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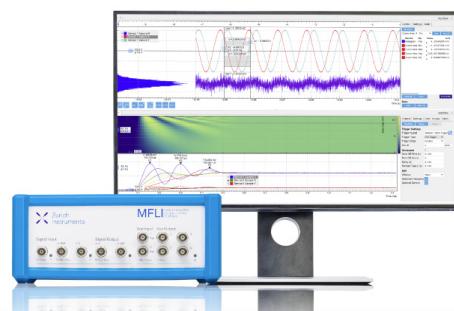
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Hareesh Chandrasekar,^{1,a)}  Junao Cheng,¹ Tianshi Wang,²  Zhanbo Xia,¹  Nicholas G. Combs,³ Christopher R. Freeze,³  Patrick B. Marshall,³ Joe McGlone,¹  Aaron Arehart,¹  Steven Ringel,^{1,4} Anderson Janotti,²  Susanne Stemmer,³ Wu Lu,¹ and Siddharth Rajan^{1,4}

AFFILIATIONS

¹Department of Electrical and Computer Engineering, The Ohio State University, Columbus, Ohio 43210, USA

²Department of Materials Science and Engineering, University of Delaware, Newark, Delaware 19716, USA

³Materials Department, University of California, Santa Barbara, California 93106, USA

⁴Department of Material Science Engineering, The Ohio State University, Columbus, Ohio 43210, USA

^{a)}Electronic mail: chandrasekar.28@osu.edu

ABSTRACT

BaSnO₃, a high mobility perovskite oxide, is an attractive material for oxide-based electronic devices. However, in addition to low-field mobility, high-field transport properties such as the saturation velocity of carriers play a major role in determining the device performance. We report on the experimental measurement of the electron saturation velocity in La-doped BaSnO₃ thin films for a range of doping densities. The predicted saturation velocities based on a simple LO-phonon emission mode, using an effective LO phonon energy of 120 meV show good agreement with the measurements of velocity saturation in La-doped BaSnO₃ films. Density-dependent saturation velocity in the range of 1.8×10^7 cm/s reducing to 2×10^6 cm/s is predicted for δ -doped BaSnO₃ channels with carrier densities ranging from 10^{13} cm⁻² to 2×10^{14} cm⁻², respectively. These results are expected to aid the informed design of BaSnO₃ as an active material for high-charge density electronic transistors.

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Perovskite oxides continue to attract a lot of interest for fundamental and applied physics in view of the plethora of electronic properties they exhibit.^{1,2} This also makes perovskites an ideal platform onto which diverse device functionalities can be integrated. However, the poor electron mobility of most perovskite oxides makes them a sub-optimal choice for electronic device applications. With a recorded room-temperature mobility of 320 cm²/V s in single-crystals,³ BaSnO₃ (BSO) is a notable exception to this rule. The cause for such high mobility in BSO thin films has been studied previously and attributed both to the low effective mass of electrons owing to the significant antibonding s-orbital-like character of the conduction-band minimum,⁴ and the low electron-phonon scattering rate due to the lower density of conduction band states.⁵ Such high mobilities in conjunction with the large and tunable doping densities ($\sim 10^{20}$ cm⁻³) achievable in this material, and the possibility of realizing heterostructures with carrier confinement make BSO promising from an electronic device perspective.⁶ Transistors fabricated from La-doped BaSnO₃ and SrSnO₃ channels (10–28 nm) are still in the early stages of development but have shown promising results compared to those based on other perovskite-oxides such as SrTiO₃ (STO).^{7–9} However, in addition to the low-field transport properties such as mobility, the

operation of electronic devices such as RF amplifiers, and highly-scaled transistors for logic, depends critically on high-field transport, i.e., saturation velocity of charge carriers in the high-mobility channel.^{10,11} While low-field transport in BSO has been studied and modeled, there are no reports on high-field transport and the physical mechanisms limiting the saturation velocity in this material, despite its relative importance for device performance. Here, we report on the experimental measurement of saturation velocity in thin films of La-doped BSO and model its dependence on the dominant LO-phonon scattering process. We obtain a reasonable agreement between the theoretical values based on a simple optical phonon emission model and the measured saturation velocities, for an experimentally relevant range of doping densities in BSO thin films.

BSO films were grown via MBE with various La concentrations on insulating (100) SrTiO₃ (STO) and (110) DyScO₃ (DSO) substrates,¹² with and without BaTiO₃ (BTO) capping layers, as summarized in Table I. Due to the lattice mismatch between BSO and STO/DSO, all films are relaxed. For samples with a BTO capping layer, 20 nm of BTO was grown on the La-doped BSO film via hybrid MBE.¹³ The saturation velocity was measured on specially designed I-shaped test structures consisting of wide source and drain contact

TABLE I. Sample stack and thicknesses of the MBE-grown La-doped BSO thin films used in this study along with their measured sheet carrier concentrations (cm^{-2}) and Hall mobilities ($\text{cm}^2/\text{V s}$).

Sample details	Sheet carrier concentration (cm^{-2})	Hall mobility ($\text{cm}^2/\text{V s}$)
BTO/La:BSO/BSO/DSO (20 nm/21 nm/11 nm/substrate)	2.65×10^{14}	96
BTO/La:BSO/BSO/STO (20 nm/16 nm/5 nm/substrate)	1.92×10^{14}	87
La:BSO/BSO/STO (20 nm/5 nm/substrate)	7.23×10^{13}	58

pads with a narrow mesa-defined channel of length L and width W [see Fig. 1(b)] connecting them. Such a structure not only confines the current flow and applied potential to the channel, but also reduces any extraneous voltage drop in the contact/access regions due to the large difference in areas between the channel and contact regions.¹⁴ The device fabrication consisted of i-line stepper lithography for all layers commencing with Ti/Al alignment markers, inductively coupled plasma-reactive ion etching (ICP-RIE) of the BTO cap layer using BCl_3/Ar , followed by ohmic contact deposition (Ti/Au, 50 nm/100 nm) using e-beam evaporation, and finishing with an ICP-RIE (BCl_3/Ar) mesa-etch of the BSO channel to define the I-shaped constrictions. Various constriction widths (2, 5 and 10 μm) and lengths (600 nm to 2 μm) were fabricated and tested on each sample. Pulsed I-V measurements (1 μs pulse width, 0.1% duty cycle) were performed using a Keithley 4200 semiconductor characterization system on the test structures. Contact resistances of 0.34, 0.49, and 0.3 $\Omega \text{ mm}$ were measured on the three samples listed in Table I, respectively, using TLM test structures. The saturation velocity was extracted as $v_{\text{sat}} = J_{\text{max}}/qn_s$, where J_{max} and n_s are the measured maximum saturation current density (ampere per millimeter) and sheet carrier concentration (cm^{-2}), respectively, and plotted as a function of electric field as shown in Fig. 2 for the sample with $n_s = 2.65 \times 10^{14} \text{ cm}^{-2}$ as an example (Fig. S2 of the supplementary material show electric field vs current density plots for the complete set of measured devices across all samples used in this study). Saturation current densities ranging from 5 to 50 A/mm were observed for the range of sample doping densities. We also observed device-device variation across each sample

comparable to that shown in Fig. 2, which we attribute to the local doping/stoichiometric variations and structural defects in the deposited films. The critical thicknesses for strain relaxation in BSO films on STO and DSO substrates have been reported to be $\sim 1 \text{ nm}$ leading to structural defects in these films (threading dislocation densities $> 10^{11} \text{ cm}^{-2}$).^{15,16} In addition, pulsed I-V measurements were also performed for a subset of devices at 80 K. A comparison between the electric field vs current density plots at 300 and 80 K for two of the measured devices on the highest doping density sample is shown in Fig. 2(b). An increase in J_{max} (and hence extracted v_{sat}) of $< 18\%$ can be observed for these two devices, which is comparable to the standard error of the mean (12%) measured across all devices at 300 K indicating that the current saturation is reflective of velocity and not mobility-limited. Figure S3 of the supplementary material also shows the electric field vs current density plot for the lowest doping density sample used in this study – $n_s = 7.23 \times 10^{13} \text{ cm}^{-2}$ showing $< 6\%$ increase in J_{max} and v_{sat} at 80 K as compared to 300 K.

In order to explain the mechanism of velocity saturation in these films, it is important to note that strong LO-phonon induced carrier scattering occurs in such polar materials.^{5,17} We performed first-principles calculations for the phonon spectrum and electron-phonon scattering rates in BSO based on the density functional theory (DFT)^{18,19} and density functional perturbation theory (DFPT)²⁰ as implemented in the Quantum ESPRESSO code,²¹ with the generalized gradient approximation of Perdew-Burke-Ernzerhof for the exchange-correlation term.²² Optimized norm-conserving Vanderbilt pseudopotentials were employed.²³ The EPW code was used to interpolate the electron-phonon matrix elements and calculate the electron-phonon scattering rates.²⁴ The phonon spectra of BSO (Fig. S3 in the supplementary material) exhibits 15 branches with the three LO phonon branches (branches 6, 12, and 15) strongly affecting electron-phonon scattering for long-range Fröhlich interactions. This can be clearly seen in Fig. 3 which plots the scattering rate for the various phonon branches as a function of electron energy with reference to the Fermi level. It is evident that the total scattering rate rises steeply beyond electron energies of 120 meV which may be taken as the net effective LO phonon energy for electron scattering due to optical phonon emission in BSO.

Given the dominant optical phonon modes in BSO and strong LO-phonon induced carrier scattering shown above, the emission of LO-phonons by energetic carriers at the source is likely to act as the velocity saturation mechanism for BSO films. Such a model has been previously used to explain velocity saturation observed in GaN HEMTs, carbon nanotubes (CNTs), and layered materials.^{25–28} To explain the model briefly, at high enough applied electric fields, it

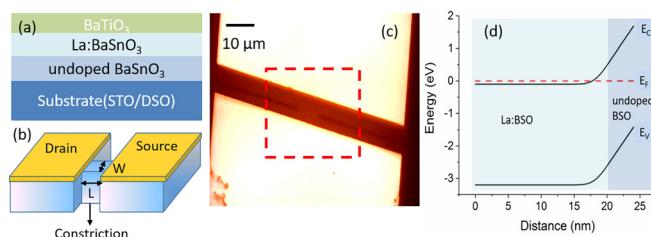


FIG. 1. (a) Cross-section of a representative La:BSO thin film stack used in this study, (b) schematic of the I-shaped test structure used for saturation velocity measurements with width "W" and length "L" as indicated, and (c) optical image of a fabricated test structure with the constriction mesa visible within the red dotted square ($L = 0.9 \mu\text{m}$, $W = 10 \mu\text{m}$). (d) Band diagram of 20 nm thick 10^{20} cm^{-3} doped La-doped BSO – 5 nm thick undoped BSO stacks (Fermi level at midgap), similar to those used in this study showing electron confinement almost throughout the La:BSO layer (depletion width $< 2.5 \text{ nm}$).

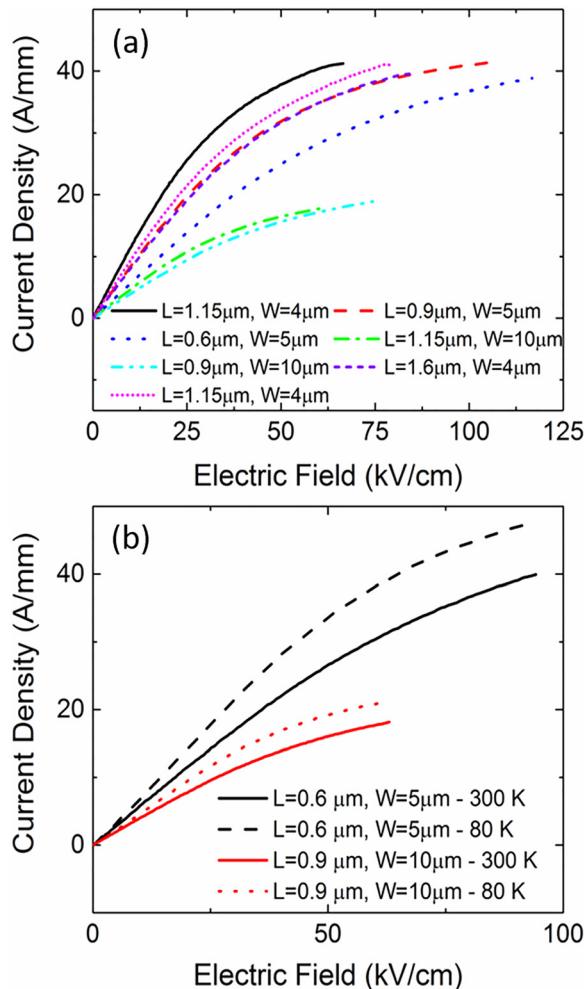


FIG. 2. Current density (ampere per millimeter) vs electric field (kilovolt per centimeter) curves for a representative La:BSO film with a doping density of $2.65 \times 10^{14} \text{ cm}^{-2}$ ($n_{3D} = 1.33 \times 10^{20} \text{ cm}^{-3}$) for the test structure dimensions indicated as measured at (a) 300 K across 7 devices, and (b) a comparison of 300 and 80 K measured data for two devices on this sample.

becomes energetically favorable for carriers injected into the channel from the source to emit LO phonons and backscatter into the source region. This causes a net balance of carriers for forward injection leading to current and hence velocity saturation. The key feature of this model is the existence of a density-dependent saturation velocity as illustrated in Fig. 4 for the case of a 2-D electron gas with carrier density lower than the crossover density (n_0) beyond which back-scattering into the bottom of the conduction band is Pauli blocked. At 0 K, the Fermi circle of radius k_F indicates the range of occupied states for a given electron density. For smaller densities, we see from Fig. 4 that the carriers can be accelerated to larger velocities (higher values of charge centroid, k_0) before the onset of optical phonon emission takes place ($k_{op} = k_F + k_0$) as compared to lower values for higher sheet carrier densities.

The total current in the device can be estimated by summing up all occupied energy levels in k -space and is given by $J = qn_s(\hbar k_0/m^*)$

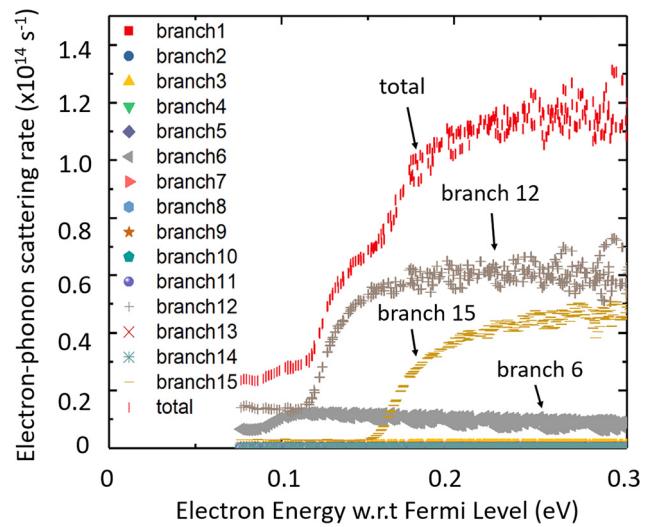


FIG. 3. Calculated electron-phonon scattering rates (in s^{-1}) in BSO as a function of electron energy with respect to the Fermi level (in electronvolts). The LO phonons representing branches 6, 12, and 15 of the phonon dispersion spectra (also see the [supplementary material](#)) play a dominant role in electron scattering with the total scattering rate increasing steeply beyond 120 meV.

for electrons in a 2DEG, where m^* is the effective mass (0.2^*m_0) for BSO²⁹ and the charge centroid k_0 is given by $m^*\omega_{op}/(2\hbar k_F)$ for $n_s > n_0$ and $k_0 = k_{op} - k_F$ for $n_s \leq n_0$.²⁸ This gives rise to a square-root dependence between the current density and sheet carrier concentration for high densities ($n_0 > n_s$) and since $J = qn_s v_{sat} v_{sat}$ decreases as $n_s^{-1/2}$ with increasing channel charge density. The present study, however, involved samples of fairly-thick La-doped BSO films (16–21 nm) which more closely resemble a 3D electron gas rather than a 2D case even after accounting for the depletion widths in these layers. The current density for 3-D carriers can be estimated by summing the occupied states across a Fermi sphere of radius k_F as

$$J = \begin{cases} qn_{3D} \frac{\hbar}{m^*} (3\pi^2(n_{0,3D} - n_{3D}))^{1/3}, & n_{3D} \leq n_{0,3D} \\ \frac{qn_{3D} E_{op}}{2\hbar(3\pi^2 n_{3D})^{1/3}}, & n_{3D} > n_{0,3D}, \end{cases} \quad (1)$$

where $n_{0,3D} (=k_{op}^3/3\pi^2 = 1.68 \times 10^{19} \text{ cm}^{-3})$ is the crossover 3D density for which optical phonon emission to the bottom of the conduction band is not Pauli blocked and E_{op} is the optical phonon energy (120 meV as discussed above). The saturation velocity extracted ($v_{sat} = J/qn_s$) from these equations for the 3D case therefore has a $n_{3D}^{-1/3}$ dependence at higher carrier densities in contrast to the $n_s^{-1/2}$ dependence for 2D confinement which also leads to higher values of v_{sat} in comparison.

Figure 5 shows the predicted saturation velocity for a range of equivalent sheet carrier concentrations of the La:BSO 3DEGs along with the experimentally measured values for comparison (n_{3D} was estimated as $n_s/t_{La:BSO}$ for each case as the depletion widths in the La:BSO layer are < 2.5 and ~ 5 nm, respectively, for the highest and lowest doping density films, and the error bars were extracted from the measured device-to-device variation on each sample, see Fig. 2(a) and S2 in the [supplementary material](#)). We see that the experimentally

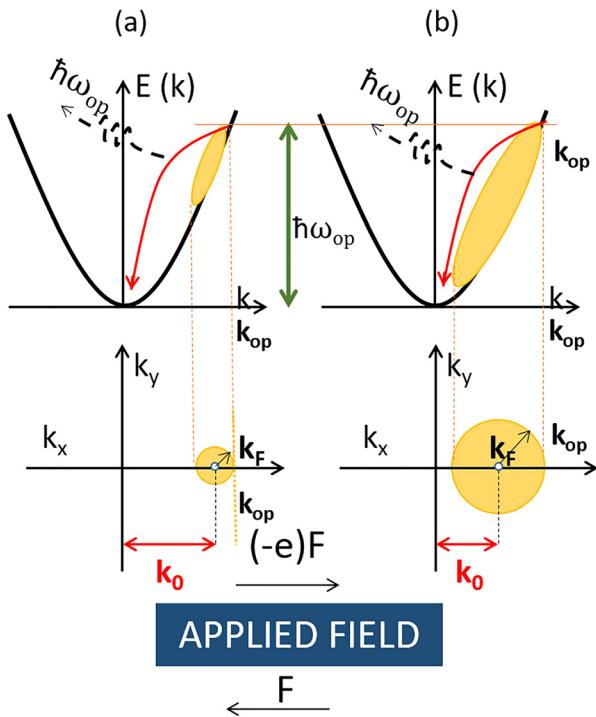


FIG. 4. Schematic showing a comparison of electron saturation velocity due to LO phonon emission for (a) smaller and (b) larger carrier densities in terms of energy band diagrams (top) and the corresponding k -space occupation of filled electrons (bottom) denoted by Fermi circles (k_F) at 0 K for the 2D case. k_0 refers to the charge centroid under high applied fields when LO-phonon emission becomes favorable ($E(k) \geq \hbar\omega_{op}$).

measured saturation velocity for a range of carrier concentrations shows a reasonable agreement with the predictions of the 3-D optical phonon model (at 0 K), indicating that optical phonon emission using an effective LO phonon energy of 120 meV is the likely cause for velocity saturation in La:BSO thin films. It can also be seen from Fig. 5 that the measured saturation velocity decreases for higher carrier densities as predicted by the model. The use of modulation-doped barriers to BaSnO₃ channels, to spatially separate out the 2DEG in the high-mobility channel from the impurity atoms in the barrier, is another promising approach that has been mooted for device applications.⁶ Hence, we also estimate the density-dependence of saturation velocity for the 2-D confinement case corresponding to δ -doped BSO channels. Since the carrier concentrations in La:BSO are typically much higher ($> 5 \times 10^{13} \text{ cm}^{-2}$) than those observed in other high charge density interfaces such as AlGaN/GaN, it is important to consider not just the occupancy of the first sub-band (the electrical quantum limit), but also that of higher order sub-bands which contribute to current densities and hence saturation velocity. In order to account for filling multiple sub-bands at realistic doping densities, a δ -doped BSO channel of thickness 5 nm was considered with confining barriers of 2 eV on either side, analogous to a finite potential well where each bound state represents a sub-band. The total current density was then obtained by summing up the contributions from each sub-band and the net saturation velocity is also shown in Fig. 5 (see the supplementary material for more details).

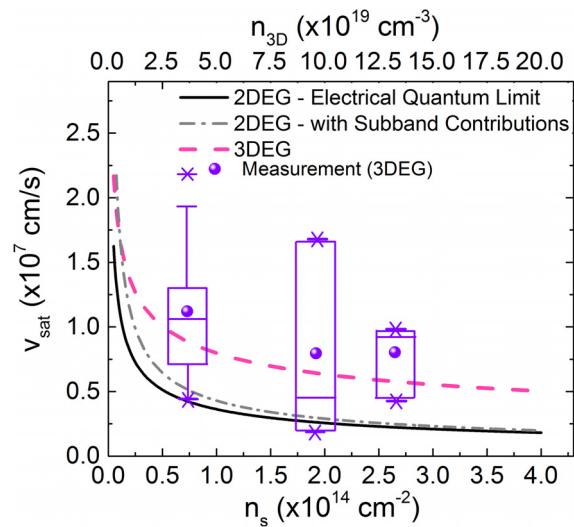


FIG. 5. LO phonon-limited saturation velocity of electrons for La-doped BSO 3DEG ($t_{\text{BSO}} = 20 \text{ nm}$) and experimentally measured values represented as box plots for the La:BSO films of Table I shown for comparison. Also shown are the density-dependent v_{sat} curves for δ -doped BSO 2DEGs in the electrical quantum limit (single sub-band) and multiple sub-band contributions ($t_{\text{BSO}} = 5 \text{ nm}$ with 2 eV barriers on either side).

The saturation velocity for δ -doped BSO channels is estimated to drop from $1.8 \times 10^7 \text{ cm/s}$ to a more or less constant value of $2 \times 10^6 \text{ cm/s}$ for sheet carrier concentrations beyond $2 \times 10^{14} \text{ cm}^{-2}$. It is evident that even though the saturation velocity drops with increasing carrier densities, the decrease is not as steep (proportional to $n_s^{-1/2}$) as the corresponding rise in charge density ($\sim n_s$ and hence the current drive) of La:BSO thin film transistors. Hence, there is a definite motivation to have highly-doped BSO channels for high charge density switches with the modulation of such large charge densities being the primary challenge for device applications.

In conclusion, we have experimentally measured the saturation velocity of La:doped-BaSnO₃ thin films for a range of achievable doping densities. The experimental values show a good agreement with the predictions of a LO-phonon emission model with an effective phonon energy of 120 meV, indicating the likelihood of optical phonon emission being the mechanism limiting velocity saturation in La:BSO thin films. Delta-doped BSO channels exhibit a density-dependent saturation velocity decreasing proportional to $n_s^{-1/2}$ from $1.8 \times 10^7 \text{ cm/s}$ to $2 \times 10^6 \text{ cm/s}$ at sheet carrier densities ranging from 10^{13} to $2 \times 10^{14} \text{ cm}^{-2}$, accounting for the contribution of multiple sub-bands necessary for such high carrier densities. The estimated and measured saturation velocities presented in this work would aid in informed device design for electronics based on thin film BSO channels.

See the [supplementary material](#) for SEM images of representative constriction structures fabricated on each sample, the electric field vs current density plots for the complete set of devices measured across all three samples used in this study along with the tabulated data, electric field vs current density plots at 80 and 300 K for the sample with $n_s = 7.23 \times 10^{13} \text{ cm}^{-2}$, the calculated phonon spectra of BaSnO₃, and

the details of the optical phonon model for the 2-D case with and without sub-band contributions.

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