# Study and Design of a Fast Start-Up Crystal Oscillator Using Precise Dithered Injection and Active Inductance

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Abstract—This paper presents a theoretical study and design of two techniques used to reduce start-up time  $(T_S)$  and energy  $(E_S)$  of Pierce crystal oscillator (XO). An analytical study of precise injection on a crystal resonator is introduced, and based on this paper, a relaxation oscillator with a dithered frequency is designed. Next, a study of negative resistance of XO's active circuitry and a method to boost its value beyond the limit set by a crystal static capacitor are presented. A gyrator-C active inductor with high linearity is developed to accelerate the start-up process by boosting the negative resistance. A prototype integrating these techniques is fabricated in a 180-nm CMOS process and shows a significant improvement compared with the prior art. Specifically,  $T_S$  and  $E_S$  are reduced by 102.7× and 2.9×, compared with the XO start-up with no assisting circuitry, to 18  $\mu$ s and 114.5 nJ for a 48-MHz XO across a temperature range of -40 °C to 90 °C. The measured steady-state power and the phase noise of the XO are 180 µW and -135 dBc/Hz at 1-kHz offset.

Index Terms—Active inductor (AI), gyrator-C, motional current, negative resistance, precise injection, quartz crystal, relaxation oscillator (RXO), start-up time, static capacitor.

#### I. Introduction

THE advent of emerging fields, such as body area networks I for health care applications and massive wireless sensing for Internet of Things, demands ultra-low-power electronics to enhance the battery lifetime. A common method of reducing the power consumption, increasing the battery lifetime, and, thus eventually, enabling battery-less systems is to power cycle the whole system and operate in an intermittent fashion [1]-[3]. The wireless sensor nodes primarily constitute a transceiver for communication, an analog-to-digital converter for data conversion, and a back-end processing block, all required to be low power. Reference frequency synthesis, digital clock timebase, and the carrier frequency generations in these blocks are often realized using a crystal oscillator (XO) [4]. An XO commonly employs a Pierce structure, as shown in Fig. 1(a), due to its many advantages, such as low-power consumption, low component count, ease of

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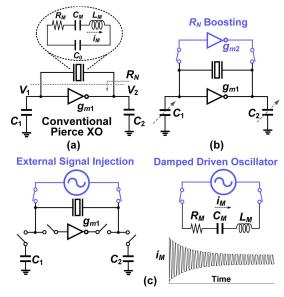


Fig. 1. (a) Pierce XO. (b) Boosting negative resistance by modifying capacitors and amplifier's gain. (c) Kick-starting the oscillator using an external periodic source and oscillation amplitude behavior under injection.

design, and low phase noise. The start-up time  $T_S$  of an XO (few milliseconds for a megahertz (MHz) crystal) constitutes a bottleneck in the effectiveness and performance of power cycling schemes, either limiting the system latency or raising the standby power.

One approach to reduce standby power consumption overhead is to minimize the XO's power dissipation. In [5], a stacked amplifier was used as the XO's active network to increase the inverter's effective transconductance for a given bias current, thus lowering the power dissipation to 19  $\mu$ W. Reference [6] implemented automatic self-power gating (ASPG) and multi-stage inverter for negative resistance (MINR) to intermittently power-off and reduce the short circuit current in the oscillator's inverter, thus lowering the power to as low as 9.2  $\mu$ W. A more efficient way, which further decreases the sleep-mode power of the system, is to duty-cycle the XO and to allow it to be active only when needed. This approach, however, would need a mechanism to quickly start and stabilize the XO before the rest of the system is awakened. Therefore, techniques to reduce  $T_S$  with minimal energy overhead are of great interest.

A commonly used approach to lower  $T_S$  is shown in Fig. 1(b), which aims at increasing the active circuitry's negative resistance  $R_N$  by modifying the inverting amplifier's  $g_m$  or the capacitors  $C_1$  and  $C_2$ . Reference [7] describes a method in which a minimum load capacitor  $C_L$  [defined as  $C_L = C_0 + C_1 C_2 / (C_1 + C_2)$ ] is applied to the oscillator during start-up, and once a stable oscillation is detected, a second capacitor bank is switched in to adjust the frequency and reach the desired steady state. Reference [8] implemented a similar concept to reduce  $T_S$  as well as start-up energy  $E_S$  by 13.3× and 6.9×, respectively, without the need to use a start-up sequence. However, this approach causes the oscillation frequency to be pulled away from the target, which results in an increase in  $T_S$ , defined as the time taken for XO to settle within a specified frequency error (e.g., ±20 ppm in [8]). Reference [9] presents two techniques to reduce  $T_S$ , namely, decreasing  $C_1/C_2$  and increasing the current of the inverting amplifier during start-up. Another approach pursued by [10] and [11] is to increase  $C_L$  to enhance maximum achievable  $R_N$ . To be effective, this approach should be accompanied by increasing the amplifier's gain concurrently, which, in turn, increases  $E_S$ . If being implemented as a highgain multi-stage circuit [6], [10], [12], the inverting amplifier can introduce a significant phase shift, which varies over process, voltage, and temperature (PVT). This phase shift may pull the XO frequency to even below the crystal's series resonance frequency  $\omega_S$  so as to make the overall phase shift around the loop 360°, compromising the XO frequency stability and accuracy. Furthermore, under this condition, the crystal no longer behaves inductively and is forced to oscillate below the frequency that it is calibrated for. Due to this problem, [12] proposed to use two different amplifiers, one for start-up and another for steady-state operation.

Among several existing techniques, external signal injection is widely used to minimize  $T_S$ . For this technique to be effective though, the injected signal frequency should be close to the XO resonance frequency (e.g., within  $\pm 0.25\%$ ). Several implementations of this method have been proposed, each with various degrees of success. Reference [13] proposes a calibration system where proper frequency setting for a tunable oscillator is determined to help quickly start the XO by precise signal injection. A similar method was presented in [14], where a ring oscillator with a calibration circuitry injects a precise signal to reduce  $T_S$  of a 32-MHz Pierce XO to 50  $\mu$ s. Reference [15] introduced a dithering technique to compensate for the frequency variations over process and temperature and reduced  $T_S$  of a 24-MHz XO to 64  $\mu$ s. For a PVT-robust injection, [16] proposed a chirp injection (CI) mechanism to sweep the injection frequency around the crystal's resonance frequency. Another CI technique was proposed in [12] to reduce the area occupied by the chirp signal generator. To improve the signal injection accuracy, [17] proposed a three-step initialization sequence. In the first step, a coarsely tuned ( $\pm 0.5\%$  frequency accuracy) ring oscillator increases the XO amplitude to 0.2 V. In the second step, a phase-locked loop (PLL) aligns the ring oscillator frequency to within 20 ppm of the XO resonance frequency and, finally, applies the injection again in the last step.  $T_S$  is reduced to 19  $\mu$ s, a 31.5×

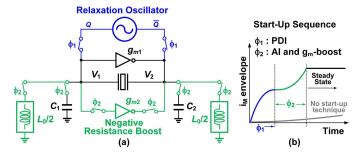


Fig. 2. (a) Proposed implementation of the fast-starting XO. (b) Oscillation amplitude growth with the start-up aids and without them.

improvement compared with a normal start-up condition. In order to continuously drive the crystal with an external oscillator, [18] proposed a synchronized signal injection technique. Since there is a frequency offset between the injection signal and the crystal resonance, the phase difference between the two accumulates over time, which results in the injection signal counteracting the crystal resonance. The underlying idea in [18] is to realign the phase of the injection signal and the crystal resonance periodically to avoid this phase accumulation. For a 0.75-V steady-state differential amplitude (0.37 V single-ended),  $T_S = 23 \mu s$  and  $E_S = 20.2 \text{ nJ}$ . A precisely timed injection method was presented in [19], and an analysis was provided to determine the optimum duration of injection. It also implemented a voltage regulation loop to limit the oscillation amplitude to  $\approx 0.2 \text{ V}$  (at the cost of higher phase noise) and achieved a  $T_S$  value of 2  $\mu$ s. Such small amplitude can easily be built-up through a signal injection over a short time. Furthermore, the regulation loop itself assists the oscillation by providing a larger bias current during the start-up transient and a smaller one in the steady state.

#### II. BACKGROUND AND THE PROPOSED IDEAS

It is well known that the envelope of the XO motional current  $i_M$  is a direct indication of the oscillation behavior. In this paper, a rigorous study of signal injection for XO  $T_S$  reduction is presented, and the conditions leading to an optimal start-up behavior are derived. It will be proven that precise injection with exactly the same frequency as the crystal's series resonance frequency provides the fastest oscillation start-up. It will also be shown that, in reality, due to non-zero injection frequency inaccuracy, this mechanism alone cannot energize the crystal to skip the regenerative process interval. Therefore, another mechanism is needed to minimize this interval and thus lower  $T_S$  close to its theoretical lower limit.

In this paper, two techniques are proposed to realize this thought process. Fig. 2(a) shows the schematic of the proposed ideas, namely a relaxation oscillator (RXO) as an injection signal source and an active inductor (AI). The initialization start-up sequence and a symbolic behavior of oscillation amplitude growth are shown in Fig. 2(b). In the first phase  $\phi_1$  of the start-up sequence, RXO rapidly increases the oscillation amplitude, equivalent to an increase of the start-up initial condition for the XO. In the second phase  $\phi_2$ , RXO is detached, while the AI,  $C_1$ ,  $C_2$ , and an additional amplifier are switched in. In the

steady state, only  $C_1$  and  $C_2$  will remain connected to sustain the oscillation.

To be able to achieve a significant reduction in  $T_S$  and  $E_S$ , a deep understanding of the fundamentals of crystal and XO operation is necessary.

The rest of this paper is organized as follows. Section III presents a transient analysis in the presence of a periodic injection signal and studies parameters affecting  $T_S$ . It also covers the design and implementation of the RXO. Section IV illustrates the AI method to boost  $R_N$  and elaborates the design tradeoffs and considerations for robust operation of the AI leading to the improvement of the XO start-up time. Section V discusses the measurements of the fabricated XO and its start-up assisting circuitry, and finally, Section VI concludes this paper.

#### III. PRECISE DITHERED SIGNAL INJECTION

Consider Fig. 1(c), demonstrating an external signal injection mechanism for a Pierce XO and  $i_M$  behavior under injection. A differential periodic square signal is generated by an external oscillator (e.g., a ring or an RC oscillator) and then is buffered and applied to the crystal. Since a crystal resonator exhibits ultra-high quality factor (~10<sup>6</sup>) and very narrow bandwidth, it heavily attenuates any applied signal with frequencies not matching its resonance frequency. Thus, only the fundamental component is considered in the Fourier series expansion of the applied signal, while any phase noise around this tone is omitted. We assume that zero initial conditions for crystal only analyze the forced response to a periodic square signal applied at time t = 0. This is a valid assumption since, in practice, the initial condition is determined by the oscillator thermal noise. Non-zero initial conditions just complicate the analysis without adding much circuit insights.

## A. Problem Statement: Damped Driven Oscillator

The characteristic differential equation for a crystal resonator excited by a periodic voltage source (i.e., damped driven oscillator), as shown in Fig. 1(c), for  $t \ge 0$  is

$$v(t) = \frac{4V_{\rm DD}}{\pi} \sin \omega_{\rm inj} t = L_M \frac{di_M}{dt} + R_M i_M + \frac{1}{C_M} \int_0^t i_M d\tau$$
(1)

where  $\omega_{\text{inj}}$  is the injection frequency.  $L_M$ ,  $R_M$ , and  $C_M$  are the motional inductor, resistor, and capacitor of the crystal, respectively. With zero initial conditions, taking the derivative of (1) results in

$$\frac{4V_{\rm DD}\omega_{\rm inj}}{\pi L_M}\cos\omega_{\rm inj}t = \frac{d^2i_M}{dt^2} + 2\alpha\frac{di_M}{dt} + \omega_S^2i_M \tag{2}$$

where  $\alpha = R_M/2L_M$  and  $\omega_S = 1/\sqrt{L_M C_M}$ . Taking the Laplace transform and then using its convolution property,  $i_M$  is derived as

$$i_{M}(t) = \frac{4V_{\text{DD}}\omega_{\text{inj}}}{\pi L_{M}\omega_{d}} \int_{0}^{t} e^{-\alpha(t-x)} \sin \omega_{d}(t-x) \cos \omega_{\text{inj}} x \ dx$$
(3)

where  $\omega_d = (\omega_S^2 - \alpha^2)^{1/2}$  is the damped natural frequency. Note that for crystal resonators,  $\alpha \ll \omega_S$ , and hence,  $\omega_d \simeq \omega_S$ . Using trigonometric identities, the integration in (3) is expanded, that is

$$\begin{split} i_M(t) &= \frac{2V_{\text{DD}}\omega_{\text{inj}}}{\pi L_M \omega_d} e^{-\alpha t} \sin \omega_d t \\ &\times \left[ \int_0^t e^{\alpha x} \cos(\omega_d - \omega_{\text{inj}}) x \ dx - \int_0^t e^{\alpha x} \cos(\omega_d + \omega_{\text{inj}}) x \ dx \right] \\ &\quad - \frac{2V_{\text{DD}}\omega_{\text{inj}}}{\pi L_M \omega_d} e^{-\alpha t} \cos \omega_d t \\ &\quad \times \left[ \int_0^t e^{\alpha x} \sin(\omega_d - \omega_{\text{inj}}) x \ dx - \int_0^t e^{\alpha x} \sin(\omega_d + \omega_{\text{inj}}) x \ dx \right]. \end{split}$$

The integrals in (4) with sum frequency components  $\omega_d + \omega_{\rm inj}$  are contributing negligibly to  $i_M(t)$  and are thus ignored. If evaluated for an ideal case of  $\omega_d = \omega_{\rm inj}$  for which the crystal amplitude undergoes its fastest growth, (5) is readily derived

$$i_M(t) \simeq i_{M,\text{env}}(t) \sin \omega_d t$$
 (5)

where  $i_{M,\text{env}}(t)$  denotes the envelope of  $i_M(t)$  and is calculated to be

$$i_{M,\text{env}}(t) = \frac{2V_{\text{DD}}}{\pi L_M \alpha} (1 - e^{-\alpha t}) = \frac{4V_{\text{DD}}}{\pi R_M} (1 - e^{-\alpha t}).$$
 (6)

 $T_S$  is defined as the time when  $i_{M,\text{env}}(t) = 0.9|I_{M,\text{SS}}|$ , where  $I_{M,\text{SS}}$  is the steady-state magnitude of  $i_M$ . It has been shown that at this time instance, the oscillation frequency has also settled within the required accuracy for most communication standards [16], [19]. The minimum achievable start-up time  $T_{S,\text{min}}$  in the XO is thus obtained from (6) and is equal to

$$T_{S,\text{min}} = \frac{2L_M}{R_M} \ln \left( 1 - \frac{\pi R_M}{4V_{\text{DD}}} \times 0.9 |I_{M,\text{SS}}| \right)^{-1}.$$
 (7)

It is instructive to acquire a quantitative insight into  $T_{S,min}$  using (7) for the widely used Pierce XO. As demonstrated in [20], in steady state

$$|I_{M,SS}| \simeq 0.5 \left(1 + \frac{C_0}{C_S}\right) \omega_{\rm osc} C_1 |V_1| \tag{8}$$

where  $\omega_{\rm osc} = \omega_S (1 + C_M/2C_L)$  is the oscillation frequency,  $V_1$  denotes the input voltage of the inverting amplifier, and  $C_S$  is the series combination of  $C_1$  and  $C_2$  in Fig. 1(a). For a sample 48-MHz crystal with parameters  $C_M = 4$  fF,  $L_M = 2.749$  mH,  $R_M = 15$   $\Omega$ ,  $C_L = 8$  pF,  $C_0 = 2$  pF, and  $|V_1| = V_{\rm DD}$ ,  $T_{S,\rm min}$  is calculated to be 11.9  $\mu$ s.

Now, assuming an injection frequency inaccuracy of  $\Delta \omega = \omega_d - \omega_{\rm inj}, i_M(t)$  becomes

$$i_{M}(t) = \frac{2V_{\text{DD}}\omega_{\text{inj}}}{\pi L_{M}\omega_{d}(\alpha^{2} + \Delta\omega^{2})} \sin \omega_{d}t$$

$$\times \left[\alpha \cos \Delta\omega t + \Delta\omega \sin \Delta\omega t - \alpha e^{-\alpha t}\right]$$

$$-\frac{2V_{\text{DD}}\omega_{\text{inj}}}{\pi L_{M}\omega_{d}(\alpha^{2} + \Delta\omega^{2})} \cos \omega_{d}t$$

$$\times \left[\alpha \sin \Delta\omega t - \Delta\omega \cos \Delta\omega t + \Delta\omega e^{-\alpha t}\right]. \tag{9}$$

In practice, even for an integrated oscillator carefully designed to produce a precise injection frequency, it is still difficult for  $\omega_{\rm inj}$  to be within  $\pm 0.1\%$  of  $\omega_d$  across PVT variations (e.g., for typical crystals operating in the MHz range,  $\alpha \sim 1$ –10 kHz, while  $\Delta\omega \sim 0.1$ –1 Mrad/s); hence,  $\alpha \ll \Delta\omega$ . Therefore, the expression in (9) is reduced to

$$i_M(t) \simeq \frac{2V_{\rm DD}}{\pi L_M \Delta \omega} \left( 1 - \frac{\Delta \omega}{\omega_d} \right) \left[ \sin \omega_d t \sin \Delta \omega t + \cos \omega_d t (\cos \Delta \omega t - e^{-\alpha t}) \right].$$
 (10)

#### B. Analysis of the Motional Current's Envelope

To calculate the envelope of  $i_M(t)$  in (10), Hilbert transform is invoked. For an arbitrary waveform v(t), a complex signal  $z(t) = v(t) + j\hat{v}(t)$  is defined, where

$$\hat{v}(t) \equiv H[v(t)] = v(t) * \frac{1}{t} = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{v(\lambda)}{t - \lambda} d\lambda$$
 (11)

is the Hilbert transform of v(t). It is proved that the magnitude of z(t) is the envelope of v(t), i.e.,  $v_{\text{env}}(t) = |z(t)| = (v^2(t) + \hat{v}^2(t))^{1/2}$ . For clarity, (10) is rewritten as

$$i_M(t) = K[x(t)\cos\omega_d t + y(t)\sin\omega_d t] \tag{12}$$

where

$$K = \frac{2V_{\text{DD}}}{\pi L_M \Delta \omega} \left( 1 - \frac{\Delta \omega}{\omega_d} \right)$$
$$x(t) = \cos \Delta \omega t - e^{-\alpha t}, \quad y(t) = \sin \Delta \omega t. \tag{13}$$

 $\hat{i}_M(t)$  is derived as

$$\hat{i}_M(t) = K[x(t)\sin\omega_d t - y(t)\cos\omega_d t]. \tag{14}$$

The envelope of  $i_M(t)$  is, thus, readily calculated from (12) and (14)

$$i_{M,\text{env}}(t) = K\sqrt{x^2(t) + y^2(t)} = \frac{2V_{\text{DD}}}{\pi L_M \Delta \omega} \left(1 - \frac{\Delta \omega}{\omega_d}\right) \times \sqrt{1 + e^{-2\alpha t} - 2\cos \Delta \omega t \ e^{-\alpha t}}.$$
 (15)

A consequence of the condition  $\alpha \ll \Delta \omega$  is that it is unlikely that the injection oscillator alone can build up the oscillation amplitude of the Pierce XO all the way to its steady state, unless the steady-state amplitude is made small (e.g., <0.2 $V_{\rm DD}$ , as was done in [19] and [21]). Therefore,  $i_{M,\rm env}(t)$  after injection is smaller than  $I_{M,\rm SS}$ , and other techniques need to complement the signal injection, as was carried out by [16] and [22]. Following the excitation period, the crystal is detached from the external source and connected to the inverting amplifier.

Fig. 3 compares the time-domain variation of  $i_{M,env}(t)$  obtained from both simulation and calculation [see (15)] of the crystal resonator under injection for two values of  $\Delta \omega = 0.1, 0.3$  Mrad/s, validating the proposed analysis. For comparison, the  $i_{M,env}(t)$  variation with injection time obtained from analysis in [19] (for the same circuit conditions and the same crystal model) is overlaid in Fig. 3. Reference [19] approximates the frequency response of crystal with an impulse function, only a valid approximation for small  $T_{inj}$ . On the contrary, the proposed dynamic analysis of the crystal's motional current is based on the characteristic

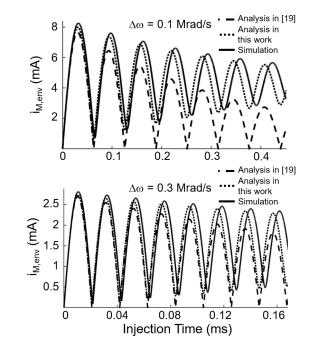


Fig. 3. Envelope of  $i_M$  for  $\Delta \omega = 0.1$  and 0.3 Mrad/s.

differential equation of the crystal with no assumption about its frequency- and/or time-domain responses.

For  $T_S$  to get sufficiently close to  $T_{S, \min}$ , the injection should cease when  $i_{M, \text{env}}(t)$  in (15) is at its maximum (see Fig. 3). This optimum injection time  $T_{\text{OPT}}$  is calculated to be  $T_{\text{OPT}} \simeq \pi/\Delta\omega$ . Moreover, the maximum of  $i_{M, \text{env}}(t)$  is

$$i_{M,\text{env}}(t)_{\text{max}} \simeq \frac{4V_{\text{DD}}}{\pi L_M \Delta \omega} \left(1 - \frac{\Delta \omega}{\omega_d}\right).$$
 (16)

It is inferred that for crystals with high Q-factors or injection sources with poor frequency accuracy,  $i_{M,env}(t)$  assumes smaller values for  $t < T_{OPT}$ , an intuitively expected result.

In the case that injection oscillator's frequency is close to  $\omega_d$ , it can be readily proved that so long as  $\Delta\omega < (4C_M/\pi C_L)\omega_{\rm osc}$ , the injection mechanism alone is capable of bringing the oscillation amplitude to its steady state.

## C. Sensitivity to Timing and Injection Frequency Inaccuracies

It was shown in Section III-B that injection should be stopped once  $i_{M,\text{env}}$  reaches its peak value to minimize  $T_S$ . Two phenomena affect  $T_S$ , namely, inaccurate injection frequency  $(\Delta\omega)$  and time  $(T_{\text{inj}})$ . Recall that  $i_{M,\text{env}}(t)$  exhibits a damped sinusoidal characteristic, as shown in Fig. 3. Thus, at the time, when  $i_{M,\text{env}}(t)$  is at maximum, its time-derivative is at minimum, which in turn lowers the impact of injection duration inaccuracy on  $T_S$ . This is in contrast with the injection approach in [19], where the injection is stopped before the envelope reaches its maximum. In case the oscillation amplitude has not reached its steady state at the end of injection period, it will grow exponentially by the amplifier

$$i_M(t) = i_{M,\text{env}}(T_{\text{inj}})e^{(t-T_{\text{inj}})/\tau}u(t-T_{\text{inj}}), \quad \tau = \frac{-2L_M}{R_M + R_N}$$
(17)

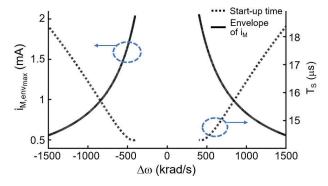


Fig. 4. Effect of injection frequency inaccuracy on a maximum value of  $i_{M,\text{env}}$  and overall  $T_S$ , given injection stops at  $t = T_{\text{OPT}}$  and  $R_N = 50R_M$ .

where u(t) is the unit step function. To derive a closed-form expression for  $T_S$ , we assume that the amplifier remains linear and retains a constant  $R_N$  as the amplitude grows. Combining (8) and (17) yields

$$T_A = \tau \ln \frac{0.9(C_S + C_0)\omega_{\text{osc}}V_{\text{DD}}}{i_{M,\text{env}}(T_{\text{inj}})}, \quad T_S = T_{\text{inj}} + T_A$$
 (18)

where  $T_A$  is the time taken for the amplitude to grow toward its steady state after injection. Combining (16) and (18), the effect of  $\Delta \omega$  on  $T_S$  is calculated as follows:

$$T_S \simeq \frac{\pi}{|\Delta\omega|} + \tau \ln[0.7L_M(C_S + C_0)\omega_{\rm osc}|\Delta\omega|]. \tag{19}$$

Fig. 4 demonstrates the sensitivity of  $T_S$  to  $\Delta \omega$  for the sample 48-MHz quartz crystal based on the quantitative evaluation of (16) and (19). Evaluating the effect of each term of (19) on  $T_S$ , if  $\Delta \omega$  or crystal's Q-factor is small, the first term will be dominant. On the other hand, as the oscillation amplitude becomes large, the active circuitry becomes nonlinear. Therefore,  $\tau$  starts to get larger, and the second term in (19) may dominate  $T_S$ . Similarly, larger Q-factors also increase the contribution of the second term on  $T_S$ . To reduce the effect of  $\Delta \omega$  on  $T_S$ , one can lower  $\tau$  to reduce  $T_S$  and its sensitivity to inaccurate frequency errors.

To evaluate the sensitivity of  $T_S$  to injection duration errors, the injection oscillator is assumed to be sufficiently precise, such that  $\Delta\omega$  falls within  $\pm 0.15\%$  of  $\omega_d$ . The frequency of this oscillator is measured and, if required, calibrated before applying to the XO. Based on (15) and (18), Fig. 5 shows the variation of  $T_S$  with  $\Delta\omega$  for four distinct injection times. For injection frequency errors less than 600 krad/s,  $T_S$  varies from 14.4 to 20.4  $\mu s$ , as  $T_{\rm inj}$  increases from 5 to 8  $\mu s$ . In practice, the phase-noise-induced frequency skirts around  $\omega_{\rm inj}$  pump larger energy within the crystal bandwidth compared with an ideal single-tone injection. As will be illustrated in Section III-E, this can be achieved through dithering, thus resulting in lower  $T_S$  variation. Moreover, as will be seen in Section IV, this sensitivity is further reduced by introducing an AI to the circuit to significantly lower  $\tau$ .

#### D. Interpretation of the Analysis

From the aforementioned equations, a number of observations are made as follows:

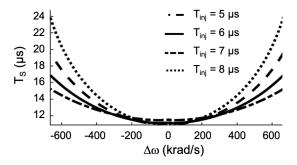


Fig. 5. Effect of injection timing inaccuracy on overall  $T_S$  for the sample crystal parameters.  $R_N$  is assumed to be  $50R_M$ .

- 1)  $i_{M,\text{env}}(t)_{\text{max}}$  can reach twice the final value under continuous injection (steady-state value).
- 2) A smaller  $\Delta \omega$  value results in larger  $i_{M,\text{env}}(t)_{\text{max}}$ ,  $T_{\text{OPT}}$ , and  $i_{M,\text{env}}(t)$  during the start-up interval  $0 < t < T_{\text{OPT}}$ .
- 3) To the first order,  $T_{OPT}$  is only a function of injection signal accuracy and not the crystal properties. In actual implementations,  $\Delta \omega$  is larger for crystals with higher operating frequencies. This is because it becomes increasingly more difficult to guarantee the accuracy of an integrated oscillator as frequency rises.
- 4) It can also be shown that smaller  $\Delta \omega$  value leads to larger local minimums for  $i_{M,env}(t)$ , an effect not predicted in [19] (see Fig. 3).

#### E. Relaxation Oscillator Implementation

Among various candidates to create injection signal, ring oscillators have been used extensively, providing features, such as fast turn-on time, small area and power dissipation at the cost of large PVT susceptibility, and low-frequency precision. Alternatively, this paper employs an RXO, which provides a more precise injection, as its frequency depends on an easily tunable RC time constant instead of transistor parameters. A modified version of the architecture in [23] is implemented at 48 MHz while maintaining the performance across PVT (see Fig. 6). To account for the crystal's ultrahigh Q, the RXO frequency  $\omega_{\rm ini}$  is modulated by toggling its capacitance  $C_2$  between 400 and 415 fF through an internal feedback, as shown in Fig. 6. Thus,  $\omega_{\text{inj}}$  alters by  $\pm 0.25\%$ , slightly spreading the injection signal power spectrum over a wider frequency range and raising the phase noise. This ensures that the RXO contains enough energy across the crystal bandwidth to limit  $T_S$  variation over temperature, resulting in a robust start-up behavior. As opposed to [15] where a relatively inaccurate ring oscillator was used, higher frequency accuracy of RXO allows for a lower dithering range of  $\pm 0.25\%$ . To reduce RXO frequency variation due to PVT, reference voltage  $V_{\text{ref}}$  is generated by a resistive voltage division ratio. Series poly and diffusion resistors with complementary temperature coefficients are employed to generate  $V_{\rm ref}$ , thereby compensating for the RXO frequency variation due to temperature across process corners [23]. These resistors employ 5 bits of coarse and 4 bits of fine-tuning, which translates to a frequency resolution of 40 kHz and a tuning range from 27 to 84 MHz. Due to several percentage-point variations

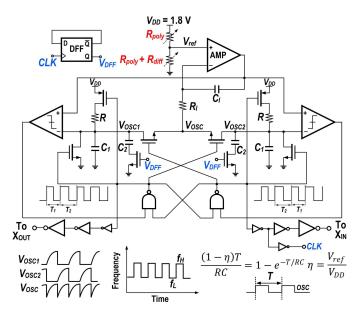


Fig. 6. RXO circuit implementation.

of on-chip resistors and capacitors, a simulation-assisted initial calibration is inevitable for any signal injection technique including the proposed precise dithered injection (PDI) (except for the chirp signal injection where the frequency is swept across a wide range). Measurement of this RXO shows frequency variation within  $\pm 0.15\%$  over -40 °C to 90 °C, significantly better than temperature-compensated ring oscillators. Simulations show  $\pm 0.2\%$  frequency variation across temperature at different process corners. Furthermore, Monte Carlo simulations of both process and mismatch variations show a sigma of 100 kHz (0.21%) in the nominal corner. The RXO and the buffer dissipate 3.6 mW from a 1.8-V supply, a significantly larger value compared with [23] because of higher operation frequency and more stringent specification on its frequency stability, which requires smaller comparators' delays. The power would be significantly lower on an advanced technology node or for smaller target frequency.

#### IV. ACTIVE INDUCTOR

## A. Effects of C<sub>0</sub> on XO Start-Up

The presence of the static capacitance  $C_0$  in the crystal greatly influences the XO behavior [see Fig. 1(a)]. Besides limiting the pull-ability of XO, it lowers the active circuitry's negative resistance according to [20]

$$R_N = \frac{-4g_m C_S^2}{(g_m C_0)^2 + 16\omega^2 C_S^2 C_I^2}. (20)$$

Furthermore, it limits the maximum negative resistance  $R_{N,\text{max}}$  and sets an optimum value of amplifier's  $g_m$  beyond which  $R_N$  will start to decrease (see Fig. 7)

$$R_{N,\text{max}} = \frac{1}{2\omega C_0(1 + C_0/C_S)}, \quad g_{m,\text{opt}} = 4C_S\omega(1 + C_S/C_0).$$
 (21)

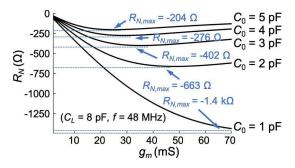


Fig. 7. Negative resistance and its maximum versus amplifier transconductance gain for various  $C_0$  values.

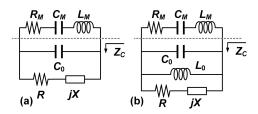


Fig. 8. One-port linear model of the XOs in (a) [12] and (b) this paper.

In addition,  $C_0$  poses a limit on how much  $C_L$  can be lowered to achieve larger  $R_N$  [8], [24]. To address the limitation imposed by  $C_0$ , [12] proposed a dual-mode  $g_m$  scheme, employing one amplifier for start-up  $(A_{XO-3})$  and another one for steady-state  $(A_{XO-1})$  operation.  $A_{XO-3}$  is designed to show an inductive reactance X around the XO nominal operation frequency to counteract  $C_0$ . Starting with Fig. 8(a) that shows a linear model of the XO, the impedance  $Z_C$  seen from the motional branch is derived as

$$Z_C = \frac{R + j(X(1 - C_0X\omega) - R^2C_0\omega)}{(1 - C_0X\omega)^2 + (RC_0\omega)^2}.$$
 (22)

In a conventional design,  $X = -1/C_S\omega$ , and crystal's motional branch is loaded with  $C_S + C_0$ . On the other hand, maximizing the real part of  $Z_C$  for the circuit model in Fig. 8(a) leads to  $X = 1/C_0\omega$ , while its imaginary part becomes  $-1/C_0\omega$ . Therefore, during start-up, when  $A_{XO-3}$  is enabled to boost the negative resistance, crystal's motional branch is effectively loaded with an equivalent capacitor of  $C_0$ , and  $\omega_{osc}$  will shift toward  $\omega_p$ . This frequency drift along with the nonlinearity effects of  $A_{XO-3}$  which was pointed out in [12] increases both amplitude and frequency settling times.

## B. Proposed $R_N$ Boosting Method

Fig. 8(b) shows a simplified linear model for the approach presented in this paper. An inductor is explicitly placed in parallel with the crystal to maximize the real part of  $Z_C$  for the circuit model in Fig. 8(b). Crystal's motional branch is now loaded with

$$Z_C = \frac{Z_{\text{amp}} L_0 s}{L_0 s + Z_{\text{amp}} (1 + L_0 C_0 s^2)}, \quad Z_{\text{amp}} = R + j X$$
 (23)

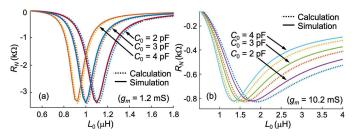


Fig. 9.  $R_N$  at 48 MHz after addition of  $L_0$  for amplifier's transconductance gain of (a) 1.2 and (b) 10.2 mS.

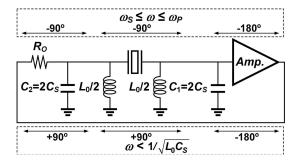


Fig. 10. Simplified phase shift around the loop of Pierce XO at different frequency ranges.

with real and imaginary parts expressed as

$$Re{Z_C} = \frac{RL_0^2\omega^2}{R^2(1 - L_0C_0\omega^2)^2 + (L_0\omega + X(1 - L_0C_0\omega^2))^2}$$
(24)  

$$Im{Z_C} = \frac{R^2L_0\omega(1 - L_0C_0\omega^2) + XL_0\omega(L_0\omega + X(1 - L_0C_0\omega^2))}{R^2(1 - L_0C_0\omega^2)^2 + (L_0\omega + X(1 - L_0C_0\omega^2))^2}.$$
(25)

 $L_0$  boosts the real part of  $Z_C$ , and in contrast to [22], this can be accomplished without imposing any constraints on  $C_S$  value or amplifier's characteristic. More precisely,  $L_0$  reduces the effective static capacitance  $C_{0,\text{eff}} = C_0[(\omega_0/\omega)^2 - 1]$  (where  $\omega_0 = 1/(L_0C_0)^{1/2}$ ), thereby increasing  $R_{N,\text{max}}$ . One may choose to leverage this property to decrease  $C_S$  so as to achieve larger  $R_N$ .

Fig. 9(a) and (b) demonstrates both simulated and calculated  $R_N$  variations with respect to  $L_0$  under three values of  $C_0$  (i.e., 2, 3, and 4 pF) and for two  $g_m$  values (i.e., 1.2 and 10.2 mS) at 48 MHz, where  $L_0$  is assumed to be an ideal inductor. As shown in Fig. 9(a) and (b), the maximum achievable  $R_N$  value is larger for an amplifier with a lower  $g_m$  value. It is also observed that this larger  $R_N$  value requires more precise and linear  $L_0$  over PVT variations, which is challenging to realize in practice. Therefore, to reduce the  $R_N$  sensitivity to  $L_0$  variation,  $g_m$  should be increased [see Fig. 9(b)].

#### C. Design Considerations for Active Inductor Implementation

The addition of  $L_0$  creates the possibility of an unwanted oscillation caused by the resonance through  $L_0$ , the crystal, and the amplifier. A qualitative view is displayed in Fig. 10. The AI is decomposed into two equal parts placed on the

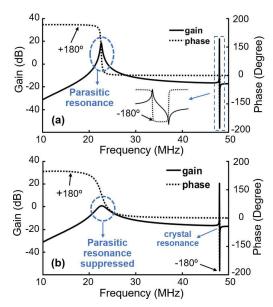


Fig. 11. (a) Tank frequency response after inclusion of  $L_0$  with a quality factor of (a) 83 and (b) 11.

crystal's input and output nodes. For the oscillation to take place, the phase shift across the loop should be  $n \times 360^{\circ}$ , where n is an integer number. Neglecting the AI first, one can identify a 180° phase lag from the amplifier, a phase lag of about 90° from  $R_O - C_2$ , and another 90° phase lag from the crystal  $-C_1$ at  $\omega_{\rm osc} = \omega_S$ , where  $R_O$  is the amplifier output resistance. On the other hand, in the presence of AIs, the resulting passive network and the crystal form a dual-resonance network with two oscillation modes. Besides the oscillation mode at  $\omega_{\rm osc} = \omega_{\rm S}$ , the second oscillation mode is created by the 90° phase leads associated with  $R_O$ – $L_0$  and crystal– $L_0$  and a 180° phase lag from the amplifier. With sufficient gain, the loop may, in fact, oscillate at this parasitic mode. One solution to suppress this mode is to decrease AI's Q-factor; an easily achievable task as the AI's Q-factor is inherently lower than that of monolithic or off-chip components. For better illustration, Fig. 11 shows the open-loop (from the amplifier's output to its input) gain and phase shift simulation of the dualresonance network for two O-factors.

The Al's Q-factor cannot be arbitrarily low because it will increase the XO resistive loss. As a secondary measure to ensure the XO oscillation in its desired mode without compromising on the Al's Q-factor, the injection mechanism raises the XO initial condition around  $\omega_S$  to a value substantially larger than the one provided by thermal noise to the unwanted mode. Once the desired operation takes over, the unwanted mode is automatically eliminated. Another issue is the possibility of operation at one of the crystal's overtones. To prevent this problem, notice that for the feedback to remain positive and oscillation to take place, the reactances at the crystal's input and output in Fig. 10 should be of the same sign (e.g., both negative) at the oscillation frequency of interest. Thus, placing half of  $L_0$  on both sides of the XO guarantees this condition to satisfy at the fundamental frequency.

Finally, when it comes to the XO circuit design, comprehensive transient and spectral simulations have been performed

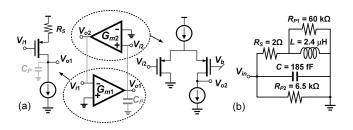


Fig. 12. AI implementation concept. (a) Constructing positive and negative transconductances. (b) Approximate model of the actual design.

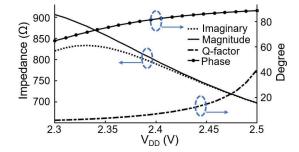


Fig. 13. AI input impedance characteristics at 48 MHz across supply.

to account for all the nonidealities (e.g., amplifier gain and bandwidth, nonlinearity, and frequency response of AI).

#### D. Circuit Implementation

Fig. 12(a) shows the building blocks of the gyrator-C AI. The negative transconductance is a degenerated commonsource stage, and the positive one is a source-coupled structure. These blocks provide large input and output impedances, thereby increasing the Q-factor of the AI. Source degeneration reduces the dependence of  $G_{m1}$  on the input level, reduces the voltage gain at the output (to keep the transistors in saturation), and improves linearity as well as sensitivity to supply variation. Fig. 13 shows the input impedance of AI at 48 MHz and the corresponding Q-factor variations versus  $V_{\rm DD}$ . The reactance varies by  $\pm 9\%$  from 2.3 to 2.5 V, roughly translating to the same variation in the effective inductance. Reduced  $G_{m1}$  value has to be compensated for by increasing  $G_{m2}$ , which leads to higher power consumption (a bias current of 1.5 mA for  $G_{m2}$  cell). Cascode current sources are used for biasing to increase the Q-factor of the structure. The pMOS transistors are used to provide the higher input voltage range since AI and XO are dc-coupled. As shown in Fig. 14, the AI schematic is comprised of two singleended structures operating at 2.4-V supply to accommodate stacked transistors and maintain constant transconductance values (and effective inductance) over a large signal swing. A combination of proportional to absolute temperature (PTAT) and constant- $g_m$  current sources with 1.5- and 1- $\mu$ A tuning resolutions, respectively, is used to bias  $M_1$  with a nominal bias current of 14  $\mu$ A, tune the effective inductance value, and reduce its variation across PVT. The AI operates over a wide frequency range (i.e., up to its self-resonance frequency), virtually accommodating all MHz crystals. The AI is notorious for being noisy and, thus, is usually used in applications

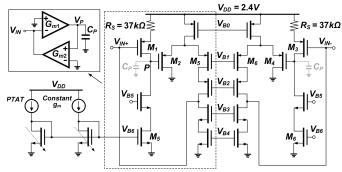


Fig. 14. AI circuit schematic.

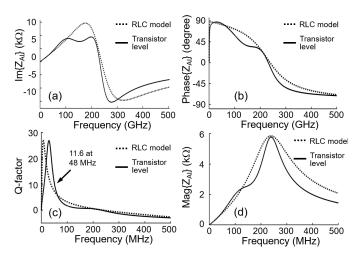


Fig. 15. AI reactance versus frequency and its equivalent circuit model.

with relaxed noise requirements. Nonetheless, for the intended purpose of the XO start-up improvement in this paper, the AI's noise, indeed, helps in reducing  $T_S$ .

Fig. 12(b) shows the synthesized equivalent RLC model for the proposed AI. The equivalent RLC components are readily derived by equating the input impedances of this model and the AI circuit in Fig. 14, that is

$$L \simeq \frac{C_P}{G_{m1}G_{m2}}, R_{P2} = R_{o2}, R_S = \frac{1}{G_{m1}G_{m2}R_{o1}}, C = C_{in}$$

$$R_{P1} = \frac{R_{o1}}{1 + g_{m1}R_S}, G_{m1} = \frac{g_{m1}}{1 + g_{m1}R_S}, G_{m2} = \frac{g_{m2}}{2}$$
 (26)

where  $C_P$  ( $R_{o1}$ ) and  $C_{\rm in}$  ( $R_{o2}$ ) are the capacitances (resistances) at the drain and gate of  $M_1$ , respectively. Fig. 15 shows and compares the frequency response and Q-factor of the AI and its RLC model. The AI has multiple poles, which causes the two responses to deviate at high frequencies. However, the model is sufficiently accurate up to  $\sim$ 0.1 GHz. Fig. 16 shows the simulation results for the negative resistance and its associated boosting ratio across temperature after the addition of the AI. The  $R_N$  values in Fig. 16 are estimated from the rate of oscillation amplitude growth in large-signal transient simulations. These values are smaller in magnitude than the ones predicted in Fig. 9 because of the AI nonlinearity, namely, variation of  $G_{m1}$  and  $G_{m2}$  with signal swing. For a given  $C_0$ , the AI maintains a relatively constant  $R_N$  ( $<\pm9\%$  worst-case variation for  $C_0=2$  pF)

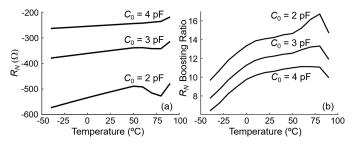


Fig. 16. Simulated temperature variations of (a)  $R_N$  after addition of the AI and (b)  $R_N$  boosting ratio.

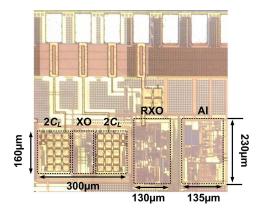


Fig. 17. Die micrograph of the prototype.

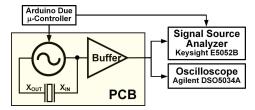


Fig. 18. Measurement setup.

across a -40 °C to 90 °C temperature range, which, thus, keeps the  $T_S$  variations small.

To lower  $T_S$  for crystals with large  $C_0$  values, the duration of the second phase  $\phi_2$  of the start-up sequence in Fig. 2 should increase. According to the simulations of motional current amplitude in the nominal process corner and at room temperature,  $T_S$  increases from 17 to 22  $\mu$ s for  $C_0$  varying from 1 to 6 pF (for the same unloaded crystal Q-factor). The optimal value of  $\phi_2$  can be found using two methods: (1) measuring crystal's  $R_M$  and  $C_0$  and using simulations to find the optimum duration and (2) using an oscillation amplitude detection circuitry to disable  $\phi_2$  when the near-steady-state amplitude is reached. Signal injection duration  $\phi_1$  is independent of  $C_0$  since  $T_{OPT}$  only depends on  $\Delta \omega$ .

### V. MEASUREMENT RESULTS

Fig. 17 shows the die micrograph of the chip fabricated in a 180-nm CMOS process. Occupying an active area of  $0.108 \text{ mm}^2$ , this chip integrated on-chip capacitors including a capacitor bank to create the equivalent 8-pF  $C_L$ . It was wire bonded into a quad-flat no-leads (QFN) package and mounted on an FR-4 PCB. Operating at 48 MHz, the oscillator employs a surface-mount crystal with a  $3.2 \times 2.5 \text{ mm}^2$  package

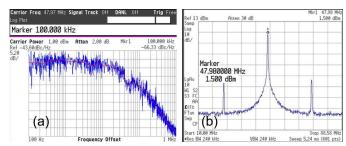


Fig. 19. (a) Measured RXO phase noise and (b) power spectral density.

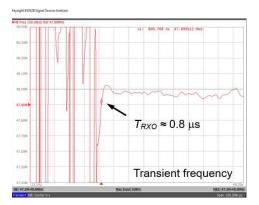


Fig. 20. RXO start-up time.

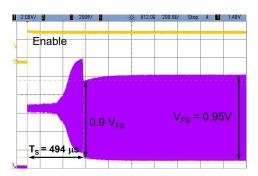


Fig. 21.  $T_S$  improvement using AI only for a large steady-state oscillation amplitude of 0.95 V.

size and dissipates 180  $\mu$ W from a 1-V supply (generated through a low dropout regulator) at steady state. The supply of 1 V was chosen for ease of comparison with prior work. The steady-state power is mainly determined by the supply voltage, operation frequency,  $C_L$ , oscillation amplitude, and crystal properties. It can be minimized through circuit techniques such as stacked-amplifier architecture in [5]; however, this was not the focus of this paper.

The measurement setup is shown in Fig. 18. An off-chip buffer was used to monitor the signal on  $X_{IN}$ , and a microcontroller generates the start-up sequence. The RXO phase noise and the power spectral density are shown in Fig. 19. The RXO phase noise was purposely increased to -66 dBc/Hz at 100-kHz offset through dithering. The two spurs in the RXO's power spectrum are due to the fact that the RXO output is the sum of two half-wave rectified signals. The measured RXO frequency settles within 0.8  $\mu$ s, as shown in Fig. 20, which is dominated by the RXO's integrator pole  $R_IC_I$  in Fig. 6. Although this start-up time is larger than

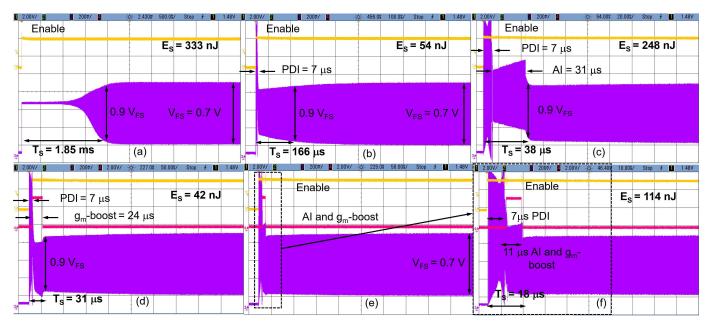


Fig. 22. Start-up behavior of XO with (a) no kick-start technique, (b) PDI only, (c) PDI and AI techniques, (d) PDI and  $g_m$ -boost, and (e) and (f) all techniques combined.

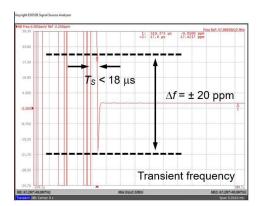


Fig. 23. Settling of XO oscillation frequency.

that of a ring oscillator, it is still negligible compared with the XO's  $T_S$ . Therefore, the accurate and stable frequency provided by the RXO justifies its usage.

Fig. 21 shows the measured voltage at  $X_{\rm IN}$ , demonstrating the oscillation start-up behavior using the AI only. The XO supply is increased to 1.5 V with a steady-state oscillation voltage of 0.95 V and  $T_S=3.96$  ms without the AI. Even at this large voltage swing, the AI is able to reduce  $T_S$  to 0.494 ms, an  $8\times$  improvement ratio.

Fig. 22(a)–(f) shows the strobed voltage  $X_{\rm IN}$  to evaluate  $T_S$  and  $E_S$  using different techniques. In the absence of any start-up assistant technique,  $T_S$  and  $E_S$  of the XO were measured to be 1.85 ms and 333 nJ, respectively. The RXO frequency was calibrated using the trimming poly and diffusion resistors (see Fig. 6), and the injection time is fixed at 7  $\mu$ s. Using the PDI technique,  $T_S$  and  $E_S$  were improved by 11.1× and 6.2× to 166  $\mu$ s and 54 nJ, respectively. Enabling the PDI and the AI without increasing the amplifier's  $g_m$  (i.e., using the same  $g_m$  value as in the steady state),  $T_S$  was reduced to 38  $\mu$ s, inferring  $\approx$ 5× boosting of  $R_N$ . Applying PDI and rising the amplifier's  $g_m$  ( $g_m$ -boost) by switching in  $g_{m2}$  [see Fig. 2(a)],  $T_S$  was



Fig. 24. Measured phase noise.

reduced to 31  $\mu$ s with a slight decrease in  $E_S$  compared with using PDI only. Combining all techniques,  $T_S$  and  $E_S$  were further reduced by  $102.7 \times$  to 18  $\mu$ s and  $2.9 \times$  to 114.5 nJ, respectively, compared with the case where no techniques were utilized. The start-up time has been significantly improved compared with prior work that boosts negative resistance (see [8] and [12]), albeit with higher  $E_S$ . In systems where latency is of concern or power dissipation during their active period is large, minimizing the start-up time is considered to be the main objective function. The increased  $E_S$  value is due to high power consumption associated with the AI and  $g_m$ -boosting techniques. Measured power consumption (estimated  $E_S$ ) for AI, RXO (including buffers), and amplifiers  $g_{m1}$  and  $g_{m2}$  [see Fig. 2(a)] is 7.2 mW (79 nJ), 3.6 mW (27 nJ), and 0.5 mW (8 nJ), respectively. According to the transient simulations of the XO start-up behavior, hypothetically, if AI is removed and the  $R_N$ -boost amplifier  $g_{m2}$  is scaled in size and power by an additional factor of 12 and 3,  $T_S \simeq$  22  $\mu s$ and  $E_S \simeq 124$  nJ. The measured  $T_S$  value varies by 2% for a 25% variation in the injection time and by  $\pm 12\%$  over a temperature range of -40 °C to 90 °C. Transient frequency of

	[16]	[15]	[8]	[22]	[19]	[17]	[18]	This Work
CMOS process (nm)	180	65	90	65	65	65	55	180
Core area (mm <sup>2</sup> )	0.12	0.08	0.072	0.023	0.09	0.069	0.049	0.108
Supply (V)	1.5	1.68	1	0.35	1	1	1.2	1
Frequency (MHz)	39.25	24	24	24	50	54	32	48
Load capacitor $C_L$ (pF)	6	6	10	6	9	6	6	8
Steady-state amplitude (V)	1.5	N/A	N/A	0.3	$0.2^{2}$	0.7	0.37	0.7
Phase noise (dBc/Hz) at 1 kHz	-147	N/A	N/A	-134	N/A	-139.5	N/A	-135
Steady-state power $(\mu W)^1$	181	393	95	31.8	195	198	190	180
Start-up time $T_S$ ( $\mu$ s)	158	64	200	400	$2.2^{2}$	19	23	18
$T_S$ improvement ratio	13.3×	6.7×	13.3×	3.3×	N/A	31.5×	17.4×	102.7×
Start-up energy $E_S$ (nJ)	349	N/A	36	14.2	13.3 <sup>2</sup>	34.9	20.2	114.5
$E_S$ improvement ratio	1.1×	N/A	6.9×	2.8×	N/A	N/A	N/A	2.9×
$\Delta T_S$ over Temp. (%)	7	±35	27.5	7.5	7	±1.25	±10	±12
Temp. range (°C)	-30 to 125	-40 to 90	-40 to 90	-40 to 90	-40 to 90	-40 to 85	-40 to 140	-40 to 90
Start-up technique	Chirp injection $g_m$ boost	Dithered injection	Dynamic load, $g_m$ boost	3-stage $g_m$ , Chirp injection	Precisely- timed injection	2-step injection	Synchronized signal injection	PDI, AI

TABLE I
MEASUREMENT SUMMARY AND COMPARISON WITH PRIOR ART

ECS-33B SMD crystal is used.

XO during start-up settles within  $\pm 20$  ppm of its steady state in <18  $\mu$ s, as shown in Fig. 23. Fig. 24 shows the measured phase noise profile of the XO, where a -135-dB/Hz phase noise at 1-kHz offset is reported. Spurious tones seen on the profile are due to weak supply bypass capacitors on board. Table I summarizes the performance of the XO using the proposed techniques in comparison with prior work. To better assess the effectiveness of various start-up techniques, both  $C_L$  and the steady-state amplitude that is proportional to the square root of crystal energy should be taken into consideration [see (8)] and are, thus, included in Table I. This paper achieves the largest  $T_S$  improvement ratio to date while maintaining an  $E_S$  improvement ratio compared with the prior art.

#### VI. CONCLUSION

This paper presented a study and design of two techniques used to reduce start-up time  $(T_S)$  and energy  $(E_S)$  of the Pierce crystal oscillator (XO). An analytical study of the external signal injection was presented, and an RXO was proposed as an alternative external injection source to minimize  $T_S$ . An overview of limitation imposed by the crystal's static capacitor on XO start-up time was presented, and an AI was designed to mitigate its effects. The simulation and measurement results of a prototype in a 180-nm CMOS process verified the efficacy of the proposed techniques. A significant increase in  $T_S$  improvement ratio was achieved across a wide temperature range.

#### ACKNOWLEDGMENT

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<sup>&</sup>lt;sup>1</sup>Heavily depends on frequency, supply, C<sub>L</sub>, crystal properties and steady-state amplitude.

 $<sup>^2</sup>$ Steady-state amplitude is limited to  $\sim$ 0.2V by a regulation loop, requiring only an external injection for a very short time.

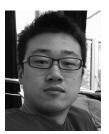
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