

Is it possible to reconcile extragalactic IMF variations with a universal Milky Way IMF?

Dávid Guszejnov[®], ^{1★} Philip F. Hopkins ^{®2} and Andrew S. Graus¹

¹Department of Astronomy, The University of Texas at Austin, Austin, TX 78712, USA

Accepted 2019 March 4. Received 2019 March 4; in original form 2019 February 8

ABSTRACT

One of the most robust observations of the stellar initial mass function (IMF) is its nearuniversality in the Milky Way and neighbouring galaxies. But recent observations of early-type galaxies can be interpreted to imply a 'bottom-heavy' IMF, while others of ultrafaint dwarfs could imply a 'top-heavy' IMF. This would impose powerful constraints on star formation models. We explore what sort of 'cloud-scale' IMF models could possibly satisfy these constraints. We utilize simulated galaxies that reproduce (broadly) the observed galaxy properties, while they also provide the detailed star formation history and properties of each progenitor star-forming cloud. We then consider generic models where the characteristic mass of the IMF is some arbitrary power-law function of progenitor cloud properties, along with wellknown literature IMF models which scale with Jeans mass, 'turbulent Bonnor-Ebert mass', temperature, the opacity limit, metallicity, or the 'protostellar heating mass'. We show that no IMF models currently in the literature – nor any model where the turnover mass is an arbitrary power-law function of a combination of cloud temperature/density/size/metallicity/velocity dispersion/magnetic field - can reproduce the claimed IMF variation in ellipticals or dwarfs without severely violating observational constraints in the Milky Way. Specifically, they predict too much variation in the 'extreme' environments of the Galaxy compared to that observed. Either the IMF varies in a more complicated manner, or alternative interpretations of the extragalactic observations must be explored.

Key words: turbulence – stars: formation – galaxies: star formation – cosmology: theory.

1 INTRODUCTION

The mass distribution of stars at formation (often called the initial mass function or *IMF*) is a key part of cosmic evolution as it affects essentially all astrophysical scales. A key finding regarding the IMF is its apparent universality in the Milky Way (MW) and its satellite galaxies (see the reviews of Chabrier 2003; Bastian, Covey & Meyer 2010; Krumholz 2014; Offner et al. 2014), regardless of the locations and age of the observed population with a few possible outliers (e.g. Espinoza, Selman & Melnick 2009). While the IMF appears to be universal in the Galaxy, recent observations of the extragalactic IMF have been extrapolated to imply significant variations. Recent studies have looked at the centres of massive early-type galaxies (ETGs) and have seen an apparent excess of low-mass stars, a 'bottom-heavy IMF' (see Treu et al. 2010; van Dokkum & Conroy 2010, 2011; Cappellari et al. 2012; Conroy & van Dokkum 2012; Posacki et al. 2015; Sonnenfeld et al. 2015; Martín-Navarro

Nonetheless, several theoretical models have been proposed to explain the claimed IMF variations. In fact, analytic sonic

²TAPIR, MC 350-17, California Institute of Technology, Pasadena, CA 91125, USA

et al. 2015b,c). One must be cautious as these measurements use fundamentally different methods (e.g. Stellar Population Synthesis, SPS) than those used for IMF measurement in the MW (e.g. star counting). For more details see the recent review of Hopkins (2018). This means that various interpretation of these extragalactic results can lead to different implied IMFs. Furthermore, several other studies conflict with the claimed variations (e.g. Smith 2014; Smith, Lucey & Conroy 2015; Smith, Lucey & Edge 2017; Collier, Smith & Lucey 2018a). Meanwhile observations relying on star counts in ultrafaint dwarf (UFD) Galaxies imply an overabundance of highmass stars, a 'top-heavy IMF' (see Geha et al. 2013; Gennaro et al. 2018a). Note, that due to large uncertainties in the results, MW-like IMFs are not entirely ruled out by many of these observations (e.g. Offner 2016), and some UFD galaxies have IMFs consistent with an MW IMF, which means that the previously observed variations could be due to observational artefacts (El-Badry, Weisz & Quataert 2017: Gennaro et al. 2018b).

^{*} E-mail: guszejnov.david@gmail.com

mass/turbulent Bonnor-Ebert mass models¹ (e.g. Hennebelle & Chabrier 2008, 2013; Hopkins 2012) provide a remarkably good fit to the observed bottom-heavy IMF in ETGs. Several empirical models have also been proposed including ones that tie the IMF variations to metallicity (Martín-Navarro et al. 2015c).² However, these models all have trouble explaining the apparent universality of the IMF in the Galaxy. For example, Guszejnov, Hopkins & Ma (2017) have shown that the above-mentioned sonic-mass based models predict too much IMF variation within the MW - dense, high Mach number regions like the Arches cluster, the 'Brick' cloud and the galactic nucleus should have bottom-heavy IMFs, while observations indicate a slightly top-heavy IMF (Espinoza et al. 2009; Hußmann et al. 2012). Furthermore, IMF measurements using star counting have consistently found no sign of metallicity dependence in globular clusters from super solar metallicities down to $[Z/H] \sim -2$ (e.g. De Marchi, Paresce & Portegies Zwart 2010, see Bastian et al. 2010 and references therein). In fact, the most successful IMF models in the MW rely on heating via protostellar radiation to self-regulate the IMF with a turnover mass that depend exceptionally weakly on the environmental properties (see Krumholz 2011). A significant problem with these models is that - due to their weak dependence on gas properties - they are likely unable to reproduce the claimed IMF variations even in extreme environments.

In this paper, we explore whether it is possible to reconcile the claimed IMF variations in ETGs and UFDs with the apparent IMF universality in the MW. Similar to Guszejnov et al. (2017), we investigate IMF models that assume that the IMF of a stellar population is set by the properties of the progenitor cloud out of which they form. We gather cloud properties from high-resolution cosmological simulations of different types of galaxies, allowing us to predict the properties of the *entire stellar population* of the galaxy for any IMF model.

The paper is organized as follows. In Section 2.1 we introduce a simple one-parameter analytic model (based on Maschberger 2013) to map the observed 'IMF slopes' to actual mass functions. In Section 2.2 we quantify both the observed IMF universality in the MW and the observed variations in UFDs and ETGs within the framework of our one-parameter model. Section 2.3 details the properties of the simulated galaxies we use for this study, while Section 2.4 details the specific IMF models we investigate. We present our final results in Section 3.

2 MODEL AND METHODS

2.1 IMF slope and characteristic mass

Observations relying on the integrated spectra of galaxies (SPS modelling) are currently unable to probe the IMF in its entire mass range. Instead they constrain the relative number for a few select types of stars, effectively calculating the 'slope' of the IMF in relatively small mass ranges. As different measurements probe slightly different regions of the IMF (Hopkins 2018), it is

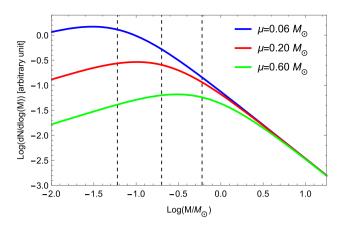


Figure 1. Effects of different characteristic masses μ in the one-parameter IMF model we adopt in this paper. The characteristic scale μ essentially sets the mass scale where the PDF deviates from the high-mass power-law behaviour.

necessary to find a model that allows one to compare between these measurements.

In this paper we use a simplified version of the L_3 parametric IMF model of Maschberger (2013). In the L_3 model the IMF has the following form:

$$\frac{\mathrm{d}N}{\mathrm{d}M} = L_3(M, \alpha, \beta) \equiv A \left(\frac{M}{\mu}\right)^{-\alpha} \left(1 + \left(\frac{M}{\mu}\right)^{1-\alpha}\right)^{-\beta}.$$
 (1)

In the low- and high-mass limits this simplifies to power laws with $-\alpha$ and $-\alpha - \beta(1 - \alpha)$ slopes, respectively. The characteristic mass scale is μ , this is where the function transitions between the two limits. Note that A is just a normalization constant that depends on α , β , and μ , as well as m_l and m_u , the low- and high-mass cut-offs of the IMF for which we use $m_l = 0.01 \, \mathrm{M}_{\odot}$ and $m_u = 150 \, \mathrm{M}_{\odot}$.

Since most observations only measure a single slope of the IMF, it is necessary to reduce the number of parameters for our IMF model. In this paper we adopt $\alpha=2.3$ and $\beta=1.4$, which are the canonical fit values for the MW IMF. The adoption of these 'fixed' slopes is further motivated by the fact that most scale-free structure formation processes naturally produce a -2 slope in the mass function (Guszejnov, Hopkins & Grudić 2018). These parameters lead to the one parameter IMF model that we adopt for the rest of the paper, where

$$\frac{\mathrm{d}N}{\mathrm{d}M} \propto \left(\frac{M}{\mu}\right)^{-2.3} \left(1 + \left(\frac{M}{\mu}\right)^{-1.3}\right)^{-1.4}.$$
 (2)

This leaves the characteristic mass scale μ as the only free parameter, so our model essentially assumes that the IMF has a universal shape that can only be shifted to lower or higher masses (see Fig. 1). As observations only constrain the IMF slope in a small dynamic range, such a one-parameter IMF can fit the observations.

Armed with this simple, one-parameter model we can create a one-to-one mapping between the slopes measured in different mass ranges and the characteristic mass (the 'peak')' turnover mass') of the IMF. Fig. 2 shows that the inferred characteristic mass is sensitive to the probed mass range, so one should be cautious when trying to compare different observations.

One of the aims of this paper is to explore the space of possible IMF models and identify what regions of this space would satisfy observational constraints. Due to the complexity of the task we limit our model space to theories where the IMF has the shape

¹In these models the IMF is regulated by isothermal turbulence, the higher the turbulent velocity dispersion the more the clouds fragment, which leads to more low-mass stars

²Note that the observed IMF variations in ETGs correlate not only with metallicity but with the galactic scale velocity dispersion as well, see Zhou et al. (2018).

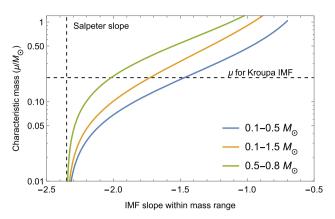


Figure 2. IMF slope and characteristic mass based on where the slope is calculated using the one-parameter IMF model of equation (2). Since most observations of the extragalactic IMF measure the 'slope' in different mass ranges, it is necessary to calculate the appropriate characteristic mass μ to interpret them (see Fig. 1 for the effects of μ on the IMF).

prescribed by equation (2) with a variable characteristic scale μ , which is *determined by the properties of the star-forming cloud*. For simplicity we further assume that μ can be approximately described as a power law in the form of

$$\mu \propto \rho^{\gamma_{\rho}} \times T^{\gamma_{T}} \times \mathcal{M}^{\gamma_{\mathcal{M}}} \times R^{\gamma_{R}} \times Z^{\gamma_{Z}} \times B^{\gamma_{B}}, \tag{3}$$

where ρ is the density, T is the temperature, R is the size scale, \mathcal{M} is the turbulent Mach number, Z is the metallicity, and B is the average magnetic field of the progenitor cloud. There are numerous examples of such IMF models, which have a somewhat fixed IMF shape and tie the characteristic mass to some property of the progenitor cloud, like Jeans mass (e.g. Bate & Bonnell 2005), turbulent properties (e.g. Hennebelle & Chabrier 2008; Padoan & Nordlund 2011; Hopkins 2012) or pressure (e.g. Krumholz 2011).

2.2 IMF constraints

In this paper we investigate the effects of the following (proposed) observational constraints on the IMF model space (see Table 3 for quick summary):

- (i) Universal IMF in the MW: It has been fairly well-established in the literature that the IMF in the MW is close to universal, regardless of the age and location of the stellar population (see reviews of Bastian et al. 2010; Offner et al. 2014; Hopkins 2018). Slight variation is possible in the characteristic mass on which we impose the conservative estimate of 0.2 dex based on fig. 3 of Bastian et al. (2010). Furthermore, based on resolved star counts the IMFs of old stellar populations have a similar or slightly more massive peak (see Fig. 5 and the references in the caption), still within the 0.2 dex limit.³
- (ii) **MW-like IMF in dwarfs**: Dwarf galaxies like the large magellanic cloud (LMC) and small magellanic cloud (SMC) appear to have the same IMF as the MW despite different galactic metallicity, stellar mass, and turbulent properties (see review Offner et al. 2014). Note that the completeness limit of these studies is $> 0.3 \, \mathrm{M}_{\odot}$ (see Da Rio, Gouliermis & Henning 2009; Gouliermis 2012) so that the

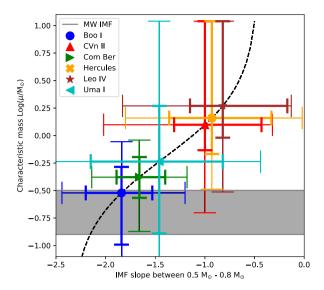


Figure 3. IMF slopes (between 0.5 and 0.8 ${\rm M}_{\odot}$) and characteristic masses of UFD galaxies based on the data of Gennaro et al. (2018a). The errorbars correspond to 1σ (thicker line) and 2σ (thinner line) confidence intervals. The dashed line shows the mapping between the IMF slope and the μ characteristic mass from Fig. 2. The shaded region shows the possible values of the IMF characteristic mass in the MW. Of the six UFD galaxies, three have characteristic masses that are within 1σ of the MW values and all of them are within 2σ . A characteristic mass that is roughly a factor of 2 higher than the MW value would be within 1σ for all galaxies, so we adopt that value as the average IMF shift for UFD galaxies.

peak of the IMF is not actually resolved, thus some variation is possible.

- (iii) **Top-heavy IMF in UFD galaxies**: Several recent observations have been extrapolated to imply top-heavy IMFs in UFD galaxies (see Geha et al. 2013; Gennaro et al. 2018a,b) but there is no consensus in the field about these claims (e.g. Offner 2016). As Fig. 3 shows, these results do not rule out an MW-like IMF with high confidence but are plausibly consistent with having a factor of 2 higher μ than in the MW. Due to this uncertainty, we explore the constraints arising from either having a top-heavy IMF or MW-like UFD IMF.
- (iv) **Bottom-heavy in ETGs**: There is a growing indirect evidence suggesting that centres of ETGs may have IMFs that are significantly more bottom heavy than the MW IMF (e.g. Treu et al. 2010; van Dokkum & Conroy 2010, 2011; Cappellari et al. 2012; Conroy & van Dokkum 2012; Sonnenfeld et al. 2015). A recent study by Conroy, van Dokkum & Villaume (2017) put the characteristic mass for one such galaxy below $0.1\,\mathrm{M}_{\odot}$, about a factor of 3 smaller than the MW value.
- (v) MW-like IMF in ETGs: Several recent studies using gravitational lensing have found ETGs to have mass-to-light ratios consistent with an MW-like IMF (see Collier et al. 2018a; Collier, Smith & Lucey 2018b). This contradicts the results from studies using stellar population synthesis models. In this paper we will investigate the effects of both constraints.

2.3 Simulations

We utilize several simulated galaxies from the Feedback in Realistic Environments (FIRE) project (Hopkins et al. 2014).⁴ These

³Note that dynamical evolution significantly alter the mass function of globular clusters leading to an apparent shift of the IMF peak to higher masses in studies that do not account for these effects (Baumgardt, De Marchi & Kroupa 2008; Kruijssen 2009). After correcting for these biases one can recover a near-universal IMF in the MW for populations of all ages.

⁴http://fire.northwestern.edu

Table 1. Properties of simulated galaxies from the FIRE project, including stellar mass M_* , target dark matter halo virial mass M_{DM} (at z=0), half-mass radius $R_{1/2}$, gas element mass resolution M_{\min} , critical density for sink particle creation n_{crit} , and the galactic average temperature T, metallicity Z and B magnetic field (when available) for progenitor clouds. See Fig. 4 for further details.

Key	Type	Redshift	$M_*/{ m M}_{\odot}$	$M_{\rm DM}/{\rm M}_{\odot}$	$R_{1/2}/\mathrm{kpc}$	$M_{\rm min}/{ m M}_{\odot}$	$n_{\rm crit}/{\rm cm}^{-3}$	$T_{\rm cloud}/{ m K}$	$\log{(Z/\rm{Z}_{\odot})}$	B/μG
m12i	MW-like	0	6×10^{10}	10 ¹²	3.5	7100	10^{3}	55	0.1	85
m11q	Dwarf, LMC-like	0	1.5×10^{9}	10^{11}	3.4	7000	10^{3}	32	-0.62	75
m10xf_14706	UFD, satellite	0	1.6×10^{5}	10^{8}	1.1	4000	10^{3}	23	-3.3	N/A
h29_HR	Early type	2.5	2×10^{11}	10^{12}	0.84	33000	200	92	-0.15	256
z5m12c	Early type	5	3×10^{10}	10^{12}	3.3	56000	200	110	-0.75	N/A

Table 2. ULIRG-like values assumed for the star-forming clouds in early-type galaxies that we use for testing IMF constraints.

ULIRG-like cloud star-forming clouds	
Density	$2 \times 10^5 \text{cm}^{-3}$
Temperature	75 K
Turbulent dispersion (σ_T)	$10 \mathrm{km} \mathrm{s}^{-1}$
Metallicity ($\log (Z/Z_{\odot})$	0.5
Magnetic field	100 μG

galaxies have been presented in detail in Hopkins et al. (2018), Anglés-Alcázar et al. (2017), and Graus et al. (2019) with one exception (z5m12c) that we will later discuss in Section 2.3.1 (also, see Section 2.3.2 on how we choose our UFD proxy). These are cosmological 'zoom-in' simulations, which means that the simulation starts from a large cosmological box that is later rerun with increased resolution in areas of matter concentration ('zooms-in' on galaxies). The simulations proceed from z > 100to present day (except **z5m12c** and **h29_HR**, see Section 2.3.1). They are run using the GIZMO code (Hopkins 2015),5 with the mesh-free Godunov 'MFM' method for the hydrodynamics (Hopkins 2015). Self-gravity is included with fully adaptive force and hydrodynamic resolution. The simulations include detailed metallicity-dependent cooling physics from $T = 10-10^{10}$ K, including photoionization/recombination, thermal bremsstrahlung, Compton, photoelectric, metal line (following Wiersma, Schaye & Smith 2009), molecular, fine structure (following Ferland et al. 2013), dust collisional, and cosmic-ray processes, including both a metagalactic UV background and each star in the simulation as a local source. The mass resolution for individual simulations is fixed and varies between $M_{\rm min} = 250 - 56000 \,\mathrm{M}_{\odot}$ among our simulated galaxies (see Table 1).

The resolution of these cosmological simulations is not high enough to resolve the formation of individual stars ($M_{\rm min}\gg 0.01\,{\rm M}_\odot$), instead star formation is approximated from resolved scales using a sink particle method. Gas is transformed into a sink particle if it:

- (i) Is locally self-gravitating
- (ii) Is self-shielding
- (iii) Is Jeans-unstable
- (iv) Exceeds a minimum density threshold ($n > n_{crit}$, see Table 1)

Such a sink particle is transformed into a 'star cluster sink particle' on its dynamical time. Each of these represent a stellar population with the same formation properties (age, metallicity etc.) and thus the same IMF.

These 'star cluster sink particles' provide feedback to the simulation via OB & AGB mass-loss, SNe Ia & II, and multiwavelength photoheating and radiation pressure; with inputs taken directly from stellar evolution models (Leitherer et al. 1999), assuming (in-code) a universal IMF (Kroupa 2002).

In this work, similar to Guszejnov et al. (2017), we use cosmological simulations instead of present-day observations because they give us access to the entire star formation history of a galaxy. In a simulation we know the properties of star-forming progenitor clouds *at all times*, allowing us to predict the IMF variation for the entire stellar population in a galaxy.

2.3.1 Finding a proper proxy for massive elliptical galaxies

For our analysis we utilize simulated present-day galaxies where the *at-formation* properties of all sink particles (star clusters) are available. We use these galaxies as proxies for the MW (m12i), LMC, and SMC (m11q) and UFDs (m10q). For ETGs we currently do not have access to such simulations so in this study we use three different proxies:

(i) h29_HR: This is a simulated FIRE galaxy with additional black hole physics that leads to extreme starburst behaviour, similar to what we expect in ETGs (see simulation A2 in Anglés-Alcázar et al. 2017 for details). Unfortunately for these runs the at-formation properties of sinks were not saved. Re-running the simulation would have been very expensive, so instead we post-processed the about 150 snapshot files of the simulation, taking actively star-forming gas from each to approximate the distribution of progenitor cloud properties over cosmic time. In our previous study (Guszejnov et al. 2017) we found that this approach provides a good approximation of the actual distribution. A major caveat with this proxy is that active galactic nucleus (AGN) feedback is poorly understood and thus it is not implemented in these simulations, despite the fact that it is believed to be one of the main mechanisms shutting off star formation.

(ii) **z5m12c**: This run was originally conceived to study galaxy scaling relation in the era of reionization (see Ma et al. 2018, for details of the simulation set-up). It utilizes the same FIRE physics suite and the progenitor cloud properties are saved for all sink particles. Although this galaxy was simulated only to z = 5, it is the progenitor of massive elliptical galaxy. The reason the simulation was not run further is due to the uncertainties in the physics that would quench star formation in such a galaxy. The stellar mass of $\mathbf{z5m12c}$ is only $3 \times 10^{10} \, \mathrm{M}_{\odot}$ at z = 5, which is only a few per cent

⁵http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html

⁶A major caveat of our analysis is that the feedback processes in the simulations assume a Kroupa IMF, so our post-processing neglects the potential feedback from a varying IMF and how it could enhance or suppress further IMF variation in a galaxy.

Table 3. Summary of observations constraints on the IMF in various environments as well as the proxies (mostly simulated galaxies from FIRE project) we use to estimate the constraints they put on IMF models. Here $\Delta\mu = \log \mu/\mu_{\rm MW}$ is the amount (in dex) the IMF characteristic mass is shifted in different environments, while $\sigma_{\mu,\rm MW}$ is the standard variation of $\log \mu$ in the Milky Way.

Environment	Co	nstraint	Reference	Proxy m12i	
Milky Way	Universal IMF Universal IMF	$\sigma_{\mu, MW} < 0.2$ $0 < \Delta \mu_{MW, z > 3} < 0.2$	Offner et al. (2014) Bastian et al. (2010) and Fig. 5		
Dwarf galaxies	MW-like IMF	$ \Delta\mu_{\mathrm{DG}} < 0.2$	Offner et al. (2014)	m11q	
UFD galaxies	Top-heavy IMF MW-like IMF	1 .		m10xf_14706	
Early-type galaxies	Bottom-heavy IMF	$ \Delta\mu_{\rm ETG} - \log 1/3 < 0.2$	Conroy et al. (2017)	z5m12c h29_HR ULIRG values	
Larry-type galaxies	MW-like IMF	$ \Delta\mu_{\mathrm{ETG}} < 0.2$	Collier et al. (2018b)	z5m12c h29_HR ULIRG values	

of the mass it would attain by $z\sim 2$, the time from which most ETG IMF measurements are from. Nevertheless, we can still use this simulated galaxy to look at the oldest population of stars in an ETGs.

(iii) Both previous proxies have important caveats, so as a complementary approach we will approximate the properties of the progenitor clouds in ETGs using typical values for galaxies with extreme star formation (e.g. an Ultra Luminous Infrared Galaxy – ULIRG), see Table 2.

Our three proxies essentially cover three possible ways to deal with the uncertain physics related to the quenching of star-formation in ETGs. With **h29_HR** we neglect it and carry on with the simulation until z = 2.5. In the case of **z5m12c** the simulation is stopped before AGN feedback could become important (z = 5), so we are essentially assuming very strong, early quenching. Finally, by using the canonical ULIRG values we avoid the potential issues with the simulations, but these values are highly arbitrary.

2.3.2 Finding a proxy for ultrafaint dwarf galaxies

To find an appropriate proxy for an UFD galaxy we use the simulations of Graus et al. (2019). With a combination of the Rockstar halo finder (Behroozi, Wechsler & Wu 2013), and the Amiga Halo Finder (AHF; Knollmann & Knebe 2009) we identify haloes and then select for galaxies with a low stellar mass ($<10^6\,\rm M_{\odot}$). In **m10xf** there are over 150 such low mass, from these we restrict our study to those whose stellar population is well-resolved (>25 'star' sink particles), which essentially sets the lower bound to our galaxy masses as $10^5\,\rm M_{\odot}$. This leaves eight galaxies, for our study we choose **m10xf.14706**, the one with the lowest stellar mass $(1.5\times10^5\,\rm M_{\odot})$. Note that picking a different galaxy from this group does not change the qualitative results of this study.

2.4 From parent cloud to IMF properties

Because the simulations resolve down to cloud scales, but no further, we treat each star-forming gas element as an independent 'parent cloud', which sets the initial conditions for its own detailed IMF model (in accordance with the IMF models we investigate). Specifically, whenever a sink particle is spawned, we record all properties of the parent gas element from which it is formed, and use these in post-processing to predict the IMF for the stellar population it spawns. From this point we infer the IMF characteristic mass μ from the initial conditions of the parent clouds that form stars

in the simulations (see Guszejnov, Krumholz & Hopkins 2016, for an example of how GMC properties could be mapped to the IMF). While we investigate the entire model space described by equation (3) we give special attention to the following classes of models that are common in the literature (summarized in Table 4):

(i) **Jeans mass models:** Gas clouds collapse primarily through the Jeans instability. This model assumes that the initial Jeans mass of the progenitor cloud sets the characteristic mass of the stars it spawns (e.g. Bate & Bonnell 2005), so

$$\mu_{\rm Jeans} \propto M_{\rm Jean} = \frac{\pi c_s^3}{6 G^{3/2} \rho^{1/2}}.$$
(4)

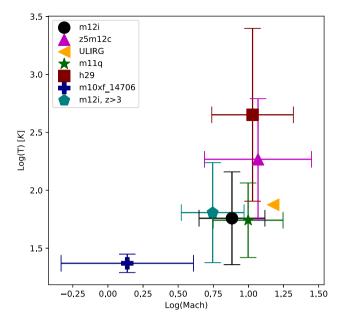
Note that the models may still assume sub-fragmentation to smaller scales, but the key assumption (for our purposes) is simply that the turnover mass is proportional to the parent cloud Jeans mass.

(ii) **Opacity-limited equation of state models:** As clouds become denser they reach the point where they become opaque to their own cooling radiation, leading to a transition from isothermal to adiabatic behaviour, suppressing fragmentation at the Jeans mass corresponding to this critical volume density $\rho_{\rm crit}$ (e.g. Low & Lynden-Bell 1976; Whitworth, Boffin & Francis 1998; Masunaga & Inutsuka 2000; Jappsen et al. 2005; Larson 2005; Glover & Mac Low 2007). Motivated by radiation transfer simulations like Bate (2009), we also investigated the case where the transition occurs at a critical surface density $\Sigma_{\rm crit}$. The resulting characteristic masses are:

$$\mu_{\text{EOS},\rho} \sim \frac{\pi c_s^3}{6 G^{3/2} \rho_{\text{crit}}^{1/2}}, \mu_{\text{EOS},\Sigma} \sim \frac{c_s^4}{G^2 \Sigma_{\text{crit}}},$$
(5)

where ρ_{crit} and Σ_{crit} are the critical densities for the isothermal-adiabatic transition.

(iii) **Turbulent/sonic mass models:** Several analytical theories derive the core mass function (CMF) and the IMF from the properties of the turbulent medium, in which they form (e.g. Padoan & Nordlund 2002; Hennebelle & Chabrier 2008; Hopkins 2012; Hennebelle & Chabrier 2013). In these models, both the CMF and IMF peaks are set by the 'sonic mass' $M_{\rm sonic}$, namely the turbulent Jeans or Bonner–Ebert mass at the sonic scale ($R_{\rm sonic}$) below-which the turbulence becomes subsonic and therefore fails to generate large density fluctuations (which seed fragmentation). The various theories give slightly different answers to this critical mass, in this paper we will use the definitions of Hopkins (2012)



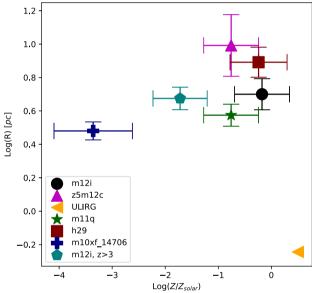


Figure 4. Galaxy-average properties of progenitor clouds (Top: turbulent Mach number versus temperature, Bottom: metallicity versus cloud size) in the simulated galaxies (see Table 1 for more details on the individual runs). The mean values are galaxy-scale averages of the logarithmic quantity weighted by stellar mass, while the errorbars show the corresponding 1σ scatter. There is significant variation not only between the different galaxies but also within individual galaxies. The average properties of star-forming clouds evolve significantly during a galaxy's lifetime, this is why this scatter is much larger than the observed scatter in present-day star-forming clouds.

and Hennebelle & Chabrier (2013), which give

$$\mu_{\text{sonic}} \sim M_{\text{sonic}} \sim \frac{2c_s^2 R_{\text{sonic}}}{G} \sim M_{\text{Jeans}} / \mathcal{M}$$
(6)

$$\mu_{\text{HC2013}} \sim M_{\text{Jeans}}/\mathcal{M}^2 \sim M_{\text{sonic}}/\mathcal{M},$$
 (7)

where R_{sonic} is defined through the linewidth–size relation

$$\sigma_{\text{turb}}^2(\lambda) = c_s^2 \frac{\lambda}{R_{\text{corpio}}}.$$
 (8)

In our simulations σ_{turb}^2 is estimated for a progenitor cloud (sink particle) by measuring the velocity dispersion (after subtracting the mean shear) between neighbouring gas particles in a sphere of radius λ (taken to be that which encloses the nearest \sim 32 gas neighbours).

(iv) **Protostellar feedback models:** Although there are a number of ways newly formed stars can regulate star formation, most studies have concluded that at the scale of the IMF peak (early protostellar collapse of $\sim\!0.1\,M_\odot$ clouds), the most important self-regulation mechanism is radiative feedback from protostellar accretion (Bate 2009; Krumholz 2011; Guszejnov et al. 2016). This sets a unique mass and spatial scale within which the protostellar heating has raised the temperature to make the core Jeans-stable, suppressing fragmentation. The resulting critical mass is

$$\mu_{\rm K11} \sim 0.15 \left(\frac{P/k_B}{10^6 \,\rm K/cm^3}\right)^{-1/18} \rm M_{\odot},$$
 (9)

where *P* is the pressure of the gas. There are several other formulas in the literature (e.g. Bate 2009); the differences are due to the detailed uncertainties in the treatment of radiation. However, for our purposes, they give *nearly identical* results, so we will focus on the model from Krumholz (2011).

(v) **Metallicity-dependent IMF models:** Some SPS analyses of ETGs have been empirically fit by assuming a trend of increasingly shallow IMF slopes with decreasing metallicity (see Martín-Navarro et al. 2015c and Fig. 5). This phenomenological model sets the slope of the IMF (in the $> 0.6\,\mathrm{M}_\odot$ range) as

Slope[
$$0.6 \,\mathrm{M}_{\odot} < M$$
] = $-2.2 - 3.1 \times [\mathrm{M/H}]$, (10)

where M/H is the logarithm of the mass-weighted total metallicity relative to the solar value. Note that the actual measurements are only sensitive to the IMF in the 0.1–2.0 M_{\odot} regime and the above relation was derived in Martín-Navarro et al. (2015c) by assuming a two-part IMF with fixed parameters below $0.6\,M_{\odot}$. To preserve generality, we use instead the single-power-law IMF fit from that work which yields

Slope[
$$0.1 \,\mathrm{M}_{\odot} < M < 1.5 \,\mathrm{M}_{\odot}$$
] = $-1.5 - 2.1 \times [\mathrm{M/H}]$. (11)

Using the one-parameter model from equation (2), we can convert the metallicity–slope relation into the μ -metallicity relation of

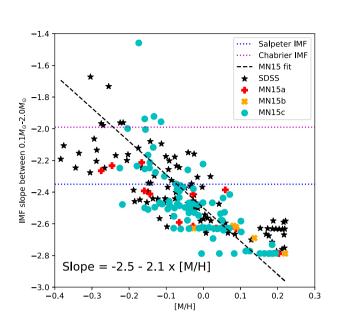
$$\log(\mu/M_{\odot}) = -1.3 - 2.4 \times [M/H] + \mathcal{O}([M/H]^2). \tag{12}$$

As shown in Fig. 5 this phenomenological model provides a good fit for the inferred extragalactic IMFs but drastically overpredicts the variations for old stellar populations within the MW.

3 RESULTS AND DISCUSSION

Using our simulation proxies we can calculate the shifts and variations of the IMF for the previously mentioned models. Table 4 shows that although some models can come close to reproducing the claimed UFD and ETG IMF variations (e.g. Hennebelle & Chabrier 2013), these drastically violate IMF universality within the MW. We find that *none of the current models in the literature can satisfy all constraints*, so we extend our search to generic models following equation (3).

Using the variations in progenitor cloud properties in the MW-like galaxy of **m12i**, we can identify the IMF models (the exponents for equation 3) that would satisfy IMF universality in the MW (this exercise is worked out in detail by Guszejnov et al. 2017).



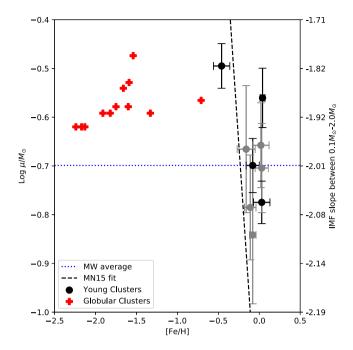


Figure 5. Left-hand panel: Galaxy-averaged single-power-law IMF slopes⁷ inferred by stellar population synthesis models from measured spectra by Martín-Navarro et al. (2015a,b,c) plotted versus galactic metallicity (see fig. 2 of Martín-Navarro et al. 2015c for uncertainties). There is a significant correlation between the inferred IMF slope and the galactic metallicity well-described by a linear fit (black, dashed line). Right-hand panel: IMF peaks inferred in the Milky Way from resolved star counts for young star forming regions (Luhman 2007; Oliveira, Jeffries & van Loon 2009; Sung & Bessell 2010; Bayo et al. 2011; Lodieu et al. 2011, 2012b; Lodieu, Deacon & Hambly 2012a; Pe na Ramírez et al. 2012; Alves de Oliveira et al. 2013, in black, the ones with large errorbars are plotted in grey) for old stellar populations in globular clusters (Paresce & De Marchi 2000, in red) as well as the IMF peak-metallicity relation inferred from Martín-Navarro et al. (2015c). It is clear that the resolved star counts in the MW rule out an IMF that is solely determined by metallicity as it was also shown by Villaume et al. (2017).

Table 4. The different IMF models compared in this paper, each with the predicted scaling of the IMF characteristic mass μ with initial parent cloud properties (Section 2.4), reference, and the predicted IMF variations/shifts. $\sigma_{\mu, MW}$ is the galaxy-wide scatter of the μ characteristic mass in a simulated MW-like galaxy (**m12i**), while $\Delta\mu_{\text{MW, z}} > 3$, $\Delta\mu_{\text{DG}}$, $\Delta\mu_{\text{UFD}}$, $\Delta\mu_{\text{HZ}}$ are the amount log μ 'shifts' in the simulated old MW populations, dwarf galaxy (**m11q**), UFD analogue (**m10xf.14706**), high z early-type galaxy (**z5m12c**), and early-type galaxy (**h29_HR**). $\Delta\mu_{\text{ULIRG}}$ (last column) shows the shift we get if we approximate the properties of the progenitor clouds in an early-type galaxy with those of an ULIRG (see Table 2). The values for these shifts/variations are colour coded based on how close they are to satisfying the constraints of Table 3. We use the following scale: green if they satisfy the constraint, orange if they fail to do so are within 0.2 dex (one MW IMF scatter), and red if they grossly violate the constrain (>0.2 dex difference). The only model that can satisfy MW universality is the protostellar heating based IMF model, which produces almost zero IMF variations in all cases.

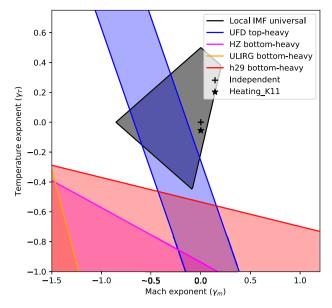
	IMF scale (μ)	Reference		IMF variation/shift [dex]						
IMF Model			Key	sink particle average					bulk properties	
				$\sigma_{\mu,\mathrm{M}W}$	$\Delta \mu_{\text{MW,z}>3}$	$\Delta\mu_{\mathrm{DG}}$	$\Delta \mu_{ m UFD}$	$\Delta \mu_{ m HZ}$	$\Delta\mu_{ m H29}$	$\Delta\mu_{ m ULIRG}$
Jeans Mass	$\propto T^{3/2} \rho^{-1/2}$	Bate & Bonnell 2005	M_Jeans	0.71	0.10	-0.03	-0.88	0.65	1.24	-0.99
Turbulent/Sonic Mass	$\propto T^{3/2} \rho^{-1/2} \mathcal{M}^{-1}$		M_Sonic	0.96	0.30	0.05	-0.13	0.47	1.16	-1.28
Turbulent/ Some Wass	$\propto T^{3/2}\rho^{-1/2}\mathcal{M}^{-2}$	Hennebelle & Chabrier 2013	HC_2013	1.98	0.37	0.12	0.61	0.28	1.01	-1.57
Opacity-limited, $\rho_{\rm crit}$	$\propto T^{3/2}$	Jappsen et al. 2005	EOS_Rho	0.60	0.07	-0.06	-0.58	0.76	1.27	0.17
Opacity-limited, Σ_{crit}	$\propto T^2$	Bate 2009	EOS_Sigma	0.80	0.10	-0.07	-0.78	1.02	1.69	0.23
Protostellar Heating	$\propto (\rho T)^{-1/18}$	Krumholz 2011	Heating_K11	0.03	0.0001	0.005	-0.01	-0.04	-0.05	-0.14
Metallicity dependent	∝ [M/H] ^{-2.4}	Martín-Navarro et al. 2015c	MN_2015	1.24	3.7	1.73	7.64	1.40	0.39	-1.62

With our additional constraints for old MW populations, dwarf galaxies, UFDs, and ETGs from Section 2.2 we can further restrict the model space (see Appendix A). We investigate both models from the literature (see Table 4 for results) and generic models following equation (3) (see Fig. 6 for an example). In general, we can draw the following conclusion:

(i) The large difference in average cloud metallicity in the older (z > 3) stellar population in our MW-like galaxies (**m12i**, see Fig. 4) compared to average and the significant scatter in metallicity in

the latter, only allows the IMF characteristic mass to have a weak metallicity dependence (see Fig. 6).

- (ii) There is little-to-no overlap between the regions that satisfy local IMF universality and those that reproduce the observed IMF shifts in ETGs (see Figs 6 and A2).
- (iii) MW universality strongly rules out most IMF models in the literature, including the turbulent/sonic mass models (see Guszejnov et al. 2017, for a detailed analysis).
- (iv) There exists a significant region of the model space that satisfies the assumption that the IMF is near universal in all types



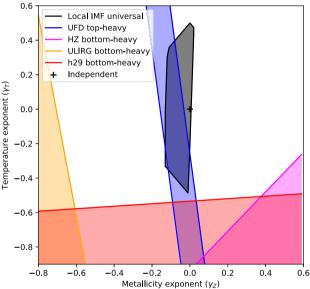


Figure 6. Power-law exponents for the Mach-number and temperature (left-hand panel) and metallicity and temperature (right-hand panel) in equation (3). The shaded regions show the exponents that satisfy IMF universality (grey region, see Fig. A1 for details), reproduce the inferred top-heavy IMF for ultrafaint dwarfs (blue region) and the bottom-heavy IMF for early-type galaxies (red, magenta, and orange regions, see Table 3 for details on constraints and Table 1 on the simulated galaxies). The symbols represent IMF models from the literature (see Table 4). There is clearly no overlap between the different types of constraints, thus there is no IMF model in this form that can satisfy all constraints.

of galaxies (<0.2 dex scatter in the galactic mean μ). An example of such 'weakly varying IMF' models is the protostellar heating model of Krumholz 2011 (Heating_K11).

None of the models detailed in Section 2.4 can reproduce the IMF variations that have been claimed for either ETGs or UFDs without grossly violating constraints from the local measurements with resolved star counts. Meanwhile the only model that reproduces the MW observations (the *Protostellar Heating* model) predicts essentially zero IMF variations in almost all environments. It is therefore natural to ask whether there even exists a model that can

reproduce both the claimed variations and the near-universality in the MW. Progenitor clouds have essentially six (nearly) independent properties: size, density, temperature, Mach number, magnetic field strength, and metallicity. We are looking for the exponents corresponding to these quantities in equation (3). If these quantities are independent then MW universality allows us to restrict the space we search to a 6D rectangle whose sides are described by: $|\gamma_X \Delta \log X_{\rm MW}| < \Delta \log \mu_{\rm MW}, \text{ where } \Delta \log X_{\rm MW} \text{ is how many orders of magnitude of scatter quantity } X \text{ has in our proxy for the MW } (\text{m12i}), \text{ while } \Delta \log \mu_{\rm MW} \text{ is the maximum allowed scatter in the MW IMF peak } (0.2 dex, see Section 2.2). Within this region we use a Monte Carlo search to find a set of exponents that would satisfy all criteria. We find the following:$

- (i) There is a significant volume in the model space that satisfies local IMF universality and produces a top-heavy IMF UFD galaxies.
- (ii) In case of our ETG proxy where we followed the galaxy evolution to $z\sim 2.5$ without AGN effects we find that there is no IMF model in the shape of equation (3) that can satisfy local IMF universality and produce the claimed bottom-heavy IMF.
- (iii) There exist a small volume in the model space that seems to satisfy local IMF universality and reproduce the observed IMF variations in both UFDs and ETGs (either **z5m12c** or ULIRG values, not both). These models however do not correspond to any known physical mechanism (e.g. $\mu \propto R^{-3/2}$). Furthermore, they all utilize the fact that the cloud sizes in **z5m12c** and in the ULIRG values are significantly different from the values in **m12i**. Note that the mass resolution and the critical density of the simulations (see Table 1) set a size scale that appears in the sink particle sizes and thus in the progenitor cloud sizes (essentially the size scale where the simulation replaces gas clouds with sink particles). To verify these models we use a lower mass resolution version of **m12i** ($\Delta m = 56000 \, \mathrm{M}_{\odot}$, like in Guszejnov et al. 2017), which clearly rules out all of these models. This means that there is no generic model that satisfies all constraints.
- (iv) If we relax the claimed variations in ETGs (e.g. a factor 2 shift instead of 3) we find that a significant volume of the model space can produce appropriate bottom-heavy IMFs for both simulation proxies (z5m12c and $h29_HR$) as well as satisfying local IMF universality and producing a top-heavy IMF for UFDs. Still, these models correspond to no known physical mechanism (e.g. $T^{-1/4}R^{-1/4}$).

4 CONCLUSIONS

In this paper we used different types of simulated galaxies to infer what constraints different observational claims impose on theoretical IMF models. We mainly focused on three common claims from the literature: (1) that the IMF in the MW and nearby dwarf galaxies is nearly universal, (2) that the IMF in ETGs is 'bottom-heavy', and (3) that the IMF in UFD galaxies is 'top-heavy'. We found that the current models in the literature either fail to reproduce the observed IMF variations or violate IMF universality in the MW.

We also investigated generic IMF models where the IMF characteristic mass is a power-law of progenitor cloud properties. Despite the high dimensionality of the model space, we find that no model where the turnover mass is an arbitrary power-law function of a

⁸In the simulations we used there is some correlation between these quantities, but we neglect them here for simplicity. Taking them into account does not change the result significantly.

combination of cloud temperature/density/size/metallicity/velocity dispersion/magnetic field can reproduce the claimed IMF variation in ellipticals or dwarfs without severely violating observational constraints in the MW.

One possibility is that the characteristic mass of the IMF is set by a yet unknown physical mechanism. Another, more likely scenario is that the magnitude of IMF variations in ETGs is overestimated in stellar population synthesis models. This would further explain why non-SPS based methods (e.g. gravitational lensing; see Collier et al. 2018a) appear to contradict SPS-based observations. There are a several possible reasons for such a bias, most of them coming from the inherent uncertainties of extrapolating stellar atmosphere models to extreme metallicities. We find that relaxing the claimed variations greatly increases the number of possible models.

ACKNOWLEDGEMENTS

Support for DG and PFH was provided by an Alfred P. Sloan Research Fellowship, NSF Collaborative Research grant #1715847 and CAREER grant #1455342, and NASA grants NNX15AT06G, JPL 1589742, 17-ATP17-0214. Numerical calculations were run on the Caltech compute cluster 'Wheeler,' allocations from XSEDE TG-AST130039 and PRAC NSF.1713353 supported by the NSF, and NASA HEC SMD-16-7592. This work used computational resources of the University of Texas at Austin and the Texas Advanced Computing Center (TACC; http://www.tacc.utexas.edu), the NASA Advanced Supercomputing (NAS) Division and the NASA Center for Climate Simulation (NCCS). DG and ASG were supported by the Harlan J. Smith McDonald Observatory Postdoctoral Fellowship. We would like to thank Stella Offner, Daniel Anglés-Alcázar, and Alexa Villaume for their help and comments.

REFERENCES

Alves de Oliveira C., Moraux E., Bouvier J., Duchêne G., Bouy H., Maschberger T., Hudelot P., 2013, A&A, 549, A123

Anglés-Alcázar D., Faucher-Giguère C.-A., Quataert E., Hopkins P. F., Feldmann R., Torrey P., Wetzel A., Kereš D., 2017, MNRAS, 472, L109

Bastian N., Covey K. R., Meyer M. R., 2010, ARA&A, 48, 339

Bate M. R., 2009, MNRAS, 392, 1363

Bate M. R., Bonnell I. A., 2005, MNRAS, 356, 1201

Baumgardt H., De Marchi G., Kroupa P., 2008, ApJ, 685, 247

Bayo A. et al., 2011, A&A, 536, A63

Behroozi P. S., Wechsler R. H., Wu H.-Y., 2013, ApJ, 762, 109

Cappellari M. et al., 2012, Nature, 484, 485

Chabrier G., 2003, PASP, 115, 763

Collier W. P., Smith R. J., Lucey J. R., 2018a, MNRAS, 473, 1103

Collier W. P., Smith R. J., Lucey J. R., 2018b, MNRAS, 478, 1595

Conroy C., van Dokkum P. G., 2012, ApJ, 760, 71

Conroy C., van Dokkum P. G., Villaume A., 2017, ApJ, 837, 166

Da Rio N., Gouliermis D. A., Henning T., 2009, ApJ, 696, 528

De Marchi G., Paresce F., Portegies Zwart S., 2010, ApJ, 718, 105

El-Badry K., Weisz D. R., Quataert E., 2017, MNRAS, 468, 319

Espinoza P., Selman F. J., Melnick J., 2009, A&A, 501, 563 Ferland G. J. et al., 2013, Rev. Mex. Astron. Astrofis., 49, 137

Geha M. et al., 2013, ApJ, 771, 29

Gennaro M. et al., 2018a, ApJ, 855, 20

Gennaro M. et al., 2018b, ApJ, 863, 38

Glover S. C. O., Mac Low M.-M., 2007, ApJS, 169, 239

Gouliermis D. A., 2012, Space Sci. Rev., 169, 1

Graus A. S. et al., 2019, preprint (arxiv:1901.05487)

Guszejnov D., Krumholz M. R., Hopkins P. F., 2016, MNRAS, 458, 673

Guszejnov D., Hopkins P. F., Ma X., 2017, MNRAS, 472, 2107

Guszejnov D., Hopkins P. F., Grudić M. Y., 2018, MNRAS, 477, 5139

Hennebelle P., Chabrier G., 2008, ApJ, 684, 395

Hennebelle P., Chabrier G., 2013, ApJ, 770, 150

Hopkins A. M., 2018, Publ. Astron. Soc. Aust., 35, 39

Hopkins P. F., 2012, MNRAS, 423, 2037

Hopkins P. F., 2015, MNRAS, 450, 53

Hopkins P. F., Kereš D., O norbe J., Faucher-Giguère C.-A., Quataert E., Murray N., Bullock J. S., 2014, MNRAS, 445, 581

Hopkins P. F. et al., 2018, MNRAS, 480, 800

Hußmann B., Stolte A., Brandner W., Gennaro M., Liermann A., 2012, A&A, 540, A57

Jappsen A.-K., Klessen R. S., Larson R. B., Li Y., Mac Low M.-M., 2005, A&A 435, 611

Knollmann S. R., Knebe A., 2009, ApJS, 182, 608

Kroupa P., 2002, Science, 295, 82

Kruijssen J. M. D., 2009, A&A, 507, 1409

Krumholz M. R., 2011, ApJ, 743, 110

Krumholz M. R., 2014, Phys. Rep., 539, 49

Larson R. B., 2005, MNRAS, 359, 211

Leitherer C. et al., 1999, ApJS, 123, 3

Lodieu N., de Wit W.-J., Carraro G., Moraux E., Bouvier J., Hambly N. C., 2011, A&A, 532, A103

Lodieu N., Deacon N. R., Hambly N. C., 2012a, MNRAS, 422, 1495

Lodieu N., Deacon N. R., Hambly N. C., Boudreault S., 2012b, MNRAS, 426, 3403

Low C., Lynden-Bell D., 1976, MNRAS, 176, 367

Luhman K. L., 2007, ApJS, 173, 104

Ma X. et al., 2018, MNRAS, 478, 1694

Martín-Navarro I., La Barbera F., Vazdekis A., Falcón-Barroso J., Ferreras I., 2015a, MNRAS, 447, 1033

Martín-Navarro I., La Barbera F., Vazdekis A., Ferré-Mateu A., Trujillo I., Beasley M. A., 2015b, MNRAS, 451, 1081

Martín-Navarro I. et al., 2015c, ApJ, 806, L31

Maschberger T., 2013, MNRAS, 429, 1725

Masunaga H., Inutsuka S.-.I., 2000, ApJ, 531, 350

Offner S. S. R., 2016, in Jablonka P., André P., van der Tak F., eds, Proc. IAU Symp. Vol. 315, From Interstellar Clouds to Star-Forming Galaxies: Universal Processes?. Int. Astron. Un., Paris. p. 73

Offner S. S. R., Clark P. C., Hennebelle P., Bastian N., Bate M. R., Hopkins P. F., Moraux E., Whitworth A. P., 2014, in Beuther H., Klessen R. S., Dullemond C. P., Henning T., eds, Protostars and Planets VI. University of Arizona Press, Tucson, p. 53

Oliveira J. M., Jeffries R. D., van Loon J. T., 2009, MNRAS, 392, 1034

Padoan P., Nordlund Å., 2002, ApJ, 576, 870

Padoan P., Nordlund Å., 2011, ApJ, 741, L22

Paresce F., De Marchi G., 2000, ApJ, 534, 870

Pe na Ramírez K., Béjar V. J. S., Zapatero Osorio M. R., Petr-Gotzens M. G., Martín E. L., 2012, ApJ, 754, 30

Posacki S., Cappellari M., Treu T., Pellegrini S., Ciotti L., 2015, MNRAS, 446, 493

Smith R. J., 2014, MNRAS, 443, L69

Smith R. J., Lucey J. R., Conroy C., 2015, MNRAS, 449, 3441

Smith R. J., Lucey J. R., Edge A. C., 2017, MNRAS, 471, 383

Sonnenfeld A., Treu T., Marshall P. J., Suyu S. H., Gavazzi R., Auger M. W., Nipoti C., 2015, ApJ, 800, 94

Sung H., Bessell M. S., 2010, AJ, 140, 2070

Treu T., Auger M. W., Koopmans L. V. E., Gavazzi R., Marshall P. J., Bolton A. S., 2010, ApJ, 709, 1195

van Dokkum P. G., Conroy C., 2010, Nature, 468, 940

van Dokkum P. G., Conroy C., 2011, ApJ, 735, L13

Villaume A., Brodie J., Conroy C., Romanowsky A. J., van Dokkum P., 2017, ApJ, 850, L14

Whitworth A. P., Boffin H. M. J., Francis N., 1998, MNRAS, 299, 554

Wiersma R. P. C., Schaye J., Smith B. D., 2009, MNRAS, 393, 99 Zhou S. et al., 2018, MNRAS, 485, 5256

APPENDIX A: EFFECTS OF INDIVIDUAL CONSTRAINTS ON THE ALLOWED IMF EXPONENTS

In this appendix we show how the individual constraints affect the available parameter space for the IMF models defined by equation (3). Fig. A1 shows that the requirement for low

galactic scatter in the μ characteristic IMF mass drastically reduce the available exponents. Requiring that old stellar populations have similar or slightly more massive μ further restricts this space, especially in the case of the metallicity exponent γ_Z . Meanwhile, Fig. A2 shows that although a large volume

of parameter space would reproduce the inferred bottom-heavy IMF in ETGs, few models in the literature can do so and only in case of using canonical ULIRG values instead of simulated galaxies.

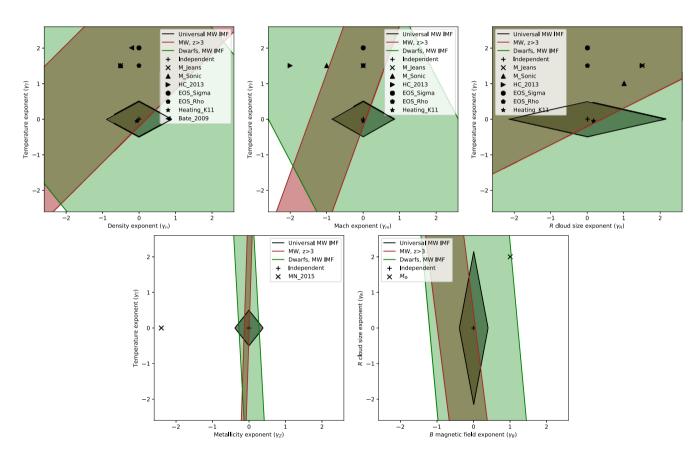


Figure A1. Power-law exponents for the density, temperature, metallicity, Mach-number, size, and magnetic field in equation (3) that satisfy IMF universality in the MW and nearby dwarf galaxies (see Table 3 for details on constraints and Table 1 for the simulated galaxies). The shaded regions show the exponents that satisfy the different constraints, while symbols represent models from the literature (Table 4). From these we can infer that there is a fairly limited volume in the model space of equation (3) that satisfies MW universality, the constraints are especially stringent on the γ_Z metallicity exponent.

4862

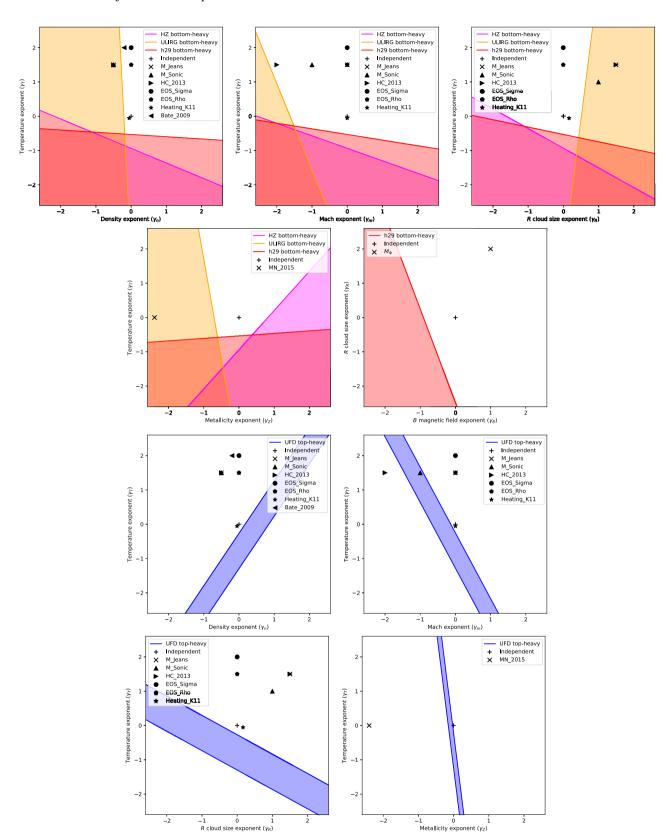


Figure A2. Power-law exponents for equation (3) that reproduce the inferred bottom-heavy IMF for early-type galaxies (top two rows) and the inferred top-heavy IMF for ultrafaint dwarf galaxies (bottom two rows), similar to Fig. A1. Note that UFD proxy (m10xf_14706) as well as one of our simulated early-type galaxies (z5m12c) did not include magnetic fields, hence they provide no constraints on the γ_B exponent. It is clear that the models in the literature fail to reproduce the bottom-heavy IMF for simulated galaxies, but some can satisfy the constraints when using canonical ULIRG values.

This paper has been typeset from a TEX/IATEX file prepared by the author.