Mexico, Albuquerque, New Mexico 87131, USA*
[45] *New Mexico State University, Las Cruces, New Mexico 88003, USA*
[46] *Physics and Astronomy Department, University of North Carolina at Greensboro, Greensboro, North Carolina 27412, USA*
[47] *Department of Physics and Astronomy, Ohio University, Athens, Ohio 45701, USA*
[48] *Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA*
[49] *IPN-Orsay, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, BP1, F-91406, Orsay, France*
[50] *Peking University, Beijing 100871, People's Republic of China*
[51] *PNPI, Petersburg Nuclear Physics Institute, Gatchina, Leningrad region, 188300, Russia*
[52] *RIKEN Nishina Center for Accelerator-Based Science, Wako, Saitama 351-0198, Japan*
[53] *RIKEN BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973-5000, USA*
[54] *Physics Department, Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima, Tokyo 171-8501, Japan*
[55] *Saint Petersburg State Polytechnic University, St. Petersburg, 195251 Russia*
[56] *Department of Physics and Astronomy, Seoul National University, Seoul 151-742, Korea*
[57] *Chemistry Department, Stony Brook University, SUNY, Stony Brook, New York 11794-3400, USA*
[58] *Department of Physics and Astronomy, Stony Brook University, SUNY, Stony Brook, New York 11794-3800, USA*
[59] *University of Tennessee, Knoxville, Tennessee 37996, USA*
[60] *Department of Physics, Tokyo Institute of Technology, Oh-okayama, Meguro, Tokyo 152-8551, Japan*
[61] *Tomonaga Center for the History of the Universe, University of Tsukuba, Tsukuba, Ibaraki 305, Japan*
[62] *Vanderbilt University, Nashville, Tennessee 37235, USA*
[63] *Weizmann Institute, Rehovot 76100, Israel*
[64] *Institute for Particle and Nuclear Physics, Wigner Research Centre for Physics, Hungarian*
Academy of Sciences (Wigner RCP, RMKI) H-1525 Budapest 114, POBox 49, Budapest, Hungary
[65] *Yonsei University, IPAP, Seoul 120-749, Korea*
[66] *Department of Physics, Faculty of Science, University of Zagreb, Bijenička c. 32 HR-10002 Zagreb, Croatia*
(Dated: April 26, 2019)

Measurements of the differential production of electrons from open-heavy-flavor hadrons with charm- and bottom-quark content in $p+p$ collisions at $\sqrt{s} = 200$ GeV are presented. The measurements proceed through displaced-vertex analyses of electron tracks from the semileptonic decay of charm and bottom hadrons using the PHENIX silicon-vertex detector. The relative contribution of electrons from bottom decays to inclusive heavy-flavor-electron production is found to be consistent

with fixed-order-plus-next-to-leading-log perturbative-QCD calculations within experimental and theoretical uncertainties. These new measurements in $p+p$ collisions provide a precision baseline for comparable forthcoming measurements in A+A collisions.

I. INTRODUCTION

Charm and bottom quarks are collectively referred to as heavy-flavor quarks. Their production in elementary $p+p$ collisions is of interest from a variety of vantage points, both in high-energy particle and nuclear physics.

From a fundamental standpoint, unlike light quarks the large masses of heavy-flavor quarks (compare $m_c \approx 1280$ MeV/c^2 and $m_b \approx 4180$ MeV/c^2 with $m_u \approx 2.2$ MeV/c^2 and $m_d \approx 4.7$ MeV/c^2) [1] are such that their production can be calculated using perturbative quantum chromodynamics (pQCD) even at low p_T. At leading order (LO), heavy quark production proceeds via gluon fusion and quark-antiquark annihilation. At next-to-leading order (NLO), processes such as flavor excitation and gluon splitting are involved. In this regime, divergences are regulated by the mass of the heavy quarks, which acts as an infrared cutoff except when the quark p_T is greater than its mass [2]. In that case, logarithmic divergences appear. The most advanced analytic pQCD techniques currently available allow for such divergences to be resummed, giving rise to the fixed-order-plus-next-to-leading-log (FONLL) approach [3]. Unfortunately, FONLL calculations exhibit very large error bands associated predominantly with uncertainties in the heavy quark masses and the renormalization scales, motivating the need for comparisons with experimental data.

A wealth of heavy-flavor-production data exists both at the Relativistic Heavy Ion Collider (RHIC) [4] and the Large Hadron Collider (LHC) [2]. At the LHC, such measurements comprise cross section measurements of inclusive heavy-flavor leptons, as well as of individual D (containing charm) and B (containing bottom) meson states. At RHIC, such measurements are consistent with FONLL calculations within uncertainties, yet systematically higher than the central value predicted by the theory. It is thus of interest to arrive at a simultaneous measurement of charm and bottom production at RHIC energies to leverage the distinct masses of these quarks to provide constraints for pQCD calculations.

Now, from the standpoint of high energy nuclear physics, heavy-ion collisions at RHIC and the LHC produce deconfined nuclear matter—known as the quark-gluon plasma (QGP). The QGP produced in these colliders can be characterized as a strongly coupled fluid [5] exhibiting, among other properties, substantial color opacity. This refers to the ability of the medium to hinder the passage of color charges, resulting in the energy loss of such particles [6]. Charm and bottom quarks are ex-

cellent probes of color opacity because they originate primarily from early-stage hard-parton-scattering processes, and thus transit through the entire evolution of the QGP medium [4].

The yield of heavy-flavor electrons at RHIC scales with the number of binary nucleon-nucleon collisions [7, 8] as a consequence of charm and bottom conservation by the strong interaction. Nevertheless, their spectrum is modified in central Au+Au collisions relative to the $p+p$ baseline, as quantified by the nuclear modification factor R_{AA} [8]. Heavy quarks are redistributed in momentum space, such that a strong suppression of heavy-flavor electrons is observed for $p_T > 5$ GeV/c, comparable in magnitude to that observed for light quarks [9, 10].

This constitutes a puzzling observation, as it challenges traditional interpretations of energy loss as proceeding exclusively through gluon radiation, requiring the inclusion of additional collisional mechanisms. To shed light on the interplay of radiative and collisional energy loss by leveraging the mass difference between charm and bottom, the PHENIX collaboration has measured separated heavy-flavor-quark yields from semileptonic decay electrons in Au+Au collisions using the silicon-vertex-detector upgrade [11]. Nuclear modification factors R_{AA} were calculated using a $p+p$ baseline measurement by the STAR collaboration [12] obtained via electron-hadron correlations with limited kinematic reach and large uncertainties.

In this paper, we present a new baseline measurement of heavy-flavor separation in $p+p$ at $\sqrt{s} = 200$ GeV using the same displaced-vertex analysis technique used in a previous PHENIX measurement made in Au+Au collisions at $\sqrt{s} = 200$ GeV [11]. Our new results with smaller uncertainties and extended kinematic range provide a valuable update for future measurements of heavy-flavor modification

II. EXPERIMENTAL SETUP

Figure 1 shows a transverse (beam) view of the PHENIX detector and its subsystems. Two midrapidity spectrometers, called the central arms, are shown on either side of the central magnet. With an acceptance of $|\eta| < 0.35$ and $\Delta\phi = \pi/2$, each arm provides tracking and particle identification capabilities. The magnetic field is generated by two pairs of coils in the pole faces of the central magnet such that when electric current runs in the same direction in both coils, a maximum field strength of 0.9 T is achieved at the beam location. A detailed description of the PHENIX detector is given in Ref. [13–15].

The drift chambers and three layers of multiwire-proportional pad chambers are the subsystems used

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* PHENIX Spokesperson: akiba@rcf.rhic.bnl.gov
† Deceased
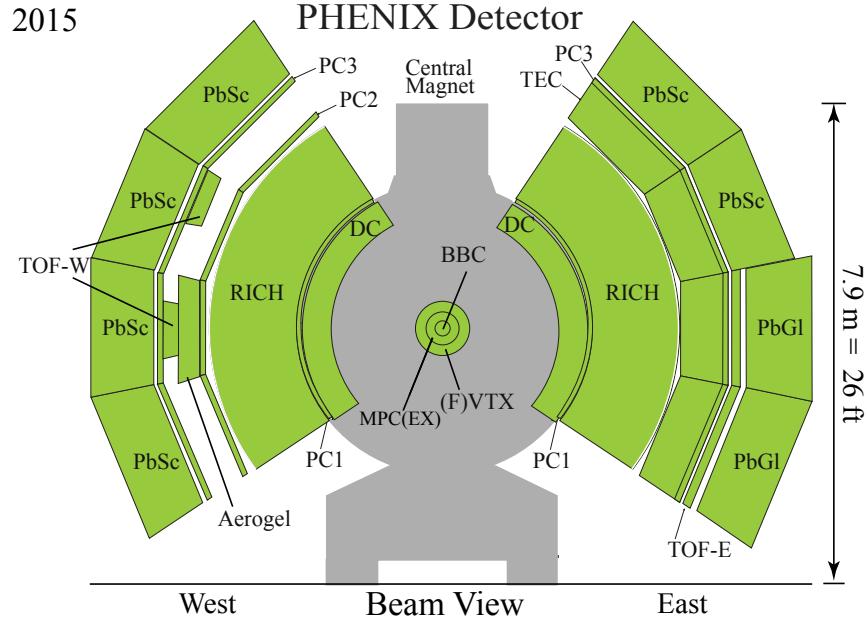
FIG. 1. Schematic view of the PHENIX detector configuration along the beam axis in the 2015 run period. The indicated subsystems are identified in the text.

for charged particle tracking [16]. The Ring Imaging Čerenkov (RICH) detector and the electromagnetic calorimeter (EMCal) are the subsystems used for electron identification. The RICH [17] comprises two independent volumes, one in each detector arm, filled with CO_2. The gas acts as a dielectric medium, in which electrons emit Čerenkov radiation for $p_T > 20$ MeV/c; pions can also emit light in the RICH above $p_T \approx 5$ GeV/c. The EMCal [18], which comprises lead-glass (PbGl) and lead-scintillator (PbSc) modules, is used to identify electrons based on the transverse shape of an electromagnetic shower and the ratio of the particle's energy deposit in the EMCal to the momentum of the reconstructed track.

Figure 2 shows the finely segmented silicon-vertex detector (VTX) [14, 19], which was installed as an upgrade in 2011 to provide tracking close to the interaction region, capable of reconstructing the primary vertex with a resolution on the order of 150 μm in $p+p$ collisions. The VTX comprises two arms with four independent layers arranged around the beam pipe at nominal radii of $r = 2.6$, 5.1, 11.8, and 16.7 cm. The material budget, expressed as a percentage of a radiation length is, for each layer, $X_0(\%) = 1.28, 1.28, 5.43$, and 5.43. Simultaneously with the VTX a new, thinner, beryllium beam pipe was installed in 2011 with a material budget of $X_0(\%) = 0.22$. Each layer comprises a series of ladders extending longitudinally. The VTX has an acceptance of $|\eta| < 1$ and $\Delta\phi \approx 0.8\pi$ per arm. Going from smallest to largest radius, individual layers are named B0, B1, B2, and B3. The innermost layers, B0 and B1, were constructed using silicon-pixel technology developed at CERN [20]. Pixels in these layers have dimensions 50μm $\times 425\mu$m, and are
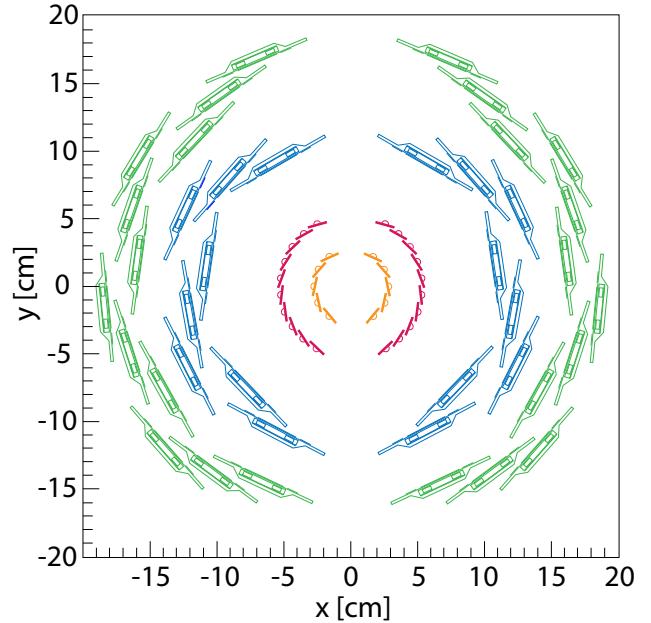

FIG. 2. Cross sectional view of the VTX detector showing the relative positions of individual layers B0, B1, B2, and B3 from smallest to largest radius.

arranged into lattices of 256×32 pixels which are read out by a single ALICE1LHCb sensor-readout chip [21]. Four readout chips constitute one sensor module, with four sensor modules in a single ladder. Layers B0 and B1 have 5 and 10 ladders per arm, respectively. Layers B2 and B3,

TABLE I. Lifetime $c\tau_0$ of selected D and B states [1].

Particle	Lifetime $c\tau_0$
D^0	129.9 μm
D^+	311.8 μm
B^0	457.2 μm
B^+	491.1 μm

were constructed using a novel silicon-stripixel technology developed at Brookhaven National Laboratory. Each 4.34×6.46 cm sensor in these layers is segmented into 80μm $\times 1000\mu$m stripixels. These are implanted with two serpentine metal strips defining two readout directions, X and U, such that the two-dimensional location of hit positions can be determined. Layers B2 and B3 have 8 and 12 ladders per arm, respectively, with 5(6) sensors per ladder in B2(B3). Stripixel sensors are read out using the SVX4 readout chip, developed by a collaboration between Fermilab and Lawrence Berkeley National Laboratory [22].

III. METHODS

The goal of this analysis is to measure the invariant yield of heavy-flavor electrons, independently for charm and bottom decays. This is accomplished by exploiting the fact that hadrons with bottom content have a longer lifetime than those with charm, as shown in Table I for B and D mesons [1]. As will be described in the following subsection, the provenance of heavy flavor electron tracks is determined statistically based on the distance of closest approach in the transverse plane (DCA_T) between the tracks and the beam center, which is the point relative to which they are reconstructed,

Thus, the longer lifetime of the B, and its decay kinematics, will result in a broader DCA_T distribution than for electrons from the shorter-lived D mesons. However, the measured electron candidate sample contains not only heavy flavor electrons, but also abundant background from a variety of sources (i.e., decays of π^0, η, ρ, ω J/ψ, $K^\pm$, K_s^0, Υ mesons and the Drell-Yan process, as well as conversions of direct and decay photons), each with its own characteristic DCA_T shape. Once this background has been determined, the DCA_T distribution of inclusive heavy flavor electrons can be isolated. The individual contributions from charm and bottom can then be obtained through an inversion procedure often referred to as unfolding [23]. We outline the steps involved in the analysis as follows:

1. Measure the DCA_T distribution of hadrons and electrons candidate tracks in data, as a function of track p_T.

2. Model the DCA_T distributions of nonheavy-flavor

background in the candidate electron sample by simulating the following electron sources: π^0, η, direct photons, J/ψ, K_s^0, $K^\pm$, and hadron contamination.

3. Determine the fraction of electrons attributable to each of the background sources considered, thus normalizing the background DCA_T distributions relative to those of electron candidates in data.

4. Separate the contribution of charm and bottom decays to the electron sample using Bayesian inference techniques. This step is constrained by the measured electron DCA_T distributions, as well as by the invariant yield of *inclusive* heavy-flavor electrons, previously published by the PHENIX collaboration [24].

This analysis used 110 pb^{-1} of integrated luminosity collected during the 2015 $p+p$ RHIC running period. A family of EMCal-RICH triggers were used to maximize the number of electron tracks available for analysis. These triggers segment the calorimeter and RICH detector into a series of tiles, triggering on events in which a certain energy threshold is exceeded in a calorimeter tile, and for some triggers requiring that a spatial match can be found in the RICH.

A. Measuring Track DCA_T

Track reconstruction is carried out using the central arm spectrometers, as detailed in Ref. [8]. Electron candidates within $1.5 < p_T[\mathrm{GeV}/c] < 6.0$ are identified by matching reconstructed tracks with hits in the RICH, and energy deposits in the EMCal.

Electrons traversing the RICH emit Čerenkov light, which is amplified by photomultiplier tubes (PMT). A maximum displacement of 5 cm is allowed between a track projection and the centroid of the hit PMTs. For tracks with $p_T < 5$ GeV/c, at least one PMT hit is required in the RICH, whereas at higher p_T at least three hits are required, given that pions in this kinematic region begin to radiate in the RICH.

Additionally, the energy E deposited by a track in the EMCal is required to match its momentum p, since—unlike hadrons—electrons deposit the majority of their energy in the calorimeter. This is quantified through the variable $dep = (E/p - \mu_{E/p})/\sigma_{E/p}$, where $\mu_{E/p}$ and $\sigma_{E/p}$ correspond to the mean and width of a Gaussian fit to the distribution of the energy-momentum ratio E/p around $E/p = 1$, respectively. A cut on $|dep| < 2$ is then used to select electrons.

Additional cuts involving the EMCal include restricting the displacement in Δz and $\Delta \phi$ between the track projection and the calorimeter shower to within three standard deviations. Finally, a cut on the probability that a given EMCal cluster originates from an electromagnetic shower—as determined from the shower shape—is used to reject hadrons.

Once identified in the central arms, reconstructed tracks are projected back to the VTX detector, where an iterative algorithm described in Ref. [11] is used to associate the track with VTX hits to create a VTX-associated track. Such tracks are required to have a hit in each of the two innermost layers of the VTX, and at least one hit in either of the outer layers, and to satisfy $\chi^2_{\mathrm{vtx}}/\mathrm{ndf} < 2$ to ensure the quality of the fit.
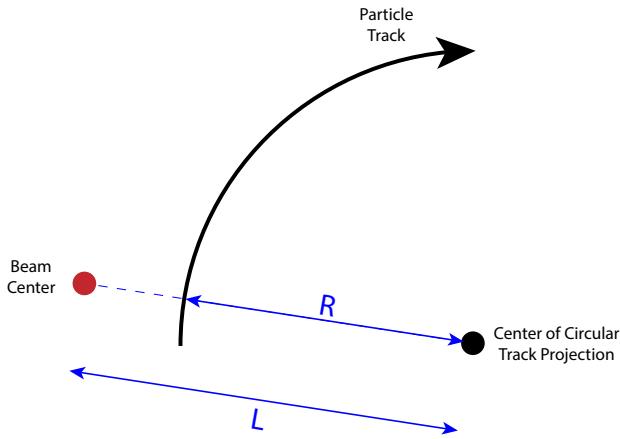

FIG. 3. Schematic diagram illustrating the definition of track DCA_T in the transverse plane, as $\mathrm{DCA}_T = L - R$.

Figure 3 shows a schematic diagram defining the DCA_T of a VTX-associated track. The circular track projection is shown in the transverse plane, where a constant magnetic field exists over the region covered by the VTX detector. The DCA_T is then defined as $\mathrm{DCA}_T = L - R$, where L is the distance between the beam center and the center of the projection, and R is the projection radius. The beam center is defined as the geometric center of the transverse region over which beam collisions occur, is constant over a given run period, and exhibits a Gaussian spread of width $\sigma_x^{(\mathrm{beam})} \approx 130$ μm and $\sigma_y^{(\mathrm{beam})} \approx 100\ \mu$m. Notice that DCA_T is a signed quantity which is not generally symmetric around zero, because electrons from some background sources exhibit asymmetric DCA_T distributions depending on the decay kinematics of their parent particles.

In a previous PHENIX analysis [11], the DCA_T was defined relative to the primary vertex of the collision, rather than the beam center. The primary vertex is determined using tracks reconstructed from VTX hits alone, with no reliance on the central arm tracking subsystems. However, given the low multiplicity of $p+p$ collisions, such a procedure does not converge to a vertex for approximately 50% all $p+p$ events. Furthermore, when it does converge—and particularly in events with electron tracks—the low number of reconstructed tracks makes it likely that the primary vertex is biased towards a displaced vertex and thus unsuitable for analysis. The choice of using the beam center for DCA_T determina-

TABLE II. Resolution of the primary vertex in the transverse plane, as a function of the number of reconstructed VTX tracks available for its determination.

Number of Tracks	$\sigma_x^{\mathrm{vertex}}$ [μm]	$\sigma_y^{\mathrm{vertex}}$ [μm]
2	296.5	207.0
3	195.0	141.2
4	157.3	113.7
5	132.7	97.0
6	118.8	77.8
7	98.8	72.8
8	89.6	60.3

tion is further justified because the primary-vertex resolution is quite similar to the beam spot spread. Table II shows the resolution of the precise vertex in the transverse plane, as a function of the number of reconstructed VTX tracks used in its determination. The resolution improves significantly with increasing number of tracks. However, due to the limited coverage of the VTX, the average number of tracks used to calculate the primary vertex in $p+p$ collisions is 3.2, such that the corresponding resolution is broader than the beam spread.
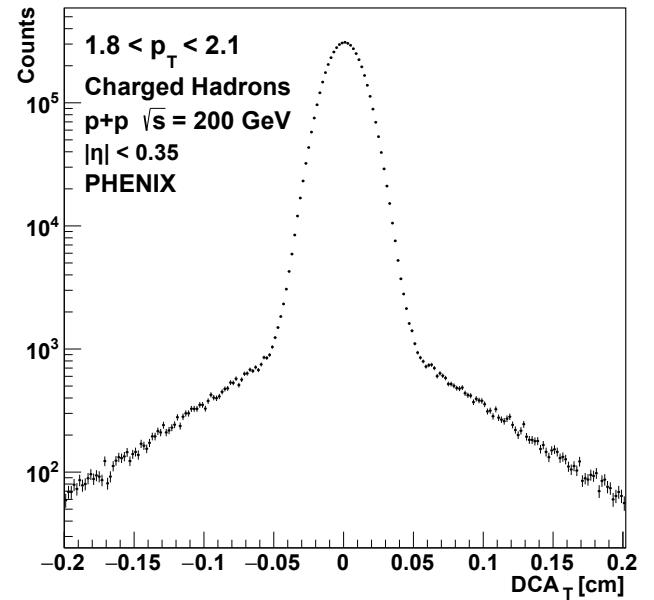

FIG. 4. DCA_T distribution of hadron tracks in data within $1.8\mathrm{GeV}/c < p_T < 2.1\mathrm{GeV}/c$, calculated relative to the beam center position.

Figure 4 shows the DCA_T distribution of hadron tracks within $1.8 < p_T[\mathrm{GeV}/c] < 2.1$, where the histogram corresponds to counts of tracks passing the analysis cuts, with no correction for acceptance or efficiency effects. Hadron tracks are subject to the same quality requirements as electron tracks, but are identified as hadrons

by requiring no RICH PMT hits. The very prominent Gaussian peak centered at $\text{DCA}_T = 0$ is attributed to particles originating from the primary collision point, with its width reflecting the beam spread, convolved with the track-pointing resolution. On the other hand, the broad tails can be attributed to long-lived light hadrons which decay, as well as background. It is observed that the DCA_T resolution improves with increasing track p_T. For this analysis, DCA_T distributions of electron candidate tracks were measured in 10 p_T bins between $1.5 < p_T[\text{GeV}/c] < 6.0$.

B. Modeling Electron Background Sources

In addition to heavy-flavor-decay electrons, the electron sample determined by applying the track cuts described in the previous section contains contributions from a variety of background sources. Namely, we consider (i) photonic electrons from the Dalitz decay of π^0 and η mesons, as well as photon conversions; (ii) nonphotonic electrons from the decay of J/ψ and the three-body decay of $K^\pm$ and K_s^0 (collectively called $Ke3$ electrons); and (iii) hadrons which are misidentified as electrons.

To isolate the heavy-flavor signal of interest, it is necessary to properly account for the background. Conversion electrons constitute the single largest source of background in this analysis owing to the material budget of the the VTX with $X_0(\%) = 13.42$ of a radiation length. In the following subsection we describe a strategy that uses the fine segmentation of the VTX itself to reject the vast majority of conversions based on the narrow opening angle topology of conversion electron pairs. The remaining background, both photonic and nonphotonic, is accounted for by constructing an electron cocktail normalized relative to the measured electron sample.

Of the background electron sources, all but misidentified hadrons can be modeled using previous measurements of primary (i.e., π^0, η, J/ψ, $K^\pm$, K_s^0) particle production combined with a knowledge of their decay modes and GEANT3 simulations of the PHENIX detector. Contributions from other sources of electrons, like the decay of vector mesons such as the Υ, ϕ, ω and ρ, as well as the Drell-Yan process, were found to contribute negligibly to the total electron background in the kinematic region of interest.

1. Photonic Electron Background

Photonic electrons originate from the Dalitz decay $(X \rightarrow e^+e^-\gamma)$ of π^0 and η mesons, and from the conversion of photons $(\gamma \rightarrow e^+e^-)$ interacting with the beam pipe or the VTX detector itself, where the photons are either direct photons or a hadronic decay product. To model this background, we start with the published cross section of π^0, η and direct photons in $p+p$ at $\sqrt{s} = 200$ GeV [25–28]. Single particles are then generated between $0 < p_T[\text{GeV}/c] < 20$ according to the published spectrum. For π^0 and η, accounting for branching ratios, the decay is forced to proceed exclusively through channels involving photons or electrons in the final state. The decay photons and electrons are fed through a GEANT3 simulation of the PHENIX detector, where the same reconstruction code and track cuts used in data are applied. The resulting reconstructed electron yield is normalized by the number of simulated primary particles, thus correctly describing the relative contribution of each primary source to the total photonic electron yield.

As previously mentioned, conversion electrons constitute the most significant source of background in this analysis, originating from the beam pipe as well as all four layers of the VTX. We can eliminate 80% of conversion electrons by imposing the requirement that tracks used in analysis have a hit in each of the innermost two layers of the VTX, thereby discarding electron tracks originating in the outer layers.

Given the narrow opening angle between the e^+e^- pair from photon conversions, a veto cut is defined to minimize the remaining conversions from the beam pipe and innermost two layers. In this approach, tracks with a VTX hit in close proximity, within a certain window in $\Delta\phi$ and Δz, are rejected. As illustration, if a conversion occurs in the beam pipe, or in B0, then nearby pairs of hits will be found in subsequent detector layers. If at least one of these electrons is reconstructed as a track, the conversion veto cut will reject it based on the presence of at least one nearby hit within the window in any layer.

The size of the conversion veto window in chrg $\times \Delta\phi$, where chrg is the charge of the track and $\Delta\phi$ is the azimuthal distance between track and cluster on the surface of a VTX chip, is shown in Fig. 5. It depends on the track p_T, as well as the layer where the nearby cluster is found. In general, because the bend of conversion electron pairs in the magnetic field decreases with photon momentum, the windows become narrower with increasing electron p_T. Furthermore, due to multiple scattering as well as the separation of electron pairs in the magnetic field, windows in the outer layers are larger than in the inner layers. The windows are asymmetric because the quantity chrg $\times \Delta\phi$ is positive by construction; the negative side of the window is populated by mismeasured tracks which do not yield a positive chrg $\times \Delta\phi$. In the longitudinal direction, the conversion veto window is $|\Delta z| < 0.05$ cm in the innermost two VTX layers, and $|\Delta z| < 0.1$ cm in the outermost two.

The survival rate ε of electrons from a given source is defined as the probability that they will not be rejected by the conversion veto cut. Figure 6 shows the survival rate of electrons from photonic and nonphotonic sources as a function of electron track p_T, where the nonphotonic survival rate has been estimated using hadrons in data as a proxy. The survival rate of photonic electrons has been further broken down by background source, namely π^0 and η decays, as well as photon conversions.
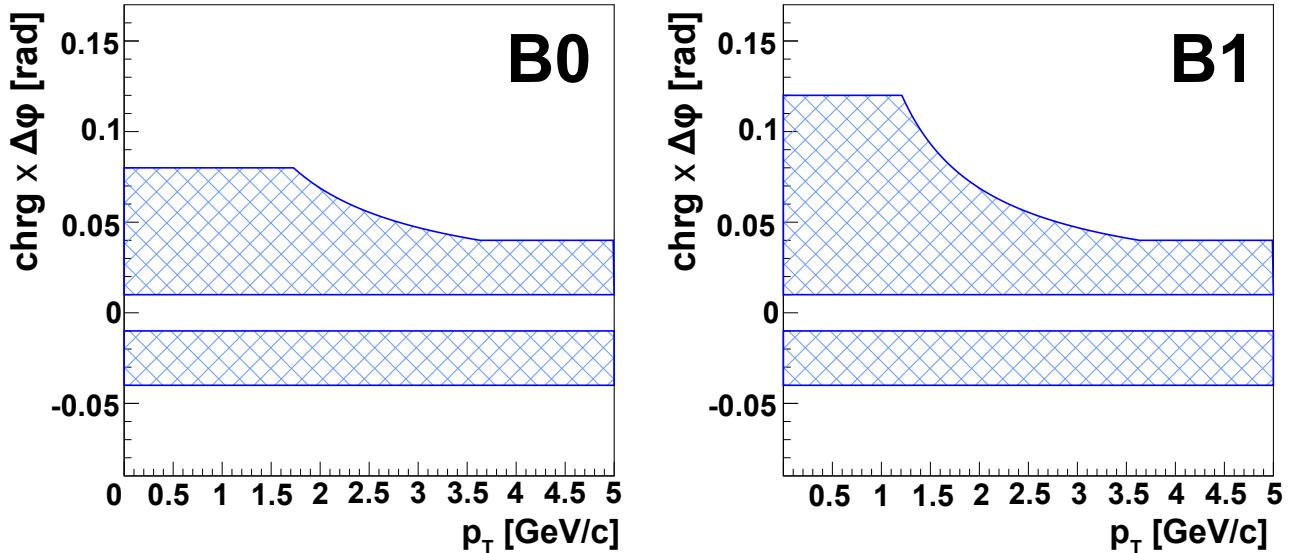
FIG. 5. Track p_T-dependent window in chrg $\times \Delta\phi$ used in the conversion veto cut in the pixel detector layers, where chrg is the charge of a given track and $\Delta\phi$ is the azimuthal separation between clusters, one of which is associated with the track.
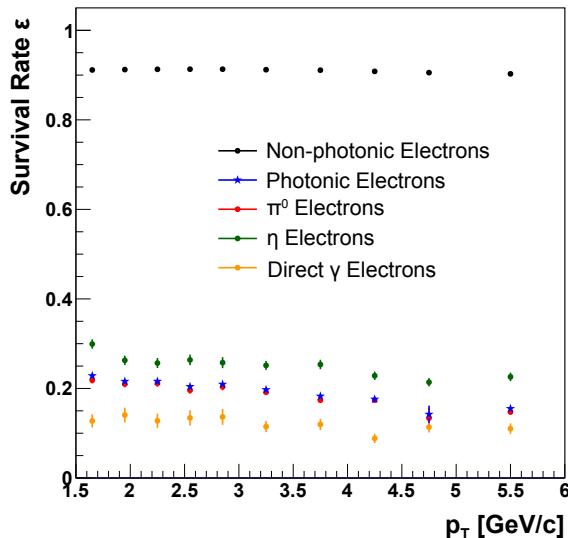

FIG. 6. Conversion veto cut survival rates for nonphotonic, and photonic electrons from various sources. The total photonic survival rate is the weighted average of the individual sources.

opening angle than conversions pairs. The survival rate of all photonic electrons combined is shown in blue in Fig. 6 to be approximately 20%. This demonstrates the ability of the conversion veto cut to reject a substantial fraction of the photonic background. In contrast, the survival rate of nonphotonic electrons is very high, at approximately 90%. The conversion veto cut rejects a small fraction of nonphotonic electrons due to the presence of uncorrelated random hits in the window, which affect all tracks regardless of their provenance. The particular size of the conversion veto windows used in this analysis represents a compromise between maintaining a large window for background rejection, and limiting its size to minimize the inclusion of uncorrelated hits.

After applying the conversion veto cut on electrons in the photonic cocktail, the contribution of each primary particle source to the total photonic background can be calculated, as shown in Fig. 7(a). Electrons from π^0 (both Dalitz and from the conversion of decay photons) dominate the background for all p_T, with direct photon external conversions becoming more significant at higher p_T.

2. Non-photonic Electron Background

Non-photonic electrons in this analysis correspond to those from the decay of J/ψ mesons, as well as the three-body decays of $K^{\pm}$ and K_s^0, collectively known as $Ke3$ electrons ($K \to e\nu\pi$). Other background electron sources, namely the decays of vector mesons such as the Υ, ρ, ω, and ϕ were considered in the background cocktail, but

Conversion electrons, such as those shown from direct photons, have the lowest survival rate of all. Electrons from π^0 and η mesons have a higher survival probability because they include—in addition to photon conversions—Dalitz electron pairs which have a wider

were found to contribute negligibly.

The approach to modeling nonphotonic background is similar to that used for photonic sources. Namely, single particles are generated according to their respective published cross section, as measured by the PHENIX collaboration [29–31], forced to decay, and the resulting particles fed through a GEANT3 simulation of the detector. Applying the full set of analysis track cuts, including the conversion veto cut, we complete the background electron cocktail. The fraction of nonphotonic electrons from each source, relative to the total photonic background is shown in Fig. 7(b). Notice that the J/ψ contribute more to the background cocktail than any other background source above $p_T \approx 3.5$ GeV/c.

3. Hadron Contamination

Despite the electron identification cuts described in the previous section, some hadron tracks will incorrectly be tagged as electrons. This contribution to the electron sample is modest and is estimated in two independent ways, making use of EMCal and RICH signals.

Unlike hadrons, electron tracks deposit the majority of their energy in the EMCal, as quantified by the ratio E/p, where E is the calorimeter energy and p is the track momentum. The variable dep, as previously defined, takes the shape of a Gaussian of zero mean and unit width for true electron tracks. In contrast, the dep distribution of hadron tracks exhibits a very different shape. Thus, a template is constructed, as a function of p_T, by fitting the dep distribution of hadrons tracks in data. The dep distribution of electron candidates is then fit with a combination of the hadron template plus a Gaussian, with a single free parameter corresponding to their relative contribution. The value of this parameter provides an estimate of the fraction of hadron contamination in the sample.

An independent way of estimating the hadron contamination is to exploit the fact that imposing a cut requiring a minimum number of PMTs fired in the RICH provides greater rejection power for hadron tracks than for electrons. The fraction of hadrons rejected by such a cut can be estimated from hadron tracks in data, while the fraction of rejected electrons can be determined through GEANT3 simulation of single electrons. With these two pieces of information it is possible to isolate the number of hadrons and electrons in the candidate electron sample, thus determining the contamination fraction.

The weighted average of the two independent estimates of hadron contamination is taken as the nominal value, with their difference as a systematic uncertainty, as shown in Fig. 8. The systematic uncertainties are assigned to encompass both estimates and are asymmetric.

Another source of contamination comprises electron tracks identified in the central arms which are associated with uncorrelated random hits in the VTX detector, leading to the creation of a spurious VTX-associated track.

The degree of contamination arising in this manner was quantified by rotating all hits in the VTX in azimuth and polar angles by a small amount and attempting to reassociate central arm tracks with the rotated hits. Given the low multiplicity of $p+p$ collisions, the contribution of misassociated central-arm tracks was found to be negligible, unlike in Au+Au collisions where it is significant.

C. Normalizing Electron Background DCA$_T$

In 2015—the year in which the $p+p$ data was collected—the VTX detector exhibited a time-varying acceptance from a changing number of dead, cold, and hot channels across the surface of each detector layer over time. This precluded the measurement of an electron candidate sample fully corrected for acceptance and efficiency effects. As a result, the simulated electrons in the background cocktail are not corrected for acceptance and efficiency, but simply constructed in such a way that the same reconstruction code and analysis cuts used in data are applied.

The cocktail can then be used to calculate the fraction of electrons from each background source relative to the total photonic background. However, to use this information to determine their normalization relative to the total sample of electron candidates, it is necessary to determine the fraction of electron candidates attributable to photonic background. This is accomplished via a data-driven method relying on the conversion veto cut.

Let N_P and N_{NP} be the number of photonic and nonphotonic electrons in the electron candidate sample obtained without applying the conversion veto cut. Also, let ε_P and ε_{UC} be the veto cut survival rate of photonic electrons due to correlated effects and due to noncorrelated effects, respectively. In this nomenclature, heavy-flavor electrons are part of the nonphotonic sample. The number of electrons measured without the conversion veto cut is then simply

$$N_e = N_P + N_{\mathrm{NP}}, \tag{1}$$

while the number of measured electrons that pass the veto cut is given by

$$\tilde{N}_e = \varepsilon_P \times \varepsilon_{UC} \times N_P + \varepsilon_{UC} \times N_{\mathrm{NP}}, \tag{2}$$

where N_P is modified by both ε_P and ε_{UC} because photonic electrons are also susceptible to rejection from uncorrelated hits in the window. Taken together, Eqs. 1 and 2 form a system of equations with N_P and N_{NP} as the only unknowns, yielding

$$N_P = \frac{\tilde{N}_e - N_e \varepsilon_{UC}}{\varepsilon_{UC}(\varepsilon_P - 1)}, \tag{3}$$

and

$$N_{\mathrm{NP}} = \frac{N_e \varepsilon_P \varepsilon_{UC} - \tilde{N}_e}{\varepsilon_{UC}(\varepsilon_P - 1)}. \tag{4}$$
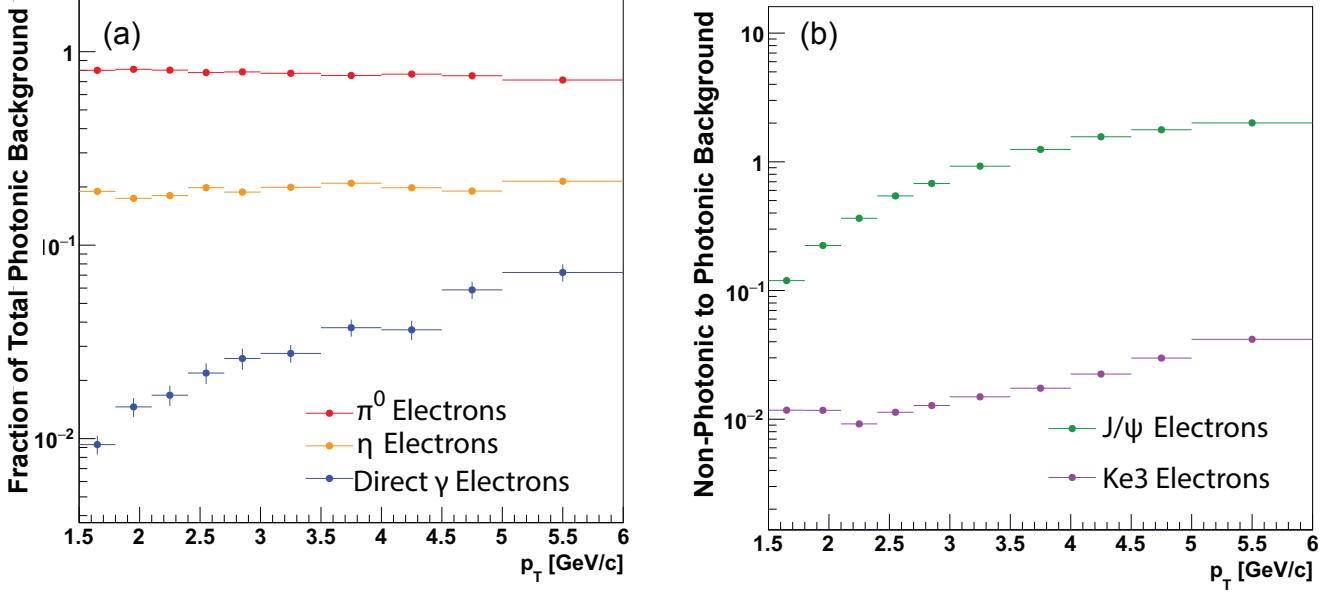
FIG. 7. (a) Fraction of electrons from individual photonic sources relative to the total photonic electron background as determined by constructing a background electron cocktail. (b) Fraction of electrons from individual nonphotonic sources relative to the total photonic background.
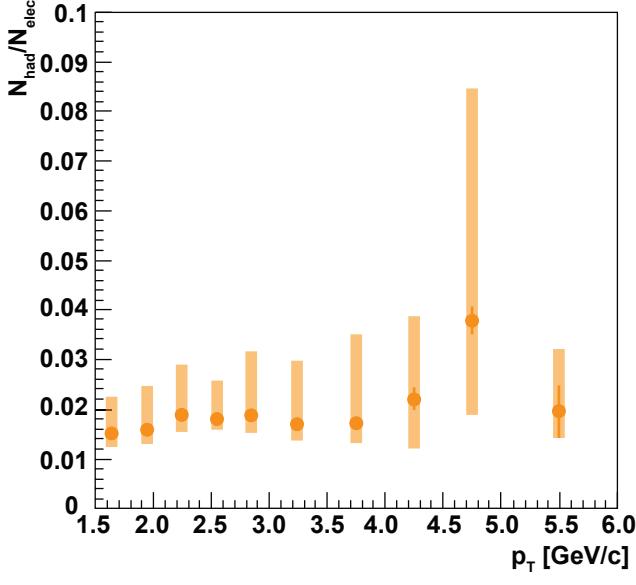

FIG. 8. Fraction of electron candidates in data attributed to hadron contamination as a function of p_T.

FIG. 9. Fraction of photonic electrons to inclusive electrons in data, as a function of electron p_T.

The fraction of photonic electrons in the sample with the conversion veto cut applied is then

$$F_P = \frac{\varepsilon_P \varepsilon_{UC} N_P}{\varepsilon_P \varepsilon_{UC} N_P + \varepsilon_{UC} N_{\mathrm{NP}}}, \tag{5}$$

and is shown in Fig. 9 as a function of electron p_T. Using F_P, the fraction of candidate electrons attributable to

each photonic source in data is

$$f_i^{\mathrm{phot}} = F_P(1 - F_{\mathrm{contam}}) \frac{\tilde{N}_i}{\tilde{N}_{\pi^0} + \tilde{N}_\eta + \tilde{N}_\gamma}, \tag{6}$$

where i is an index referring to a primary particle species (i.e., π^0, η, γ); $\tilde{N}_i$ is the number of electrons from the ith

source that pass the conversion veto cut in the electron cocktail, and $1 - F_{\text{contam}}$ is the purity of the electron sample from hadron contamination.

In the case of nonphotonic background, it is impossible to construct a similar expression because the electron cocktail does not include contributions from heavy-flavor mesons. Therefore, the nonphotonic background is normalized relative to the simulated π^0 electron yield, whose absolute normalization has been previously determined, as follows

$$f_j^{\text{nonphot}} = f_{\pi^0}^{\text{phot}} \frac{\tilde{N}_j}{\tilde{N}_{\pi^0}}, \qquad (7)$$

with j indexing the primary particles giving rise to nonphotonic electrons (i.e., J/ψ and $Ke3$).
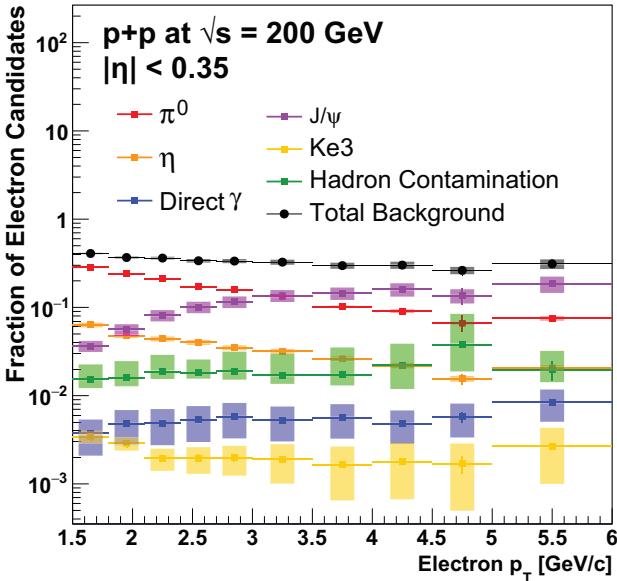
FIG. 10. Fraction of the measured candidate electron sample attributable to various sources of background electrons as a function of p_T.

These factors, shown in Fig. 10, are used to normalize the DCA_T distribution of each background electron source relative to the electron candidate sample. Fig. 11 shows the DCA_T distribution of electrons from each background species within $1.8 < p_T[\text{GeV}/c] < 2.1$, normalized relative to the total number of electron candidates in that p_T bin. Unlike prompt electrons, which exhibit a Gaussian DCA_T shape, $Ke3$ electrons originate from long-lived kaon decays, which results in their characteristic DCA_T shape.

In general, the resolution of the DCA_T is a consequence of the width of the beam spot convolved with the track-pointing resolution. However, the simulations used to create the background electron cocktail were run using a single reference value for the beam spot size, which in reality fluctuates over time during data-taking. Therefore, it is necessary to correct for the difference in resolution
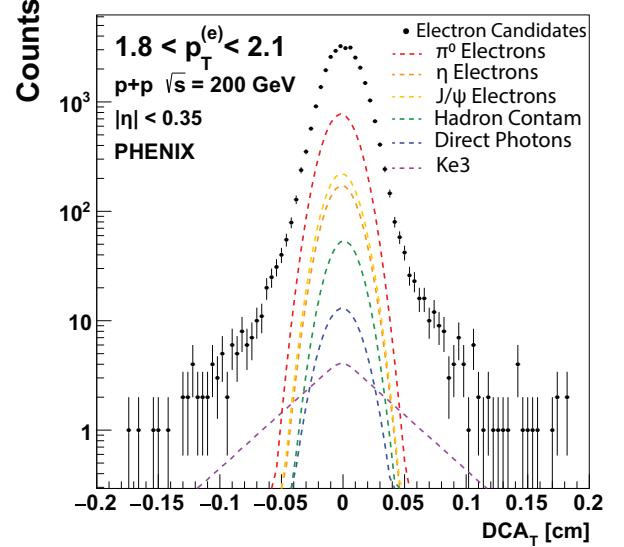
FIG. 11. DCA_T distribution of candidate electron tracks within $1.8 < p_T[\text{GeV}/c] < 2.1$, which pass the conversion veto cut. Also shown are the absolutely normalized DCA_T distributions from each simulated background electron source, as well as hadron contamination.

TABLE III. Resolution of the DCA_T distribution of charged pion tracks as reconstructed in data and in Monte Carlo GEANT3 simulations of the PHENIX detector.

Electron p_T [GeV/c]	Data Resolution [μm]	MC Resolution [μm]
$1.5 < p_T < 1.8$	134.1	122.1
$1.8 < p_T < 2.1$	131.7	121.0
$2.1 < p_T < 2.4$	130.1	119.9
$2.4 < p_T < 2.7$	128.9	118.9
$2.7 < p_T < 3.0$	127.9	118.5
$3.0 < p_T < 3.5$	126.8	118.2
$3.5 < p_T < 4.0$	126.2	117.9
$4.0 < p_T < 4.5$	125.5	117.6
$4.5 < p_T < 5.0$	125.1	117.2
$5.0 < p_T < 6.0$	124.8	116.9

between simulations and data. This was accomplished by comparing, as a function of p_T, the DCA_T resolution of charged pions in data and simulation, as quoted in Table III deriving a p_T-dependent factor such that the simulated DCA_T distributions could be broadened to match the resolution in data. This broadening factor was applied to electrons from every species in the background electron cocktail.

D. Heavy-Flavor Separation via Unfolding

Having normalized the electron background DCA_T distributions, it is possible to isolate the corresponding distributions of electrons from heavy-flavor decays in data. If the shapes of the parent hadron spectra were known a priori, it would be a straightforward matter to use the knowledge of heavy-flavor-decay kinematics to determine the shape of the DCA_T distributions of charm and bottom electrons separately, whose relative normalization could then be constrained by the measured inclusive DCA_T.
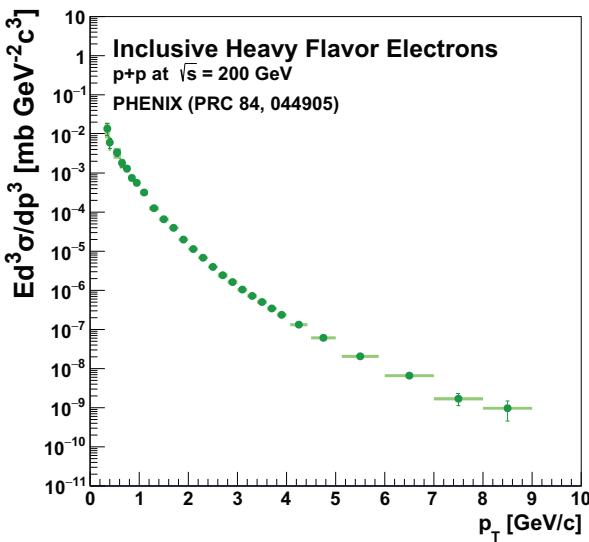
FIG. 12. Invariant cross section of inclusive heavy-flavor-electron production in $p+p$ collisions, as measured by the PHENIX experiment [24], and used as input for the flavor-electron-separation-unfolding procedure.

However, because such spectral shapes are not known for D and B mesons, it becomes necessary to solve an inverse problem where the model parameters (i.e., the spectrum of hadrons containing open charm and bottom, as a function of p_T) are inferred from data observations, namely the DCA_T and spectrum of inclusive heavy-flavor electrons. For the spectrum, an earlier PHENIX measurement [24] was used, shown in Fig. 12.

To solve the inverse problem, it is necessary to construct a mapping from the model parameters to the data. Given that the heavy-flavor-decay kinematics are known, it is possible to assign a probability for a heavy flavor hadron at a given $p_T^{(h)}$ to decay into an electron with a certain $p_T^{(e)}$ and DCA_T. Such mapping makes it possible to quantify the likelihood that a given set of trial hadron spectra is consistent with the measured electron spectrum and DCA_T distributions.

We use a probabilistic approach [23] to the unfolding

problem based on Bayesian inference, identical to that used by PHENIX to separate charm and bottom electron yields in Au+Au collisions [11]. Let $\mathbf{Y}^{\mathrm{data}}$ be a vector whose individual elements correspond to the yield of inclusive heavy-flavor electrons, as shown in Fig. 12. Similarly, $\mathbf{D}_j^{\mathrm{data}}$ is a vector of the binned DCA_T distribution of electrons in data, for tracks in the jth p_T bin, out of nine bins between $1.5 < p_T[\mathrm{GeV}/c] < 6.0$. The two observables are combined in a 'data' vector

$$\boldsymbol{x} = (\mathbf{Y}^{\mathrm{data}}, \mathbf{D}_0^{\mathrm{data}}, \dots, \mathbf{D}_8^{\mathrm{data}}). \qquad (8)$$

The model parameters are also represented as a vector

$$\boldsymbol{\theta} = (\boldsymbol{\theta}_c, \boldsymbol{\theta}_b), \qquad (9)$$

where $\boldsymbol{\theta}_c$ and $\boldsymbol{\theta}_b$ correspond to the charm and bottom hadron yields, respectively, in 17 p_T bins each, between $0 < p_T[\mathrm{GeV}/c] < 20$.

Bayes' theorem, as written below

$$P(\boldsymbol{\theta} \mid \boldsymbol{x}) = \frac{P(\boldsymbol{x} \mid \boldsymbol{\theta})\pi(\boldsymbol{\theta})}{P(\boldsymbol{x})}, \qquad (10)$$

relates the probability that a given set of model parameters $\boldsymbol{\theta}$ are true given the data $\boldsymbol{x}$, to the probability that the data follow from an assumed set of model parameters. While the former probability—known as the *posterior*—is a difficult quantity to estimate, the latter—known as the *likelihood*—is straightforward to compute given the knowledge of heavy-flavor decays. The quantity $\pi(\boldsymbol{\theta})$, known as the *prior*, corresponds to the knowledge of the model parameters prior to the data being analyzed. The denominator $P(\boldsymbol{x})$, sometimes known as the *evidence*, provides the normalization for the posterior. Thus, Bayes' theorem allows us to take a first guess regarding the model parameters, as encoded in the prior, and refine it through the inclusion of data in the likelihood.

The 17 bins for both the charm and bottom hadron spectra within $0 < p_T^{(h)}[\mathrm{GeV}/c] < 20$, as represented by $\boldsymbol{\theta}$, define a 34-dimensional space of model parameters. Starting with an initial set of values given by the prior $\pi(\boldsymbol{\theta})$, corresponding to the charm and bottom yields as calculated with PYTHIA[1], the unfolding proceeds by drawing trial sets of hadron yields, corresponding to individual points in the multi-dimensional parameter space. Because sampling such a large-dimensional space uniformly is computationally prohibitive, we use a Markov chain Monte Carlo (MCMC) algorithm [32], which proceeds iteratively until convergence of the final solution

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[1] We used PYTHIA6.2, with parton distribution functions (PDFs) given by CTEQ5L. The following parameters were modified: MSEL = 5, MSTP(91) = 1, PARP(91) = 1.5, MSTP(33) = 1, PARP(31) = 2.5. For bottom (charm) hadron studies, PARJ(13) = 0.75 (0.63), PARJ(2) = 0.29 (0.2), PARJ(1) = 0.35 (0.15).

is achieved. In this analysis, three iterations suffice for convergence with 500 parallel "walkers" and 1000 burn-in steps, as described in [32].

For each trial $\boldsymbol{\theta}$, we predict an electron p_T spectrum and DCA_T distribution as follows

$$\boldsymbol{Y}(\boldsymbol{\theta}) = \boldsymbol{M}^{(\boldsymbol{Y})}\boldsymbol{\theta}_c + \boldsymbol{M}^{(\boldsymbol{Y})}\boldsymbol{\theta}_b, \tag{11}$$

$$\boldsymbol{D}_j(\boldsymbol{\theta}) = \boldsymbol{M}_j^{(\boldsymbol{D})}\boldsymbol{\theta}_c + \boldsymbol{M}_j^{(\boldsymbol{D})}\boldsymbol{\theta}_b, \tag{12}$$

where $\boldsymbol{M}^{\boldsymbol{Y}} : p_T^{(h)} \to p_T^{(e)}$ is a matrix encoding the probability of a hadron of $p_T^{(h)}$ of any rapidity to yield an electron of $p_T^{(e)}$ at midrapidity, while $\boldsymbol{M}_j^{(\boldsymbol{D})} : p_T^{(h)} \to \mathrm{DCA}_T^{(e)}$ encodes the probability of yielding an electron at a given DCA_T value. The construction of these matrices using the PYTHIA generator is described in detail in Ref. [11], and includes the decays of charm hadrons ($D^\pm, D^0, D_s$, and Λ_c), and bottom hadrons ($B^\pm$, B^0, B_sm and Λ_b). Additional Monte Carlo generators could be used to construct the matrix, but this would be computationally prohibitive. For the purposes of this analysis, an additional matrix was introduced to model the detector response, mapping the *truth* p_T and DCA_T values in $\boldsymbol{M}^{(\boldsymbol{Y})}$ and $\boldsymbol{M}_j^{(\boldsymbol{D})}$ to their *reconstructed* counterparts, allowing for a direct comparison between the data and the predicted distributions from a given set of trial parameters $\boldsymbol{\theta}$.

The predicted spectrum and DCA_T distributions are then used to compute the (log)likelihood as follows

$$\begin{aligned}\ln P(\boldsymbol{x} \mid \boldsymbol{\theta}) = {}& \ln P(\boldsymbol{Y}^{\mathrm{data}} \mid \boldsymbol{Y}(\boldsymbol{\theta})) \\ & + \sum_{j=0}^{8} \ln P(\boldsymbol{D}_j^{\mathrm{data}} \mid \boldsymbol{D}_j(\boldsymbol{\theta})), \end{aligned} \tag{13}$$

where the log-likelihood for the $\boldsymbol{Y}^{\mathrm{data}}$ term is modeled as a multi-variate Gaussian with diagonal covariance, while the log-likelihood for the $\boldsymbol{D}_j$ term is modeled by a multivariate Poisson distribution, with full details provided in Ref. [11].

To constrain the shape of the unfolded charm and bottom spectra, ensuring its smoothness, a regularization term is added to the log-likelihood function, as follows

$$\ln \pi(\boldsymbol{\theta}) = -\alpha^2(|\boldsymbol{L}\boldsymbol{R}_c|^2 + |\boldsymbol{L}\boldsymbol{R}_b|^2), \tag{14}$$

where $\boldsymbol{R}_c$ and $\boldsymbol{R}_b$ correspond to the ratios of the trial vector of charm and bottom spectra to the prior. The matrix $\boldsymbol{L}$ is a 17×17 discretized second-order finite-difference matrix, effectively corresponding to the second derivative operator. Thus, the addition of this term enhances the log-likelihood for solutions with large curvature, effectively penalizing deviations from smoothness. The optimal regularization strength α is determined by carrying out a scan of various possible parameter values

and calculating the total log-likelihood of the unfolding solution in each case, comparing it to the case with no regularization. The desired optimal value is that which maximizes the log-likelihood, and is found to be $\alpha = 1$.

The end result of the Monte Carlo exploration of the parameter space is a set of probability distributions for each of the 34 model parameters, corresponding to the value of each bin of the charm and bottom hadron spectra integrated over all rapidities, including the correlations among them, as depicted in Fig. 13(a). The diagonal of the triangle shows the marginal probability distribution for each of the 17 bins of the charm and bottom hadron spectra. Correlations among bins are shown in the upper triangular [green] area for p_T^c and p_T^c, the far-right triangular [blue] area for p_T^b and p_T^b, and the lower-left square [orange] area for p_T^b and p_T^c. Panels Fig. 13(b) and (d) show the marginal distributions in detail for charm and bottom hadrons in two selected p_T bins. We select the parameter that maximizes the marginal distributions as the desired value of the spectrum at each bin; the 16th and 84th quantiles of the distribution are taken as the 1σ uncertainty associated with the point estimate, as indicated by the dotted lines.

Panel Fig. 13(c) shows the joint probability distribution of the charm and bottom hadron yields for the p_T bins in Fig. 13(b) and (d). The shape of the distribution indicates the existence of a strong negative correlation between the yields in the bins at hand. It is possible to see that the bins are largely uncorrelated, except for intermediate p_T^b and p_T^c, where a strong negative correlation exists due to the yields being similar in this kinematic region. For the correlations among bins in the same hadron spectrum, a very strong positive correlation is seen among neighboring p_T bins owing to the smoothness requirement on the unfolded spectra, which is imposed via regularization.

The unfolded yield of charm and bottom hadrons can be tested for consistency with the inputs provided, namely the spectrum and DCA_T distributions of inclusive heavy-flavor electrons, by applying the decay matrices to the unfolded result. Figure 14 shows the so-called 'refolded' spectra of charm (bottom) electrons in green (blue), along with their sum, in red. The refolded inclusive spectrum compares very well with the published spectrum, as shown by the ratio plot in the bottom panel. Similarly, Fig. 15 shows, for every electron p_T bin, the refolded inclusive electron DCA_T distributions, its charm and bottom components, and the total background DCA_T, obtained as discussed in section III C. The ratio plots in the bottom panel demonstrate an excellent agreement with the DCA_T of measured electrons. The shaded gray region indicates the range over which the DCA_T is used in the unfolding procedure. Notice that bottom electrons have a broader DCA_T than those from charm, as expected.
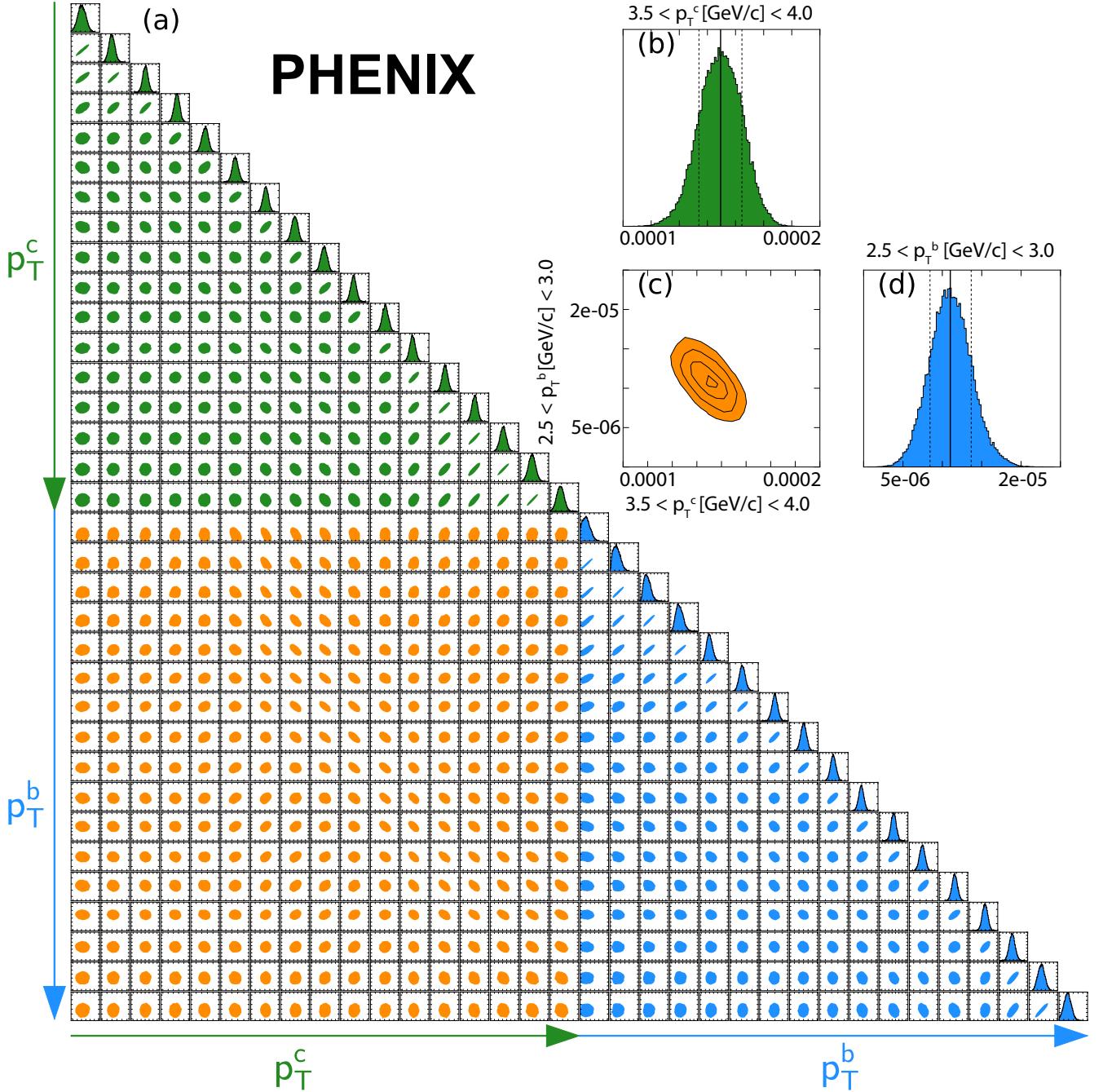
FIG. 13. (a) Joint probability distributions of bottom and charm hadron yields. The marginalized distribution for each p_T bin is shown along the diagonal. Correlations among bins are shown in the upper triangular [green] area for p_T^c and p_T^c, the far-right triangular [blue] area for p_T^b and p_T^b, and the lower-left [orange] area for p_T^b and p_T^c. (b)-(d) Correlation between charm and bottom yields in two particular p_T bins, along with the marginalized distributions in those bins. See text for details.

IV. SYSTEMATIC UNCERTAINTIES

The unfolding procedure, as described in section III D, takes the measured electron DCA_T distributions and published electron spectrum as inputs, along with their corresponding statistical uncertainties, which are propagated to the final result. However, additional sources of systematic uncertainty must be taken into account. Namely, we identify the following as the most significant:

1. the normalization of individual sources in the background electron cocktail;

2. the systematic uncertainty on the inclusive heavy-flavor electron spectrum;
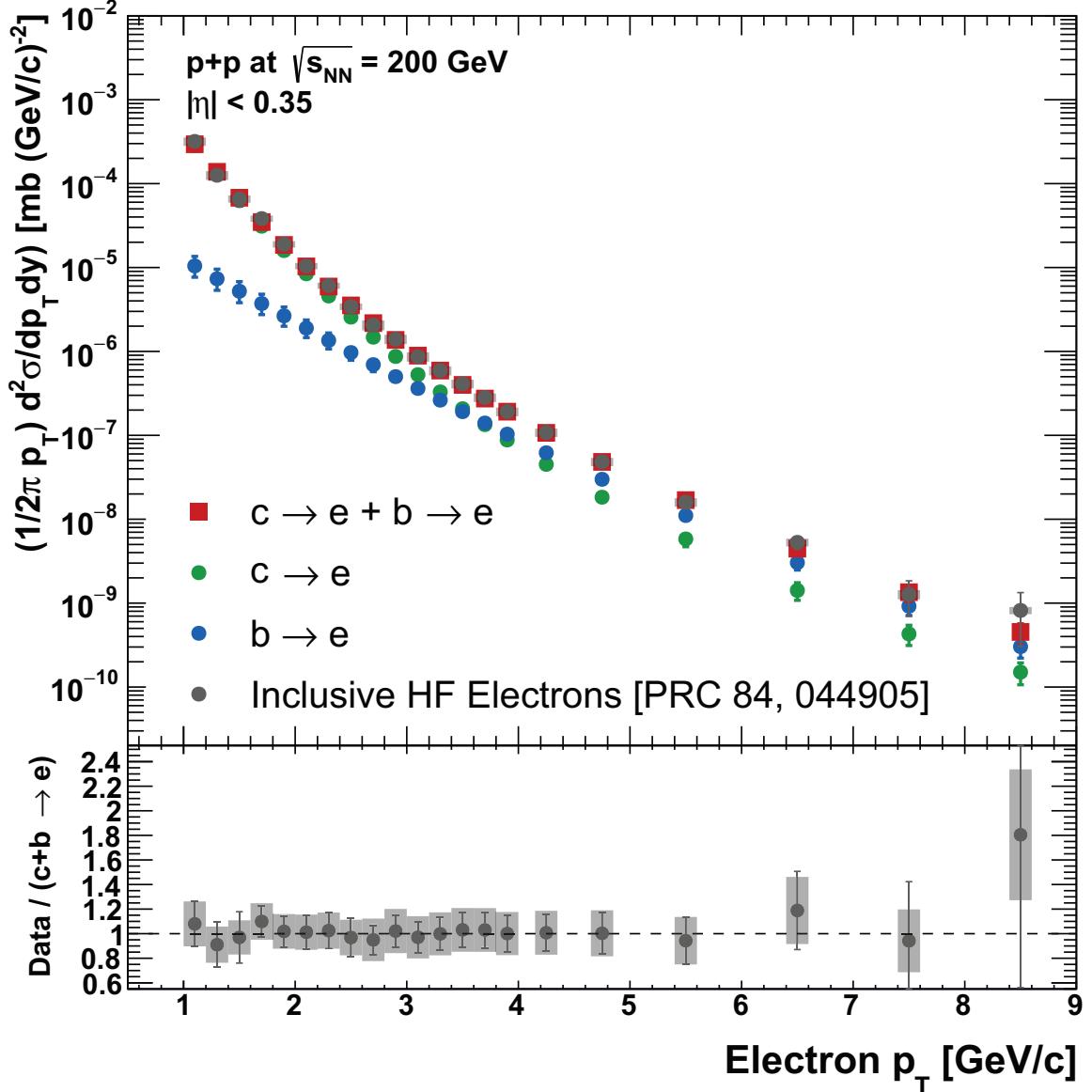
FIG. 14. Inclusive heavy-flavor-electron invariant yield from the refolded charm and bottom yields (closed squares [red]) compared to published data (closed circles [gray]). Individual refolded spectra from charm and bottom are shown in green and blue, respectively.

3. the choice of the regularization parameter strength α in the unfolding procedure; and

4. the choice of prior used in the unfolding.

The uncertainty associated with the normalization of individual electron background components originates from the parameterization of the associated primary particle spectrum. Each spectrum is repeatedly deformed randomly within the extent of its own statistical and sys-tematic uncertainties, with a new parameterization being obtained at every iteration. The RMS value of all param-eterizations is then taken as the associated systematic un-certainty. In this manner, a systematic uncertainty will exist for every background electron source in the cocktail. Their combined effect on the unfolded result is estimated by running the unfolding procedure for every combina-tion of individual background normalizations, raised and lowered by their associated parameterization uncertainty.
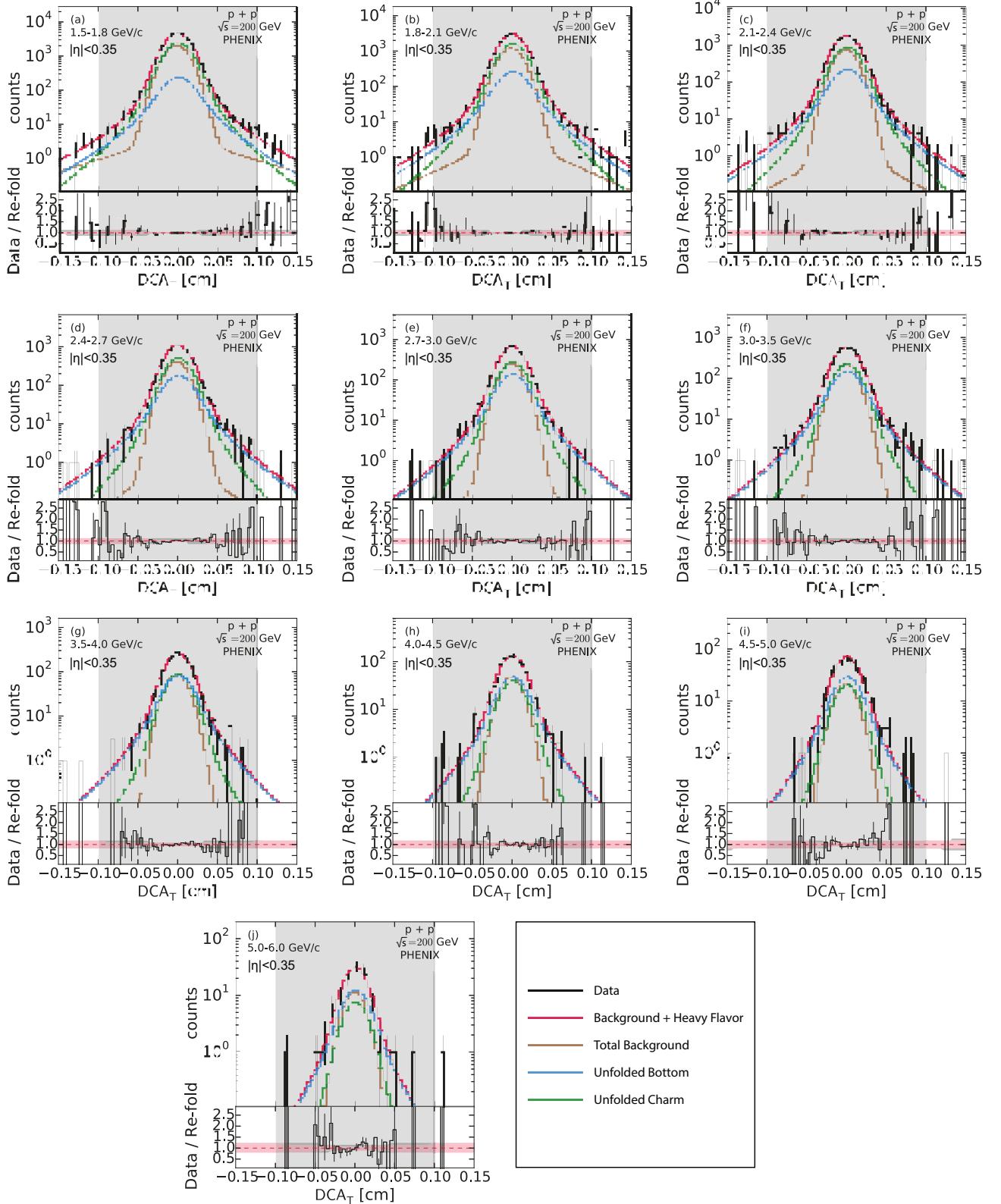
FIG. 15. DCA$_T$ distribution of electron candidates in various p_T bins, along with the contribution from total background electrons (brown) and the refolded electrons from charm (green) and bottom (blue) hadron decays. The sum of these three components is shown in red, and the ratio with the data is shown in the bottom panels. The shaded gray areas indicate the region over which the DCA$_T$ provides constraints for the unfolding procedure.

To estimate the p_T-correlated systematic uncertainties associated with the inclusive heavy-flavor-electron spectrum, we deform the shape of the spectrum by tilting and kinking the curve about two pivot points, at $p_T = 2.5$ GeV/c and $p_T = 5.0$ GeV/c. The choice of these points is motivated by specific features of the previous analysis which produced the inclusive heavy-flavor-electron spectrum [24], related to the method of background subtraction. Tilting refers to a rotation of the spectrum about one of the two pivots, such that the first and last points go up and down, respectively, by a fraction of their systematic uncertainty. The kinking of the spectrum introduces a deformation whereby the spectrum takes on a "v" shape at the pivots. This procedure resulted in 8 variations of the spectrum. The ones that resulted in the largest deviation from the nominal unfolded result were taken as the associated systematic uncertainty.

Section III D described how the optimal value of the regularization strength α maximizes the total log-likelihood of the unfolded solution. An uncertainty on this value is determined by finding the values of α around the maximum which lead to a decrease of the log-likelihood by half a unit, effectively corresponding to a 1σ uncertainty. The deviations of the unfold result obtained with these values ($\alpha = 0.71$ and $\alpha = 1.55$), relative to the *nominal* result when using the optimal parameter, define the extent of the associated systematic uncertainty.

Finally, a systematic uncertainty is associated with the choice of $\boldsymbol{\theta}_{\mathrm{prior}}$. The magnitude of this uncertainty is estimated by selecting a different prior and evaluating the change in the unfold result. In particular, the heavy-flavor-hadron yields obtained with PYTHIA were scaled by a modified blast wave calculation, as described in Ref. [33]. Because a feature of Markov chains, such as the one used in this analysis, is that the probability of reaching a given state is independent of the starting point, the sensitivity to the initial choice of prior is expected to be minimal after a sufficient number of iterations.

Figure 16 shows the relative contribution of each source of uncertainty as a function of p_T, to the unfolded fraction of electrons from bottom decays. The most significant contribution comes from the unfold uncertainty, which originates from the statistical uncertainty on the inclusive heavy-flavor spectrum and DCA_T as it is propagated through the unfold procedure. The next most significant contribution comes from the background electron cocktail and its normalization, supplying an approximate 10% uncertainty at low p_T. The total systematic uncertainty is obtained by adding the contributions of every source in quadrature.

V. RESULTS AND DISCUSSION

Figure 17 shows the invariant cross section of charm and bottom hadrons integrated over all rapidity, corresponding to the values that maximize the probability distribution associated with each hadron p_T bin, shown
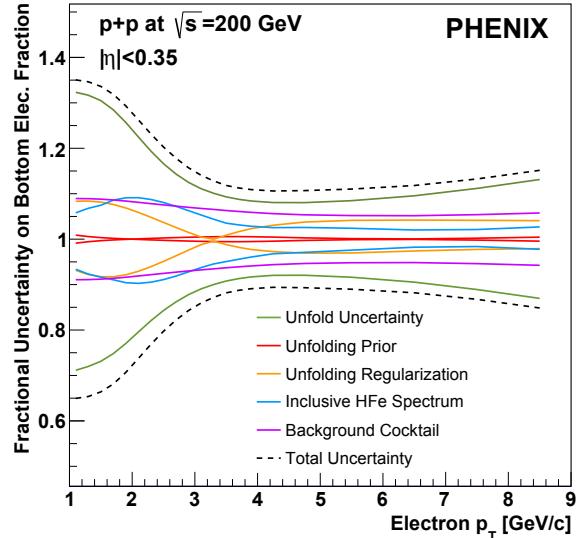
FIG. 16. Fractional uncertainty on the bottom electron fraction, defined as $1\pm$ the relative uncertainty of each source.

along the diagonal of Fig. 13. The uncertainties incorporate both the unfolding uncertainty (which includes the propagation of the total uncertainty in the inclusive heavy-flavor-electron measurements provided as input) as well as the systematic uncertainties discussed in section IV. The uncertainty band is narrowest in the region where electron DCA_T measurements provide constraint to the unfold procedure, namely $1.5 < p_T[\mathrm{GeV}/c] < 6.0$. As presented, the hadron cross section is integrated over rapidity by construction, following directly from the procedure used to populate the decay matrices used in the unfolding procedure. Namely, hadrons simulated in PYTHIA at all rapidities are allowed to decay, recording only the probability of producing an electron within $|\eta| < 0.35$. It thus follows that the cross sections in Fig. 17 depend on the hadron rapidity distribution implemented in the PYTHIA generator. This model dependence implies an associated uncertainty which has not been evaluated since, as previously mentioned, this would be computationally prohibitive. Furthermore, the model dependence is reduced when applying the decay matrix to arrive at results in electron space.

To compare the unfolded differential hadron cross sections to existing measurements, we use the PYTHIA generator to calculate the ratio of open heavy-flavor hadrons of a given species at midrapidity relative to inclusive-hadron production as a function of p_T. In this manner, the unfolded yield of D^0 mesons within $|y| < 1$ can be compared to a measurement by the STAR collaboration [34] obtained by fully reconstructing the hadron decays, as shown in Fig. 18. The unfolded D^0 yield is fit with a modified Hagedorn function, with the ratio of data relative to the fit being shown in the bottom panel. Good agreement with results published by STAR is observed within uncertainties.
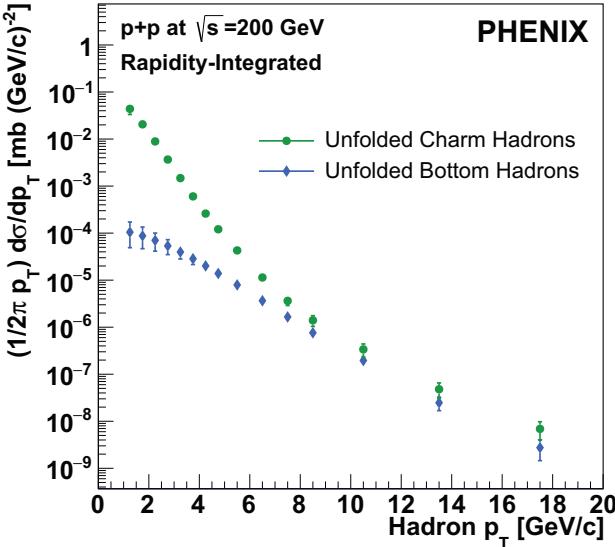
FIG. 17. Unfolded charm and bottom hadron yields in bins of of transverse momentum. The yields are integrated over all rapidities, and the error bars depict the combined statistical and systematic uncertainties.

The model dependence of the unfolded charm and bottom cross sections can be reduced by applying the decay model—that is, multiplying the hadron cross sections by the decay matrices—to obtain the refolded cross section of heavy-flavor-decay electrons in the PHENIX central arm acceptance. The result can be normalized to obtain the fully invariant differential cross sections shown in Fig. 19, where the $b \to e$ curve has been scaled down by a factor of 100 for ease of visualization. Also shown are FONLL[2] pQCD calculations [3], which are in reasonable agreement with both charm and bottom cross sections within uncertainties. The large uncertainties in FONLL are driven by variations in the factorization and renormalization scales, as well as uncertainties in the heavy quark masses and the PDFs used. The central FONLL curves in Fig. 19 correspond to the total cross sections for charm and bottom of $\sigma_c(\text{FONLL}) = 242$ μb and $\sigma_b(\text{FONLL}) = 1.80$ μb. Notice that, unlike the rapidity-

FIG. 18. Unfolded differential cross section of D^0 mesons at midrapidity $|y| < 1$, compared to a corresponding measurement by the STAR experiment [35] obtained by direct reconstruction of the hadron decays.

integrated hadron observables in Figs. 17 and 18, the electron spectra in Fig. 19 are reported at midrapidity by construction, following from the definition of the decay matrix. Like other heavy-flavor measurements at RHIC, the results presented are higher than the FONLL calculation. However, it is notable that the agreement with the central FONLL prediction improves at high p_T, where the effects of the quark mass in the calculation become less significant.

The ratio of electrons from bottom to inclusive heavy-flavor decays, $b \to e/(c \to e + b \to e)$, can be constructed from the electron cross sections, and is shown in Fig. 20. In this measurement, the electrons from the feed-down decay $b \to c \to e$ are considered part of the bottom electron sample. The contribution of bottom decays to the inclusive electron sample is seen to increase sharply with p_T, coming to dominate over that of charm quarks above $p_T \approx 4$ GeV/c. The solid gray line corresponds to the FONLL calculation, with its uncertainty depicted by dashed gray lines. The measured bottom electron frac-
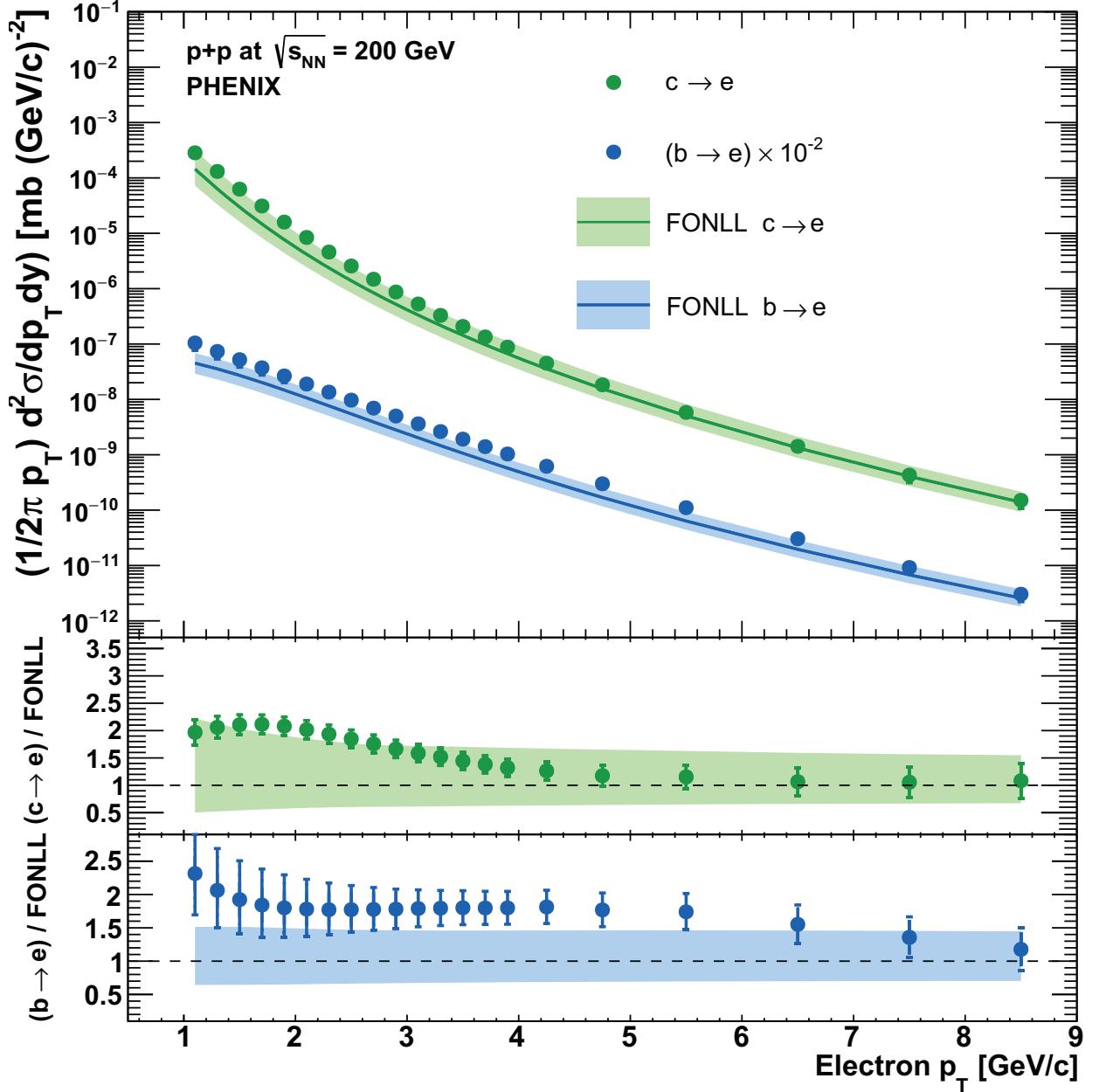
FIG. 19. Refolded spectra of electrons at midrapidity from charm and bottom decays, compared to FONLL calculations [3]. The bottom electron spectrum has been scaled down by a factor of 100 for easier comparison.

tion is observed to be consistent with the FONLL calculation within uncertainties. In particular, good agreement with the central FONLL value is seen below $p_T \approx 3$ GeV/c, with the measured fraction rising slightly above that at higher p_T.

Figure 21 shows a comparison of the unfolded bottom electron fraction with earlier measurements made by the STAR [12] and PHENIX [36] collaborations using electron-hadron and electron-D correlations. It is apparent that the size of the dataset, combined with the unfolding method used in the present analysis provides a result with smaller total uncertainty and significantly extended kinematic reach at low p_T. Furthermore, the unfolded result provides a more direct determination
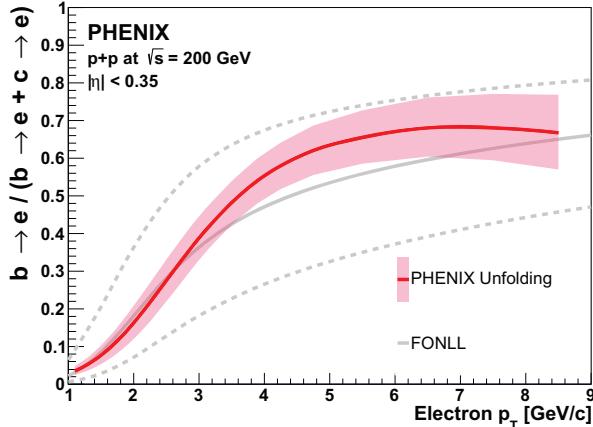
FIG. 20. Fraction of bottom electrons obtained with the un-folding procedure (red), compared to a pQCD FONLL cal-culation (gray) [3], with uncertainties arising from the quark masses and regularization scales.
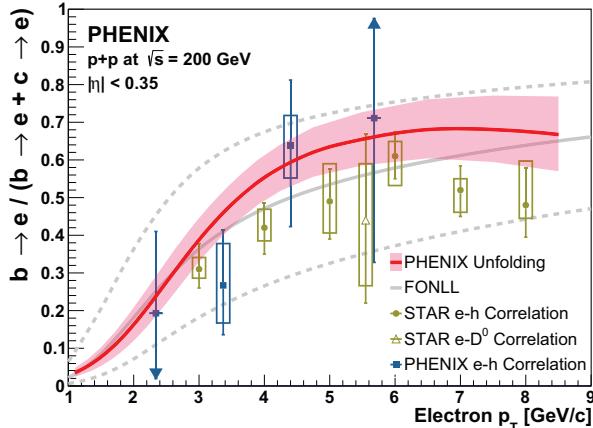
FIG. 21. Fraction of bottom electrons obtained with the un-folding procedure (red), compared to previous measurements by PHENIX [36] and STAR [12] using electron-hadron cor-relations. Also shown are theory comparisons to a pQCD FONLL calculation [3].

of the bottom electron fraction since—unlike the earlier measurements—it does not depend on model-dependent PYTHIA templates of event kinematics to describe the shape of electron-hadron correlations.

The previous PHENIX electron-hadron results, plot-ted with blue markers, are in good agreement with the new unfolded measurement. Similarly, the STAR measurement—while systematically lower—is also con-sistent with the unfolded bottom fraction on account of its large combined statistical and systematic uncertain-ties. The degree of agreement between these two mea-surements was quantified by calculating—under the null hypothesis that the two results are equal—the proba-bility of obtaining a difference more extreme than that

currently observed between the measurements. The re-sulting p-value using a two-sample chi-square statistic is found to be 0.15, indicating that the null hypothesis can-not be rejected. In short, both the unfold and the STAR bottom fraction measurements are consistent given the uncertainties.

VI. SUMMARY

We have reported on a new measurement of the differential-invariant production cross section of separated-heavy-flavor electrons in $p+p$ collisions at $\sqrt{s} = 200$ GeV, at midrapidity $|\eta| < 0.35$ and within $1.0 < p_T^{(e)} < 9.0$ GeV/c. The measurement proceeds via an unfolding analysis where the yield of open-heavy-flavor hadrons is inferred from the inclusive-heavy-flavor electron spectrum, and the electron DCA_T distribution measured with the PHENIX silicon-vertex detector. The individual yields of charm and bottom electrons, as well as the bottom electron fraction, are found to be con-sistent with FONLL calculations. This measurement will provide a precision baseline for future-heavy-flavor-separation analyses. In particular, forthcoming PHENIX results using a high-statistics Au+Au dataset promise to reduce current uncertainties and shed light on the cen-trality dependence of charm and bottom suppression.

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