

# Continuous Wave Resonant Photon Stimulated Electron Energy-Gain and Electron Energy-Loss Spectroscopy of Individual Plasmonic Nanoparticles

Chenze Liu,<sup>†,‡,§</sup> Yueying Wu,<sup>†,‡,§</sup> Zhongwei Hu,<sup>§,‡</sup> Jacob A. Busche,<sup>§,‡</sup> Elliot K. Beutler,<sup>§</sup> Nicholas P. Montoni,<sup>§</sup> Thomas M. Moore,<sup>||</sup> Gregory A. Magel,<sup>||</sup> Jon P. Camden,<sup>‡,||</sup> David J. Masiello,<sup>\*,§,||</sup> Gerd Duscher,<sup>\*,†</sup> and Philip D. Rack<sup>\*,†,⊥</sup>

<sup>†</sup>Department of Materials Science and Engineering, University of Tennessee, Knoxville, Tennessee 37996, United States

<sup>‡</sup>Department of Chemistry and Biochemistry, University of Notre Dame, Notre Dame, Indiana 46556, United States

<sup>§</sup>Department of Chemistry, University of Washington, Seattle, Washington 98195, United States

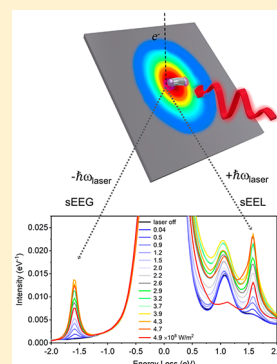
<sup>||</sup>Waviks Inc., 10330 Markison Road, Dallas, Texas 75238, United States

<sup>⊥</sup>Center for Nanophase Materials Sciences, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, United States

## Supporting Information

**ABSTRACT:** The unique optical properties of surface plasmon resonances in nanostructured materials have attracted considerable attention, broadly impacting both fundamental research and applied technologies ranging from sensing and optoelectronics to quantum computing. Electron energy-loss spectroscopy in the transmission electron microscope has revealed valuable information about the full plasmonic spectrum of these materials with nanoscale spatial resolution. Here we report a novel approach for experimentally accessing the photon-stimulated electron energy-gain and stimulated electron energy-loss responses of individual plasmonic nanoparticles via the simultaneous irradiation of a continuous wave laser and continuous current, monochromated electron probe. Stimulated gain and loss probabilities are equivalent and increase linearly in the low-irradiance range of  $0.5 \times 10^8$  to  $4 \times 10^8$  W/m<sup>2</sup>, above which excessive heating reduces the observed probabilities; importantly in our low-irradiance regime, the photon energy must be tuned in resonance with the plasmon energy for the stimulated gain and loss peaks to emerge. Theoretical modeling based on Fermi's golden rule elucidates how the plasmon resonantly and coherently shuttles energy quanta between the electron probe and the radiation field and vice versa in stimulated electron energy-loss and -gain events. This study opens a fundamentally new approach to explore the quantum physics of excited-state plasmon resonances that does not rely on high-intensity laser pulses or any modification to the EELS detector.

**KEYWORDS:** plasmon resonance, electron energy loss (EEL), electron energy gain (EEG), (scanning) transmission electron microscope ((S)TEM), laser



The ability of nanostructured metals to support plasmon resonances in response to light has implications in many scientific fields and applications such as optoelectronics,<sup>1–3</sup> optical computing,<sup>4,5</sup> and readout strategies for quantum computing.<sup>6,7</sup> Because plasmon excitations are sensitive to their environment, biological and chemical processes can be probed using environment-induced plasmon modulation.<sup>8,9</sup> Plasmons can also transfer electromagnetic energy radiatively,<sup>10</sup> nonradiatively,<sup>11</sup> and/or via hot electron injection and thus can be used to catalyze reactions.<sup>12–14</sup> Due to these, and other, emerging uses, a deeper understanding of plasmon excited states is essential. Electron energy loss spectroscopy in the (scanning) transmission electron microscope ((S)TEM) has been used to gain insight into the physics of plasmonic structures at the nanoscale.<sup>15–17</sup> While theory has facilitated the distinction of bright and dark plasmon modes in more simple structures, distinguishing these modes in complex

geometries remains a challenge, as does imaging their photoexcited internal field structure.

Optical pump–probe strategies have long been critical tools to unravel complex materials phenomena. While the probe size typically limits spatial resolution, the temporal domain of pump–probe techniques is virtually unparalleled with sub-femtosecond laser pulses.<sup>18</sup> To push the spatial resolution over the past two decades optical pumps and focused electron probes have merged into ultrafast electron microscopies (UEMs) with modalities such as diffraction<sup>19,20</sup> and photo-induced near-field electron microscopy (see refs 21–25 for recent perspectives and reviews). For instance, 4D ( $x, y, z, t$ ) UEM systems utilize photocathodes, which are exposed to short laser pulses to generate electron beamlets (and single

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63 electrons) that synchronously arrive at the sample relative to a  
64 pulsed laser. Although only a few UEM systems exist  
65 worldwide, a wealth of interesting excited-state near-field  
66 information has been revealed as described below.

67 Electron energy gain due to electron/phonon coupling was  
68 first observed by Boerch et al. in 1966<sup>26</sup> and more recently in  
69 high energy resolution (S)TEM-based electron energy-loss  
70 spectroscopy (EELS).<sup>27,28</sup> Photon-stimulated electron energy-  
71 gain (sEEG) spectroscopy was first suggested by Howie,<sup>29</sup> and  
72 later Garcia de Abajo et al.<sup>30</sup> developed a theoretical  
73 framework for sEEG and suggested optical power densities  
74 of  $\sim 10^{10}$  W/m<sup>2</sup> would be necessary to observe continuous  
75 wave (cw) sEEG spectroscopy of gold nanostructures. The  
76 allure of sEEG spectroscopy is the possibility of accessing  
77 near-field phenomena not limited by the width of the zero loss  
78 peak (ZLP) or detector energy resolution, but rather by the  
79 spectral resolution of the stimulating optical pump. More  
80 recently, Barwick et al.<sup>31</sup> introduced photoinduced near-field  
81 electron microscopy (PINEM), which couples an intense laser  
82 pulse indirectly to a fast electron probe through the laser-  
83 induced evanescent near-field of the target material, thereby  
84 generating stimulated electron energy-loss (sEEL) and sEEG  
85 signals at discrete multiples of the photon energy ( $\pm n\hbar\omega$ ).  
86 They studied the electron energy-gain and stimulated energy-  
87 loss spectra of carbon nanotubes and compared them to silver  
88 nanorods.<sup>31</sup> The  $\sim 10^{14}$  W/m<sup>2</sup>, 200 fs pulses produced  
89 symmetric gain/loss spectra evidencing photon–plasmon–  
90 electron interactions involving up to 8 photon quanta. Later,  
91 energy-filtered PINEM maps were used to image the  
92 interference of Fabry–Perot-type surface plasmon polariton  
93 waves<sup>21</sup> as well as to visualize the channel-like patterns formed  
94 in the near-fields of entangled silver nanoparticles.<sup>32</sup> Recently,  
95 spectrally resolved PINEM experiments of silver nanorods  
96 have confirmed that optical energy resolutions of  $\sim 20$  meV  
97 can be obtained via a tunable light source.<sup>33</sup> Theoretical  
98 treatments of photoinduced sEEG have also been devel-  
99 oped,<sup>15,34–36</sup> and it was suggested that cw sEEG could be  
100 realized with irradiance values on the order of  $10^8$  W/m<sup>2</sup> for  
101 silver nanoparticles, though some have hypothesized<sup>23</sup> that  
102 impractically high sample heating would result at these cw  
103 irradiances, thus rendering cw sEEG/sEEL unfeasible.

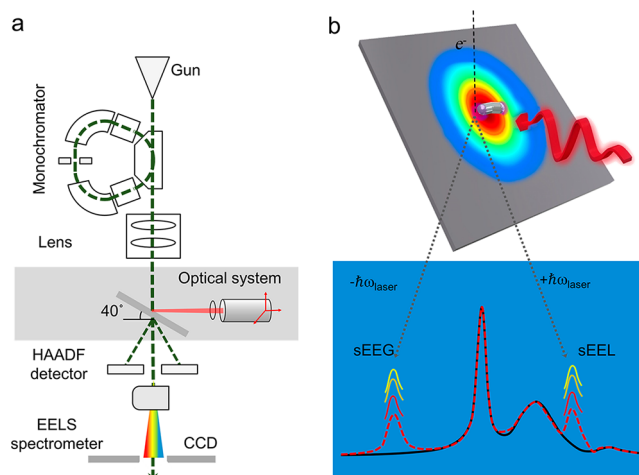
104 In an attempt to circumvent the need for a photocathode as  
105 done in standard PINEM experiments, recently, Das et al.<sup>37</sup>  
106 has reported a new method in which a high-power pulsed  
107 nanosecond laser ( $\sim 2$  eV photons, 5 ns pulse width, 10 kHz,  
108 duty cycle of  $5 \times 10^{-3}$  %, and peak irradiance on the order of  
109  $10^{14}$  W/m<sup>2</sup>) is used to expose the sample. sEEL and sEEG  
110 peaks at  $\pm 1$  and  $\pm 2\hbar\omega$  were realized with a modified detector  
111 that is synchronized with the laser pulse and only collects  
112 electrons that have interacted concurrently with the laser  
113 irradiation. Importantly, because they operated in a  
114 perturbative regime where no more than one gain event  
115 occurs per electron, they realized a resonant mode when the  
116 photon energy was tuned to the plasmon peak resonance  
117 energy. Furthermore, they overviewed a theory of dissipative  
118 quantum evolution and determined the number of photo-  
119 excited plasmons generated by the illumination to be on the  
120 order of 1.2 in their resonant regime.

121 As most PINEM experiments have demonstrated, at high  
122 enough photon irradiance virtually any photon–target  
123 interaction can stimulate loss/gain signals even when the  
124 optical transition (plasmonic or not) is weak. For instance,  
125 even biological samples have recently been imaged via

PINEM.<sup>38,39</sup> Here, through a combination of experiment  
and theory, we demonstrate a low-irradiance cw regime ( $10^8$   
W/m<sup>2</sup>) where strong photon–plasmon coupling is critical to  
observing the sEEL and sEEG signals; in this way, we expect  
bright plasmon modes to couple stronger than dark plasmon  
modes. This resonant mode provides the ability to spectrally  
and spatially map the steady-state near-field of individual  
plasmonic nanostructures via cw photoexcitation and a  
continuous electron source in the (S)TEM.

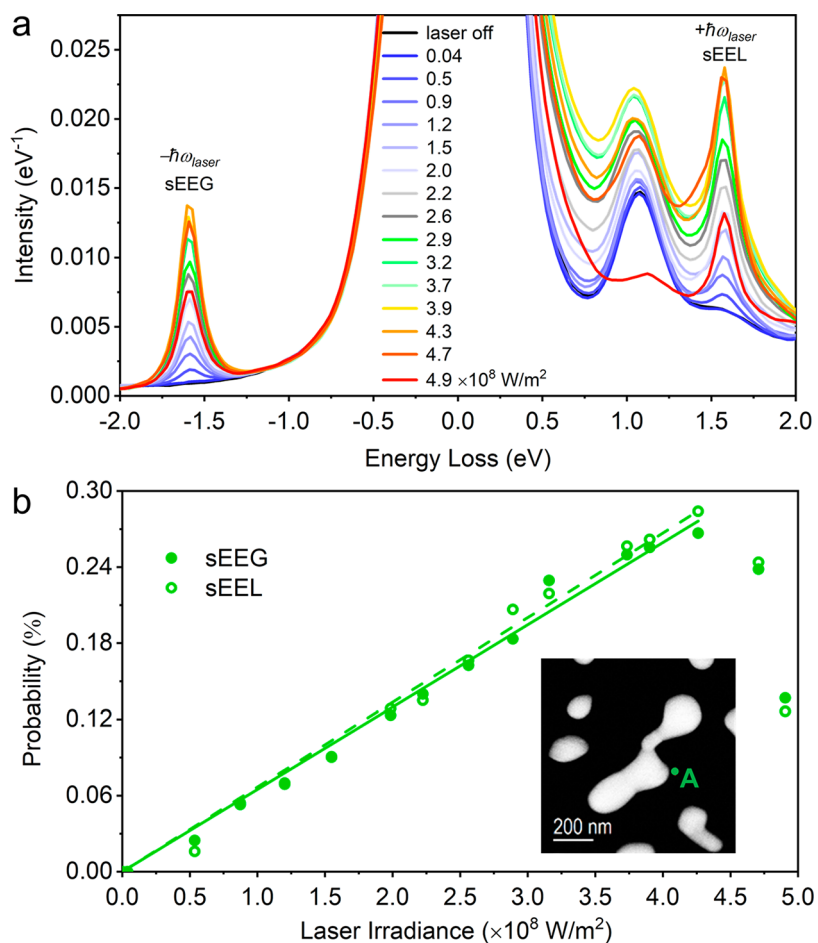
## RESULTS AND DISCUSSION

Motivated by these studies and the desire to investigate  
excited-state phenomena in plasmonic nanomaterials, we  
leveraged a recently developed optical delivery system that  
can be attached to any (S)TEM for both photothermal  
heating<sup>40</sup> and excitation modalities and used it to image the  
plasmonic responses of individual silver nanoparticles in the  
weak-field cw limit. The particles are photothermally dewetted  
from a continuous 30 nm thick silver film (see SI-I for detailed  
image) using our in situ laser delivery system. Fortuitously, the  
photothermally dewet nanostructures do not have any silver  
oxidation because they are generated in high vacuum and  
provided a distribution of particle shapes and sizes in which to  
probe for resonance with our laser energy. Figure 1a is a



**Figure 1.** Overview of (S)TEM/EELS and laser system. (a) Schematic of the monochromated (S)TEM/EELS instrument with the optical delivery system mounted orthogonal to the electron beam. (b) Illustration of the coincident and cw focused laser light and 200 keV electron beam; the laser spot has a 3.7  $\mu\text{m}$  radius Gaussian profile and interacts with the sample to produce signature sEEL and sEEG peaks whose intensities vary with laser irradiance.

schematic illustrating the system, developed by Waviks, Inc.,  
attached to a monochromated (S)TEM. The system consists  
of a laser diode with an emission wavelength of 785 nm and a  
1 nm (or 1.4 meV) full-width at half-maximum (fwhm) line  
width. The tunable laser optical power (up to 215 mW) is  
coupled to a 5  $\mu\text{m}$  diameter single-mode fiber optic, and the  
end of the fiber is placed at the focal distance of the lens  
subsystem, which reimages the fiber-optic end with unit  
magnification at an approximate working distance of 1 cm. As  
shown in Figure 1a and b, the unpolarized 3.7  $\mu\text{m}$  radius  
Gaussian laser spot (at  $1/e^2$  irradiance measured at normal  
incidence and thus slightly elongated due to the tilt) is focused  
and aligned to the (S)TEM electron coincident point on a 40°



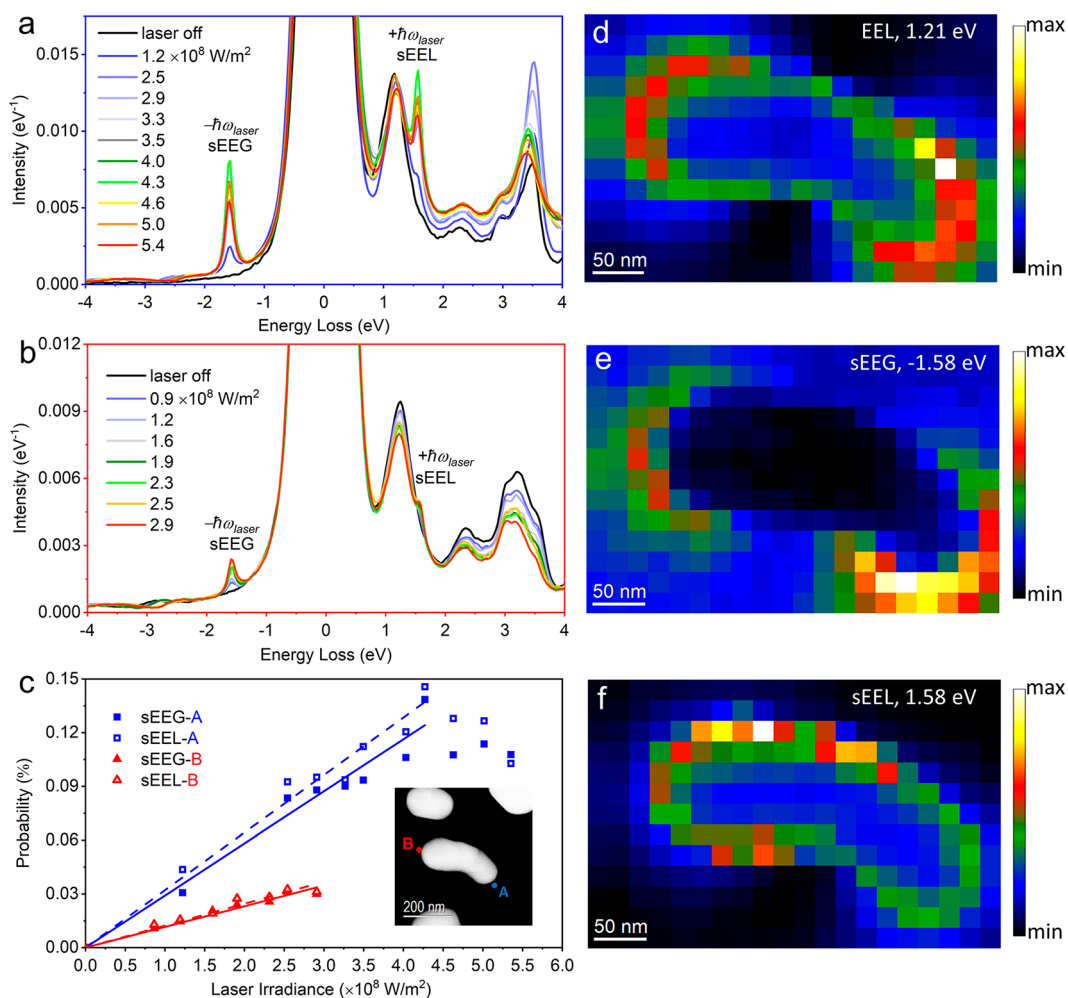
**Figure 2.** sEEL and sEEG of a silver irregular nanoparticle as a function of laser irradiance. (a) Unprocessed low-loss EEL/EEG point spectra of a photothermally dewetted silver nanoparticle as a function of laser irradiance ( $\times 10^8$  W/m<sup>2</sup>) at the aloof beam position indicated by the green bullet and label A. (b) Integrated sEEG and sEEL probabilities as a function of laser irradiance for the spectra in (a). The solid and dashed lines are linear fits to the sEEG and sEEL data, respectively.

tilted sample via a three-axis nanomanipulator system (see Wu et al. for system details).<sup>40</sup> While all results presented here were operated in cw, the laser can be pulsed down to a several-nanosecond pulse width at up to 16 MHz frequency at a wavelength of 785 nm (1.58 eV). At maximum power and focus, a cw irradiance on the 40° tilted substrate can reach up to  $\sim 2 \times 10^9$  W/m<sup>2</sup>.

**Figure 2a** shows the unprocessed low-loss sEEL/sEEG point spectra of a photothermally dewetted silver nanoparticle (see HAADF (S)TEM image in inset) as a function of laser power at the aloof beam position indicated by position A (see SI-ii for full spectra). Inspection of the EEL spectrum (without laser irradiation) reveals an energy resolution of 0.136 eV as measured by the fwhm of the ZLP. During the experiment, there are slight changes in the ZLP attributed to microscope instabilities and a change in the high-energy side of the background consistent with electron beam induced carbon deposition from prolonged electron exposure. The surface plasmons are clearly visible and no noise reduction or other data enhancement was performed on the spectra. In the laser-irradiated spectra, two additional peaks emerge and are attributed to the sEEL and sEEG peaks at  $\pm \hbar \omega_{\text{laser}}$ , respectively, at  $\pm 1.58$  eV. For clarity we plot the data using standard EELS convention so the sEEG signature is at negative electron energy loss.

For the zero-irradiance spectra (laser off), there are two plasmon peaks in this low-loss region of interest: one centered at  $\sim 1.05$  eV and another small peak centered near the laser wavelength 1.48 eV. Detailed peak fitting of the spectra was performed to analyze the full low-loss/gain spectra (see SI-iii for details). Notably, the average fwhm of the sEEL and sEEG peak fits ( $0.136 \pm 0.0089$  eV) match well with the fwhm of the ZLP.

**Figure 2b** is a plot of the integrated sEEG and sEEL probabilities as a function of laser irradiance for the spectra in **Figure 2a**. Interestingly, the EEL spectrum in **Figure 2a** at zero laser irradiance has only a small plasmon peak near the 1.58 eV laser energy; however, the laser couples strongly to this apparent bright mode, which also interacts with the field of the swift ( $< 500$  attosecond interaction time) passing STEM electron, as evidenced by the strong sEEL and sEEG peaks in the spectrum. Notably, the sEEL and sEEG peaks increase approximately linearly as a function of laser irradiance in the range of  $8.8 \times 10^7$  to  $4.3 \times 10^8$  W/m<sup>2</sup>. Consistent with previous PINEM results<sup>31,32</sup> and as discussed below in our modeling results, the sEEL and sEEG peak intensities have approximately the same integrated probability. Note that because of the relatively low cw laser irradiance values relative to PINEM, only single quantum exchanges of energy between the laser, target, and electron beam are observed, as no multiphoton sEEL and sEEG responses are detected. Addi-



**Figure 3.** sEEL and sEEG of a silver rod-like nanoparticle as a function of laser irradiance. Unprocessed low-loss EEL spectra of silver rod-like structures at (a) position A and (b) position B as a function of laser irradiance ( $\times 10^8$   $\text{W/m}^2$ ) at the aloof beam position. The positions A and B are indicated in the inset of (c). (c) Integrated sEEG and sEEL probabilities as a function of laser irradiance. The solid (sEEG) and dashed (sEEL) lines are linear fits for the data obtained at position B (blue) and C (red), respectively. The solid and dashed lines are linear fits to the sEEG and sEEL data, respectively. EEL maps of (d) the 1.21 eV dipole peak at zero irradiance, (e)  $-1.58$  eV sEEG map, and (f) the  $+1.58$  eV sEEL map, both at  $2 \times 10^8$   $\text{W/m}^2$  irradiance.

tionally, and consistent with the lower irradiance, there is no detectable change in the ZLP intensity. Interestingly, both peak intensities decrease at irradiance values of  $>4.3 \times 10^8$   $\text{W/m}^2$ , which is attributed to photothermal heating of the silver nanostructure, which is known to damp plasmons and shift the resonance to lower energy. Anecdotaly, when the laser is increased slightly to  $5 \times 10^8$   $\text{W/m}^2$ , the silver nanostructures studied evaporate completely (see SI-iv for images). Furthermore, the broad plasmon modes associated with the electron-beam-induced carbon deposition also concurrently decrease in the  $>4.3 \times 10^8$   $\text{W/m}^2$  irradiance region.

Figure 3a and b show the point spectra as a function of irradiance at the aloof positions of the rod-like structure shown in the inset of Figure 3c (see SI-ii for full low-loss spectra); again no data processing was performed for the spectra. Figure 3c is a plot of the integrated sEEL and sEEG probabilities as a function of irradiance taken at these two positions (ignoring the spontaneous EEL contribution convoluted on the loss side); note the sEEL and sEEG probabilities are again comparable for each position. The rod has approximate dimensions of  $\sim 330$  nm long, an average width of  $\sim 120$  nm, and average height of  $\sim 100$  nm (assuming an equilibrium

wetting angle for the trans-axial dimension of  $135^\circ$ ). At the aloof positions at the rod ends, the spectra consist of peaks associated with the longitudinal dipole (1.21 eV), longitudinal quadrupole (2.3 eV), and several higher energy ( $>3$  eV) modes including the transverse dipole among higher order modes. Note the intensity of the higher order mode peak at  $\sim 3.5$  eV varies in the unprocessed data, which has contributions from carbon deposition (and removal at higher irradiance) and likely slight electron beam mispositioning over the duration of the experiment. No multiphoton sEEL is contributing, as evidenced by the energy-gain region having no peaks at  $-\hbar\omega_{\text{laser}} = 3.16$  eV. Figure 3d illustrates the 1.21 eV dipole mode EELS map at zero irradiance, which has the expected high probability distribution at the rod ends (see SI-v for complementary 2.3 eV quadrupole mode map). Figure 3e and f are the associated sEEG and sEEL probability maps, respectively, when exposed to an irradiance of  $\sim 2 \times 10^8$   $\text{W/m}^2$ . The sEEG probability map is consistent with the longitudinal dipole map, which suggests good coupling to this bright mode despite the laser energy being detuned  $\sim 0.37$  eV to higher energy from the dipole plasmon resonance. As the spectra illustrate in Figure 3a and b and the longitudinal

dipole map suggests in Figure 3d, the EEL probability is slightly higher on the right side of the rod, and thus concomitantly the sEEG and sEEL probabilities are slightly higher on the right-hand side of the rod. For position A, where relatively higher laser powers were explored, the sEEL and sEEG probabilities decrease when the irradiance exceeded  $\sim 4 \times 10^8 \text{ W/m}^2$ , and the silver nanostructure evaporated when the irradiance exceeded  $5.4 \times 10^8 \text{ W/m}^2$  (see image in SI-vi).

According to Das et al.,<sup>37</sup> at low laser intensities where the stimulated sEELS and sEEGS intensities are on the order of the spontaneous EELS intensity, the mean number of stimulated plasmons ( $M$ ) can be deduced by taking a ratio of the spontaneous plus stimulated loss intensity to the stimulated gain intensity, where this ratio is equal to  $(M + 1)/M$ . Based on the deconvolved spectra that includes only the longitudinal dipole peak (at 1.2 eV) and the stimulated gain (at  $-1.58 \text{ eV}$ ) and loss (at  $1.58 \text{ eV}$ ) peaks, the experimental peak integrated intensities were determined from Figure 3a spectra collected at  $1.2, 2.5$ , and  $4 \times 10^8 \text{ W/m}^2$  irradiance. The experimental ratios were determined to be  $24.1, 10.5$ , and  $8.7$ , respectively; thus the mean number of photoexcited plasmons at these irradiances were estimated to be  $0.04, 0.10$ , and  $0.13$ , respectively.

Due to the weak interaction of light with matter and the low cw laser intensity and (S)TEM electron current used herein, the spectral signatures of sEEL and sEEG can be well understood using time-dependent perturbation theory up to second order in electron–plasmon and photon–plasmon interactions. Each of these interactions either reduce or increase the (S)TEM electron momentum from  $\hbar k_i$  to  $\hbar k_f = \hbar k_i - \hbar q$ , with  $\hbar q$  being a small ( $|\hbar q| \ll \hbar k_i$ ) transfer momentum that is positive in energy-loss events and negative in energy-gain events.

In both cases, the cw laser and nanoparticle plasmons are assumed to have reached a steady state prior to the electron–plasmon interaction. Additionally, we choose the initial

population  $M_\lambda(\omega) = M_\lambda^{\max} \frac{\gamma_{\text{laser}}^2}{(\omega - \omega_{\text{laser}})^2 + \gamma_{\text{laser}}^2}$  of each plasmon state  $\lambda$  to be frequency-dependent to model the excitation of a continuous plasmon density of states by a laser of line width  $\gamma_{\text{laser}}$  and peak frequency  $\omega_{\text{laser}}$ . Letting the laser polarization and longitudinal dipole plasmon be oriented along the  $x$ -axis, the longitudinal plasmon occupation number is  $M_x(\omega) \geq 0$  such that the initial state of the three dipole plasmons is  $|M_x(\omega), 0_y, 0_z\rangle$ , with the occupation numbers of the undriven transverse ( $y, z$ ) plasmons taken to be zero. The initial state of the laser-populated photon field is given by the collective photon state  $|\{N\}\rangle = | \dots, N_\omega, N_{\alpha'}, N_{\alpha''}, \dots \rangle$ , with  $\alpha$  the collective index of each photon mode and  $N_\alpha$  the occupation number of the  $\alpha$ th photon mode. Additionally, the initial state of the (S)TEM electron, whose motion along directions perpendicular to its propagation axis can be safely neglected for sufficiently small  $q$ , is well-approximated as a box-quantized, one-dimensional free particle with a wave function  $\langle \mathbf{r} | k_i \rangle = \phi_R(\mathbf{R}) \exp(ik_z z) / \sqrt{L}$ . Here,  $\mathbf{R}$  is the cylindrical radial vector and  $|\phi_R(\mathbf{R})| \approx \delta(\mathbf{R} - \mathbf{R}_0)$ , with  $\mathbf{R}_0$  being the impact parameter of the electron.<sup>36</sup> To be consistent with the

definition of the photon field, the electron wave function is described in second quantization (see SI-vi) as  $|k_i\rangle = | \dots, 0, 1_{k_i}, 0, \dots \rangle$ , with all modes having an occupation number of zero except the  $k_i^{\text{th}}$  state of momentum  $\hbar k_i$ , which has an occupation number of one.

Collectively, the initial state of the system is then  $|i\rangle = |k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\}\rangle$ , and the allowed final states are determined by the electron–plasmon and photon–plasmon

coupling,  $\hat{H}_{\text{el-pl}} = -\hat{\mathbf{d}} \cdot \hat{\mathbf{E}}_{\text{el}} = \sum_{kk'\lambda} (g_{k'k\lambda} \hat{c}_k^\dagger \hat{c}_k \hat{b}_\lambda^\dagger + g_{k'k\lambda}^* \hat{c}_k^\dagger \hat{c}_k \hat{b}_\lambda)$  and  $\hat{H}_{\text{ph-pl}} = -\hat{\mathbf{d}} \cdot \hat{\mathbf{E}}_{\text{ph}} = \sum_{\alpha\lambda} g_{\alpha\lambda} (\hat{b}_\lambda^\dagger \hat{a}_\alpha - \hat{b}_\lambda \hat{a}_\alpha^\dagger)$ , with  $\lambda = x, y, z$  labeling the three nanoparticle dipole plasmons and  $\hat{\mathbf{E}}_{\text{el}}$  and  $\hat{\mathbf{E}}_{\text{ph}}$  being the time-dependent electric field operators of the electron and photon fields. Here,  $\hat{\mathbf{d}} = \sum_\lambda d_\lambda (\hat{b}_\lambda + \hat{b}_\lambda^\dagger) \mathbf{e}_\lambda$  is the transition dipole operator of the dipole plasmon modes of the rod with  $\hat{b}_\lambda$  being the annihilation operator of the dipole plasmon oriented in the  $\lambda$ -direction, denoted by the unit vector  $\mathbf{e}_\lambda$ . Analogously,  $\hat{a}_\alpha$  and  $\hat{c}_k$  are the annihilation operators of the  $\alpha$ th photon mode and  $k$ th electron mode, respectively. The coupling strengths

$$g_{k'k\lambda} = -\frac{2ek' - kld_\lambda}{\gamma^2 L} \kappa_\lambda \left( \frac{|k' - k|R_0}{\gamma} \right)$$

and

$$g_{\alpha\lambda} = -i \sqrt{\frac{2\pi\hbar\omega_\alpha}{V}} d_\lambda (\mathbf{e}_\lambda \cdot \mathbf{e}_{\alpha})$$

in which

$$\kappa_{x,y} \left( \frac{|k' - k|R_0}{\gamma} \right) = -\gamma K_1 \left( \frac{|k' - k|R_0}{\gamma} \right) \frac{\mathbf{R}_0 \cdot \mathbf{e}_{x,y}}{R_0}$$

and

$$\kappa_z \left( \frac{|k' - k|R_0}{\gamma} \right) = -i \frac{k' - k}{|k' - k|} K_0 \left( \frac{|k' - k|R_0}{\gamma} \right)$$

depend upon the radiation mode frequencies  $\omega_\omega$  polarizations  $\mathbf{e}_\omega$  and quantization volume  $V$ , as well as the Lorentz contraction factor  $\gamma$  and quantization length  $L$  (see SI-vi).

Inspection of the different allowed time orderings of  $\hat{H}_{\text{el-pl}}$  and  $\hat{H}_{\text{ph-pl}}$  within the calculation of a second-order transition rate from  $|i\rangle = |k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\}\rangle$ , to  $|f\rangle = |k_f, \{N'\}, \{M'_x(\omega), M'_y, M'_z\}\rangle$ , reveals that only four second-order scattering processes contribute: the plasmon may gain (simultaneous plasmon excitation (SPE)) or lose (simultaneous plasmon deexcitation (SPD)) two quanta of energy during the interaction, or it may simply mediate energy transfer from the photon field to the electron probe (stimulated electron energy-gain (sEEG)) or vice versa (stimulated electron-induced emission of radiation (sEIRE)).

Of the four processes, only SPE and sEIRE can contribute to the total loss signal. As SPE is the stimulated analog of the more commonly known EEL process, one might expect its contribution to the loss signal to be of prime importance. The transition rate for SPE is given by

$$w_{\text{SPE}}^{(2)} = \frac{2\pi}{\hbar} \left| \sum_m \frac{\langle k_f, \{..., N_\alpha - 1, ...\}, \{M_x(\omega) + 2, 0_y, 0_z\} | \hat{H}_{\text{el-pl}} | m \rangle \langle m | \hat{H}_{\text{ph-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_m} \right. \\ \left. + \sum_{m'} \frac{\langle k_f, \{..., N_\alpha - 1, ...\}, \{M_x(\omega) + 2, 0_y, 0_z\} | \hat{H}_{\text{ph-pl}} | m' \rangle \langle m' | \hat{H}_{\text{el-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_{m'}} \right|^2 \delta(E_f - E_i) \quad (1)$$

353

354

355 wherein the first term describes the properly time-ordered  
356 single-electron and single-photon interaction with the initial  
357 plasmon state  $|\{M_x(\omega), 0_y, 0_z\}\rangle$ , leaving the (S)TEM electron  
358 decelerated ( $q > 0$ ) by interaction with the excited surface  
359 plasmon. The second represents the improper time ordering of  
360 the two interactions, in which the electron scattering precedes  
361 the absorption of a photon. While not intuitive, the fact that  
362 both time orderings contribute to this scattering process (as  
363 opposed to the strictly causal interactions) has been discussed

extensively in the literature.<sup>41–43</sup> Remarkably, the addition of  
the two oppositely time-ordered terms in eq 1 (see SI-vi)  
results in a transition rate of zero. As a result, the second-order  
contribution to the total loss signal is completely determined  
by the rate of the sEIRE process as demonstrated below (see  
also SI-vi), with SPE providing no contribution.

Analyzing the two possible gain processes, SPD and sEEG,  
one can show that the transition rate of SPD,

$$w_{\text{SPD}}^{(2)} = \frac{2\pi}{\hbar} \left| \sum_m \frac{\langle k_f, \{..., N_\alpha + 1, ...\}, \{M_x(\omega) - 2, 0_y, 0_z\} | \hat{H}_{\text{el-pl}} | m \rangle \langle m | \hat{H}_{\text{ph-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_m} \right. \\ \left. + \sum_{m'} \frac{\langle k_f, \{..., N_\alpha + 1, ...\}, \{M_x(\omega) - 2, 0_y, 0_z\} | \hat{H}_{\text{ph-pl}} | m' \rangle \langle m' | \hat{H}_{\text{el-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_{m'}} \right|^2 \delta(E_f - E_i) \quad (2)$$

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374 is also zero by similar reasoning (see SI-vi). Therefore, the  
375 second-order contributions to the total loss and gain signals  
376 are entirely described by the transition rates  $w_{\text{sEIRE}}^{(2)}$  and  $w_{\text{sEEG}}^{(2)}$ ,  
377 respectively, which describe the likelihood that the (S)TEM

electron and a photon will interact simultaneously with the  
plasmon, causing a deceleration and acceleration of the  
electron, respectively. These transition rates can be calculated  
as

$$w_{\text{sEIRE}}^{(2)} = \frac{2\pi}{\hbar} \left| \sum_m \frac{\langle k_f, \{..., N_\alpha + 1, ...\}, \{M_x(\omega), 0_y, 0_z\} | \hat{H}_{\text{el-pl}} | m \rangle \langle m | \hat{H}_{\text{ph-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_m} \right. \\ \left. + \sum_{m'} \frac{\langle k_f, \{..., N_\alpha + 1, ...\}, \{M_x(\omega), 0_y, 0_z\} | \hat{H}_{\text{ph-pl}} | m' \rangle \langle m' | \hat{H}_{\text{el-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_{m'}} \right|^2 \delta(E_f - E_i) \quad (3)$$

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383

384

and

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$$w_{\text{sEEG}}^{(2)} = \frac{2\pi}{\hbar} \left| \sum_m \frac{\langle k_f, \{..., N_\alpha - 1, ...\}, \{M_x(\omega), 0_y, 0_z\} | \hat{H}_{\text{el-pl}} | m \rangle \langle m | \hat{H}_{\text{ph-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_m} \right. \\ \left. + \sum_{m'} \frac{\langle k_f, \{..., N_\alpha - 1, ...\}, \{M_x(\omega), 0_y, 0_z\} | \hat{H}_{\text{ph-pl}} | m' \rangle \langle m' | \hat{H}_{\text{el-pl}} | k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\} \rangle}{E_i - E_{m'}} \right|^2 \delta(E_f - E_i) \quad (4)$$

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387

388 with  $k_f < k_i$  in  $w_{\text{sEIRE}}^{(2)}$  and  $k_f > k_i$  in  $w_{\text{sEEG}}^{(2)}$ . It is straightforward  
389 to show that the second-order sEEG transition rate recovers  
390 the same result given in ref 36 with  $M_x(\omega) \rightarrow 0$ , as the second  
391 (improper) term of eq 4 becomes zero. However, even at finite  
392  $M_x(\omega)$ , both  $w_{\text{sEEG}}^{(2)}$  and  $w_{\text{sEIRE}}^{(2)}$  turn out to be independent of  
393 the initial plasmon occupation number (see SI-vi) and  $w_{\text{sEEG}}^{(2)}$   
394 agrees with previous work for any  $M_x(\omega)$ . It is also important  
395 to note that even though sEIRE photons are not detected in  
396 our experiment, eq 3 nonetheless shows that the loss  
397 signatures of the sEIRE process are encoded in the final  
398 electron energy spectrum.

In addition to the second-order contributions to the total  
loss rate, the fast electron probe can also lose or gain energy  
by interacting with the laser-excited plasmon mode *without* the  
simultaneous creation or destruction of a photon. The rates of  
these phenomena are calculated at first order. In the case of  
energy loss, the electron can further lose energy to modes  
beyond those that are pumped by the laser such that the total  
first-order energy loss rate of all three plasmons is

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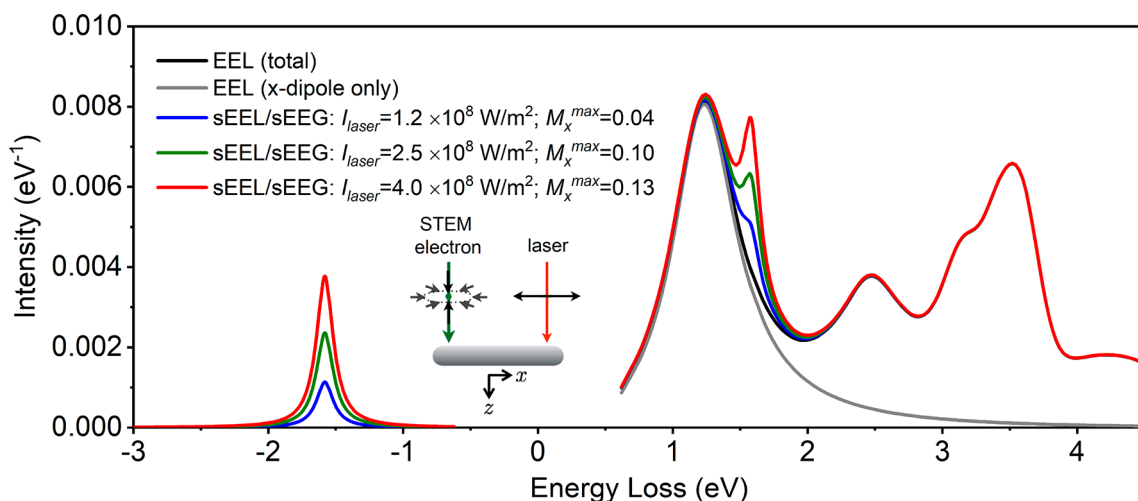
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**Figure 4.** Computed total loss and gain spectra of a silver nanorod interacting with the pair of co-propagating cw laser and STEM-electron beams illustrated in the inset. The simulated EEL spectrum is also shown for reference and is the limiting behavior of the sEEL signal when the laser field is removed. The sEEL and sEEG profiles are symmetrically distributed at  $\pm\hbar\omega_{\text{laser}} = \pm 1.58$  eV and, after subtracting the EEL spectral profile, are otherwise of equal amplitude up to a factor of  $(N + 1)/N$ . The sEEL and sEEG spectra were calculated with an electron beam impact parameter of 107 nm and a plasmon effective mass of  $1.6 \times 10^{-34}$  g. Additionally, the theoretical curves were calculated with a maximum plasmon occupation number of  $M_x^{\text{max}}$  of 0.04, 0.10, and 0.13, which are extracted from the measured  $I_{\text{laser}} = 1.2, 2.5,$  and  $4.0 \times 10^8$  W/m<sup>2</sup> spectra in Figure 3 together with eqs 7 and 8. Finally, all curves were convolved with a normalized Lorentzian distribution with a fwhm of 150 meV to model the finite energy resolution of the instrument.

$$w_{\text{EEL}} + w_{\text{sEEL}}^{(1)} = \sum_{\lambda} \frac{2\pi}{\hbar} |\langle k_f, \{N\}, \{..., M_x(\omega) + 1, ... \}|$$

$$\hat{H}_{\text{el-pl}} |k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\}\rangle^2 \delta(E_f - E_i)$$

with  $w_{\text{EEL}}$  the well-known spontaneous EEL rate and  $w_{\text{sEEL}}^{(1)}$  the first-order stimulated EEL rate (SI-vi). Therefore,  $w_{\text{sEEL}}^{(1)}$  and  $w_{\text{EEL}}$  must be added to  $w_{\text{SEIRE}}^{(2)}$  to reconstruct the total loss spectrum measured in our experiment.

Similarly, the total first-order contribution to the gain rate is

$$w_{\text{sEEG}}^{(1)} = \frac{2\pi}{\hbar} |\langle k_f, \{N\}, \{M_x(\omega) - 1, 0_y, 0_z\}| \hat{H}_{\text{el-pl}}$$

$$|k_i, \{N\}, \{M_x(\omega), 0_y, 0_z\}\rangle^2 \delta(E_f - E_i)$$

which, in contrast to the first-order loss rate, contains no spontaneous contributions. It is thus clear that the total gain signal,  $w_{\text{sEEG}}^{(1)} + w_{\text{sEEG}}^{(2)}$ , is entirely caused by the sEEG process, allowing the label “total gain” to be dropped. Similarly on dropping the label “total loss” in favor of sEEL now that all loss processes are accounted for, the sEEL and sEEG functions can be expressed in the following intuitive forms (see SI-vi),

$$\Gamma_{\text{sEEL}}(\omega) \approx \Gamma_{\text{EEL}}(\omega) + \left( M_x(\omega) + \frac{\pi}{2\hbar\omega_x} \sigma_x(\omega_x) I(\omega) \right) \Gamma_{\text{EELx}}(\omega) \quad (5)$$

419

420 and

$$\Gamma_{\text{sEEG}}(\omega) = \left( M_x(-\omega) + \frac{\pi}{2\hbar\omega_x} \sigma_x(\omega_x) I(-\omega) \right) \Gamma_{\text{EELx}}^{(-)}(\omega) \quad (6)$$

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which are simply related to the sum of the individual rates<sup>36</sup> over the full spectrum of possible final states of the electron probe and photon field and are expressed in units of percent per unit loss/gain energy. Specifically,  $\Gamma_{\text{EELx}}(\omega)$  is a measure of EEL to only the longitudinal dipole plasmon with natural frequency  $\Omega_x = \omega_x - i\gamma_x(\omega)$ , while  $\Gamma_{\text{EEL}}(\omega)$  is simply the sum of the EEL contributions from all three dipolar plasmons

modes.  $I(\omega)$  is the spectral intensity, measured in units of 429 intensity per unit frequency of the cw laser source and  $\sigma_x(\omega)$  is 430 the extinction cross section of the longitudinal dipole plasmon. 431 In eq 6, the superscript  $(-)$  indicates that the EELx function 432 of eq 5 has been reflected across  $\omega = 0$  such that the sEEG 433 signal appears at negative frequencies. Explicitly, 434

$$\Gamma_{\text{EELx}}(\omega) = \frac{4e^2\omega^2}{\pi\hbar^2v^4\gamma^4} \left[ \frac{\gamma^2(\mathbf{R}_0 \cdot \mathbf{e}_x)^2}{R_0^2} K_1^2 \left( \frac{|\omega|R}{v\gamma} \right) \right] \text{Im}\{\alpha_x(\omega)\}$$

with  $\alpha_x(\omega) = d_x^2/(\hbar\Omega_x - \hbar\omega)$ ; the expression for  $\Gamma_{\text{EELx}}^{(-)}(\omega)$  can 435 then be acquired by letting  $\omega \rightarrow -\omega$ . 436

For sufficiently narrow laser line widths, eqs 5 and 6 can be 437 simplified by letting 438

$$I(\omega)\Gamma_{\text{EELx}}(\omega) \rightarrow I_{\text{laser}} \frac{1}{\pi} \frac{\gamma_{\text{laser}}}{(\omega - \omega_{\text{laser}})^2 + \gamma_{\text{laser}}^2} \Gamma_{\text{EELx}}(\omega_{\text{laser}})$$

and 439

$$I(-\omega)\Gamma_{\text{EELx}}^{(-)}(\omega) \rightarrow I_{\text{laser}} \frac{1}{\pi} \frac{\gamma_{\text{laser}}}{(-\omega - \omega_{\text{laser}})^2 + \gamma_{\text{laser}}^2} \Gamma_{\text{EELx}}^{(-)}(-\omega_{\text{laser}})$$

respectively, with  $I_{\text{laser}}$  the peak laser irradiance, giving (see SI- 440 vi) 441

$$\begin{aligned} \Gamma_{\text{sEEL}}(\omega) &\approx \Gamma_{\text{EEL}}(\omega) + M_x(\omega)\Gamma_{\text{EELx}}(\omega) \\ &+ \left( \frac{\sigma_x(\omega_x)I_{\text{laser}}}{2\hbar\omega_x} \frac{N+1}{N} \frac{\gamma_{\text{laser}}}{(\omega - \omega_{\text{laser}})^2 + \gamma_{\text{laser}}^2} \right) \Gamma_{\text{EELx}}(\omega_{\text{laser}}) \end{aligned} \quad (7) \quad 442$$

and 443

$$\begin{aligned} \Gamma_{\text{sEEG}}(\omega) &\approx M_x(-\omega)\Gamma_{\text{EELx}}^{(-)}(\omega) \\ &+ \frac{\sigma_x(\omega_x)I_{\text{laser}}}{2\hbar\omega_x} \frac{\gamma_{\text{laser}}}{(-\omega - \omega_{\text{laser}})^2 + \gamma_{\text{laser}}^2} \Gamma_{\text{EELx}}^{(-)}(-\omega_{\text{laser}}) \end{aligned} \quad (8) \quad 444$$

Here  $N$  is the occupation number of the single cw laser mode 445 modeled in the narrow-width limit. Note that for large  $N$ , the 446

sEEL and sEEG functions become equivalent, up to the magnitude of the EEL signal, at each  $\pm\omega$ . Note also that sEEL reduces to EEL, while sEEG vanishes in the limit where the laser irradiance (and therefore  $M_x(\omega)$ ) is reduced to zero. These expressions, while approximate, make explicit the dependence of sEEL and sEEG upon optical extinction and EELS and provide a simple route to computing sEEL and sEEG spectra using continuum optical and electron scattering codes such as the DDA,<sup>44,45</sup> MNPBEM,<sup>46</sup> and e-DDA.<sup>47,48</sup>

Figure 4 shows the theoretical sEEL, sEEG, and EEL spectra calculated for a  $321 \times 120 \times 120$  nm<sup>3</sup> silver nanorod lying on a SiO<sub>2</sub> substrate in a vacuum. Here, the electron beam and laser field co-propagate down an axis that is oriented normal to the long axis of the nanorod (see inset). The spectra are convolved pointwise with a normalized Lorentzian distribution of variance determined by the width of the ZLP (150 meV). Subtraction of the EEL spectrum from the sEEL spectrum would show that the stimulated gain and loss functions are nearly equivalent in amplitude as noted previously<sup>36</sup> with the difference arising only from the ratio  $(N + 1)/N$  that appears in  $w_{\text{SEIRE}}^{(2)}$ . In the limit of large laser occupation numbers ( $N + 1 \approx N$ ), integration of the experimental sEEL and sEEG spectra of Figure 3 as well as the theory given in eqs 7 and 8 between 0 and  $\pm 2$  eV allows for the inference of  $M_x^{\text{max}}$ . For peak laser intensities of 1.2, 2.5, and  $4.0 \times 10^8$  W/m<sup>2</sup>, the inferred maximum plasmon occupation numbers are 0.04, 0.10, and 0.13, respectively. Comparison of Figures 4 and 3a highlights the remarkable quantitative agreement between the sEEG and sEEL peaks of experiment and theory. This supports the idea that the low-intensity cw laser used in our experiment only weakly populates the nanoparticle plasmon mode, yet we are still able to measure gain signal.

The experimental demonstration and theoretical underpinnings of low-irradiance laser sEEL and sEEG illustrated here are an exciting first step in co-continuous electron and photon photoinduced near-field electron microscopy using a monochromated STEM and high-resolution EELS. To extend the optical power range, higher thermal conductivity and smaller membranes could be used to enhance heat dissipation at high irradiance. Furthermore, multispectral cw photoexcited sEEL and sEEG would be possible by coupling other laser diode wavelengths to the single-mode fiber, a project that is now underway. For instance, while EELS conveniently has access to the entire plasmonic spectrum, the combination of EELS and multispectral low-irradiance photoexcited sEEL and sEEG could distinguish between optically bright and dark modes as well as the excited-state internal field structure of the former. Thus, we envision that the near-field optical phenomena previously only visible with highly specialized UEMs will be accessible with a standard (S)TEM system equipped with the cw optical delivery source.<sup>40</sup>

## CONCLUSION

In summary, we have demonstrated stimulated electron energy-loss and stimulated electron energy-gain spectroscopy with a continuous wave laser source and monochromated electron source in a (S)TEM. These signatures emerge at an irradiance value of  $\sim 5 \times 10^7$  W/m<sup>2</sup> and increase approximately linearly to  $\sim 5 \times 10^8$  W/m<sup>2</sup>. Above this irradiance range, photothermal heating causes the sEEG and sEEL probability to decrease. sEEL and sEEG mapping of a rod-like silver nanostructure confirms that 1.58 eV photons couple to the bright longitudinal dipole plasmon mode.

Analytical modeling of the simultaneous (S)TEM electron– and cw laser photon–plasmon interactions based on time-dependent perturbation theory demonstrates the connection between the total loss and gain spectra and the more intuitive optical extinction, laser intensity, and normal EEL spectrum. By exploiting this connection, model simulations of the sEEL and sEEG of an individual silver nanorod elucidate the fundamental processing underlying our experimental observations. The ability to visualize the field structure of excited-state plasmons opens up new directions for optically stimulated fast electron spectroscopy of electronically excited nanomaterials, such as, the direct testing of optoelectronic circuits. One can also imagine that, coupled with a gas cell, plasmon-based sensors and catalytic reactions can be synchronously imaged and correlated to those modes that are bright. Importantly, the photon delivery instrument used in this study can be attached to practically any microscope and equipped with various light sources, thus providing a more universal approach to visualizing atomic scale near-field phenomena that are critical to many photonic applications.

## METHODS

**Sample Preparation.** An  $\sim 25$  nm silver film was RF magnetron sputter deposited directly onto 20 nm SiO<sub>2</sub> membranes (TEMwindows.com, a division of SiMPore Inc., Rochester, NY, USA). The silver film was sputtered at 20 W RF power, 25 standard cubic cm per minute Ar flow, and 5 mTorr chamber pressure.

**Experimental Apparatus.** A new photon delivery system was mounted on the monochromated Carl Zeiss LIBRA 200MC (S)TEM, as shown schematically in Figure 1. The optical delivery setup and laser information were elaborated in our previous work.<sup>40</sup> Peak powers up to  $>200$  mW can be delivered to the sample from a 785 nm wavelength laser diode system coupled through a 5  $\mu$ m single-mode fiber. The laser is gated by a software-controlled pulse generator that can vary the laser pulse width from a few nanoseconds to cw at repetition rates up to 16 MHz.

**EELS Experiments.** The TEM was operated at 200 kV in (S)TEM mode with a camera length of 945 mm. The collection semiangle ( $\beta$ ) was 45 mrad, and the convergence semiangle ( $\alpha$ ) was 10 mrad. The low-loss spectra were collected with a monochromator slit of 0.5  $\mu$ m, and a dispersion of 30 meV per channel was chosen for the spectrometer acquisition. The average energy resolution (defined as the full width at half-maximum of the zero-loss peak) was measured to be 136 meV for a summed spectrum; the energy spread for all single and summed spectra collected was between 120 and 150 meV. For each low-loss point spectrum, 10 frames with a dwell time of 0.1 s each were summed up to yield high count values and signal-to-noise ratios. The average energy resolution (defined as the full width at half-maximum of the zero-loss peak) was measured to be 136 meV. For the EELS map acquisition, a region of interest with  $20 \times 13$  pixel spectra (1 pixel  $\sim 19.5$  nm  $\times$  19.5 nm) is defined over the entire silver nanoparticle. The pixel dwell time for each pixel in the EEL maps is 0.3 s. The maps of the sEEG (−1.58 eV), sEEL (1.58 eV), 1.21 eV dipole mode, and the 2.3 eV quadrupole mode are generated using the Gatan Digital Micrograph software by plotting spectra intensity in designated energy slices within the 3D spectrum image data cube ( $x, y$ , energy-loss).

## ■ ASSOCIATED CONTENT

## ■ Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphotonics.9b00830.

STEM image of the dewet silver film, full low-loss electron energy loss spectra, peak fitting description and tabular data, STEM images before and after high laser fluence exposure, EELS map of the quadrupole mode of the rod-like structure from Figure 3 and representative point spectra from the map, detailed theoretical description of sEEL and sEEG modeling, detailed peak fitting script and procedure (PDF)

## ■ AUTHOR INFORMATION

## Corresponding Authors

\*E-mail: masiello@chem.washington.edu.

\*E-mail: gduscher@utk.edu.

\*E-mail: prack@utk.edu.

## ORCID

Chenze Liu: 0000-0001-6599-1616

Yueying Wu: 0000-0003-4345-2771

Zhongwei Hu: 0000-0002-2783-7981

Jacob A. Busche: 0000-0003-4797-9415

Jon P. Camden: 0000-0002-6179-2692

David J. Masiello: 0000-0002-1187-0920

Philip D. Rack: 0000-0002-9964-3254

## Author Contributions

C. Liu, Y. Wu, Z. Hu, and J. A. Busche are co-first authors.

## Author Contributions

C.L. and Y.W. performed the laser/(S)TEM/EELS experiments under the direction of P.D.R. and G.D. P.D.R., G.D., J.P.C., Y.W., and C.L. collaborated on the interpretation of the experimental results. C.L. and G.D. did the majority of the computer analysis of the experimental data. T.M.M. and G.A.M. designed and built the laser delivery system. Z.H., J.A.B., E.K.B., and N.P.M. formulated the theoretical model and performed numerical simulations with help from D.J.M. P.D.R., G.D., Z.H., C.L., J.A.B., and D.J.M. wrote the paper with contributions from all coauthors.

## Notes

The authors declare no competing financial interest.

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