Engineering Quantum States of Matter for Atomic Clocks in Shallow Optical Lattices

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We investigate the effects of stimulated scattering of optical lattice photons on atomic coherence times in a state-of-the art 87 Sr optical lattice clock. Such scattering processes are found to limit the achievable coherence times to less than 12 s (corresponding to a quality factor of 1×10^{16}), significantly shorter than the predicted 145(40) s lifetime of 87 Sr's excited clock state. We suggest that shallow, state-independent optical lattices with increased lattice constants can give rise to sufficiently small lattice photon scattering and motional dephasing rates as to enable coherence times on the order of the clock transition's natural lifetime. Not only should this scheme be compatible with the relatively high atomic density associated with Fermi-degenerate gases in three-dimensional optical lattices, but we anticipate that certain properties of various quantum states of matter—such as the localization of atoms in a Mott insulator—can be used to suppress dephasing due to tunneling.

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Owing to dramatic improvements in both the precision and accuracy of atomic spectroscopy over the last decade [1–3], there is growing interest in the use of atomic clocks as quantum sensors in tests of fundamental physics [4–8]. Recent demonstrations of spectroscopic techniques, which are immune to local oscillator noise, promise to dramatically improve the precision of such tests [9–12]. In the absence of local oscillator noise, frequency measurements of a single atom follow a binomial distribution and, for Ramsey spectroscopy [13], are spread about its true transition frequency ω_0 by an amount $(\omega_0 T)^{-1}$, given in fractional frequency units with T being the coherent evolution time. In the absence of entanglement, interrogation of a sample of N atoms with an experimental cycle time $T_{\rm cyc}$ results in a quantum projection noise (QPN) limit [14],

$$\sigma_{\rm QPN} = \frac{1}{\omega_0 T} \sqrt{\frac{T_{\rm cyc}}{N}}.$$
 (1)

That is, one wants to increase the interrogation time and use a larger number of atoms in order to reduce the measurement noise.

To date, the lowest reported QPN limit ($\sigma_{\text{QPN}} = 1.5 \times 10^{-17}/\sqrt{\text{Hz}}$) was achieved using a Fermi-degenerate gas of $N \approx 10^4$ ⁸⁷Sr ($\omega_0 \approx 2\pi \times 429$ THz) atoms loaded into the Mott-insulating regime of a three-dimensional (3D) optical lattice [12,15]. In these experiments, coherence times were found to be less than 12 s and presumed to be limited by Raman scattering of photons from the deep optical lattice [16,17]. While these scattering processes may be reduced by operating in a shallower optical potential, one then introduces site-to-site tunneling as an additional dephasing mechanism [18–20].

In this Letter, we discuss a solution that simultaneously addresses both the lattice photon scattering and tunneling induced dephasing problems in 3D optical lattice clocks: shallow optical lattices with increased lattice constants, a. We find that not only should the decreased kinetic energies in the ground band of such a lattice be sufficient to suppress motional dephasing in a single atom picture, but additionally, for a nuclear-spin polarized Fermi gas at half-filling, inter-electronic-orbital interactions should provide an additional mechanism for reducing motional dephasing rates. In such a system, atom numbers on the order of $N=10^5$ and coherent interrogation times up to T=140 s seem readily achievable and correspond to a QPN limit of $\sigma_{\rm QPN} < 10^{-19}/\sqrt{\rm Hz}$.

Before describing the details of our proposal, we build upon previous work which investigated trap depth dependent depopulation of the 5s5p 3P_0 excited clock state ($|e\rangle$) in 87 Sr one-dimensional optical lattices as a signature of the Raman scattering problem [16,17]. By leveraging the improved control over motional degrees of freedom [15] and imaging techniques [12] available in a Fermi-degenerate 3D optical lattice clock, we additionally investigate the corresponding loss of Ramsey fringe contrast.

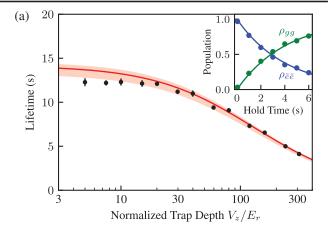
A spin-polarized degenerate fermi gas is created by evaporatively cooling atoms in an equal mixture of the $m_F = -5/2, ..., 9/2$ magnetic sublevels of the $5s^2$ 1S_0 electronic ground state ($|g\rangle$) before a focused laser beam, detuned from the 5s5p 3P_1 intercombination line, provides a state-dependent potential, removing nearly all but the $m_F = 9/2$ atoms from the trap. Approximately 2×10^3 atoms with a temperature of 20% of the Fermi temperature are then loaded from the running wave optical dipole trap

into a cubic optical lattice. Each arm (i=x, y, z) of the lattice is formed by a retroreflected laser at the magic wavelength (λ_{magic}) [21], and is characterized by a variable depth V_i and a lattice constant $a_0 = \lambda_{\text{magic}}/2 = 407$ nm. The i=z lattice arm is oriented along both gravity and an applied 0.5 mT magnetic bias field. We perform an additional step of spin purification by coherently driving $|g, m_F = 9/2\rangle \rightarrow |e, m_F = 9/2\rangle$ with $\lambda_{\text{clk}} = 698$ nm clock light, propagating along the i=x lattice axis, then removing all remaining $|g\rangle$ atoms by cycling on the $5s^2$ $^1S_0 \leftrightarrow 5s6p$ 1P_1 transition with resonant 461 nm light.

For the excited state lifetime measurement, we insert a variable hold time before a series of 5 μ s pulses of 461 nm light form an absorption image of the $|g\rangle$ atoms on a CCD camera, providing a count of the $|g\rangle$ atoms, N_g , while also removing the imaged atoms from the trap. We obtain a count of the remaining atoms, $N_{\bar{e}}$, by optically pumping $5s5p^3P_0$, $^3P_2 \rightarrow 5s5p^3P_1$ with light resonant on the $5s5p^3P_0$, $^3P_2 \leftrightarrow 5s6s^3S_1$ transitions at 679 nm and 707 nm. Atoms then rapidly decay to the ground state, via the 21 μ s lived $5s5p^3P_1$ [22], where they are subsequently imaged with 461 nm light. We note that this readout method counts not only atoms in $|e, m_F = 9/2\rangle$, but all atoms in the metastable $5s5p^3P_0$, 3P_2 manifold in the quantity $N_{\bar{e}}$. The decay of the excited population $\rho_{\bar{e}\,\bar{e}} = N_{\bar{e}}/(N_g + N_{\bar{e}})$ is then fit to extract a 1/e lifetime.

These lifetimes are measured for various lattice depths, V_z , ranging from $5E_r$ to $310E_r$, while fixing $V_x = 59(2)E_r$ and $V_v = 70(2)E_r$, where $E_r = h^2/8ma_0^2 \approx h \times 3.5 \text{ kHz}$ is the lattice photon recoil energy, h the Planck constant, and m the atomic mass. Figure 1(a) shows the trap depth dependence of the extracted lifetimes. We find the measured lifetimes to be significantly shorter than the predicted $\tau_0 = 145(40)$ s natural lifetime [23], yet largely consistent with numerical simulations with no free parameters (shaded red region) in which two-photon Raman transitions, stimulated by the lattice light, distribute atoms amongst the $5s5p^3P_I$ manifold where the atoms can then spontaneously decay to the ground state from $5s5p^3P_1$. The vacuum limited lifetime of atoms prepared in $|g\rangle$ is independently measured to be > 100 s. An energy level diagram depicting the Raman scattering processes, and the master equation used in the simulation can be found in Ref. [24].

Such scattering events are detrimental to clock operation as they destroy the coherence ρ_{eg} between the two clock states [32]. Using imaging spectroscopy [12,15], we observe this loss in coherence as a reduction in the Ramsey fringe contrast for increasing dark time, T. The contrast decay at a given lattice depth is then fit to extract a 1/e coherence time. The results of such measurements are shown in Fig. 1(b) for the same lattice conditions as in Fig. 1(a). The observed coherence times are found to scale proportionally to $V_{\rm tot}^{-1}$ ($V_{\rm tot} = \sum_i V_i$) for $V_z > 20E_r$, yet they fall significantly below the predicted decoherence rate due to Raman scattering (shaded red region) [24].



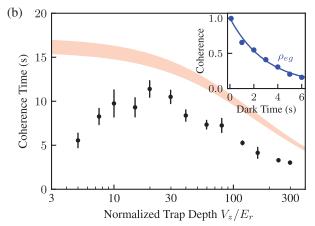


FIG. 1. Measured (a) lifetimes and (b) coherence times. Experimental data are shown in black points along with 1σ error bars. Results of the master equation simulation are shown as shaded red regions. The solid red line in (a) represents the fitted decay rate from Ref. [17].

This suggests that other, lattice depth dependent, decoherence mechanisms are present in the system. Rayleigh scattering is not expected to directly contribute as a dephasing mechanism since the scattering amplitudes are identical for both clock states in a magic wavelength trap [16,25]. However, both Raman and Rayleigh scattering processes can heat atoms out of the ground band of the lattice [33] at which point, we suspect, they are able to tunnel around and dephase through contact interactions.

For $V_z < 20E_r$, coherence times are seen deviate from the $V_{\rm tot.}^{-1}$ scaling and instead rapidly decay. This decay is accompanied by a loss in atom number which we attribute to significant tunneling rates along the i=z lattice and inelastic collisions [34]. This demonstrates the difficulty in overcoming the Raman scattering problem in conventional optical lattice clocks. One would like to operate in an optical trap shallow enough to make scattering induced decoherence rates comparable to the natural lifetime—one requires $V_i \lesssim 4E_r$ for $^{87}{\rm Sr}$ —but then one finds additional, tunneling enabled dephasing mechanisms due to the increased kinetic energy scale.

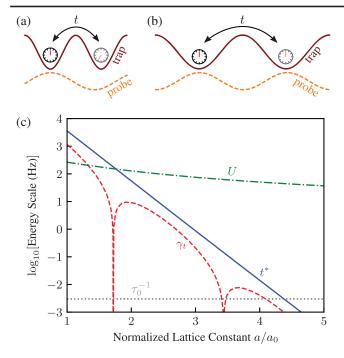


FIG. 2. (a) Motional dephasing in a conventional, $a/\lambda_{\rm clk}\approx 0.6$ lattice. An atom in an equal superposition of $|g\rangle$ and $|e\rangle$ is depicted as the face of a clock where the position of the hand reflects the relative phase between the atomic superposition and the local oscillator. Upon tunneling to an adjacent lattice site, the relative phase changes by an amount $\phi\approx 1.2\pi$. (b) Motional dephasing can be eliminated by matching the lattice constant to the probe wavelength. An atom then sees the same local oscillator phase at each lattice site. (c) Calculated motional dephasing rates (γ_t) , kinetic energies $(t^*=12t)$, and interaction energies (U) as a function of lattice spacing, a, in a $V=4E_r$ lattice. The horizontal grey line represents the inverse lifetime (τ_0^{-1}) of the strontium clock transition. Single particle motional effects are suppressed below the natural decay rate for $a\gtrsim 2~\mu{\rm m}$.

We address this issue in the following proposal. Hereafter, we assume a uniform lattice, $V_i = V$, and for the time being, a noninteracting gas. For a Ramsey type experiment in an inertial reference frame, tunneling at a rate t along the direction of the probe laser results in a loss in contrast of the spectroscopic signal according to $\rho_{eg} = |\mathcal{J}_0[4tT\sin(\phi/2)]|$, \mathcal{J}_0 being the zeroth order Bessel function of the first kind [20], and $\phi = 2\pi a/\lambda_{\rm clk}$, the site-to-site phase shift of the clock light where we now allow for a variable lattice constant, a, as depicted in Figs. 2(a) and 2(b). For the purpose of comparing different energy scales of the system, we define the argument of the Bessel function,

$$\gamma_t = 4t |\sin(\phi/2)|,\tag{2}$$

as the "motional dephasing rate." As a practical example, such a variable spacing lattice can be engineered, while restricting the wavelength of the trapping light to be magic by interfering the lattice beams at an arbitrary angle, θ ,

giving a spacing $a = \lambda_{\text{magic}}/|2\sin(\theta/2)|$ [35–37], or with an optical tweezer array [38].

Under the harmonic approximation, the tunneling rate for fixed V scales exponentially with a as [39]

$$\frac{t(a)}{t(a_0)} = \sqrt{\frac{a_0}{a}} \exp\left[\sqrt{\frac{V}{E_r}} \left(1 - \frac{a}{a_0}\right)\right]. \tag{3}$$

One can think of this intuitively as a change in the lattice constant rescaling the lattice recoil energy, $E_r \rightarrow (a_0/a)^2 E_r$, such that the lattice depth in units of the new recoil energy can be made quite large for modest increases in a/a_0 . Numerical values of γ_t and the total kinetic energy, $t^* = 12t$, for a $V = 4E_r$ lattice are shown in Fig. 2(c). For a sufficiently large lattice constant, the atomic limit $(t \rightarrow 0)$ is achieved where tunneling related effects can be neglected. We find that both γ_t and t^* are suppressed below τ_0^{-1} for lattice spacings $a \gtrsim 2~\mu m$.

Additionally, γ_t is found to sharply drop to zero upon matching the condition $a/\lambda_{\text{clk}} \mod 1 = 0$. These resonances can be understood in a momentum space picture where the clock photon recoil is matched to a reciprocal lattice vector and thus absorption or emission of a clock photon leaves each atom's motional state unchanged. In this case, for a nuclear-spin polarized gas at half filling, the system behaves as a band insulator throughout clock spectroscopy as the indistinguishability of all atoms is preserved. This scheme, however, requires an accuracy in θ beyond the 2×10^{-5} , and 2×10^{-2} levels for the $a/\lambda_{\rm clk} = 1$, 2 configurations, respectively. Throughout this range of parameters $(1 < a/a_0 < 5)$ the lattice band gap is greater than $h \times 2$ kHz, and the effective Rabi coupling is suppressed by no more than 60% of the bare Rabi coupling such that carrier resolved spectroscopy is easily achievable; linepulling effects from off-resonant excitation of motional sidebands can be suppressed below the 10^{-19} level for Rabi frequencies below 10 Hz, as shown in Fig. S4 [24].

Many-body effects arise through an on-site interaction energy U parametrized by the anti-symmetric inter-electronic-orbital s-wave scattering length, $a_{eg^-} = 69.1(0.9)a_B$ [40], where a_B is the Bohr radius. This energy scale decreases algebraically with an increasing lattice constant,

$$\frac{U(a)}{U(a_0)} = \left(\frac{a_0}{a}\right)^{3/2},\tag{4}$$

such that for sufficiently large lattice spacings, the system enters the Mott-insulating regime $(t^*/U \ll 1)$ [41,42]. Here, for a sufficiently cold gas at half-filling, the only available excitations below the energy gap U are of the order of the superexchange energy $J=4t^2/U$. Thus we expect, for a sufficiently weak probe pulse, the motional dephasing rates to be suppressed by a factor of t/U as

compared to the noninteracting case. Numerical values for U in a $V = 4E_r$ lattice are shown in Fig. 2(c).

We investigate these effects with a "toy model" consisting of a double well potential. We assign the following Hamiltonian in the rotating wave approximation,

$$H/\hbar = \sum_{x} \left(\frac{\Delta}{4} (n_{x,e} - n_{x,g}) + \frac{U}{2} n_{x,g} n_{x,e} + \frac{\Omega}{2} e^{i\phi_x} c_{x,e}^{\dagger} c_{x,g} \right) - t \sum_{\sigma} c_{\mathrm{L},\sigma}^{\dagger} c_{\mathrm{R},\sigma} + \text{H.c.} \quad (5)$$

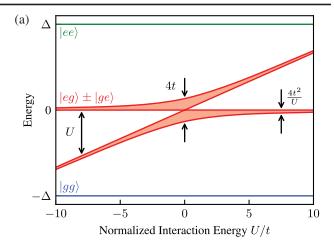
to such a system. Here $c_{x,\sigma}^{\dagger}$ ($c_{x,\sigma}$) creates (destroys) a fermion with internal state $\sigma \in \{g,e\}$ in well $x \in \{L,R\}$, $n_{x,\sigma} = c_{x,\sigma}^{\dagger} c_{x,\sigma}$, $\Delta = \omega - \omega_0$ is the difference between the frequency of the driving field ω from the atomic resonance, ω_0 , Ω is the Rabi coupling strength, and $\phi_x = 2\pi(a/\lambda_{\rm clk})\delta_{x,\rm R}$ is the site-dependent phase shift of the clock light, with $\delta_{i,j}$ being the Kronecker delta function. The two atom spectrum of this Hamiltonian with $\Omega = 0$ is shown in Fig. 3(a).

We simulate Ramsey spectroscopy of one and two atoms in the double well by numerically integrating the Schrödinger equation. A resonant ($\Delta=0$) $\pi/2$ pulse with $\Omega\gg t$ places each atom in an equal superposition of ground and excited electronic states. For $a/\lambda_{\rm clk} \bmod 1 \neq 0$, this pulse also changes the system's motional state. During field-free evolution ($\Omega=0$), the different motional states beat against each other causing a dephasing of the spectroscopic feature. We quantify this effect with the following relation,

$$\gamma = \sqrt{\langle H^2 \rangle - \langle H \rangle^2}.$$
 (6)

For a single atom, this quantity approximates the dephasing rate in an infinite-sized lattice, γ_t , falling off with an envelope proportional to t as shown in Fig. 3(b) (red dashed line). For two atoms, we observe that as one begins to resolve the interaction energy ($\Omega \ll U$) the dephasing rate becomes proportional to the superexchange energy, falling off with an envelope proportional to t^2/U as shown in Fig. 3(b) (solid blue line). While the exact numerical prefactor differs slightly from what one would get for an infinite lattice [43], the general conclusion is the same: the minimum lattice spacing such that $\gamma \tau_0 < 1$ is significantly relaxed as compared to the noninteracting case.

We have identified scattering of lattice photons as a dominant decoherence mechanism in a state-of-the-art 3D optical lattice clock and proposed a number of ways in which quantum materials may be engineered to overcome such limits. The improved clock stability associated with longer coherence times will directly enable new searches for time variation of fundamental constants and tests of general relativity on sub-mm length scales. Additionally, the shallow optical potentials described in this Letter will



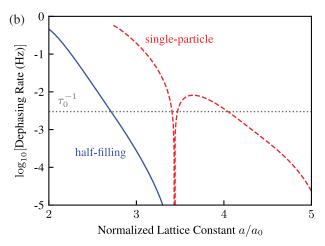


FIG. 3. (a) Energy spectrum of Eq. (5) at half-filling. States with zero, one, and two atoms in $|e\rangle$ are shown as blue, red, and green lines, respectively. The $|gg\rangle$ and $|ee\rangle$ states are noninteracting due to the Pauli exclusion principle. The $|eq\rangle \pm$ $|ge\rangle$ states are spread by twice the Bloch band width at U=0. Whereas in the Mott-insulating regime $(U/t \gg 1)$, an energy gap U opens up and a pair of weakly interacting states become spectroscopically resolvable. (b) Dephasing rates, as given by Eq. (6), for one (red dashed line) and two (solid blue line) atoms in a double well potential. The tunneling rates and interaction strengths as a function of lattice spacing are taken from Fig. 2(c) and inserted into the double well Hamiltonian with $\Omega/2\pi =$ 0.5 Hz. The curves are not plotted for $4t > \Omega$ where the analogy between the double well system and an infinite lattice breaks down as the discrete levels of the finite sized system become resolved.

help reduce systematic clock shifts related to the traps themselves, especially terms that are nonlinear in trap depth [44,45]. Future work will investigate the use of atomic collisions to create metrologically useful entanglement [46] and study collective radiative effects [47,48] for various lattice constants including the resonance condition in Fig. 2(b).

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- [1] A. D. Ludlow, T. Zelevinsky, G. K. Campbell, S. Blatt, M. M. Boyd, M. H. G. de Miranda, M. J. Martin, J. W. Thomsen, S. M. Foreman, J. Ye, T. M. Fortier, J. E. Stalnaker, S. A. Diddams, Y. Le Coq, Z. W. Barber, N. Poli, N. D. Lemke, K. M. Beck, and C. W. Oates, Sr lattice clock at 1 × 10⁻¹⁶ fractional uncertainty by remote optical evaluation with a Ca clock, Science 319, 1805 (2008).
- [2] B. J. Bloom, T. L. Nicholson, J. R. Williams, S. L. Campbell, M. Bishof, X. Zhang, W. Zhang, S. L. Bromley, and J. Ye, An optical lattice clock with accuracy and stability at the 10⁻¹⁸ level, Nature (London) 506, 71 (2014).
- [3] W. F. McGrew, X. Zhang, R. J. Fasano, S. A. Schäffer, K. Beloy, D. Nicolodi, R. C. Brown, N. Hinkley, G. Milani, M. Schioppo, T. H. Yoon, and A. D. Ludlow, Atomic clock performance enabling geodesy below the centimetre level, Nature (London) 564, 87 (2018).
- [4] S. Blatt, A. D. Ludlow, G. K. Campbell, J. W. Thomsen, T. Zelevinsky, M. M. Boyd, J. Ye, X. Baillard, M. Fouché, R. Le Targat, A. Brusch, P. Lemonde, M. Takamoto, F.-L. Hong, H. Katori, and V. V. Flambaum, New Limits on Coupling of Fundamental Constants to Gravity Using ⁸⁷Sr Optical Lattice Clocks, Phys. Rev. Lett. 100, 140801 (2008).
- [5] S. Kolkowitz, I. Pikovski, N. Langellier, M. D. Lukin, R. L. Walsworth, and J. Ye, Gravitational wave detection with optical lattice atomic clocks, Phys. Rev. D 94, 124043 (2016).
- [6] K. Van Tilburg, N. Leefer, L. Bougas, and D. Budker, Search for Ultralight Scalar Dark Matter with Atomic Spectroscopy, Phys. Rev. Lett. 115, 011802 (2015).
- [7] T. Pruttivarasin, M. Ramm, S. G. Porsev, I. I. Tupitsyn, M. S. Safronova, M. A. Hohensee, and H. Häffner, Michelson-Morley analogue for electrons using trapped ions to test Lorentz symmetry, Nature (London) 517, 592 (2015).
- [8] C. Sanner, N. Huntemann, R. Lange, C. Tamm, E. Peik, M. S. Safronova, and S. G. Porsev, Optical clock comparison for Lorentz symmetry testing, Nature (London) 567, 204 (2019).
- [9] C. W. Chou, D. B. Hume, M. J. Thorpe, D. J. Wineland, and T. Rosenband, Quantum Coherence between Two Atoms beyond $Q = 10^{15}$, Phys. Rev. Lett. **106**, 160801 (2011).
- [10] N. Nemitz, T. Ohkubo, M. Takamoto, I. Ushijima, M. Das, N. Ohmae, and H. Katori, Frequency ratio of Yb and Sr clocks with 5×10^{-17} uncertainty at 150 seconds averaging time, Nat. Photonics **10**, 258 (2016).
- [11] M. Schioppo, R. C. Brown, W. F. McGrew, N. Hinkley, R. J. Fasano, K. Beloy, T. H. Yoon, G. Milani, D. Nicolodi, J. A. Sherman, N. B. Phillips, C. W. Oates, and A. D. Ludlow,

- Ultrastable optical clock with two cold-atom ensembles, Nat. Photonics 11, 48 (2017).
- [12] G. E. Marti, R. B. Hutson, A. Goban, S. L. Campbell, N. Poli, and J. Ye, Imaging Optical Frequencies with 100 μ Hz Precision and 1.1 μ m Resolution, Phys. Rev. Lett. **120**, 103201 (2018).
- [13] *Molecular Beams*, edited by N. F. Ramsey (Oxford University Press, Oxford, 1956).
- [14] W. M. Itano, J. C. Bergquist, J. J. Bollinger, J. M. Gilligan, D. J. Heinzen, F. L. Moore, M. G. Raizen, and D. J. Wineland, Quantum projection noise: Population fluctuations in twolevel systems, Phys. Rev. A 47, 3554 (1993).
- [15] S. L. Campbell, R. B. Hutson, G. E. Marti, A. Goban, N. Darkwah Oppong, R. L. McNally, L. Sonderhouse, J. M. Robinson, W. Zhang, B. J. Bloom, and J. Ye, A Fermi-degenerate three-dimensional optical lattice clock, Science 358, 90 (2017).
- [16] M. Martin, Quantum metrology and many-body physics: Pushing the frontier of the optical lattice clock, Ph.D. thesis, University of Colorado Boulder, 2013.
- [17] S. Dörscher, R. Schwarz, A. Al-Masoudi, S. Falke, U. Sterr, and C. Lisdat, Lattice-induced photon scattering in an optical lattice clock, Phys. Rev. A 97, 063419 (2018).
- [18] P. Lemonde and P. Wolf, Optical lattice clock with atoms confined in a shallow trap, Phys. Rev. A 72, 033409 (2005).
- [19] S. Kolkowitz, S. L. Bromley, T. Bothwell, M. L. Wall, G. E. Marti, A. P. Koller, X. Zhang, A. M. Rey, and J. Ye, Spin-orbit-coupled fermions in an optical lattice clock, Nature (London) 542, 66 (2017).
- [20] S. L. Bromley, S. Kolkowitz, T. Bothwell, D. Kedar, A. Safavi-Naini, M. L. Wall, C. Salomon, A. M. Rey, and J. Ye, Dynamics of interacting fermions under spin-orbit coupling in an optical lattice clock, Nat. Phys. 14, 399 (2018).
- [21] J. Ye, H. J. Kimble, and H. Katori, Quantum state engineering and precision metrology using state-insensitive light traps, Science **320**, 1734 (2008).
- [22] T. L. Nicholson, S. L. Campbell, R. B. Hutson, G. E. Marti, B. J. Bloom, R. L. McNally, W. Zhang, M. D. Barrett, M. S. Safronova, G. F. Strouse, W. L. Tew, and J. Ye, Systematic evaluation of an atomic clock at 2×10^{-18} total uncertainty, Nat. Commun. **6**, 6896 (2015).
- [23] M. M. Boyd, T. Zelevinsky, A. D. Ludlow, S. Blatt, T. Zanon-Willette, S. M. Foreman, and J. Ye, Nuclear spin effects in optical lattice clocks, Phys. Rev. A 76, 022510 (2007).
- [24] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.123.123401 for a derivation of the master equation. This document includes Refs. [17,22,25–31].
- [25] H. Uys, M. J. Biercuk, A. P. VanDevender, C. Ospelkaus, D. Meiser, R. Ozeri, and J. J. Bollinger, Decoherence due to Elastic Rayleigh Scattering, Phys. Rev. Lett. 105, 200401 (2010).
- [26] T. Middelmann, S. Falke, C. Lisdat, and U. Sterr, High Accuracy Correction of Blackbody Radiation Shift in an Optical Lattice Clock, Phys. Rev. Lett. 109, 263004 (2012).
- [27] S. G. Porsev, M. S. Safronova, and C. W. Clark, Relativistic calculations of C_6 and C_8 coefficients for strontium dimers, Phys. Rev. A **90**, 052715 (2014).

- [28] M. S. Safronova, S. G. Porsev, U. I. Safronova, M. G. Kozlov, and C. W. Clark, Blackbody-radiation shift in the Sr optical atomic clock, Phys. Rev. A 87, 012509 (2013).
- [29] M. Yasuda and H. Katori, Lifetime Measurement of the ${}^{3}P_{2}$ Metastable State of Strontium Atoms, Phys. Rev. Lett. **92**, 153004 (2004).
- [30] M. Takamoto, H. Katori, S. I. Marmo, V. D. Ovsiannikov, and V. G. Pal'chikov, Prospects for Optical Clocks with a Blue-Detuned Lattice, Phys. Rev. Lett. 102, 063002 (2009).
- [31] H. Lignier, C. Sias, D. Ciampini, Y. Singh, A. Zenesini, O. Morsch, and E. Arimondo, Dynamical Control of Matter-Wave Tunneling in Periodic Potentials, Phys. Rev. Lett. 99, 220403 (2007).
- [32] C. Cohen-Tannoudji, J. Dupont-Roc, and G. Grynberg, Atom-Photon Interactions (John Wiley & Sons, New York, 1998).
- [33] F. Gerbier and Y. Castin, Heating rates for an atom in a fardetuned optical lattice, Phys. Rev. A 82, 013615 (2010).
- [34] M. Bishof, M. J. Martin, M. D. Swallows, C. Benko, Y. Lin, G. Quéméner, A. M. Rey, and J. Ye, Inelastic collisions and density-dependent excitation suppression in a ⁸⁷Sr optical lattice clock, Phys. Rev. A 84, 052716 (2011).
- [35] O. Morsch, J. H. Müller, M. Cristiani, D. Ciampini, and E. Arimondo, Bloch Oscillations and Mean-Field Effects of Bose-Einstein Condensates in 1D Optical Lattices, Phys. Rev. Lett. 87, 140402 (2001).
- [36] J. H. Huckans, I. B. Spielman, B. L. Tolra, W. D. Phillips, and J. V. Porto, Quantum and classical dynamics of a Bose-Einstein condensate in a large-period optical lattice, Phys. Rev. A **80**, 043609 (2009).
- [37] S. Al-Assam, R. A. Williams, and C. J. Foot, Ultracold atoms in an optical lattice with dynamically variable periodicity, Phys. Rev. A 82, 021604(R) (2010).
- [38] M. A. Norcia, A. W. Young, W. J. Eckner, E. Oelker, J. Ye, and A. M. Kaufman, Seconds-scale coherence on an optical clock transition in a tweezer array, arXiv:1904.10934.

- [39] I. Bloch, J. Dalibard, and W. Zwerger, Many-body physics with ultracold gases, Rev. Mod. Phys. 80, 885 (2008).
- [40] A. Goban, R. B. Hutson, G. E. Marti, S. L. Campbell, M. A. Perlin, P. A. Julienne, J. P. D'Incao, A. M. Rey, and J. Ye, Emergence of multi-body interactions in a fermionic lattice clock, Nature (London) 563, 369 (2018).
- [41] R. Jördens, N. Strohmaier, K. Günter, H. Moritz, and T. Esslinger, A Mott insulator of fermionic atoms in an optical lattice, Nature (London) 455, 204 (2008).
- [42] U. Schneider, L. Hackermüller, S. Will, T. Best, I. Bloch, T. A. Costi, R. W. Helmes, D. Rasch, and A. Rosch, Metallic and insulating phases of repulsively interacting fermions in a 3D optical lattice, Science **322**, 1520 (2008).
- [43] F. H. L. Essler, H. Frahm, F. Göhmann, A. Klümper, and V. E. Korepin, *The One-Dimensional Hubbard Model* (Cambridge University Press, Cambridge, England, 2005).
- [44] S. G. Porsev, M. S. Safronova, U. I. Safronova, and M. G. Kozlov, Multipolar Polarizabilities and Hyperpolarizabilities in the Sr Optical Lattice Clock, Phys. Rev. Lett. 120, 063204 (2018).
- [45] I. Ushijima, M. Takamoto, and H. Katori, Operational Magic Intensity for Sr Optical Lattice Clocks, Phys. Rev. Lett. 121, 263202 (2018).
- [46] P. He, M. Perlin, S. R. Muleady, R. J. Lewis-Swan, R. B. Hutson, J. Ye, and A. M. Rey, Engineering spin squeezing in a 3D optical lattice with interacting spin-orbit-coupled fermions, arXiv:1904.07866.
- [47] D. E. Chang, J. Ye, and M. D. Lukin, Controlling dipole-dipole frequency shifts in a lattice-based optical atomic clock, Phys. Rev. A **69**, 023810 (2004).
- [48] S. L. Bromley, B. Zhu, M. Bishof, X. Zhang, T. Bothwell, J. Schachenmayer, T. L. Nicholson, R. Kaiser, S. F. Yelin, M. D. Lukin, A. M. Rey, and J. Ye, Collective atomic scattering and motional effects in a dense coherent medium, Nat. Commun. 7, 11039 (2016).