

# The $\text{ArNH}_2^+$ Noble Gas Molecule: Stability, Vibrational Frequencies, and Spectroscopic Constants

Ryan C. Fortenberry\*

*Department of Chemistry & Biochemistry, University of Mississippi, University, MS 38655-1848, U.S.A.*

---

## Abstract

The detection of  $\text{ArH}^+$  in the Crab nebula has led to speculation of other noble gas-containing molecules existing beyond the laboratory. Here, the previously unreported  $\text{ArNH}_2^+$  molecule is shown through high-level coupled cluster theory quartic force field computations to possess a notable Ar–N bond strength (36.8 kcal/mol), a sizable dipole moment (2.78 D), near-prolate rotational character, and fairly bright vibrational transitions at  $3256.0\text{ cm}^{-1}$  and  $475.7\text{ cm}^{-1}$  on opposite ends of the infrared scale. Three of the other vibrational frequencies have observable intensities, and all of these data are provided for the three main isotopes of argon:  $^{36}\text{ArNH}_2^+$ ,  $^{38}\text{ArNH}_2^+$ , and  $^{40}\text{ArNH}_2^+$ . These spectroscopic data should be useful in assisting any potential observations of the molecule whether in astrophysical or laboratory environments even if in the latter  $\text{ArNH}_2^+$  could be a contaminant in argon matrix spectroscopic studies.

*Keywords:* Noble gas chemistry; rovibrational spectroscopy; quantum chemistry; quartic force fields; astrochemistry

---

## 1. Introduction

Thus far, the only noble gas molecule known in nature is the argonium cation ( $\text{ArH}^+$ ) [1–3], but the inventory of potential noble gas molecules is growing, especially due in large part to structural and spectroscopic data generated by highly-accurate quantum chemical computations. Most notably, the predicted existence and spectral features of the  $\text{ArOH}^+$  cation [4–6] preceded the laboratory detection of this simple noble gas hydroxide [7]. Interstellar conditions are likely best for observation of noble gas molecules outside of the laboratory, and argon is one of the group-of-eleven most abundant atoms in the observable Universe [8, 9]. Hence, molecules containing this noble gas atom may yet be observable if only their spectroscopic data be determined.

Argon atoms bonded in proton-bound complexes [10], to ethynyl or cyano groups [11, 12], hydrogen clusters [13–18], water [19, 20], and even  $\text{CH}_2$  [21, 22] have been documented and largely rovibrationally characterized by various groups including our own. Most notably, the experimental rotational constants [23] for  $^{40}\text{ArH}_3^+$  compare with our

---

\*Corresponding author

Email address: [r410@olemiss.edu](mailto:r410@olemiss.edu) (Ryan C. Fortenberry)

Preprint submitted to Elsevier

January 23, 2019

theoretical values to within 60 MHz for the  $B$  and  $C$  constants and  $D_J$  values within 6.0 kHz [17]. In general, rotational constants for strongly bound systems agree between our standard approach and gas phase experiment to within 30 MHz and vibrational frequencies within  $5.0\text{ cm}^{-1}$  and sometimes to within  $1.0\text{ cm}^{-1}$  [24–36]. Hence, further analysis of more strongly-bound argon-containing cations should provide more accurate rotational constants and vibrational frequencies for laboratory or even astrophysical detection.

The commonality of carbon and its strong bonding characteristics has naturally led to more studies on molecules containing Ar–C bonds. However, Ar–O and even Ar–N bonds have been shown previously to possess relatively high bond strengths. Most notably, the Ar–O bond in  $\text{ArOH}^+$  has been computed to be 73.70 kcal/mol in its ground doublet state and 16.35 kcal/mol in its excited triplet state [5].  $\text{ArNH}^+$  is also known to be well-bound and has been characterized theoretically [37]. However,  $\text{NH}^+$  has conspicuously not been observed in the interstellar medium (ISM) [38] implying that  $\text{ArNH}^+$  may not be a common interstellar species for reasons agnostic to a noble gas atom’s willingness to bond. Hence, a step beyond to  $\text{ArNH}_2^+$  may provide a more likely interstellar, noble gas molecular cation. Both  $\text{NH}$  [39] and  $\text{NH}_2$  [40] are known in the ISM, and several molecules of the R– $\text{NH}_2$  format are known [41] including the simplest (and one of the first known interstellar species) ammonia [42], methylamine [43], and amino acetonitrile [44]. Hence, bonding an argon to the amino cation is possible in the ISM. Additionally, such bonding is also possible in argon matrix, condensed phase experiments where  $\text{ArNH}_2^+$  may be a contaminant in any spectrum of  $\text{NH}_2$  derivatives. This work will explore the rotational and vibrational properties of this molecule in order to aid in growing the number of physically observed noble gas molecules.

## 2. Computational Details

The spectroscopic constants and vibrational frequencies are computed via a fourth-order Taylor series expansion of the potential portion of the internuclear Hamiltonian or, more commonly, a quartic force field (QFF). This energy is determined here through a composite scheme [45, 46, 24, 25] but all computations rely on coupled cluster theory at the singles, doubles, and perturbative triples [CCSD(T)] level [47, 48], the MOLPRO2015.1 program [49, 50], and all correlation consistent basis sets include the extra tight  $d$  functions for the argon atom. The reference geometry is based on CCSD(T)/aug-cc-pV5Z [51, 52] optimized parameters with correction for the Martin-Taylor (MT) core correlating basis set [53] coming from differences in those optimized geometries including and excluding the core electrons. From this reference geometry, displacements of  $0.005\text{ Å}$ , and  $0.005$  radians are made based on the below coordinates utilized in previous studies

of non-planar, tetraatomic,  $C_s$  molecules [54, 22]:

$$S_1(a') = r(\text{Ar} - \text{N}) \quad (1)$$

$$S_2(a') = \frac{1}{\sqrt{2}}[r(\text{H}_1 - \text{N}) + r(\text{H}_2 - \text{N})] \quad (2)$$

$$S_3(a') = \frac{1}{\sqrt{2}}[\angle(\text{H}_1 - \text{N} - \text{Ar}) + \angle(\text{H}_2 - \text{N} - \text{Ar})] \quad (3)$$

$$S_4(a') = \angle(\text{H}_1 - \text{N} - \text{H}_2) \quad (4)$$

$$S_5(a'') = \frac{1}{\sqrt{2}}[r(\text{H}_1 - \text{N}) - r(\text{H}_2 - \text{N})] \quad (5)$$

$$S_6(a'') = \frac{1}{\sqrt{2}}[\angle(\text{H}_1 - \text{N} - \text{Ar}) - \angle(\text{H}_2 - \text{N} - \text{Ar})]. \quad (6)$$

At each of the 665 total points, CCSD(T)/aug-cc-pVTZ, aug-cc-pVQZ, and aug-cc-pV5Z energies are computed and extrapolated to the complete basis set (CBS) limit via a three-point formula [55]. Then, corrections for the CCSD(T)/MT with core and CCSD(T)/MT without core energies are added to this. Furthermore, CCSD(T)/cc-pVTZ-DK scalar relativistic [56] corrections are added from computations with such relativity turned on and turned off. This creates the so-called CcCR QFF [25] so named for CBS (“C”), core correlation (“cC”), and relativity (“R”).

The points are then fit via a least-squares procedure with a sum of squared residuals of  $2.5 \times 10^{-18}$  a.u.<sup>2</sup>. Refitting zeroes the gradients and produces the CcCR equilibrium geometry and final force constants that define the QFF. The INTDER program [57] transforms the symmetry-internal coordinates into Cartesian coordinates for more flexibility in the rotational [58] and vibrational [59, 60] second-order perturbation theory (VPT2) computations within the SPECTRO program [61]. Only a  $\nu_5/\nu_4$   $C$ -type Coriolis resonance is present in this molecule.

The  $^{36}\text{Ar}$ ,  $^{38}\text{Ar}$ , and  $^{40}\text{Ar}$  isotopes are included in this study since the last is most common on Earth while the other two are much more abundant in the ISM than their heavier brother. The CCSD(T)/aug-cc-pV5Z dipole moment is computed with the origin at the center-of-mass, and the double-harmonic vibrational intensities are computed with second-order Møller-Plesset perturbation theory (MP2) with the 6-31+G( $d$ ) basis set in the Gaussian09 program [62–64] which has been shown to produce good agreement with more advanced theory for semi-quantitative interpretations of the vibrational intensities [65, 66].

### 3. Results and Discussion

First,  $\text{ArNH}_2^+$  is a stable system. The CCSD(T)/aug-cc-pV5Z Ar–N dissociation energy is 36.8 kcal/mol. Additionally, the  $F_{11}$  force constant for the harmonic frequency of the Ar–N stretch in Table 1 is 1.869 mdyne/Å<sup>2</sup>. The numbering of the force constants comes from the numbering of the displacements given in the previous section. The  $F_{11}$  value is nearly exactly the same as the 1.865 mdyne/Å<sup>2</sup>  $F_{11}$  value in  $\text{ArNH}^+$  [37]. Hence, the two species will have similar behavior in the heavy-atom stretch and will have notable bonding. This is carried out in the vibrational frequencies given in Table 2. The anharmonic  $\nu_6$  Ar–N stretch in  $^{40}\text{ArNH}_2^+$  is 475.7 cm<sup>−1</sup> which is less than the

Table 1: The  $\text{ArNH}_2^+$  CcCR Simple-Internal Force Constants (in  $\text{mdyn}/\text{\AA}^n \cdot \text{rad}^m$ ).

F <sub>66</sub>	0.833612	F <sub>662</sub>	-0.0945	F <sub>6665</sub>	-0.29	F <sub>6532</sub>	-0.45	F <sub>3331</sub>	2.48
F <sub>65</sub>	-0.073616	F <sub>652</sub>	0.1008	F <sub>6655</sub>	-0.51	F <sub>5532</sub>	-0.04	F <sub>6621</sub>	0.42
F <sub>55</sub>	6.408817	F <sub>552</sub>	-28.7448	F <sub>6555</sub>	-0.06	F <sub>4432</sub>	0.18	F <sub>6521</sub>	-0.32
F <sub>44</sub>	0.633115	F <sub>442</sub>	-0.3744	F <sub>5555</sub>	116.21	F <sub>4332</sub>	0.13	F <sub>5521</sub>	-0.27
F <sub>43</sub>	-0.017270	F <sub>432</sub>	0.1158	F <sub>6644</sub>	0.61	F <sub>3332</sub>	0.02	F <sub>4421</sub>	0.00
F <sub>33</sub>	0.966241	F <sub>332</sub>	0.0671	F <sub>6544</sub>	0.03	F <sub>6622</sub>	-0.54	F <sub>4321</sub>	-0.18
F <sub>42</sub>	0.296459	F <sub>422</sub>	-0.4570	F <sub>5544</sub>	-0.89	F <sub>6522</sub>	-0.15	F <sub>3321</sub>	-0.14
F <sub>32</sub>	0.032223	F <sub>322</sub>	0.0255	F <sub>4444</sub>	-0.71	F <sub>5522</sub>	115.20	F <sub>4221</sub>	-0.16
F <sub>22</sub>	6.291929	F <sub>222</sub>	-28.8205	F <sub>6643</sub>	0.08	F <sub>4422</sub>	0.35	F <sub>3221</sub>	-0.37
F <sub>41</sub>	0.037066	F <sub>661</sub>	-1.5360	F <sub>6543</sub>	0.06	F <sub>4322</sub>	0.08	F <sub>2221</sub>	-0.16
F <sub>31</sub>	0.525248	F <sub>651</sub>	-0.0992	F <sub>5543</sub>	0.05	F <sub>3322</sub>	-0.53	F <sub>6611</sub>	1.56
F <sub>21</sub>	-0.196890	F <sub>551</sub>	0.3343	F <sub>4443</sub>	-0.05	F <sub>4222</sub>	-0.12	F <sub>6511</sub>	1.27
F <sub>11</sub>	1.869259	F <sub>441</sub>	0.0657	F <sub>6633</sub>	0.32	F <sub>3222</sub>	-0.18	F <sub>5511</sub>	-0.98
F <sub>664</sub>	-0.3429	F <sub>431</sub>	0.3219	F <sub>6533</sub>	-0.17	F <sub>2222</sub>	114.54	F <sub>4411</sub>	-0.10
F <sub>654</sub>	-0.0314	F <sub>331</sub>	-1.1118	F <sub>5533</sub>	-0.51	F <sub>6641</sub>	0.29	F <sub>4311</sub>	-0.43
F <sub>554</sub>	0.2516	F <sub>421</sub>	0.0093	F <sub>4433</sub>	0.61	F <sub>6541</sub>	0.06	F <sub>3311</sub>	0.06
F <sub>444</sub>	-0.7069	F <sub>321</sub>	-0.2555	F <sub>4333</sub>	0.36	F <sub>5541</sub>	-0.06	F <sub>4211</sub>	-0.38
F <sub>663</sub>	-0.6863	F <sub>221</sub>	0.2318	F <sub>3333</sub>	2.94	F <sub>4441</sub>	-0.05	F <sub>3211</sub>	0.87
F <sub>653</sub>	-0.0722	F <sub>411</sub>	-0.0864	F <sub>6642</sub>	0.15	F <sub>6631</sub>	1.51	F <sub>2211</sub>	-0.32
F <sub>553</sub>	0.0184	F <sub>311</sub>	-2.2473	F <sub>6542</sub>	0.05	F <sub>6531</sub>	0.35	F <sub>4111</sub>	-0.32
F <sub>443</sub>	-0.0020	F <sub>211</sub>	0.0721	F <sub>5542</sub>	-0.81	F <sub>5531</sub>	-0.21	F <sub>3111</sub>	4.99
F <sub>433</sub>	0.5642	F <sub>111</sub>	-9.9053	F <sub>4442</sub>	0.82	F <sub>4431</sub>	0.34	F <sub>2111</sub>	1.82
F <sub>333</sub>	-0.4233	F <sub>6666</sub>	1.52	F <sub>6632</sub>	-0.20	F <sub>4331</sub>	0.51	F <sub>1111</sub>	41.97

same frequency in  $^{40}\text{ArNH}^+$  at  $516.4 \text{ cm}^{-1}$ . However, they are of the same magnitude, and the additional mass of the hydrogen atom is likely responsible for the decrease in the vibrational frequency. Regardless, the dissociation energy is  $12870.1 \text{ cm}^{-1}$  indicating that the molecular system cannot undergo vibrational predissociation upon single-mode vibrational excitation from the amino cation moiety. The barrier to inversion through the  $C_{2v}$  saddle point is computed here via CCSD(T)/aug-cc-pVTZ to be  $6271 \text{ cm}^{-1}$  providing a deep enough well for the present VPT2 computations to be reliable and the structure to be  $C_s$ . With respect to the  $\nu_4$  mode, several quanta of excitation would be required to overcome the barrier.

Furthermore, the two N–H stretching vibrational frequencies are notably perturbed by the presence of the argon atom. The  $\nu_1$  symmetric stretch at  $3256.0 \text{ cm}^{-1}$  is  $45 \text{ cm}^{-1}$  lower than the  $3301 \text{ cm}^{-1}$  frequency in lone  $\text{NH}_2$ , and the  $\nu_2$  antisymmetric stretch at  $3168.1 \text{ cm}^{-1}$  is  $49 \text{ cm}^{-1}$  less than the  $3219 \text{ cm}^{-1}$   $\text{NH}_2$  fundamental [67]. Certainly, the mass of the argon atom plays a role in these reductions, but the atom must be bonded for it to have such an effect.

The rest of the fundamental vibrational frequencies are also given in Table 2. These fall in the  $1460 \text{ cm}^{-1}$  to  $1130 \text{ cm}^{-1}$  range in the mid-infrared. The  $\nu_4$  argon atom out-of-plane bend (OPB) can also be characterized as the symmetric, but out-of-plane deformation of the concerted hydrogen atoms. Hence, the  $\nu_5$  antisymmetric hydrogen bend (or, equivalently,  $\text{NH}_2$  twist) is a mere  $62.2 \text{ cm}^{-1}$  less at  $1136.2 \text{ cm}^{-1}$  since both motions involve the hydrogen atoms bending about the nitrogen atom.

All but one of the vibrational frequencies have notable intensities with the bookending

$\nu_6$  Ar–N stretch and the  $\nu_1$  symmetric N–H stretches being the brightest by basically the same amount at  $\sim 100$  km/mol. The antisymmetric hydrogen bend is practically vibrationally dark, but the other three fundamental modes have intensities on the order of the antisymmetric stretch in water.

Additionally, this molecule will have an observable rotational spectrum. Its dipole moment is quite large at 2.78 D indicating that the observed rotational lines will be marked. Even with the deformation of the hydrogen atoms out of plane due to the lone pair on the nitrogen, this molecule is near-prolate due to the large mass of the argon atom. The  $^{40}\text{ArNH}^+$   $B_0$  rotational constant is 12151.9 MHz, and  $C_0$  is 11924.5 MHz, a difference of less than 2.0 %. However, the  $A_0$  constant is over  $20\times$  larger giving classic near-prolate rotational spectroscopic structure. Additionally, the  $B$  and  $C$  constants for the different isotopologues are given in Table 2 in order to aid in radioastronomical or microwave laboratory experimental searches for this molecule. The vibrationally-excited rotational constants are also provided with the numbering now indicative of the fundamental vibrational frequencies given at the bottom of Table 2.

#### 4. Conclusions

The  $\text{ArNH}_2^+$  noble gas, molecular cation has a stable Ar–N bond born out through both computations of the dissociation energy and treatment of this vibrational motion. This molecule has notable absorption features both in the hydride stretching ( $3256.0\text{ cm}^{-1}$ ) and in the far-infrared ( $475.7\text{ cm}^{-1}$ ). Additionally, a strong dipole moment and near-prolate character should make the rotational spectrum of  $\text{ArNH}_2^+$  relatively straight-forward to decipher in the laboratory. Laboratory synthesis of  $\text{ArCH}_2^+$  proceeded through reactions of  $\text{CH}_3\text{Br}^{2+}$  and argon atoms [21], and similar reactions may be possible with  $\text{NH}_3\text{Br}^{2+}$  leading to  $\text{ArNH}_2^+$  especially due to the noted stability of the ammonium cation in at least laboratory analysis. Additionally, this molecule may also form in condensed phase spectroscopic experiments in argon matrices potentially as a contaminant in any observed spectra. If so or even through other means, the present data will be helpful in spectroscopically characterizing this molecule in both the laboratory or potentially even in interstellar environments.

#### 5. Acknowledgements

NASA grant NNX17AH15G, NSF grant OIA-1757220, and start-up funds provided by the University of Mississippi supported this work.

#### References

- [1] Barlow, M. J.; Swinyard, B. M.; Owen, P. J.; Cernicharo, J.; Gomez, H. L.; Ivison, R. J.; Krause, O.; Lim, T. L.; Matsuura, M.; Miller, S.; Olofsson, G.; Polehampton, E. T. Detection of a Noble Gas Molecular Ion,  $^{36}\text{ArH}^+$ , in the Crab Nebula. *Science* **2013**, *342*, 1343–1345.
- [2] Roueff, E.; Alekseyev, A. B.; Bourlot, J. L. Photodissociation of Interstellar  $\text{ArH}^+$ . *Astron. Astrophys.* **2014**, *566*, A30.
- [3] Schilke, P. et al. Ubiquitous Argonium ( $\text{ArH}^+$ ) in the Diffuse Interstellar Medium: A Molecular Tracer of Almost Purely Atomic Gas. *Astron. Astrophys.* **2014**, *566*, A29.
- [4] Frash, M. V.; Hopkinson, A. C.; Bohme, D. K. A Quantum-Chemical Study of the Geometries and Electronic Structures of  $\text{ArO}$  and  $[\text{Ar},\text{O},\text{H}]^+$ : Proton Affinities of Singlet and Triplet  $\text{ArO}$ . *Phys. Chem. Chem. Phys.* **2000**, *2*, 2271–2274.

- [5] Theis, R. A.; Fortenberry, R. C. Potential Interstellar Noble Gas Molecules:  $\text{ArOH}^+$  and  $\text{NeOH}^+$  Rovibrational Analysis from Quantum Chemical Quartic Force Fields. *Mol. Astrophys.* **2016**, *2*, 18–24.
- [6] Fortenberry, R. C. Quantum Astrochemical Spectroscopy. *Int. J. Quant. Chem.* **2017**, *117*, 81–91.
- [7] Wagner, J. P.; McDonald II, D. C.; Duncan, M. A. An Argon–Oxygen Covalent Bond in the  $\text{ArOH}^+$  Molecular Ion. *Angew. Chem. Int. Ed* **2018**, *57*, 5081–5085.
- [8] Savage, B. D.; Sembach, K. R. Interstellar Abundances from Absorption-Line Observations with the *Hubble Space Telescope*. *Annu. Rev. Astron. Astrophys.* **1996**, *34*, 279–329.
- [9] McCall, B. J. Dissociative Recombination of Cold  $\text{H}_3^+$  and Its Interstellar Implications. *Phil. Trans. Royal Soc. A* **2006**, *364*, 2953–2963.
- [10] Fortenberry, R. C. Rovibrational Characterization of the Proton-Bound, Noble Gas Complexes:  $\text{ArHNe}^+$ ,  $\text{ArHAr}^+$ , and  $\text{NeHNe}^+$ . *ACS Earth Space Chem.* **2017**, *1*, 60–69.
- [11] Ascenzi, D.; Tosi, P.; Roithová, J.; Ricketts, C. L.; Lockyear, D. S. J. F.; Parkes, M. A.; Price, S. D. Generation of the Organo-Rare Gas Dications  $\text{HCCRg}^{2+}$  ( $\text{Rg} = \text{Ar}$  and  $\text{Kr}$ ) in the Reaction of Acetylene Dications with Rare Gases. *Phys. Chem. Chem. Phys.* **2008**, *10*, 7121–7128.
- [12] Novak, C. M.; Fortenberry, R. C. The Rovibrational Spectra of Three, Stable Noble Gas Molecules:  $\text{NeCCH}^+$ ,  $\text{ArCCH}^+$ , and  $\text{ArCN}^+$ . *Phys. Chem. Chem. Phys.* **2017**, *19*, 5230–5238.
- [13] Pauzat, F.; Ellinger, Y.  $\text{H}_3^+$  as a Trap for Noble Gases: 1 - The Case of Argon. *Planet. Space Sci.* **2005**, *53*, 1389.
- [14] Pauzat, F.; Ellinger, Y.  $\text{H}_3^+$  as a Trap for Noble Gases - 2: Structure and Energetics of  $\text{XH}_3^+$  Complexes from X=Neon to Xenon. *J. Chem. Phys.* **2007**, *127*, 014308.
- [15] Pauzat, F.; Ellinger, Y.; Pilmè, J.; Mousis, O.  $\text{H}_3^+$  as a Trap for Noble Gases - 3: Multiple Trapping of Neon, Argon, and Krypton in  $\text{X}_n\text{H}_3^+$  ( $n = 1 - 3$ ). *J. Chem. Phys.* **2009**, *130*, 174313.
- [16] Theis, R. A.; Morgan, W. J.; Fortenberry, R. C.  $\text{ArH}_2^+$  and  $\text{NeH}_2^+$  as Global Minima in the  $\text{Ar}^+/\text{Ne}^+ + \text{H}_2$  Reactions: Energetic, Spectroscopic, and Structural Data. *Mon. Not. R. Astron. Soc.* **2015**, *446*, 195–204.
- [17] Theis, R. A.; Fortenberry, R. C. Trihydrogen Cation with Neon and Argon: Structural, Energetic, and Spectroscopic Data from Quartic Force Fields. *J. Phys. Chem. A* **2015**, *119*, 4915–4922.
- [18] Pauzat, F.; Bacchus-Montabonel, M.-C.; Ellinger, Y.; Mousis, O. Trapping of Noble Gases by Radiation Association with  $\text{H}_3^+$  in the Protosolar Nebula. *Astrophys. J. Lett.* **2016**, *821*, L33.
- [19] Pauzat, F.; Ellinger, Y.; Mousis, O.; Dib, M. A.; Ozgurel, O. Gas-Phase Sequestration of Noble Gases in the Protosolar Nebula: Possible Consequences on the Outer Solar System Composition. *Astrophys. J.* **2013**, *777*, 29.
- [20] Westbrook, B. R.; Dreux, K. M.; Tschumper, G. S.; Francisco, J. S.; Fortenberry, R. C. Binding of the Atomic Cations Hydrogen through Argon to Water and Hydrogen Sulfide. *Phys. Chem. Chem. Phys.* **2018**, *20*, 25967–25973.
- [21] Ascenzi, D.; Tosi, P.; Roithová, J.; Schröder, D. Gas-Phase Synthesis of the Rare-Gas Carbene Cation  $\text{ArCH}_2^+$  Using Doubly Ionised Bromomethane as a Superelectrophilic Reagent. *Chem. Comm.* **2008**, 4055–4057.
- [22] Fortenberry, R. C.; Ascenzi, D.  $\text{ArCH}_2^+$ : A Detectable Noble Gas Molecule. *Chem. Phys. Chem.* **2018**, *19*, 1–6.
- [23] Bailleux, S.; Bogey, M.; Bolvin, H.; Civis, S.; Cordonnier, M.; Krupnov, A. F.; Tretyakov, M. Y.; Walters, A.; Coudert, L. H. Sub-Millimeter-Wave Spectroscopy of the  $\text{Ar}\cdot\text{H}_3^+$  and  $\text{Ar}\cdot\text{D}_3^+$  Ionic Complexes. *J. Molec. Spectrosc.* **1998**, *190*, 130–139.
- [24] Huang, X.; Taylor, P. R.; Lee, T. J. Highly Accurate Quartic Force Field, Vibrational Frequencies, and Spectroscopic Constants for Cyclic and Linear  $\text{C}_3\text{H}_3^+$ . *J. Phys. Chem. A* **2011**, *115*, 5005–5016.
- [25] Fortenberry, R. C.; Huang, X.; Francisco, J. S.; Crawford, T. D.; Lee, T. J. The *trans*-HOCO Radical: Fundamental Vibrational Frequencies, Quartic Force Fields, and Spectroscopic constants. *J. Chem. Phys.* **2011**, *135*, 134301.
- [26] Fortenberry, R. C.; Huang, X.; Francisco, J. S.; Crawford, T. D.; Lee, T. J. Fundamental Vibrational Frequencies and Spectroscopic Constants of  $\text{HOCS}^+$ ,  $\text{HSCO}^+$ , and Isotopologues via Quartic Force Fields. *J. Phys. Chem. A* **2012**, *116*, 9582–9590.
- [27] Huang, X.; Fortenberry, R. C.; Lee, T. J. Protonated Nitrous Oxide,  $\text{NNOH}^+$ : Fundamental Vibrational Frequencies and Spectroscopic Constants from Quartic Force Fields. *J. Chem. Phys.* **2013**, *139*, 084313.
- [28] Huang, X.; Fortenberry, R. C.; Lee, T. J. Spectroscopic Constants and Vibrational Frequencies for *l*- $\text{C}_3\text{H}^+$  and Isotopologues from Highly-Accurate Quartic Force Fields: The Detection of *l*- $\text{C}_3\text{H}^+$  in the Horsehead Nebula PDR Questioned. *Astrophys. J. Lett.* **2013**, *768*, 25.

- [29] Fortenberry, R. C.; Huang, X.; Crawford, T. D.; Lee, T. J. Quartic Force Field Rovibrational Analysis of Protonated Acetylene,  $\text{C}_2\text{H}_3^+$ , and Its Isotopologues. *J. Phys. Chem. A* **2014**, *118*, 7034–7043.
- [30] Zhao, D.; Doney, K. D.; Linnartz, H. Laboratory Gas-Phase Detection of the Cyclopropenyl Cation ( $\text{c-C}_3\text{H}_3^+$ ). *Astrophys. J. Lett.* **2014**, *791*, L28.
- [31] Morgan, W. J.; Fortenberry, R. C. Quartic Force Fields for Excited Electronic States: Rovibronic Reference Data for the  $1^2A'$  and  $1^2A''$  States of the Isoformyl Radical, HOC. *Spectrochim. Acta A* **2015**, *135*, 965–972.
- [32] Morgan, W. J.; Fortenberry, R. C. Theoretical Rovibronic Treatment of the  $\tilde{X}^2\Sigma^+$  and  $\tilde{A}^2\Pi$  States of  $\text{C}_2\text{H}$  &  $\tilde{X}^1\Sigma^+$  State of  $\text{C}_2\text{H}^-$  from Quartic Force Fields. *J. Phys. Chem. A* **2015**, *119*, 7013–7025.
- [33] Fortenberry, R. C.; Lee, T. J.; Müller, H. S. P. Excited Vibrational Level Rotational Constants for  $\text{SiC}_2$ : A Sensitive Molecular Diagnostic for Astrophysical Conditions. *Molec. Astrophys.* **2015**, *1*, 13–19.
- [34] Kitchens, M. J. R.; Fortenberry, R. C. The Rovibrational Nature of Closed-Shell Third-Row Triatomics: HOX and HXO, X =  $\text{Si}^+$ , P,  $\text{S}^+$ , and Cl. *Chem. Phys.* **2016**, *472*, 119–127.
- [35] Bizzocchi, L.; Lattanzi, V.; Laas, J.; Spezzano, S.; Giuliano, B. M.; Prudenzeno, D.; Endres, C.; Sipilä, O.; Caselli, P. Accurate Sub-millimetre Rest Frequencies for  $\text{HOCO}^+$  and  $\text{DOCO}^+$  Ions. *Astron. Astrophys.* **2017**, *602*, A34.
- [36] Palmer, C. Z.; Fortenberry, R. C. Rovibrational Considerations for the Monomers and Dimers of Magnesium Hydride ( $\text{MgH}_2$ ) and Magnesium Fluoride ( $\text{MgF}_2$ ). *J. Phys. Chem. A* **2018**, *122*, 7079–7088.
- [37] Novak, C. M.; Fortenberry, R. C. Theoretical Rovibrational Analysis of the Covalent Noble Gas Compound  $\text{ArNH}^+$ . *J. Molec. Spectrosc.* **2016**, *322*, 29–32.
- [38] Persson, C. M.; Hajigholi, M.; Hassel, G. E.; Olofsson, A. O. H.; Black, J. H.; Herbst, E.; Müller, H. S. P.; Cernicharo, J.; Wirstrom, E. S.; Olberg, M.; Hjalmarsen, A.; Lis, D. C.; Cuppen, H. M.; Gerin, M.; Menten, K. M. Upper Limits to Interstellar  $\text{NH}^+$  and *para*- $\text{NH}_2$  Abundances. Herschel-HIFI Observations towards Sgr B2 (M) and G10.6-0.4 (W31C). *Astron. Astrophys.* **2014**, *567*, A130.
- [39] Meyer, D. M.; Roth, K. C. Discovery of Interstellar NH. *Astrophys. J.* **1992**, *376*, L49–L52.
- [40] van Dishoeck, E. F.; Jansen, D. J.; Schilke, P.; Phillips, T. G. Detection of the Interstellar  $\text{NH}_2$  Radical. *Astrophys. J.* **1993**, *416*, L83–L86.
- [41] McCarthy, M. C.; Thaddeus, P. Microwave and Laser Spectroscopy of Carbon Chains and Rings. *Chem. Soc. Rev.* **2001**, *30*, 177–185.
- [42] Cheung, A. C.; Rank, D. M.; Townes, C. H.; Thornton, D. D.; Welch, W. J. Detection of  $\text{NH}_3$  Molecules in the Interstellar Medium by Their Microwave Emission. *Phys. Rev. Lett.* **1968**, *21*, 1701–1705.
- [43] Kaifu, N.; Morimoto, M.; Nagane, K.; Akabane, K.; Iguchi, T.; Takagi, K. Detection of Interstellar Methylamine. *Astrophys. J.* **1974**, *191*, L135–L137.
- [44] Belloche, A.; Menten, K. M.; Comito, C.; Müller, H. S. P.; Schilke, P.; J. Ott, S. T.; Hieret, C. Detection of amino acetonitrile in Sgr B2(N). *Astron. Astrophys.* **2008**, *482*, 179–196.
- [45] Huang, X.; Lee, T. J. A Procedure for Computing Accurate *Ab Initio* Quartic Force Fields: Application to  $\text{HO}_2^+$  and  $\text{H}_2\text{O}$ . *J. Chem. Phys.* **2008**, *129*, 044312.
- [46] Huang, X.; Lee, T. J. Accurate *Ab Initio* Quartic Force Fields for  $\text{NH}_2^-$  and  $\text{CCH}^-$  and Rovibrational Spectroscopic Constants for Their Isotopologues. *J. Chem. Phys.* **2009**, *131*, 104301.
- [47] Scheiner, A. C.; Scuseria, G. E.; Rice, J. E.; Lee, T. J.; Schaefer III, H. F. Analytic Evaluation of Energy Gradients for the Single and Double Excitation Coupled Cluster (CCSD) Wave Function: Theory and Application. *J. Chem. Phys.* **1987**, *87*, 5361–5373.
- [48] Raghavachari, K.; Trucks, G. W.; Pople, J. A.; Head-Gordon, M. A Fifth-Order Perturbation Comparison of Electron Correlation Theories. *Chem. Phys. Lett.* **1989**, *157*, 479–483.
- [49] Werner, H.-J. et al. MOLPRO, Version 2015.1, a Package of *ab Initio* Programs. 2015; see <http://www.molpro.net>.
- [50] Werner, H.-J.; Knowles, P. J.; Knizia, G.; Manby, F. R.; Schütz, M. Molpro: A General-Purpose Quantum Chemistry Program Package. *WIREs Comput. Mol. Sci.* **2012**, *2*, 242–253.
- [51] Peterson, K. A.; Dunning, T. H. Benchmark Calculations with Correlated Molecular Wave Functions. VII. Binding Energy and Structure of the HF Dimer. *J. Chem. Phys.* **1995**, *102*, 2032–2041.
- [52] Dunning, T. H. Gaussian Basis Sets for Use in Correlated Molecular Calculations. I. The Atoms Boron through Neon and Hydrogen. *J. Chem. Phys.* **1989**, *90*, 1007–1023.

- [53] Martin, J. M. L.; Taylor, P. R. Basis Set Convergence for Geometry and Harmonic Frequencies. Are  $h$  Functions Enough? *Chem. Phys. Lett.* **1994**, *225*, 473–479.
- [54] Fortenberry, R. C.; Trabelsi, T.; Francisco, J. S. Hydrogen Sulfide as a Scavenger of Sulfur Atomic Cation. *J. Phys. Chem. A* **2018**, *122*, 4983–4987.
- [55] Martin, J. M. L.; Lee, T. J. The Atomization Energy and Proton Affinity of  $\text{NH}_3$ . An *Ab Initio* Calibration Study. *Chem. Phys. Lett.* **1996**, *258*, 136–143.
- [56] Douglas, M.; Kroll, N. Quantum Electrodynamical Corrections to the Fine Structure of Helium. *Ann. Phys.* **1974**, *82*, 89–155.
- [57] Allen, W. D.; coworkers, 2005; *INTDER* 2005 is a General Program Written by W. D. Allen and Coworkers, which Performs Vibrational Analysis and Higher-Order Non-Linear Transformations.
- [58] Mills, I. M. In *Molecular Spectroscopy - Modern Research*; Rao, K. N., Mathews, C. W., Eds.; Academic Press: New York, 1972; pp 115–140.
- [59] Watson, J. K. G. In *Vibrational Spectra and Structure*; Daring, J. R., Ed.; Elsevier: Amsterdam, 1977; pp 1–89.
- [60] Papousek, D.; Aliev, M. R. *Molecular Vibration-Rotation Spectra*; Elsevier: Amsterdam, 1982.
- [61] Gaw, J. F.; Willets, A.; Green, W. H.; Handy, N. C. In *Advances in Molecular Vibrations and Collision Dynamics*; Bowman, J. M., Ratner, M. A., Eds.; JAI Press, Inc.: Greenwich, Connecticut, 1991; pp 170–185.
- [62] Møller, C.; Plesset, M. S. Note on an Approximation Treatment for Many-Electron Systems. *Phys. Rev.* **1934**, *46*, 618–622.
- [63] Hehre, W. J.; Ditchfeld, R.; Pople, J. A. Self-Consistent Molecular Orbital Methods. XII. Further Extensions of Gaussian-Type Basis Sets for Use in Molecular Orbital Studies of Organic Molecules. *J. Chem. Phys.* **1972**, *56*, 2257.
- [64] Frisch, M. J. et al. Gaussian 09 Revision D.01. 2009; Gaussian Inc. Wallingford CT.
- [65] Yu, Q.; Bowman, J. M.; Fortenberry, R. C.; Mancini, J. S.; Lee, T. J.; Crawford, T. D.; Klemperer, W.; Francisco, J. S. The Structure, Anharmonic Vibrational Frequencies, and Intensities of  $\text{NNHNN}^+$ . *J. Phys. Chem. A* **2015**, *119*, 11623–11631.
- [66] Finney, B.; Fortenberry, R. C.; Francisco, J. S.; Peterson, K. A. A Spectroscopic Case for SPSi Detection: The Third-Row in a Single Molecule. *J. Chem. Phys.* **2016**, *145*, 124311.
- [67] McKellar, A. R. W.; Vervloet, M.; Burkholder, J. B.; Howard, C. J. A Combined Analysis of the  $\nu_1$ ,  $\nu_3$ , and  $2\nu_2$  Vibrational States of the  $\text{NH}_2$  Radical Using Fourier Transform Absorption and Emission Data. *J. Molec. Spectrosc.* **1990**, *142*, 319–335.



Table 2: The CcCR QFF  $\text{ArNH}_2^+$  Equilibrium and Zero-Point ( $R_\alpha$ ) Structures, Vibrational Frequencies, Harmonic Intensities (in parenthesis in km/mol), and Spectroscopic Constants for the  $^{36}\text{Ar}$ ,  $^{38}\text{Ar}$ , and  $^{40}\text{Ar}$  Isotopologues.

	$^{36}\text{ArNH}^+$	$^{38}\text{ArNH}^+$	$^{40}\text{ArNH}^+$
$r_e(\text{Ar}-\text{N})$ Å	1.856 320	—	—
$r_e(\text{N}-\text{H})$ Å	1.030 553	—	—
$\angle(\text{Ar}-\text{N}-\text{H})$	97.706	—	—
$\angle(\text{H}-\text{N}-\text{H})$	106.554	—	—
$\tau(\text{H}-\text{Ar}-\text{N}-\text{H})$	107.747	—	—
$A_e$ MHz	253039.4	253037.8	253036.4
$B_e$ MHz	12748.7	12545.6	12362.4
$C_e$ MHz	12510.9	12315.3	12138.7
$D_J$ MHz	0.033	0.032	0.031
$D_{JK}$ MHz	0.371	0.362	0.354
$D_K$ MHz	7.245	7.254	7.262
$d_1$ kHz	-0.749	-0.715	-0.684
$d_2$ kHz	-0.020	-0.020	-0.018
$H_J$ Hz	-0.018	-0.017	-0.016
$H_{JK}$ Hz	1.840	1.769	1.706
$H_{KJ}$ Hz	35.292	34.392	33.592
$H_K$ kHz	462.134	462.892	463.563
$h_1$ mHz	3.411	3.210	3.037
$h_2$ mHz	0.401	0.371	0.345
$h_3$ mHz	0.013	0.012	0.011
$r_0(\text{Ar}-\text{N})$ Å	1.875 057	1.874 990	1.874 928
$r_0(\text{N}-\text{H})$ Å	1.041 581	1.041 576	1.041 572
$\angle(\text{Ar}-\text{N}-\text{H})$	97.706	97.707	97.707
$\angle(\text{H}-\text{N}-\text{H})$	106.606	106.606	106.606
$\tau(\text{H}-\text{Ar}-\text{N}-\text{H})$	107.799	107.799	107.799
$A_0$ MHz	249491.0	249488.5	249486.2
$B_0$ MHz	12530.6	12331.5	12151.9
$C_0$ MHz	12288.9	12097.4	11924.5
$A_1$ MHz	245615.0	245612.5	245610.2
$B_1$ MHz	12481.9	12283.8	12105.0
$C_1$ MHz	12481.9	12058.0	11885.6
$A_2$ MHz	244747.0	244744.5	244742.2
$B_2$ MHz	12487.7	12289.4	12110.5
$C_2$ MHz	12246.7	12055.9	11883.6
$A_3$ MHz	247284.3	247279.8	247275.9
$B_3$ MHz	12526.6	12326.8	12146.6
$C_3$ MHz	12243.1	12052.2	11879.8
$A_4$ MHz	252090.5	252081.5	252073.4
$B_4$ MHz	12456.4	12259.5	12081.7
$C_4$ MHz	12262.3	12071.4	11898.9
$A_5$ MHz	250729.1	250733.0	250736.6
$B_5$ MHz	12392.9	12195.9	12018.0
$C_5$ MHz	12126.3	11937.6	11767.1
$A_6$ MHz	249383.5	249381.0	249378.8
$B_6$ MHz	12401.8	12205.7	12028.7
$C_6$ MHz	12162.0	11973.5	11803.1
$\mu_x$ D			1.78
$\mu_y$ D			2.13
$\mu$ D			2.78
$\omega_1$ ( $a'$ ) symmetric N-H $\text{cm}^{-1}$	3437.4	3437.4	3437.4 (106)
$\omega_2$ ( $a''$ ) antisym. N-H $\text{cm}^{-1}$	3332.3	3332.3	3332.3 (65)
$\omega_3$ ( $a'$ ) symmetric H-N-Ar bend $\text{cm}^{-1}$	1521.7	1521.7	1521.7 (77)
$\omega_4$ ( $a'$ ) Ar OPB $\text{cm}^{-1}$	1233.7	1233.3	1233.0 (87)
$\omega_5$ ( $a''$ ) antisym. H-N-Ar bend $\text{cm}^{-1}$	1177.5	1177.2	1176.9 (2)
$\omega_6$ ( $a'$ ) Ar-N $\text{cm}^{-1}$	507.2	503.2	499.5 (102)
$\nu_1$ ( $a'$ ) symmetric N-H $\text{cm}^{-1}$	3256.0	3256.0	3256.0
$\nu_2$ ( $a''$ ) antisym. N-H $\text{cm}^{-1}$	3168.0	3168.1	3168.1
$\nu_3$ ( $a'$ ) symmetric H-N-Ar bend $\text{cm}^{-1}$	1457.2	1457.2	1457.1
$\nu_4$ ( $a'$ ) Ar OPB $\text{cm}^{-1}$	1199.1	1198.8	1198.4
$\nu_5$ ( $a''$ ) antisym. H-N-Ar bend $\text{cm}^{-1}$	1136.7	1136.4	1136.2
$\nu_6$ ( $a'$ ) Ar-N $\text{cm}^{-1}$	482.9	479.1	475.7
Zero-Point $\text{cm}^{-1}$	5514.4	5512.1	5510.0