1	Serial dependence generalizes across different stimulus formats, but not different sensory
2	modalities
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16	ABSTRACT
17	Visual perception is thought to be supported by a stabilization mechanism integrating information over
18	time, resulting in a systematic attractive bias in experimental contexts. Previous studies show that this
19	effect, whereby a current stimulus appears more similar to a previous one, depends on attention,
20	suggesting an active high-level mechanism that modulates perception. Here, we test the hypothesis that
21	such a mechanism may generalize across different stimulus formats or sensory modalities, effectively
22	abstracting from the low-level properties of the stimuli. Participants performed a numerosity
23	discrimination task, with task-relevant dot-array stimuli preceded by a sequence of visual (flashes) or
24	auditory (tones) stimuli encompassing different numerosities. Our results show a clear attractive bias
25	induced by visual sequential numerosity affecting an array of simultaneously presented dots, thus
26	operating across different stimulus formats. Conversely, auditory sequences did not affect the judgment
27	on visual numerosities. Overall, our results demonstrate that serial dependence in numerosity perception
28	operates according to the abstract representation of numerical magnitude of visual stimuli irrespective of
29	their format. These results thus support the idea that a high-level mechanism mediates visual stability and
30	continuity, which integrates relevant information over time irrespective of the low-level sensory
31	properties of the stimuli.
32	

# 33 KEYWORDS

34 Serial dependence; numerosity perception; visual stability.

**35** INTRODUCTION

36 One remarkable feature of our conscious visual perception is its stability and continuity over time: we

37 usually experience a smooth and seamless flow despite the noisiness of brain signals and the instability of

38 biological sensors. How does the brain keep vision stable and continuous? One possibility, raised by

39 recent studies, is that it does so by integrating information over time to smooth out noise from neural

40 signals and facilitate a continuous representation (e.g., Fischer & Whitney, 2014; Burr & Cicchini, 2014).

41

42 While such a process, resulting in a "continuity field," has potentially significant advantages in our

43 everyday perception due to the stability of the external world (Burr & Cicchini, 2014; Cicchini et al.,

44 2018), it results in systematic biases in the experimental context. Specifically, a current stimulus appears

45 more similar to a previous one than it actually is, even if the two stimuli are completely uncorrelated.

46 Such an attractive bias, named *serial dependence*, has been taken as a signature of a stabilization process.

47 Furthermore, serial dependence has been observed across several very different visual dimensions,

48 spanning from orientation (Fischer & Whitney, 2014; Cicchini et al., 2018), position (Manassi et al.,

49 2018), and numerosity (Corbett et al., 2011; Cicchini et al., 2014; Fornaciai & Park, 2018a), to motion

50 (Alais et al., 2017), visual variance (Suarez-Pinilla et al., 2018), face identity (Liberman et al., 2014) and

51 attractiveness (Xia et al., 2016), which suggests a general perceptual mechanism.

52

53 Although the nature of serial dependence has been subject to debate (Fritsche et al., 2017; Bliss et al., 54 2018), there is increasing evidence that it directly operates on perception (Cicchini et al., 2017; Manassi 55 et al., 2018; Fornaciai & Park, 2018a; Fornaciai & Park, 2018b; Pascucci et al., 2019). In a recent series 56 of experiments (Fornaciai & Park, 2018a), we demonstrated that serial dependence occurs in a spatially 57 localized fashion, which is the hallmark of a perceptual effect, but it also depends on attention. Indeed, it 58 occurs only if stimuli (or at least their spatial positions) are attended or behaviorally relevant (Fornaciai & 59 Park, 2018a; see also Fischer & Whitney, 2014). These results thus point to a model of serial dependence 60 based on high-level, spatially-specific modulations affecting the low-level perceptual processing of 61 attended/relevant stimuli, likely by means of modulatory feedback signals (e.g., see Lamme & Roelfsema, 62 2000).

63

64 A prediction based on the idea of a modulatory feedback mechanism is that serial dependence may

65 operate according to a more abstract representation of the stimuli, not completely tied to their low-level

sensory features. In the context of numerosity perception, a growing amount of evidence suggests that

67 approximate numerical processing is rooted into the sensory processing stream, starting from early

68 sensory areas (Fornaciai & Park, 2017; Fornaciai et al., 2017; Fornaciai & Park, 2018c; Cavdaroglu et al.,

69 2015; Cavdaroglu & Knops, 2018). However, later on in the processing stream, numerosity information

rom seems to be represented in an abstract format, relatively independent from its sensory origin (Piazza et al.,

71 2007; Arrighi et al., 2014; Anobile et al., 2016). A serial dependence mechanism based on a high-level

72 representation and modulatory feedback may thus be based on such an abstract representation of

- 73 numerosity.
- 74

75 Here, we address this very hypothesis by testing whether serial dependence in numerosity perception 76 works across different formats such as sequential (i.e., a series of events over time) and simultaneous (i.e., 77 a set of objects in space) numerosities, and across different sensory modalities (visual and auditory). To 78 do so, we employed a paradigm used in previous studies (Fornaciai & Park, 2018a), in which a task-79 irrelevant "inducer" is presented prior to task-relevant dot-array stimuli, with participants performing a 80 numerosity discrimination task. Differently from previous studies, however, we presented the inducer as a 81 sequence of visual (cross-format condition) or auditory (cross-modal condition) stimuli and measured its 82 effect on subsequent task-relevant dot-arrays. If serial dependence operates at the level of abstract 83 numerosity representation in the visual domain, an attractive bias should be observed in the visual 84 sequential inducer condition. If serial dependence operates at an even more abstract level encompassing 85 both visual and auditory domains, an attractive bias should be observed in both visual and auditory 86 inducer conditions.

87

To preview, our results show that serial dependence generalizes across different stimulus formats, but not
across different sensory modalities, thus supporting the idea of serial dependence as a high-level
mechanism, operating according to an abstract representation of the stimuli irrespective of their low-level

91 sensory properties, but limited to the modality of presentation.

92

# 93 METHODS

# 94 Participants

95 A total of 70 participants (including the author MF) took part in the study (47 females, mean age (mean  $\pm$ 96 SD = 20.07 ± 2.11 years old). Participants were rewarded with course credit, and signed a written 97 informed consent before participating in the study. All participants tested in the study were naïve to the 98 purpose of the experiment (with the exception of the author MF), had normal or corrected-to-normal 99 vision, and reported no history of neurological, attentional or psychiatric disorder. All the experimental 100 procedures were approved by the Institutional Review Board of the University of Massachusetts at 101 Amherst and were in line with the declaration of Helsinki. Note that the sample size included in each 102 experiment (see *Results*) was determined a priori based on the expected effect derived from previous

103 studies from our group. Namely, considering an expected effect size (Cohen's d) of approximately 0.6

104 (based on previous experiments employing a similar paradigm, both published and unpublished), a power

of 0.95, and a one-tailed t distribution, the total required sample size is 32 participants (for eachexperiment).

107

108 Apparatus and stimuli

109 All the stimuli employed in the experiment were created using the Psychophysics Toolbox (Brainard,

110 1997; Kleiner et al., 2007; Pelli, 1997) on Matlab (version r2016b; The Mathworks, Inc.). Visual stimuli

111 were presented on a monitor screen running at 144 Hz, with a resolution of  $1920 \times 1080$  pixel, and

encompassing approximately 35×20 degrees of visual angle from a viewing distance of about 80 cm.

113

114 The visual stimuli employed in the numerosity discrimination task were arrays of black and white dots 115 presented on a gray background. Such dot-array stimuli were systematically constructed to vary across 116 several non-numerical dimensions, in order to span equal ranges in three orthogonal dimensions: 117 numerosity (N), size (Sz), and spacing (Sp) (see Park et al., 2016; DeWind et al., 2015). Note that since 118 the main goal of the present study was to assess serial dependence effects on approximate numerical 119 judgments, we collapsed together the different non-numerical dimensions during data analysis. For details 120 about this stimulus construction scheme, see Park et al. (2016) and DeWind et al. (2015). Stimulus 121 parameters were set as follows. The reference stimulus always comprised 16 dots. Probe arrays comprised 122 8, 10, 13, 16, 20, 25, or 32 dots. The smaller individual area of each dot was set to 113 pixel<sup>2</sup> (0.038 deg<sup>2</sup>), 123 corresponding to a diameter of 0.11 deg (6 pixels), while the maximum individual area was 452 pixel<sup>2</sup> 124 (0.15 deg<sup>2</sup>), corresponding to a diameter of 0.22 deg (12 pixel). The minimum field area, corresponding to 125 the circular area within which the dots were drawn, was 70,686 pixel<sup>2</sup> (23.9 deg<sup>2</sup>), encompassing 5.5 126 degrees of visual angle in diameter (300 pixels), while the maximum field area was 282,743 pixel<sup>2</sup> (95.7 127 deg<sup>2</sup>), encompassing 11 degrees in diameter (600 pixels). In all cases, individual dot size was kept equal 128 within an array, and the minimum distance between any two dots was no smaller than the radius of the 129 dots.

130

131 Inducer stimuli, on the other hand, could be either a sequence of brief sounds, or a sequence of brief

132 visual flashes. In both cases, they included either 10 or 25 stimuli. Auditory inducer stimuli were pure

tones (frequency = 700 Hz) played by means of two speakers (Logitech Multimedia Speakers 2200)

134 located behind the screen in positions corresponding to that of the visual stimuli (sound intensity ~65 dB).

135 Visual inducer stimuli were white circles with a constant radius of 2.5 deg, presented at 85% contrast. In

136 Exp. 1, in both conditions (auditory and visual), 10- and 25-stimulus sequences had the same temporal

137 frequency (10 Hz), with each stimulus (either a visual flash or an auditory tone) presented for about 20 ms 138 with an interstimulus interval of about 80 ms. Doing so, the inducer sequence including 10 stimuli had a 139 total duration of 1 s, while the sequence including 25 stimuli had a duration of 2.5 s. In Exp. 2, only 140 visual stimuli were used. In this case, visual sequences could either have the same temporal frequency as 141 in Exp. 1 (10 Hz), and thus different durations (1 s and 2.5 s respectively for 10 and 25 flashes), or the 142 same duration (2.5 s), thus presenting different temporal frequencies (4 and 10 Hz). In this latter case, the 143 duration of each flash was kept equal to the other conditions (20 ms), but the interstimulus interval was 144 longer (230 ms).

145





- 147 FIGURE 1. Experimental Procedures. (A) Visual sequential inducer condition in Exp. 1. The stimulation
- 148 procedure in this condition involved a visual sequential inducer comprising either 10 or 25 brief flashes
- 149 *(each displayed for 20 ms with an interstimulus interval of 80 ms), followed by a 16-dot reference*
- 150 stimulus (after 400-500 ms), and finally a variable probe stimulus including 8-32 dots (after 700 ms). At

151 *the end of the sequence, in most of the trials, participants had to report whether the reference or the* 

- 152 probe stimulus contained more dots. To make subjects pay attention to the inducer stimulus, they were
- 153 occasionally asked to report whether the inducer sequence contained "a few" or "a lot" of stimuli; in
- 154 *this case the numerosity discrimination task was skipped, and the trial was excluded from data analysis.*
- 155 *After providing a response, the next trial started automatically after 1,100-1,200 ms. In Exp. 2, the*
- 156 procedure was largely identical to the visual inducer condition of Exp. 1, except that the different inducer
- 157 sequences corresponding to different numerosities (10 or 25) could be presented with the same duration
- 158 (2.5 s) or the same temporal frequency (10 Hz). (B) Auditory sequential inducer condition in Exp. 1. In
- 159 this condition, the procedure was identical to the visual condition in Exp. 1, with the exception that
- 160 *instead of flashes the inducer included either 10 or 25 brief sounds (pure tones, frequency = 700 Hz).*
- 161 *Note that the stimuli are not depicted in scale.*
- 162

# 163 *Procedure*

- 164 All the experimental conditions of the study were performed in a quiet and dimly illuminated room.
- 165 Participants sat in front of a monitor screen at a distance of about 80 cm. In all the experiments,
- 166 participants fixated on a central fixation cross, while they performed a numerosity discrimination task as a
- 167 main task, reporting whether a reference (16 dots) or a probe (8-32 dots) seemed to contain more dots. In
- 168 order to induce serial dependencies affecting the perceived numerosity of the reference dot-array, an
- 169 "inducer" stimulus was presented at the beginning of each trial. In Exp. 1, the inducer was either a visual
- 170 or an auditory sequence, presented for 1 s or 2.5 s according to the number of stimuli included in the
- 171 sequence (either 10 or 25). After an interval of 400-500 ms starting at the offset of the last stimulus in the
- inducer sequence, the reference was presented on the screen for 30 ms, followed by the probe after 700
- 173 ms (similarly presented for 30 ms). At the end of the sequence, the fixation cross turned red signaling the
- 174 end of the trial, and participants were asked to report which stimulus contained the larger number of dots
- by pressing the appropriate key on a standard keyboard. After providing a response, the next trial started
- automatically after 1,100-1,200 ms. Procedure in Exp. 2 was identical to Exp. 1, with the exception that
- 177 only visual sequences were employed, and the stimuli were controlled for duration and temporal
- 178 frequency. Namely, in different trials randomly intermixed throughout each block, the visual inducer
- sequences (10 and 25 stimuli) were equalized for duration (i.e., thus spanning both 2.5 s but presenting
- 180 different temporal frequencies: 4 or 10 Hz), or were equalized for temporal frequency (TF; i.e., same 10
- 181 Hz temporal frequency but different durations as in Exp. 1). In both Exp. 1 and Exp. 2, a secondary task
- 182 concerning the inducer sequence was included to encourage participants to pay attention to it (i.e.,
- 183 similarly to Fornaciai & Park, 2018a). Namely, at the end of some trials (4 trials in each block; see
- below), participants were asked to report whether the inducer contained "a few" or "a lot" of stimuli.

185 Subjects were shown a few examples of different sequences before starting the experiment in order for 186 them to understand how to perform the secondary task. When participants performed this secondary task, 187 they did not have to judge numerosity. The trials that contained this secondary task were excluded from 188 data analysis. In all the experiments, reference and probe dot-array stimuli could be presented either on 189 the left or on the right of the central fixation cross, with a horizontal eccentricity of 11 deg. Visual inducer 190 stimuli were presented on the screen at a position corresponding to the center of the subsequent dot-array 191 stimuli, thus again with a 11 deg horizontal eccentricity. Auditory stimuli were played from two speakers 192 positioned behind the screen corresponding to the possible location of the visual stimuli on the left and on 193 the right of the central fixation cross. Participants completed 4 blocks of 60 trials in each of the two 194 conditions of Exp. 1, and 8 blocks of 60 trials in Exp. 2. Each block in all the experiments comprised 4 195 "catch" trials in which participants performed the secondary task. An equal amount of trials was collected 196 for the different combinations of inducer numerosity and probe numerosity. Participants performed a brief 197 training session (10-15 trials) before starting the actual experiment, in order to ensure that they understand 198 the task. An entire experimental session typically took around 50 minutes, and participants were 199 encouraged to take frequent breaks when needed.

200

#### 201 Behavioral data analysis

202 Across all the experiments, the numerosity discrimination performance was analyzed separately for each 203 subject and condition. The serial dependence effect was assessed by analyzing trials corresponding to 204 different inducer numerosities, which are designed to bias the perceived numerosity of the reference 205 stimulus in opposite directions. To achieve a measure of participants' accuracy and precision in the task, 206 the distribution of response probabilities as a function of probe numerosity was fitted with a cumulative 207 Gaussian curve, according to the Maximum Likelihood method (Watson, 1979). The point of subjective 208 equality (PSE), which is the probe numerosity perceptually matching the reference numerosity (thus 209 reflecting the accuracy in the task and the reference perceived numerosity), was taken as the median of 210 the best-fitting cumulative Gaussian curve to all the data of each participant in each condition. 211 Participants' precision in the task was assessed to exclude subjects showing insufficient performance. To 212 this aim, we used the just-noticeable difference (JND), obtained as the difference in numerosity between 213 chance level (50%) responses and 75% "probe more numerous" responses. We excluded participants 214 showing a JND higher than 10 dots. Although this threshold is arbitrary, with the current numerosity 215 range a JND higher than 10 dots would most likely result from a very poor discrimination performance, 216 making the result noisy and difficult to interpret. A total of 6 subjects was excluded from data analysis 217 based on this criterion, across all the experiments. One more participant was instead excluded because an

unusually high PSE (i.e., more than three SD higher than the average of the group). Additionally, a finger

219	error rate correction (2%) was applied to account for lapses of attention or random response errors
220	(Wichmann & Hill, 2001).
221	
222	To assess the serial dependence effects within each condition, a paired t-test was performed comparing
223	the distribution of PSEs corresponding to different inducer numerosities. Moreover, to obtain a direct
224	measure of the serial dependence effect and compare it across different experiments, we calculated a
225	serial dependence index taken as the difference in PSE in the high-numerosity inducer condition (i.e., for
226	instance 25 stimuli) and the low-numerosity inducer condition (i.e., for instance 10 stimuli). Additionally,
227	to achieve another index of the strength of the serial dependence effect we also computed the net
228	difference between the two inducer conditions as follows:
229	
230	$Effect = abs(((PSE_{ind25} - PSE_{ind10})/PSE_{ind10}) \times 100);$
231	
232	Where $PSE_{ind10}$ refers to the subject's PSE in the lower inducer condition (10 flashes/sound), and $PSE_{ind25}$
233	refers to the PSE in the higher inducer condition (25 flashes/sound).
234	
235	A t-test was used to compare the distribution of serial dependence effects across different conditions (i.e.,
236	visual and auditory). Finally, we also tested for a correlation between the level of precision in the task and
237	serial dependence. To do so, we used for each participant a measure of JND obtained by collapsing
238	together the two inducer numerosity conditions (in Exp. 1), and also collapsing together different inducer
239	types (same duration and same TF, in Exp. 2), in order to get a single JND value for each participant.
240	These JND values were log-transformed to achieve normality. We then assessed the correlation of such a
241	measure of precision with the indices of serial dependence effect calculated as reported above.
242	
243	RESULTS



245

FIGURE 2. Average psychometric curves in the two conditions of Experiment 1. (A) Psychometric curves
in the visual condition, representing the lower (10 flashes) and higher (25 flashes) inducer condition. (B)
Psychometric curves in the auditory condition, representing the lower (10 sounds) and higher (25 sounds)
inducer condition. Note that average psychometric curves were computed by pooling the data from all
participants together.

- 251
- 252
- 253 Experiment 1

254 Participants (N = 34) compared the numerosity of the *reference* and the *probe* dot arrays, while the

reference array was preceded by a sequential numerosity inducer either in visual or auditory modalities.

256 First, by plotting the average psychometric curves of the visual condition (Fig. 2A), it is immediately

257 clear that the two sequential inducer conditions result in a relative shift of the curves, with a more

258 leftward-shifted curve in the lower inducer condition (10 flashes), and a relative rightward shift in the

- higher inducer condition (25 flashes). On the other hand, in the auditory condition (Fig. 2B), the two
- 260 curves are almost perfectly superimposed, suggesting that the influence of an auditory inducer is much

reduced compared to the visual one.

262

To achieve a more precise index of performance in the two conditions, we analyzed the data individually
for each participant and condition. The results, illustrated in Figure 3, confirm that a visual sequential
inducer (Fig. 3A) was highly effective in inducing attractive serial dependencies, systematically biasing

- the perceived numerosity of the subsequent reference dot array. In other words, when the 16-dot reference
- 267 was preceded by a sequence of 10 flashes, its perceived numerosity was significantly lower compared to
- 268 the same 16-dot reference preceded by 25 flashes (t(33) = 3.094, p = 0.004, d = 0.53), with an average
- difference in perceived numerosity of about 5.3% ( $\pm 1.7\%$ , SEM). On the other hand, an auditory
- 270 sequential inducer was not as effective (Fig. 3B), resulting in no significant attractive bias on the

perceived numerosity of the reference dot array, and with even a non-significant trend in the opposite (repulsive) direction (t(33) = -0.895, p = 0.377, d = 0.15, average difference =  $1.1\% \pm 1.6\%$ ). Comparing the distribution of the serial dependence effect (i.e., PSE in the higher inducer minus PSE in the lower inducer; Fig. 3C) directly between the two inducer conditions showed a statistically significant difference (t(33) = 2.77, p = 0.009, d = 0.47), again demonstrating that visual and auditory inducers yielded largely different effects.

277



279FIGURE 3. Results of Experiment 1. (A) Visual inducer condition. In this condition, a visual sequence of280flashes induced strong and systematic attractive biases affecting the perceived numerosity of the281subsequent reference dot-array. (B) Auditory inducer condition. An auditory sequential inducer, however,282did not affect the perceived numerosity of the dot-array stimulus. (C) Average serial dependence effect283index in the visual and auditory condition. The serial dependence effect index was calculated as the PSE284in the larger inducer condition (25 dots) minus PSE in the smaller inducer condition (10 dots) in each285participant. Error bars are SEM. n.s. = not significant, \*\* p < 0.01.

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Finally, regarding the performance in the "catch" task that participants performed on some trials (i.e., discriminating whether the inducer contained a few or many flashes/sounds), the proportion of correct responses (mean  $\pm$  SEM) was 79.2%  $\pm$  2.96% in the visual condition, and 90.1%  $\pm$  2.63% in the auditory condition. The proportion of correct responses was significantly higher in the auditory condition (t(33) = 4.55, p < 0.001). This may indicate that performing the attentional task in the visual modality might have been more difficult compared to performing it on auditory stimuli, possibly due to a bigger attentional load with stimuli in the same modality.



Results from Experiment 1 show that serial dependence operates across stimulus formats (although only
in the same modality), suggesting that the effect arises at a relatively high – more abstract –

299 representational level, beyond low-level sensory properties of the dot array stimuli. Nevertheless, because

300 the two inducer stimuli were kept in a constant temporal frequency and thus had different durations, the

301 results could be interpreted as having the duration information rather than numerosity driving the

302 attractive biases in numerosity judgment. Indeed, interactions between magnitude dimensions such as

time and numerosity are well known (Dormal et al., 2006; Xuan et al., 2007; Lambrechts et al., 2013;

Tsouli et al., 2018; Fornaciai et al., 2018). Thus, in Exp. 2, we tested to what extent the attractive serial
dependence found in Experiment 1 can be generalized in cases where duration is not always correlated
with numerosity.





FIGURE 4. Results of Experiment 2. (A) Average PSE as a function of inducer numerosity in the same
duration (light gray) and same temporal frequency (dark gray) condition. (B) Average serial dependence
effect indexes in the two conditions of Exp. 2. Error bars are SEM.

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313 Experiment 2 (N = 30) was identical to the visual inducer condition in Exp. 1, except the two sequential 314 inducers were on half of the trials in same duration or on the other half in same temporal frequency, but 315 importantly always in different numerosities (10 dots versus 25 dots). The results, as illustrated in Figure 316 4, indicate that visual sequential inducers again significantly biased the representation of the subsequent 317 reference dot-array stimulus in the attractive direction regardless of whether the two inducers were in same duration (t(29) = 2.3812, p = 0.0240, d = 0.435) or in same temporal frequency (t(29) = 3.2814, p = 0.0240, d = 0.435)318 0.0027, d = 0.60). The average difference between the two inducer conditions was  $3.9\% \pm 1.5\%$  and 4.8%319  $\pm$  1.4%, respectively for the same duration and same TF condition. While the effect seems somehow 320

- 321 stronger in the same TF condition (which is basically the same as in Exp. 1), comparing the distribution
- 322 of serial dependence effects across the two conditions did not reveal any statistically significant difference
- 323 (Fig. 4B; t(29) = 0.4844, p = 0.632, d = 0.09). Such a comparable effect across the two control conditions
- 324 suggests that the effect is most likely determined by the numerosity of the sequence, with smaller if any
- 325 influence of other attributes such as duration or temporal frequency.
- 326



FIGURE 5. Correlation between serial dependence and precision in the task. Scatterplot illustrating the
correlation between the log-transformed JND and the serial dependence effect, including data from both
Exp. 1 (only the visual condition) and Exp. 2.

- 331
- 332 Moreover, we tested for a correlation between participants' precision in the task (JND) and the magnitude 333 of the serial dependence effect across both Exp. 1 and Exp. 2 (Fig. 5). Doing so, we observed a 334 statistically significant correlation (r = 0.304, p = 0.0146) between JND and the index of serial 335 dependence effect. This shows that the strength of serial dependence varies as a function of the precision 336 of perceptual estimates. Although the correlational nature of this result does not allow us to pinpoint the 337 exact direction of the effect, a possibility is that in conditions of higher uncertainty or noisier 338 representation (i.e., high JND), the visual system may give a stronger weight to past information, 339 resulting in stronger serial dependencies (see Discussion). 340 341 Finally, the proportion of correct responses across the two conditions of Exp. 2 was  $80.8\% \pm 2.75\%$ . 342 343 DISCUSSION
- 344 In the present study, we addressed the hypothesis that serial dependence in numerosity perception may
- 345 operate according to an abstract representation of approximate numerical magnitude. This prediction

346 comes from the idea that serial dependence results from a high-level modulatory process affecting 347 perception, as suggested by recent studies (Fornaciai & Park, 2018a; Pascucci et al., 2019). Indeed, 348 previous studies show that serial dependence is both spatially localized and dependent on attention 349 (Fornaciai & Park, 2018a) suggesting the involvement of a spatially-localized modulation of early visual 350 activity mediated by attention (e.g., Somers et al., 1999). The current results support this idea by showing 351 that the effect generalizes across different visual presentation formats. Namely, the numerosity of a 352 sequential inducer affects the perceived numerosity of a subsequently presented dot-array stimulus, with a 353 clear attractive trend. A control experiment (Exp. 2) showed that other features of the sequential inducer 354 like duration or temporal frequency have little influence on serial dependence in this context, similarly to 355 what has been previously demonstrated with cross-format numerosity adaptation (Arright et al., 2014). In 356 contrast to the case of a visual sequential inducer, an auditory sequential inducer did not systematically 357 affect the perceived numerosity of visual dot-array stimuli, showing that serial dependence operates in a 358 within-modality fashion. This additionally suggests that serial dependence is a distinct mechanism 359 compared to perceptual adaptation, which has been shown to generalize also across different sensory 360 modalities (Arrighi et al., 2014). Finally, the specificity for sensory modality also suggests that the effect 361 is perceptual in nature, and that it is distinct from priming, which has been demonstrated to work across 362 modalities (e.g., McKone & Dennis, 2000; Greene et al., 2001; Buchner et al., 2003; Vallet et al., 2010). Note that in this context a *perceptual* effect does not necessarily involve a bias in the early *sensory* 363 364 processing. While the effect may arise at higher-level processing stages after sensory encoding (see below 365 for further discussion about possible neural underpinnings), the crucial point is that such an effect would 366 operate directly on perception, distorting the subjective experience (i.e., appearance) of a stimulus. 367

368 How do the present results compare with previous findings? On the one hand, such a cross-format effect 369 is surprising, as earlier studies on serial dependence show that the effect depends on the similarity 370 between two stimuli. For instance, several studies since Fischer & Whitney (2014), using a continuous 371 series of stimuli and a reproduction task, show that the effect of past stimuli declines as the difference 372 compared to the current one becomes too large (Fischer & Whitney, 2014; Fritsche et al., 2017; Manassi 373 et al., 2018). This led some authors to conceptualize serial dependence as a sort of weighted average akin 374 to a Kalman filter (Burr & Cicchini, 2014). In our paradigm, stimuli in different formats had completely 375 different low-level features. Yet, we observed a systematic attractive effect very similar to previous 376 results (Fornaciai & Park, 2018a). This pattern is not irrelevant to our previous finding in which using 8 377 and 32-dot inducers was equally effective as using 12 and 24-dot inducers in eliciting serial dependence 378 for a 16-dot reference (Fornaciai & Park, 2018a), suggesting a relatively low specificity of the effect.

379 These results indicate some qualitative differences between our results using numerosity information in a 380 discrimination task and some other previous studies using orientation information in a reproduction task. 381

382 One possibility is that such a selectivity in previous studies may be a feature of serial dependence in 383 circular dimensions (i.e., orientation as in Fischer & Whitney, 2014 and Fritsche et al., 2017; Pascucci et 384 al., 2019; or the circular position space in Manassi et al., 2018), while it may not emerge in magnitude 385 dimensions such as numerosity. Another possibility is instead related to the difference in the paradigm 386 used. While a reproduction task requires participants to reproduce a stimulus with a high degree of 387 precision - thus requiring paying more attention to its specific value - a two-alternative forced-choice 388 paradigm like the one used in the present study may shift the focus to broader categories such as "more" 389 versus "less," irrespective of the specific magnitude of the stimuli. While our data cannot disentangle 390 these possibilities, this remains an interesting question for future studies. Irrespective from this, our data 391 show that what actually matters is not the similarity in the superficial sensory feature of the stimuli, but 392 the information that can be extracted from them.

393

394 Our results are in line with earlier studies suggesting a generalized and abstract representation of 395 numerosity (Piazza et al., 2007; Arrighi et al., 2014; Anobile et al., 2016). Indeed, while numerosity 396 processing seems to be deeply rooted into modality-specific sensory pathways (Cavdaroglu et al., 2015; 397 Cavdaroglu & Knops, 2018; Fornaciai et al., 2017; Fornaciai & Park, 2018c) and interacting with several 398 sensory systems like color and motion perception (Fornaciai & Park, 2017), both psychophysical (e.g., 399 Arrighi et al., 2014; Anobile et al., 2016) and neuroimaging (e.g., Piazza et al., 2007) data show that 400 numerical magnitude is represented in a more abstract fashion at a relatively high-level in the cortical 401 processing hierarchy (e.g., in parietal cortex). According to this idea, then, it is not surprising that serial 402 dependence operates according to the numerical magnitude of the stimuli irrespective of their format. In 403 this scenario, serial dependence would operate according to a relatively high-level representation of past 404 stimuli (i.e., in this case the inducer), to affect the processing of the current stimulus starting from the 405 earliest levels of visual processing (Fornaciai & Park, 2018b).

406

407 It is interesting to note that the paradigm used in the present study closely resembles the one used by

408 Arrighi et al. (2014) to assess cross-format numerosity adaptation effects. Strikingly, while Arrighi et al.

409 (2014) observed a strong repulsive effect consistent with perceptual adaptation, here we observed a

410 systematic attractive bias. The different outcomes of a similar paradigm, however, may depend on the

- 411 specific parameters of inducer/adaptor stimuli used in different context. The most important one, in our
- 412 interpretation, is the duration of the stimuli: while the long adaptation procedure used by Arrighi et al.

413 (2014) – more focused on the temporal frequency of the stimuli rather than on their number – would more

414 easily induce a repulsive effect, the shorter stimuli used in the present study would provide an attractive

415 bias. Another example of this difference in the effect due to the duration of the stimuli is also evident in

416 previous studies. For instance, in a previous study from our group (Fornaciai & Park, 2018), we used a

417 paradigm (i.e., see Exp. 3 in Fornaciai & Park, 2018) very similar to the classic numerosity adaptation

418 procedure (e.g., Burr & Ross, 2008), except for the duration of the inducer/adaptor stimuli. Similarly,

419 while using very long sustained stimuli yields a repulsive effect, our results employing very brief stimuli

420 showed systematic attractive effects.

421

422 A crucial question, then, is: what are the possible neural substrates of this cross-format serial dependence 423 bias? While an account based on a bias at the early levels of sensory processing (e.g., Fischer & Whitney, 424 2014) does not fit the observed effect due to wide differences in the stimuli used, the present results seem 425 more consistent with an account of serial dependence based on the persistence of perceptual decision 426 templates at a read-out/decision stage (Pascucci et al., 2019). In a recent study, Pascucci et al. (2019) 427 conceptualized attractive serial dependence as a bias occurring at a relatively high-level processing stage, 428 affecting the decoding of early sensory activity performed by read-out "decision" units. Namely, traces of 429 past perceptual decisions would linger at such high-level stage, effectively modulating the read-out 430 weights applied to interpret low-level activity. Such a modulation, in turn, would bias the resulting 431 perceptual representation of the current stimulus, directly affecting the appearance of the stimulus. A 432 similar account of serial dependence based on a high-level neural mechanism was also provided by 433 Fritsche et al. (2017). However, such an account was mostly based on a working memory bias, which is 434 not consistent with results showing that serial dependence affects perception directly (e.g., Cicchini et al., 435 2018, Fornaciai & Park, 2018; Manassi et al., 2018; Pascucci et al., 2019).

436

437 Taking into account previous research on numerosity perception, our results thus fit with this model

438 (Pascucci et al., 2019) in pinpointing a relatively high level locus for serial dependence. At the neural

439 level, parietal areas were often associated with an abstract representation of numerosity independent from

440 the stimulation format. In this scenario, therefore, parietal neurons would thus represent the read-out units

441 biased by attractive serial dependence, while numerosity-related activity in early visual cortex (e.g.,

442 Fornaciai & Park, 2018; DeWind et al., 2018) would not be affected directly. The fact that auditory

443 inducers do not affect the perceived numerosity of visual stimuli, however, limits this interpretation by

444 suggesting that such read-out units only receive visual signals, while previous studies observed other

- 445 types of perceptual effects (such as adaptation) generalizing also across sensory modalities (Arrighi et al.,
- 446 2014).

448 Additionally, it is also interesting to note that the present findings are consistent with recent results 449 concerning a different process: trans-saccadic integration. Indeed, it has been shown that integration of 450 numerosity information across eye movements is insensitive to changes in the low-level features of the 451 stimuli, such as the luminance/color of the items (Hübner & Schütz, 2017). Although the manipulations 452 performed by Hübner & Schütz (2017) are not as extensive as presenting different stimulus formats, this 453 finding also suggests that integration of numerosity information occurs at a relatively high level in the 454 visual hierarchy. Moreover, it has been also shown that trans-saccadic integration depends on attention 455 (Stewart & Schütz, 2018), again similarly to what has been previously demonstrated for serial dependence 456 (Fischer & Whitney, 2014; Fornaciai & Park, 2018a), suggesting that the two integrative processes may 457 even involve partially overlapping or similar neural mechanisms. 458

459 Another interesting point concerns the correlation observed between serial dependence and JND (Fig. 5). 460 This correlation may suggest that the magnitude of the effect varies as a function of the precision of 461 perceptual estimates – that is, in conditions of higher uncertainty (i.e., as indexed by lower precision), the 462 visual system may rely to a greater extent on past inputs to disambiguate or improve the representation of 463 current sensory stimulation. However, although this explanation is in line with previous studies (Cicchini 464 et al., 2018b), the correlational nature of this result does not allow us to draw a strong conclusion about 465 this point. In fact, across several previous experiments from our group (Fornaciai & Park, 2018a; 466 Fornaciai & Park, in press), we rarely observed a correlation between JND and serial dependence (i.e., 467 only in 3 out of 10 independent experiments). Although this is a potentially interesting point, thus, the 468 fact that this correlation is very difficult to replicate makes it difficult to draw any conclusion from it. 469 Looking at Fig. 5, however, it is also evident that there is a relatively large variability in the magnitude of 470 the serial dependence effect across participants, with a few data points actually showing negative 471 (repulsive) effects. As serial dependence is highly dependent on attention, a possibility is that the degree 472 to which participants paid attention to the inducer may have determined the strength of the attractive 473 effect. Unfortunately, too few trials were collected in the catch task to achieve a realistic index of 474 participants' attention. An intriguing possibility for future studies would thus be to modulate attention 475 more extensively, for instance by using a double-task design in every trial, and/or secondary tasks loading 476 attention to different extents.

477

Finally, another potentially important point to consider when interpreting the results, concerns the specificparadigm employed in this study. Indeed, the fully sequential stimulation procedure used here represents a

480 limitation: when measuring the effect of the inducer on the reference stimulus, some effect might have

481 extended to the subsequent probe stimulus, effectively reducing the magnitude of serial dependence. In 482 fact, in a recent study from our group (Fornaciai & Park, in press), we observed a stronger effect when 483 presenting reference and probe simultaneously in two different portions of the visual field. However, 484 although a sequential presentation is not the optimal procedure in this context, this only makes our test 485 more conservative. Another possibility related to this point, on the other hand, is that the absence of an 486 effect in the auditory condition might reflect a particularly long effect, extending to the probe and thus 487 compensating the change in perceived numerosity of the reference. While we cannot conclusively rule out 488 this possibility, previous research show that serial dependence in numerosity perception sharply decreases 489 after one stimulus (Cicchini et al., 2014), making more plausible that the null effect in the auditory 490 condition is genuine. Additionally, also having a constant reference stimulus may not be optimal in this 491 context. Indeed, the reduced uncertainty of such a constant stimulus may in turn reduce the magnitude of 492 the serial dependence effect. Thus, another interesting possibility for future studies is to use more variable

- 493 stimuli to increase uncertainty.
- 494

To conclude, our results show that, at least in the context of a numerosity discrimination task, serial dependence affects stimuli irrespective of their presentation format, and hence irrespective from their sensory properties. This finding advances our understanding of serial dependence by showing that at least in some contexts it operates on an abstract representation of the stimuli, affecting similar representations extracted from widely different stimuli. This in turn converges with recent evidence ascribing the phenomenon of serial dependence to a relatively high-level processing stage, possibly at the level of read-

- 501 out decision units interpreting low-level sensory activity to form a perceptual representation.
- 502

#### 503 AUTHOR CONTRIBUTIONS

504 M.F. and J.P. devised the study. M.F. collected the data. M.F. and J.P. analyzed the data, interpreted the 505 results, wrote and revised the manuscript.

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# 507 CONFLICT OF INTEREST

508 The authors declare no competing financial interests.

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