



## Research paper

The atmospheric impact of the reaction of N<sub>2</sub>O with NO<sub>3</sub>: A theoretical study

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## HIGHLIGHTS

- Nitrous oxide is a greenhouse gas and a potential O<sub>3</sub>-depleting substance.
- OH, Cl, and NO<sub>3</sub> do not react fast enough with N<sub>2</sub>O.
- These reactions are too slow to be observed experimentally.
- A reaction of NO<sub>3</sub> with N<sub>2</sub>O might influence the atmospheric lifetime of N<sub>2</sub>O.
- Mechanism and kinetics of the NO<sub>3</sub> + N<sub>2</sub>O reaction have been studied for the first time.

## ABSTRACT

The reaction of N<sub>2</sub>O with NO<sub>3</sub> is studied for the first time using high-level quantum chemical calculations, followed by statistical rate coefficient estimations. Two reaction pathways giving NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub> and NO<sub>2</sub> + 2NO have been explored. The formation of NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub> is exothermic by 30 kcal mol<sup>-1</sup> while that of NO<sub>2</sub> + 2NO is endothermic by 13 kcal mol<sup>-1</sup>. Both mechanisms have significant reaction barriers, and the reaction rate constants are very low: about  $6 \times 10^{-43}$  cm<sup>3</sup> s<sup>-1</sup> at 298 K. Therefore, this reaction is not expected to affect the lifetime of N<sub>2</sub>O in the atmosphere.

## 1. Introduction

Nitrous oxide, N<sub>2</sub>O, is a major greenhouse gas and its emissions are now the largest of all ozone layer depleting gases [1]. One of the key reasons for these two influences is the long atmospheric lifetime of N<sub>2</sub>O (roughly 120 years), which appears not to have any appreciable loss pathway in the troposphere where it is emitted. If there were any reactions in the troposphere that lead to destruction of N<sub>2</sub>O, the atmospheric lifetime of this species would be altered even if the reaction were slow. Therefore, a search for potential slow reactions of tropospheric free radicals with N<sub>2</sub>O is of interest.

It is not always easy to directly measure the rate coefficients for very slow radical-molecule reactions due to various experimental difficulties. These include the need to avoid impurity reactions and unwanted side reactions, and the need to use of very large concentrations of N<sub>2</sub>O with potential deleterious effects on the ability to detect the radicals. Therefore, assessing the feasibility of slow reactions via theoretical

calculations represents an attractive alternative, especially for small molecules. Quantum chemistry calculations have advanced to a stage that it is now fairly straightforward to obtain energetics that are accurate to a few tenths of kcal mol<sup>-1</sup>. In addition, approaches for calculating rate coefficients using the mapped out potential energy surfaces have advanced. Therefore, we have undertaken a study of the potentially important atmospheric reaction of NO<sub>3</sub> with N<sub>2</sub>O. The abundance of NO<sub>3</sub>, though highly variable, is sufficiently large that this reaction could have an impact on the lifetime of N<sub>2</sub>O if the rate coefficient were of the order of  $10^{-20}$  cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup>, or larger.

Previously, Cantrell et al. [2] attempted to measure this rate coefficient and obtained an upper limit of  $2 \times 10^{-17}$  cm<sup>3</sup> molecule<sup>-1</sup> s<sup>-1</sup>. As can be inferred from the preceding, this is not a sufficiently stringent upper limit to dismiss the possibility that this reaction contributes meaningfully to the loss of N<sub>2</sub>O in the atmosphere. Therefore, better estimates are needed. A computational estimation of the rate coefficient for the reaction of NO<sub>3</sub> with N<sub>2</sub>O is the goal of this focused study.

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### 1.1. Quantum chemical calculations

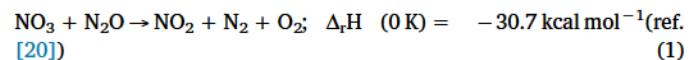
The title reaction involves seven heavy atoms, so high-accuracy HEAT [3–5] calculations would be extremely time consuming; consequently, a compromise is made here. This work is based in part on calculations done with the composite G3B3 method [6], which is a variation of G3 theory [7]. G3B3 [6] uses geometries and harmonic zero-point vibrational corrections obtained at the B3LYP/6-31G(d) level of theory, followed by a series of single-point energy calculations done with methods including QCISD(T)/6-31G(d), MP4/6-31+G(d), MP4/6-31G(2df,p), and MP2/G3Large in order to estimate the QCISD(T) level at the complete basis set limit. In addition, empirical high-level corrections (HLC) and spin-orbit corrections [6] are also included [7]. It is expected that the G3B3 calculations provide (roughly) chemical accuracy (i.e., within 1–2 kcal mol<sup>−1</sup>) for relative energies. As can be seen in Fig. 1, such a level of accuracy is indeed achieved for the reaction enthalpies of two main pathways, and it is expected that this accuracy will not be seriously degraded for transition state (TS) structures. Moreover, intrinsic reaction coordinate (IRC) [8–10] calculations were also performed in order to verify that the located transition state structures properly connect reactant(s) and products. It should be mentioned that NO<sub>3</sub> is a notoriously difficult molecule for both experiments and theory. DFT calculations with B3LYP give a C<sub>2v</sub> equilibrium geometry for NO<sub>3</sub>, although the experimentally determined ground state average geometry is D<sub>3h</sub>. Although a comparison of equilibrium geometries with experimental structures is fraught with difficulties, especially for a system of this type, it is true that the potential surface for NO<sub>3</sub> near the minimum is extremely flat. Hence, many methods give symmetric structures while many others give broken symmetry structures. However, the energetics are largely insensitive, owing to the flatness of the potential. The G3B3 and IRC calculations were done using the Gaussian 09 program suite [11].

In addition to the G3B3 calculations, we have also used high-level coupled-cluster calculations to characterize key stationary points (see Fig. 1) for the purpose of chemical kinetics analysis. First, geometries were optimized using the coupled-cluster method with single, double, and perturbative triple excitations (CCSD(T)) [12–14] in combination with the atomic natural orbital double-zeta (ANO0) basis set [15,16],

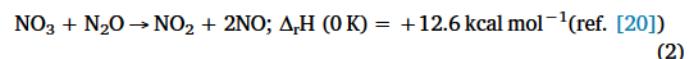
followed by harmonic vibrational analyses in order to check if they are real minima or first-order saddle points. Second, the ANO0 geometries and Hessian matrix obtained above were used for reoptimizing with a larger triple-zeta (ANO1) basis set [15,16]. Third, single-point energies were refined using the same CCSD(T) method, but with Dunning's quadruple-zeta basis set [17], cc-pVQZ. Finally, additional minor corrections have been applied for the effects of scalar relativity, the diagonal Born–Oppenheimer correction (DBOC), and spin-orbit coupling. As can be seen in Fig. 1, both the simple G3B3 and more elaborate CCSD(T)/cc-pVQZ calculations agree well (within 1–2 kcal mol<sup>−1</sup>) with one another, although the CCSD(T) values are systematically about 1–2 kcal mol<sup>−1</sup> lower. A similar difference has been found in the reaction of OH with N<sub>2</sub>O [18]. All CCSD(T) calculations are done using the CFOUR quantum chemistry package [19].

### 1.2. Reaction mechanisms and energetics

Two pathways have been characterized for the thermal reaction of NO<sub>3</sub> radical with N<sub>2</sub>O (with the reaction enthalpies obtained from published data (ref. [20])). The first:



(hereafter defined as pathway 1) is very exothermic [20], and leads to the formation of three stable molecules, NO<sub>2</sub>, N<sub>2</sub> and O<sub>2</sub>. The second pathway (hereafter defined as pathway 2)



is endothermic [20], resulting in NO<sub>2</sub> + 2NO, and therefore is highly unlikely to occur under atmospheric conditions. The G3B3 calculations give −29.9 and 12.9 kcal mol<sup>−1</sup> for reactions (1) and (2), respectively, which agree within 1 kcal mol<sup>−1</sup> with both the CCSD(T) calculations and well established thermochemical values [20]. The optimized geometries of various species are given in the supplementary material, while those of key transition states and intermediates along the reaction coordinate obtained with the DFT-B3LYP method are shown in Fig. 1. The calculated relative energies including zero-point energy corrections

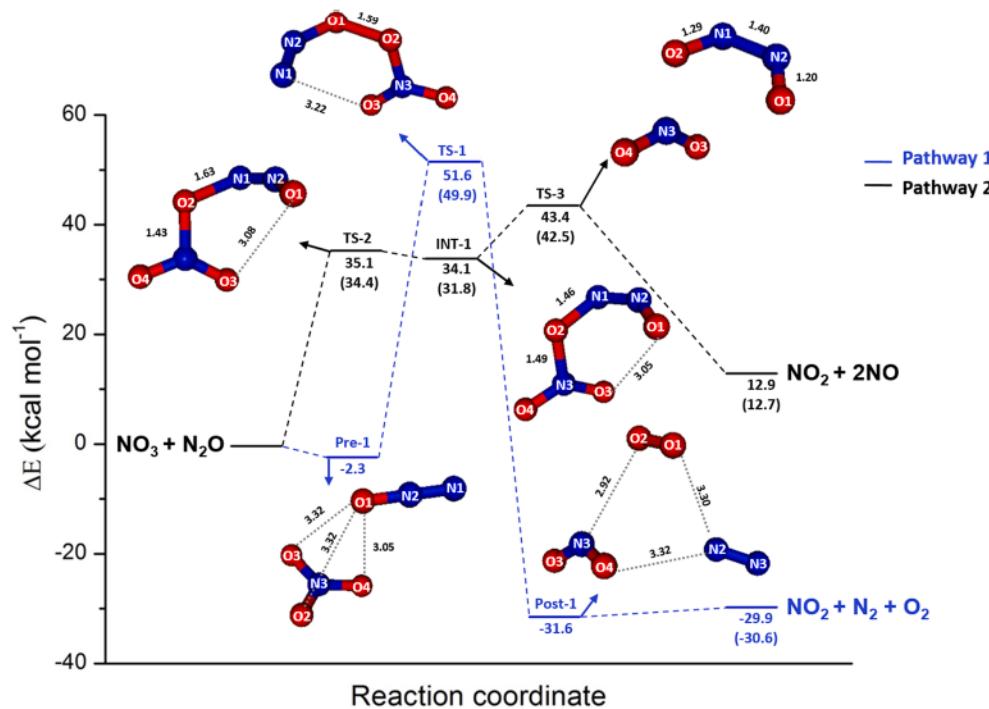


Fig. 1. The potential energy surface for the reaction of NO<sub>3</sub> radical with N<sub>2</sub>O calculated using the G3B3 method. The energy values given in parenthesis are obtained at the CCSD(T)/cc-pVQZ level of theory. The black and blue lines correspond to the endothermic and exothermic pathways respectively. The bond lengths are given in Å. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 1

Calculated relative energies (kcal mol<sup>-1</sup>) of various species involved in the reaction of NO<sub>3</sub> with N<sub>2</sub>O for the exothermic and endothermic channels.

NO <sub>3</sub> + N <sub>2</sub> O → NO <sub>2</sub> + N <sub>2</sub> + O <sub>2</sub>			NO <sub>3</sub> + N <sub>2</sub> O → NO <sub>2</sub> + 2NO		
Species	G3B3	CCSD(T)/cc-pVQZ	Species	G3B3	CCSD(T)/cc-pVQZ
Pre-1	-2.3	n/a	TS-2	35.1	34.4
TS-1	51.6	49.9	INT1	34.1	31.8
Post-1	-31.6	n/a	TS-3	43.4	42.5
NO <sub>2</sub> + N <sub>2</sub> + O <sub>2</sub>	-29.9	-30.6	NO <sub>2</sub> + 2NO	12.9	12.7
(-30.72 ± 0.1) <sup>a)</sup>		(-30.72 ± 0.1) <sup>a)</sup>		(12.60 ± 0.1) <sup>a)</sup>	

<sup>a)</sup> Taken from ATcT, version 1.122d, 2019 [31].

for various species are given in Table 1.

For pathway 1 as presented in Fig. 1, NO<sub>3</sub> attacks the oxygen end of N<sub>2</sub>O. Initially, a weakly bound pre-reactive complex is formed (Pre-1) with a binding energy of -2.3 kcal mol<sup>-1</sup> as calculated with G3B3. This complex then proceeds to abstract an O atom through TS-1 leading to Post-1. The barrier height of TS-1 is calculated to be 51.6 and 49.9 kcal mol<sup>-1</sup> using the G3B3 and CCSD(T) methods, respectively. Post-1, a post-reaction complex with a relative energy of -31.6 kcal mol<sup>-1</sup>, when produced, should rapidly dissociate at temperatures relevant to the atmosphere to the final products, NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub> driven by the very large entropy increase, together with a negligible barrier and low endothermicity (~1 kcal mol<sup>-1</sup>). According to Fig. 1, TS-1 is the key saddle point, because passing over (or through) TS-1 is the rate-determining step. Yet, TS-1 has a large spin contamination (<S<sup>2</sup>>) of 1.5. So, in addition to UHF-CCSD(T) method, ROHF-CCSD(T) was also used for optimization. A comparison of two optimized geometries are displayed in Fig. 2 with the ROHF-CCSD(T) values shown in parentheses. Inspection of Fig. 2 shows that the two geometries are in good agreement: there are small differences of 0.015 Å for the O–O bond length and of 0.4 degrees for the ∠NOO angle. However, there is a difference of 2 kcal mol<sup>-1</sup> (not shown in Fig. 1) for the calculated barrier heights, where the ROHF-CCSD(T) method gives a lower value. Because of this, we take the 49.9 kcal mol<sup>-1</sup> barrier height from ROHF-CCSD(T)/cc-pVQZ, but recognize that it is associated with a relatively large uncertainty (up to perhaps 3–5 kcal mol<sup>-1</sup>).

For pathway 2 as displayed in Fig. 1, NO<sub>3</sub> can attack the nitrogen end of N<sub>2</sub>O via TS-2 leading to the formation of an intermediate adduct, INT1. The energy barrier of TS-2 is calculated to be 35.1 and 34.4 kcal mol<sup>-1</sup> using the G3B3 and UHF-CCSD(T) methods, respectively. INT1 lies a few kcal mol<sup>-1</sup> lower than TS-2. There are two possible pathways starting at INT1: it either dissociates via TS-2 back to

the initial reactants, NO<sub>3</sub> + N<sub>2</sub>O, or decomposes further via TS-3 to give products, NO<sub>2</sub> + 2NO. Given that the redissociation step faces a much lower barrier, it is expected to be dominant. As a result, the rate-determining step in this scenario is to surmount TS-3.

### 1.3. Statistical rate coefficient calculations

#### Pathway 1: NO<sub>3</sub> + N<sub>2</sub>O → TS-1 → NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub>

As seen in Fig. 1, when formed from the association of NO<sub>3</sub> with N<sub>2</sub>O, Pre-1 rapidly re-dissociates back to reactants because the subsequent O-abstraction step must overcome a very high barrier. As a result, the canonical equilibrium, NO<sub>3</sub> + N<sub>2</sub>O ⇌ Pre-1, is quickly established before the following O-abstraction can occur. In addition, Post-1 – as produced by passing over TS-1 – has substantial internal energy, and thus rapidly decomposes to products, NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub>. Because of this, the influences of Pre-1 and Post-1 on kinetics of the reaction are negligible (for example, it makes a difference of less than 5% at any atmospheric relevant temperature, see the Supplementary Material). Consequently, a kinetics scheme in this scenario can be simplified to: NO<sub>3</sub> + N<sub>2</sub>O → TS-1 → NO<sub>2</sub> + N<sub>2</sub> + O<sub>2</sub>, which does not go through a long-lived intermediate, and therefore is expected to be pressure-independent. Thermal rate constants can be calculated using transition state theory (TST) [21,22] at the high-pressure limit:

$$k_{\text{TST}}(T) = \frac{\sigma}{h} \times \frac{Q_{\text{tr}}^{\neq} Q_e^{\neq}}{Q_{\text{NO}_3}^{\text{re}} \cdot Q_{\text{N}_2\text{O}}^{\text{re}}} \times \sum_{J=0}^{\infty} (2J+1) \int_0^{\infty} G_{\text{rv}}^{\neq}(E, J) \exp(-E/k_B T) dE \quad (3)$$

where h is Planck's constant, k<sub>B</sub> is Boltzmann's constant, and  $\sigma = 12$  is the reaction path degeneracy. For the latter, note that rotational symmetry numbers are 6, 1, and 1, respectively, for NO<sub>3</sub>, N<sub>2</sub>O, and TS-1. In addition, TS-1 is chiral and therefore has a mirror image. Q<sub>NO<sub>3</sub></sub><sup>re</sup> and Q<sub>N<sub>2</sub>O</sub><sup>re</sup> are the complete partition functions for NO<sub>3</sub> and N<sub>2</sub>O, respectively. Q<sub>tr</sub> is the translational partition function and Q<sub>e</sub> is the electronic partition function (the superscripts "re" and "≠" designate reactants and transition state, respectively). J is the total angular momentum quantum number. G<sub>rv</sub><sup>≠</sup> is the sum of rovibrational states for TS-1 obtained by convoluting vibrational and rotational quantum states [23]:

$$G_{\text{rv}}^{\neq}(E, J) = \int_0^E G_v^{\neq}(E - E_r) \rho_r^{\neq}(E_r) dE_r \quad (4)$$

where  $\rho_r^{\neq}(E_r)$  is the density of states at energy E<sub>r</sub>. It is assumed that all stationary points on the potential energy surface are approximated by a rigid-rotor symmetric top [23], for which rotational energy levels are given by Eq. (5):

$$E_r(J, K) = J(J+1)\bar{B} + (A - \bar{B})K^2, \text{ with } \bar{B} = \sqrt{B \cdot C} \text{ and } -J \leq K \leq +J \quad (5)$$

With A, B, and C as the rotational constants. It should be mentioned that tunneling effects with an asymmetric Eckart model [24] are included in computing G<sub>v</sub><sup>≠</sup> in Eq. (4) through Eq. (6) [25]:

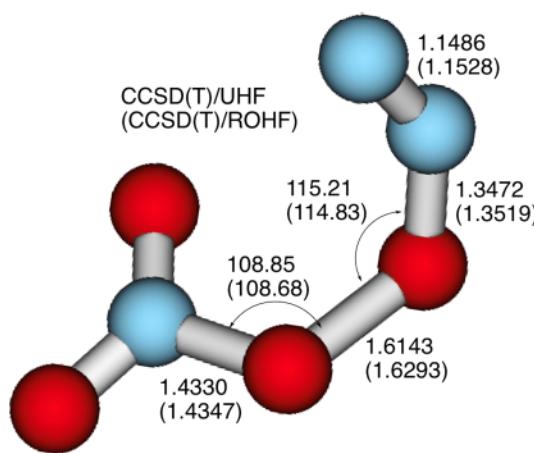


Fig. 2. Geometrical parameters of TS-1 are optimized using UHF-CCSD(T)/ANO1 and ROHF-CCSD(T)/ANO1 (parenthesis) levels of theory. The energy at the ROHF-CCSD(T)/ANO1 level of theory is 2 kcal mol<sup>-1</sup> lower than that of the other.

**Table 2**

Calculated thermal rate constants ( $\text{cm}^3 \text{molecule}^{-1} \text{s}^{-1}$ ) and tunneling corrections for the direct O-abstraction pathway 1:  $\text{NO}_3 + \text{N}_2\text{O} \rightarrow \text{N}_2 + \text{NO}_2 + \text{O}_2$ .

T (K)	CTST	CTST/Eckart	Tunneling correction
100	$2.82 \times 10^{-121}$	$6.04 \times 10^{-102}$	$2.15 \times 10^{19}$
125	$1.81 \times 10^{-99}$	$4.94 \times 10^{-87}$	$2.73 \times 10^{12}$
150	$6.54 \times 10^{-93}$	$5.38 \times 10^{-85}$	$8.23 \times 10^7$
175	$1.70 \times 10^{-74}$	$1.10 \times 10^{-69}$	$6.48 \times 10^4$
200	$1.14 \times 10^{-66}$	$6.14 \times 10^{-64}$	538
225	$1.44 \times 10^{-60}$	$5.16 \times 10^{-59}$	35.9
250	$1.12 \times 10^{-55}$	$1.14 \times 10^{-54}$	10.2
275	$1.15 \times 10^{-51}$	$6.20 \times 10^{-51}$	5.41
300	$2.58 \times 10^{-48}$	$9.56 \times 10^{-48}$	3.72
325	$1.79 \times 10^{-45}$	$5.18 \times 10^{-45}$	2.89
350	$4.96 \times 10^{-43}$	$1.20 \times 10^{-42}$	2.42
375	$6.56 \times 10^{-41}$	$1.39 \times 10^{-40}$	2.12
400	$4.78 \times 10^{-39}$	$9.10 \times 10^{-39}$	1.91

$$G_v^\#(E) = \int_0^E P(x) \text{Eckart} \times \rho_v^\#(E-x) dx \quad (6)$$

Here  $P(x)$  is the asymmetric Eckart tunneling probability.

The rate constants calculated as a function of temperature are shown in **Table 2**. Inspection of **Table 2** shows that  $k(T)$  increases sharply by about *sixty-three orders of magnitude* when temperature rises from 100 to 400 K, as expected for a reaction having a high reaction barrier. Because of the motion of the heavy oxygen atom, the tunneling correction also increases significantly with decreasing temperature: it is a factor of *ca.* 4 at 300 K and becomes about  $2 \times 10^{19}$  at 100 K; but, even such a large tunneling enhancement is insufficient to overcome the very small rate constant caused by the high barrier. At room temperature, the calculated rate constant is  $1 \times 10^{-47} \text{ cm}^3 \text{molecule}^{-1} \text{s}^{-1}$ , which corresponds to a  $\text{N}_2\text{O}$  lifetime of  $2 \times 10^{38} \text{ s}$  (about  $10^{31}$  years), assuming an atmospheric  $[\text{NO}_3] \approx 5 \times 10^8 \text{ molecules/cm}^3$  [26]. Note that the globally averaged  $\text{NO}_3$  abundance is ill-defined and would be much smaller. Even if this rate coefficient were ten orders of magnitude larger, it would not make any contribution to the atmospheric removal of  $\text{N}_2\text{O}$ . At the lower temperatures, the rate coefficient will be even smaller. Therefore (even allowing for considerable uncertainty in our calculations), it can be safely concluded that reaction pathway 1 has absolutely no relevance in the atmosphere; it is most certainly not a potential sink for  $\text{N}_2\text{O}$ .

#### Pathway 2: $\text{NO}_3 + \text{N}_2\text{O} \rightarrow \text{TS-2} \rightarrow \text{INT1} \rightarrow \text{TS-3} \rightarrow \text{NO}_2 + 2\text{NO}$

As shown in **Fig. 1**, the endothermic reaction pathway 2 to form  $\text{NO}_2 + 2\text{NO}$  from  $\text{NO}_3 + \text{N}_2\text{O}$  passes through an intermediate  $\text{INT1}$ , which does not have a long lifetime. Therefore, this pathway may depend on pressure. If it does, a master equation analysis is required to compute rate constants as functions of both temperature and pressure. To check this idea, we have computed thermal rate constants at two extreme conditions: the low- and high-pressure limits where analytical solutions can be obtained through Eq. (7) and Eq. (8), respectively.

At the low-P limit [27,28]:

$$k(T)_{P=0} = \frac{\sigma}{h} \times \frac{Q_{\text{tr}}^\# Q_e^\#}{Q_{\text{NO}_3}^{\text{re}} \cdot Q_{\text{N}_2\text{O}}^{\text{re}}} \times \sum_{J=0}^{\infty} (2J+1) \int_0^\infty G_{\text{eff}}^\#(E, J) \exp(-E/k_B T) dE \quad (7a)$$

Here  $G_{\text{eff}}^\#$  is the effective sum of rovibrational quantum states, which is given by Eq. (7b):

$$G_{\text{eff}}^\# = \frac{G_{\text{TS2}}^\#(E, J) \times G_{\text{TS3}}^\#(E, J)}{G_{\text{TS2}}^\#(E, J) + G_{\text{TS3}}^\#(E, J)} \quad (7b)$$

At the high-P limit [28]:

$$k(T)_{P=\infty} = \frac{k_2(T) \times k_3(T)}{k_{-2}(T) + k_3(T)} \quad (8)$$

**Table 3**

Calculated individual thermal rate constants (in the reaction pathway 2) at the high-pressure limit.

T (K)	$k_2(T)$ in $\text{cm}^3 \text{molecule}^{-1} \text{s}^{-1}$	$k_{-2}(T)$ in $\text{s}^{-1}$	$k_3(T)$ in $\text{s}^{-1}$
100	$3.38 \times 10^{-86}$	$4.89 \times 10^6$	$3.84 \times 10^{-7}$
125	$1.09 \times 10^{-71}$	$2.07 \times 10^7$	$1.60 \times 10^{-5}$
150	$6.32 \times 10^{-62}$	$6.44 \times 10^7$	$8.56 \times 10^{-4}$
175	$6.62 \times 10^{-55}$	$1.56 \times 10^8$	$3.59 \times 10^{-2}$
200	$1.30 \times 10^{-49}$	$3.14 \times 10^8$	$8.45 \times 10^{-1}$
225	$1.77 \times 10^{-45}$	$5.51 \times 10^8$	$1.13 \times 10^1$
250	$3.70 \times 10^{-42}$	$8.70 \times 10^8$	$9.63 \times 10^1$
275	$1.97 \times 10^{-39}$	$1.27 \times 10^9$	$5.74 \times 10^2$
300	$3.76 \times 10^{-37}$	$1.75 \times 10^9$	$2.59 \times 10^3$
325	$3.24 \times 10^{-35}$	$2.29 \times 10^9$	$9.38 \times 10^3$
350	$1.50 \times 10^{-33}$	$2.89 \times 10^9$	$2.85 \times 10^4$
375	$4.20 \times 10^{-32}$	$3.52 \times 10^9$	$7.49 \times 10^4$
400	$7.86 \times 10^{-31}$	$4.20 \times 10^9$	$1.75 \times 10^5$

where  $k_2(T)$  is the thermal rate constant for the forward step:  $\text{NO}_3 + \text{N}_2\text{O} \rightarrow \text{TS-2} \rightarrow \text{INT1}$ ,  $k_{-2}(T)$  is the thermal rate constant for the reverse process:  $\text{INT1} \rightarrow \text{TS-2} \rightarrow \text{NO}_3 + \text{N}_2\text{O}$ , and  $k_3(T)$  is the thermal rate constant for the formation of the products:  $\text{INT1} \rightarrow \text{TS-3} \rightarrow \text{NO}_2 + 2\text{NO}$ .

These three rate constants are computed using TST and presented in **Table 3**. Inspection of **Table 3** shows that the loss of  $\text{INT1}$  through  $\text{TS-2}$  is many orders of magnitude faster than via  $\text{TS-3}$ , so that  $\text{INT1}$  rapidly re-dissociates back to the initial reactants once it is produced. Consequently,  $\text{INT1}$  has a very short lifetime that is not compatible with thermalization via collisions with a third body such as  $\text{N}_2$  (and/or  $\text{O}_2$ ) under atmospheric conditions. In other words, this reaction pathway is pressure-independent (also supported by the numbers in **Table 4** where the difference between the low- and high-pressure rate constants is much smaller than 1%).

Comparison of the rate coefficient calculated at 298 K with the only reported value is useful. Cantrell et al. [2] measured the rate coefficient at  $P = 1 \text{ atm}$  in air. Their reported upper limit is consistent with our calculations, but it is to be noted that our value is many orders of magnitude smaller than their upper limit.

Inspection of **Table 4** shows that the calculated rate constants increase with temperature, as expected for a reaction having a high barrier. At room temperature, we obtain a rate constant of *ca.*  $6 \times 10^{-43} \text{ cm}^3 \text{molecule}^{-1} \text{s}^{-1}$  which, although five orders of magnitude faster than pathway 1, still leads to a calculated atmospheric lifetime of  $\text{N}_2\text{O}$  of *ca.*  $\sim 3 \times 10^{33} \text{ s}$  ( $> 10^{26}$  years). Thus, taken together with our results for Reaction (1), the contribution of  $\text{NO}_3$  reacting with  $\text{N}_2\text{O}$  to

**Table 4**

Calculated rate constants ( $\text{cm}^3 \text{molecule}^{-1} \text{s}^{-1}$ ) at the low- and high-pressure limits for the addition/elimination reaction pathway 2:  $\text{NO}_3 + \text{N}_2\text{O} \rightarrow \text{O}_2\text{NONNO} \rightarrow \text{NO}_2 + 2\text{NO}$ .

T (K)	Low-P limit <sup>a)</sup>	High-P limit <sup>b)</sup>	diff. (%) <sup>c)</sup>
100	$2.6460 \times 10^{-99}$	$2.6460 \times 10^{-99}$	0
125	$8.4208 \times 10^{-84}$	$8.4208 \times 10^{-84}$	0
150	$8.4022 \times 10^{-73}$	$8.4022 \times 10^{-73}$	0
175	$1.5226 \times 10^{-64}$	$1.5226 \times 10^{-64}$	0
200	$3.4888 \times 10^{-58}$	$3.4894 \times 10^{-58}$	$1.33 \times 10^{-2}$
225	$3.6344 \times 10^{-53}$	$3.6354 \times 10^{-53}$	$2.48 \times 10^{-2}$
250	$4.0874 \times 10^{-49}$	$4.0890 \times 10^{-49}$	$4.09 \times 10^{-2}$
275	$8.8806 \times 10^{-46}$	$8.8862 \times 10^{-46}$	$6.23 \times 10^{-2}$
300	$5.5558 \times 10^{-43}$	$5.5616 \times 10^{-43}$	$8.99 \times 10^{-2}$
325	$1.3233 \times 10^{-40}$	$1.3269 \times 10^{-40}$	$1.25 \times 10^{-1}$
350	$1.4762 \times 10^{-38}$	$1.4787 \times 10^{-38}$	$1.67 \times 10^{-1}$
375	$8.9186 \times 10^{-37}$	$8.9380 \times 10^{-37}$	$2.18 \times 10^{-1}$
400	$3.2716 \times 10^{-35}$	$3.2808 \times 10^{-35}$	$2.78 \times 10^{-1}$

<sup>a)</sup> Eq. (5) in the main text.

<sup>b)</sup> Eq. (6) in the main text.

<sup>c)</sup> Difference (%) =  $[k(T, P = \infty) - k(T, P = 0)] \times 100\% / k(T, P = \infty)$

the lifetime of  $\text{N}_2\text{O}$  in the atmosphere is completely negligible. Even local influences of  $\text{NO}_3$  on  $\text{N}_2\text{O}$ , and vice-versa, would be negligible. At lower atmospheric temperatures, the loss rate would be even smaller. It is of importance to compare the impact of  $\text{NO}_3$  on the lifetime of  $\text{N}_2\text{O}$  with that of  $\text{OH}$  (ref. [18]). As reported previously [18], at room temperature the pseudo first-order reaction rate constant of  $\text{N}_2\text{O}$  with  $\text{OH}$  is predicted to be about  $7 \times 10^{-22} \text{ s}^{-1}$ , which is about  $10^{12}$  times faster than the title reaction. So, it can be concluded that the influence of  $\text{NO}_3$  is entirely negligible.

It is worth noting that our calculated thermal rate constants may be in error by a few orders of magnitudes due to numerous possible errors in our kinetics calculations that involve barrier heights, RRHO model, tunneling corrections, and so on. Yet, the main conclusion obtained from this study is that the loss of  $\text{N}_2\text{O}$  through either pathway 1 or pathway 2 is utterly negligible in Earth's atmosphere or even on a geological timescale.

## 2. Discussion

As stated in the introduction,  $\text{N}_2\text{O}$  is one of the most important greenhouse gases, trailing only  $\text{CO}_2$  and  $\text{CH}_4$  in importance, and is believed to be the most important ozone-depleting substance emission of the 21st Century [1]. Its concentration in the atmosphere has risen steadily in modern times (a roughly linear rise of *ca.* 0.8 ppb  $\text{yr}^{-1}$  (since 1980 [29]), which has been attributed in large part to an increase in food production. If steps are not made to mitigate its anthropogenic sources (it also has natural sources), its importance as an atmospheric constituent will continue to increase. While it is known that  $\text{N}_2\text{O}$  can be destroyed by photolysis and via reaction with  $\text{O}(\text{¹D})$  atoms in the upper atmosphere – the modeling of which leads to its estimated atmospheric lifetime of 114 years [30] – other chemical sinks for the molecule are unknown. Accordingly, this is the second in a series of studies that investigate “slow” reactions of  $\text{N}_2\text{O}$ , done with an eye towards discovering potential chemical sinks that are relevant on a time scale of centuries to perhaps millenia. And this is also the second study to investigate a plausible reaction (the first being reaction of  $\text{N}_2\text{O}$  with the hydroxyl radical,  $\text{OH}$  [18]) to find that  $\text{N}_2\text{O}$  is exquisitely unreactive; atmospheric lifetimes found so far are so long that they are several orders of magnitude greater than that of the universe itself.

It seems likely that  $\text{N}_2\text{O}$  is resistant to all potential chemical loss mechanisms in the atmosphere (apart from reaction with  $\text{O}(\text{¹D})$  in the stratosphere), and that it is simply a highly unreactive atmospheric molecule like  $\text{CO}_2$ . One could rationalize this by recognizing that it is isoelectronic with  $\text{CO}_2$ ; decomposition reactions of the latter will lead to the most stable diatomic molecule (CO) while those of nitrous oxide lead to the second most stable diatomic molecule ( $\text{N}_2$ ). Hence, the fact that both molecules lack chemical sinks in the troposphere is not particularly surprising; the consequence of such a situation is that  $\text{N}_2\text{O}$  will continue to grow in importance as a greenhouse gas, and is a molecule that is “*here to stay*”.

## 3. Conclusions

Since it is very difficult to measure very slow free radical reactions, in this work we have estimated the rate coefficient for the potential reaction of  $\text{NO}_3$  with  $\text{N}_2\text{O}$  using high-level quantum chemical and statistical chemical kinetics calculations. We find that there are potentially two reaction pathways, both of which have substantial barriers. The following kinetics analysis shows that these reactions are extremely slow and negligible in Earth's atmosphere. It should be noted that uncertainties of even 5 kcal  $\text{mol}^{-1}$  do not alter the conclusions regarding the loss of  $\text{N}_2\text{O}$  from the troposphere since the upper limits for the rate coefficients are so small.

## Declaration of Competing Interest

Author declares that there is no conflicts of interest.

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## Appendix A. Supplementary material

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.cplett.2019.136605>. Theoretical methods, optimized geometries, and rovibrational parameters for various stationary points are provided.

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