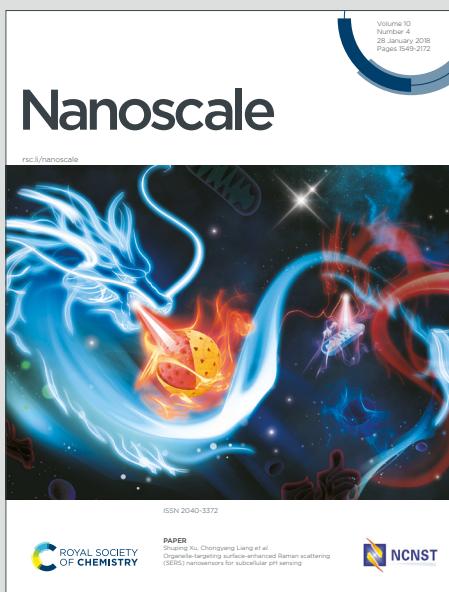


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**Semiconducting  $\text{SN}_2$  Monolayer with Three-Dimensional Auxetic**View Article Online  
DOI: 10.1039/C9NR07263B**Properties: A Global Minimum with Tetracoordinated Sulfurs**Fengyu Li,<sup>a, #\*</sup> Xiaodong Lv,<sup>a, #</sup> Jinxing Gu,<sup>b</sup> Kaixiong Tu,<sup>b</sup> Jian Gong,<sup>a</sup> Peng Jin,<sup>c,\*</sup>Zhongfang Chen<sup>b,\*</sup><sup>a</sup> *School of Physical Science and Technology, Inner Mongolia University, Hohhot, 010021, China*<sup>b</sup> *Department of Chemistry, The Institute for Functional Nanomaterials, University of Puerto Rico, Rio Piedras Campus, San Juan, PR 00931, USA*<sup>c</sup> *School of Materials Science and Engineering, Hebei University of Technology, Tianjin 300130, China.*

\*Corresponding Author: fengyuli@imu.edu.cn (FL); china.peng.jin@gmail.com (PJ); zhongfangchen@gmail.com (ZC)

# Equal contribution to this work.

**Abstract**

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Designing new two-dimensional (2D) materials, exploring their unique properties and diverse potential applications are of paramount importance to condensed matter physics and materials science. In this work, we predicted a novel 2D  $S\text{-SN}_2$  monolayer ( $S\text{-SN}_2$ ) by means of density functional theory (DFT) computations. In the  $S\text{-SN}_2$  monolayer, each S atom is tetracoordinated with four N atoms, and each N atom bridges two S atoms, thus forming a tri-sublayer structure with square lattice. The monolayer exhibits good stability, as demonstrated by the moderate cohesive energy, all positive phonon modes, and the structural integrity maintained through 10 ps molecular dynamics simulations up to 1000 K. It is an indirect-bandgap semiconductor with high hole mobility, and the bandgap can be tuned by changing the thickness and external strains (the indirect-bandgap to direct-bandgap transition occurs when the biaxial tensile strain reaches 4%). Significantly, it has large Young's modulus and three-dimensional auxetic properties (both in-plane and out-of-plane negative Poisson's ratios). Therefore, the  $S\text{-SN}_2$  monolayer holds great potential applications in electronics, photoelectronics and mechanics.

**Keywords:** two-dimensional materials, density functional theory, stability, strain, electronic properties, auxetic properties, optical properties, tetracoordinated sulfur

## 1. Introduction

Binary sulfur-nitrogen molecules with different chemical compositions and configurations have been investigated for years,<sup>1–3</sup> however, most of them could only exist at low temperatures. For example, dinitrogen sulfide (N<sub>2</sub>S) will decompose into N<sub>2</sub> and S<sub>2</sub> when the temperature is higher than 160 K. The disulfur nitride could be produced in a microwave-discharged argon/nitrogen/sulfur steam and trapped in solid argon at 12 K.<sup>4</sup> The reported sulfur-nitrogen crystals are mainly composed of ring clusters<sup>5–8</sup> or SN chains.<sup>9,10</sup> Recently, Li *et al.* performed a systematic computational study on the structural, electronic and bonding properties of sulfur nitrides, and predicted four high-pressure phases of SN<sub>x</sub>.<sup>11</sup> Among them, the SN<sub>2</sub> with orthorhombic *Pnnm* space group is a direct-bandgap semiconductor (bandgap: 0.66 eV) at 60 GPa, and quite recently, the proposed SN<sub>2</sub> solid was successfully synthesized above 64 GPa.<sup>12</sup>

In addition to the three-dimensional (3D) binary sulfur nitrides, their 2D counterparts were also predicted theoretically. Very recently, Chen's group proposed a dynamically and thermally stable trisulfur dinitride (S<sub>3</sub>N<sub>2</sub>) 2D crystal, whose indirect band gap is as wide as 3.92 eV, and could be further tuned by forming multilayers, nanoribbons and nanotubes.<sup>13</sup> Based on the structure of 1T-MoS<sub>2</sub>, Lin *et al.* theoretically designed a 1T-SN<sub>2</sub> single-layer.<sup>14</sup> 1T-SN<sub>2</sub> was computed to be an indirect-bandgap semiconductor with wide bandgap (2.83 eV), and the bandgap could be narrowed by external biaxial stretching. The 1T-SN<sub>2</sub> monolayer has dynamical stability, however, its thermal and mechanical stabilities are to be determined, its bandgaps under uniaxial strain and the thickness of multilayers are yet unknown. More importantly, is 1T-SN<sub>2</sub> monolayer the lowest-energy configuration of the 2D

SN<sub>2</sub> crystals? If not, what is the structure of the most stable SN<sub>2</sub> monolayer and what intriguing properties will it possess?

To address the above issues, we performed a global minimum search for SN<sub>2</sub> in the 2D space, and a novel *S*-SN<sub>2</sub> monolayer with tetracoordinated S atoms was reached. The *S*-SN<sub>2</sub> monolayer is extraordinarily stable and is an indirect-bandgap semiconductor with a slightly narrow bandgap of 2.79 eV compared to that of the 1*T*-SN<sub>2</sub> (2.89 eV). Significantly, it features in-plane and out-of-plane negative Poisson's ratios, and is thus a potential 3D auxetic material.

## 2. Computational Methods

All spin-polarized density functional theory (DFT) computations were carried out by using the generalized gradient approximation (GGA) in the form of the Perdew-Burke-Ernzerhof exchange-correlation functional (PBE).<sup>15</sup> Projector augmented wave (PAW) method<sup>16</sup> was used as implemented in the Vienna ab initio simulation package (VASP) code.<sup>17</sup> The PBE-D2 approach<sup>18</sup> with dispersion energy correction was used for the geometry optimization of the bulk and few layers. The Monkhorst-Pack scheme<sup>19</sup> of 9×9×1 *k*-points mesh was applied for the unit cell geometry optimizations, while a larger grid (25×25×1) was used for the electronic structure computations. The HSE06 functional<sup>20</sup> was utilized to obtain more accurate band structures. The dynamic energy cutoff for the plane-wave basis set was set to be 600 eV. During the geometry optimizations, both the lattice constants *a* and *b*, and the atomic positions were fully relaxed until the atomic forces on the atoms were less than 10<sup>-5</sup> eV/Å and the total energy change was less than 10<sup>-6</sup> eV. To avoid interactions between periodic images, a large vacuum region of ~15 Å was applied to the perpendicular direction of the 2D layer.

First-principles molecular dynamics (FPMD) simulations were performed to assess the thermal stability of the 2D materials at the PBE level with the temperature controlled by the Nosé-Hoover method.<sup>21</sup> The initial configurations were annealed at different temperatures. At each temperature, the MD simulation in an NVT canonical ensemble lasted for 10 ps with a time step of 0.5 fs.

The particle-swarm optimization (PSO) multidimensional method, as implemented in the CALYPSO code,<sup>22</sup> was employed to search for the low-energy structures. In our PSO simulations, the population size was set at 30, the number of generations was maintained at 50. The unit cells contained 3, 6, 9 and 12 total atoms. The structure relaxations employed the PBE functional, as implemented in VASP software.

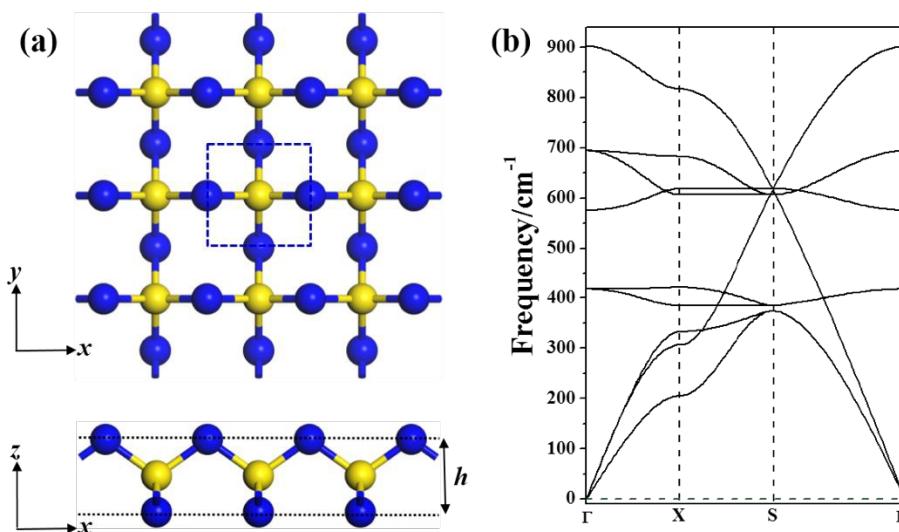
### 3. Results and Discussion

#### 3.1. Geometric Properties of the *S*-SN<sub>2</sub> Monolayer

Our global minimum search for SN<sub>2</sub> in the 2D space revealed that a novel square lattice structure with tetracoordinate S atoms (Fig. 1a) has the lowest energy. The unit cell of this SN<sub>2</sub> monolayer consists of one S atom and two N atoms. The optimized structure of the monolayer has the symmetry of  $P\bar{4}M2$  with the square lattice of 2.63 Å, in which each S atom is tetracoordinated with four N atoms, and each N atom bridges two S atoms, thus forming a tri-sublayer structure (Fig. 1a). To differentiate this new structure from the previous reported 1T-SN<sub>2</sub>,<sup>14</sup> we denote this new monolayer as *S*-SN<sub>2</sub> considering its square lattice.

The N–S bonds (*d*) of *S*-SN<sub>2</sub> have the uniform length of 1.62 Å, and the layer thickness (*h*) is 1.88 Å, both shorter than those of the previously proposed 1T-SN<sub>2</sub> monolayer (the *d* and *h* values are 1.80 and 1.90 Å, respectively, at the same level of

theory). Note that structurally the  $S\text{-}\text{SN}_2$  monolayer well resembles the recently proposed monolayers of Tetra- $\text{MoN}_2$ <sup>23</sup> and  $\text{CO}_2$ ,<sup>24</sup> and the orthorhombic  $\text{SN}_2$  ( $Pnnm$ ) predicted by Li *et al.* can be considered as its bulk precursor.<sup>11</sup> In the  $Pnnm\text{-}\text{SN}_2$  solid, the S atoms are hexa-coordinated and N atoms are tri-coordinated, the  $(0\ 0\ 1)$  slab can be viewed as the twisted  $S\text{-}\text{SN}_2$  monolayer.



**Fig. 1** The  $S\text{-}\text{SN}_2$  monolayer: (a) Optimized structure from top and side views (a  $3\times 3\times 1$  supercell, the unit cell is highlighted by the blue dashed square), blue and yellow balls denote N and S atoms, respectively; (b) Computed phonon spectrum.

Note that the sulfur atoms adopt the hexacoordinated and tetracoordinated states in the  $1T\text{-}\text{SN}_2$  and  $S\text{-}\text{SN}_2$  monolayers, respectively. The hexacoordination of S was also realized in the dimeric N-Chloroiminosulfur tetrafluoride.<sup>25</sup> However, the tetracoordination of S, which was regarded to be only found in intermediates because of the strain,<sup>26</sup> was barely obtained in experiment.<sup>27</sup> It was recognized that usually electron-withdrawing groups such as F, O, and N are needed to stabilize the hypervalent state of sulfur.<sup>28</sup> Thus, we expect that the  $1T/S\text{-}\text{SN}_2$  monolayer containing

the hexa/tetracoordinated S moiety is stabilized by the N atoms, each of which withdraws 0.19/0.23  $e^-$  from S according to our Hirshfeld charge analysis.<sup>29</sup>

### 3.2. Stability of the S-SN<sub>2</sub> Monolayer

The intriguing structure of S-SN<sub>2</sub> monolayer inspired us to further examine its stability. Firstly, we computed its cohesive energy ( $E_{coh}$ ), which is obtained by  $E_{coh} = (nE_N + mE_S - E_{SN_2})/(n+m)$ , where  $E_N$ ,  $E_S$  and  $E_{SN_2}$  are the total energies of a single N atom, a single S atom, and the SN<sub>2</sub> monolayer, respectively.  $n$  and  $m$  are the number of N and S atoms in the supercell. According to this definition, a material with a more positive  $E_{coh}$  value has a higher thermodynamic stability. The cohesive energy of the S-SN<sub>2</sub> monolayer is 3.24 eV/atom, larger than those of the 1T-SN<sub>2</sub> monolayer (3.08 eV/atom) and the 3D SN<sub>2</sub> crystal (2.68 eV/atom at 60 GPa),<sup>11</sup> but smaller than the  $E_{coh}$  value (3.45 eV/atom) of the cage-like S<sub>4</sub>N<sub>4</sub> molecular crystal,<sup>30</sup> the starting material for various synthetic routes in sulfur-nitrogen chemistry. In comparison, the cohesive energies of the experimentally realized 2D silicene<sup>31,32</sup> and phosphorene<sup>33,34</sup> are 3.54 and 3.48 eV/atom, respectively, at the same level of theory. The rather favorable cohesive energy of the S-SN<sub>2</sub> monolayer ensures that it has a strongly connected network, and is very promising to be synthesized.

Secondly, we confirmed that the S-SN<sub>2</sub> monolayer is also dynamically stable, as demonstrated by the real frequency values in the phonon spectrum (Fig. 1b). The highest frequency is 900 cm<sup>-1</sup>, which is ~50 cm<sup>-1</sup> higher than that of 1T-SN<sub>2</sub>,<sup>14</sup> and also higher than those of silicene (580 cm<sup>-1</sup>)<sup>35</sup> and phosphorene (456 cm<sup>-1</sup>),<sup>36</sup> indicating its remarkable dynamic stability.

Thirdly, we examined its thermal stability by performing first-principles molecular dynamics (FPMD) simulations with a 5×5 supercell. Our simulations at

300 K, 500 K, 1000 K, and 1500 K showed that the  $S\text{-}\text{SN}_2$  monolayer maintained its structural integrity throughout the 10 ps FPMD simulation up to 1000 K, but seriously distorted at 1500 K (Fig. S1). The slightly distorted structure after the simulation at 1000 K can recover the initial configuration of  $S\text{-}\text{SN}_2$  monolayer upon full atomic relaxation. In comparison, the reported 1T- $\text{SN}_2$  monolayer can also maintain the structural integrity up to 1000 K in our FPMD simulations (Fig. S2), while the proposed  $\text{S}_3\text{N}_2$  monolayer would dissociate into multiple S-N chains and clusters at the same high temperature.<sup>13</sup>

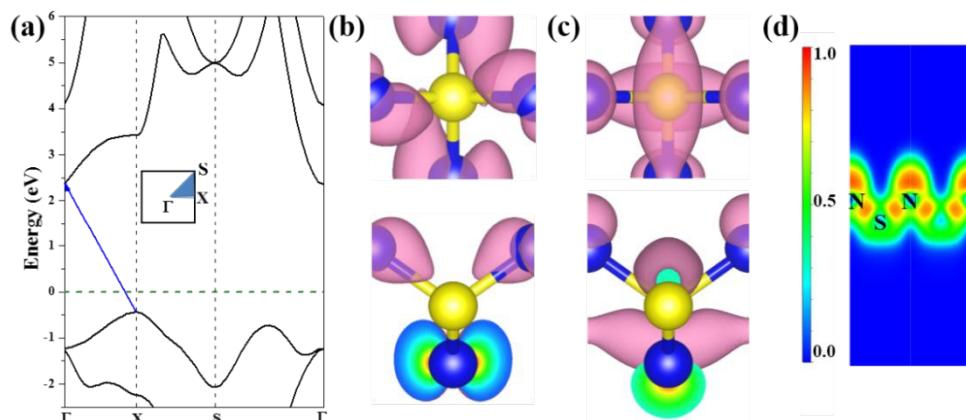
The above results demonstrated that the  $S\text{-}\text{SN}_2$  monolayer is rather stable, and is expected to be experimentally feasible. Reminiscing the aromaticity in the ring structure of  $\text{S}_2\text{N}_2$  and other sulfur-nitrogen molecules,<sup>3,37</sup> the high stability of the  $S\text{-}\text{SN}_2$  monolayer raised another question: is the  $S\text{-}\text{SN}_2$  monolayer also aromaticity? To address this question, we examined the chemical bonding patterns of the  $S\text{-}\text{SN}_2$  monolayer by using the solid state adaptive natural density partitioning (SSAdNDP) method.<sup>38</sup> The SSAdNDP results suggest that besides the two  $sp$ -orbital lone-pairs and two  $p$ -orbital lone-pairs on N atoms, there are four two-center-two-electron bonds between N and S in the unitcell of  $S\text{-}\text{SN}_2$  monolayer (Fig. S3). As a result, the  $S\text{-}\text{SN}_2$  monolayer is not aromatic. Nevertheless, the  $sp^2(\text{N})\text{-}sp^3(\text{S})$  hybridization bonds lead to robust connection between the N and S atoms, and thus result in the pronouncing stability of 2D N–S network.

### 3.3. Electronic and Optical Properties of the $S\text{-}\text{SN}_2$ Monolayer.

We further investigated the electronic properties of  $S\text{-}\text{SN}_2$  monolayer at the HSE06 level of theory. Similar to the 1T- $\text{SN}_2$  monolayer, which has an indirect bandgap ( $E_g$ ) of 2.89 eV according to our calculations (2.83 eV in the literature<sup>14</sup>),

the  $S\text{-}\text{SN}_2$  monolayer is also an indirect-gap semiconductor with the bandgap of 2.79 eV (Fig. 2a). The valence band maxima (VBM) are mainly composed of  $p$  orbitals of nitrogen atoms, similar to the case of Tetra- $\text{MoN}_2$ ,<sup>23a</sup> while the conduction band minima (CBM) consist of both  $S\text{-}p$  and  $\text{N}\text{-}p$  states (Fig. 2b,c).

To gain further insights into the chemical bonding of the  $S\text{-}\text{SN}_2$  monolayer, we examined the electron localization function (ELF), as visualized in Fig. 2d. Since the S atoms donate electrons to N atoms as suggested by the Hirshfeld charge analysis (0.23  $e^-$  per N atom), the electron density around N atoms is rather localized with high ELF values. The electrons localized between S and N atoms show some deviation from the bond center, indicating the nature of polar covalent bonding, which partially contributes to the high thermal stability of the  $S\text{-}\text{SN}_2$  monolayer.



**Fig. 2** The  $S\text{-}\text{SN}_2$  monolayer: (a) Band structure (the Fermi energy was set to be zero and denoted by the green dashed line), (b) spatial distributions of wave functions of VBM and (c) CBM from the top and side views (isovalue:  $0.02 \text{ e}\text{\AA}^{-3}$ ); (d) ELF map sliced perpendicular to the 2D plane, red ( $\text{ELF} = 1$ ) and blue ( $\text{ELF} = 0$ ) indicate accumulated and vanishing electron density, respectively.

Since applying external strain is an effective way to engineer the band structures

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of 2D nanomaterials, we studied the effect of uniaxial and biaxial (tensile and compressive) strains ( $\eta$ ) along  $x$  and  $y$  directions on the band structure of the  $S\text{-}\text{SN}_2$  monolayer, in comparison with the  $1T\text{-}\text{SN}_2$  monolayer. During the uniaxial and biaxial strains, the dynamic stabilities of the  $S\text{-}\text{SN}_2$  monolayer could be reserved with  $\eta$  in the range of  $-2\% \leq \eta \leq 8\%$  and  $-2\% \leq \eta \leq 9\%$ , respectively. When the uniaxial (biaxial) strain of 9% (10%) or larger is imposed to the  $S\text{-}\text{SN}_2$  monolayer, imaginary frequencies will appear in the calculated phonon spectra (Fig. S4), indicating that the dynamic instability of the monolayer under such extreme strains.

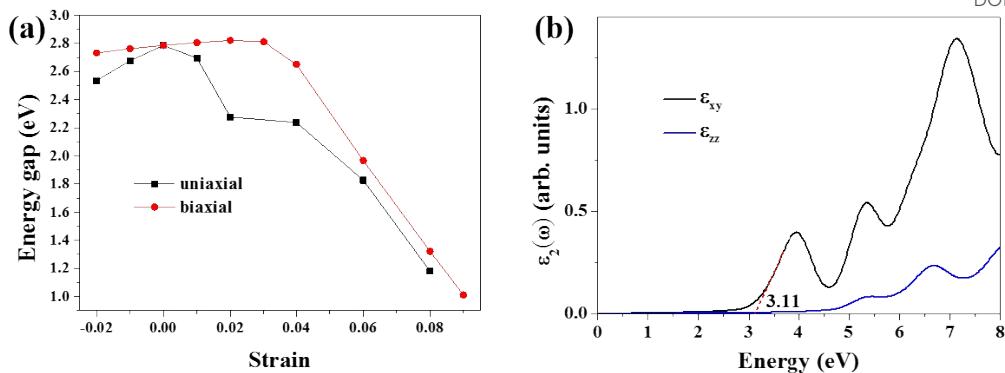
When the uniaxial strains (either compression or stretching) are applied to the  $S\text{-}\text{SN}_2$  monolayer, the bandgap decreases compared to that of the equilibrium structure (Fig. 3a). In particular, the uniaxial tensile strain could effectively decrease the bandgap: the value is reduced from the original 2.79 eV to 1.18 eV under uniaxial tensile of 8% (Fig. S5). The uniaxial strains destroy the symmetry in the reciprocal space of the  $S\text{-}\text{SN}_2$  monolayer, and the CBM shifts down under both compression and expansion strains along the  $x$ -direction (remaining at  $\Gamma$  point for  $-2\% \leq \eta \leq 7\%$ , but switching to  $\text{Y}$  point for  $\eta = 8\%$ ), while the VBM oscillates around the  $\text{X}$  point, as a result, the bandgap is decreased regarding to the pristine  $E_g$ .

In comparison, we examined the effect of uniaxial strain on the electronic structure of the  $1T\text{-}\text{SN}_2$  monolayer. Interestingly, under the strain modulation, the  $1T\text{-}\text{SN}_2$  monolayer remains the indirect-gap semiconducting nature. The band gap of  $1T\text{-}\text{SN}_2$  exhibits a quasi-linear relation with the uniaxial strain in either  $x$  (armchair) or  $y$  (zigzag) direction (Fig. S5): the band gap increases (decreases) monotonically with the tensile (compressive) strain along  $x$  direction, and the gap change is in a relative small range (2.82~2.96 eV) when the strain of  $-2\%$  to  $2\%$  is applied; however, along

*y* direction, the band gap decreases (increases) in a more pronounced manner with the tensile (compressive) strain. When the *y*-axial tensile strain is as large as 5%, the gap value reduces to 2.44 eV from 2.89 eV of the pristine monolayer; when the -2% compressive strain is imposed along the *y* direction, the gap is enlarged to 3.14 eV.

When applying biaxial strains to the *S*-SN<sub>2</sub> monolayer in the range of -2%~3%, the bandgap increases almost linearly with increasing the strain (2.73~2.82 eV). When the tensile strain is even larger, at the external tensile of 4%, the bandgap drops from the linear relation, and the indirect-gap to direct-gap transition occurs (bandgap of 2.65 eV, Fig. S5). Further increasing the strain continues to narrow the bandgap, but transits to indirect bandgap again, since the VBM moves from X/Y *k*-point for  $\eta = 4\%$  to the value between X and  $\Gamma$  *k*-points for larger stretches, and under the biaxial tensile of 9%, the indirect bandgap of the *S*-SN<sub>2</sub> monolayer is 1.01 eV. In comparison, the band gap of the 1*T*-SN<sub>2</sub> monolayer decreases monotonically from ~4.3 to ~0.6 eV as the biaxial strain increases from -10% to 10%.<sup>14</sup>

Overall, the strain-tailored band structure of the *S*-SN<sub>2</sub> monolayer can be contributed to the variation of the N–S bonds: the uniaxial or biaxial stretching weakens the N–S bonds, and as a result the CBM moves to lower energies and the bandgap was narrowed (Fig. S6), which is in line with previous DFT finding that the strain effect on the band structures of boron nitride monolayers originates from the B–N bonding.<sup>39</sup>



**Fig. 3** (a) The HSE06 band gap as a function of the external strains for the  $S\text{-}\text{Sn}_2$  monolayer. (b) The imaginary dielectric constants (The red dashed line denotes an approximate linear fitting for estimating the band edge of the first adsorption peak).

Note that the  $S\text{-}\text{Sn}_2$  monolayer is an indirect-gap semiconductor with the VBM and CBM located at the  $X$  and  $\Gamma$  points, respectively. This is beneficial to restrain the recombination of the photo-activated electron-hole pairs.<sup>40</sup> Thus, we also investigated the optical adsorption property of the  $S\text{-}\text{Sn}_2$  monolayer by computing the imaginary parts of the dielectric function  $\varepsilon_2(\omega)$ . As shown in Fig. 3b,  $S\text{-}\text{Sn}_2$  exhibits adsorption starting at  $\sim 2.2$  eV, and the optical gap (estimated by linear fitting of the first adsorption peak) is 3.11 eV, much smaller than that of 1T- $\text{Sn}_2$  (3.86 eV, Fig. S7). Therefore, the  $S\text{-}\text{Sn}_2$  monolayer might be used as the visible-light-driven photocatalysts.

### 3.4. Carrier Mobility of the $S\text{-}\text{Sn}_2$ Monolayer

We then systematically investigated the carrier mobility of the  $S\text{-}\text{Sn}_2$  monolayer to better understand its electronic properties using the deformation potential (DP) theory,<sup>41</sup> which has been extensively applied to evaluate the carrier mobility of various 2D materials,<sup>34,42–49</sup> and is derived from the following expression:

$$\mu = \frac{2e\hbar^3 C}{3k_B T |m^*|^2 E_1^2}$$

where,  $\hbar$  is the reduced Planck constant,  $k_B$  is the Boltzmann constant,  $T$  is the temperature (the room temperature 300 K was adopted in our study),  $m^*$  is the effective mass in the transport direction,  $E_1$  and  $C$  are the DP constant and the in-plane stiffness, respectively.  $E_1$  signifies the shift of the band edges  $E_{edge}$  (VBM and CBM) induced by the strain  $\delta$  ( $\delta = \Delta a/a_o$ ,  $\Delta a$  and  $a_o$  are the variation and equilibrium lattice lengths, respectively), with the form of  $E_1 = \partial E_{edge} / \partial \delta$ . The in-plane stiffness can be determined by  $C = (\partial^2 E / \partial \delta^2) / S_o$ , where  $E$  is the total energy of the supercell,  $\delta$  is the applied uniaxial strain, and  $S_o$  is the area of the equilibrium supercell.

The carrier mobility of the S-SN<sub>2</sub> monolayer was evaluated along the  $x$  and  $y$  directions (Fig. 1a). The details of computing the in-plane stiffness  $C$  and the DP constant  $E_1$  are given in Fig. S6 and Table 1. The S-SN<sub>2</sub> monolayer shows very high hole mobility of  $1.16 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> for holes along both  $x$  and  $y$  directions, much higher than that of MoS<sub>2</sub> (200 cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>),<sup>46</sup> while the electron mobility ( $0.16 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>) is comparable to those of black phosphorene ( $0.08 \times 10^3$ – $1.14 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>).<sup>45</sup> In comparison, the 1T-SN<sub>2</sub> monolayer has anisotropic carrier mobility along the  $x$  and  $y$  directions (Fig. S7,8), and the electron mobility ( $\sim 2 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>) is higher than those of holes ( $0.24 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> and  $0.05 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> in  $x$  and  $y$  directions, respectively) in either direction, which is different from S-SN<sub>2</sub>, MoS<sub>2</sub> and phosphorene with more mobile holes.<sup>45,46</sup> The anisotropy of electron and hole

mobilities was found in many 2D materials, such as the group 15 monolayers,<sup>50</sup> the methyl-terminated germanene,<sup>51</sup> 8B-*Pmmn* borophene/borophane,<sup>52</sup> and MXenes.<sup>53</sup>

**Table 1** The calculated effective mass  $m^*$ , DP constant  $E_I$ , in-plane stiffness  $C$ , and carrier mobility  $m$  of the *S*-SN<sub>2</sub> and 1*T*-SN<sub>2</sub> (in italic) monolayers along  $x$  and  $y$  directions.

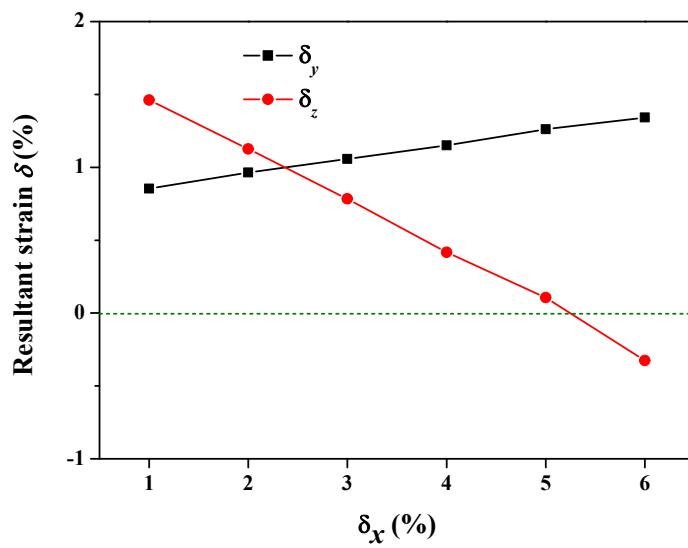
Carrier	$m^*$	$m^*$	$ E_{Ix} $	$ E_{Iy} $	$C_x$	$C_y$	$\mu_x$	$\mu_y$
type	$x/m_0$	$y/m_0$	(eV)		(J m <sup>-2</sup> )		(10 <sup>3</sup> cm <sup>2</sup> V <sup>-1</sup> s <sup>-1</sup> )	
electron	0.47		10.43		279.82		0.16	
	0.80	0.28	1.79	4.76	242.20	242.20	1.67	1.87
hole	-2.46		0.75		279.82		1.16	
	-0.88	-1.36	4.26	6.33	242.20	242.20	0.24	0.05

### 3.5. Mechanical Properties of the *S*-SN<sub>2</sub> Monolayer

Besides the electronic properties, we also investigated the mechanical properties of the *S*-SN<sub>2</sub> monolayer by examining the elastic constants. The computed elastic constants of graphene are  $C_{11} = C_{22} = 351.77$  N/m and  $C_{12} = C_{21} = 60.13$  N/m, which are in good agreement with previous experimental measurements<sup>54</sup> and computational results.<sup>55</sup> For the *S*-SN<sub>2</sub> monolayer, the computed elastic constants are  $C_{11} = C_{22} = 282.89$  N/m,  $C_{12} = C_{21} = -29.50$  N/m, and  $C_{44} = 10.34$  N/m. Based on the mechanical stability criteria ( $C_{11}C_{22} - C_{12}^2 > 0$ ,  $C_{44} > 0$ ),<sup>56</sup> the *S*-SN<sub>2</sub> monolayer is mechanically stable and isotropic: it has a negative in-plane Poisson's ratio of -0.104 ( $C_{12}/C_{11}$ ) for both  $x$  and  $y$  directions, and a high in-plane Young's modulus ( $(C_{11}C_{22} - C_{12}C_{21})/C_{22}$ ) of 279.82 N/m, larger than those of 1*T*-SN<sub>2</sub> (242.20 N/m) and MoS<sub>2</sub> (124.06 N/m) monolayers at the same level of theory.

To confirm the unusual negative Poisson's ratio (NPR), we examined a series of uniaxial tensile strains as illustrated in Fig. 4. When elongating along  $x$  direction by  $\delta_x$

( $1\% \leq \delta_x \leq 5\%$ ) of the  $S\text{-}\text{SN}_2$  monolayer, expansions in both the in-plane  $y$  direction and the out-of-plane  $z$  direction were found as indicated by the positive resultant strains along  $y$  and  $z$  directions ( $\delta_y$  and  $\delta_z$ ). More specifically, the resultant strain  $\delta_y$  increases monotonically from 0.85% to 1.34% when the applied tensile  $\delta_x$  enhances from 1% to 6%; while the resultant  $\delta_z$  decreases from 1.46% to 0.11% when  $\delta_x$  is increased from 1% to 5%, and the  $\delta_z$  value decreases to a negative value of  $-0.33\%$  when  $\delta_x$  reaches 6%. The coexistence of the out-of-plane NPR and the in-plane NPR suggests that the  $S\text{-}\text{SN}_2$  monolayer is new family member of 2D monolayers with 3D auxetic properties following the just predicted  $\text{S}_3\text{N}_2$  monolayers with  $\alpha$ -heart structure (whose in-plane NPR is  $-0.026$ , much smaller than the corresponding value  $-0.104$  of the  $S\text{-}\text{SN}_2$ ).<sup>57</sup>



**Fig. 4** Mechanical response of the  $S\text{-}\text{SN}_2$  monolayer under uniaxial tensile strain along  $x$  direction.

### 3.6. The $S\text{-}\text{SN}_2$ Bilayers

Thickness and stacking pattern were also examined to get further insights into the electronic properties of  $S\text{-}\text{SN}_2$ , since they can affect the properties of 2D materials.<sup>40c,58</sup> Two possible stacking patterns of  $S\text{-}\text{SN}_2$  bilayer, namely AA and AB stackings, were considered (Fig. S9). In comparison, we also examined the stacking patters of the  $1T\text{-}\text{SN}_2$  bilayer (four patterns, AA, AA', AB, and AB', Fig. S10).

The interlayer distances (4.55 and 4.81 Å for AA and AB stacking, respectively) of the  $S\text{-}\text{SN}_2$  bilayers are larger than those of  $1T\text{-}\text{SN}_2$  bilayers (2.95~3.07 Å, Table S1). The binding energy ( $E_b$ ) of the  $\text{SN}_2$  bilayer in different stacking configurations is calculated via  $E_b = (2 \times E_{\text{monolayer}} - E_{\text{bilayer}})/2$ , where  $E_{\text{monolayer}}$  and  $E_{\text{bilayer}}$  are the total energies of the  $\text{SN}_2$  monolayer and bilayer, respectively. The binding energies of the  $S\text{-}\text{SN}_2$  bilayers (0.30 and 0.29 eV for AA and AB stacking, respectively) are comparable to or slightly higher than those of  $1T\text{-}\text{SN}_2$  bilayers (0.28~0.29 eV, Table S1).

As expected, the bandgaps of  $S\text{-}\text{SN}_2$  bilayer in AA and AB stacking configurations are respectively reduced to 2.64 and 2.60 eV (Fig. S9) compared to that of the monolayer (2.79 eV), the  $S\text{-}\text{SN}_2$  bulk in the AA stacking remains being indirect semiconducting but with a further reduced band gap of 2.58 eV.

Similarly, the indirect band width of  $1T\text{-}\text{SN}_2$  bilayer was narrowed compared to that of monolayer: 2.76 and 2.69 eV for the AB and AA stacking, respectively. Since the band gap is more sensitive in the AA stacking pattern and the stability of AA stacking is very close to the AB stacking for  $1T\text{-}\text{SN}_2$  bilayer, we further computed the electronic structures of the  $1T\text{-}\text{SN}_2$  trilayer and tetrалayer in AA stacking (Fig. S11). The band gap turns to be 2.59 and 2.54 eV, respectively, and the  $1T\text{-}\text{SN}_2$  bulk in AA stacking has an indirect bandgap of 2.28 eV.

#### 4. Conclusion

In summary, we predicted a new phase of  $\text{SN}_2$  monolayer, namely  $S\text{-}\text{SN}_2$ , by using first-principles calculations combined with the particle-swarm optimization method. Its structure belongs to space group  $\bar{P}4M2$  and features the unusual tetracoordinated S. The moderate cohesive energy, absence of imaginary modes in phonon spectrum, and structural integrity through 10 ps FPMD simulations up to 1000 K indicate the high stability of the  $S\text{-}\text{SN}_2$  monolayer. The  $S\text{-}\text{SN}_2$  monolayer is an indirect-bandgap semiconductor with high hole mobilities, and shows adsorption in the visual-light region. The bandgap of the  $S\text{-}\text{SN}_2$  monolayer can be further tuned by thickness and external strains, and an indirect-direct bandgap transition could be induced under the biaxial tensile strain. Moreover, it has large Young's modulus, and the coexistence of out-of-plane and in-plane negative Poisson's ratios renders the  $S\text{-}\text{SN}_2$  monolayer 3D auxetic properties. Therefore, the  $S\text{-}\text{SN}_2$  monolayer is expected to have wide applications in electronics, photoelectronics, and mechanics. Especially, we are calling for more efforts in developing 2D crystals with 3D auxetic properties, which will bring us more breakthroughs in materials with novel Poisson's ratio materials.

#### Conflicts of interest

There are no conflicts of interest to declare.

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