

# Test Compaction by Test Removal under Transparent-Scan

Irith Pomeranz

**Abstract**—This paper describes a new approach to test compaction under transparent-scan. Transparent-scan achieves higher levels of test compaction than possible with conventional scan-based tests by interleaving scan shift cycles and functional clock cycles in arbitrary ways. Earlier approaches relied on the computation of a single transparent-scan sequence, and the omission of test vectors from it. However, a single transparent-scan sequence can be prohibitively long. In the approach described in this paper, a transparent-scan test set consists of several sequences whose lengths are limited. Test compaction is achieved by combining sequences into longer sequences that detect more faults, and removing from the test set entire sequences that become unnecessary. Experimental results for benchmark circuits demonstrate the ability of the procedure to achieve test compaction without creating prohibitively long transparent-scan sequences.

**Index Terms**—full-scan circuits, test compaction, test generation, transparent-scan.

## I. INTRODUCTION

Test compaction procedures reduce the number of tests that need to be applied for the detection of target faults, thus reducing the test application time and test data volume [1]–[4]. By using multicycle tests it is possible to reduce the number of tests further compared to single-cycle or two-cycle tests [5]–[11]. A multicycle test typically has multiple functional clock cycles between its scan operations. The reduction in the number of tests is achieved because each functional clock cycle can activate and propagate additional faults, resulting in a test that detects more faults. The test application time is reduced because scan operations dominate the test application time, and fewer tests require fewer scan operations.

Another approach to reducing the test application time is transparent-scan [12]. Under transparent-scan, the scan enable and scan chain inputs of a standard-scan circuit are considered as regular primary inputs, and the scan chain outputs are considered as regular primary outputs. As a regular primary input, the scan enable input is allowed to assume arbitrary sequences of values. This allows, e.g., shorter scan operations (shorter runs of scan shift cycles) to be used compared with a conventional scan-based test set. In general it allows to create arbitrary sequences of scan shift and functional clock cycles. This can be used for reducing the number of clock cycles that are required for detecting a given set of faults.

In the procedure described in [12], a conventional scan-based test set is first translated into a transparent-scan sequence. This is achieved by translating every scan shift cycle and every functional clock cycle of the test set into a corresponding clock cycle of the transparent-scan sequence. The transparent-scan sequence is then compacted by omitting clock cycles that are not necessary for the detection of target faults. The omission of clock cycles creates runs of scan shift and functional clock cycles that do not exist in the initial sequence. Test compaction is achieved because the sequence requires fewer clock cycles for test application.

To enhance the ability to omit clock cycles from a transparent-scan sequence, the procedure described in [13] embeds broadside tests in the transparent-scan sequence. This is achieved by replacing pairs of scan shift cycles with pairs of functional clock cycles when these are surrounded by additional scan shift cycles. After the modification,

more clock cycles contribute to the detection of faults, and other clock cycles can be omitted.

The procedure described in [14] achieves test compaction by sharing transparent-scan sequences among different circuits. The original primary inputs and outputs of every circuit are included in a single scan chain together with its state variables. Consequently, every circuit has two inputs. Every circuit also has its own conventional scan-based test set. The procedure translates every test into a two-bit transparent-scan sequence. All the sequences have a similar format but possibly different lengths for different circuits. This allows sharing of test sequences among different circuits.

This paper describes a new approach to test compaction for a single circuit under transparent-scan that makes the following contribution.

Instead of computing a single transparent-scan sequence as in [12] and [13], the procedure described in this paper computes a set of shorter transparent-scan sequences where the length of a sequence is limited. The importance of limiting the length of a transparent-scan sequence results from the fact that this length can be prohibitive. Let us consider a circuit with  $k$  state variables that are included in a single scan chain. Suppose that a conventional single-cycle test set  $C$  for the circuit contains  $m$  tests. The number of clock cycles required for applying the test set  $C$  is  $(m+1)k+m$ . This number is obtained by overlapping the scan-out operation of one test with the scan-in operation of the next test. In this case,  $m$  tests require  $m+1$  scan operations of  $k$  clock cycles, and  $m$  functional clock cycles. If  $C$  is translated into a single transparent-scan sequence  $T$ , the length of  $T$  is also equal to  $(m+1)k+m$ . A test compaction procedure that is applied to  $T$  needs to consider the set of target faults  $F$  under a sequence of this length.

The procedure described in this paper first translates every test  $c_i \in C$  into a transparent-scan sequence  $S_i$ , and includes  $S_i$  in a test set that is denoted by  $S$ . The length of  $S_i$  is equal to  $2k+1$  for a circuit with  $k$  state variables that are included in a single scan chain. If all the transparent-scan sequences in  $S$  are combined, by overlapping the scan-out operation of one test with the scan-in operation of the next test, a single transparent-scan sequence of length  $(m+1)k+m$  will be obtained. However, the procedure limits the number of sequences that it may combine into a single sequence by using a constant that is denoted by  $\mu$ . The number of clock cycles required for applying  $\mu$  conventional scan-based tests is  $(\mu+1)k+\mu$ . This is also the largest length of a transparent-scan sequence that the procedure may create by combining sequences in  $S$ . By keeping  $\mu \ll m$ , the procedure avoids the need to consider all the target faults under the  $(m+1)k+m$  clock cycles of a single transparent-scan sequence.

Another important difference between the test compaction procedure described in this paper and earlier ones is in the approach to test compaction. To achieve test compaction, the procedures from [12] and [13] rely on the omission of clock cycles from a transparent-scan sequence. Instead, the procedure described in this paper removes entire sequences from  $S$ . It is important to note in this regard that, for the discussion in this paper, the conventional scan-based test set  $C$  is already compact. Being compact, no test can be removed from  $C$  without losing fault coverage. The test compaction procedure combines transparent-scan sequences in  $S$  to obtain new transparent-scan sequences of limited lengths, and modifies the sequences to increase the numbers of faults they detect. This allows it to remove other sequences from  $S$ .

In addition, in [13] as well as in works on the compaction of functional test sequences, the omission of clock cycles, and the modification of a sequence, are implemented by separate procedures. This is appropriate since the goal of the modification in earlier works is to enhance the ability to achieve test compaction. In the procedure described in this paper, the goal is to increase the number of faults

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that a combined sequence detects in order to allow other sequences to be removed. The omission of clock cycles can contribute to this goal. Furthermore, it can contribute in ways that cannot be materialized if the two procedures are applied separately. Therefore, the modification of the sequence includes the omission of clock cycles in the procedure described in this paper.

For simplicity of discussion, all the state variables of a circuit are assumed to be included in a single scan chain of length  $k$ , with a scan enable input  $s_{en}$ , and a scan chain input  $s_{in}$ . This affects only the translation of a conventional scan-based test into a transparent-scan sequence. A scan shift cycle has  $s_{en} = 1$ , and a functional clock cycle has  $s_{en} = 0$ .

The conventional scan-based test set  $C$  consists of single-cycle tests for single stuck-at faults. The use of two-cycle or multicycle tests affects only the translation of  $C$  into an initial set  $S$  of transparent-scan sequences. Different fault models can be accommodated by using different fault simulation procedures.

To increase the opportunities for faults to be detected under transparent-scan, original primary outputs and scan chain outputs are observed at every clock cycle of a transparent-scan sequence. Output compaction is appropriate for implementing this option. No other hardware cost is associated with transparent-scan. The computational cost of transparent-scan is related to the need to perform sequential fault simulation for transparent-scan sequences. This cost is reduced (but not eliminated) by limiting the lengths of the transparent-scan sequences as suggested in this paper.

The paper is organized as follows. Section II discusses the transparent-scan test set  $S$  that is obtained from a conventional scan-based test set  $C$ . The test set  $S$  is the initial test set for the test compaction procedure that is described in Section III. Section IV provides experimental results.

## II. INITIAL TEST SET

This section describes the derivation of an initial set of transparent-scan sequences  $S$  from a given conventional single-cycle test set  $C$ .

A conventional single-cycle test  $c_i \in C$  has the form  $c_i = \langle p_i, v_i \rangle$ , where  $p_i$  is a scan-in state, and  $v_i$  is a primary input vector. After  $p_i$  is scanned in, the primary input vector  $v_i$  is applied during a functional clock cycle. The test ends with a scan-out operation.

The test  $c_i = \langle p_i, v_i \rangle$  is translated into a transparent-scan sequence of length  $2k + 1$  that includes  $k$  scan shift cycles for a scan-in operation, a functional clock cycle, and  $k$  scan shift cycles for a scan-out operation. A clock cycle of the sequence is denoted by  $u$ . The sequence assigned to the original primary inputs is denoted by  $V_i$ . The original primary input vector at clock cycle  $u$  is denoted by  $V_i(u)$ . The sequence assigned to the scan enable input  $s_{en}$  is denoted by  $EN_i$ , with  $EN_i(u)$  being the value of  $s_{en}$  at clock cycle  $u$ . The sequence assigned to the scan chain input  $s_{in}$  is denoted by  $IN_i$ , with  $IN_i(u)$  being the value of  $s_{in}$  at clock cycle  $u$ . This notation is illustrated by Table I. For Table I,  $c_i = \langle 00110, 01 \rangle$ .

The transparent-scan sequence corresponding to  $c_i$  is obtained as follows. The scan-in operation is translated into  $k$  scan shift cycles with  $0 \leq u \leq k - 1$ , and  $EN_i(u) = 1$ .  $IN_i(u)$  assumes the corresponding bits of  $p_i$  such that the circuit reaches state  $p_i$  at clock cycle  $k$ . In Table I, with  $p_i = 00110$ ,  $EN_i(u) = 1$  for  $0 \leq u \leq 4$ ,  $IN_i(0) = 0$ ,  $IN_i(1) = 1$ ,  $IN_i(2) = 1$ ,  $IN_i(3) = 0$  and  $IN_i(4) = 0$ .

The functional clock cycle of the test is translated into  $EN_i(u) = 0$  and  $V_i(u) = v_i$  for  $u = k$ . In Table I,  $EN_i(5) = 0$  and  $V_i(5) = 01$ .

The scan-out operation at the end of the test is translated into  $k$  scan shift cycles where  $EN_i(u) = 1$ , for  $k + 1 \leq u \leq 2k$ . In Table I,  $EN_i(u) = 1$  for  $6 \leq u \leq 10$ .

TABLE I  
TRANSPARENT-SCAN SEQUENCE

| $u$ | (a) Initial Translation |           |           | (b) Final Translation |           |           |
|-----|-------------------------|-----------|-----------|-----------------------|-----------|-----------|
|     | $V_i(u)$                | $EN_i(u)$ | $IN_i(u)$ | $V_i(u)$              | $EN_i(u)$ | $IN_i(u)$ |
| 0   | xx                      | 1         | 0         | 01                    | 1         | 0         |
| 1   | xx                      | 1         | 1         | 01                    | 1         | 1         |
| 2   | xx                      | 1         | 1         | 01                    | 1         | 1         |
| 3   | xx                      | 1         | 0         | 01                    | 1         | 0         |
| 4   | xx                      | 1         | 0         | 01                    | 1         | 0         |
| 5   | 01                      | 0         | x         | 01                    | 0         | 0         |
| 6   | xx                      | 1         | x         | xx                    | 1         | x         |
| 7   | xx                      | 1         | x         | xx                    | 1         | x         |
| 8   | xx                      | 1         | x         | xx                    | 1         | x         |
| 9   | xx                      | 1         | x         | xx                    | 1         | x         |
| 10  | xx                      | 1         | x         | xx                    | 1         | x         |

Values that are not specified by  $c_i$  are left unspecified ( $x$ ) in Table I(a). Some of these values are kept unspecified in order to allow overlapping of  $S_i$  with other transparent-scan sequences, while other values are specified in order to increase the ability of the sequence to detect target faults. The unspecified values are discussed next. Table I(b) shows the final sequence that is included in  $S$  based on the sequence from Table I(a).

The unspecified primary input vectors at clock cycles  $0 \leq u < k$  are specified to be equal to  $v_i$ , or  $V_i(u) = v_i$  for  $0 \leq u < k$ .

The unspecified primary input vectors at clock cycles  $k + 1 \leq u \leq 2k$  are left unspecified. If another sequence is overlapped with  $S_i$ , the primary input vectors from this sequence will be used.

The unspecified value on  $IN_i(k)$  is assigned a zero value by default. This value is not important for fault detection since clock cycle  $u = k$  is a functional clock cycle.

Considering the unspecified values of  $IN_i(u)$ , for  $k + 1 \leq u \leq 2k$ , these values are needed for overlapping  $S_i$  with another sequence. Therefore, they are left unspecified.

After the initial set of transparent-scan sequences  $S$  is obtained, fault simulation with fault dropping is carried out for the set of target faults  $F$ . Considering a transparent-scan sequence  $S_i \in S$ , sequential fault simulation is carried out for  $F$  to find the subset of target faults that the sequence detects. This subset is denoted by  $F_i$ .

The tester memory required for transparent-scan is as follows. The original primary inputs are held constant for the duration of a subsequence that corresponds to a single-cycle test in  $C$ , and ends with its functional clock cycle. Therefore, the number of original primary input vectors that need to be stored is not increased relative to  $C$ . The scan enable sequence needs to be stored together with the scan chain input sequence. This doubles the amount of memory for the scan chain input sequence when the circuit has a single scan chain. With  $m \geq 1$  scan chains, the increase because of the scan enable sequence is  $(m + 1)/m \leq 2$ . Test compaction may reduce the number of original primary input vectors, the number of scan enable and scan chain input sequences, and their lengths.

## III. TEST COMPACTION PROCEDURE

This section describes the test compaction procedure. The procedure is illustrated by Figure 1.

### A. Combining Transparent-Scan Sequences

The test compaction procedure combines a pair of transparent-scan sequences,  $S_i \in S$  and  $S_j \in S$ , in order to obtain a longer sequence. With a longer sequence, the procedure has more flexibility to interleave functional clock cycles and scan shift cycles in ways that increase the number of detected faults. Creating longer sequences that detect more faults allows other sequences to be removed from  $S$ . The combination of sequences is performed within the limit of  $(\mu + 1)k + \mu$  on the length of a transparent-scan sequence.

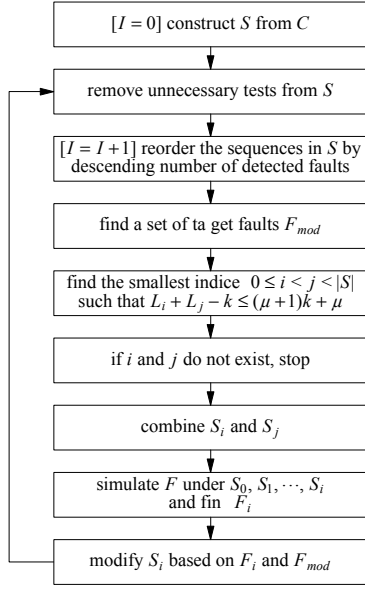


Fig. 1. Test compaction procedure

TABLE II

COMBINATION AND MODIFICATION OF TRANSPARENT-SCAN SEQUENCES

| u  | (a) Combination |           |           | (b) Modification |           |           |               |
|----|-----------------|-----------|-----------|------------------|-----------|-----------|---------------|
|    | $V_i(u)$        | $EN_i(u)$ | $IN_i(u)$ | $V_i(u)$         | $EN_i(u)$ | $IN_i(u)$ | $\Omega_i(u)$ |
| 0  | 01              | 1         | 0         | 11               | 1         | 0         | 0             |
| 1  | 01              | 1         | 1         | 11               | 1         | 0         | 0             |
| 2  | 01              | 1         | 1         | 11               | 1         | 1         | 0             |
| 3  | 01              | 1         | 0         | 11               | 1         | 0         | 0             |
| 4  | 01              | 1         | 0         | 11               | 1         | 1         | 0             |
| 5  | 01              | 0         | 0         | 11               | 0         | 0         | 0             |
| 6  | 10              | 1         | 1         | 00               | 0         | 1         | 0             |
| 7  | 10              | 1         | 1         | 00               | 0         | 1         | 1             |
| 8  | 10              | 1         | 0         | 00               | 1         | 1         | 0             |
| 9  | 10              | 1         | 0         | 00               | 0         | 0         | 0             |
| 10 | 10              | 1         | 1         | 00               | 1         | 0         | 0             |
| 11 | 10              | 0         | 0         | 00               | 0         | 0         | 1             |
| 12 | xx              | 1         | x         | xx               | 1         | x         | 0             |
| 13 | xx              | 1         | x         | xx               | 1         | x         | 0             |
| 14 | xx              | 1         | x         | xx               | 1         | x         | 0             |
| 15 | xx              | 1         | x         | xx               | 1         | x         | 0             |
| 16 | xx              | 1         | x         | xx               | 1         | x         | 0             |

To describe the combination of a pair of transparent-scan sequences, the length of  $S_i$  is denoted by  $L_i$ . The vector at clock cycle  $u$  of  $S_i$  is denoted by  $S_i(u)$ . We have that  $S_i(u) = V_i(u)EN_i(u)IN_i(u)$ .

When a pair of sequences,  $S_i \in S$  and  $S_j \in S$ , is combined, the length of the resulting sequence is  $L_i + L_j - k$  (because of the overlapping of the scan-out operation of  $S_i$  with the scan-in operation of  $S_j$ ). The resulting sequence replaces  $S_i$ . The new  $S_i$  detects all the faults that  $S_i$  and  $S_j$  detect (all the faults in  $F_i$  and  $F_j$ ). This always allows  $S_j$  to be removed from  $S$ . The procedure combines  $S_i \in S$  and  $S_j \in S$  such that  $i < j$  and  $L_i + L_j - k \leq (\mu + 1)k + \mu$ .

Table II(a) shows an example where two transparent-scan sequences  $S_i \in S$  and  $S_j \in S$  are combined into a single sequence that replaces  $S_i$ . The sequences are obtained from the conventional scan-based tests  $c_i = \langle 00110, 01 \rangle$  (whose transparent-scan sequence is shown in Table I), and  $c_j = \langle 10011, 10 \rangle$ . The combined sequence can be further combined with another sequence.

In general, combining  $S_i$  and  $S_j$ , and placing the result in  $S_i$ , is performed as follows.

(1) The first  $k$  clock cycles of  $S_j$  are copied into the last  $k$  clock cycles of  $S_i$ . This overlaps the scan-out operation of  $S_i$  with the scan-

in operation of  $S_j$ . Because of the unspecified values in the last clock cycles of  $S_i$ , none of the values that are important for the application of  $S_i$  is lost. This is implemented by assigning  $S_i(u_i) = S_j(u_j)$  for  $(u_i, u_j) = (L_i - k, 0), (L_i - k + 1, 1), \dots, (L_i - 1, k - 1)$ .

(2) The remaining clock cycles of  $S_j$  are concatenated to  $S_i$ . This is implemented by assigning  $S_i(L_i) = S_j(u_j)$  and  $L_i = L_i + 1$  for  $u_j = k, k + 1, \dots, L_j - 1$ .

Fault simulation with fault dropping of  $F$  under  $S_0, S_1, \dots, S_i$  updates the set of faults that  $S_i$  detects after it is combined with  $S_j$ .

### B. Modifying $S_i$

Let  $S_i$  be obtained by combining  $S_i$  and  $S_j$ . Let  $F_i$  be the subset of faults that  $S_i$  detects after the combination. The test compaction procedure modifies  $S_i$  to increase the number of faults it detects by targeting two subsets of faults. (1) The procedure requires  $S_i$  to continue detecting all the faults in  $F_i$ . (2) The procedure attempts to ensure that  $S_i$  would detect as many additional faults as possible. The faults that the procedure targets are detected by sequences in  $S$  with small numbers of detected faults. Such sequences are likely to be the easiest to remove. The set of target faults is denoted by  $F_{mod}$ . The derivation of  $F_{mod}$  is described later.

The procedure accepts modifications of  $S_i$  where all the faults from  $F_i$  are detected, and the number of detected faults from  $F_{mod}$  does not decrease. Other modifications are not accepted.

A modification of  $S_i$  must also ensure that  $S_i$  can be overlapped with other sequences. For this purpose, it is necessary to maintain the scan-in operation at the beginning of  $S_i$ , the scan-out operation at the end of  $S_i$ , and the unspecified values at the end of  $S_i$ . Every other bit of  $S_i$  can be complemented. This includes the bits of  $V_i(u)$  and  $IN_i(u)$  for  $0 \leq u < L_i - k$ , and  $EN_i(u)$  for  $k \leq u < L_i - k$ .

In addition, a clock cycle of  $S_i$  can be omitted. As discussed earlier, the modification of the sequence and the omission of clock cycles are considered together since both can contribute to an increase in the number of detected faults, and they may interact in ways that cannot be utilized if they are considered separately.

For uniformity, the option of omitting a clock cycle from  $S_i$  is implemented by introducing a sequence that is denoted by  $\Omega_i$ . We have that  $\Omega_i(u) = 0$  if clock cycle  $u$  is retained in  $S_i$ , and  $\Omega_i(u) = 1$  if clock cycle  $u$  is omitted. After the modification of  $S_i$  is complete, clock cycle  $u$  is omitted from  $S_i$  for every  $u$  such that  $\Omega_i(u) = 1$ . Initially,  $\Omega_i(u) = 0$  for  $0 \leq u < L_i$ . The procedure may complement  $\Omega_i(u)$ , for  $k \leq u < L_i - k$ , in order to omit clock cycle  $u$ .

The possibility of complementing  $EN_i(u)$  or  $\Omega_i(u)$ , for  $k \leq u < L_i - k$ , contributes to test compaction that cannot be achieved with conventional scan-based tests. The complementation of these bits allows arbitrary subsequences of scan shift cycles and functional clock cycles to be formed that are only possible under transparent-scan. Complementing some of the other bits ensures that the overall effect of using transparent-scan is as significant as possible.

When the procedure modifies  $V_i(u)$ , it ensures that the number of different original primary input vectors in  $S_i$  does not increase. This is achieved by considering a single original primary input for modification, and complementing it for every clock cycle  $u$  such that  $0 \leq u < L_i - k$ . Denoting the number of original primary inputs by  $n$ , and an original primary input by  $a_p$ , for  $0 \leq p < n$ , the set of bits that the procedure considers for complementation is  $B = \{a_p : 0 \leq p < n\} \cup \{EN_i(u) : k \leq u < L_i - k\} \cup \{IN_i(u) : 0 \leq u < L_i - k\} \cup \{\Omega_i(u) : k \leq u < L_i - k\}$ .

Table II(b) shows a modified transparent-scan sequence that may be obtained from the sequence in Table II(a). The modified sequence is obtained by complementing  $a_0$ ,  $EN_i(u)$  for  $u = 6, 7$  and  $9$ ,  $IN_i(u)$  for  $u = 1, 4, 8$  and  $10$ , and  $\Omega_i(u)$  for  $u = 7$  and  $11$ . Clock cycles  $u = 7$  and  $11$  need to be omitted to obtain the final sequence.

The procedure considers the bits from  $B$  one at a time in a random order. Before this process starts,  $D_{mod,i} = \emptyset$  indicates that  $S_i$  does not detect any faults from  $F_{mod} - F_i$ . When a bit  $b \in B$  is considered, the procedure complements it to obtain from  $S_i$  a sequence that is denoted by  $S_{i,b}$ . The procedure performs fault simulation of  $F_i$  under  $S_{i,b}$  to determine whether all the faults in  $F_i$  are detected. If they are, the procedure simulates  $F_{mod} - F_i$  under  $S_{i,b}$ . Let the subset of detected faults be  $D_{mod,i,b}$ . The procedure accepts the complementation if  $|D_{mod,i,b}| \geq |D_{mod,i}|$ . In this case, it assigns  $S_i = S_{i,b}$ . Otherwise, it discards  $S_{i,b}$ .

#### C. Additional Procedures and Computational Effort

The procedure from Figure 1 removes unnecessary sequences from the initial test set  $S$ , and after it combines a pair of sequences. When a test  $c_i \in C$  is translated into a transparent-scan sequence  $S_i \in S$ , the original primary outputs and scan chain output are observed at every clock cycle of  $S_i$ . As a result,  $S_i$  may detect more faults than  $c_i$ . Considering the initial transparent-scan test set  $S$ , a sequence  $S_i \in S$  may be unnecessary even though  $c_i$  is necessary in  $C$ . In addition, as the test compaction procedure combines and modifies sequences in  $S$  to increase the numbers of faults they detect, other sequences in  $S$  become unnecessary.

To identify sequences that can be removed from  $S$ , the test compaction procedure performs fault simulation followed by forward-looking reverse order fault simulation of  $S$ . A sequence that does not detect any faults is removed from  $S$  by this process.

For the procedure to be as effective as possible, it is advantageous if the sequences is combines,  $S_i$  and  $S_j$ , detect the largest numbers of faults in  $S$ . The test compaction procedure uses fault simulation with fault dropping to reorder  $S$  such that sequences appear by order of descending number of detected faults (third step in Figure 1). For a sequence  $S_i$ , the set of detected faults is denoted by  $F_i$ . If  $|F_i| < |F_j|$  is obtained for  $i < j$ , reordering ensures that  $S_j$  appears in  $S$  before  $S_i$ . After reordering, the procedure repeats the fault simulation process to recompute the sets of detected faults. Reordering and fault simulation with fault dropping are performed until fault simulation with fault dropping yields  $|F_0| \geq |F_1| \geq |F_2| \geq \dots$

In this order, the procedure combines  $S_i$  and  $S_j$ , for the lowest  $i$  and  $j$ , whose combined length does not exceed the limit given by  $\mu$ . By using the lowest possible values of  $i$  and  $j$ , the procedure considers the sequences with the largest sets of detected faults.

The sequences that are the most likely to be removed from  $S$  are the ones at the end of  $S$ , detecting the smallest numbers of faults. The procedure defines the set  $F_{mod}$  of target faults for the modification of  $S_i$  based on these sequences (fourth step in Figure 1) as follows.

The procedure first assigns  $F_{mod} = \emptyset$ . For every sequence  $S_a \in S$  with the smallest  $|F_a|$ , the procedure adds the faults from  $F_a$  to  $F_{mod}$ . It should be noted that, even if fault simulation of  $S_0, S_1, \dots, S_i$  (eighth step in Figure 1) updates  $F_i$  to include faults from  $F_{mod}$ , the procedure still targets the faults in  $F_i$  and  $F_{mod} - F_i$  for the modification of  $S_i$ .

The worst-case computational effort of the test compaction procedure is determined by the modification of combined sequences, as follows. For a conventional scan-based test set  $C$  that contains  $m$  tests, the procedure obtains an initial transparent-scan test set with  $m$  sequences. The procedure combines a pair of sequences in every iteration. Therefore, the number of iterations is  $O(m)$ . This is also the number of combined sequences that the procedure considers.

To modify a combined sequence, the procedure considers  $O(n+k)$  bits in the set  $B$ . For every bit it simulates at most  $|F_i \cup F_{mod}|$  faults, or  $O(|F|)$  faults. With a constant for  $\mu$ , the length of a sequence is  $O(k)$ . Overall, the computational effort of the procedure

is determined by the need to perform fault simulation for  $O(m(n+k)|F|)$  faults and clock cycles.

#### IV. EXPERIMENTAL RESULTS

The test compaction procedure from Figure 1 is applied to single stuck-at faults in benchmark circuits using a compact scan-based test set for  $C$ . The procedure is also applied to sequence detectors for the all-one sequence of length 64, 128, 256 and 512 to illustrate its performance for a functional unit as its size is increased.

The procedure is applied with  $\mu = 4$  to limit the length of a transparent-scan sequence. Since the omission of clock cycles may reduce the length of a sequence, it is possible for the procedure to combine more than four sequences without exceeding this limit every time  $k + 1$  or more clock cycles are omitted.

The level of test compaction is measured by the number of clock cycles that are required for applying  $S$ . This number is computed as  $cyc = k + \sum \{L_i - k : S_i \in S\}$ , taking into consideration that scan-out and scan-in operations will be overlapped for consecutive tests. For ease of references,  $cyc_I$  is the number of clock cycles required for applying the test set obtained in iteration  $I$ . The initial test set corresponds to iteration  $I = 0$ , with  $cyc_0$  clock cycles.

The results are shown in Table III as follows. The first row for every circuit describes the initial transparent-scan test set  $S$ . Additional rows describe the test set  $S$  when the number of clock cycles,  $cyc_I$ , is reduced to approximately  $0.9cyc_0, 0.8cyc_0, \dots$ . The last row describes the final test set.

After the circuit name, column *sv* shows the number of state variables,  $k$ . Column *iter* shows the iteration of the test compaction procedure. Column  $F_{mod}$  shows the fraction of faults in  $F_{mod}$  for the iteration,  $|F_{mod}|/|F|$ .

Column *seq* shows the number of transparent-scan sequences in  $S$ . Column *max* shows the maximum length of a transparent-scan sequence. Column *cycles* shows the total number of clock cycles  $cyc_I$  required for applying all the sequences in  $S$ . Column *ratio* shows the ratio  $cyc_I/cyc_0$ .

Column *f.c.* shows the fault coverage of  $S$ . The test compaction procedure ensures that the fault coverage does not decrease. Column *ntime* shows the normalized run time, where the cumulative run time of the test compaction procedure is divided by the run time for obtaining the initial transparent-scan test set  $S$  from  $C$ . This includes only fault simulation with fault dropping and forward-looking reverse order fault simulation of  $S$ .

The following points can be seen from Table III. There are many circuits where the test compaction procedure reduces the number of clock cycles required for applying the transparent-scan test set significantly compared with the initial test set, and compared with a compact conventional scan-based test set.

For some circuits, the first significant reduction in the number of clock cycles is achieved after a small number of iterations. This implies that sequences, other than the ones combined, can be removed from the test set after a small number of iterations. For other circuits, it takes several iterations before other sequences can be removed.

The normalized run time is similar for benchmark circuits of different sizes. This indicates that the procedure scales similar to a fault simulation procedure for transparent-scan sequences of minimal length, as in the initial test set. In a large design, fault simulation is expected to be applicable to logic blocks within the design. To further demonstrate the scalability of the procedure, Figure 2 shows the normalized run time as a function of the number of state variables when the number of clock cycles is reduced to approximately  $0.9cyc_0$ . Figure 2 demonstrates that the normalized run time does not increase with the number of state variables, which is used for measuring the circuit size. The sequence detectors further demonstrate the scalability

TABLE III  
EXPERIMENTAL RESULTS

| circuit        | sv  | iter | Fmod    | seq | max  | cycles | ratio | f.c.    | ntime  |
|----------------|-----|------|---------|-----|------|--------|-------|---------|--------|
| s1423          | 74  | 0    | -       | 26  | 149  | 2024   | 1.000 | 99.076  | 1.00   |
| s1423          | 74  | 13   | 0.00198 | 10  | 371  | 1762   | 0.871 | 99.076  | 28.09  |
| s1423          | 74  | 16   | 0.00132 | 6   | 371  | 1665   | 0.823 | 99.076  | 30.67  |
| s5378          | 179 | 0    | -       | 100 | 359  | 18179  | 1.000 | 99.131  | 1.00   |
| s5378          | 179 | 14   | 0.00326 | 76  | 899  | 16191  | 0.891 | 99.131  | 35.16  |
| s5378          | 179 | 29   | 0.00348 | 55  | 899  | 14330  | 0.788 | 99.131  | 52.04  |
| s5378          | 179 | 43   | 0.00304 | 37  | 899  | 12634  | 0.695 | 99.131  | 65.15  |
| s5378          | 179 | 61   | 0.00043 | 18  | 899  | 10993  | 0.605 | 99.131  | 78.53  |
| s9234          | 228 | 0    | -       | 111 | 457  | 25647  | 1.000 | 93.475  | 1.00   |
| s9234          | 228 | 80   | 0.00029 | 27  | 1136 | 23352  | 0.911 | 93.475  | 98.31  |
| s13207         | 669 | 0    | -       | 183 | 1339 | 123279 | 1.000 | 98.462  | 1.00   |
| s13207         | 669 | 4    | 0.00540 | 153 | 3344 | 105854 | 0.859 | 98.462  | 20.36  |
| s13207         | 669 | 5    | 0.00448 | 138 | 3344 | 96474  | 0.783 | 98.462  | 22.44  |
| s13207         | 669 | 8    | 0.00224 | 108 | 3346 | 78373  | 0.636 | 98.462  | 27.92  |
| s13207         | 669 | 10   | 0.00153 | 98  | 3346 | 73011  | 0.592 | 98.462  | 30.55  |
| s13207         | 669 | 15   | 0.00071 | 74  | 3346 | 60187  | 0.488 | 98.462  | 35.08  |
| b04            | 66  | 0    | -       | 42  | 133  | 2880   | 1.000 | 99.851  | 1.00   |
| b04            | 66  | 7    | 0.00966 | 29  | 331  | 2464   | 0.856 | 99.851  | 21.20  |
| b04            | 66  | 12   | 0.00817 | 21  | 331  | 2201   | 0.764 | 99.851  | 28.20  |
| b04            | 66  | 18   | 0.00669 | 13  | 331  | 1990   | 0.691 | 99.851  | 33.51  |
| b04            | 66  | 22   | 0.00149 | 8   | 331  | 1803   | 0.626 | 99.851  | 36.12  |
| b14            | 247 | 0    | -       | 327 | 495  | 81343  | 1.000 | 94.870  | 1.00   |
| b14            | 247 | 33   | 0.01262 | 261 | 1234 | 72983  | 0.897 | 94.870  | 59.20  |
| b14            | 247 | 71   | 0.01272 | 202 | 1234 | 67276  | 0.827 | 94.870  | 103.31 |
| des_area       | 128 | 0    | -       | 115 | 257  | 14963  | 1.000 | 100.000 | 1.00   |
| des_area       | 128 | 13   | 0.00101 | 95  | 639  | 13386  | 0.895 | 100.000 | 34.79  |
| des_area       | 128 | 24   | 0.00101 | 82  | 639  | 11936  | 0.798 | 100.000 | 48.33  |
| des_area       | 128 | 35   | 0.00101 | 70  | 639  | 10441  | 0.698 | 100.000 | 60.23  |
| des_area       | 128 | 45   | 0.00101 | 57  | 639  | 8969   | 0.599 | 100.000 | 73.01  |
| des_area       | 128 | 54   | 0.00081 | 45  | 639  | 7430   | 0.497 | 100.000 | 79.34  |
| des_area       | 128 | 66   | 0.00101 | 33  | 639  | 5958   | 0.398 | 100.000 | 89.25  |
| des_area       | 128 | 78   | 0.00101 | 21  | 639  | 4468   | 0.299 | 100.000 | 99.30  |
| des_area       | 128 | 89   | 0.00040 | 9   | 639  | 2915   | 0.195 | 100.000 | 108.07 |
| des_area       | 128 | 92   | 0.00010 | 6   | 639  | 2574   | 0.172 | 100.000 | 111.01 |
| i2c            | 128 | 0    | -       | 45  | 257  | 5933   | 1.000 | 100.000 | 1.00   |
| i2c            | 128 | 21   | 0.00214 | 20  | 641  | 5309   | 0.895 | 100.000 | 53.79  |
| i2c            | 128 | 30   | 0.00043 | 10  | 641  | 4956   | 0.835 | 100.000 | 63.53  |
| pci_spoci_ctrl | 60  | 0    | -       | 146 | 121  | 8966   | 1.000 | 99.942  | 1.00   |
| pci_spoci_ctrl | 60  | 84   | 0.01514 | 52  | 299  | 8003   | 0.893 | 99.942  | 94.40  |
| pci_spoci_ctrl | 60  | 102  | 0.00058 | 34  | 299  | 7908   | 0.882 | 99.942  | 108.32 |
| sasc           | 117 | 0    | -       | 22  | 235  | 2713   | 1.000 | 100.000 | 1.00   |
| sasc           | 117 | 6    | 0.00059 | 14  | 578  | 2439   | 0.899 | 100.000 | 47.22  |
| sasc           | 117 | 9    | 0.00356 | 8   | 578  | 2036   | 0.750 | 100.000 | 54.67  |
| sasc           | 117 | 10   | 0.00237 | 6   | 578  | 1892   | 0.697 | 100.000 | 55.68  |
| sasc           | 117 | 11   | 0.00119 | 4   | 578  | 1677   | 0.618 | 100.000 | 56.52  |
| simple_spi     | 131 | 0    | -       | 36  | 263  | 4883   | 1.000 | 100.000 | 1.00   |
| simple_spi     | 131 | 11   | 0.00095 | 22  | 650  | 4333   | 0.887 | 100.000 | 45.69  |
| simple_spi     | 131 | 18   | 0.00143 | 15  | 650  | 3876   | 0.794 | 100.000 | 54.06  |
| simple_spi     | 131 | 24   | 0.00095 | 8   | 650  | 3383   | 0.693 | 100.000 | 59.13  |
| spi            | 229 | 0    | -       | 394 | 459  | 90849  | 1.000 | 99.985  | 1.00   |
| spi            | 229 | 34   | 0.01185 | 321 | 1147 | 81708  | 0.899 | 99.985  | 55.24  |
| spi            | 229 | 51   | 0.00985 | 265 | 1147 | 72631  | 0.799 | 99.985  | 69.61  |
| spi            | 229 | 74   | 0.00785 | 198 | 1147 | 62342  | 0.686 | 99.985  | 85.01  |
| spi            | 229 | 93   | 0.00446 | 140 | 1147 | 53181  | 0.585 | 99.985  | 94.23  |
| systemcdes     | 190 | 0    | -       | 78  | 381  | 15088  | 1.000 | 100.000 | 1.00   |
| systemcdes     | 190 | 3    | 0.00030 | 65  | 928  | 13152  | 0.872 | 100.000 | 20.81  |
| systemcdes     | 190 | 4    | 0.00045 | 58  | 928  | 11989  | 0.795 | 100.000 | 21.97  |
| systemcdes     | 190 | 5    | 0.00106 | 48  | 928  | 10246  | 0.679 | 100.000 | 23.42  |
| systemcdes     | 190 | 6    | 0.00030 | 38  | 928  | 8482   | 0.562 | 100.000 | 25.48  |
| systemcdes     | 190 | 7    | 0.00151 | 31  | 928  | 7332   | 0.486 | 100.000 | 26.00  |
| systemcdes     | 190 | 9    | 0.00061 | 20  | 928  | 5570   | 0.369 | 100.000 | 27.13  |
| systemcdes     | 190 | 11   | 0.00061 | 12  | 928  | 4358   | 0.289 | 100.000 | 27.90  |
| systemcdes     | 190 | 13   | 0.00015 | 5   | 928  | 3184   | 0.211 | 100.000 | 28.35  |
| usb_phy        | 98  | 0    | -       | 32  | 197  | 3266   | 1.000 | 100.000 | 1.00   |
| usb_phy        | 98  | 10   | 0.00538 | 19  | 481  | 2889   | 0.885 | 100.000 | 38.13  |
| usb_phy        | 98  | 12   | 0.00385 | 14  | 481  | 2584   | 0.791 | 100.000 | 41.91  |
| usb_phy        | 98  | 16   | 0.00308 | 8   | 481  | 2222   | 0.680 | 100.000 | 46.81  |
| usb_phy        | 98  | 18   | 0.00077 | 6   | 481  | 2144   | 0.656 | 100.000 | 48.21  |
| all1sd.64      | 63  | 0    | -       | 65  | 127  | 4223   | 1.000 | 100.000 | 1.00   |
| all1sd.64      | 63  | 1    | 0.00262 | 1   | 191  | 191    | 0.045 | 100.000 | 1.80   |
| all1sd.128     | 127 | 0    | -       | 129 | 255  | 16639  | 1.000 | 100.000 | 1.00   |
| all1sd.128     | 127 | 1    | 0.00131 | 1   | 383  | 383    | 0.023 | 100.000 | 1.70   |
| all1sd.256     | 255 | 0    | -       | 257 | 511  | 66047  | 1.000 | 100.000 | 1.00   |
| all1sd.256     | 255 | 1    | 0.00065 | 1   | 767  | 767    | 0.012 | 100.000 | 1.70   |
| all1sd.512     | 511 | 0    | -       | 513 | 1023 | 263167 | 1.000 | 100.000 | 1.00   |
| all1sd.512     | 511 | 1    | 0.00033 | 1   | 1535 | 1535   | 0.006 | 100.000 | 1.76   |

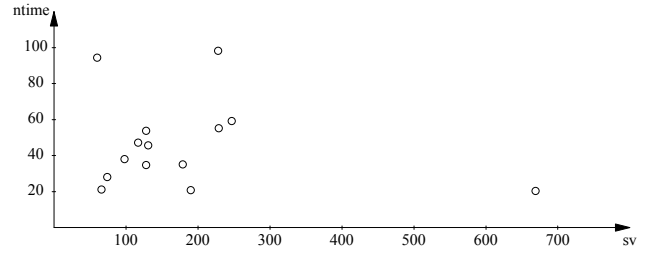


Fig. 2. Scalability

## V. CONCLUDING REMARKS

This paper described a new approach to test compaction under transparent-scan. In this approach, a transparent-scan test set consists of several transparent-scan sequences whose lengths are limited. As sequences are combined into longer sequences that detect more faults, without exceeding the length limit, test compaction is achieved by removing entire sequences from the test set, and to a lesser extent, omitting clock cycles from the combined sequences. Experimental results for benchmark circuits demonstrated the ability of the procedure to achieve test compaction without creating prohibitively long transparent-scan sequences.

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of the procedure. For these circuits also, the normalized run time does not increase as the circuit size is increased.