Wide-angle spectrally selective absorbers and thermal emitters based on inverse opals

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Abstract

Engineered optical absorbers are of substantial interest for applications ranging from stray light reduction to energy conversion. We demonstrate a large-area (centimeter-scale) metamaterial that features near-unity frequency-selective absorption in the mid-infrared wavelength range. The metamaterial comprises a self-assembled porous structure known as an inverse opal, here made of silica. The structure's large volume fraction of voids, together with the vibrational resonances of silica in the mid-infrared spectral range, reduce the metamaterial's refractive index to close to that of air and introduce considerable optical absorption. As a result, the frequency-selective structure efficiently absorbs incident light of both polarizations even at very oblique incidence angles. The absorber remains stable at high temperatures (measured up to ~900 °C), enabling its operation as a frequency-selective thermal emitter. The excellent performance of this absorber/emitter and ease of fabrication make it a promising surface coating for passive radiative cooling, laser safety, and other large-area applications.

Electromagnetic-wave absorption based on metamaterials has been a rapidly growing motif in different research fields, including energy conversion [1] and thermoregulation [2]. At optical frequencies, engineered absorbers are used for stray light reduction in the visible range [3], [4], refractive-index sensing in the near-infrared range [5]–[7], and thermal emitters [8]–[11] in the mid-infrared range. To achieve high absorption, the reflection, transmission, and scattering must all be minimized; this can be realized by an absorbing structure or material that is impedance-matched to the incident medium [12].

Since the wavelength of optical-frequency electromagnetic radiation is on the order of hundreds to thousands of nanometers, typical engineered optical absorbers are comprised of nanostructured materials [13], [14]. At the same time, many applications require inexpensive large-area absorbers [15], [16], motivating designs that can be fabricated without the use of top-down lithography. Examples of such lithography-free absorbers include carbon nanotube (CNT) forests [3], [17], and lossy low-index films like polydimethylsiloxane (PDMS) [18].

Here, we demonstrate a wide-angle large-area absorber for mid-infrared light with polarization-independent spectral selectivity, realized using a metamaterial based on inverse opals (IOs), which are highly porous structures obtained through assembly of colloids that serve as a sacrificial structuring agent for a background matrix material (here we use sol-gel silica; more information about the synthesis can be found in *Sup. Info. 1*) [19]. In IOs, the size and arrangement of the pores and the material composition (background matrix, as well as dopants and other inclusions) can all be engineered, creating a large design space. The pores are also interconnected and can be infiltrated with fluids [20], which may be relevant for dynamic tunability, sensing, or catalytic applications [21]–[25].

The diameter of the templating colloidal spheres used for IOs is typically on the order of a few hundred nanometers. After selective removal of the colloids, the corresponding volume comprises an interconnected array of air pockets while the surrounding volume is the glassy matrix material. The resulting composite material thus has an effective refractive index close to that of air (in particular, when using silica as the matrix material), as has been observed at visible frequencies [26]. In the mid-infrared range, the vibrational resonances of silica [27] introduce substantial optical loss, resulting in an absorbing metamaterial that is well matched to the refractive index of air, thus minimizing reflections at the interface between air and the IO film.

A scanning electron microscope (SEM) image of an inverse opal film with void size of 250 nm is presented in Fig. 1(a), showing the highly interconnected porous structure. The high degree of ordering (which can be disrupted through the addition of salts in the assembly process) is unimportant for the functionality at mid-infrared wavelengths; however, it is convenient for the modeling of the effective refractive index, since the volume fraction of background matrix and voids is well known for a face-centered cubic (fcc) lattice, 26% and 74%, respectively [19]. We performed infrared variable-angle spectroscopic ellipsometry (J.A. Woollam IR-VASE Mark II) on a 2-μm-thick IO film on silicon and extracted its optical properties (Fig. 1 (b), (c)). To convert the measured ellipsometric parameters, Ψ and Δ [28] (see *Sup. Info. 2* for raw data), into the

effective refractive index and absorption coefficient, we modeled the IO thin film using the Bruggeman effective medium approximation (EMA, see *Supp. Info. 2*) [29]. We first focused on 1.8 to 3 μm , a spectral range in which SiO₂ is nearly dispersionless and its refractive index is well known [30], and fit to the fraction of air present in the film (i.e. the film porosity). The resulting fitted porosity is ~76%, which is very close to the theoretical value of the porosity based on the fcc structure of the opal assembly ($\sqrt{2}\pi/6 = 74\%$) [19]. Fixing the porosity at this value, we then fit the ellipsometric measurements in the wavelength range of 6 to 12 μ m, in which silica has vibrational resonances. The resulting Kramers–Kronig-consistent fitted effective complex refractive index of the inverse opal film, $n_{IO} + i\kappa_{IO}$, along with the fitted values assuming no porosity are shown in Fig. 1(b, c); details about the fitting parameters are provided in *Sup. Info.* 2. The void size of the IOs (~250 nm) is significantly smaller than the wavelength in the mid-infrared range, ensuring the validity of the effective-medium assumption [31]. For comparison, the optical properties of an amorphous SiO₂ thin film from literature [30] are also displayed in the same figure. The IO film has n_{IO} very close to one ($n_{air} = 1$), and a significantly reduced but non-zero κ_{IO} compared to the bulk amorphous SiO₂.

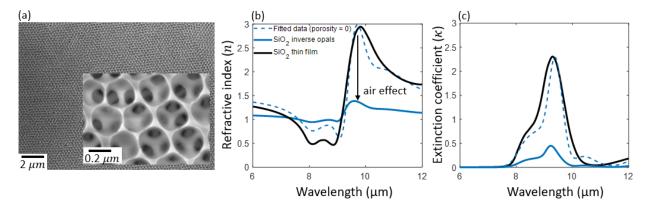


Figure 1) (a) Scanning electron microscope (SEM) image of the inverse opals (IO) used in this study, showing the nano-porous interconnected structure with a void diameter of 250 nm. The inset SEM image of the same sample, magnified $10\times$, shows the high porosity and interconnectivity the IO. **(b)** Real (n) and **(c)** imaginary (κ) parts of the complex refractive index of the inverse opal film (solid blue lines) along with the fitted values assuming no porosity (dashed blue lines), and bulk sputtered amorphous SiO_2 (black lines) [19], for wavelengths close to the vibrational resonances of SiO_2 . Optical properties of inverse opals are measured via variable-angle ellipsometry and fitted using the Bruggeman effective-medium theory [21].

Using the extracted refractive indices in Fig. 1(b, c) and the transfer-matrix method [32], [33] (See Sup. Info. 3), we calculated the optical impedance, Z_{IO} , of 2- and 4- μm thick IO film on a silicon substrate. Figure 2(a) shows the magnitude of the difference between Z_{IO} and the free-space impedance, Z_0 . We also calculated the impedance difference, $|Z_{ox} - Z_0|$, between Z_0 and a homogeneous silica film of the same thickness on the same silicon substrate for the two thicknesses of 2 and 4 μm (Fig. 2(a), dashed lines). In a portion of the mid-infrared spectral range, the combination of the large volume fraction of air inclusions and the presence of strong vibrational

resonances in silica results in a close match between the impedance of the IO structure and that of air; i.e., $|Z_{IO} - Z_0|$ approaches zero. We observed a large contrast between the $|Z_{ox} - Z_0|$ and $|Z_{IO} - Z_0|$, especially near the vibrational resonances.

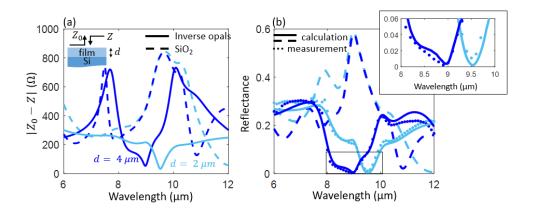


Figure 2) (a) The difference between the optical impedance of free space, $Z_0=377~\Omega$, and the calculated impedance (using the transfer-matrix method), of a structure comprising a layer of IOs (Z_{IO} , solid lines) or homogeneous SiO₂ (Z_{ox} , dashed lines) at two different thicknesses (2 and 4 μ m), on top of a semi-infinite silicon substrate. (b) Measured (dotted) and calculated (solid lines) reflectance of the IO films, as well as bulk SiO₂ (calculated, dashed lines), at near-normal incidence. The reflectance of the IO film is suppressed due to impedance matching with air for wavelengths of 8 to 10 μ m. The inset zooms in on the region of lowest reflectance.

To confirm the absorption around the resonances, we performed reflectance measurements using Fourier transform spectroscopy (FTS). Figure 2(b) shows the calculated (solid lines) and measured (dotted lines) values for the reflectance of the IO films at two thicknesses (2 μ m and 4 μ m) on top of a doped silicon substrate. The calculation was performed via the transfer-matrix method, using the optical properties extracted from ellipsometry [Fig. 1(b-c)]. The measurement was made using a Bruker Vertex 70 coupled to a Hyperion 2000 infrared microscope, with a numerical aperture of 0.4. As expected, the reflectance of the IO film becomes very small in the spectral region where the impedance is nearly matched to that of free space. In the same wavelength range, the reflectance of thin-film SiO₂ is quite large due to the large impedance mismatch.

We subsequently analyzed the angle-dependent reflectance of two IO films of different thicknesses (2 and 4 µm, as before) on silicon, for both s- and p- polarizations (Fig. 3). For both thicknesses, the reflectance decreases to nearly zero close to the spectral position of the vibrational resonances. Note that changing the film thickness affects the bandwidth of the suppressed reflectance region. Increasing thickness results in more light absorption in the spectral region where the IO film has a lower absorption coefficient. The optical impedance of the structure at oblique incidence is provided in *Sup. Info. 3*.

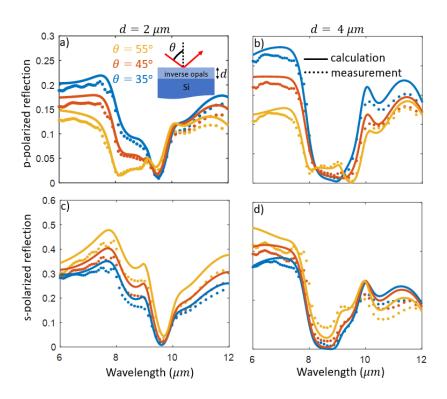


Figure 3) Calculated (solid line) and measured (dots) reflectance at oblique incidence ($\theta = 35^{\circ}$, 45° , and 55°) for p- and s-polarized light for two different thicknesses of the inverse opal films (d = 2 and $4 \mu m$).

The selective absorptivity of the IO structures implies that they can serve as a selective thermal emitters; this is encoded in Kirchhoff's law of thermal radiation, which equates the absorptivity at every wavelength (and angle and polarization) to the object's emissivity, assuming equilibrium conditions [11], [16]. Kirchhoff's law is also often used in the characterization of thermal emission from non-scattering samples, because it is frequently easier to infer absorptivity from reflectance and transmittance measurements than to directly measure thermal emission [32], [33]. For the samples in this work, however, it was difficult to apply Kirchhoff's law directly to our measurements because the semi-transparent silicon substrate was single-side polished, and the scattering from the back side is difficult to quantify.

To obtain accurate measurements of the emissivity, we performed direct emission measurements using FTS, as previously described in refs. [34], [35]. We collected the thermal emission from the samples at 150 °C and normalized the values to the emission from a laboratory blackbody reference at the same temperature. A forest of vertically aligned CNTs (height = 0.5 mm) on a silicon wafer was used as the reference. We calibrated the emissivity of the CNT forest by comparing measured emission to the well-characterized thermal emission from flat wafers of fused silica and sapphire. Detailed information regarding this measurement is provided in *Sup. Info.* 4.

Using the direct thermal-emission technique, we measured the polarized oblique-angle emissivity by rotating the sample and placing a polarizer directly in front of it; this was done for s- and p-polarizations at three oblique angles [Fig. 4(a, b)]. The accuracy of angle- and polarization-

resolved direct thermal-emission measurements were confirmed by performing similar measurements on flat wafers of fused silica and sapphire; see *Sup. Info. 5*.

For further confirmation of the measurements, we calculated the expected emissivity of this structure using Kirchhoff's law and the extracted optical properties of the IO films in Fig. 1(b-c). Two different emissivity spectra were calculated as presented in Fig. 4(a-b); one set of curves corresponds to the structure's emissivity assuming zero transmission through the Si substrate, (*i.e.*, absorptance A = 1 - R when $T_{Si} = 0$; dotted lines), and the other assumes a lossless substrate (*i.e.*, $A_{Si} = 0$, A = 1 - R - T; dashed lines). For the spectral regions where the IO film has relatively low loss ($\lambda < 8 \,\mu m$ or > 10 μm), these calculations provide upper and lower bounds on the actual emissivity.

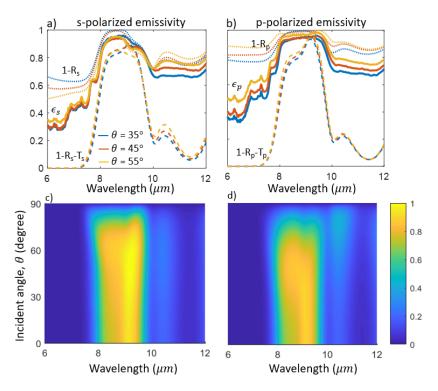


Figure 4) Experimental emissivity (solid lines) via direct-emission measurements at 150 °C for 4-µm-thick IO on silicon wafer at different incidence angles (θ = 0°, 35°, 45°, and 55°) for (**a**) s-polarized light and (**b**) p-polarized light, along with calculated upper (dotted lines) and lower bounds (dashed lines) on the emissivity in the spectral range where the IO film is low loss (λ < 8 µm or > 10 µm). In the spectral range where the IO film is low loss (λ < 8 µm or >10 µm), we expect a substantial contribution to the emissivity from the lossy silicon substrate. Calculated absorption (1 – transmission – reflection) within the film is shown versus wavelength and incident angle for (**c**) s polarization and (**d**) p polarization.

The large-area near-unity absorption at oblique incidence can be readily visualized using long-wave infrared ("thermal") imaging. Infrared-camera images typically attribute a pixel brightness to the intensity of detected thermal radiation from that pixel, assuming a constant emissivity for all pixels of the image. In Fig. 5(a), we show such infrared images of a silica glass slide (labeled

"silica" in the image) next to the IO sample measured in Fig. 4. We used a FLIR A325sc camera with a bandwidth of 7.5 to 13.0 μ m. To isolate the high-emissivity region of the IO identified in Fig. 4, we positioned a filter with a passband of 8.2 to 10.6 μ m in front of the camera. The infrared images with and without the filter can be seen in the bottom and top rows of Fig. 5, respectively, with the images taken from the normal direction, as well as for oblique angles of 35°, 45°, and 55°. These images demonstrate the large and broad-angle spectral selectivity of our selective thermal emitter. The "lines" of high apparent temperature seen along the bottom edges of the silica samples are due to roughness, which creates a gradient of refractive index, and thus enhances emissivity, similar to the effect for other porous structures; see *Sup. Info.* 6. Note that since our FLIR infrared camera and the readout software have a fixed built-in algorithm to detect the temperature using measured thermal radiation in the 8 to 14 μ m range, it is no longer possible to directly interpret the infrared image as a temperature map when the object is viewed through a bandpass filter. Instead, in Fig. 5 we report an "Apparent temperature", defined as the temperature reported by the camera software, without any adjustments made due to the presence of the filter.

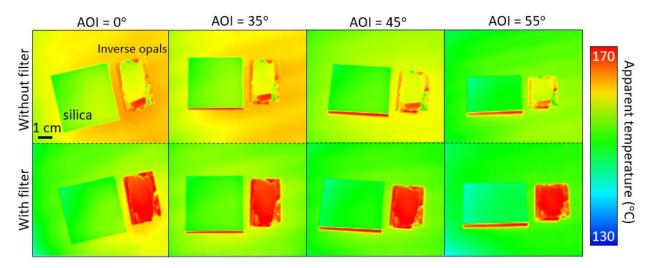


Figure 5) Mid-infrared images of our IO absorber and a reference silica glass slide at 150 °C, imaged at angles (AOI) of 0 to 55°, without (top) and with (bottom) a filter that selects the wavelength range corresponding to high absorptivity/emissivity of the sample (8.2 to 10.6 μ m). The close-to-unity emissivity of the IO absorber results in a large apparent temperature.

In conclusion, we demonstrated a large-area mid-infrared absorber/emitter based on a self-assembled silica inverse-opal (IO) metamaterial with a thickness less than half of the free-space wavelength. The device shows little angular and polarization dependence across its working wavelength of 8 to 10 μ m, maintains a greater than 80% absorption for incidence angles as large as 80°, and is stable up to at least ~900 °C. The broad-angle absorption is a consequence of impedance matching to the near-unity refractive index of the IO structure with considerable optical losses, resulting from the combination of mid-infrared vibrational resonance of the silica comprising the opal matrix and the large volume fraction of air inclusions. By utilizing alternative matrix materials with a different set of vibrational resonances and/or by depositing materials within

the IO voids, the self-assembly approach can enable large-area wide-angle absorbers and thermal emitters across the infrared range. Further functionality may be realized with full or partial fluid infiltration through the structure to achieve dynamic tunability, or for sensing or photo-thermal catalysis. Various applications may also benefit from the high degree of order achievable with IOs, including simultaneous optical effects at visible wavelengths.

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