

# Structure and Vibrational Properties of Potassium-Promoted Tungsten Oxide Catalyst Monomeric Sites Supported on Alumina ( $K_2O/WO_3/Al_2O_3$ ) Characterized Using Periodic Density Functional Theory

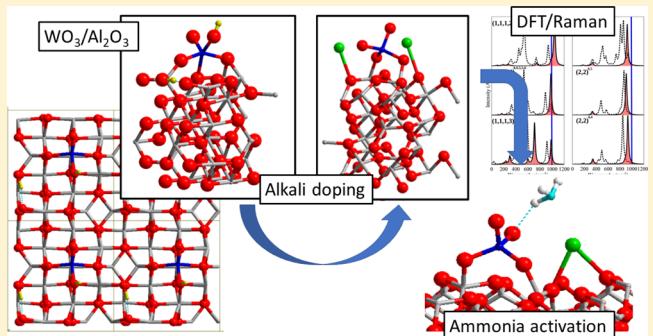
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**ABSTRACT:**  $Al_2O_3$ -supported tungsten oxide catalysts have been instrumental in many industrially relevant reactions and their reactivity is controlled by their molecular structure. In turn, their molecular structure has primarily been derived via Raman measurements with assignments made using model compounds of known local (molecular) coordination. In this work, the structure and simulated Raman spectra of unpromoted and  $K^+$ -promoted tungsten oxide catalyst monomeric sites supported on  $\gamma$ - $Al_2O_3$ (110) ( $K_2O/WO_x/\gamma$ - $Al_2O_3$ (110)) were studied using periodic DFT methods. Two different  $WO_x$ -grafted monomers on the  $\gamma$ - $Al_2O_3$ (110) surface were identified with a total energy difference of 0.17 eV between both structures. Importantly, both structures showed the presence of  $W=O$  and  $W-OH$  moieties, thus providing additional insights into experimental Raman data, which typically describe only  $W=O$  moieties. The grafted  $WO_3$  species were stabilized when the present  $W-OH$  groups were oriented toward the alumina surface leading to the formation of H-bonds, calculated at  $1039\text{ cm}^{-1}$ , for example in the vicinity of the  $W=O$  vibrations. The  $W=O$  bond length was altered in the presence of  $K^+$ , as shown experimentally and theoretically in blue shifting of the Raman band corresponding to  $W=O$ . The  $W$  vibrations were well localized in the calculated spectra, and little shifts were observed upon the different  $WO_x$  molecular geometry, explaining why a single Raman peak is mostly observed experimentally. The acidity of the lowest energy catalyst structures was investigated by simulated  $NH_3$  adsorption vibrational frequency and binding energy calculations. Results suggested that  $NH_3$  prefers to bind in a Lewis-like structure with no proton donation from either  $W-OH$  or  $Al-OH$  moiety. This challenged some of the literature observations where Brønsted acid sites have been suggested to exist on near-monolayer coverage  $WO_x$  species on  $\gamma$ - $Al_2O_3$  prepared by calcining at moderate (400 °C) to high temperatures (700 °C). Overall, this work provided new insights into the molecular structure of  $WO_x/\gamma$ - $Al_2O_3$  and  $K_2O/WO_x/\gamma$ - $Al_2O_3$  catalysts not immediately available from experimental measurements alone.



aqueous  $K_2WO_4$  solution via impregnation of  $Al_2O_3$ .<sup>17,18</sup> Different groups have investigated the role of the support in this catalyst, and the most commonly studied supports are silica,<sup>21</sup> alumina,<sup>21,22</sup> zirconia,<sup>21,23</sup> and titania<sup>24</sup>—partly owing to their specific physicochemical properties and partly to their abundance and relatively low prices.<sup>25</sup> Interestingly,  $K_2WO_4$  emerged to be the common active material in most cases, suggesting a particular catalyst structure leading to enhanced catalytic properties. Computationally, such small, isolated K and W-containing structures can be modeled to gain some understanding regarding their structures and effects on the catalytic material. Molecular structures of these K and W-containing catalysts as well as the resulting structure–property relationships are hence of fundamental importance.

In a supported transition metal oxide catalyst, the two most important parameters that control the catalytic performance are as follows. The first parameter is the nature and structure of the surface species, for example, the active sites present on the surface of the support as they can be acidic or basic, either Lewis and Brønsted, which affects the overall catalytic mechanism. The molecular geometry of the active site is of importance, as different molecular geometries of the active site exhibit different catalytic properties. In general, these supported metal oxide species on the surface can be isolated, oligomeric, semipolymeric, or fully polymeric, which further has implications on the mechanism that the catalytic process proceeds.<sup>21,26–28</sup> The second parameter is the active metal oxide coverage, where the maximum amount of metal oxide that can be anchored on the support in a two-dimensional fashion catalyst affects the overall activity.<sup>27</sup>  $WO_3$  supported on  $\gamma-Al_2O_3$  exhibits strong interaction with the support leading to observable changes in the properties of both tungsten oxide and alumina. For example, supported  $WO_3$  inhibits transformation of  $\gamma-Al_2O_3$  into  $\alpha-Al_2O_3$ , normally taking place via condensation of hydroxyl groups and elimination of  $H_2O$ .<sup>22</sup> This is due to the fact that  $WO_3$  species bond to the surface via the condensation of the hydroxyl groups.<sup>22,29</sup> Direct reaction between  $WO_3$  and  $Al_2O_3$  has only been experimentally observed at high temperatures of  $\sim 1150$  °C, when the tungsten oxide coverage is at or below the monolayer (1 ML =  $\sim 4.3$  W atoms/nm<sup>2</sup>). At high coverages ( $\sim 3 \times$  ML), the reaction between  $WO_3$  and  $Al_2O_3$  was observed even at  $\sim 500$  °C. It was reasoned that until monolayer coverage a virtually irreducible and highly dispersed tungsten oxide species was present on the alumina surface. On the other hand, above monolayer coverage, an easy-to-reduce, bulk-like  $WO_3$  species in the form of crystallites (3–10 nm in size) was present on the surface, which led to the observed decrease in the temperature requirement.<sup>22</sup> X-ray absorption near edge spectroscopy (XANES) and Raman spectroscopy data indicated that at low coverages ( $\sim 1/3 \times$  ML) and dehydrated conditions,  $WO_3$  surface species possessed a distorted tetrahedral molecular structure, while at higher coverages and hydrated conditions it exhibited octahedral symmetry.<sup>21,30,31</sup> Raman analysis of low coverage  $WO_3/Al_2O_3$  also indicated distorted tetrahedral with  $W=O$  and  $W-O-W$  bonds present hinting at the possibility of both monomeric and dimeric units<sup>31</sup> similar to those observed on silica.<sup>32</sup> As the coverage increased to a near monolayer, XANES and Raman data suggested the presence of distorted octahedral  $WO_3$  species.<sup>31</sup> These results have also been corroborated by UV-DRS measurements to provide the edge energies ( $E_g$ ) and ligand to metal charge transfer (LCMT) band information. In particular, UV-DRS at low

tungsten loadings ( $\sim 0.5$  W/nm<sup>2</sup>),  $\sim 1/10 \times$  ML, under hydrated and dehydrated conditions resulted in  $E_g$  values of 5.3 and 5.1 eV, respectively, and exhibited one LCMT at  $\sim 228$  nm, suggesting the presence of mono-tungstate  $WO_4$  surface species. On the other hand, at circum-monolayer loading ( $\sim 4.5$  W/nm<sup>2</sup>),  $E_g$  values at hydrated and dehydrated conditions were 4.1 and 4.0 eV, respectively, and several LCMT bands were observed at  $\sim 228$  and 254 nm. It was concluded that a mixture of mono- and poly-tungstates existed on the surface as indicated by the intermediate  $E_g$  value and multiple LCMT bands.<sup>5,21</sup> It was proposed that the change in the nature of the surface species (i.e., mono- vs di- vs poly-tungstate) as the tungsten oxide loading increased was related to the strong Brønsted acid sites which were spectroscopically observed at coverages of 1.4 W/nm<sup>2</sup> ( $1/3 \times$  ML) and above.<sup>5</sup> In situ Raman spectra revealed that addition of  $K_2O$  to the supported  $WO_3/Al_2O_3$  catalyst increased the concentration of isolated surface  $WO_x$  species and did not form  $K_2WO_4$  nanoparticles at near monolayer coverage.<sup>19</sup>

Although the  $Al_2O_3$  surfaces and its polymorphs  $\alpha$ - and the  $\gamma$ -have been studied theoretically by Raybaud et al.,<sup>33–36</sup> much less effort has been directed into computationally modeling the structure and properties of active  $WO_x$  sites on  $Al_2O_3$  and interactions of  $WO_x$  with the support. McBriarty et al.<sup>37</sup> modeled adsorbed, octahedral, 6-coordinated  $WO_x$  on  $\alpha-Al_2O_3(0001)$  surface at  $0.5 \times$  ML and showed that the protonation of oxidized  $WO_x/\alpha-Al_2O_3(0001)$  is not stable—a result in agreement with the experimental observation of nonfacile reducibility at lower tungsten loadings.<sup>22</sup> Monomeric  $WO_x$  or dimeric  $-O-W-O-W-O-$  species were used with  $W-O(OH)$  and  $W-(OH)_2$ —termination bonded to O-terminated  $\alpha-Al_2O_3(0001)$ .<sup>38</sup> These hydroxyl groups on  $WO_x$  moiety acted as Brønsted sites for  $NH_3$  adsorption. However, the exact structure of  $WO_x$  supported on  $Al_2O_3$  with and without  $K_2O$  at catalytically relevant temperatures and their structure–function relationships have not yet been characterized at the atomic level using ab initio methods despite abundantly available experimental data. It is already known that the  $WO_x-Al_2O_3$  interactions considerably influence the electronic and geometric properties of the surface species and their stability and reactivity. Therefore, it is crucial to model such systems to improve our understanding them and to help design better ones in the future. In the present study, density functional theory (DFT) calculations are used to model structural and vibrational properties of the isolated monomeric  $WO_3/Al_2O_3$  and  $K_2O/WO_3/Al_2O_3$  sites. The results are compared with the in situ Raman spectra of the catalysts, while changes in acidity are computed using  $NH_3$  as a probe molecule.

## THEORETICAL AND EXPERIMENTAL DETAILS

**Quantum Chemical Calculations.** All calculations are performed using ab initio plane-wave pseudopotential approach as implemented in VASP.<sup>39,40</sup> The PW91 functional<sup>41</sup> has been chosen to perform the periodic DFT calculations. The valence electrons are treated explicitly and their interactions with the ionic cores are described by the projector augmented-wave method,<sup>42</sup> which allows to use a low energy cutoff equal to 400 eV for the plane-wave basis. The Gamma point is used in the Brillouin-zone integration. The positions of all the atoms in the super cell are relaxed, until the total energy differences decrease below  $10^{-6}$  eV (forces acting on atoms fall below 0.005 eV/Å).

Vibrational spectra have been calculated for selected surface species within the harmonic approximation. Only the W center atom and its first and second neighbors (O–Al and OH groups) are considered in the Hessian matrix. This matrix is computed by the finite difference method followed by a diagonalization procedure. The eigenvalues of the resulting matrix lead to the frequency values. The assignment of the vibrational modes is done by inspection of the corresponding eigenvectors. The Raman intensities were estimated by the derivative of the macroscopic dielectric tensor (polarizability) with respect to the normal mode, following the method of Fonari and Stauffer.<sup>43</sup>

**Surface Model Description.** The surface slab model was adopted from the previous work.<sup>36,44</sup> In particular, 5-layer (110) surface termination of  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> model Al<sub>24</sub>O<sub>36</sub> was utilized as shown in Figure 1 with two bottom layers frozen

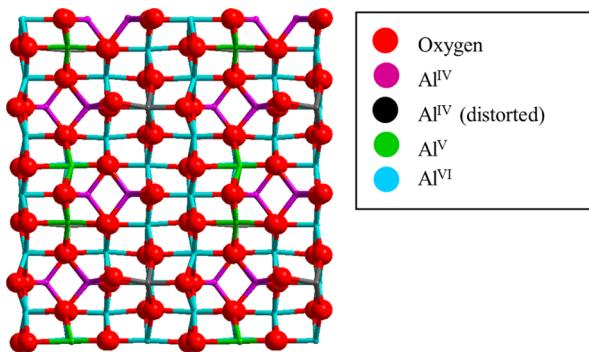


Figure 1.  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>(110) surface showing the different coordinations of Al. It should be noted that sites exposed at the surface have one coordination number less.

during the optimization. This is due to the higher reactivity of Al<sub>2</sub>O<sub>3</sub>(110) termination toward adsorbing mononuclear species, such as HReO<sub>4</sub>.<sup>45</sup> Al<sub>2</sub>O<sub>3</sub>(110) surface also possesses low-coordinated Al<sup>III</sup> and Al<sup>IV</sup> sites, which present efficient acceptor orbitals of low energy and form via truncation of tetra-coordinated Al atoms that are specific to the  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> structure.<sup>45,46</sup> Al<sup>IV</sup> are derived from aluminum atoms inherited

from bulk octahedral aluminum atoms, and Al<sup>III</sup> are derived from aluminum atoms originating from bulk tetrahedral aluminum atoms.<sup>44</sup> After surface relaxation, Al<sup>IV</sup> obtain pseudotetrahedral coordination, whereas Al<sup>III</sup>—pseudoplanar. The topmost surface oxygen atoms are of  $\mu_2$ -O and  $\mu_3$ -O coordination. The unit cells have a dimension of 8.068  $\times$  8.397 Å<sup>2</sup>, corresponding to a W coverage of 1.47 nm<sup>-2</sup>, which is approximately 1/3 ML.

Relative stability of the species was evaluated at 550 K using Boltzmann population via 1

$$p (\%) = \frac{e^{(-\Delta E_{\text{ads}}/kT)}}{\sum e^{(-\Delta E_{\text{ads}}/kT)}} \quad (1)$$

where  $k = 8.617 \times 10^{-5}$  eV/K,  $\Delta E_{\text{ads}}$  is 0 K adsorption energy without any vibrational corrections, and  $T = 550$  K.

**Synthesis of Model-Supported WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> and K<sub>2</sub>O/WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> and In Situ Raman Analysis of Their Surface Structure.** WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> and K<sub>2</sub>O/WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts were prepared by co-impregnation of KOH and ammonium metatungstate [(NH<sub>4</sub>)<sub>2</sub>W<sub>12</sub>O<sub>40</sub>· $x$ H<sub>2</sub>O, 99.9%+ purity] on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> (surface area  $\approx 170$  m<sup>2</sup>/g), drying under ambient conditions for 8 h, 120 °C for 16 h and subsequent calcination at 500 °C for 4 h. Raman spectra of dehydrated samples were taken with a visible (532 nm) laser excitation on a single-stage HORIBA-Jobin Yvon Lab Ram-HR Raman spectrometer equipped with a confocal microscope (Olympus BX-30) and a notch filter (Kaiser Super Notch). The visible excitation was generated by an Nd-YAG doubled diode pumped laser (Coherent Compass 315M-150; output power, 150 mW; sample power, 10 mW) with the scattered photons directed into a single monochromator and focused onto a UV-sensitive liquid-N<sub>2</sub> cooled CCD detector (HORIBA-Jobin Yvon CCD-3000V) with a spectral resolution of  $\sim 2$  cm<sup>-1</sup> for the given parameters.

## RESULTS AND DISCUSSION

**Molecular Structure of WO<sub>3</sub> Species on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>(110).** First, a systematic study on the possible configurations of the surface species resulting from H<sub>2</sub>WO<sub>4</sub> grafting was investigated using computational methods. As shown in Figure 2, the H

### Nomenclature of the models

(A,B,C,D) <sup>e<sub>1</sub>,e<sub>2</sub>,...</sup>	A = number of cations of H <sub>2</sub> WO <sub>4</sub> -precursor present on surface B = number of cations of H <sub>2</sub> WO <sub>4</sub> -precursor present on W (W-OH groups) C = number of W=O groups D = number of W-O-Al bonds e <sub>s</sub> = Al-coordination of the adsorption site
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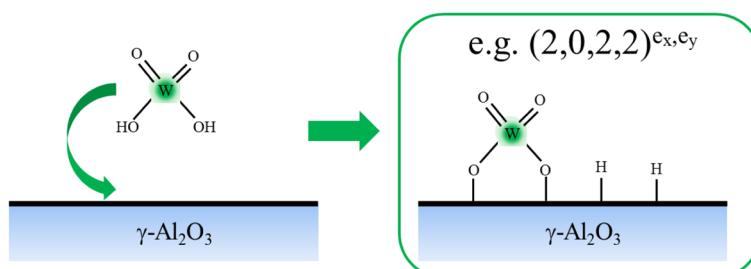


Figure 2. Conceptual surface site model nomenclature shown using a schematic representation of the grafting modes of the W precursor H<sub>2</sub>WO<sub>4</sub>. Surface K<sub>2</sub>WO<sub>4</sub> isolated model site is obtained by substituting two protons with K<sup>+</sup> atoms to maintain charge neutrality. The superscript e indicates the oxygen to which it is coordinated and can be have up to six different e<sub>x</sub>, e<sub>y</sub>, ... values, according to the coordination sphere of tungsten observed in the model.

atoms can be placed around the W center or on surface oxygen forming a surface hydroxyl group.

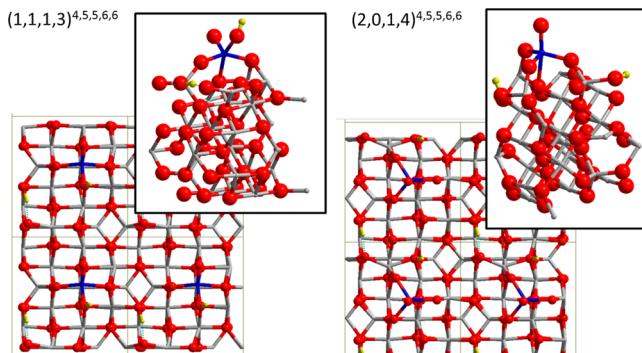
Eighteen different configurations of these  $\text{WO}_x$  species were studied computational on different grafting sites on the  $\gamma\text{-Al}_2\text{O}_3(110)$  surface. The relative total energies, shown in Table 1, indicate a competition ( $\Delta E = 0.17$  eV) between the

**Table 1. Adsorption Energy, Relative Adsorption Energy, and Boltzmann Population at 550 K for the 18 Grafting Configurations ( $\text{H}_2\text{WO}_4$ ) Studied<sup>a</sup>**

configuration	$\Delta E_{\text{ads}}$	$\Delta\Delta E_{\text{ads}}$	Boltzmann population $p$ , %
(1,1,1,3) <sup>4,5,5,6,6</sup>	-4.43	0.00	97
(2,0,1,4) <sup>4,4,5,5,6</sup>	-4.25	0.17	3
(1,1,1,2) <sup>4,4</sup>	-4.12	0.30	
(1,1,0,4) <sup>4,5,5,6</sup>	-4.04	0.38	
(2,0,2,3) <sup>4,4,5</sup>	-4.02	0.41	
(2,0,2,3) <sup>4,5,5</sup>	-3.86	0.57	
(2,0,2,2) <sup>4,4</sup>	-3.84	0.58	
(1,1,0,4) <sup>4,4,5,5,6</sup>	-3.39	1.04	
(0,2,0,4) <sup>4,4,4,5</sup>	-3.16	1.27	
(2,0,1,3) <sup>4,5,5</sup>	-2.82	1.61	
(0,2,0,4) <sup>4,4,4,5,5</sup>	-2.52	1.90	
(1,1,1,3) <sup>3,5,5</sup>	-1.66	2.77	
(1,1,1,2) <sup>5,5</sup>	-1.58	2.85	
(0,2,0,3) <sup>3,5,5</sup>	-1.21	3.22	

<sup>a</sup>Energies in eV.

structure (1,1,1,3)<sup>4,5,5,6,6</sup> and (2,0,1,4)<sup>4,4,5,5,6</sup>, that is, a  $\text{WO}_x$  with one oxo and one hydroxyl group and a W monomer with one oxo group. These are shown in Figure 3. The most stable



**Figure 3.** Two most stable configurations of  $\text{WO}_x$  species resulting from  $\text{H}_2\text{WO}_4$  grafting on the  $\gamma\text{-Al}_2\text{O}_3(110)$  surface. (Color code: blue: W, red: O; gray: Al, and yellow: H).

structure with an undissociated W precursor (0,2,4)<sup>4,4,4,5</sup> is 1.27 eV higher in energy compared with the most stable structure (1,1,1,3)<sup>4,5,5,6,6</sup>. It is clear that the monomer species with two hydroxyl groups on the W center are energetically unfavorable (by more than 1 eV), and can thus be eliminated from the list of possible stable W oxide monomer species on the surface. The species with only one W=O or one W-OH group are at least 0.4 eV higher in energy, compared with the (1,1,1,3)<sup>4,5,5,6,6</sup> structure, which can also be considered energetically unfavorable (or, from another perspective, energetically activated). In general, grafted species were stabilized when the present W-OH groups are oriented toward the surface, in order to form H-bonds with the surface. The  $\text{WO}_x$  species were also more stabilized when its

coordination is maximized up to 6, surrounded preferably by Al atoms in coordination: 6, 4, 5, and 3. Species having protons on  $\gamma\text{-Al}_2\text{O}_3(110)$  bound to 3-coordinated oxygen atoms were also stabilized.

In the (1,1,1,3)<sup>4,5,5,6,6</sup> structure, the W=O and the W-OH bond lengths are 1.71 and 1.89 Å, respectively. The W-OAl bond lengths are 1.97, 1.84, and 2.17 Å. In the (2,0,1,4)<sup>4,4,5,5,6</sup> structure, the W=O bond distance is 1.72 Å. The W-OAl bonds are 1.85, 1.86, 1.90, and 2.30 Å. For comparison, the tungsten W=O bonds have lengths between 1.71 and 1.74 Å on amorphous silica,<sup>32</sup> which are comparable to our results.

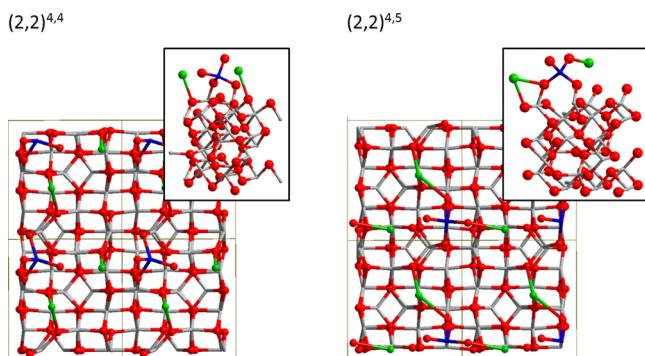
**Effect of  $\text{K}^+$  Promotion on the Surface  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$  Molecular Structure.** Alkali metal ion doping is known to modify the acid–base character of tungsten oxide catalysts.<sup>13,15,19,20</sup> For example, addition of 5.0%  $\text{K}_2\text{O}$  wt to 19%  $\text{WO}_3/\text{Al}_2\text{O}_3$  increased the population of the isolated surface  $\text{WO}_x$  species.<sup>19</sup> The shift of the W=O Raman band from 1021 to 963–985 cm<sup>-1</sup> indicated that potassium atom was interacting with the surface  $\text{WO}_x$  species and elongating the W=O bond.<sup>30</sup> In the absence of  $\text{K}^+$ , the isolated surface  $\text{WO}_x$  sites on  $\text{Al}_2\text{O}_3$  were difficult to reduce. However, addition of  $\text{K}_2\text{O}$  made the surface  $\text{WO}_x$  sites more reducible at elevated (>650 °C) temperatures.<sup>19</sup> Strong acidic gas molecules, such as  $\text{SO}_2$ , were found to preferentially bind to  $\text{K}_2\text{O}$  because of the strong  $\text{K}_2\text{O}$  basicity and its interaction with surface  $\text{WO}_x$ . To investigate the effects of  $\text{K}^+$  promotion, the models were constructed starting from the  $\text{H}_2\text{WO}_4$  structures, discussed in the previous section, placing the  $\text{K}^+$  cations next to the W monomer. To preserve charge neutrality,  $\text{WO}_x$  and surface bound protons were substituted with K atoms. The substitutions of  $\text{H}^+$  by  $\text{K}^+$  yielded less complex model diversity, that is, different models converged to the same final optimized geometry. The grafting site, that is, the coordination of the W–O–Al Al atoms, was altered in some cases by the effect of relaxation because of the electrostatic forces introduced by the  $\text{K}^+$  cations, which leads to less geometrically different models. A new nomenclature was adopted consisting of only two numbers and the coordination of the Al atoms on which the W monomer is grafted. The two numbers were the number of W=O bonds and the number of W–O–Al, linkages. The resulting adsorption energies together with the relative energy and the computed Boltzmann populations are shown in Table 2.

The two most stable geometries (see Table 2) for  $\text{K}_2\text{WO}_4$  grafting on the  $\gamma\text{-Al}_2\text{O}_3(110)$  surface were obtained from the following initial structures (2,0,2,2)<sup>4,4</sup> and (1,1,1,3)<sup>3,5,5</sup> for the first structure (2,2)<sup>4,4</sup> and from structure (1,1,1,2)<sup>4,4</sup> for the second structure (2,2)<sup>4,5</sup>. Both structures are iso-energetic, showing only a difference in the position of the cations and the position of the  $\text{WO}_4$  species on the surface. In the first structure, the cation is positioned closer to the W=O group than in the second one (see Figure 4). In structure (2,2)<sup>4,4</sup>, the intercation distance is 4.50 Å and the W=O bond length is 1.75–1.79 Å. The closest distance between  $\text{K}^+$  and W=O oxygen is 3.03 Å. In structure (2,2)<sup>4,5</sup>, the intercation distance is 4.33 Å and the W=O bond length is 1.77–1.78 Å. The closest distance between  $\text{K}^+$  and W=O oxygen is 2.72 Å. Starting from the different conformations and the corresponding proton positions shown in Table 2, an interesting observation emerges. One can clearly see that the potassium cations prefer to interact with the surface rather than with the  $\text{WO}_x$  monomer. Via the newly formed O–K bond, these  $\text{K}^+$  cations interact directly with the  $\gamma\text{-Al}_2\text{O}_3(110)$  surface, for

**Table 2. Adsorption Energy, Relative Adsorption Energy, and Boltzmann Population at 550 K for the K<sup>+</sup> Promoted WO<sub>x</sub>/γ-Al<sub>2</sub>O<sub>3</sub>(110) Grafting Configurations Studied<sup>a</sup>**

configuration	starting configuration	$\Delta E_{\text{ads}}$	$\Delta \Delta E_{\text{ads}}$	Boltzmann population $p$ , %
(2,2) <sup>4,4</sup>	(2,0,2,2) <sup>4,4</sup> (1,1,1,3) <sup>3,5,5</sup>	-4.86	0.00	37
(2,2) <sup>4,5</sup>	(1,1,1,2) <sup>4,4</sup>	-4.85	0.004	34
(2,2) <sup>4,4<sup>2</sup></sup>	(2,0,2,3) <sup>4,4,5</sup>	-4.78	0.07	8
(2,3) <sup>4,5</sup>	(2,0,1,3) <sup>4,5,5</sup> (1,1,1,3) <sup>3,5,5</sup>	-4.77	0.09	6
(1,4) <sup>4,4,4,5,6</sup>	(1,1,0,4) <sup>4,5,5,6</sup>	-4.71	0.14	2
(2,2) <sup>4,4,4</sup>	(0,2,0,4) <sup>4,4,4,5,5,5</sup>	-4.68	0.18	1
(2,2) <sup>4,4,5</sup>	(2,0,2,3) <sup>4,5,5</sup> (1,1,0,4) <sup>4,4,5,5,6</sup>	-4.61	0.25	
(1,4) <sup>4,4,4,4,4</sup>	(2,0,1,4) <sup>4,4,5,5,6</sup>	-4.57	0.29	
(2,2) <sup>4,4,5</sup>	(1,1,1,3) <sup>4,5,5,6,6</sup>	-4.36	0.49	
(2,2) <sup>4,5</sup>	(1,1,1,2) <sup>5,5</sup>	-3.10	1.76	
(2,2) <sup>4,4</sup>	(0,2,0,3) <sup>3,5,5</sup>	-2.04	2.82	

<sup>a</sup>Energies shown are in eV.

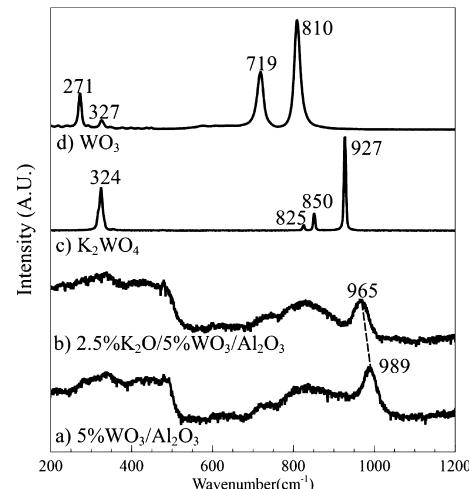


**Figure 4.** Two most stable configurations for K<sub>2</sub>WO<sub>4</sub> grafting on the γ-Al<sub>2</sub>O<sub>3</sub>(110) surface. (Color code: blue: W, red: O, gray: Al, and green: K).

example, the W—O—Al bridge site is not particularly preferred compared with the Al—O—Al bridge for the interaction with K<sup>+</sup>. The O—W—O site bonded to K<sup>+</sup> destabilizes the system (see Table 2, the least stable (2,2)<sup>4,4</sup> structure). Another interesting observation to notice is that the K<sup>+</sup> cations are separated by about 4.5 Å within the unit cell due to the coverage. The grafting site is dominated by distorted Al atoms with coordination number of 4 and, to a lesser extent, coordination number of 5. It follows that with increasing W coverage, the equivalent K<sup>+</sup> doping will tend to destabilize the catalyst, for example, increase the relative energy of the overall system. It is interesting to note that the most stable H<sub>2</sub>WO<sub>4</sub> system (1,1,1,3)<sup>4,5,5,6,6</sup> is destabilized after the substitution of H<sup>+</sup> with K<sup>+</sup> because of a strong distortion of the tetrahedral configuration of WO<sub>x</sub> and electrostatic destabilization of the W—O—Al linkages. In the contrary, one of the most unstable (i.e., the most reactive H<sub>2</sub>WO<sub>4</sub>) systems—(1,1,1,3)<sup>3,5,5</sup>—is strongly stabilized after substitution of H<sup>+</sup> by K<sup>+</sup>. Indeed, the W tetrahedral configuration is respected and K<sup>+</sup> is stabilized by the surface oxygen atoms. The position of the cation at this coverage is clearly determined by the strong electrostatic interactions. The most energetically optimal position should have a maximum coordination of the cation. The types of oxygen atoms that were used as coordination sphere is important, for example, W=O oxygen atoms, Al—O—W oxygen atoms, and Al—O—Al oxygen atoms. Moreover, there

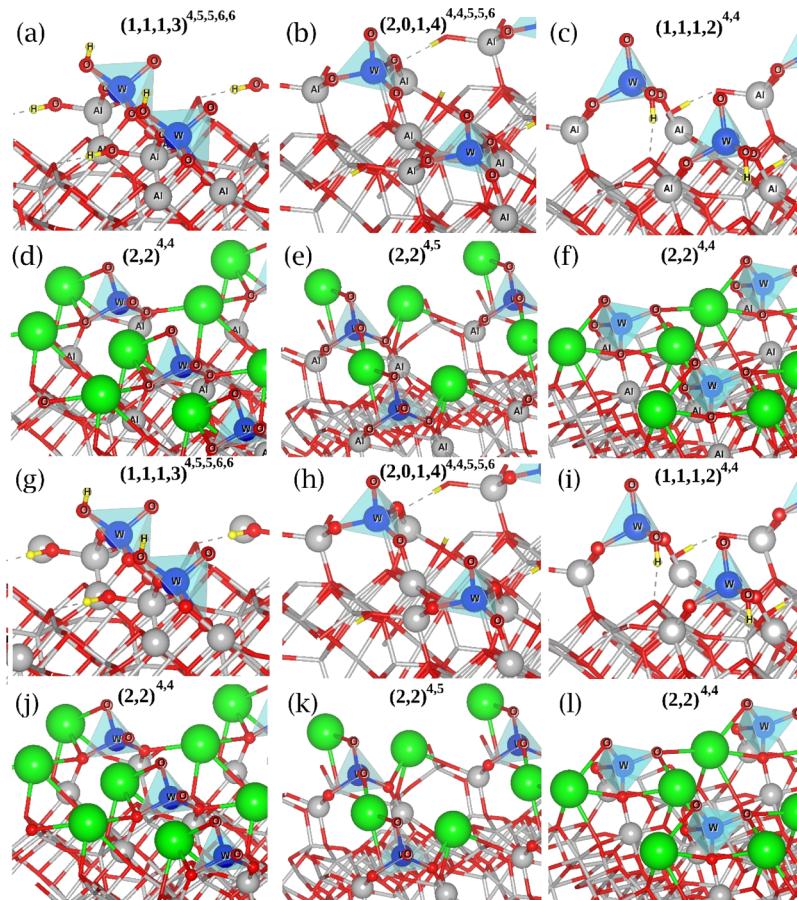
can be, in the proximity of the acidic center, a competition with the redox centers (W atoms). Combining this with the molecular structure and coordination to the surface of WO<sub>x</sub>, three coordination groups can be distinguished, based on their relative stability: (a) the structures containing mono-oxo W species, (b) di-oxo species with a minimal distorted tetrahedral configuration with K<sup>+</sup> cations positioned near high coordination sites, and (c) di-oxo species with tetrahedral configuration destabilized by under-coordinated K<sup>+</sup> cations present close to the W=O oxygen atom.

**Raman Spectroscopy and Theoretical Spectra Calculations of WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> and K<sub>2</sub>O/WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>.** Experimental Raman spectra of 5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> and 2.5% K<sub>2</sub>O/5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> sites with concentrations expressed in weight percent of metal are shown in Figure 5. Raman spectra of the crystalline



**Figure 5.** Raman spectrum for (a) 5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>, (b) 2.5%K<sub>2</sub>O/5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>, (c) K<sub>2</sub>WO<sub>4</sub>, and (d) WO<sub>3</sub>.

WO<sub>3</sub> and K<sub>2</sub>WO<sub>4</sub> reference compounds are shown for reference. Crystalline WO<sub>3</sub> exhibits strong Raman bands at 271, 719, and 810 cm<sup>-1</sup>, whereas crystalline K<sub>2</sub>WO<sub>4</sub> possesses intense Raman bands at 324 and 927 cm<sup>-1</sup>. The spectra are consistent with the oligomeric WO<sub>6</sub> and isolated WO<sub>4</sub> sites present in the bulk WO<sub>3</sub> and K<sub>2</sub>WO<sub>4</sub> crystals, respectively.<sup>19,21</sup> The Raman spectra of the dehydrated supported 5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> and 2.5% K<sub>2</sub>O/5% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts are also shown in Figure 5. The Raman spectrum of supported 5% WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> exhibits a band at 989 cm<sup>-1</sup>, and the absence of characteristic Raman bands from crystalline WO<sub>3</sub> indicates that the supported tungsten oxide phase is only present as surface WO<sub>x</sub> species on the Al<sub>2</sub>O<sub>3</sub> support. This Raman band at 989 cm<sup>-1</sup> corresponds to the stretching mode of isolated and oligomeric mono-oxo O=WO<sub>4/5</sub> surface species.<sup>47</sup> The Raman spectrum for the K<sup>+</sup>-promoted supported 2.5%K<sub>2</sub>O/5%WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst exhibits the W=O band at 965 cm<sup>-1</sup>. The absence of strong and sharp Raman bands from crystalline K<sub>2</sub>WO<sub>4</sub> reveals that the supported tungsten oxide phases are present as surface WO<sub>x</sub> species on the alumina support.<sup>48</sup> The shift of the W=O Raman band from 989 to 965 cm<sup>-1</sup> indicates that the potassium is interacting with the surface WO<sub>x</sub> species and results in lengthening of the W=O bond.<sup>48</sup> These data are also consistent with the literature observations, where the addition of K<sub>2</sub>O for the supported near monolayer coverage 19% WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> catalyst increased the UV-vis  $E_g$



**Figure 6.** Molecular structures used to obtain the theoretical Raman spectra, where only the atoms labeled with letters were relaxed during the geometry optimization. (gray: Al, blue: W, red: O, yellow: H, green: K). Resulting spectra are shown in **Figure 7**.

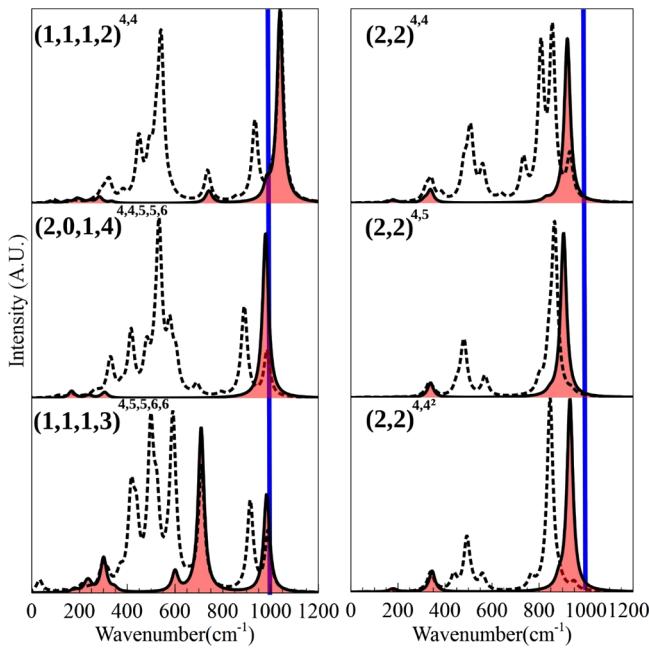
value to 4.9 eV showing an increase in the population of isolated surface  $\text{WO}_x$  species at the expense of the oligomeric surface  $\text{WO}_x$  species.<sup>19</sup>

Next, we computed Raman bands of the three lowest energy structures  $(1,1,1,3)^{4,5,5,6,6}$ ,  $(2,0,1,4)^{4,4,5,5,6}$ , and  $(1,1,1,2)^{4,4}$  of  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$  structures shown in **Table 1** and  $(2,2)^{4,4}$ ,  $(2,2)^{4,4}$ , and  $(2,2)^{4,4}$   $\text{K}^+$ -promoted  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$  structures shown in **Table 2** (here, the two  $(2,2)^{4,4}$  structures ( $(2,2)^{4,4}$  and  $(2,2)^{4,4^2}$ ) originated from the three different original protonated structures, namely  $(2,0,2,2)^{4,4}$ ,  $(1,1,1,3)^{3,5,5}$ , and  $(2,0,2,3)^{4,4,5}$ ) that are similar but not identical. The structures used to obtain the theoretical Raman spectra are shown in **Figure 6**. In particular, **Figure 6a–f** identifies structures with  $\text{WO}_x$  moiety and the nearest neighbors relaxed during the frequency calculations for  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3$  and  $\text{K}^+$ -promoted  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3$ , respectively. **Figure 6g** through **1** shows the molecular structure with only the corresponding  $\text{O}=\text{W}=\text{O}(\text{H})$  moiety relaxed.

All Raman spectra were normalized to the peak of the highest intensity here corresponding to that of  $\text{W}=\text{O}=\text{W}$  symmetric stretch at around  $980\text{ cm}^{-1}$ . The resulting spectra are shown in **Figure 7**. In particular, the dashed line spectra correspond to the calculations where a W atom center and its first and second neighbors (O, OH, and O-Al groups) were relaxed (see **Figure 6a–f**). The shaded spectra correspond to the Raman vibrations where only the W atom center and the atoms not linked to the surface (O and OH) were allowed to relax (see **Figure 6g–l**). This procedure was developed to

decouple majority Al–O–W contribution, which otherwise could result in a broad and complex peak structure.

The unpromoted  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3$  catalyst exhibits a characteristic measured Raman band at  $989\text{ cm}^{-1}$  (see **Figure 5**) corresponding to the  $\text{W}=\text{O}$  vibration. Experimentally, however, other vibrational contributions are rarely reported and derived computational models present a unique opportunity to describe the overall Raman vibrational system. Structure  $(1,1,1,3)^{4,5,5,6,6}$  shows, besides the typical  $\text{WO}-\text{H}$  stretching mode at  $3857\text{ cm}^{-1}$ , a  $\text{W}=\text{O}$  stretching at  $984\text{ cm}^{-1}$ . This too good agreement is probably due to canceling of errors often encountered in DFT calculations.<sup>49</sup> The  $\text{W}-\text{O}$  stretching is found at  $709\text{ cm}^{-1}$ , which could correspond the experimental broad and difficult to resolve  $721\text{ cm}^{-1}$  band. An antisymmetric OH stretch is observed at  $600\text{ cm}^{-1}$ . Finally, the low frequency modes observed in theoretical Raman spectrum are difficult to distinguish in the experimental one. For structure  $(2,0,1,4)^{4,4,5,5,6}$ , the experimental  $\text{W}=\text{O}$  vibration frequency is also predicted correctly, which corresponds to a tri-coordinated  $\text{W}=\text{O}$  stretching mode at  $979\text{ cm}^{-1}$  in the calculated Raman spectrum. This is only  $5\text{ cm}^{-1}$  lower compared with the bi-coordinated  $(1,1,1,3)^{4,5,5,6,6}$  ( $\text{HO}\text{W}=\text{O}$  stretching). Other low frequency bands are shown in **Table 3**, and because of the complexity of the experimental spectra, the matching is difficult to observe. This interesting observation has implications for the experimental spectra. Often discussed and assigned mono-oxo  $\text{WO}_x$  species ascribed to the peak at  $\sim 980\text{ cm}^{-1}$  can also be due to the partially hydrated ( $\text{HO}\text{W}=\text{O}$  moiety-containing species. If the proton is not



**Figure 7.** Calculated Raman spectra of  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3$  (left side) and  $\text{K}^+$ -promoted  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3$  (right side) structures shown in Figure 6 obtained between 1200 and 0  $\text{cm}^{-1}$ . Dashed line spectra: a W center and its first and second neighbors (O and OH) are relaxed. Color spectra: only atoms not linked to the surface (W, O, and OH) are relaxed. Blue vertical line corresponds to 980  $\text{cm}^{-1}$  value obtained in Raman experiments of isolated  $\text{WO}_x$  species.

H-bonded to any neighboring atom, its bending vibration will not be present at 1039  $\text{cm}^{-1}$  as in (1,1,1,2)<sup>4,4</sup> case (vide infra) and the distinction between pure di-oxo and mono-oxo hydroxylated moieties will not be possible experimentally but not theoretically. The only distinction, as shown in Figure 7, between di-oxo and mono-oxo hydroxylated  $\text{WO}_x$  can be a strong  $\nu_a(\text{W}=\text{O}_\text{H})$  vibration at 600  $\text{cm}^{-1}$  in the (1,1,1,3)<sup>4,5,5,6,6</sup> structure, not present in (2,0,1,4)<sup>4,4,5,5,6</sup>. Finally, in the (1,1,1,2)<sup>4,4</sup> structure containing a  $\text{WO}-\text{H}$  group hydrogen-bonded to the surface, a OH stretching mode at 3074  $\text{cm}^{-1}$  is present with the corresponding strong bending mode calculated at 1039  $\text{cm}^{-1}$ . The  $\text{W}=\text{O}$  has a stretching mode at 985  $\text{cm}^{-1}$ . Stretching  $\text{W}-\text{OH}$  vibrations are observed at 743  $\text{cm}^{-1}$ . The low frequency bands assignments are attributed to other stretching, bending, and libration modes. Notably, the Raman band at 1015  $\text{cm}^{-1}$  has previously been assigned to surface  $\text{WO}_5/\text{WO}_6$  poly-tungstate like species after dehydration at 450  $^\circ\text{C}$  but not on the samples exposed to ambient conditions.<sup>21</sup> Our data thus suggest that an alternative assignment to this peak as the shift toward higher wavenumbers, typically associated with bond elongation, can potentially also occur due to the  $(\text{O})=\text{W}-\text{OH}$  moiety.

An analysis of the Raman spectra, which include first and second neighbors of W (dashed line in Figure 7), allowed us to conclude that the peaks between 890 and 920  $\text{cm}^{-1}$  might be attributed to  $\text{W}=\text{O}-\text{Al}$  stretching modes. The peaks in the range from 330 to 560  $\text{cm}^{-1}$  include  $\text{O}-\text{Al}-\text{O}$  superficial and  $\text{W}=\text{O}-\text{Al}$  vibrational modes. Hence, when comparing the calculated total DFT spectra with the corresponding experimental, the relative intensities of the vibrations involving  $\text{WO}_x$  and those involving  $\text{O}-\text{Al}-\text{O}$  superficial and  $\text{W}=\text{O}-\text{Al}$  (effectively the support) support need to be taken into account. The  $\text{O}-\text{Al}-\text{O}$  superficial and  $\text{W}=\text{O}-\text{Al}$  vibrations

**Table 3. Calculated Raman Wavenumbers of Atoms Not Linked to the Surface (O and OH) Corresponding to the Different Types of Vibrations: a-Antisymmetric, s-Symmetric,  $\nu$ -Stretching,  $\delta$ -Bending, and L-Libration (R-Rocking, W-Wagging, and T-Twisting)<sup>a</sup>**

freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.	freq	assign.
$\text{H}_2\text{WO}_4$ precursor																			
(1,1,1,3) <sup>4,5,5,6</sup>																			
(2,0,1,4) <sup>4,4,5,6</sup>																			
(1,1,1,2) <sup>4,4</sup>																			
984	$\nu(\text{W}=\text{O})$	979	$\nu(\text{W}=\text{O}_\text{s})$	1039	$\delta(\text{W}=\text{O}_\text{h})$	985	$\nu(\text{W}=\text{O}_\text{s})$	743	$\nu(\text{W}=\text{O}_\text{h})$	931	$\nu_s(\text{O}=\text{W}=\text{O})$	884	$\nu_a(\text{O}=\text{W}=\text{O})$	904	$\nu_s(\text{O}=\text{W}=\text{O})$	848	$\nu_a(\text{O}=\text{W}=\text{O})$	920	$\nu_s(\text{O}=\text{W}=\text{O})$
709	$\nu(\text{W}=\text{O}_\text{h})$	600	$\nu_a(\text{W}=\text{O}_\text{h})$	346	$\text{W}(\text{O}=\text{W}=\text{O}_\text{h})$	306	$\nu(\text{W}=\text{O}) + \delta(\text{O}=\text{W}=\text{O}_\text{s})$	283	$\delta(\text{O}_\text{h}=\text{W}=\text{O}_\text{s})$	207	$\delta(\text{O}_\text{h}=\text{W}=\text{O}_\text{s}) + \nu_s(\text{O}=\text{W}=\text{O})$	189	$\nu_a(\text{O}=\text{W}=\text{O}) + \delta(\text{O}_\text{h}=\text{W}=\text{O})$	183	$\text{R}(\text{O}=\text{W}=\text{O})$	338	$\delta(\text{O}=\text{W}=\text{O})$		
300	$\text{W}(\text{O}=\text{W}=\text{O}_\text{h})$	224	$\delta(\text{O}=\text{W}=\text{O}_\text{h}) + \text{W}(\text{W}=\text{O}_\text{h}\text{H})$	179	$\text{W}(\text{W}=\text{O}_\text{h}\text{H})$	170	$\text{W}(\text{O}=\text{W}=\text{O})$	170	$\text{W}(\text{O}=\text{W}=\text{O})$	180	$\text{R}(\text{O}=\text{W}=\text{O})$	316	$\text{W}(\text{O}=\text{W}=\text{O})$	180	$\text{R}(\text{O}=\text{W}=\text{O})$	338	$\delta(\text{O}=\text{W}=\text{O})$		

<sup>a</sup>  $\text{O}_\text{h}$ —oxygen atom bonded with hydrogen.

should be weighed over different representative models. This will result in an increased  $\text{WO}_x$  vibration and explain why experimental Raman spectra of  $\text{WO}_x/\text{Al}_2\text{O}_3$  in this work and in the references lack any discernible peaks below  $900 \text{ cm}^{-1}$ .

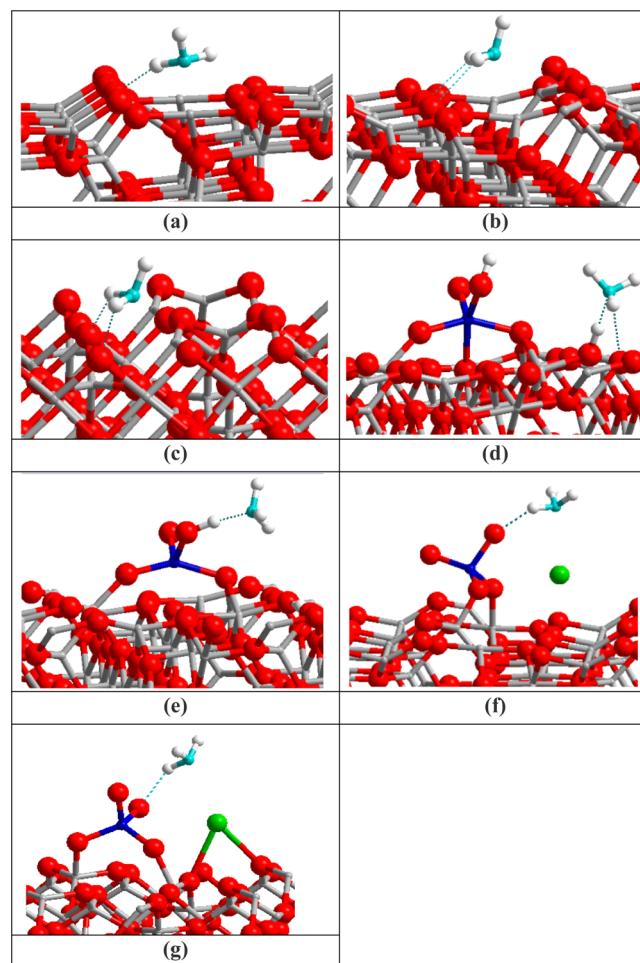
The presence of  $\text{K}^+$  results in the  $\text{W}=\text{O}$  symmetric stretching red-shift to  $965 \text{ cm}^{-1}$  experimentally, as shown in Figure 5. Our calculations predicted a stronger shift to  $\sim 920 \text{ cm}^{-1}$  in all three lowest energy structures, namely  $(2,2)^{4,4}$ ,  $(2,2)^{4,5}$ , and  $(2,2)^{4,4^2}$ . In  $(2,2)^{4,4}$ , symmetric stretching is found at  $931 \text{ cm}^{-1}$ , antisymmetric stretching at  $884 \text{ cm}^{-1}$ , and bending  $\text{O}=\text{W}=\text{O}$  mode at  $345 \text{ cm}^{-1}$ . Other libration modes are observed on low frequency ranges. For both  $(2,2)^{4,5}$  and  $(2,2)^{4,4^2}$  structures, the  $\text{W}=\text{O}$  stretching is calculated at  $904$  and  $920 \text{ cm}^{-1}$ , respectively. It is interesting to note that these are nearly equal to the one observed in  $\text{K}_2\text{WO}_4$  in Figure 5. In a similar way as with the unpromoted  $\text{WO}_x$  spectral calculations,  $890$ – $920 \text{ cm}^{-1}$  region peaks are attributed to  $\text{W}=\text{O}-\text{Al}$  stretching modes while those between  $330$  and  $560 \text{ cm}^{-1}$  to other  $\text{O}-\text{Al}-\text{O}$  superficial and  $\text{W}=\text{O}-\text{Al}$  vibrational modes. These data are apparent from Figure 7 dashed line simulated spectra. We propose that experimental spectra will have very complex (and hence broadened) contributions from the surface bonds, difficult to resolve. Hence, a single peak is mostly pronounced for these species,  $\text{WO}_x$  and  $\text{K}^+$  promoted  $\text{WO}_x$  alike. In the latter case,  $\text{K}^+$  should result in even stronger bond polarizing effect.

In summary, the unpromoted and  $\text{K}^+$  promoted structures, that reproduce the best experimental data, were  $(1,1,1,3)^{4,5,5,6,6}$  and  $(2,2)^{4,5}$ , respectively. The other structures are also present on the surface but with lower populations. In other words, isolated  $\text{WO}_x$  species is expected to possess both  $=\text{O}$  and  $\text{OH}$  groups on  $\text{Al}_2\text{O}_3$  surface and  $\text{K}^+$  promotion would result in a clear spectral shift regardless the final coordination of  $\text{K}^+$  ions.

**Surface Acidity Testing via DFT Calculations of  $\text{NH}_3$  Adsorption on  $\text{WO}_3/\text{Al}_2\text{O}_3$  and  $\text{K}_2\text{O}/\text{WO}_3/\text{Al}_2\text{O}_3$ .**  $\text{NH}_3$  is a probe molecule used in experimental acidity tests of the catalyst structures. Three cases of  $\text{NH}_3$  were considered and calculated in this work, for example, on  $\gamma\text{-Al}_2\text{O}_3(110)$ ,  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ , and  $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ . The latter two correspond to the lowest energy, for example,  $(1,1,1,3)^{4,5,5,6,6}$  and  $(2,2)^{4,4}$  structures, in Tables 1 and 2. Several unique adsorption sites are present, as shown in Figure 8, that were explored on each surface and calculated the corresponding vibrational frequencies. Here,  $\gamma\text{-Al}_2\text{O}_3(110)$  is considered as fully dehydroxylated surface with primarily Lewis acid sites available.

The tabulated experimental vibrational frequencies of  $\text{NH}_3$  adsorbed on  $\gamma\text{-Al}_2\text{O}_3$ ,  $\text{WO}_3/\gamma\text{-Al}_2\text{O}_3$ , and  $\text{K}_2\text{O}/\text{WO}_3/\gamma\text{-Al}_2\text{O}_3$  are shown in Table 4.

For  $\gamma\text{-Al}_2\text{O}_3$ ,  $\text{NH}_3$  adsorption yielded major bands at  $3400$ ,  $3355$ ,  $1600$ ,  $1285$ , and  $1230 \text{ cm}^{-1}$ .<sup>50,52</sup> All of these bands were attributed to  $\text{NH}_3$  coordinated to Lewis acid sites, given that the  $\gamma\text{-Al}_2\text{O}_3$  was pretreated at temperatures higher than  $400 \text{ }^\circ\text{C}$  and that almost no band corresponding to  $\text{NH}_3$  adsorbed on Brønsted acid sites was observed for such samples.<sup>50,52</sup> On the other hand, when  $\gamma\text{-Al}_2\text{O}_3$  was pretreated at temperatures less than  $400 \text{ }^\circ\text{C}$ , extra bands were observed, which were attributed to  $\text{NH}_4^+$  species on Brønsted acid sites. Major bands corresponding to  $\text{NH}_4^+$  species on Brønsted acid sites are  $3100$ ,  $1560$ ,  $1510$ ,  $1470$ ,  $1450$ , and  $1410 \text{ cm}^{-1}$ .<sup>51</sup> Therefore, the pretreatment temperature changes the nature of the acid sites present on the surface of  $\gamma\text{-Al}_2\text{O}_3$ , which also corresponds



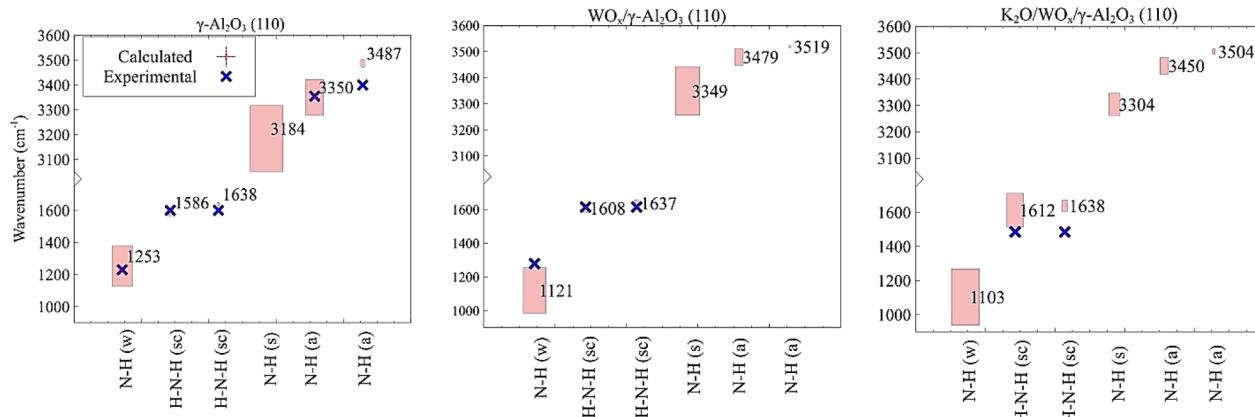
**Figure 8.** Computed  $\text{NH}_3$  adsorbed structures on (a–c)  $\gamma\text{-Al}_2\text{O}_3(110)$ , (d,e)  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ , and (f,g)  $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ .

to a change in the heat of adsorption of  $\text{NH}_3$ .<sup>51</sup> A comparison of calculated  $\text{NH}_3$  adsorption bands on  $\gamma\text{-Al}_2\text{O}_3$  shown in Figure 8a–c versus the observed experimental bands is shown in Figure 9. It can be seen that the experimental values agree well with the calculated values for all vibrational modes. Furthermore, the DFT calculations show a doublet at  $1638$  and  $1586 \text{ cm}^{-1}$  for  $\text{NH}_3$  coordinated to two different Lewis acid sites or Lewis and Brønsted sites. However, experimental results only show a singlet at  $1600$ – $1610 \text{ cm}^{-1}$  for Lewis acid sites. For pretreatment temperatures of  $<400 \text{ }^\circ\text{C}$ , the only other band in this region would be from  $\text{NH}_4^+$  species on a Brønsted acid site at  $1560 \text{ cm}^{-1}$ .<sup>51</sup> However, the N–H stretch with a DFT calculated average value of  $3184 \text{ cm}^{-1}$  was not observed in experiments at all.

For 20%  $\text{WO}_x/\text{Al}_2\text{O}_3$ ,  $\text{NH}_3$  adsorption yielded major bands at  $1674$ ,  $1615$ ,  $1432$ , and  $1279 \text{ cm}^{-1}$ .<sup>19</sup> The bands at  $1615$  and  $1279 \text{ cm}^{-1}$  were attributed to  $\text{NH}_3$  coordinated to Lewis acid sites and the ones at  $1674$  and  $1432 \text{ cm}^{-1}$  were attributed to  $\text{NH}_4^+$  on Brønsted acid sites.<sup>19</sup> In that study, the sample was pretreated at  $400 \text{ }^\circ\text{C}$ , which is why both Lewis and Brønsted acid sites were observed. A comparison of DFT calculated  $\text{NH}_3$  adsorption shown in Figure 8d,e versus the observed experimental bands is shown in Figure 9. The experimental values agree well with the calculated values for lower wavenumber modes ( $1200$ – $1700 \text{ cm}^{-1}$ ), which correspond

Table 4. Summary of the Experimental Data for NH<sub>3</sub> Adsorption on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, WO<sub>x</sub>/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, and K<sub>2</sub>O/WO<sub>x</sub>/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>

refs	details/comments	bands (cm <sup>-1</sup> )	description
50	NH <sub>3</sub> adsorption on $\gamma$ -Al <sub>2</sub> O <sub>3</sub> adsorption conducted at 50 °C $\gamma$ -alumina pretreated at 800 °C	3400 3355 3386 3335 3100 1600 1510	coordinatively held NH <sub>3</sub> on Lewis acid sites coordinatively held NH <sub>3</sub> on Lewis acid sites -NH <sub>2</sub> -NH <sub>2</sub> NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites coordinatively held NH <sub>3</sub> on Lewis acid sites -NH <sub>2</sub>
51	NH <sub>3</sub> adsorption on $\gamma$ -Al <sub>2</sub> O <sub>3</sub> adsorption conducted at 25 & 150 °C $\gamma$ -alumina pretreated at 330 °C	1230 1450, 1470 1600 1560	coordinatively held NH <sub>3</sub> on Lewis acid sites NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites coordinatively held NH <sub>3</sub> on Lewis acid sites (at 150 °C: NH <sub>4</sub> <sup>+</sup> on Brønsted site or NH <sub>2</sub> <sup>-</sup> )
52	NH <sub>3</sub> adsorption on $\gamma$ -Al <sub>2</sub> O <sub>3</sub> adsorption conducted at 25 °C $\gamma$ -alumina pretreated at 600 °C NOTE: for alumina pretreated at temperatures >400 °C, almost no Brønsted sites were present. Brønsted sites would correspond to the following bands	1230, 1285 1410, 1510, 1560	coordinatively held NH <sub>3</sub> on Lewis acid sites NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites
53	NH <sub>3</sub> adsorption on crystalline WO <sub>x</sub> adsorption conducted at 25, 100, 200, 250, 300 °C WO <sub>x</sub> pretreated at 700 °C	3393, 3318, 3167, 1601, 1270, and 1221 3253, 3203, 1467, and 1395	coordinatively held NH <sub>3</sub> on Lewis acid sites NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites
19	NH <sub>3</sub> adsorption on isolated site 20% WO <sub>x</sub> /Al <sub>2</sub> O <sub>3</sub> adsorption conducted at 120, 200, 300, 400 °C catalyst pretreated at 400 °C	1615 1279 1674 1432	coordinatively held NH <sub>3</sub> on Lewis acid sites NH <sub>4</sub> <sup>+</sup> on Brønsted acid sites
19	NH <sub>3</sub> adsorption on isolated site 5%K <sub>2</sub> O/19%WO <sub>x</sub> /Al <sub>2</sub> O <sub>3</sub> adsorption conducted at 120, 200, 300, 400 °C catalyst pretreated at 400 °C	1646	coordinatively held NH <sub>3</sub> on K <sup>+</sup> sites



**Figure 9.** Comparison of the experimental (blue cross marks) and DFT calculated (shaded pink) values of adsorbed NH<sub>3</sub> vibrations on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>(110), WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>(110), and K<sub>2</sub>O/WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>(110). Missing blue cross marks indicate that experimental data were not available for that vibration. The shaded pink region is the range of DFT calculated values for each vibration of NH<sub>3</sub> adsorbed on various sites. Tabulated frequencies of experimental NH<sub>3</sub> adsorption on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>, and K<sub>2</sub>O/WO<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> are summarized in Table 4.

to N–H wagging and H–N–H scissoring. However, the N–H stretches (symmetric & asymmetric) with calculated average values of 3349, 3479, and 3519 cm<sup>-1</sup> were not found in experimental reports, according to the best of our knowledge.<sup>19</sup> The DFT calculations showed a doublet at 1637 and 1608 cm<sup>-1</sup> for NH<sub>3</sub> coordinated to a W–OH moiety without

resulting proton donation. However, experimental results only show a singlet at 1615 cm<sup>-1</sup>. The only other band observed in the 1600–1700 cm<sup>-1</sup> region came from NH<sub>4</sub><sup>+</sup> species on Brønsted acid site at 1674 cm<sup>-1</sup>. Therefore, from our DFT calculated values, it cannot be ascertained if it is a vibration from NH<sub>3</sub> adsorbed on two different Lewis acid sites or if it is a

mixture of Lewis and Brønsted acid sites. Our calculations, however, show that  $\text{NH}_3$  always prefers to bind to W–OH moiety via weak H-bonded interaction and peaks due to the Brønsted acid would likely result from the interaction with the  $\text{Al}_2\text{O}_3$  support.

Lastly,  $\text{NH}_3$  adsorption on 5%  $\text{K}_2\text{O}/19\%\text{WO}_x/\text{Al}_2\text{O}_3$  reported in the literature yielded a major band at  $1646\text{ cm}^{-1}$ .<sup>19</sup> This band was attributed to  $\text{NH}_3$  adsorbed onto a K site, and it was argued that addition of K effectively eliminated all acidity.<sup>19</sup> A comparison of calculated  $\text{NH}_3$  adsorption bands versus the observed experimental bands is shown in Figure 9. The only experimental band observed was at  $1646\text{ cm}^{-1}$ , and no other band was reported. The DFT calculations, however, showed calculated bands at 1103, 1612, 1638, 3304, 3450, and  $3504\text{ cm}^{-1}$ . From Figure 8f,g it can be seen that  $\text{NH}_3$  indeed binds to  $\text{K}^+$  ions, thus confirming recent experimental assignments.<sup>19</sup> Our calculations also show that exact speciation of the adsorption site acidity with  $\text{NH}_3$  in this complex system is rather challenging as all of the coordination modes result in a Lewis-like behavior.

Adsorption energies ( $\Delta E_{\text{ads}}$ , eV) for various  $\text{NH}_3$  adsorption sites shown in Figure 8 were calculated and are listed in Table 5. It can be clearly seen that  $\gamma\text{-Al}_2\text{O}_3(110)$  surface has the

**Table 5. Calculated Adsorption Energy ( $\Delta E_{\text{ads}}$ ) Values for  $\text{NH}_3$  Structures Shown in Figure 8: (a–c)  $\gamma\text{-Al}_2\text{O}_3(110)$ , (d,e)  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ , and (f,g)  $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$**

composition	case	$\Delta E_{\text{ads}}$ (eV)
$\gamma\text{-Al}_2\text{O}_3(110)$	A	-1.98
	B	-1.22
	C	-1.47
$\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$	D	-0.71
	E	-0.10
$\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$	F	-0.47
	G	-0.45

strongest adsorption (most exothermic  $\Delta E_{\text{ads}}$  values), followed by  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$  and  $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ . The structures with  $\text{K}^+$  have the weakest  $\text{NH}_3$  adsorption (least exothermic values), as  $\text{K}^+$  is a Lewis base so the basic  $\text{NH}_3$  molecules have weakened (or very little) interaction with the surface. It is interesting to note that for  $\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ , the  $\Delta E_{\text{ads}}$  values vary significantly from -0.71 versus -0.10 eV, depending on if the  $\text{NH}_3$  is bonded to a proton on O–Al (catalyst support) or a proton on the W–OH ( $\text{WO}_x$  surface species) respectively. As the  $\gamma\text{-Al}_2\text{O}_3(110)$  support has a greater density of stronger acid sites, the  $\text{NH}_3$  adsorption is more exothermic. Hence, temperature-programmed methods should allow us to distinguish the three different types of surface sites available on  $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ .

## CONCLUSIONS

In this study, the structure and Raman spectra of unpromoted and  $\text{K}^+$ -promoted tungsten oxide catalyst monomeric sites supported on  $\gamma\text{-Al}_2\text{O}_3(110)$  ( $\text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$ ) were investigated using periodic DFT calculations and supporting Raman experiments. One  $\text{WO}_3$ -grafted monomer on the  $\gamma\text{-Al}_2\text{O}_3(110)$  surface was identified to be dominated by the  $(1,1,1,3)^{4,5,5,6}$  structure together with the  $(2,0,1,4)^{4,4,5,5,6}$  structure, with a total energy difference of 0.17 eV between both structures. Both structures showed  $\text{W}=\text{O}$  and  $\text{W}-\text{OH}$

groups along with three  $\text{Al}-\text{O}-\text{W}$  linkages. The grafted  $\text{WO}_3$  species were stabilized when the present W–OH groups are oriented toward the alumina surface leading to the formation of H-bonds. This is different from the literature reports where distorted mono-oxo species are typically postulated and attributed to the experimental Raman band in  $970\text{--}1014\text{ cm}^{-1}$ . It was also found that W–OH moiety bound to the surface support oxygen atoms (but not uncoordinated) can possess bending modes in the vicinity of those typically attributed to  $\text{W}=\text{O}$  vibrations. In the case of the  $\text{K}^+$ -promoted  $\text{WO}_x$  species, the  $(2,2)^{4,4}$  and  $(2,2)^{4,5}$  structures were the most stable. The  $\text{W}=\text{O}$  bond elongated in the presence of  $\text{K}^+$  in agreement with the experimental observations with the Raman band at 989 that shifting to  $965\text{ cm}^{-1}$ . The calculated  $\text{W}=\text{O}$  and  $\text{W}-\text{OH}$  vibrations were well localized in the calculated spectra and little shifts are observed upon the change in the  $\text{WO}_x$  geometry. Importantly,  $\text{WO}_x$  species, as suggested by our calculations, are expected to possess both  $\text{W}=\text{O}$  and  $\text{W}-\text{OH}$  groups from both energetics and vibrational arguments. For the most stable model structures, the adsorption of  $\text{NH}_3$  was simulated to probe the acidity of the catalyst. The vibrational frequencies obtained suggested that  $\text{NH}_3$  binds via Lewis-like coordination, even with the protons of W–OH or Al–OH groups. Calculated binding energies decrease in strength with  $\text{NH}_3$  adsorbed on  $\gamma\text{-Al}_2\text{O}_3(110) > \text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110) > \text{K}_2\text{O}/\text{WO}_x/\gamma\text{-Al}_2\text{O}_3(110)$  with some diversity found between W–OH $\cdots\text{HNH}_2$  and Al–OH $\cdots\text{HNH}_2$  groups.

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### Notes

The authors declare no competing financial interest.

## ACKNOWLEDGMENTS

This work by J.B. and D.K. was supported as part of UNCAGE-ME, an Energy Frontier Research Center funded by the U.S. Department of Energy, Office of Science, Basic Energy Sciences under award no. DE-SC0012577. This work used the Extreme Science and Engineering Discovery Environment (XSEDE),<sup>54</sup> which is supported by National Science Foundation grant number ACI-1053575. G.B. and P.Q. thank CONICET and UNL for financial support. Prof. Israel Wachs is acknowledged for assistance with Raman measurements.

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