



# The Curious Case of KOI 4: Confirming *Kepler*'s First Exoplanet Detection

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## Abstract

The discovery of thousands of planetary systems by *Kepler* has demonstrated that planets are ubiquitous. However, a major challenge has been the confirmation of *Kepler* planet candidates, many of which still await confirmation. One of the most enigmatic examples is KOI 4.01, *Kepler*'s first discovered planet candidate detection (as KOI 1.01, 2.01, and 3.01 were known prior to launch). Here we present the confirmation and characterization of KOI 4.01 (now Kepler-1658), using a combination of asteroseismology and radial velocities. Kepler-1658 is a massive, evolved subgiant ( $M_* = 1.45 \pm 0.06 M_\odot$ ,  $R_* = 2.89 \pm 0.12 R_\odot$ ) hosting a massive ( $M_p = 5.88 \pm 0.47 M_J$ ,  $R_p = 1.07 \pm 0.05 R_J$ ) hot Jupiter that orbits every 3.85 days. Kepler-1658 joins a small population of evolved hosts with short-period ( $\leq 100$  days) planets and is now the closest known planet in terms of orbital period to an evolved star. Because of its uniqueness and short orbital period, Kepler-1658 is a new benchmark system for testing tidal dissipation and hot Jupiter formation theories. Using all four years of the *Kepler* data, we constrain the orbital decay rate to be  $\dot{P} \leq -0.42 \text{ s yr}^{-1}$ , corresponding to a strong observational limit of  $Q'_* \geq 4.826 \times 10^3$  for the tidal quality factor in evolved stars. With an effective temperature of  $T_{\text{eff}} \sim 6200 \text{ K}$ , Kepler-1658 sits close to the spin-orbit misalignment boundary at  $\sim 6250 \text{ K}$ , making it a prime target for follow-up observations to better constrain its obliquity and to provide insight into theories for hot Jupiter formation and migration.

**Key words:** asteroseismology – planets and satellites: individual (KOI 4.01) – stars: individual (Kepler-1658) – techniques: photometric, radial velocities, spectroscopic

**Supporting material:** machine-readable tables

## 1. Introduction

The *Kepler* mission (Borucki et al. 2010; Koch et al. 2010; Borucki 2016) revolutionized the field of exoplanetary science. Pre-*Kepler* exoplanet discoveries were biased toward close-in giant planets (hot Jupiters), a planet type absent from our own solar system. However, *Kepler* later revealed that hot Jupiters are in fact rare, and smaller sub-Neptune-sized planets are ubiquitous in inner planetary systems (Howard et al. 2012; Dressing & Charbonneau 2013; Petigura et al. 2013; Gaidos & Mann 2014; Morton & Swift 2014; Silburt et al. 2015).

When the *Kepler* spacecraft launched in 2009 March, three planets in the *Kepler* field were already known from ground-based transit observations (O'Donovan et al. 2006; Pál et al. 2008; Bakos et al. 2010). These targets were designated the first three KOI (*Kepler* object of interest) numbers, making KOI 4.01 *Kepler*'s first new planet candidate (PC). The initial

classification in the *Kepler* Input Catalog (KIC; Brown et al. 2011) for KOI 4 implied a 1.1 solar radius ( $R_\odot$ ) main-sequence star with an effective temperature ( $T_{\text{eff}}$ ) of 6240 K (Brown et al. 2011). Based on a primary transit depth of 0.13%, this stellar classification implied that KOI 4 is orbited by a Neptune-sized planet. However, because a deep secondary eclipse was observed, KOI 4.01 was marked as a false positive (FP) in early *Kepler* KOI catalogs, since a secondary eclipse would not be observable for a Neptune-sized planet orbiting a main-sequence star.

The NASA Exoplanet Archive reveals a more detailed picture of the complex vetting history of *Kepler*'s first exoplanet candidate. KOI 4.01 was not listed in the first KOI catalog (Borucki et al. 2011a) but appeared as a moderate probability candidate in the second KOI catalog (Borucki et al. 2011b), with the host star noted as a rapid rotator ( $v \sin i = 40 \text{ km s}^{-1}$ ). In the third catalog, Batalha et al. (2013) listed KOI 4.01 as a PC but it was marked back to a FP in the fourth catalog (Burke et al. 2014), likely due to the secondary eclipse.

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The fifth (Rowe et al. 2015) and sixth (Mullally et al. 2015) catalogs did not disposition existing KOIs within certain parameter spaces. The seventh catalog (Coughlin et al. 2016) was the first fully uniform catalog using the Robovetter pipeline, marking 237 KOIs that were previously FPs back to PCs using updated stellar parameters, including KOI 4. In the final catalog (Thompson et al. 2018), the Robovetter also dispositioned it as a PC. Until now, *Kepler's* first new planet candidate has awaited confirmation as a genuine planet detection.

Systems like KOI 4.01 are interesting because giant planets at short orbital periods ( $P < 100$  days) are rare around subgiant stars (e.g., Johnson et al. 2007, 2010; Reffert et al. 2015; Lillo-Box et al. 2016; Veras 2016), although the reason for this is still a topic of debate. On the one hand, this may be related to the stellar mass. Subgiant host stars are thought to be more massive than main-sequence stars targeted for planet detection. A higher mass could shorten the lifetime of the protoplanetary disk and lead to fewer short-period giant planets orbiting these type of stars (e.g., Burkert & Ida 2007; Kretke et al. 2009). Other authors have suggested that subgiants have fewer short-period planets because these objects may get destroyed by tidal evolution, which is likely stronger for more evolved stars (e.g., Villaver & Livio 2009; Schlaufman & Winn 2013). Distinguishing between those scenarios is further complicated by the fact that it is challenging to derive the stellar masses of evolved stars (Lloyd 2011, 2013; Johnson et al. 2013; Ghezzi et al. 2018).

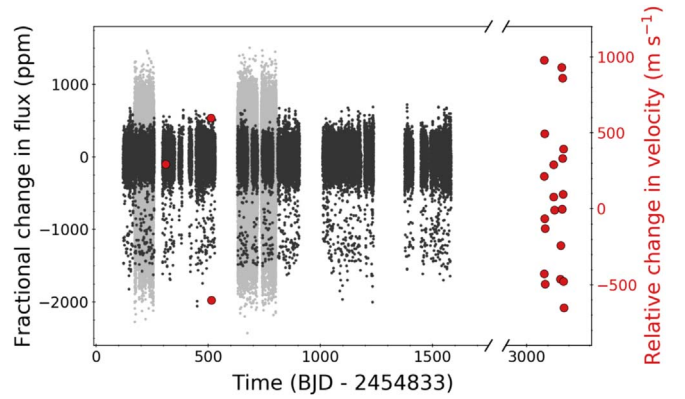
Here we confirm and characterize KOI 4.01, hereafter Kepler-1658, using a combination of asteroseismology and spectroscopic follow-up observations. Due to its short orbital period, Kepler-1658 b is an ideal target to constrain the role of tides around more evolved stars. In addition, we are able to constrain the stellar mass and other stellar parameters to high precision and accuracy by analyzing the stellar oscillations and comparing these to stellar models. We conclude by discussing future observations that could provide insight for theories of hot Jupiter formation and migration.

## 2. Observations

### 2.1. Kepler Photometry

The *Kepler* spacecraft had two observing modes: long cadence (29.4 minutes; Jenkins et al. 2010) and short cadence (58.85 s; Gilliland et al. 2010b). In the nominal *Kepler* mission most *Kepler* targets were observed in long cadence, while 512 short-cadence slots remained for select targets. Short-cadence observations are important for the asteroseismology of dwarfs and subgiants, whose oscillations occur on timescales faster than 30 minutes (Gilliland et al. 2010a; Chaplin & Miglio 2013).

Decisions on which targets to observe in short cadence were made on a quarter-by-quarter basis. In particular, once planet candidates were detected and assigned a KOI number, targets were put on short cadence if the probability of detecting oscillations was deemed as significant (Chaplin et al. 2011a). Kepler-1658 was observed in long cadence for most of the mission aside from three quarters, while it was only observed in short cadence in Quarters 2, 4, 7, and 8, for a total of 213.7 days (Figure 1).



**Figure 1.** *Kepler* photometry and radial velocity observations for KOI 4.01. Long-cadence photometric data are shown in dark gray while short cadence are shown in light gray. Three high-resolution spectra (red points) were initially taken of KOI 4.01 during the mission before it was marked as a false positive. This was followed by a break of 7 yr before it was re-observed by our team in 2017.

### 2.2. Imaging

Kepler-1658 was observed by Robo-AO, a robotic, visible light, laser adaptive optics (AO) imager that searched for nearby companions that could potentially contaminate target light curves (Law et al. 2014; Baranec et al. 2016; Ziegler et al. 2017). Law et al. (2014) reported a nearby companion to Kepler-1658 at a separation of  $3''.42$  and a contrast of 4.46 mag in the LP600 filter, which has a similar wavelength coverage to the *Kepler* bandpass. In addition to Robo-AO, the *Kepler* UKIRT survey reported a detection of the same companion with a contrast of 4.23  $\Delta$ mag in the J-band (Furlan et al. 2017). Gaia Data Release 2 reported parallaxes of  $1.24 \pm 0.03$  mas and  $0.75 \pm 0.05$  mas corresponding to Kepler-1658 and its companion, respectively (Lindgren et al. 2016). Therefore, we conclude that the two targets are not physically associated.

### 2.3. Spectroscopy and Radial Velocities

Initial spectroscopic follow-up of Kepler-1658 was obtained by the *Kepler* Follow-up Observing Program, including the High Resolution Echelle Spectrometer (HIRES; Vogt 1994) on the 10 m telescope at Keck Observatory (Maunakea, Hawaii), the Fibre-fed Echelle Spectrograph (FIES; Djupvik & Andersen 2010) on the 2.5 m Nordic Optical Telescope at the Roque de los Muchachos Observatory (La Palma, Spain), and the Tillinghast Reflector Echelle Spectrograph (TRES; Fűrész 2008) on the 1.5 m Tillinghast reflector at the F. L. Whipple Observatory (Mt. Hopkins, Arizona). The observing notes archived at the *Kepler* Community Follow-up Observing Program<sup>17</sup> show that these spectra confirmed that Kepler-1658 is a rapid rotator which, combined with the detection of the close companion (see the previous section), discouraged further follow-up observations to confirm the planet candidate.

Following the asteroseismic reclassification of the host star (see the next section), we initiated an intensive radial velocity (RV) follow-up program using TRES, a fiber-fed échelle spectrograph spanning the spectral range of 3900–9100 Å with a resolving power of  $R \sim 44,000$ . We obtained 23 spectra with TRES between UT 2009 November 8 and 2017 September 13 using the medium  $2''/3$  fiber. The spectra were reduced and

<sup>17</sup> <https://exofop.ipac.caltech.edu/kepler/>

**Table 1**  
TRES Radial Velocity Observations

Time (BJD TDB)	RV (m s <sup>-1</sup> )	$\sigma_{RV}$ (m s <sup>-1</sup> )	BS <sup>1</sup> (m s <sup>-1</sup> )	$\sigma_{BS}$ (m s <sup>-1</sup> )
2455143.566982	-648.64	261.20	-11.1	205.7
2455343.873508	-344.33	223.72	-22.9	138.1
2455345.873597	-1542.39	153.02	244.2	72.1
2457914.843718	0.00	155.26	-114.2	41.6
2457915.936919	-756.57	165.32	-122.5	64.7
2457916.865409	-1391.09	159.21	220.9	58.9
2457917.929198	-1031.39	103.84	-5.9	70.9
2457918.888799	-480.41	155.26	-87.2	52.9
2457919.869505	-1095.83	109.08	108.9	59.6
2457920.859134	-1458.12	187.52	238.5	95.2
2457960.932038	-679.80	156.99	-40.2	136.6
2457961.930294	-891.62	232.50	26.1	127.6
2457965.808860	-977.16	131.20	-142.2	61.5
2457993.735605	-1424.46	200.28	21.1	96.0
2457994.753312	-1205.20	190.75	168.0	50.2
2457999.668199	-48.17	137.98	-223.2	68.9
2458001.720710	-971.08	146.58	-48.9	89.2
2458002.718939	-640.20	127.69	-98.9	60.0
2458003.661261	-118.49	103.28	-274.6	85.1
2458006.701108	-873.64	137.11	66.8	77.7
2458007.747359	-578.74	130.97	-45.6	66.9
2458008.800582	-1439.71	156.00	-6.5	74.5
2458009.717813	-1611.87	145.55	149.4	40.9

**Note.**<sup>a</sup> Line bisector spans and uncertainties, as discussed in Section 2.3.

(This table is available in machine-readable form.)

extracted as outlined in Buchhave et al. (2010). The average exposure time of  $\sim 1800$  s, corresponding to a mean signal-to-noise ratio (S/N) per resolution element of  $\sim 53$  at the peak of the continuum near the Mg b triplet at 519 nm. We used the strongest S/N spectrum as a template to derive relative RVs by cross-correlating the remaining spectra order-by-order against the template, which is given a relative velocity of  $0 \text{ km s}^{-1}$ , by definition.

Monitoring of standard stars with TRES shows that the long-term zero-point of the instrument is stable to within  $\pm 5 \text{ m s}^{-1}$  over recent years. Due to mechanical and optical upgrades to TRES in the early years, there were major shifts in the instrumental zero-point of the velocity system. The correction for the 2009 observation was  $-115 \text{ m s}^{-1}$  and the correction for both 2010 observations was  $-82 \text{ m s}^{-1}$ .

A bisector analysis was performed on the TRES spectra as described in Torres et al. (2007) to check for asymmetries in the line profile which could be indicative of an unresolved eclipsing binary. The line bisector spans (BS) showed no correlation with the measured RVs and are small compared to the orbital semi-amplitude. All of the relative velocities, bisector values, and associated uncertainties are listed in Table 1.

**3. Host Star Characterization***3.1. Atmospheric Parameters*

Atmospheric parameters were derived from the TRES and FIES spectra using the stellar parameter classification code (SPC; see Buchhave et al. 2012). We adopted a weighted mean of the solutions to the individual spectra, yielding

**Table 2**  
Stellar Parameters

Parameter	KIC 3861595
Basic Properties	
2MASS ID	19372557+3856505
R.A.	19 37 25.575
Decl.	+38 56 50.515
Magnitude ( <i>Kepler</i> )	10.195
Magnitude ( <i>V</i> )	11.62
Magnitude ( <i>TESS</i> )	10.98
Spectroscopy	
Effective temperature, $T_{\text{eff}}$ (K)	$6216 \pm 78$
Metallicity, [m/H]	$-0.18 \pm 0.10$
Projected rotation speed, $v \sin i$ (km s <sup>-1</sup> ) <sup>a</sup>	$33.95 \pm 0.97$
Asteroseismology	
Stellar mass, $M_*$ ( $M_{\odot}$ )	$1.447 \pm 0.058$
Stellar radius, $R_*$ ( $R_{\odot}$ )	$2.891^{+0.130}_{-0.106}$
Stellar density, $\rho_*$ (g cm <sup>-3</sup> )	$0.0834 \pm 0.0079$
Surface gravity, $\log g$ (dex)	$3.673 \pm 0.026$

**Note.**<sup>a</sup> Using FIES spectrum, as discussed in Section 3.3.

$T_{\text{eff}} = 6216 \pm 51 \text{ K}$ ,  $\log g = 3.57 \pm 0.1 \text{ dex}$ , and  $[m/H] = -0.18 \pm 0.08 \text{ dex}$ . The SPC-derived  $\log g$  is in good agreement with the asteroseismic detection (see below), and thus no iterations between the spectroscopic and asteroseismic solution were required.

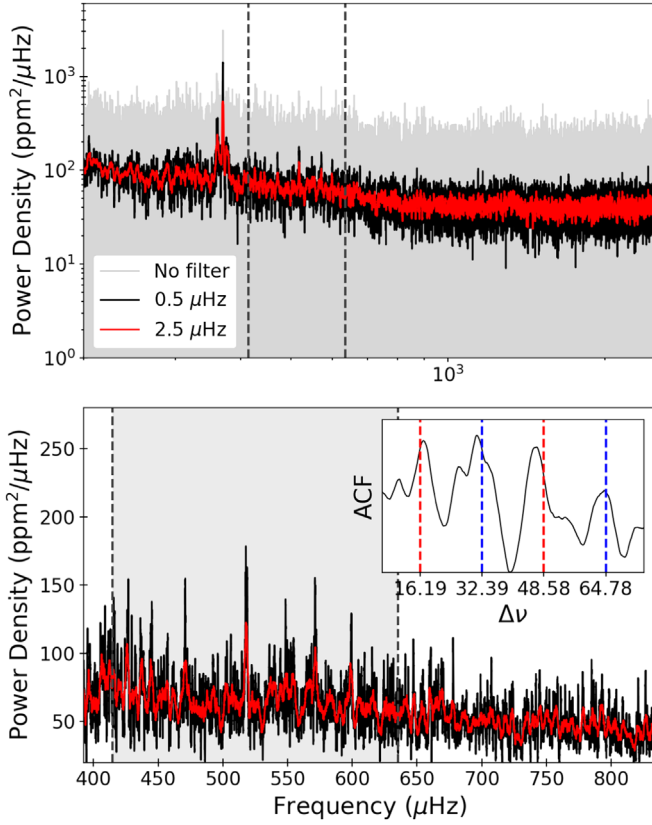
We also analyzed the HIRES spectrum using Specmatch-emp (Yee et al. 2017), yielding consistent values within  $2\sigma$  ( $T_{\text{eff}} = 6241 \pm 110 \text{ K}$ ,  $[m/H] = -0.05 \pm 0.09 \text{ dex}$ ). We adopted the weighted SPC values as our final solution, and added  $59 \text{ K}$  in  $T_{\text{eff}}$  and  $0.062 \text{ dex}$  in  $[m/H]$  in quadrature to the formal uncertainties to account for systematic differences between spectroscopic methods (Torres et al. 2012). The final adopted values are listed in Table 2.

*3.2. Asteroseismology*

Asteroseismology, the study of stellar oscillations, and transits form a powerful synergy to investigate exoplanet systems (Stello et al. 2009b; Gilliland et al. 2010a; Huber et al. 2013b; Van Eylen et al. 2014; Huber 2015). Currently, more than one hundred *Kepler* exoplanet host stars have been characterized through asteroseismology (Huber et al. 2013b; Lundkvist et al. 2016).

We performed a search for oscillations in Kepler-1658 in the *Kepler* short-cadence data. The asteroseismic analysis included removing any data with nonzero quality flags, clipping transits and outliers, then normalizing each individual quarter before concatenating the light curve. A high-pass filter was used to remove long-period systematics before computing the power spectrum. Box filters of widths of  $0.5$  and  $2.5 \mu\text{Hz}$  were used to smooth the power spectrum in order to make the signal clear. The power spectrum for Kepler-1658 can be seen in Figure 2, showing a characteristic frequency-dependent noise due to granulation and a power excess marked by the gray dashed lines. We note that the strong peak near  $\sim 300 \mu\text{Hz}$  is a well-known artifact of *Kepler* short-cadence data (Gilliland et al. 2010b).





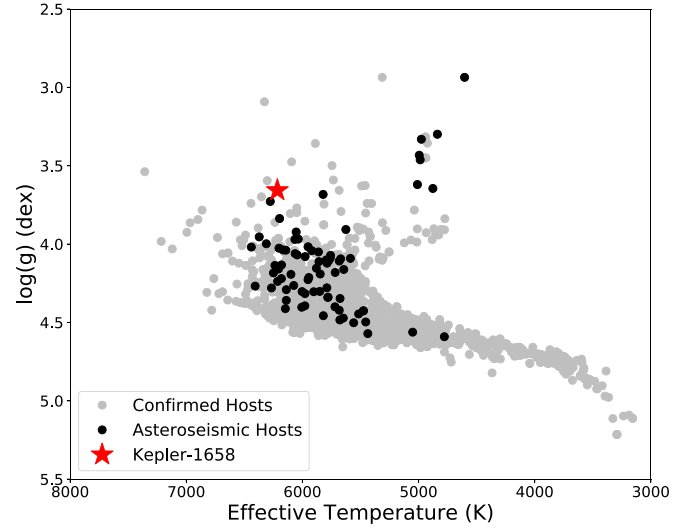
**Figure 2.** Power spectrum of the *Kepler* short-cadence data for Kepler-1658. Top: power spectrum in log-log scale, where the region of oscillations is marked by the dashed lines. The original power is shown in gray and smoothing filters of widths of 0.5 and 2.5  $\mu\text{Hz}$  are shown in black and red, respectively. Bottom: power spectrum in linear space zoomed in on the region of oscillations. The shaded area highlights the power that is used to calculate the autocorrelation, shown in the inset.

Since the power excess has relatively low S/N, we used an autocorrelation to confirm the oscillations. The region with excess power should have a width that we can estimate using a linear scaling relation,

$$w = w_{\odot} \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right), \quad (1)$$

where  $w_{\odot} = 1300 \mu\text{Hz}$  is the width of oscillations in the Sun. To prevent adding noise to the calculated autocorrelation, only the power in this region was used. Confirming the oscillations requires detecting peaks with a regular spacing that follows the well-known correlation between  $\Delta\nu$  and  $\nu_{\max}$  (Hekker et al. 2009, 2011a, 2011b; Stello et al. 2009a; Mosser et al. 2010; Huber et al. 2011). The autocorrelation of the power spectrum is shown in the inset in Figure 2 and confirms the detection of oscillations. The red and blue dashed lines mark the expected positions of regular spacings based on asteroseismic scaling relations. Red is the expected spacing of adjacent radial and dipole modes ( $\sim n \Delta\nu/2$ ) and blue is the expected spacing of consecutive radial modes ( $\sim n \Delta\nu$ ).

The low S/N of the seismic detection, combined with the possible presence of mixed modes, make the autocorrelation an imprecise tool to measure  $\Delta\nu$ . Additionally, the short-cadence artifact at  $\approx 300 \mu\text{Hz}$  prevents a reliable background fit to the power spectrum and thus a measurement of  $\nu_{\max}$ . To determine



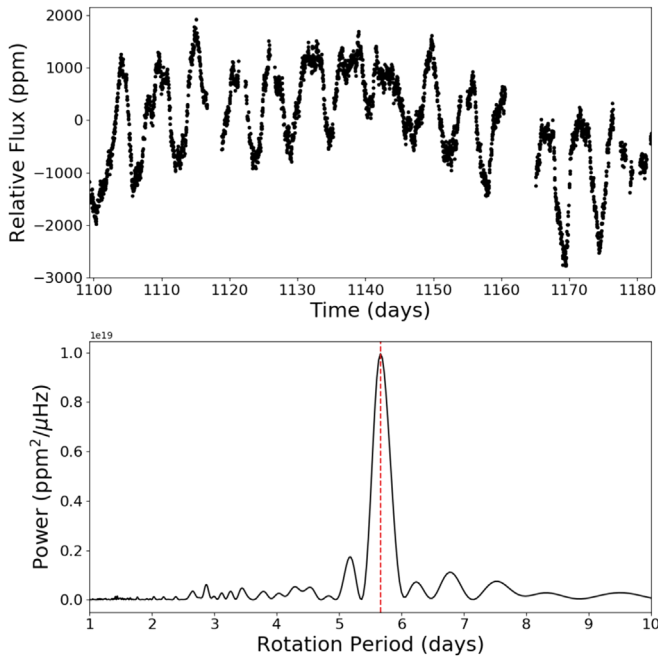
**Figure 3.** Surface gravity vs. effective temperature for confirmed *Kepler* exoplanet hosts. The gray points represent confirmed hosts, with known asteroseismic hosts in black. Kepler-1658, represented by the red star, sits in an underpopulated area of stellar parameter space as a massive, evolved subgiant.

$\Delta\nu$ , we computed échelle diagrams over a grid of trial  $\Delta\nu$  values separated by  $0.1 \mu\text{Hz}$  to identify the spacing which produces straight ridges of modes of consecutive overtones, a method commonly adopted to verify the accuracy of  $\Delta\nu$  values (Bedding et al. 2010). We identified  $32.5 \mu\text{Hz}$  as the correct spacing, consistent with four independent analyses by co-authors (Campante et al. 2010; Chaplin et al. 2011b; Bedding 2012; Davies et al. 2016). We adopted the result from the manual analysis as our final value and adopted the scatter over all methods as an uncertainty, yielding  $\Delta\nu = 32.5 \pm 1.6 \mu\text{Hz}$ .

Since the low S/N does not allow reliable constraints on individual frequencies or  $\nu_{\max}$ , we used grid-based modeling (Gai et al. 2011) with atmospheric parameters from spectroscopy and the asteroseismic  $\Delta\nu$  to derive a full set of host star properties. To perform grid-modeling we used the open-source code *isoclassify*<sup>18</sup> (Huber et al. 2017), which adopts a grid of MIST isochrones (Choi et al. 2016) to probabilistically infer stellar parameters given any combination of photometric, spectroscopic, or asteroseismic input parameters and adopts theoretically motivated corrections for the  $\Delta\nu$  scaling relation from Sharma et al. (2016). The results confirm that Kepler-1658 is a relatively massive ( $M_{\star} = 1.45 \pm 0.06 M_{\odot}$ ) and evolved ( $R_{\star} = 2.89 \pm 0.12 R_{\odot}$ ) subgiant star (Table 2). Kepler-1658 joins a small sample of subgiant host stars for which the stellar mass is accurately determined through asteroseismology (Figure 3).

We note that the  $\Delta\nu$  scaling relation is based on simplified assumptions compared to analyses using individual mode frequencies, and thus may be affected by systematic errors. However, independent model calculations have demonstrated that the relation is accurate to  $<1\%$  in  $\Delta\nu$  ( $<0.5\%$  in  $\rho$ ) for stars in the  $T_{\text{eff}}$  and  $[\text{m}/\text{H}]$  range of Kepler-1658 (White et al. 2011; Rodrigues et al. 2017). Therefore, any potential systematic error in  $\rho_{\star}$  introduced using the  $\Delta\nu$  scaling relation is negligible compared to our adopted uncertainties.

<sup>18</sup> <https://github.com/danxhuber/isoclassify>



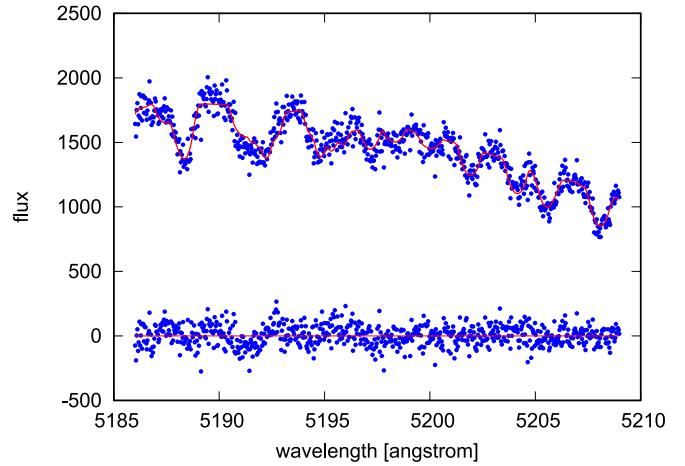
**Figure 4.** Top: transit-clipped Quarter 11 long-cadence light curve for Kepler-1658. Bottom: Lomb-Scargle periodogram showing a strong peak at  $5.66 \pm 0.31$  days, which we interpret as the stellar rotation period.

### 3.3. Stellar Rotation

The top panel of Figure 4 shows the unfiltered light curve of Kepler-1658 from Quarter 11, demonstrating strong evidence for rotational modulation due to spots. The photometric variability has an amplitude of  $\sim 0.1\%$  and shows a strong peak at  $5.66 \pm 0.31$  days in the Lomb-Scargle (LS) periodogram (bottom panel of Figure 4). We tested for temporal variations of the stellar rotation by calculating an LS periodogram of the unfiltered light curve for each quarter available. The analysis demonstrated that the equatorial rotation velocity does not change over the *Kepler* baseline. Combining this rotation period with the asteroseismic radius, we compute an equatorial rotation velocity,  $v = 25.82 \pm 1.77 \text{ km s}^{-1}$ .

In order to estimate the projected rotation velocity ( $v \sin i$ ) of Kepler-1658, we analyzed the FIES spectrum using the technique described by Hirano et al. (2012). In brief, we convolved a theoretical, unbroadened spectrum generated by adopting the stellar parameters for Kepler-1658 (Coelho et al. 2005) with the rotation plus macroturbulence broadening kernel (and instrumental profile), assuming the radial-tangential model (Gray 2005). The broadening kernel has several parameters, including  $v \sin i$ , the macroturbulent velocity  $\zeta$ , and stellar limb-darkening parameters, but we only optimized  $v \sin i$ , along with the overall normalization parameters describing the spectrum continuum.

We attempted the fits for three different spectral segments (5126–5154 Å, 5186–5209 Å, and 5376–5407 Å), where an example of one segment is shown in Figure 5. The uncertainty of  $v \sin i$  was derived based on the scatter of the best-fit values for these segments. For the macroturbulent velocity, we adopted  $\zeta = 4.7 \pm 1.2 \text{ km s}^{-1}$  based on the empirical relation between  $T_{\text{eff}}$  and  $\zeta$  derived by Hirano et al. (2014), but we found that choice of  $\zeta$  has very little impact on the estimated



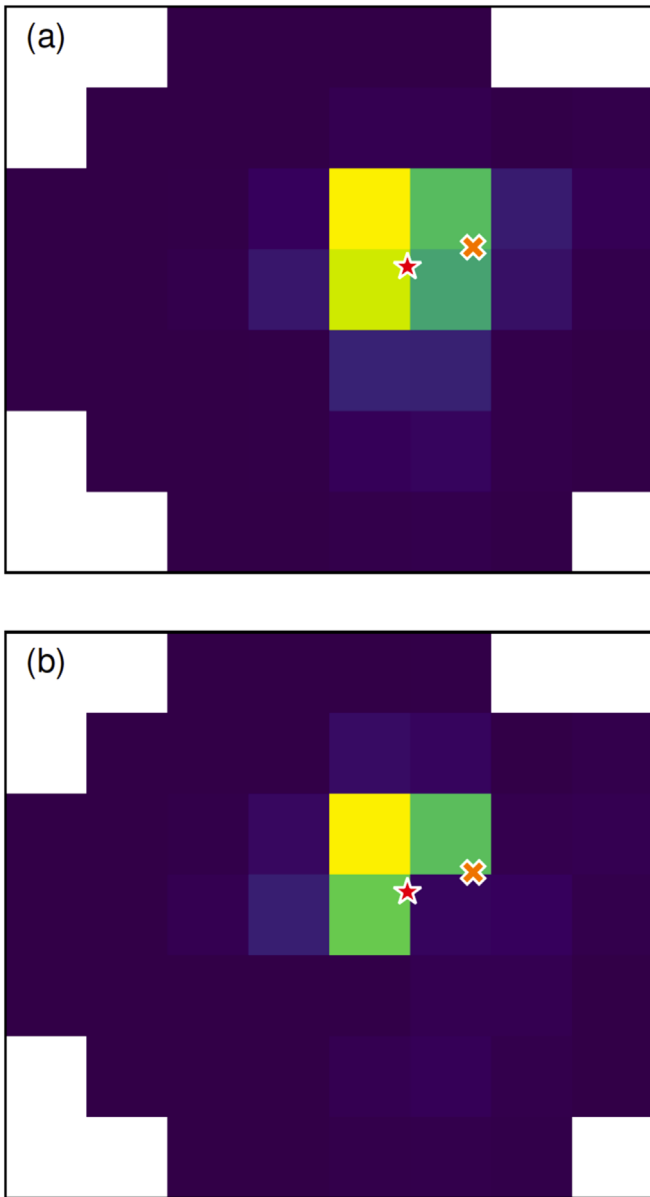
**Figure 5.** One FIES spectral segment of Kepler-1658. A theoretical, unbroadened spectrum is convolved with rotation and a macroturbulent broadening kernel to fit the spectrum and is shown in red, where the scatter in the residuals of the best-fit  $v \sin i$  value is shown below the spectrum.

$v \sin i$ , due to the latter’s large value (variation less than  $0.2 \text{ km s}^{-1}$ ). We found the  $v \sin i$  for Kepler-1658 to be  $33.95 \pm 0.97 \text{ km s}^{-1}$ .

There is a clear discrepancy between the equatorial rotation velocity ( $v$ ) and projected rotation velocity ( $v \sin i$ ) we computed, with  $v \sin i \gg v$ . As discussed in Section 2.2, there is a companion within the  $4''$  *Kepler* pixel and is therefore not resolved. As a result, we tested whether this rotational signal is coming from Kepler-1658 or from its neighbor using *Kepler* target pixel files.

Since the angular separation between Kepler-1658 and its neighbor is the size of a *Kepler* pixel, we wanted to identify in which pixel the rotational signal is strongest. We used the difference imaging technique (Bryson et al. 2013; Colman et al. 2017), which involved phasing the light curve on the period of the rotational signal, binning by a factor of 1000, and selecting the data that fell within  $\pm 1\%$  of the peaks and troughs of the phased light curve. To create the difference image, we subtracted the data around the troughs from the data around the peaks. We did this for each pixel, creating a difference image which gives an indication of the relative strength of the rotational signal over the postage stamp. We then compared the difference image to an average image from the same observing quarter (Figure 6), and found that in 11 of the 17 quarters the pixel with the brightest flux is the same as the pixel where the rotational signal is the strongest. Differences in the other six quarters did not exceed one pixel and were inconsistent with the relative positions of the KOI 4 and the imaged companion (see the symbols in Figure 5). These results strongly imply that the rotational signal is coming from Kepler-1658.

To account for the discrepancy between  $v$  and  $v \sin i$ , we could introduce a latitudinal differential rotation of 20%–40%. According to Collier Cameron (2007), the magnitude of differential rotation for a star with  $T_{\text{eff}} = 6216 \text{ K}$  is estimated to be  $\Delta\Omega \sim 0.28 \text{ radian day}^{-1}$ . From the rotation period of the star, the angular velocity of the spot is  $\Omega \sim 1.1 \text{ radian day}^{-1}$ . The observed high  $v \sin i$  could be explained if the spot that *Kepler* observed is long-lived, located at a relatively high latitude, and its angular velocity at the equator is  $\sim 1.5 \text{ radian day}^{-1}$ .



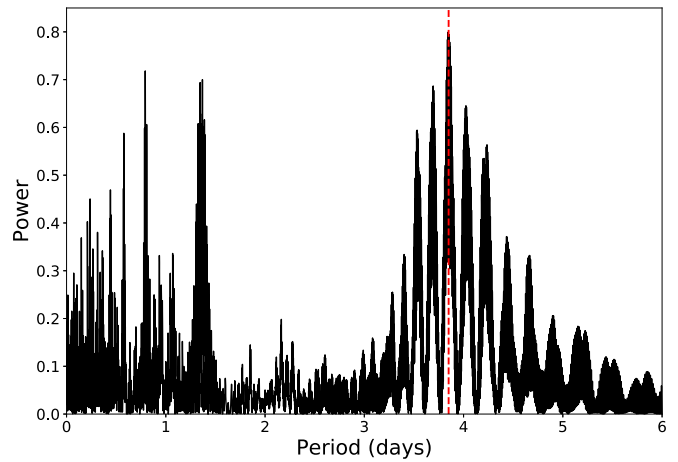
**Figure 6.** Panel (a): target pixel files of Kepler-1658 averaged over one full quarter. Panel (b): a difference image using frames coinciding with the maxima and minima of a phase curve calculated from the measured rotation period. The star marks the location of Kepler-1658, and the companion identified using AO imaging is marked with a cross.

## 4. Orbital and Planetary Parameters

### 4.1. Confirmation of Kepler-1658 b

An unambiguous confirmation of a transiting exoplanet is typically performed by detecting RV variations that are in phase with the ephemeris determined from transits. The initial three RVs were taken as part of the *Kepler* follow-up program during the *Kepler* mission. We obtained 20 more TRES RVs once we realized that it was possible that Kepler-1658 was hosting a planet (Figure 1), for a total of 23 RV observations.

As discussed in Section 3.3, Kepler-1658 is rotating rapidly, thus resulting in RVs with relatively large uncertainties. Despite this limitation, a periodogram of the RV data only reveals a highly significant peak that is fully consistent with the same period of the transit signal (Figure 7). Additionally, phasing the RVs with the ephemeris and orbital period from



**Figure 7.** Periodogram of the radial velocity data. The red dashed line marks the period recovered from the light curve. The peak with the same period as the transit light curve has a false alarm probability of  $4.38 \times 10^{-5}$ .

*Kepler* reveals a clear variation with a semi-amplitude,  $K_* = 579.45^{+43.13}_{-42.94} \text{ m s}^{-1}$ , well above the detection threshold set by the RV uncertainties (Figure 8(d)). Therefore, the consistency between the RV and transit data unambiguously confirms Kepler-1658 b as a hot Jupiter.

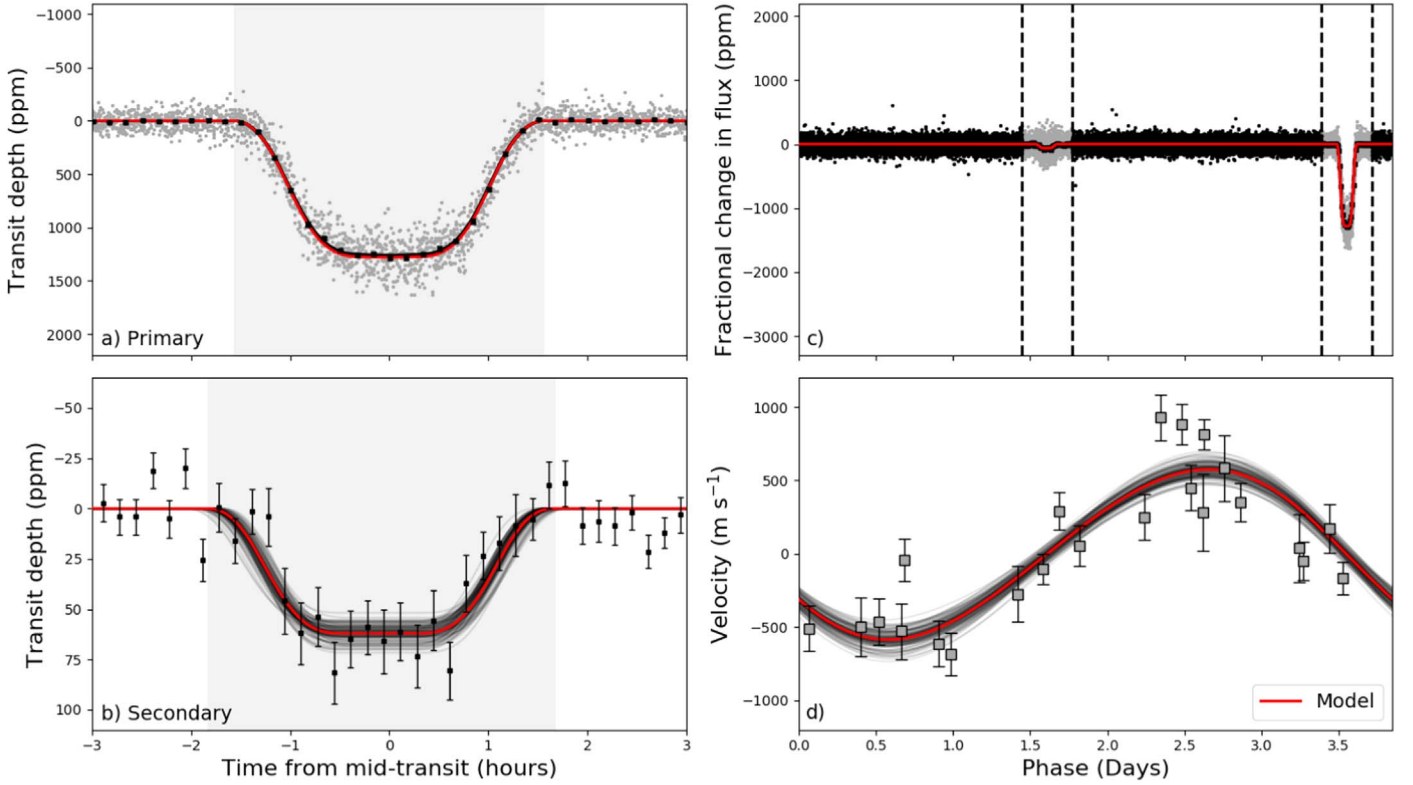
### 4.2. Transit and RV Modeling

To perform a combined transit and RV fit we used the TRES measurements in Table 1 and *Kepler* long-cadence data, which cover a baseline four times longer than the short-cadence data. For computational efficiency, we only used three times the transit duration centered at the time of mid-transit for both the primary and secondary eclipses (Figure 8(c)).

We modeled the light curve and RV observations using *ktransit*,<sup>19</sup> an implementation of the analytical model by Mandel & Agol (2002). We assumed a linear ephemeris (constant orbital period) and quadratic limb-darkening law. The model was fitted for the following parameters: orbital period ( $P$ ), time of mid-transit ( $T_0$ ), linear ( $u_1$ ) and quadratic ( $u_2$ ) limb-darkening coefficients, mean stellar density ( $\rho_*$ ), systematic RV offset ( $\gamma$ ), eccentricity times the sine of the argument of periastron ( $e \sin \omega$ ), eccentricity times the cosine of the argument of periastron ( $e \cos \omega$ ), occultation depth ( $\delta_{\text{occ}}$ ), impact parameter ( $b$ ), ratio of the planetary radius to the stellar radius ( $R_p/R_*$ ), photometric zero-point ( $z$ ), and velocity semi-amplitude ( $K_*$ ). The predicted RV jitter due to stellar variability for a star like Kepler-1658 is on the order of a few  $\text{m s}^{-1}$  (e.g., Yu et al. 2018), and thus negligible compared to the formal RV uncertainties ( $\sim 100\text{--}200 \text{ m s}^{-1}$ ).

We used a Gaussian prior of  $0.083 \pm 0.008 \text{ g cm}^{-3}$  for the mean stellar density derived from asteroseismology, as discussed in Section 3.2. Since Kepler-1658 is a rapid rotator resulting in large RV uncertainties, having an independent measurement of the mean stellar density helped break the degeneracies that exist between  $e$  and  $\omega$ . Using stellar parameters  $T_{\text{eff}} = 6216 \text{ K}$ ,  $\log g = 3.57$  (dex), and  $[\text{m}/\text{H}] = -0.18$ , we extracted limb-darkening coefficients  $u_1 = 0.3033$  and  $u_2 = 0.3133$  from the archived tables (Claret & Bloemen 2011) using the nearest grid point. We assigned Gaussian priors

<sup>19</sup> <https://github.com/mrtommyb/ktransit>



**Figure 8.** Simultaneous transit and RV fit through an MCMC analysis of Kepler-1658. Panels (a)–(b): phase-folded light curve centered on the primary and secondary transits, where the black squares are 10 minutes bins. The original data points from panel (b) have been removed for clarity. Panel (c): full phase-folded light curve, where only gray points are used in the MCMC analysis. Panel (d): TRES RV observations. The median value for each parameter is used to generate a model and is shown in red. One hundred samples are drawn at random and added with transparency to give an idea of the uncertainty in the model.

for the limb-darkening coefficients, using the Claret & Bloemen (2011) values as the center of the distribution with a width of 0.6. Additional priors on  $u_1$  and  $u_2$  are implemented, using linear combinations to prevent the parameters from taking nonphysical values (Burke et al. 2008; Barclay et al. 2015). We used a Jeffreys prior for eccentricity ( $1/e$ ) to avoid a positive bias (Eastman et al. 2013). The remaining parameters were assigned uniform (flat) priors and are listed in Table 3.

We explored the parameter space by fitting the planet transit and RV data simultaneously using *emcee*, a Markov chain Monte Carlo (MCMC) algorithm (Foreman-Mackey et al. 2013a). We initialized 30 walkers, each taking  $10^5$  steps. A burn-in phase of  $4 \times 10^3$  steps was removed from each chain before concatenating samples to obtain the final posterior distribution for each parameter. A corner plot is shown in Figure 9 to demonstrate convergence of the 13-dimensional parameter space, highlighting known correlations in the parameter space.

#### 4.3. System Parameters

All of the physical parameters and corresponding uncertainties for Kepler-1658 derived from the joint transit and RV model can be found in Table 4. In addition to the transit and RV observations, asteroseismology was critical to break parameter degeneracies. Specifically, since Kepler-1658 b has such a short orbital period, an eccentricity of  $e = 0.06 \pm 0.02$  initially seemed unlikely but is required due to the observed transit duration (2.6 hr) and the strong constraint from the asteroseismic mean stellar density. A visualization of this can be seen in Figures 8(a)–(b), where the time from mid-transit of the primary and secondary is plotted on the same timescale. The difference in transit

**Table 3**  
Model Parameters

Parameter	Prior
$z$	$\mathcal{U}[-1; 1]$
$u_1^a$	$\mathcal{N}(0.3033; 0.6)$
$u_2^a$	$\mathcal{N}(0.3133; 0.6)$
	$u_1 \geq 0$
	$u_1 + u_2 \leq 1$
	$u_1 + 2u_2 \geq 0$
$\gamma$ (m s <sup>-1</sup> )	$\mathcal{U}[-1200; -700]$
$K$ (m s <sup>-1</sup> )	$\mathcal{U}[350; 850]$
$P$ (days)	$\mathcal{U}[3.75; 3.95]$
$T_0$ (BKJD) <sup>b</sup>	$\mathcal{U}[171.9; 173.9]$
$b$	$\mathcal{U}[0; 1]$
$R_p/R_*$	$\mathcal{U}[0.02; 0.06]$
$e \sin \omega$	$\mathcal{U}[-1; 1]$
$e \cos \omega$	$\mathcal{U}[-1; 1]$
$e$	$1/e$
$\delta_{\text{occ}}$ (ppm)	$\mathcal{U}[0; 200]$
$\rho_*$ (g cm <sup>-3</sup> ) <sup>c</sup>	$\mathcal{N}(0.0834; 0.0079)$

#### Notes.

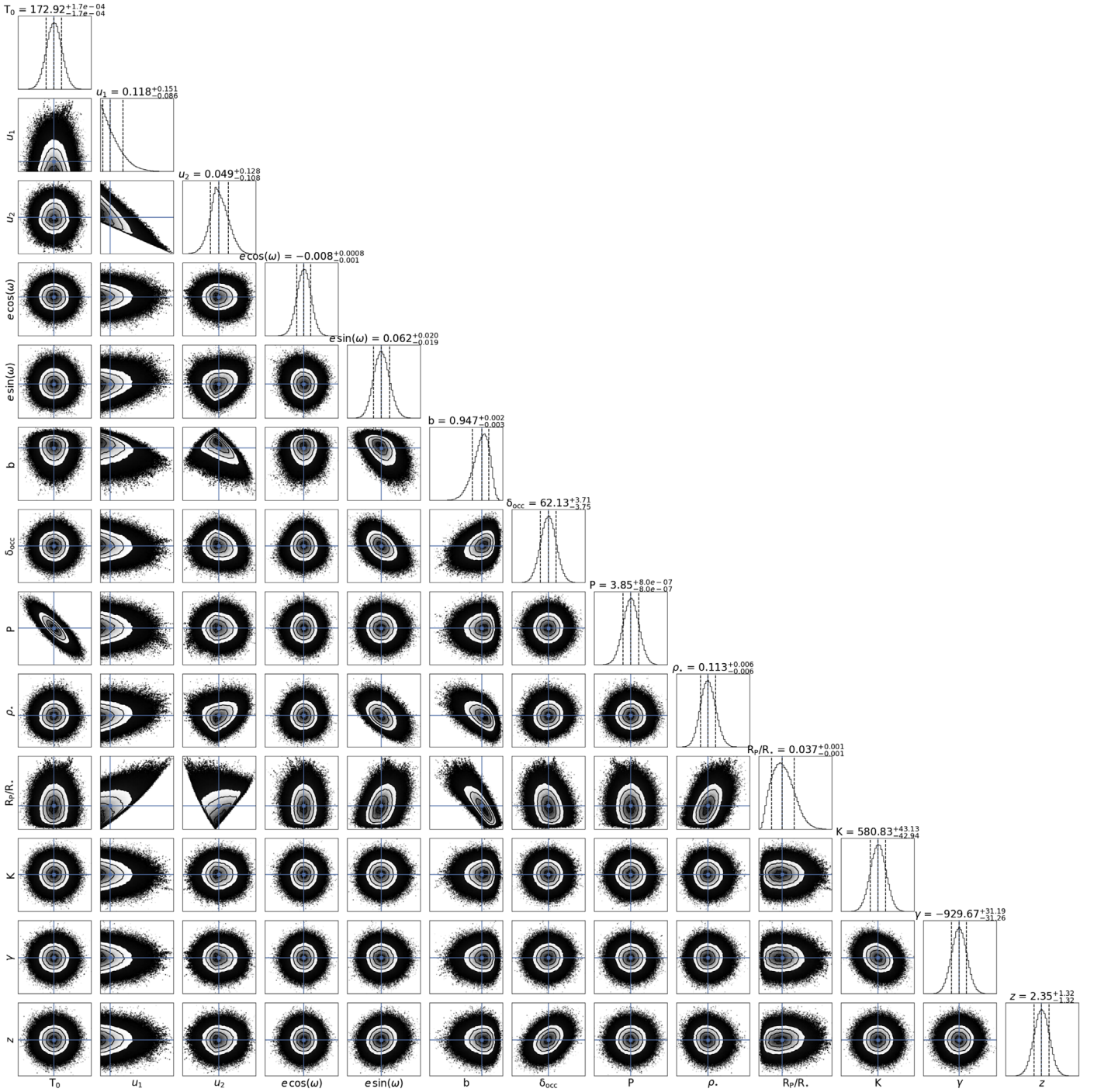
<sup>a</sup> Adopted from the archived tables of Claret & Bloemen (2011) with additional priors to prevent nonphysical values.

<sup>b</sup> BKJD is the time system used by *Kepler* and is defined by the Barycentric Julian Date (BJD)—2,454,833.

<sup>c</sup> Adopted from the asteroseismic analysis.

durations and the slight offset of the secondary eclipse can only be explained by a mild eccentricity since we have the strong prior constraint on the mean stellar density from asteroseismology.





**Figure 9.** Posterior distributions for the 13-dimensional MCMC analysis of the simultaneous transit and RV fit. The parameters across the bottom are time of mid-transit ( $T_0$ ), linear ( $u_1$ ) and quadratic ( $u_2$ ) limb-darkening coefficients, eccentricity times the cosine of the argument of periastron ( $e \cos \omega$ ), eccentricity times the sine of the argument of periastron ( $e \sin \omega$ ), impact parameter ( $b$ ), occultation depth ( $\delta_{\text{occ}}$ ), orbital period ( $P$ ), mean stellar density ( $\rho_*$ ), ratio of the planetary radius to the stellar radius ( $R_p/R_*$ ), velocity semi-amplitude ( $K_*$ ), systematic RV offset ( $\gamma$ ), and photometric zero-point ( $z$ ).

Furlan et al. (2017) reported planet radius correction factors (PRCF) for photometric contamination from nearby stellar companions. Depending on the separation and contrast ratio, the companion can contribute to the total flux throughout the phase of the orbit, including the primary transit, thus underestimating the radius of the planet. Since RV observations confirm that the planet is orbiting the primary star, we obtained a final planetary radius of

$R_p = 1.07 \pm 0.05 R_J$  using a  $\text{PRCF} = 1.0065 \pm 0.0003\%$  (Furlan et al. 2017). We note that this is PRCF is based on a measured contrast in the LP600 filter (see Section 2.2), which is commonly assumed to be similar to the *Kepler* bandpass (Law et al. 2014; Baranec et al. 2016; Ziegler et al. 2017). The PRCF was taken into account before deriving physical planet parameters and is therefore taken into consideration for the final values listed in Table 4.



**Table 4**  
MCMC Parameter Summary

Parameter	Best-fit	Median	84%	16%
Fitted Parameters				
$z$ (ppm)	1.703	2.350	+1.316	−1.317
$P$ (days)	3.8494	3.8494	+8.04-7	−8.01e-7
$T_0$ (BJD)	172.9241	172.9241	+1.69-4	−1.67e-4
$b$	0.9501	0.9471	+0.0025	−0.0032
$R_p/R_*$	0.0359	0.0369	+0.0008	−0.0007
$e \sin \omega$	0.0580	0.0622	+0.0198	−0.0188
$e \cos \omega$	−0.0081	−0.0084	+0.0008	−0.0008
$\delta_{\text{occ}}$ (ppm)	61.842	62.127	+3.712	−3.750
$u_1$	0.0154	0.1179	+0.1513	−0.0859
$u_2$	0.0453	0.0487	+0.1276	−0.1082
$\gamma$ (m s <sup>−1</sup> )	−915.88	−929.67	+31.19	−31.26
$K$ (m s <sup>−1</sup> )	575.80	580.83	+43.13	−42.94
$\rho_p$ (g cm <sup>−3</sup> )	0.1068	0.1130	+0.0063	−0.0060
Derived Parameters				
$a$ (au)	0.0546	0.0544	0.0007	−0.0007
$R_p$ (R <sub>J</sub> ) <sup>a</sup>	1.04	1.07	+0.05	−0.05
$a/R_*$	4.07	4.04	0.18	−0.17
$e$	0.0585	0.0628	+0.0197	−0.0185
$\omega$ (°)	−7.99	−7.73	+1.93	−3.37
$M_p$ (M <sub>J</sub> ) <sup>a</sup>	5.88	5.88	+0.47	−0.46
$\rho_p$ (g cm <sup>−3</sup> )	7.00	6.36	+1.07	−0.91
$i$ (°)	76.55	76.52	+0.58	−0.59
$A_\lambda$	0.785	0.734	+0.090	−0.081

**Note.**<sup>a</sup> Adopting a Jupiter radius of  $6.9911 \times 10^4$  km and mass of  $1.898 \times 10^{27}$  kg.

The secondary eclipse allows an estimate of the planetary albedo. According to Winn (2010), a geometric albedo can be determined by

$$A_\lambda = \delta_{\text{occ}}(\lambda) \left( \frac{R_p}{a} \right)^{-2}, \quad (2)$$

where  $\delta_{\text{occ}}$  is the occultation depth. Using Equation (2), we derived a geometric albedo of  $0.724^{+0.090}_{-0.081}$  in the *Kepler* bandpass. This value is consistent to within  $1\text{--}2\sigma$  of RoboVetter’s analysis by Coughlin et al. (2016), which estimated a value of either  $0.494^{+0.186}_{-0.083}$  or  $0.348^{+0.145}_{-0.062}$ , depending on the light-curve detrending method used.

Following Winn (2010), the planet inclination can be derived by

$$b_{\text{tra}} = \frac{a \cos i}{R_*} \left( \frac{1 - e^2}{1 + e \sin \omega} \right), \quad (3)$$

where  $b_{\text{tra}}$  is the impact parameter  $b$  of the primary transit and  $a$  is the planet’s semimajor axis. Using Equation (2), we obtained an inclination,  $i = 76.52 \pm 0.59$ . This is consistent with the short orbital period and high impact parameter,  $b = 0.947 \pm 0.003$ .

The inclination of the orbital plane of the planet is used to break the  $M_p \sin i$  degeneracy that would otherwise exist from RV observations alone. Given that  $M_p \ll M_*$ , the data

determine  $M_p/M_*^{2/3}$  through

$$\frac{M_p}{(M_p + M_*)^{2/3}} = \frac{K_* \sqrt{1 - e^2}}{\sin i} \left( \frac{P}{2\pi G} \right)^{1/3}, \quad (4)$$

but not  $M_p$  itself (Winn 2010). Because asteroseismology provides a stellar mass, the planet mass can be determined through Equation (4), yielding  $M_p = 5.87 \pm 0.46 M_J$ . Combined with the corrected radius, we find a bulk density of  $\rho_p = 6.36^{+1.07}_{-0.91}$  g cm<sup>−3</sup>.

The mean stellar density modeled from the light curve,  $\rho_* = 0.113 \pm 0.006$ , converged  $3\sigma$  higher than the mean stellar density determined through asteroseismology. Analytical solutions for transit models are based on assumptions that the scaled semimajor axis,  $a/R_* \gtrsim 8$ , and the impact parameter,  $b \ll 1$  (Seager & Mallén-Ornelas 2003; Winn 2010). We speculate that this inconsistency is due to the fact that the *Kepler*-1658 system falls in a parameter space where these approximations no longer hold ( $a/R_* \approx 4$ ,  $b \approx 0.95$ ).

## 5. Discussion

### 5.1. Orbital Period Decay

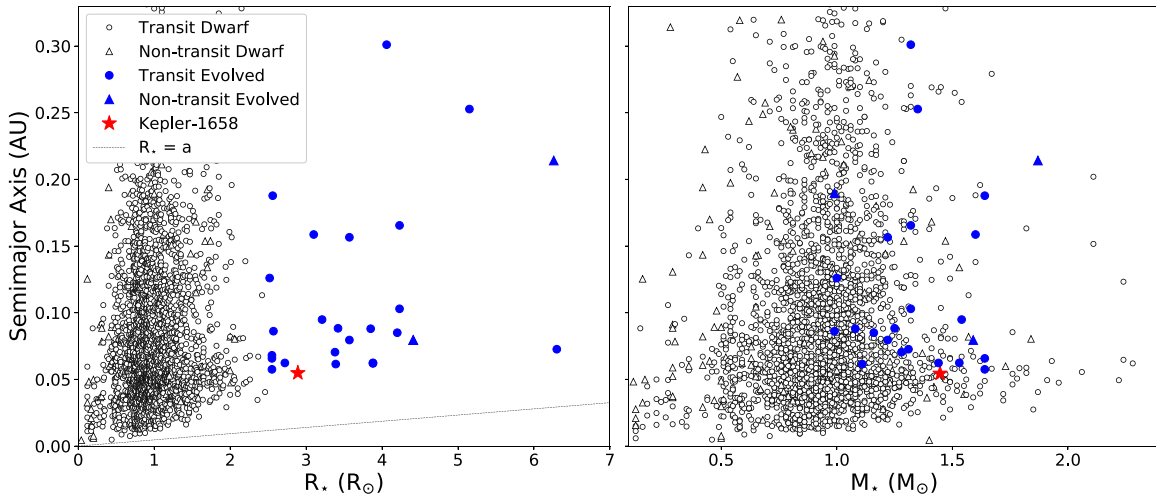
*Kepler*-1658 joins a rare population of exoplanets in close-in orbits around evolved, high-mass subgiant stars (Figure 10). One theory for the lack of such planets is tidal evolution, occurring when a close-in giant planet tidally interacts with its host star (Levrard et al. 2009; Schlaufman & Winn 2013). Tidal interactions in a two-body system are complex, and different driving mechanisms depend on a number of parameters (Zahn 1989; Barker & Ogilvie 2009; Lai 2012; Rogers et al. 2013). A system undergoing tidal dissipation conserves total angular momentum but dissipates its energy, and ultimately the dynamical evolution in the system is determined by the transfer of angular momentum between rotational and orbital parameters (Zahn 1977; Hut 1981).

There are only two possible outcomes to tidal evolution, depending on the stability of the system. One is a stable equilibrium in a coplanar, circular, synchronous orbit. If the total angular momentum in the system exceeds a critical value, then the system becomes unstable, mostly dependent on the moments of inertia of both the host star and planet. A telltale sign of instability is when the orbital period of the planet is shorter than the rotational period of the star. When this happens, the planet deposits angular momentum onto the star, causing the star to spin up and the orbit to shrink (Levrard et al. 2009; Adams et al. 2010; Schlaufman & Winn 2013; Blecic et al. 2014; Maciejewski et al. 2016; Van Eylen et al. 2016). In this latter scenario, there is no stable equilibrium point and the planet will migrate inward until it is eventually engulfed by the host star. However, even systems that are marginally stable can be susceptible to inward planet migration due to evolutionary effects or angular momentum loss through magnetized winds (van Saders & Pinsonneault 2013).

Following Levrard et al. (2009), we can estimate the timescale of orbital decay using

$$\tau_a \simeq \frac{1}{48} \frac{Q'_*}{n} \left( \frac{a}{R_*} \right)^5 \left( \frac{M_*}{M_p} \right), \quad (5)$$

where  $n$  is the mean orbital angular velocity and  $Q'_*$  is the tidal quality factor, which is a single parameter that encapsulates



**Figure 10.** Confirmed exoplanets taken from the NASA exoplanet archive (accessed on 2018 November 7, with the error bars omitted for clarity) Left: semimajor axis vs. stellar radius, where the dotted line represents  $R_* = a$ . Of all the evolved stars, Kepler-1658 is the closest short-period planet orbiting an evolved star. Right: semimajor axis vs. stellar mass. Short-period planets ( $\leq 100$  days) orbiting evolved stars ( $\geq 2.5 R_\odot$ ) are shown in blue, with values taken from HD 102956 (Johnson et al. 2010), Kepler-56 (Huber et al. 2013a), Kepler-278 and Kepler-391 (Rowe et al. 2014), Kepler-91 (Lillo-Box et al. 2014), Kepler-432 (Ciceri et al. 2015; Quinn et al. 2015), Kepler-435 (Almenara et al. 2015), K2-11 (Montet et al. 2015), HIP 67851 (Jones et al. 2015), 8 UMi (Lee et al. 2015), K2-39 (Van Eylen et al. 2016), K2-97 (Grunblatt et al. 2016), Kepler-637, Kepler-815, Kepler-1004, and Kepler-1270 (Morton et al. 2016), TYC 3667-1280-1 (Niedzielski et al. 2016), K2-132 (Grunblatt et al. 2017), HAT-P-67 (Zhou et al. 2017), KELT-11 (Pepper et al. 2017), WASP-73 (Stassun et al. 2017), and 24 Boo (Takarada et al. 2018).

physical processes that occur in tidal dissipation. A more recent paper by Lai (2012) suggests that  $Q'_*$  can vary for different tidal processes (e.g., orbital decay and spin-orbit alignment). In addition, tidal theory is very poorly constrained observationally, resulting in possible values for  $Q'_*$  that span several orders of magnitude, ranging from  $10^2$  to  $10^{10}$  (Barker & Ogilvie 2009; Levrard et al. 2009; Adams et al. 2010; Schlaufman & Winn 2013; Blecic et al. 2014). Therefore, tidal dissipation timescales remain highly uncertain. Observations of orbital period decay would provide better constraints on  $Q'_*$ , which is currently poorly understood due to the complex nature of tidal interactions. Orbital period decay of a hot Jupiter was first proposed by Lin et al. (1996) and was only recently detected in WASP-12b by Maciejewski et al. (2016). Based on ten years of transit data, Maciejewski et al. (2016) reported a tidal quality factor of  $2.5 \times 10^5$  for a main-sequence host star. Patra et al. (2017) use new transit times of WASP-12b to further confirm evidence of period decay and find a consistent tidal quality factor of  $2 \times 10^5$ .

For subgiant and giant stars such as Kepler-1658, Schlaufman & Winn (2013) suggest that the stars become more dissipative as they evolve off the MS, with  $Q'_*$  closer to  $10^2$ – $10^3$ . Kepler-1658 is a prime target to constrain orbital period decay because it has a scaled semimajor axis of  $a/R_* \approx 4$  (Figure 10) and the timescale of period decay is a sensitive function of this parameter (Equation (5)). There is also evidence that the Kepler-1658 system is unstable because the orbital period of the planet is less than the stellar rotation period.

In order to test for evidence of period decay, we divided the long-cadence light curves into segments with a length corresponding to the orbital period,  $P = 3.85$  days. We modeled the individual transits using `ktransit` and used a similar MCMC analysis to determine the transit times. All other parameters were fixed to the values from the global fit

discussed in Section 4.2. The individual transit times are shown in Figure 11 and listed in Table 5.

Following Maciejewski et al. (2016), we modeled the period decay rate by adding a quadratic term to the previously assumed linear ephemeris,

$$T_x = T_0 + Px + \frac{1}{2}\delta Px^2, \quad (6)$$

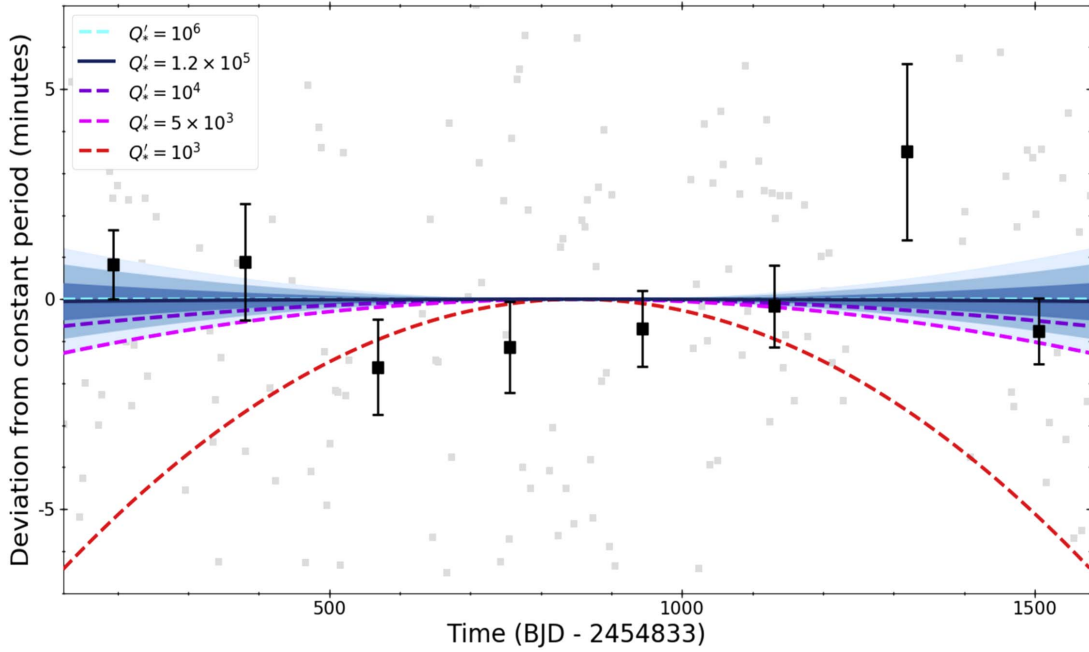
where  $x$  is the orbit number,  $T_x$  is the time of mid-transit of  $x$  orbit, and  $\delta P$  is the change in orbital period between consecutive orbits ( $P\dot{P}$ ). We used the MCMC analysis described by Foreman-Mackey et al. (2013a) to fit for  $T_0$ ,  $P$ , and  $\delta P$ . We placed uniform priors on  $T_0$  and  $\delta P$  and a Gaussian prior on  $P$ , as derived from the combined transit and RV fit result.

Our analysis found  $\delta P = (-.2048 \pm 1.723) \times 10^{-8}$  days, corresponding to a decay rate of  $\dot{P} = -16.8 \pm 141.25 \text{ ms yr}^{-1}$ , where a negative value is indicative of orbital decay. This corresponds to an infall timescale of 20 Myr. For consistency and comparison to the values reported in Maciejewski et al. (2016), we used

$$Q'_* = 9P\dot{P}^{-1} \frac{M_p}{M_*} \left( \frac{R_*}{a} \right)^5 \left( \omega_* - \frac{2\pi}{P} \right) \quad (7)$$

to estimate the tidal quality factor, where  $\omega_*$  is the stellar rotation rate. Using Equation (10), we calculated a tidal quality factor,  $Q'_* = 1.219 \times 10^5$ , consistent with that reported by Maciejewski et al. (2016). Figure 11 shows the timing residuals of a linear ephemeris plotted with the quadratic model, including our median fit with the  $1\sigma$ ,  $2\sigma$ , and  $3\sigma$  levels shown in different transparencies. Theoretical values are added for comparison.

Although the MCMC analysis is suggestive of period decay, the result is consistent with zero within  $1\sigma$ , as seen in



**Figure 11.** Deviation from a constant orbital period vs. epoch for Kepler-1658. Original transit times using *Kepler* long-cadence data are shown in gray and binned data is shown in black. Our analysis found a tidal quality factor of  $Q'_* = 1.219 \times 10^5$ , shown by the blue line with the  $1\sigma$ ,  $2\sigma$ , and  $3\sigma$  levels shown in different transparencies. Theoretical values of  $Q'_* = 10^3$ ,  $5 \times 10^3$ ,  $10^4$ , and  $10^6$  are shown. Our results provide a strong lower limit for the tidal quality factor, ruling out  $Q'_* \leq 4.826 \times 10^3$  for evolved subgiants for the first time observationally.

**Table 5**  
Individual Transit Times

Epoch (BJD)	84%	16%
2454955.88020	0.00176	-0.00174
2454959.72578	0.00121	-0.00116
2454967.43397	0.00112	-0.00118
2454971.28509	0.00158	-0.00154
2454975.12848	0.00131	-0.00130
2454978.97490	0.00132	-0.00125
2454982.82490	0.00173	-0.00179
2454986.67586	0.00152	-0.00152
2454990.52639	0.00138	-0.00129
2454994.37652	0.00196	-0.00198
2455005.92202	0.00189	-0.00191
2455009.77189	0.00129	-0.00126
2455013.62780	0.00333	-0.00284

(This table is available in its entirety in machine-readable form.)

Figure 11. However, we can still provide a strong constraint for the tidal quality factor in subgiants. We report a  $3\sigma$  upper limit of  $\delta P \leq -5.17 \times 10^{-8}$  days, or a decay rate of  $\dot{P} \leq -0.424 \text{ s yr}^{-1}$ . This corresponds to a lower limit of  $Q'_* \geq 4.826 \times 10^3$  and thus clearly rules out lower tidal quality factors suggested for subgiants in the literature and places strong constraints on tidal theories for evolved stars by effectively ruling out  $\sim 2$  orders of magnitude.

### 5.2. Spin–Orbit Misalignment

Kepler-1658 is rapidly rotating, suggesting that it started farther up the main sequence than the Sun, with a negligible or nonexistent convective envelope to effectively spin the star down

through magnetic braking (van Saders & Pinsonneault 2013). Solar-like oscillations are excited by near-surface convection, implying that host star now has a convection zone. More specifically, Kepler-1658 has  $T_{\text{eff}} \approx 6210 \text{ K}$ , suggesting that it recently crossed the transition between exoplanet systems showing small and large spin–orbit misalignments (Winn et al. 2010). Therefore, Kepler-1658 may provide valuable insight into the dynamical formation history of hot Jupiters.

The obliquity, or the angle measured between the orbital angular momentum vector and rotational axis of the star, is defined as

$$\cos \psi = \cos i_* \cos i + \sin i_* \sin i \cos \lambda, \quad (8)$$

where  $\lambda$  is the sky-projected obliquity,  $i$  is the planet’s inclination, and  $i_*$  is the stellar inclination. The sky-projected obliquity  $\lambda$  can be directly measured through the Rossiter–McLaughlin (RM) effect for close-in giant planets if that star is rotating fast enough (McLaughlin 1924; Rossiter 1924; Ohta et al. 2005; Winn et al. 2009). The planet’s inclination is trivially measured for transiting systems.

The stellar inclination can be measured through relative amplitudes of rotationally split dipole modes (Gizon & Solanki 2003). Stellar inclinations measured through asteroseismology demand a long baseline to achieve sufficient frequency resolution and S/N. The asteroseismic technique has been applied to more than a handful of exoplanet hosts (Chaplin et al. 2013; Huber et al. 2013a; Davies et al. 2015; Campante et al. 2016a; Kamiaka et al. 2018), but is not applicable to Kepler-1658 due to the low S/N.

Alternatively, the stellar spin inclination can be measured if there is evidence of rotational modulation (Winn et al. 2007; Schlafman 2010). More specifically, the relation between the

inclination, rotation period, and rotational velocity is given by

$$\sin i_* = \left( \frac{P_{\text{rot}}}{2\pi R_*} \right) v \sin i. \quad (9)$$

The detection of the rotational period in Kepler-1658 allows us to put constraints on the stellar inclination through Equation (9). As discussed in Section 3.3, the observed  $v \sin i$  and rotation period imply  $i \approx 90^\circ$ . With no prior information on the projected obliquity  $\lambda$ , the true obliquity can range from  $16^\circ.50 \leq \psi \leq 163^\circ.50$ , providing tentative evidence for a spin-orbit misalignment. Future spectroscopic observations while the planet is transiting would allow further constraints on the true obliquity. The expected signal of the RV anomaly due to the RM effect through

$$\Delta v_{\text{RM}} \sim v \sin i \left( \frac{R_p}{R_*} \right)^2, \quad (10)$$

yields  $\Delta v_{\text{RM}} \sim 55 \text{ m s}^{-1}$  for KOI 4.01. The detection of the RM effect would add Kepler-1658 to the small number of systems for which true obliquity measurements are possible (Benomar et al. 2014; Lund et al. 2014).

## 6. Conclusions

We have used asteroseismology and spectroscopy to confirm Kepler-1658 b, *Kepler's* first planet detection. Our main conclusions can be summarized as follows.

1. Kepler-1658 is a subgiant with  $T_{\text{eff}} = 6216 \pm 78 \text{ K}$ ,  $R_* = 2.89 \pm 0.12 R_\odot$ , and  $M_* = 1.45 \pm 0.06 M_\odot$ . As a massive subgiant, Kepler-1658 is currently undergoing a rapid phase of stellar evolution, joining only 9 known exoplanet hosts with similar properties (15 including statistically validated planets).
2. Kepler-1658 b is a hot Jupiter with  $R_p = 1.07 \pm 0.05 R_J$  and  $M_p = 5.73 \pm 0.45 M_J$ , with an orbital period of 3.85 days. The planet is part of a small population of short-period ( $P \lesssim 100$  days,  $a \lesssim 0.5$  au) planets around evolved ( $R_* \gtrsim 2.5 R_\odot$ ,  $\log g \lesssim 3.7$ ) stars. Sitting at an orbital distance of only  $\approx 0.05$  au, Kepler-1658 b is one of the closest known planets to an evolved star. We find tentative evidence for a mild eccentricity ( $e = 0.06 \pm 0.02$ ), consistent with tidal evolution studies suggesting moderate eccentricities of short-period planets around evolved stars (Villaver & Livio 2009; Grunblatt et al. 2018).
3. Individual transit times over four years of *Kepler* observations place a strong upper limit of the orbital period decay rate,  $\dot{P} \leq -0.42 \text{ s yr}^{-1}$ , setting a lower limit on the tidal quality factor  $Q'_* \geq 4.826 \times 10^3$ . Our measurements provide the first strong observational limit on tidal quality factors of subgiant stars, ruling out  $\sim 2$  orders of magnitude of suggested theoretical values in the literature.
4. Kepler-1658 sits close to the proposed misalignment boundary of 6250 K for hot Jupiter obliquities. While the combination of the rotation period,  $v \sin i$ , and stellar radius only provide tentative evidence for a high obliquity ( $16^\circ.50 \leq \psi \leq 163^\circ.50$ ), future spectroscopic observations of the RM effect may be able to provide stronger constraints on obliquity damping and thus hot Jupiter migration theories.

The *Kepler* field will be observed by the *Transiting Exoplanet Survey Satellite* (*TESS*; Ricker et al. 2015) in mid-2019. Extending the baseline of transit observations to over a decade for Kepler-1658 will allow for a stronger constraint on orbital period decay in more evolved systems. Extrapolating our period decay analysis to the time Kepler-1658 would be observed by *TESS* would rule out another order of magnitude for the tidal quality factor in subgiant stars.

Kepler-1658 is typical of the asteroseismic host stars we expect to find with *TESS*. Campante et al. (2016b) estimated that *TESS* will find at least 100 asteroseismic exoplanet hosts, and the first detection by Huber et al. (2019) confirms that this yield will be biased toward evolved subgiants similar to Kepler-1658 due to the increase of asteroseismic detection probabilities with stellar luminosity. Since targets found by *TESS* will be more amenable to follow-up, we expect that larger samples of short-period planets around evolved stars will provide better clues into planet formation, tidal migration, and dynamical evolution studies.












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*Software:* astropy (Astropy Collaboration et al. 2013), emcee (Foreman-Mackey et al. 2013b), Matplotlib (Hunter 2007), Pandas (McKinney 2010), SciPy (Jones et al. 2001).

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