## Observation of $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$

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We report the first observation of the hadronic transition $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$, using $496 \mathrm{fb}^{-1}$ data collected at the $\Upsilon(4 S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^{+} e^{-}$collider. We reconstruct the $\eta^{\prime}$ meson through its decays to $\rho^{0} \gamma$ and to $\pi^{+} \pi^{-} \eta$, with $\eta \rightarrow \gamma \gamma$. We measure $\mathcal{B}\left(\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)\right)=[3.43 \pm 0.88($ stat $) \pm 0.21($ syst $)] \times 10^{-5}$, with a significance of $5.7 \sigma$.

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One of the major challenges in particle physics is the treatment of quantum chromodynamics (QCD) in the nonperturbative regime [1]. In particular, heavy quarkonia, i.e., bound states of one heavy quark and its antiquark, thanks to their intrinsic multiscale behavior, are one of the most promising and clean laboratories in which to explore these dynamics [2]. Hadronic transitions between bottomonia (i.e., $b \bar{b}$ bound states) have been, in the past few years, a fertile field for both experiment and theory. On the basis of heavy quark spin symmetry, the QCD multipole expansion (QCDME) model predicts that transitions involving the $\eta$ particle should be suppressed relative to dipion transitions [3]. Several recent results [4-7] challenge this long-standing expectation. Following these measurements, it has been argued that the light-quark degrees of freedom actively intervene in the transitions [8].

Few processes for the $\Upsilon(4 S)$ meson decaying to the non$B \bar{B}$ system have been measured thus far [9]. There have been no searches for the kinematically allowed transition $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$, which is expected to be as strong as $\Upsilon(4 S) \rightarrow \eta \Upsilon(1 S)$ [8], where the relative strength of the $\eta^{\prime}$ and $\eta$ transitions depends on the relative $u \bar{u}+d \bar{d}$ content of the mesons, and is predicted to range between $20 \%$ and $60 \%$. In contrast, a significant dominance of the $\eta^{\prime}$ transition is predicted by QCDME models. In the charmonium sector, searches for $\psi(4160) \rightarrow \eta^{\prime} J / \psi$ and $Y(4260) \rightarrow \eta^{\prime} J / \psi$ transitions have been made by CLEO [10] without the observation of significant signals, while the observation of $e^{+} e^{-} \rightarrow \eta^{\prime} J / \psi$ at center-of-mass energies of 4.226 and 4.258 GeV has been reported by BESIII [11].

In this Letter, we present the first observation of the transition $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$. The $\Upsilon(1 S)$ meson is reconstructed via its leptonic decay to two muons, which is considerably cleaner than the dielectron mode. The $\eta^{\prime}$ meson is reconstructed via its decays to $\rho^{0} \gamma$ and to $\pi^{+} \pi^{-} \eta$, with the $\eta$ meson reconstructed as two photons.

We use a sample of $(538 \pm 8) \times 10^{6} \Upsilon(4 S)$ mesons, corresponding to an integrated luminosity of $496 \mathrm{fb}^{-1}$,

[^1]collected by the Belle experiment at the KEKB asymmetric-energy $e^{+} e^{-}$collider [12,13]. In addition, a data sample corresponding to $56 \mathrm{fb}^{-1}$, collected about 60 MeV below the resonance, is used to estimate the background contribution.

The Belle detector (described in detail elsewhere [ 14,15$]$ ) is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters, and an electromagnetic calorimeter comprised of $\mathrm{CsI}(\mathrm{Tl})$ crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux return located outside of the coil (KLM) is instrumented to detect $K_{L}^{0}$ mesons and to identify muons.

Monte Carlo (MC) simulated events are used for the efficiency determination and the selection optimization; these are generated using EvtGEn [16] and simulated to model the detector response using GEANT3 [17]. The changing detector performance and accelerator conditions are taken into account in the simulation. The distributions of generated dimuon decays incorporate the $\Upsilon(1 S)$ polarization. The angular distribution in the $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$ transition is simulated as a vector decaying to a pseudoscalar and a vector. The $\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \eta$ and the $\eta \rightarrow \gamma \gamma$ decays are generated uniformly in phase space, while the $\eta^{\prime} \rightarrow$ $\rho^{0} \gamma \rightarrow \pi^{+} \pi^{-} \gamma$ decay is generated assuming the appropriate helicity. Final state radiation effects are modeled in the generator by Рнотоs [18].

Charged tracks must originate from a cylindrical region of length $\pm 5 \mathrm{~cm}$ along the $z$ axis, which is aligned opposite to the positron beam, and radius 1 cm in the transverse plane, centered on the $e^{+} e^{-}$interaction point, and must have a transverse momentum $\left(p_{T}\right)$ greater than $0.1 \mathrm{GeV} / c$. Charged particles are assigned a likelihood $\mathcal{L}_{i}$, with $i=\mu$, $\pi, K$ [19], based on the range of the particle extrapolated from the CDC through the KLM; particles are identified as muons if the likelihood ratio $\mathcal{P}_{\mu}=\mathcal{L}_{\mu} /\left(\mathcal{L}_{\mu}+\mathcal{L}_{\pi}+\mathcal{L}_{K}\right)$ exceeds 0.8 , corresponding to a muon efficiency of about $91.5 \%$ over the polar angle range $20^{\circ} \leq \theta \leq 155^{\circ}$ and the momentum range $0.7 \mathrm{GeV} / c \leq p \leq 3.0 \mathrm{GeV} / c$ in the laboratory frame. Electron identification uses a similar likelihood ratio $\mathcal{P}_{e}$ based on CDC, ACC, and ECL information [20]. Charged particles that are not identified as muons and having a likelihood ratio $\mathcal{P}_{e}<0.1$ are treated
as pions. Calorimeter clusters not associated with reconstructed charged tracks and with energies greater than 50 MeV are classified as photon candidates. Pairs of oppositely charged tracks, of which at least one is positively identified as a muon, are selected as dimuon candidates. Pairs of oppositely charged tracks, both classified as pions, are selected as dipion candidates. Retained events contain exactly one dimuon candidate and one dipion candidate. For $\eta^{\prime} \rightarrow \rho^{0} \gamma$ decays, hereinafter labeled as $2 \pi 1 \gamma$, only events with at least one photon and with the photon-dipion invariant mass within $50 \mathrm{MeV} / c^{2}( \pm 3 \sigma)$ of the nominal $\eta^{\prime}$ mass [9] are retained. Similarly, for the $\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \eta, \eta \rightarrow \gamma \gamma$ decay chain, hereinafter labeled as $2 \pi 2 \gamma$, only events with at least two photons having an invariant mass within $50 \mathrm{MeV} / c^{2}( \pm 3 \sigma)$ of the nominal $\eta$ mass [9] and with an invariant-mass difference $M\left(\pi^{+} \pi^{-} \gamma \gamma\right)-M(\gamma \gamma)$ within $20 \mathrm{MeV} / c^{2}( \pm 3 \sigma)$ of $M\left(\eta^{\prime}\right)-$ $M(\eta)$ are considered. In $2 \pi 1 \gamma(2 \pi 2 \gamma)$ final states, 1.2 (1.4) candidates per event are present on average, where the multiplicity is due to one or more accidental photons. The ambiguity is resolved by choosing the one whose reconstructed $\eta^{\prime}$ mass is closest to the nominal value. This choice has an efficiency of $\sim 90 \%$ on the MC-simulated signal samples. The events with $\left|\sqrt{s}-M\left[\mathrm{r}(1 S) \eta^{\prime}\right] c^{2}\right|<$ 150 MeV , where $\quad M\left[\mathrm{Y}(1 S) \eta^{\prime}\right]=M\left(\mu^{+} \mu^{-} \pi^{+} \pi^{-} \gamma\right)$ [M( $\left.\left.\mu^{+} \mu^{-} \pi^{+} \pi^{-} \gamma \gamma\right)\right]$ in the $2 \pi 1 \gamma[2 \pi 2 \gamma]$ final state and $\sqrt{s}$ is the center-of-mass (c.m.) $e^{+} e^{-}$energy, are retained.

The kinematic bound expressed by the quantity $p_{\mathrm{KB}}=$ $p(\mu \mu)_{\text {c.m. }}-\left[s-M(\mu \mu)^{2} c^{4}\right] /(2 c \sqrt{s})$, where $p(\mu \mu)_{\text {c.m. }}$ is the c.m. momentum of the dimuon system, is constrained to negative values for signal events and is used to reject part of the background contribution due to QED processes [ $e^{+} e^{-} \rightarrow e^{+} e^{-}(\gamma)$ and $e^{+} e^{-} \rightarrow \mu^{+} \mu^{-}(\gamma)$ ]. Further reductions of QED processes and of cosmic background events are achieved by requiring the opening angle of the charged pion candidates in the c.m. frame to satisfy $\left|\cos \theta(\pi \pi)_{\text {c.m. }}\right|<0.9$.

The $2 \pi 1 \gamma$ final state has contributions from dipion transitions to the $\mathrm{\Upsilon}(1 S)$ resonance from either $\mathrm{\Upsilon}(2 S, 3 S)$ resonances produced in initial state radiation events or the $\Upsilon(4 S)$ resonance in which a random photon is incorporated into the $\eta^{\prime}$ candidate. The high production cross section values [21] and decay rates [9] make these processes competitive with the signal transition, and particular care is needed to reduce them to negligible levels. A boosted decision tree (BDT) method, as implemented in the Toolkit for Multivariate Data Analysis package [22], is trained to separate the signal events from those due to dipion transitions. The performance of the classifier is optimized and tested using MC-simulated samples for both the signal and dipion transitions. The input variables used to construct the BDT are the difference between invariant masses $\Delta M_{\pi \pi}=M\left(\mu^{+} \mu^{-} \pi^{+} \pi^{-}\right)-M\left(\mu^{+} \mu^{-}\right)$and the total reconstructed mass of the event $M\left(\mu^{+} \mu^{+} \pi^{+} \pi^{-} \gamma\right)$. The highest discrimination is provided by $\Delta M_{\pi \pi}$. This variable is
broadly distributed for signal events, while backgrounds are sharply peaked at the values $563.0 \pm 0.4,894.9 \pm 0.6$, and $1119.1 \pm 1.2 \mathrm{MeV} / c^{2}$, for $\mathrm{r}(2 S), \mathrm{r}(3 S)$, and $\Upsilon(4 S) \rightarrow \pi^{+} \pi^{-} \Upsilon(1 S)$, respectively [9], with experimental resolutions of a few $\mathrm{MeV} / c^{2}$. It has been verified that, with respect to a cut-based approach, the BDT method enhances the dipion rejection while retaining a higher signal efficiency. The reconstructed invariant mass of the $\eta^{\prime}$ candidate must lie within $0.93 \mathrm{GeV} / c^{2}<M\left(\pi^{+} \pi^{-} \gamma\right)<$ $0.98 \mathrm{GeV} / c^{2}$, which retains $90 \%$ of signal events.

The overall selection efficiencies for the signal events in the $2 \pi 1 \gamma$ and $2 \pi 2 \gamma$ final states are $\epsilon=(17.64 \pm 0.05) \%$ and ( $5.02 \pm 0.03$ ) \%, respectively, as determined from MC-simulated samples. The selection efficiency for $\Upsilon(2 S, 3 S, 4 S) \rightarrow$ $\pi^{+} \pi^{-} \Upsilon(1 S)$ events is in the range of $10^{-6}-10^{-4}$, making their contribution negligible. The contributions from these and other background sources are measured with a data sample collected below the $\Upsilon(4 S)$ resonance; a fraction of less than $\sim 10^{-8}$ of the data remains in the $2 \pi 1 \gamma$ final state, while no events are present in the $2 \pi 2 \gamma$ final state.

The signal events are identified by the variable

$$
\begin{equation*}
\Delta M_{\eta^{\prime}}=M[\mathrm{r}(4 S)]-M[\mathrm{r}(1 S)]-M\left(\eta^{\prime}\right), \tag{1}
\end{equation*}
$$

where $\quad M[\Upsilon(1 S)]=M\left(\mu^{+} \mu^{-}\right)$in both final states; for the $2 \pi 1 \gamma \quad[2 \pi 2 \gamma]$ final state, $M[\Upsilon(4 S)]=$ $M\left(\mu^{+} \mu^{-} \pi^{+} \pi^{-} \gamma\right)\left[M\left(\mu^{+} \mu^{-} \pi^{+} \pi^{-} \gamma \gamma\right)\right]$ and $M\left(\eta^{\prime}\right)=M\left(\pi^{+} \pi^{-} \gamma\right)$ [M( $\left.\pi^{+} \pi^{-} \gamma \gamma\right)$ ]. The expected resolution for the signal is $7-8 \mathrm{MeV} / c^{2}$, depending on the reconstructed $\eta^{\prime}$ decay mode. The distribution of $\Delta M_{\eta^{\prime}}$ versus $M\left(\eta^{\prime}\right)$ [ $\left.M\left(\eta^{\prime}\right)-M(\eta)\right]$ for the $2 \pi 1 \gamma[2 \pi 2 \gamma]$ candidates is shown in Fig. 1 [Fig. 2] in a broad range of the abscissa in order to illustrate the distribution.


FIG. 1. Distribution of $\Delta M_{\eta^{\prime}}$ versus $M\left(\eta^{\prime}\right)$ for the selected events (binned into the boxes) in the $2 \pi 1 \gamma$ final state. The vertical dashed lines show the $\pm 3 \sigma$ selected region. The signal-selection region of $0.93 \mathrm{GeV} / c^{2}<M\left(\pi^{+} \pi^{-} \gamma\right)<0.98 \mathrm{GeV} / c^{2}$ is bounded by the vertical solid lines. The two-dimensional region where $97 \%$ of the signal events are expected is bounded by these vertical lines and the two red horizontal lines.


FIG. 2. Distribution of $\Delta M_{\eta^{\prime}}$ versus $M\left(\eta^{\prime}\right)-M(\eta)$ for the selected events (binned into the boxes) in the $2 \pi 2 \gamma$ final state. The vertical dashed lines show the $\pm 3 \sigma$ selected region. The twodimensional region where $97 \%$ of the signal events are expected is bounded by these vertical lines and the two red horizontal lines.

The signal and background yields are determined by an unbinned maximum likelihood fit to the $\Delta M_{\eta^{\prime}}$ distribution, shown in Fig. 3. The signal component is parametrized by a Gaussian-like analytical function


FIG. 3. Fit to the $\Delta M_{\eta^{\prime}}$ distribution for $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$ candidates reconstructed in the $2 \pi 1 \gamma$ (top) and $2 \pi 2 \gamma$ (bottom) final states. Data are shown as points, and the solid blue line shows the best fit to the data, while the dashed red line shows the background contribution.

$$
\begin{equation*}
\mathcal{F}(x)=\exp \left(-\frac{(x-\mu)^{2}}{2 \sigma_{L, R}^{2}+\alpha_{L, R}(x-\mu)^{2}}\right) \tag{2}
\end{equation*}
$$

with mean value $\mu$, distinct widths $\sigma_{L, R}$, and asymmetrictail parameters $\alpha_{L, R}$ on either side of the peak. The background is described by a very broad Gaussian (linear) function in the $2 \pi 1 \gamma(2 \pi 2 \gamma)$ final state. The signal shape parameters are fixed to the values determined from the MCsimulated sample. The signal and background yields in the $2 \pi 1 \gamma$ final state are $N_{\text {sig }}=22 \pm 7$ and $N_{\text {bkg }}=96 \pm 11$, respectively. In the $2 \pi 2 \gamma$ final state, the signal and background yields are $N_{\text {sig }}=5.0 \pm 2.3$ and $N_{\text {bkg }}=2.0 \pm 1.6$, respectively.

The statistical significance of the signal is determined as $\sqrt{2 \log \left[\mathcal{L}\left(N_{\text {sig }}\right) / \mathcal{L}(0)\right]}$, where $\mathcal{L}\left(N_{\text {sig }}\right) / \mathcal{L}(0)$ is the ratio between the likelihood values for a fit that includes a signal component versus a fit with only the background hypothesis. The statistical significance is estimated to be $4.2 \sigma$ ( $4.1 \sigma$ ) in the $2 \pi 1 \gamma(2 \pi 2 \gamma)$ final state.

Several sources of systematic uncertainty affect the branching fraction measurement, including the number of $\Upsilon(4 S)$ events $N_{\Upsilon(4 S)}( \pm 1.4 \%)$ and the values used for the secondary branching fractions $\mathcal{B}_{\text {secondary }}( \pm 2.7 \%$ for $2 \pi 1 \gamma$ and $\pm 2.6 \%$ for $2 \pi 2 \gamma$ ) [9]. The uncertainties in charged track reconstruction ( $\pm 1.4 \%$ ) and muon identification efficiency $( \pm 1.1 \%)$ are determined by comparing data and MC events using independent control samples. The largest contribution to the systematic uncertainty comes from the signal extraction procedure $( \pm 6.8 \%$ for $2 \pi 1 \gamma$ and $\pm 2.0 \%$ for $2 \pi 2 \gamma$ ). The uncertainty due to the choice of signal parameterizations is estimated by changing the functional forms used; the systematic uncertainty for the background form is evaluated by using second-order polynomial or exponential functions and by varying the range chosen for the fit. An additional uncertainty is related to the chosen values for the signal shape parameters and is evaluated by repeating the fit while varying each of them by $\pm 1 \sigma$ with respect to their nominal value. In each case, the uncertainty is estimated as the variation in the signal yield when using an alternate configuration with respect to that obtained with the nominal one. Not all of the partial width of $\eta^{\prime} \rightarrow \pi^{+} \pi^{-} \gamma$ can be explained by a resonant decay through a $\rho^{0}$ [23,24]. The potential systematic bias in the signal efficiency due to the presence of nonresonant decays is estimated by comparing the selection efficiencies between the default resonant sample and a completely nonresonant one. Half of the difference is conservatively assigned as a systematic error $(-1.9 \%$ for $2 \pi 1 \gamma)$. Other possible sources of systematic uncertainties, due to discrepancies between the data and MC simulations in the efficiency of the applied selection requirements or in the photon energy calibration, have been found to be relatively small. The total systematic uncertainty is obtained by adding in quadrature all of the contributions and amounts
to $7.6 \%$ for the $2 \pi 1 \gamma$ final state and $3.5 \%$ for the $2 \pi 2 \gamma$ final state.

The value of the branching fraction $\mathcal{B}$ is calculated as

$$
\begin{equation*}
\mathcal{B}=\frac{N_{\text {sig }}}{\epsilon \times N_{\mathrm{Y}(4 S)} \times \mathcal{B}_{\text {secondary }}} . \tag{3}
\end{equation*}
$$

We measure $\mathcal{B}=(3.19 \pm 0.96($ stat $) \pm 0.24($ syst $)) \times 10^{-5}$ in the $2 \pi 1 \gamma$ final state and $\mathcal{B}=(4.53 \pm 2.12($ stat $) \pm$ 0.16 (syst)) $\times 10^{-5}$ in the $2 \pi 2 \gamma$ final state. The measurements obtained from the two independent subsamples are combined in a weighted average, where the weight is the inverse of the squared sum of the statistical and systematic uncertainties on each yield, considering only the systematic contributions that are uncorrelated between the two channels. The systematic uncertainties in common between the two channels are then added in quadrature to obtain the total uncertainty. The measured branching fraction is $\mathcal{B}\left(\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)\right)=$ $(3.43 \pm 0.88($ stat $) \pm 0.21($ syst $)) \times 10^{-5}$. The statistical significance of the combined measurement is estimated by performing a simultaneous fit to the two disjoint data sets, using the same parameterizations as before and constraining the signal normalization so that the ratio of the signal yield divided by the signal efficiency and the secondary branching fractions is the same in the two data sets. The statistical significance of the combined measurement is $5.8 \sigma$; this is reduced to $5.7 \sigma$ when considering yield-related systematic uncertainties by convolving the likelihood function with a Gaussian whose width equals the systematic uncertainty. This measurement represents the first observation of the hadronic transition $\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)$.

We also determine the ratios of branching fractions:

$$
\begin{equation*}
R_{\eta^{\prime} / h}=\frac{\mathcal{B}\left(\Upsilon(4 S) \rightarrow \eta^{\prime} \Upsilon(1 S)\right)}{\mathcal{B}(\Upsilon(4 S) \rightarrow h \Upsilon(1 S))} \tag{4}
\end{equation*}
$$

where the decay is mediated by a hadronic state $h=\eta$ or $\pi^{+} \pi^{-}$. For $\mathcal{B}(\Upsilon(4 S) \rightarrow h \Upsilon(1 S))$, we use the values obtained in Ref. [5], which analyzes the same data sample considered in this Letter. Several systematic uncertainties cancel, being common to the numerator and denominator. The results from the two $\eta^{\prime}$ decay modes are combined in a weighted average, as for the branching fraction measurement, and are $R_{\eta^{\prime} / \eta}=0.20 \pm 0.06$ and $R_{\eta^{\prime} / \pi^{+} \pi^{-}}=0.42 \pm 0.11$. The former ratio, in particular, is in agreement with the expected value in the case of an admixture of a state containing light quarks in addition to the $b \bar{b}$ pair in the $\Upsilon(4 S)$ in bottomonium hadronic transitions; a value of 0.2 is predicted in Eq. (6) in Ref. [8], with a reasonable assumption of the ratio of the form factors, i.e., $F\left(p_{\eta}\right) / F\left(p_{\eta^{\prime}}\right) \approx 1$.

The past few years have seen a large amount of activity by both experiment and theory to study more closely the unexpected nature of $\eta$ transitions between bottomonium states. Following this path, the described measurement, being the first observation of an $\eta^{\prime}$ transition, adds another
tile to our effort to understand the puzzle of hadronic transitions between heavy quarkonia.

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