

The Electrothermal Instability on Pulsed Power Ablations of Thin Foils

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Abstract—Presented are results from optical imaging of atmospheric ablations of thin aluminum foils. These experiments were performed to evaluate the growth of temperature perturbations attributed to the electrothermal instability (ETI). ETI has been shown to seed magnetohydrodynamic (MHD) instabilities on pulsed-power-driven ablations of initially solid metallic targets, a topic of interest to various programs in pulsed-power-driven plasma physics that depend on stable liner implosions. Experimental observations presented herein demonstrate exponentially growing temperature perturbations perpendicular to the direction of current with growth rates consistent with linear ETI theory. High-temperature regions were observed to enter the vapor phase before sufficient energy had been deposited in the bulk foil to overcome the latent heat of vaporization, indicating significant spatial heterogeneity in energy deposition rates. The growth rates of these perturbations scale as the square of current density, the predicted behavior for long-wavelength ETI structures. The development of these structures was unchanged by physical deformation of the foil surface, but dramatically influenced by incorporating areas of local high resistance in the foil loads. Extending the observation window in time showed a transition from perpendicular to parallel filaments, which is significant because ETI is predicted to switch orientations when the bulk foil material transitions into the plasma state. Collectively, these results provide experimental validation of many theoretical predictions regarding ETI.

Index Terms—Electrothermal effects, optical imaging, plasma pinch, plasma stability

I. INTRODUCTION

THE ablation of initially solid metals on pulsed power drivers is an active area of research with applications in dynamic material properties [1, 2], intense radiation generation [3-6], and magnetized liner inertial fusion (MagLIF) [7-11]. These experiments typically seek to minimize the growth of magnetohydrodynamic (MHD) instabilities, such as the magneto-Rayleigh-Taylor (MRT) instability [11, 12], for

optimum performance. Theoretical and experimental studies have provided significant evidence showing that the initial surface perturbations from which these instabilities grow can be seeded by a phenomenon known as the electrothermal instability (ETI) [13-17]. Therefore, controlling ETI may provide a means to reduce the impact of plasma instabilities on ablations of metallic targets.

ETI refers to the growth of a temperature perturbation in an ohmically heated medium with temperature-dependent resistivity $\eta(T)$. These temperature perturbations tend to manifest as striations of hot and cold material perpendicular to the flow of current when $\partial\eta/\partial T \propto 0$ (e.g. in condensed metals) and as filamentations parallel to the flow of current when $\frac{\partial\eta}{\partial T} \propto 0$ (e.g. in Spitzer-like plasma). A qualitative description of the mechanism believed to be responsible for the self-organization of initial perturbations into striations or filamentations (depending on the sign of $\partial\eta/\partial T$) is presented in Fig. 1.

The general linear dispersion relation for ETI [13, 18] in a thin foil or cylindrical liner of thickness d with current density J directed along the z -axis, neglecting the effects of material expansion, is given by

$$\gamma(t, T, k) s = \frac{2 \frac{\eta}{T} \left(1 - \frac{c \kappa \alpha^4}{1 + \left(\frac{\gamma}{\gamma_0} \right)} \right) - k^4 \kappa}{\rho c_v}. \quad (1)$$

In (1), γ is the instantaneous growth rate of ETI as a function of time t , temperature T , and wavenumber k $s \approx \pi/\lambda$; α is the angle between a perturbation and the z -axis (such that $\cos \alpha = 0$ when the wave vector is in the z -direction); κ , ρ , and c_v are the temperature-dependent thermal conductivity, density, and specific heat capacity of the unperturbed material; and γ_0 is a characteristic growth rate given by

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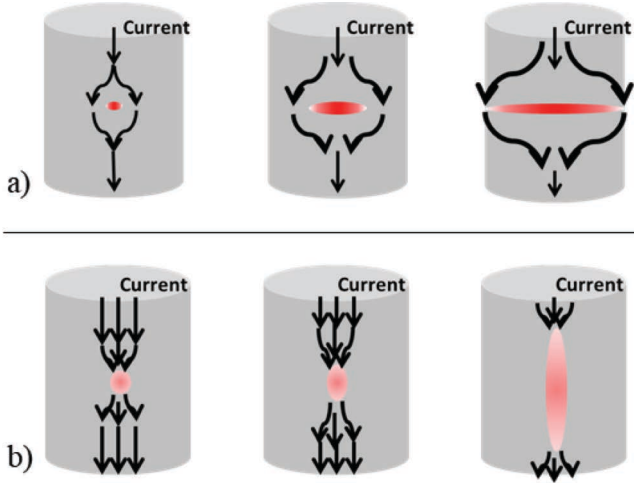


Fig. 1. Self-correlation of ETI on ohmically heated objects. (a) Striation-form, $\partial\eta/\partial T > 0$: initial hotspots grow from nonuniformities in resistivity and increase in resistance as temperature rises due to locally increased Ohmic heating (left). Current density concentrates near the edges of the hotspot, which leads to areas of increased heating on either side of the hotspot (center), expanding the hotspot in the direction perpendicular to current until the hotspot has become a striation (right). (b) Filamentation-form, $\partial\eta/\partial T < 0$: an initial hotspot is less resistive, which draws more current into the hotspot than surrounding material (left). This causes areas of high current density above and below the hotspot, increasing the Ohmic heating in these regions and expanding the hotspot vertically (center), continuing in the direction parallel to current until the hotspot has become a filament (right).

$$\gamma_0 = \frac{2k\eta}{\mu d} \quad (2)$$

where μ is the permeability of the material. The first term in (1) is the dominant growth term when $\partial\eta/\partial T > 0$, the second term is the dominant growth term when $\partial\eta/\partial T < 0$, and the third term describes damping due to thermal conductivity.

Growth of the $\partial\eta/\partial T > 0$ striation form of ETI is of particular interest to pulsed power plasma physics experiments, as these exponentially growing, perpendicular-to-current temperature perturbations cause sections of the initially solid metallic target to ablate before the bulk material. Surface perturbations arising from this process can provide the initial seed on the plasma-vacuum boundary from which magnetohydrodynamic [19, 20] and magneto-Rayleigh-Taylor [11, 15, 16] instabilities can grow. When $\partial\eta/\partial T$ is positive, as is initially the case during a pulsed-power ablation of a condensed metal target, the minimum growing ETI wavelength is given by

$$\lambda_{min} = \frac{2\pi}{J} \sqrt{\kappa \left(\frac{\partial\eta}{\partial T} \right)^{-1}} \quad (3)$$

and the maximum growth rate, corresponding to $\cos \alpha = 0$, for a given wavelength is

$$\gamma_m(t, T, k) = \frac{\partial\eta}{\partial T} \frac{J^2}{\rho c_v} - \frac{k^2 \kappa}{\rho c_v}. \quad (4)$$

For large wavelength perturbations, $\lambda = 2\pi/k \gg \lambda_{min}$, the first term in Eq. (4) dominates, i.e.

$$\gamma_{max}(t, T) = \frac{\partial\eta}{\partial T} \frac{J^2}{\rho c_v}. \quad (5)$$

It is noteworthy that while $\partial\eta/\partial T$, ρ , and c_v are in general functions of temperature, for many metals, including aluminum, the ratio $\frac{\partial\eta}{\partial T}/\rho c_v$ is approximately constant over a large temperature range. (For liquid aluminum, this ratio varies from $3.3 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$ to $3.8 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$ between the melting point and the vaporization point at atmospheric pressure [21-26].) Therefore, it is anticipated that large-wavelength ETI perturbations exhibit a growth rate that is approximately proportional to J^2 in such materials.

When $\partial\eta/\partial T$ is negative, which is expected to occur when the target has fully ablated and entered a plasma state exhibiting Spitzer-like resistivity, (1) is quadratic in γ , with maximum growth rate corresponding to $\alpha = \pi/2$. Regardless of the sign of $\partial\eta/\partial T$, manipulation of Eq. (1) also yields a condition on α :

$$\cos^2 \alpha < \frac{1}{2} \left(1 - \frac{k^2 \kappa}{J^2} \left(\frac{\partial\eta}{\partial T} \right)^{-1} \right). \quad (6)$$

Note that (1)-(6) are derived assuming the current-carrying material does not expand. While this is a reasonable assumption for solids and liquids, the effects of material expansion may become important once the material reaches the vaporization point. The linear dispersion relation for perpendicular-to-current ETI structures allowing for material expansion, derived in [27], is given by

$$\gamma = \frac{J^2 \frac{\partial\eta}{\partial T} - k^2 \kappa + \frac{\rho}{T^*} \left(c_v \frac{\partial T}{\partial t} - J^2 \frac{\partial\eta}{\partial \rho} \right)}{\rho c_v + \frac{p}{T^*}}. \quad (7)$$

where p is pressure and T^* is a characteristic temperature function of pressure and density established using a simplified equation of state. The first two terms in (7) are analogous to the expansion-free case in (4), the third term represents an additional destabilizing term arising from material heating, and the fourth term represents the increase in resistivity with decreasing density. These terms allow perpendicular-to-current ETI to continue to grow even after the material has transitioned into the plasma state until $\partial\eta/\partial T$ becomes sufficiently negative to overcome the additional growth terms.

Previous experimental work by Awe et al. [28] demonstrated the growth of bright, hot regions on pulsed power ablations of electrically thick (physical size greater than skin depth δ), cylindrical rods. The Awe study demonstrated self-organization of initial resistivity perturbations into perpendicular-to-current striations (as in Fig. 1); additionally, the transition to parallel-to-current filamentations was observed after the rod surface ablated [28]. In this article, we establish a procedure for estimating the position-dependent temperature of ablating, ultrathin (0.4 to 2.0 μm thickness) aluminum foils from light emission observed on an ultrafast intensified charge-coupled device (ICCD) camera. By choosing a geometry that is electrically thin (thickness $\ll \delta$), we restrict the generally three-dimensional process of current division to two dimensions, allowing for more direct comparison with linear ETI theory summarized in (1)-(7). Additionally, correlating light emission to temperature allows for direct comparison of experimental

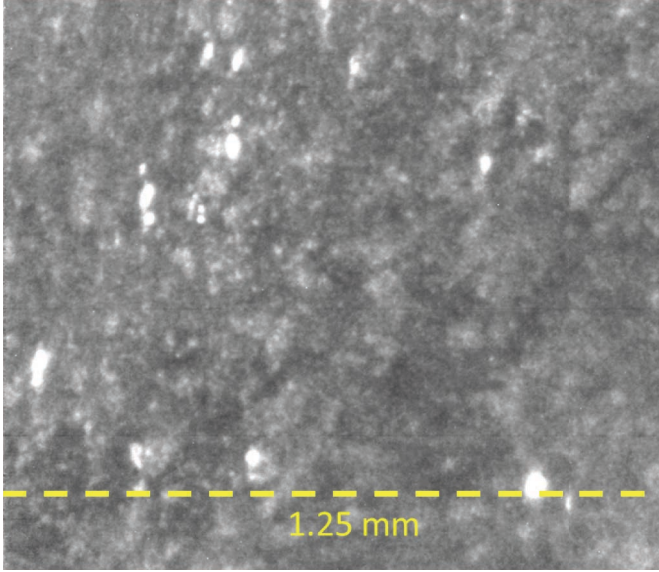


Fig. 3. Pre-shot image showing typical foil surface characteristics. Bright spots are due to a combination of sharp points on the surface of the foil resulting from folds and impurity inclusions of differing reflectance.

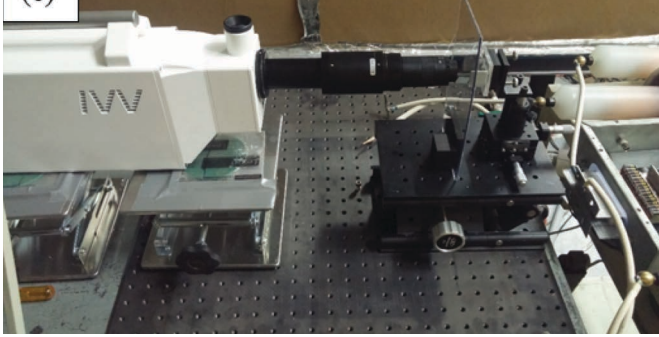


Fig. 2. Summary of experimental setup. (a) Circuit schematic of simple pulsed power device used for foil ablations. (b) Schematic of load hardware showing foil load location and experimental variation in foil dimensions. (c) Experimental setup showing ultrafast framing camera with zoom imaging lens positioned to image a foil load. A Plexiglas sheet positioned between the load and the imaging lens prevents debris from the exploding foil from damaging the lens.

and predicted ETI growth rates.

Our experimental setup is described in Section II. Section III details the procedure employed to estimate position-dependent temperature from light emission observed on the ICCD. In Section IV, we present 12-frame temperature measurements of ablating aluminum foils, demonstrating physics consistent with the theory of ETI. Section V presents a growth rate analysis of the experimentally measured temperature perturbations. Our results and analysis yield the following four key observations: 1) ablations of thin metallic liners demonstrated exponentially growing temperature perturbations perpendicular to the direction of current flow prior to the bulk material entering the plasma phase; 2) the growth rate of large-wavelength perturbations scaled with J^2 , the predicted ETI behavior; 3) the seeding of these perturbations was unchanged by physical deformation of the foil surface, but dramatically influenced by including areas of local high resistance; and (4) extending the observation window late showed a transition from perpendicular striations of hotter material to parallel filaments

of hotter material. Our conclusions are summarized in Section VI.

II. EXPERIMENTAL SETUP

Ablations of thin planar foils in ambient, atmospheric pressure air were carried out on a pulse generator consisting of a single 240 nF capacitor in series with a self-breaking spark gap switch which closes at an applied voltage of 13 kV. HV-insulated wires connecting the pulse generator to the load have an equivalent inductance of 864 nH, and a resistor array totaling 0.83Ω is connected in series to the output of the switch. This relatively large impedance (along with the equivalent series resistance and inductance of the switch and capacitor of 0.28Ω and 80 nH) leads to a pulse of 4 kA peak current and 600 ns risetime that is load-independent to within 5% for all foil loads used in this study. A schematic of the pulse generator/load circuit is shown in Fig. 2(a).

Load current density was varied between shots by changing the dimensions of the foil loads. The experiments described in this work utilized Goodfellow aluminum foils of thicknesses 400 nm, 800 nm, and $2.0 \mu\text{m}$. These foils are of 99.1% rated purity, with impurities primarily consisting of iron (0.47%), silicon (0.16%), titanium (0.07%), and gallium (0.05%). Foils were cut into strips of length 15 mm with widths varying from 2.5 mm to 10 mm using a razor edge. This variance of thickness and width allowed the investigation of a peak current density parameter space of approximately $2 \times 10^7 \text{ A/cm}^2$ to $4 \times 10^7 \text{ A/cm}^2$. A manufacturer-specified uncertainty on foil thickness of 25%, along with an estimated cutting width uncertainty of 10%, places an uncertainty of 27% on the current density. The thickness uncertainty is due to the rolling process used to generate the thin foils, which introduces perturbations of much longer characteristic length scale than the dimensions of the foils used in these experiments. Additionally, examination of the razor-cut foil edges under an optical microscope showed edge fraying on the order of $\sim 10 \mu\text{m}$ (less than 1% of the foil widths used in these experiments). Therefore, we include a 27% on the foils on a shot-to-shot basis, with intra-shot current density variation on the order of a few percent.

The load hardware consisted of two aluminum plates connected to the anode and cathode of the pulse generator which were spaced 9 mm apart and mounted on a plastic support structure. For each shot, foils were cut and placed on the support structure; the load hardware plates were secured on top of the foil to provide electrical contact (see Fig. 2(b)). The assembled load hardware was affixed to optical stands and placed on an array of translation stages to allow controlled movement in the x-, y-, and z-directions. Time-dependent load current and voltage were measured using a Pearson Electronics wideband current monitor and two ground-referenced North Star PVM-5 high voltage probes connected to the anode and cathode plates. These diagnostics allowed for time-resolved measurements of power delivered to the load.

The primary optical diagnostic fielded in these experiments was a 12-frame, ultrafast, intensified charge-coupled device (ICCD) camera produced by Invisible Vision. The maximum

frame rate of this camera is 2×10^8 frames per second, and minimum exposure time per frame is 5 ns. An Edmund Optics VZM-1000 Zoom Imaging Lens was mounted on the camera to provide optical magnification ranging from 2.5 to 10 (see Fig. 2(c)). A backlit 1951 USAF resolution test target positioned at the in-focus imaging distance for the maximum 10X magnification yielded a minimum resolvable wavelength of 2.5 μm (400 line pairs / mm).

The framing camera was used to collect self-emission in the visible portion of the spectrum from the ablating foils as a function of time. A response vs. wavelength curve supplied by the manufacturer was used for the calibration procedure described in Section III. Several shots utilized time-integrated spectroscopy to obtain information about the composition of plasma formed during foil ablation. The Acton SP-750i spectrometer fielded on these shots was calibrated in-situ for absolute irradiance using a 40 W, OL-245 standard of spectral irradiance; wavelength-shift calibration was performed using neon, argon, and mercury lamps positioned at the location of the load hardware.

For each shot, the translation stages were used to make fine adjustments to load position to optimize focus and to fix the camera imaging window on the center of the foil, which was maintained as the region of interest to minimize the contribution of edge effects such as contact resistance with the electrodes. Each foil was imaged in-situ prior to the shot using a long (~ 10 ms) exposure setting on the framing camera and illuminating the surface of the foil with a high-intensity LED flashlight. Microscopic foil nonuniformities including wrinkles and impurity inclusions are visible on these pre-shot images (see Fig. 3).

III. PROCEDURE FOR ESTIMATING MATERIAL TEMPERATURE

To allow observation of the electrothermal instability as a perturbation in temperature (as opposed to a physical boundary perturbation characteristic of most plasma instabilities), it was necessary to develop a method to correlate the time-resolved light emission measurements on the framing camera with instantaneous surface temperature. Blackbody-like thermal radiation was assumed to be the dominant mechanism responsible for the self-emission detected by the camera as the foil material transitioned through the liquid, vapor, and weakly ionized plasma states. (Note that because the minimum resolvable emission using this diagnostic corresponded to a surface temperature of ~ 2500 K, no emission was observable while the foil material was in the solid state.) To support this assumption, the contributions from competing mechanisms of line emission, Bremsstrahlung radiation, and radiative recombination/free-bound transmission emission were considered and found to be no more than a few percent of the total observed visible-spectrum radiation. These calculations employed conservative estimates of electron temperature and number density, applied late into the current pulse after most of the capacitively stored energy has been deposited into the ablating foil. Details of these calculations can be found in [29].

Bright striations of hotter material were consistently

observed on aluminum foil ablations; the dynamics of these striations are addressed in Section IV. Time-integrated spectroscopic analysis of emitted light from these ablations consistently showed 466 nm lines attributed to Al-II superimposed onto a blackbody emission curve. Varying the background gas by conducting the ablation within a transparent plastic enclosure and flowing N_2 , Ar, or SF_6 fill gases did not alter the measured spectra, and no lines attributable to the background gas were visible on any shots on which spectroscopy was fielded (the effects of surface contaminants, such as hydrocarbons, were not considered in this study). Conducting ablations on a similar setup in vacuum resulted in substantially lower total emission levels. The observed dynamics of emitting features were qualitatively similar between air, N_2 , and Ar, but emitting features expanded noticeably slower in SF_6 . Quantitative changes in dynamics of the ablating features due to different background gases were considered outside the scope of the present study. We interpret these results to indicate 1) the source of the light emission is weakly ionized aluminum, not the background gas and 2) the presence of ambient pressure slows the expansion of vaporized aluminum (compared to its velocity in vacuum) to the medium-dependent shock velocity [30,31]. The presence of nonzero ambient pressure causes sections of the aluminum that have entered the vapor phase to remain in good electrical contact with the bulk material longer for ablations in air compared to ablations in vacuum. For this reason, atmospheric pressure ablations provide a longer timescale to observe the electrothermal instability, allowing more electrical energy to be deposited into these regions before they disperse explosively. All ablations analyzed in this manuscript were performed in ambient, atmospheric pressure air.

With the assumptions that light emission originates from the ablating foil material and behaves as a graybody, temperature can be computed from camera response, which is linear with incident irradiance at values below saturation according to manufacturer specifications. This calibration is accomplished by determining the integral radiated power for a graybody source of given temperature, image size, and emissivity; adjusting for the wavelength-dependent response of the camera; and calibrating against a graybody source of known temperature and emissivity. This process provides 12-frame temperature imaging with the same spatial and temporal resolution as the framing camera system.

To calibrate camera response, a tungsten standard of spectral irradiance (emissivity 0.43) with known steady-state temperature 2977 K was placed at the in-focus distance from the lens on 10X magnification and imaged using the framing camera at various exposure times. This process yielded the 0-255 grayscale camera response (per pixel, per nanosecond of exposure) associated with a blackbody radiating at 2977 K at the location of the foil load, which was found to be 0.33 ns^{-1} . Blackbody spectra at temperatures from 2000 K to 10000 K were convolved with the wavelength-dependent camera response curves and integrated over wavelength to give proportional values of camera response as a function of temperature. Absolute calibration of camera response as a

function of blackbody emitter temperature was obtained by normalizing proportional camera response to 0.33 ns^{-1} at 2977 K and 10X magnification. This calibration was extended to other magnifications through the relation

$$\frac{R}{R_{10}} s \left(\frac{10}{m}\right)^2 \left(\frac{D}{D_{10}}\right)^2 \quad (8)$$

where R is the camera response on the 0-255 scale for a given temperature, R_{10} is the camera response for 10X magnification for the same temperature, m is the magnification, D is the in-focus distance at magnification m , and D_{10} is the in-focus distance for 10X magnification. In (8), the $\left(\frac{10}{m}\right)^2$ factor accounts for the increased collection area per pixel at lower magnifications and the $\left(\frac{D}{D_{10}}\right)^2$ factor is due to the inverse square relationship with distance. In general, the temperature range that can be reliably measured by the camera varies from shot to shot as the camera response depends on both exposure time and magnification; the minima and maxima are set by the temperatures corresponding to responses of 10 (the noise floor) and 245 (approaching saturation, above which camera response is nonlinear with incident power). The camera response varied on the order of 5-10% from frame to frame on the constant temperature calibration source, which places an approximated $\pm 5\%$ uncertainty on these temperature measurements obtained from camera response.

To correlate camera response with emitting surface temperature of an ablating aluminum foil, the emissivity of aluminum in the temperature range of interest is also required. While the emissivity of solid and liquid aluminum has been experimentally measured at temperatures below 1500 K [32] little information exists on aluminum emissivity at temperatures in the 2000 K to 10000 K range. For this work, emissivity ϵ_{Al} of both bi-phase liquid/vapor aluminum at the vaporization point and superheated aluminum vapor was assumed to be 1. This assumption places a lower bound on the temperature of the emitting regions. For comparison, the difference in temperature calculated using $\epsilon_{Al} \approx 1$ compared with $\epsilon \approx 0.7$ (typical of refractory metals near their ~ 3000 K melting points) is around 25%, while the difference compared with $\epsilon \sim 0.1$ (characteristic of liquid aluminum above 1000 K) is around 50%. While these errors are significantly larger than the $\pm 5\%$ error due to the camera response uncertainty, it is noteworthy that measurements using this temperature inversion technique of partially vaporized, bi-phase aluminum with expected temperature equal to T_{vapor} (2743 K, the atmospheric pressure vaporization temperature of aluminum) yielded values centered around 2700 K. These measurements are discussed in detail in Section IV. We make the following two observations on the accuracy of the measurement technique: (1) the intrinsic camera response error places a $\pm 7\%$ uncertainty on the *lower bound* of position-dependent temperature measurements; and (2) the uncertainty *with respect to the lower bound* may be as high as 50% due to the unknown emissivity of very hot aluminum, but our experimental evidence suggests this second uncertainty

may be much lower in practice.

IV. EXPERIMENTAL OBSERVATIONS OF TEMPERATURE PERTURBATIONS

Image sequences of ablating foils were converted into temperature data using the response calibrations described in the previous section. A total of 102 shots were conducted in ambient air over the current density parameter space of interest. While the framing camera was timed too early or too late relative to start-of-current to capture the onset of resolvable light emission on some shots, the formation of hot, perpendicular-to-current striations was observed without exception for shots with good camera timing (~ 60 out of the 102 total shots). Fig. 4 shows a typical temperature measurement sequence for the central 1.25 mm x 1.08 mm region of an 800-nm thick, 10-mm wide foil, demonstrating the formation of striations arising from merging of initial hotspots. Temperature measurements presented in this section represent the lower bounds calculated from camera response assuming $\epsilon \approx 1$. As described in Section III, the exposure time and pixel size of each image establishes a resolvable temperature range, above which the camera reads saturation and below which the camera reads below the noise floor of response.

Comparing the time integral of the power deposited in the foil (as measured from the voltage and current data) with the total energy required to vaporize the foil from room temperature revealed that the bright filamentary structures consistently occurred before the bulk foil had vaporized. During the formation and development of the bright striations, the energy deposited in the foil divided by the foil mass was larger than the quantity q_1 , the integral of the specific heat from room temperature to boiling temperature plus the latent heat of fusion, but smaller than q_2 , the latent heat of vaporization plus q_1 . Moreover, for all but the smallest cross-section foils, the

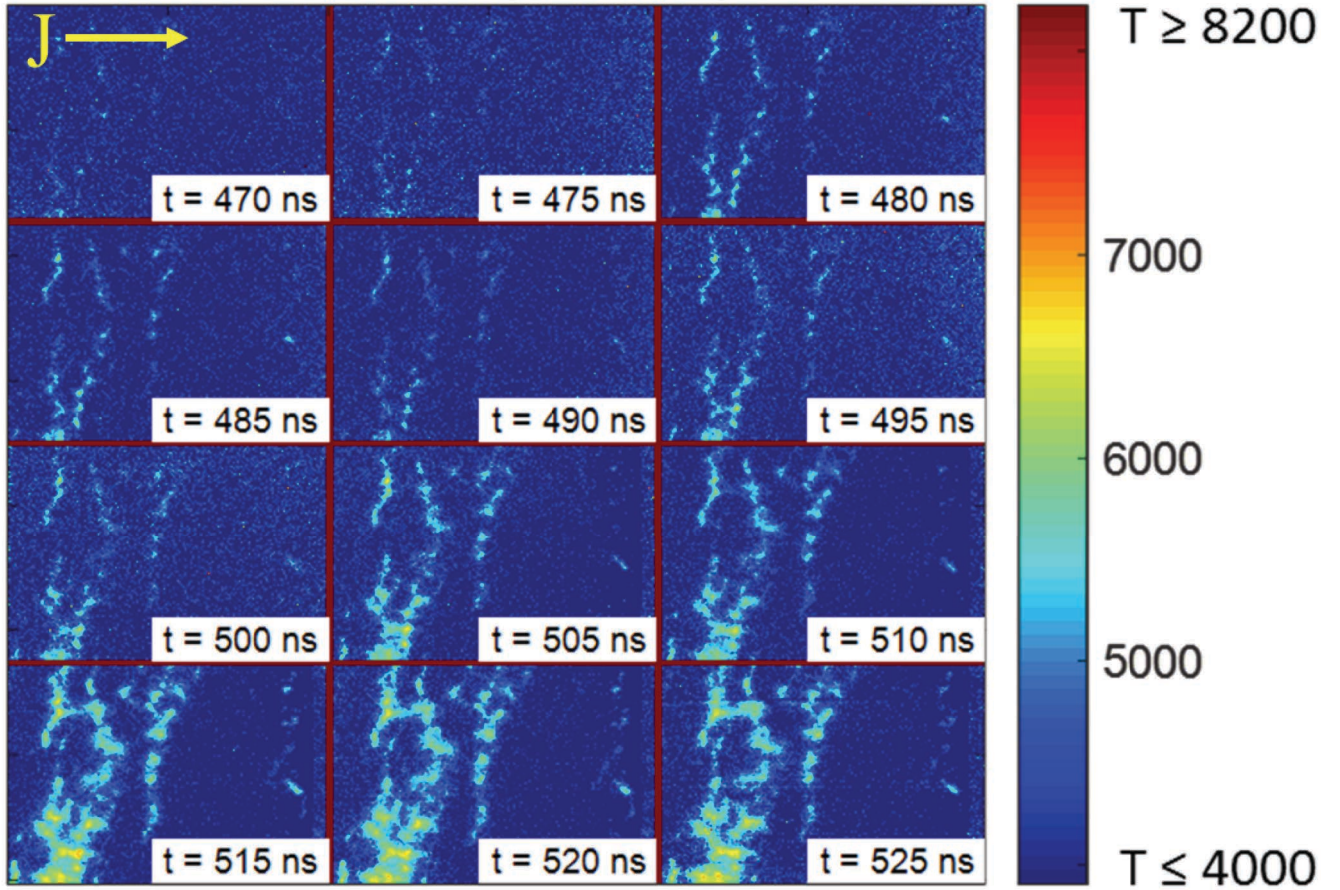


Fig. 4. Temperature surface maps (in K) for an 800 nm x 1.0 cm x 0.9 cm foil; average current density over the observation window was 3.9×10^7 A/cm². Image sizes are 1.08 mm x 1.25 mm, current flows from left to right. Temperatures outside the range of 4000 to 8200 K are unresolvable because they are outside of the boundaries set by the noise floor and saturation limits of the camera. Temperatures above the 4000-K noise floor represent a lower bound due to the $\epsilon = 1$ assumption with uncertainty on this lower bound of $\pm 5\%$.

stored energy in the capacitor bank divided by the foil mass was lower than q_2 (but significantly higher than q_1). As these bright spots correspond to temperature measurements significantly hotter than the vaporization temperature of aluminum—thousands of kelvins hotter in some cases—this observation indicates the existence of significant spatial heterogeneity in energy deposition prior to the bulk foil explosion.

Because the time frame of interest for each shot uniformly occurred after the bulk foil had received sufficient energy to reach the vaporization temperature but before enough energy had been deposited to overcome the latent heat of vaporization, it was anticipated that the unperturbed aluminum should be in the bi-phase liquid-vapor transition at these times. The “dark” regions of framing camera images are therefore expected to correspond to the vaporization temperature of aluminum at atmospheric pressure T_{vapor} (2743 K). To verify this assumption, several shots were performed with long (40–80 ns) exposure times to resolve these relatively low temperatures at the cost of temporal resolution (see Fig. 5).

Fig. 5 shows striations beginning to form, with the hottest spots already exceeding the maximum resolvable temperature of 4200 K. Far from these striations, the temperature of the material is in the 2600 K to 2800 K range, showing excellent agreement with the predicted 2743 K. For all shots with a higher resolvable temperature floor, such as the shot shown in Fig. 5,

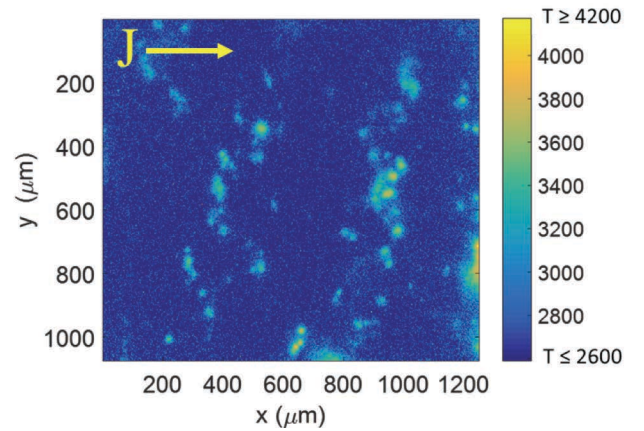


Fig. 5. Temperature plot (in Kelvin) of an 80-ns exposure image, taken on an 800 nm x 1.0 cm x 0.9 cm aluminum foil to establish the temperature of the background aluminum (which is always below the noise floor on shorter exposure images). For this exposure and magnification, resolvable temperature range is 2600 K to 4200 K. Temperatures above the noise floor represent a lower bound due to the $\epsilon = 1$ assumption with uncertainty on this lower bound of $\pm 5\%$.

the bulk foil material is therefore assumed to be at $T_b = T_{\text{vapor}}$. The hot, bright striations are then taken to be perturbations in temperature superimposed on the bulk bi-phase aluminum. Setting the average temperature of the foil equal to T_{vapor} inherently assumes that the mass contained in the hot striations is small compared to the total mass of the foil. This assumption

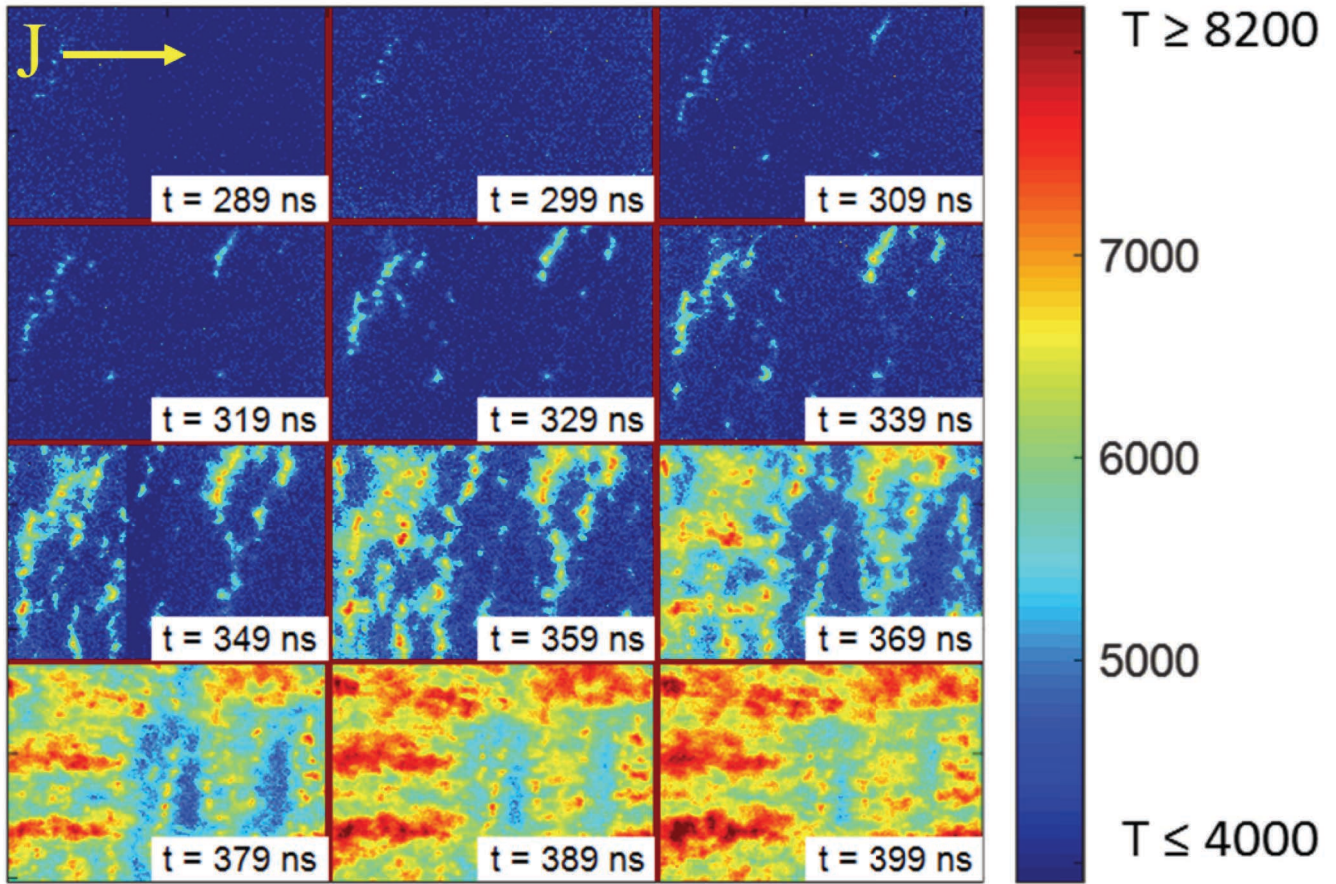


Fig. 6. Temperature surface plot of an 800 nm x 0.7 cm x 0.9 cm aluminum foil ablation showing plasma from vaporized sections of the foil merging and developing filamentary (parallel-to-current) structures late in time. Image sizes are 1.08 mm x 1.25 mm, current flows from left to right. Temperatures above the noise floor represent a lower bound due to the $\epsilon = 1$ assumption with uncertainty on this lower bound of $\pm 5\%$.

is reasonable because the deposited energy, which has already been established as insufficient to bulk vaporize the foil during the time frame of interest, was certainly insufficient to raise a sizeable fraction of the material to temperatures greatly exceeding the vaporization temperature.

Structures parallel to the direction of current, believed to be the filamentation form of ETI, were also observed on several of the highest current density shots that included late-time images. These late frames showed plasma features that began to merge and form optically thick filaments above the surface of the bulk material. Fig. 6 presents a typical temperature surface plot sequence showing this phenomenon.

Although the later frames of Fig. 6 appear to be completely covered in hot plasma, sufficient energy had not been delivered to the foil to vaporize the bulk material by the last frame. This is possibly explained by a continuing runaway heating process in zones which had already vaporized due to ETI due to the additional effects of the density dependence of resistivity. Further heating of vaporized striations may be sufficient to cause ionization and the transition to a Spitzer-like, negative $\partial\eta/\partial T$ regime above the surface of the background aluminum (which is still bi-phase liquid/vapor at T_{vapor}). This top layer of plasma would then be expected to be unstable to filamentation-form ETI. A future computational study may be warranted to investigate this phenomenon further.

In general, the merging of initial hotspots to form perpendicular-to-current striations appeared to be a random process. As the initial foils were known to contain both surface deformations (wrinkles) and impurity inclusions, a series of six shots was performed to probe the relative contribution to ETI formation due to the two types of imperfections. For the first three shots, a standard #0-80 screw was rolled onto strips of 800 nm aluminum foil to impress grooves approximately 320 μm apart that dominated the natural folds in the foil. These grooves were impressed at 70 degrees relative to the direction of current flow to minimize the chance of confusing randomly occurring perpendicular-to-current structures with structures seeded by the grooves; this 70-degree angle is well above the minimum growing angular condition for striation-form ETI given by (3). A groove-seeded foil and associated temperature measurement sequence are shown in Fig. 7. Fig. 7 demonstrates a lack of correlation between the initial surface perturbations and the ETI that develops; this result was consistent with the other shots taken with the same initial conditions.

To mimic the effect of resistive inclusion seeding, three additional shots were conducted on foils that had two holes of approximately 50 μm diameter machined ~ 1 cm apart. These holes were positioned such that the line joining them was approximately 75 degrees from the parallel-to-current direction. Because one of the primary impurities in the aluminum foils

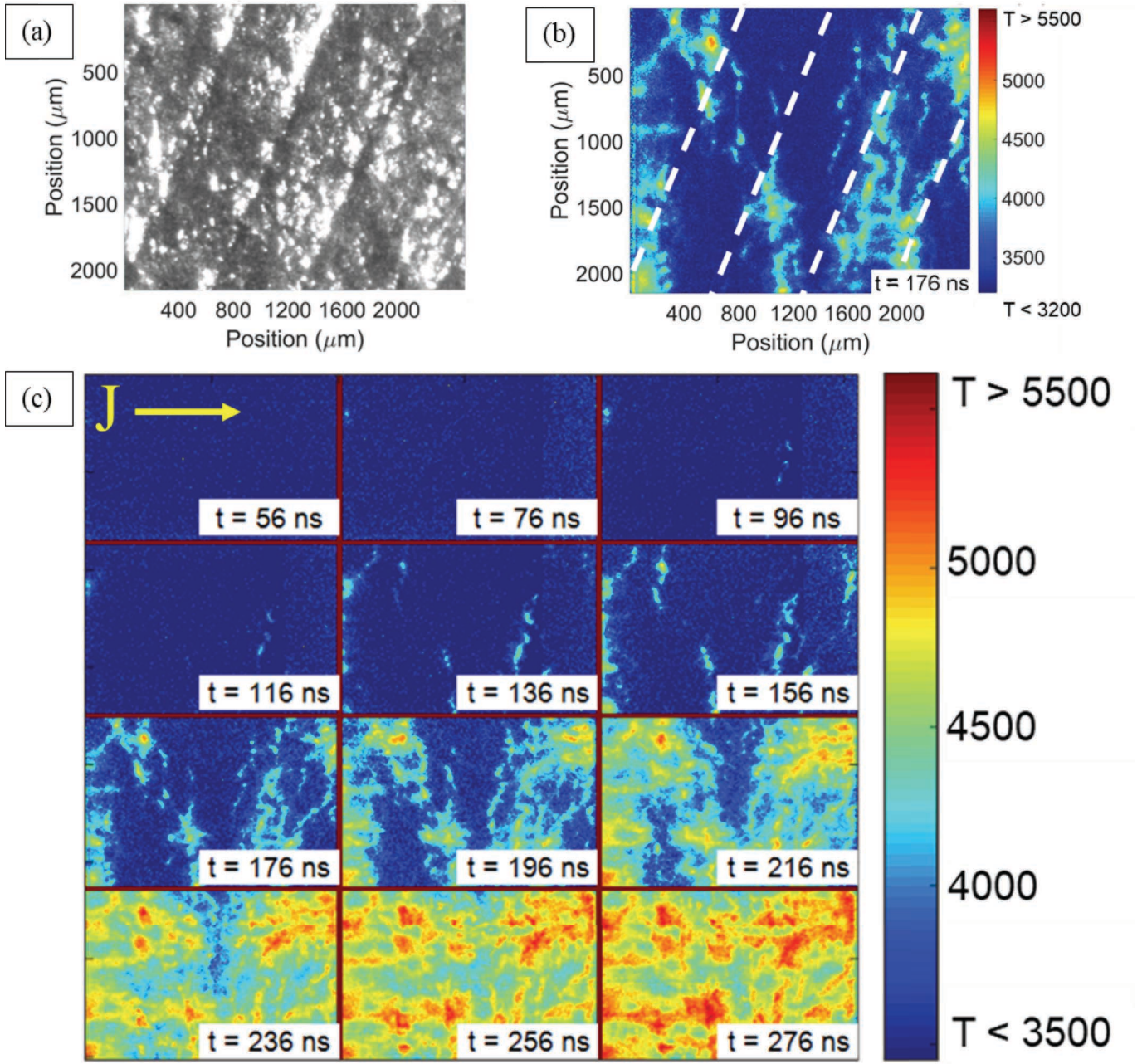


Fig. 7. (a) Pre-shot image showing grooves embedded in an $800 \text{ nm} \times 0.7 \text{ cm} \times 0.9 \text{ cm}$ foil to impose a long-wavelength surface deformation. Grooves are approximately $320 \mu\text{m}$ apart. (b) Selected image around the formation time of the first striations. The white lines show the location of the initial temperature grooves (c) Full temperature plot sequence showing instability growth. All image sizes are $2.5 \text{ mm} \times 2.15 \text{ mm}$; current flows from left to right. Temperatures above the noise floor represent a lower bound due to the $\epsilon = 1$ assumption with uncertainty on this lower bound of $\pm 5\%$.

used throughout this study is silicon (which has a room temperature resistivity that is 7 to 8 orders of magnitude higher than aluminum) the holes were taken to be a good approximation of a large silicon inclusion. Fig. 8 shows typical results from a shot with the machined holes.

A clear ETI striation can be seen on Fig. 8(b), joining the position of the holes shown on Fig. 8(a). This provides experimental confirmation for the self-correlation of ETI around a resistive hotspot as proposed conceptually in Fig. 1. Fig. 8(c) shows that the seeded structure is the first ETI striation to form and is dominant up until most of the striations have expanded and merged. This observation may provide the physical mechanism responsible for the previously observed

reduction in density of ETI striations with increasing material purity [28].

V. ANALYSIS OF STRIATION-FORM ETI GROWTH RATES

To compare the experimental data with theoretical predictions of ETI growth rate, a procedure was established to determine a temporally and spatially averaged growth rate for the observation window of a given shot. For each of the 12 temperature map images in a shot sequence, a 10×1 -pixel binning algorithm was applied in the perpendicular-to-current direction (vertical on the images) to locally average the signal, reducing each original 860×1000 -pixel image to 86 horizontal

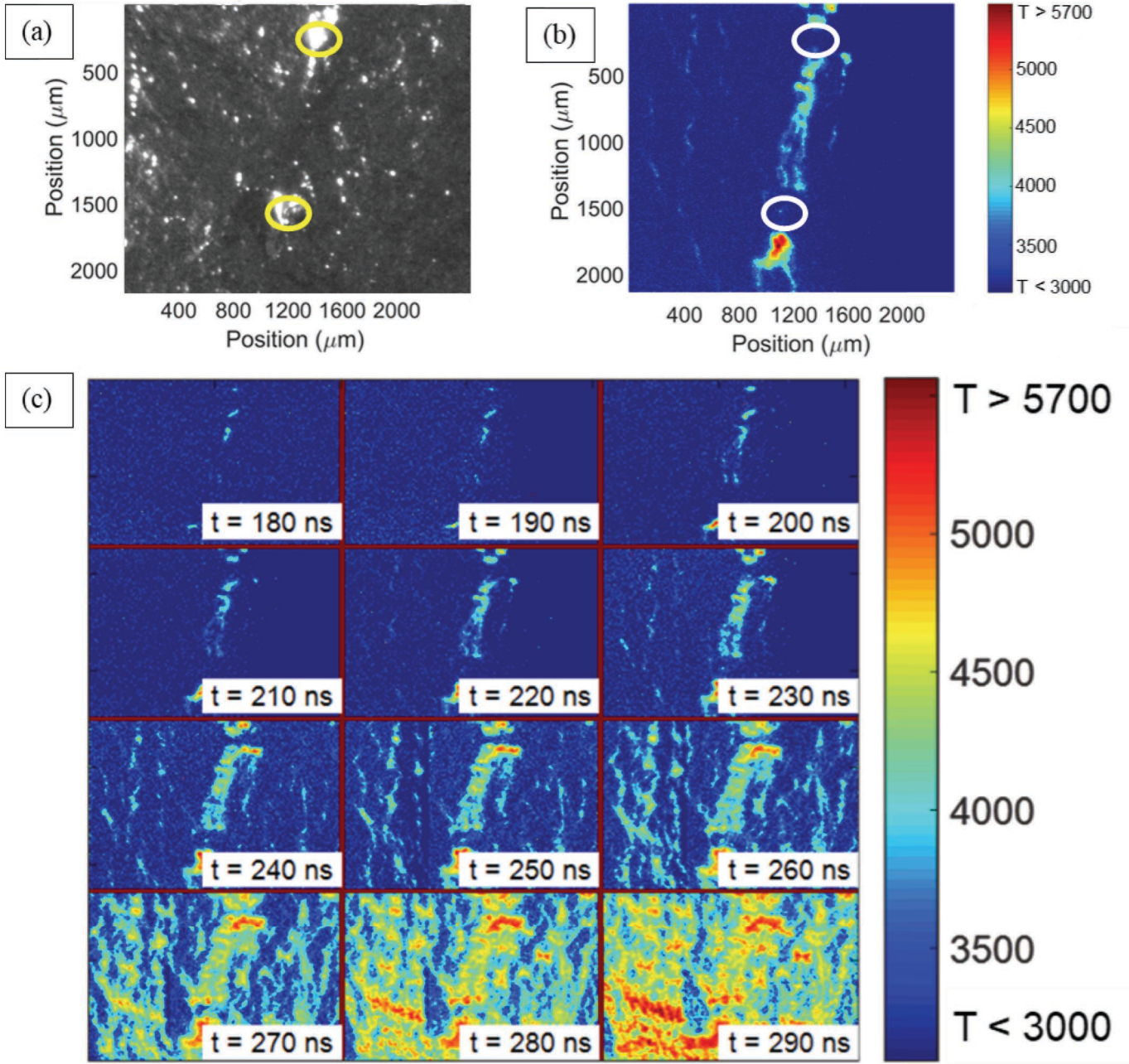


Fig. 8. (a) Pre-shot image showing two holes (highlighted in yellow circles) with diameter $\sim 50 \mu\text{m}$ punctured in a $400 \text{ nm} \times 1.0 \text{ cm} \times 0.9 \text{ cm}$ foil to approximate large inclusions of high resistivity impurities. (b) Temperature plot generated from image taken at 220 ns showing ETI preferentially forming along the line between the holes (locations highlighted with the white circles) before growing elsewhere along the foil (c) Full shot temperature sequence. Note the seeded striation begins to grow $\sim 50 \text{ ns}$ prior to random striations. All image sizes are $2.5 \text{ mm} \times 2.15 \text{ mm}$; current flows from left to right. Temperatures above the noise floor represent a lower bound due to the $\epsilon = 1$ assumption with uncertainty on this lower bound of $\pm 5\%$.

lineouts. This binning process reduces the impact of individual saturated pixels that appeared in small numbers on all camera images due to noise while still preserving resolution in the parallel-to-current (horizontal) direction. Two example lineouts from a $800 \text{ nm} \times 0.7 \text{ cm} \times 0.9 \text{ cm}$ foil are shown in Fig. 9(a) and (b).

Of the 102 total shots, 13 were identified with all 12 images taking place during the growing temperature perturbation phase on all frames (i.e. no all-black or all-saturated frames in the sequence) and selected for growth rate analysis. As described in Section IV, the unperturbed bulk temperature was assumed to be T_{vapor} , 2743 K. To measure growth rate, temperature

peaks are extracted from lineouts, and the measured, lower-bound temperature of each peak T_{peak} is plotted as a function of time over the 12 frames. The growth rate for a given peak is determined by fitting a linear function to the natural logarithm of δT , where $\delta T(t) = T_{\text{peak}}(t) - T_{\text{vapor}}$ (see Fig. 9(c) and (d)). All values of growth rate calculated in this manner for a given shot are averaged to give a characteristic growth rate for that shot (downselected to exclude peaks that saturate the camera on later frames; at a minimum 25 growth rates were averaged per shot). Uncertainty on each growth rate lineout σ_{growth} is taken to be the 95% confidence interval on the fit of $\ln(\delta T)$ vs. T ,

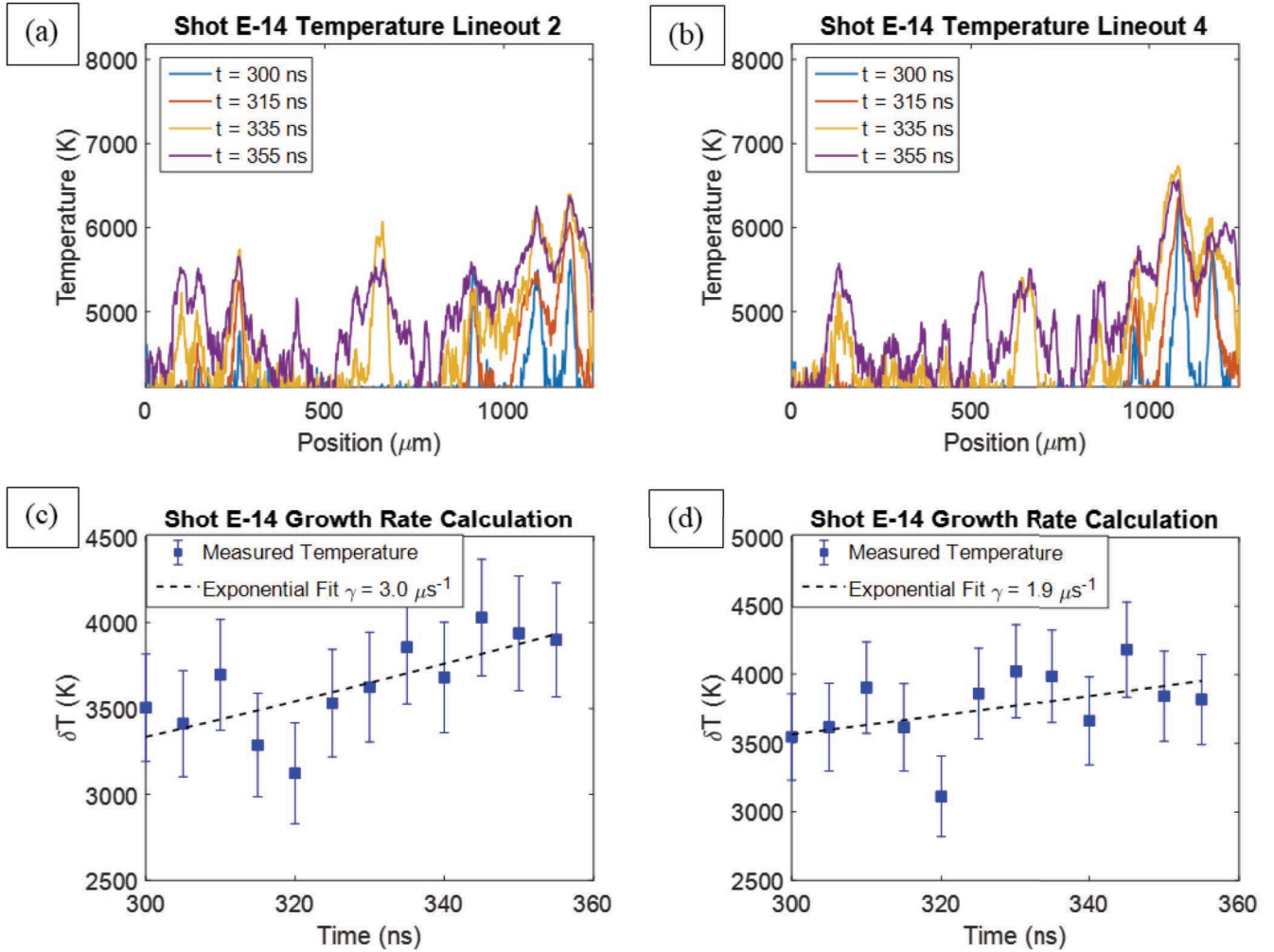


Fig. 9. (a) and (b) Example temperature lineouts (2 lineouts of the total 86 obtained from the shot; 4 of the available 12 frames are shown per lineout) from an 800 nm x 0.7 cm x 0.9 cm foil ablation. The y-axes are truncated at 4000 K because temperatures below this value cannot be resolved for the specified magnification and exposure time. (c) and (d) Corresponding growth rate plots from the highest temperature points on each temperature lineout. Error bars represent the frame-to-frame $\pm 5\%$ response error of the camera.

with σ_{growth} represented as a fraction of the measured growth rate. The total uncertainty in growth rate for a given shot is then approximated by $\Sigma_n |\sigma_{growth}| / (n\sqrt{n})$, where n is the number of lineouts used in the averaging process.

The linear theoretical growth rate of striation-form ETI given by (4) depends on both time and temperature. In addition, η , c_v , κ , and ρ vary as a function of temperature within a single phase and as deposited energy during the constant-temperature vaporization process. To determine the time-dependent theoretical growth rate, the average temperature of the foil and enthalpy change from room temperature during the vaporization phase change were tracked as a function of time for each shot using the input power measurements. Values of η , c_v , κ , and ρ are interpolated as functions of temperature and/or enthalpy from available data in the literature [21-26], under the assumption that these values are weak functions of pressure. Theoretical ETI growth rates are then calculated, as functions of time, for wavenumber k ranging from $k = 10^6 \text{ m}^{-1}$ (near the minimum experimentally resolvable wavelength) to $k = 10^4 \text{ m}^{-1}$ (a large enough wavelength such that $\gamma > 0.99\gamma_{max}$), using the input energy measured for each shot. The measured

temporally and spatially averaged growth rate is then compared to theoretical ETI growth rates over the observation window. Fig. 10 shows an example growth rate comparison, with the measured average growth rate indicated by the dashed black line; the calculated, time-dependent growth rates for various ETI wavelengths indicated by the colored curves; and the observation window of the 12-frame ICCD indicated by the shaded box.

Fig. 10 shows measured average growth rates in reasonably good agreement with calculated ETI growth rates in the range of $\lambda = 30 \text{ μm}$, the smallest experimentally observed growing wavelength across all shots, to $\lambda = 628 \text{ μm}$, a perturbation sufficiently large to grow approximately as γ_{max} , ignoring the growth rate reduction due to thermal conductivity in (4). Generally, measured average growth rates were found to fall within or close to the range bounded by the calculated growth rates γ_{30} (the growth rate for $\lambda = 30 \text{ μm}$) and γ_{max} . The growth rate results from all 13 analyzed shots are summarized in Fig. 11.

From Fig. 11, measured growth rates from five out of the thirteen shots fall in the window bounded by γ_{30} and γ_{max} , and

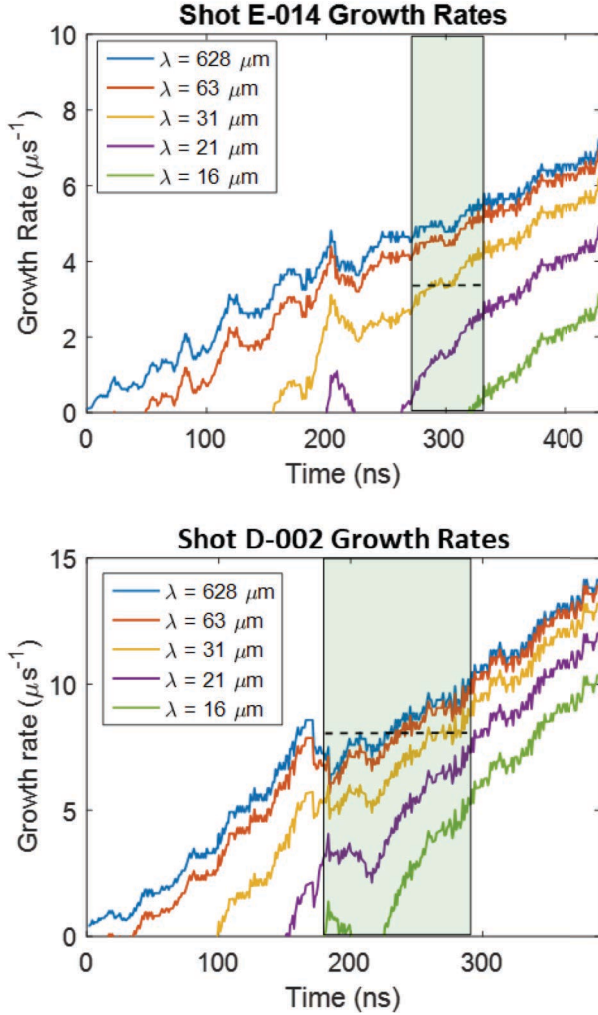


Fig. 10. Example time-dependent growth rates $\gamma(t, T, k)$ calculated from (4) with the imaging window indicated as a shaded box. The measured average growth rate is shown as a dashed horizontal line to compare with the theoretical values. The blue (top) curve is approximately indicative of γ_{max} as its corresponding wavelength is two orders of magnitude greater than λ_{min} .

the remaining measured growth rates fall within 50% of these theoretical upper and lower bounds. It is noteworthy that $\delta T/T_{vapor}$ exceeded unity for most of these experiments, so it is somewhat surprising that the experimental data shows a degree of quantitative agreement with linear theory. This agreement is even more remarkable when considering 1) the sources of error, which include the $\pm 27\%$ error on current density and $\pm 5\%$ error on the camera response; and 2) the assumptions that the background aluminum is expansionless and that its properties can be approximated as pressure-independent.

As discussed in Section II, the growth rate γ_{max} of long-wavelength ETI is anticipated to scale with the square of current density; additionally, the growth rate of long-wavelength ETI with zero current density should be zero. Because the majority of observed perturbations had long wavelengths on the order of 100s of μm , measured growth rates are expected to scale approximately quadratically with J . Fig. 12 shows the measured growth rates plotted as a function of current density with a least-squares curve fit to J^2 .

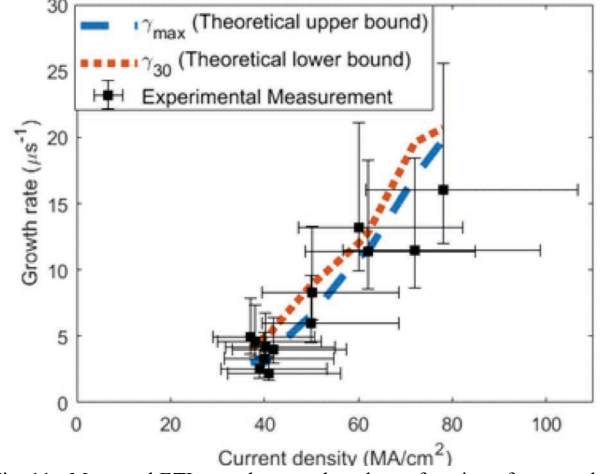


Fig. 11. Measured ETI growth rates plotted as a function of current density. Theoretical growth rates calculated from corresponding current and voltage measurements are shown as dashed lines for γ_{max} (top line) and γ_{30} (bottom line). These curves represent the maximum and minimum growth expected from ETI theory for wavelengths observed on experimental data. Horizontal error bars on the represent the uncertainty in current density due to the uncertainty in foil width and thickness; vertical error bars represent uncertainty from the averaged growth rate fits to experimental δT data.

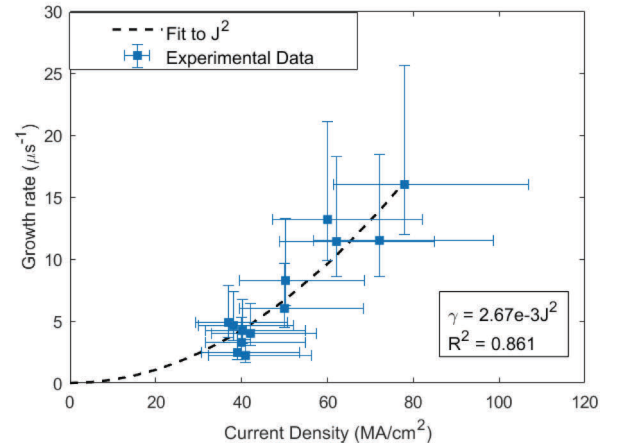


Fig. 12. Experimentally measured growth rates from Table 5.1 plotted against current density. Results are consistent with quadratic dependence on current with zero y-intercept.

The data shown in Fig. 12 are reasonably well characterized by a quadratic dependence on J^2 . The least-squares best fit proportionality constant was found to be $2.7 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$, with a 95% confidence interval of $1.1 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$ to $4.3 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$. This is consistent with the theoretically predicted value, $3.8 \times 10^{-17} \text{ m}^4/(\text{A}^2 \cdot \text{s})$, which is the ratio $(\partial \eta / \partial T) / (\rho c_v)$ for liquid aluminum at the vaporization temperature [21-26]. The consistency between experimental measurements and theoretical prediction demonstrated in Figs. 10, 11, and 12 provides significant evidence that the growing temperature perturbations observed on the ablating foils are in fact manifestations of the striation form of ETI.

VI. CONCLUSION

Pulsed power ablations of thin metallic foils were carried out to investigate the growth of ETI over a range of current densities. A temperature diagnostic was developed using a 12-

frame ultrafast ICCD to provide time-resolved measurements of temperature perturbations on the foil surfaces. The experimentally observed temperature perturbations exhibited four key phenomena consistent with the theoretical understanding of ETI: 1) temperature perturbations in the perpendicular-to-current orientation self-correlated and grew exponentially with rates in good agreement with theoretical striation-form ETI growth; 2) the growth rate of large wavelengths scaled approximately as the square of current density; 3) the seeding of perturbations depended more strongly on high-resistivity inclusions than deformation of the foil surface; and 4) temperature perturbations transitioned from a perpendicular-to-current orientation to a parallel-to-current orientation at times much later than the start of visible light emission. These findings agree well with previous experimental study of the electrothermal instability [13, 28] and provide strong experimental evidence of the growth of striation-form ETI on pulsed power ablations of electrically thin, initially solid metal loads. Experimental validation of ETI theory motivates ongoing campaigns to reduce ETI on pulsed power ablation experiments and thereby delay the formation of destructive plasma instabilities.

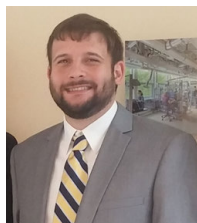
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