Jointly Optimized 3D Drone Mounted Base Station Deployment and User Association in Drone Assisted Mobile Access Networks

Xiang Sun, Member, IEEE, Nirwan Ansari, Fellow, IEEE, and Rafael Fierro, Senior Member, IEEE

Abstract—In drone assisted mobile networks, a drone mounted base station (DBS) is deployed over a hotspot area to help user equipments (UEs) download their traffic from the macro base station (MBS), thus improving the throughput and spectrum efficiency (SE) of the UEs. Finding the optimal 3D position of the DBS to maximize the overall SE of the UEs in the hotspot area is challenging because the 3D DBS placement and user association problems are coupled together. In this paper, we formulate the problem of jointly optimizing the 3D DBS placement and user association to maximize the overall SE in the context of drone assisted mobile networks. The spectrum efficiency aware DBS placement and user association (STAR) algorithm is designed to decompose the original problem into two subproblems, i.e., user association and DBS placement, and to iteratively solve the two subproblems until the overall SE of the hotspot area cannot be improved further. The performance of STAR is demonstrated via extensive simulations.

Index Terms—Drone base station, spectral efficiency, user association, deployment, drone assisted mobile networks.

I. INTRODUCTION

Owing to quick and flexible deployment, drones have been widely used in various applications, such as public safety [1], disaster relief [2]–[7], content caching [8], and location-based services [9]. In drone assisted mobile access networks, a drone mounted base station (DBS) can be deployed over a hotspot area, which may appear sporadically, to speed up the content delivery rate of users in the hotspot area [10]. For example, a new hotspot might arise after an accident owing to an auto accident, when mobile users begin to stress the access point by downloading and watching related news content. Deploying a DBS over a hotspot area could significantly improve the network performance in terms of throughput or spectrum efficiency (SE) of user equipments (UEs) in the hotspot area [11]–[13]. Specifically, Fig. 1 shows the drone assisted mobile access network architecture, where a DBS is deployed over a hotspot area, and so all the UEs can download their requested contents from their macro base station (MBS) via the DBS, which acts as a relay node to receive data from the MBS via the wireless backhaul link and transmit data to the corresponding UEs via the wireless access links. Here, the DBS is operated in the out-of-band mode [14], [15]. That is, the frequency band of the backhaul link is different from the frequency band of the access links, thus avoiding the interference between the access link and the backhaul link. Here, free space optical (FSO) communications is applied as the wireless backhaul solution, and the traditional RF communications is used as the wireless access solution. Note that the data rate achieved by the FSO communications is much higher than the RF communications [16], [17], and so we assume that the bottleneck of transmitting data from the MBS to UEs via the DBS is the wireless access links. Then, the objective of the drone assisted mobile access network is to maximize the overall throughput of the wireless access links between the DBS/MBS and the UEs in the hotspot by determining the 3D position of the DBS. Note that the overall throughput of the UEs in the hotspot area depends on not only the SE between the DBS and the UEs but also the amount of bandwidth allocated to the UEs, where the overall SE is determined by the DBS placement method, and the amount of bandwidth assigned to the UEs depends on the bandwidth allocation method. The DBS placement and bandwidth allocation problem cannot be jointly optimized/solved because they are operating under different time scales. That is, in the LTE network setup, bandwidth allocation is conducted in each millisecond [18]; yet, it is impossible and unnecessary to adjust the 3D location of a DBS in each
millisecond. In this paper, we are focusing on the DBS placement problem to maximize the overall SE in the hotspot area. In fact, increasing the overall SE potentially increases the overall throughput for a given bandwidth allocation method.

The hotspot area is discretized into a number of small locations with the same size. The SE of a location is defined as the number of bits being downloaded from the DBS/MBS to the UEs in the location per second per Hertz, and thus the overall SE of the hotspot refers to the sum of the SEs of the locations in the hotspot area. Finding the optimal position of the DBS to maximize the overall SE of a hotspot area is challenging because DBS placement and user association are coupled together. Here, the user association problem is to determine whether a location is associated with the DBS or the MBS.\(^1\) The optimal user association that maximizes the overall SE of the hotspot area is to associate a location with the DBS or the MBS, depending on which incurs a larger SE. That is, as shown in Fig. 1, if the SE from the DBS to a location is higher than that from the MBS to the location, then the location is associated with the DBS, and vice versa. The DBS placement determines the user association since a different DBS placement results in a different SE between a location and the DBS, and thus leads to a different user association. On the other hand, the user association determines the DBS placement. DBS placement can only affect the SEs of the locations associated with the DBS, and so the optimal DBS placement is to maximize the overall SEs of the locations associated with the DBS. Thus, a different user association of the DBS may incur a different optimal DBS placement. The motivation of the paper is to jointly optimize the 3D DBS placement and user association in order to maximize the overall SE of the hotspot area. The contributions of the paper are summarized as follows:

1. We illustrate the motivation of jointly optimizing 3D DBS placement and user association.
2. We formulate the problem of jointly optimizing 3D DBS placement and user association to maximize the overall SE of the hotspot area. We develop the spectrum efficiency aware DBS placement and user association (STAR) algorithm to efficiently solve the problem.
3. The performance of STAR is verified via simulations.

The rest of the paper is organized as follows. In Section VI, we briefly review the related works. In Section III, we introduce the probabilistic pathloss model and derive the related SE model. Based on these models, we formulate the joint 3D DBS placement and user association optimization problem. In Section IV, we design the STAR algorithm to solve the problem. In Section V, we present and analyze the simulation results. The conclusion is presented in Section VII.

II. RELATED WORKS

Applying DBSs to assist mobile access networks to improve the quality of services (QoS) of UEs has been proposed by many works [10], [19]–[21], and how to place the DBSs in the 3D space to maximize the performance of the mobile access networks is a big challenge. Al-Hourani et al. [22] proposed a method to find the optimal altitude of a DBS in order to maximize the coverage of the DBS. They considered the wireless access link between a DBS and a UE as a probabilistic line-of-sight (LoS) link. That is, a higher altitude of the DBS incurs a higher probability of LoS between the UE and the DBS, thus potentially reducing the pathloss between the UE and the DBS. On the other hand, a higher altitude of the DBS incurs a longer distance between the UE and the DBS, thus potentially increasing the pathloss between the UE and the DBS. Hence, they derived the optimal altitude of the DBS to maximize the horizontal distance between the DBS and the UE while guaranteeing the pathloss between the DBS and the UE to be less than a predefined threshold (i.e., the maximum pathloss that allows the UE to successfully receive the signal from the DBS). Alzenad et al. [23] proposed a 3D DBS placement method aiming to maximize the number of covered UEs by using the minimum transmission power. The 3D DBS placement problem is decoupled into the vertical dimension and horizontal dimension DBS placement problems, where the horizontal dimension DBS placement is modeled as the circle placement problem to determine the latitude and longitude of the DBS in order to maximize the number of UEs covered by the DBS. Meanwhile, the vertical dimension DBS placement is modeled as the smallest enclosing circle problem to optimize the altitude of the DBS in order to minimize the transmission power of the DBS while guaranteeing that the UEs, which were previously covered by the DBS in the horizontal dimension DBS placement, can still be covered by the DBS. Similarly, Yaliniz et al. [24] proposed a 3D DBS placement method to maximize the number of the UEs served by the DBS while meeting the QoS of the UEs. Here, the QoS of a UE is measured as the minimum signal-to-noise ratio (SNR). Azari et al. [25] derived an optimal altitude of the DBS in order to maximize the coverage of the DBS while guaranteeing the minimum outage performance, which is defined as the outage probability of the covered UE (i.e., the probability of the UE's instantaneous SNR less than the SNR threshold) larger than a predefined value.

Many works have investigated the deployment of multiple DBSs over a given area. Ahmed et al. [26] designed an algorithm to deploy the minimum number of DBSs to cover more UEs. The intuition of the algorithm is to find the position of a DBS that can associate with the most number of UEs that could not be covered by the previously deployed DBSs. The algorithm terminates once all the UEs have been covered by the deployed DBSs. Given the number of available DBSs and the locations of BSs in a hotspot area, Savkin and Huang [27] designed a distributed algorithm to determine the horizontal locations of the DBSs such that the distances between UEs and their DBSs are minimized, and the DBSs are able to communicate with at least one BS in the hotspot area. By considering the limited power supply of drones, Huang et al. [28] considered the scenario in which DBSs have to fly to nearby charging stations after hovering in a certain time period to serve UEs. Given the number of available DBSs, they derived a multiple-DBS placement solution to determine the horizontal locations of these DBSs that maximizes the number of served UEs in a given area subject to the constraint that all
the DBSs have enough energy to hover at least a predefined time period and fly to the nearest charging station for charging their batteries. Under the same scenario, they proposed another 2D DBS placement method to serve more UEs and generate less interference [29] among DBSs. Lyu et al. [30] considered the scenario with no available ground BSs in a given area, and so DBSs have to connect to the core network via satellites. Meanwhile, they assumed that the link between a DBS and a UE is LoS, the altitudes of the DBSs are fixed, and all the DBSs have the same coverage size. They derived a 2D DBS placement algorithm to minimize the number of required DBSs, while guaranteeing every UE in the area to be covered by at least one DBS.

In drone assisted mobile access networks, a UE can either be associated with the DBS or the MBS. Thus, jointly optimizing the user association and DBS placement, which is considered by previous works, can potentially improve the performance of the mobile access network. Our previous works [13], [31] focused on the same topic. In [13], we designed a latency aware DBS placement method to jointly optimize the horizontal location of the DBS and the user association such that the traffic loads of the two base stations are balanced. Yet, the altitude of the DBS is considered to be fixed, and thus not optimized. In [31], we designed a SE aware DBS placement and user association algorithm to jointly optimize the altitude of the DBS and the user association in order to maximize the SE of the hotspot area. However, the horizontal position of the DBS is always at the center of the hotspot, and so is not optimized. Esrafilian and Gesbert [32] designed a joint user association and DBS placement problem to maximize the SE of the worst UE in the area in the context of uplink communications. However, maximizing the SE of the worst UE is not equivalent to maximizing the overall SE of the UEs in the area. We will provide the performance comparison via extensive simulations in Section V.

III. SYSTEM MODEL

A hotspot area is discretized into a number of small locations with the same size. Denote \( I \) as the set of these locations, each indexed by \( i \). Denote \( h \) as the altitude of the DBS. Meanwhile, let \( l_{it} \) be the horizontal distance between location \( i \) and location \( i' \), where \( i, i' \in I \). Thus, the horizontal distance between the DBS and the UEs in location \( i \) is \( l_i = \sum_{i \in I} x_{i} l_{it} \), where \( x_{i} \) is a binary variable to indicate whether the DBS is deployed over location \( i' \) (i.e., \( x_{i} = 1 \)) or not (i.e., \( x_{i} = 0 \)). Hence, the 3D distance between the DBS and the UEs in location \( i \) can be expressed as

\[
d_i = \sqrt{l_i^2 + h^2} = \sqrt{\sum_{i \in I} x_{i} l_{it}^2 + h^2}.
\]

A. Pathloss Model Between the DBS and a Location

The wireless propagation channel between the DBS and the UEs in location \( i \) can be divided into two scenarios, i.e., the links between the DBS and the UEs in location \( i \) with line-of-sight (LoS) connections and those with non-line-of-sight (NLoS) connections [22], [33], [34]. In the NLoS scenario, UEs can still communicate with the DBS, but suffer from much stronger reflections and diffractions [35], [36]. The probability of having LoS between the DBS and the UEs in location \( i \) can be modeled as [22]

\[
\rho_i = \frac{1}{1 + \alpha e^{-\beta(h_i - \alpha)}}
\]

\[
= \frac{1}{1 + \alpha e^{-\beta \left( \frac{\pi}{4} \arctan \left( \frac{h}{\sum_{i \in I} x_{i} l_{it}^2} \right) - \alpha \right)}},
\]

where \( \theta_i \) (in degrees) is the elevation angle between the DBS and location \( i \), and \( \alpha \) and \( \beta \) are the environmental parameters determined by the environment of the hotspot area (e.g., rural, urban, etc.). Thus, the average pathloss (in dB) between the DBS and the UEs in location \( i \) can be estimated as [37], [38]

\[
\eta_i = 20 \log_{10} \left( \frac{4 \pi f_d d_i}{c} \right) + \rho_i \xi_i^{\text{los}} + (1 - \rho_i) \xi_i^{\text{nlos}}.
\]

Here, \( 20 \log_{10} \left( \frac{4 \pi f_d d_i}{c} \right) \) indicates the free space pathloss (where \( f_c \) is the carrier frequency and \( d_i \) is the 3D distance between the DBS and location \( i \)) and \( \rho_i \xi_i^{\text{los}} + (1 - \rho_i) \xi_i^{\text{nlos}} \) is the average additional pathloss (where \( \xi_i^{\text{los}} \) and \( \xi_i^{\text{nlos}} \) are the average additional pathloss for LoS and NLoS scenario, respectively) between the DBS and the UEs in location \( i \). Here, \( \xi_i^{\text{nlos}} < \xi_i^{\text{los}} \).

B. Spectrum Efficiency Model

The UEs in location \( i \) can be associated with either the MBS or the DBS in downloading their traffic. However, associating with different base stations may incur different SEs. Here, we provide two models to estimate the SEs of enabling the UEs to download data from the MBS and the DBS, respectively.

1) Spectrum Efficiency Between the DBS and a Location: Denote \( g_{i}^{d} \) as the channel gain from the DBS to the UEs in location \( i \). Assume that the pathloss is the major factor to determine the channel gain between the DBS and the UEs in location \( i \) (i.e., shadowing and fading effects are not considered). Thus, the channel gain \( g_{i}^{d} \) can be estimated by \( g_{i}^{d} = 10^{-\eta_i/10} \). Consequently, the SE of transmitting data from the DBS to the UEs in location \( i \) can be obtained by

\[
\varphi_i^{d} = \log_2 \left( 1 + \frac{p_d^{d} 10^{-\eta_i/10}}{\sigma^2} \right),
\]

where \( p_d^{d} \) is the transmission power of the DBS and \( \sigma^2 \) denotes the noise power level.

2) Spectrum Efficiency Between the MBS and a Location: Similarly, the SE of transmitting data from the MBS to the UEs in location \( i \) can be obtained by

\[
\varphi_i^{m} = \log_2 \left( 1 + \frac{p_m^{m} 10^{-\eta_i^{m}/10}}{\sigma^2} \right),
\]

where \( p_m^{m} \) is the transmission power of the MBS and \( \eta_i^{m} \) is the pathloss from the MBS to the UEs in location \( i \).

C. Problem Formulation

In drone assisted mobile access networks, a DBS is placed in a hotspot area \( I \) to help the MBS in delivering traffic to the UEs...
in the hotspot. The objective is to maximize the sum of SEs of all the locations, i.e.,

\[
P_0 : \arg \max_{x_i, y_i} \sum_{t \in \mathcal{X}} w_i \left( y_i \varphi_i^d + (1 - y_i) \varphi_i^m \right) \tag{6}
\]

s.t. \[
\sum_{t \in \mathcal{X}} x_t = 1, \tag{7}
\]
\[
h_{\min} \leq h \leq h_{\max}, \quad \forall i \in \mathcal{I}, x_{i}, y_{i} \in \{0, 1\}, \tag{8}
\]

where \( y_{i} \) is a binary variable to indicate whether location \( i \) is associated with the DBS (i.e., \( y_{i} = 1 \)) or not (i.e., \( y_{i} = 0 \)) and \( w_{i} \) is the weight of location \( i \). Here, the weight of location \( i \) can be defined as the number of UEs in location \( i \) divided by the total number of UEs in the hotspot area. In order to meet the objective of \( P_0 \), the DBS placement is in favor of increasing the SEs of locations having larger values of weight [28], [29].

Constraint (7) indicates that the DBS should be placed over a location within the hotspot area. Constraint (8) implies that the altitude of the DBS should be between \( h_{\min} \) and \( h_{\max} \), which are defined as the minimum and maximum altitude attainable by the DBS, respectively.

IV. SPECTRUM EFFICIENCY AWARE DBS PLACEMENT AND USER ASSOCIATION

We design a spectrum efficiency aware DBS placement and user association (STAR) algorithm to efficiently solve the above problem. The basic idea of STAR is to decompose \( P_0 \) into two subproblems, i.e., user association and DBS placement, and iteratively solve the two subproblems until the total SE of the hotspot area cannot be further improved.

A. User Association

If the DBS placement is given, \( P_0 \) can be converted into

\[
\arg \max_{y_i} \sum_{t \in \mathcal{X}} w_i \left( \varphi_i^d - \varphi_i^m \right) y_i + \sum_{t \in \mathcal{X}} w_i \varphi_i^m
\]

s.t. \[
\forall i \in \mathcal{I}, y_i \in \{0, 1\}.
\]

The optimal user association, i.e., the optimal value of \( y_i \), to maximize the objective function can be easily derived, i.e.,

\[
y_i^* = \begin{cases} 
1, & \varphi_i^d > \varphi_i^m \\
0, & \varphi_i^d \leq \varphi_i^m.
\end{cases} \tag{10}
\]

B. DBS Placement

Once the user association is updated, the original problem \( P_0 \) can be converted into

\[
P_1 : \arg \max_{x_i, h} \sum_{t \in \mathcal{A}} w_i \varphi_i^d \\
\text{s.t.} \quad \text{Constraint (7), (8), and (9)}, \tag{11}
\]

where \( \mathcal{A} \) is the set of locations associated with the DBS, i.e., \( \mathcal{A} = \{ i \in \mathcal{I} | y_i = 1 \} \). The physical meaning of \( P_1 \) is to find the optimal 3D placement of the DBS such that the total SEs of the locations associated with the DBS is maximized.

Note that \( \varphi_i^d = \log_2 \left( 1 + \frac{p_i^{\text{tot}} \eta_i^d}{\sigma_i^2} \right) \) (i.e., Eq. (4)). If \( p_i^{\text{tot}} \gg \sigma_i^2 \), we have

\[
\varphi_i^d = \log_2 \left( \frac{p_i^{\text{tot}} \eta_i^d}{\sigma_i^2} \right). \tag{12}
\]

Plugging Eq. (12) into the objective of \( P_1 \), we have

\[
\arg \max_{x_i, h} \sum_{t \in \mathcal{A}} w_i \log_2 \left( \frac{p_i^{\text{tot}} \eta_i^d}{\sigma_i^2} \right) \\
\leftrightarrow \arg \max_{x_i, h} \sum_{t \in \mathcal{A}} w_i \eta_i^d \\
\Rightarrow \arg \min_{x_i, h} \sum_{t \in \mathcal{A}} w_i \eta_i^d, \tag{13}
\]

where \( \leftrightarrow \) means that the two expressions are equivalent. Eq. (13) implies that the objective of \( P_1 \) is equivalent to minimizing the total pathloss between the DBS and the locations associated with the DBS. Plugging Eq. (3) and Eq. (1) into Eq. (13), the objective function of \( P_1 \) can be converted into

\[
\arg \min_{x_i, h} \sum_{t \in \mathcal{A}} w_i \left( 20 \log_{10} \left( \frac{4\pi f_c \sqrt{\sum_{t \in \mathcal{X}} x_t^2 h_i^2 + h^2}}{c} \right) \\
+ \rho_i \xi_i^{\text{los}} + (1 - \rho_i) \xi_i^{\text{nlos}} \right) \\
\Rightarrow \arg \min_{x_i, h} \sum_{t \in \mathcal{A}} w_i \left( \rho_i (\xi_i^{\text{nlos}} - \xi_i^{\text{los}}) \\
- 20 \log_{10} \left( \frac{\sum_{t \in \mathcal{X}} x_t^2 h_i^2}{\sum_{t \in \mathcal{X}} x_t^2 + h^2} \right) \right) \\
+ \sum_{t \in \mathcal{A}} \left( 20 w_i \log_{10} \left( \sum_{t \in \mathcal{X}} x_t^2 \right) \right). \tag{14}
\]

The objective function (i.e., Eq. (14)) comprises two parts, the first part is determined by both the altitude (i.e., \( h \)) and the horizontal location (i.e., \( x_i \)) of the DBS; however, the second part is only determined by the horizontal location of the DBS. The intution of the DBS placement algorithm is to first determine the horizontal location of the DBS by minimizing the second part of the objective function, i.e.,

\[
P_2 : \arg \min_{x_i} \sum_{t \in \mathcal{A}} \left( 20 w_i \log_{10} \left( \sum_{t \in \mathcal{X}} x_t^2 \right) \right) \\
\text{s.t.} \quad \sum_{t \in \mathcal{X}} x_t = 1, \\
\forall i \in \mathcal{I}, x_i \in \{0, 1\}.
\]

After determining the horizontal location of the DBS (by solving \( P_2 \)), the optimal altitude of the DBS is calculated by minimizing
the first part of the objective function, i.e.,

\[ P3 : \]

\[
\begin{align*}
\arg \min_h \sum_{i \in A} u_i \times \left( \rho_i (\xi_{los} - \xi_{nilos}) - 20 \log_{10} \left( \frac{\sum_{v \in \mathbb{Z}} x_{iv} l_{iv}^2 + h^2}{\sqrt{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}^2 + h^2}} \right) \right)
\end{align*}
\]

s.t. \( h_{\text{min}} \leq h \leq h_{\text{max}} \),

where \( x_{iv}^* \) is the optimal solution of \( P2 \).

1) **Horizontal Location of the DBS:** As mentioned before, the horizontal location of the DBS is to derive the optimal solution of \( P2 \). Here, \( P2 \) can be transformed into

\[
\begin{align*}
\arg \min_{x_{i'}} \log_{10} \left( \prod_{v \in \mathbb{Z}} \left( \sum_{v \in X} x_{iv} l_{iv}^{w_i} \right)^{u_i} \right)
\end{align*}
\]

\[
\begin{align*}
\Leftrightarrow \arg \min_{x_{i'}} \sum_{v \in \mathbb{Z}} \left( x_{i'} \prod_{v \in \mathbb{Z}} (l_{iv}^{w_i})^{u_i} \right)
\end{align*}
\]

s.t. \[ \sum_{v \in \mathbb{Z}} x_{iv} = 1, \quad \forall v' \in \mathbb{Z}, \quad x_{iv} \in \{0, 1\}. \]

It is easy to derive the optimal solution of the transformed problem, i.e.,

\[ x_{i'v}^* = \begin{cases} 1, & i' = i^*, \\ 0, & \text{otherwise}. \end{cases} \]  \hspace{1cm} (15)

where \( i^* \) is the location such that the products of the distances between the location and other locations in \( A \) is the minimum, i.e., \( i^* = \arg \min_{i' \in \mathbb{Z}} \{ \prod_{v \in \mathbb{Z}} (l_{i'v})^{w_i} \} \).

2) **Altitude of the DBS:** The optimal altitude of the DBS can be obtained by solving \( P3 \). However, it is non-trivial to solve \( P3 \) since the objective function is neither convex nor concave. Here, we apply the Projected Gradient Descent method \([39]\) to find the local optimal solution of \( P3 \). The basic idea of applying Projected Gradient Descent to find the local optimal solution of \( h \) is to iteratively move the value of \( h \) in the direction of steepest descent, which is defined by the negative of the gradient of the objective function in \( P3 \). Specifically, define \( f \) as the objective function of \( P3 \), i.e.,

\[ f(h) = \sum_{i \in A} w_i \times \left( \rho_i (\xi_{los} - \xi_{nilos}) - 20 \log_{10} \left( \frac{\sum_{v \in \mathbb{Z}} x_{iv} l_{iv}^2 + h^2}{\sqrt{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}^2 + h^2}} \right) \right) \]

\[ \times \left( \rho_i (\xi_{los} - \xi_{nilos}) - 20 \log_{10} \left( \frac{\sum_{v \in \mathbb{Z}} x_{iv} l_{iv}^2 + h^2}{\sqrt{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}^2 + h^2}} \right) \right). \]  \hspace{1cm} (16)

\[ \begin{align*}
\nabla f(h) &= \sum_{i \in A} u_i \left( \frac{180}{\pi} \beta \times \left( \xi_{los} - \xi_{nilos} \right) e^{-\beta \left( \frac{\pi}{180} \arctan \left( \frac{h}{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}} \right) - \alpha \right)} \times \frac{\sum_{v \in \mathbb{Z}} x_{iv} l_{iv}^{w_i}}{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}^{w_i} + h^2} \right) + \frac{20}{\ln 10} \frac{h}{\sum_{v \in \mathbb{Z}} x_{iv}^2 l_{iv}^{w_i} + h^2} \right) \right) \end{align*}
\]

So, the gradient of \( f \) with respect to \( h \) is expressed in Eq. (17), shown at the bottom of this page.\(^2\) Thus, the steps of the Projected Gradient Descent method are described as follows:

1) Pick an initial value of \( h \), e.g., \( h^{(0)} = h_{\text{min}} + \frac{h_{\text{max}}}{2} \).

2) For each iteration \( k (k > 0) \), update the value of \( h \), i.e.,

\[ h^{(k+1)} = h^{(k)} - \delta^{(k)} \nabla f \left( h^{(k)} \right), \]  \hspace{1cm} (18)

where \( h^{(k)} \) and \( h^{(k+1)} \) are the value of \( h \) in iteration \( k \) and \( k + 1 \), respectively, \( \nabla f(h^{(k)}) \) is the value of the gradient of \( f \) at point \( h = h^{(k)} \), and \( \delta^{(k)} \) is the step size in iteration \( k \) (where \( k > 0 \)), which is calculated based on the Barzilai-Borwein method \([40]\), i.e.,

\[ \delta^{(k)} = \frac{h^{(k)} - h^{(k-1)}}{\nabla f \left( h^{(k)} \right) - \nabla f \left( h^{(k-1)} \right)}. \]  \hspace{1cm} (19)

3) Project the value of \( h^{(k+1)} \) into the feasible set, i.e.,

\[ h^{(k+1)} = \begin{cases} h^{(k+1)}, & h_{\text{min}} \leq h \leq h_{\text{max}}. \\ h_{\text{min}}, & h < h_{\text{min}}. \\ h_{\text{max}}, & h > h_{\text{max}}. \end{cases} \]

4) The iteration continues until

\[ \left| f \left( h^{(k+1)} \right) - f \left( h^{(k)} \right) \right| \leq \varepsilon, \]  \hspace{1cm} (21)

where \( \varepsilon \) is a predefined threshold.

The algorithm of applying Projected Gradient Descent to derive the optimal altitude of the DBS, denoted as \( \text{PGD}(x_{iv}^*) \), is summarized in Algorithm 1.

\( ^2 \)Note that \( \forall h \in [h_{\text{min}}, h_{\text{max}}], \nabla f(h) \) always exist as long as at least one location is associated with the DBS, i.e., \( \sum_{v \in \mathbb{Z}} x_{iv}^2 \geq 1 \).
Algorithm 2: STAR.

1: \( \forall i \in \mathcal{I}, y_i = 1 \) (i.e., \( \mathcal{A} = \mathcal{I} \)).
2: Initialize the horizontal location of the DBS \( x_i^h \) based on Eq. (15).
3: Initialize the altitude of the DBS \( h^* = \text{PGD}(x_i^h) \).
4: According to the calculated 3D position of the DBS, update \( y_i = 1 \) based on Eq. (10).
5: Update \( \mathcal{A} \), where \( \mathcal{A} = \{ i \in \mathcal{I} : y_i = 1 \} \).
6: Calculate the SE of the hotspot area \( \varphi_{\text{new}}(x_i^h, y_i, h^*) \).
7: do
8: \( \varphi_{\text{old}} = \varphi_{\text{new}} \).
9: Update \( x_i^h \) based on Eq. (15).
10: Update \( h = \text{PGD}(x_i^h) \).
11: Update \( y_i \) based on Eq. (10).
12: Update \( \mathcal{A} \), where \( \mathcal{A} = \{ i \in \mathcal{I} : y_i = 1 \} \).
13: Calculate \( \varphi_{\text{new}}(x_i^h, y_i, h^*) \).
14: while \( \varphi_{\text{old}} \leq \varphi_{\text{new}} \).
15: return \( x_i^h, y_i \), and \( h^* \).

C. Summary of STAR

As mentioned before, the idea of STAR is to iteratively run user association and DBS placement until the total SE of the hotspot cannot be further improved. Here, the total SE of the hotspot \( \varphi \) (which is a function of \( x_i, y_i \), and \( h \)) is calculated based on the objective of \( \mathcal{P} \), i.e.,

\[
\varphi(x_i, y_i, h) = \sum_{i \in \mathcal{I}} w_i(y_i \varphi_i^d + (1 - y_i) \varphi_i^m). \tag{22}
\]

In STAR, \( \varphi_{\text{old}} \) and \( \varphi_{\text{new}} \) are used to keep track of the total SE of the hotspot area incurred in the previous and current iteration, respectively. In general, STAR comprises two stages.

1) Initialization stage (Steps 1–6 in Algorithm 2): initially, all the locations are associated with the DBS, i.e., \( \forall i \in \mathcal{I}, y_i = 1 \) (or \( \mathcal{A} = \mathcal{I} \)). Based on the user association, calculate the horizontal location of the DBS (i.e., \( x_i^h \)) based on Eq. (15) and the altitude of the DBS (i.e., \( h^* \)) by executing \( \text{PGD}(x_i^h) \). Based on the calculated 3D position of the DBS (\( x_i^h, h^* \)), update the user association variable \( y_i \) (\( \forall i \in \mathcal{I} \)) based on Eq. (10) as well as \( \mathcal{A} \). Then, calculate the total SE of the hotspot (i.e., \( \varphi_{\text{new}}(x_i^h, y_i, h^*) \)) according to the current 3D position of the DBS and the user association.

2) Iteration stage (Steps 7–14 in Algorithm 2): in each iteration, the total SE of the hotspot generated from the previous iteration is recorded (i.e., \( \varphi_{\text{old}} = \varphi_{\text{new}} \)). According to the user association area of the DBS (i.e., \( \mathcal{A} \)) generated from the previous iteration, the 3D position of the DBS is updated. Consequently, the user association area of the DBS is updated based on the new 3D position of the DBS, and the total SE of the hotspot area is calculated based on the updated values of \( x_i^h, y_i \), and \( h^* \). The iteration continues until \( \varphi_{\text{old}} < \varphi_{\text{new}} \).

Note that STAR produces a feasible DBS placement and user association after a finite number of iterations, and terminates. It is easy to derive the convergence of STAR. That is, the overall SE should be increased in each iteration (otherwise, STAR terminates), and the maximum overall SE of the network is finite. Thus, STAR must terminate after it reaches the maximum overall SE within a finite number of iterations.

V. SIMULATION RESULTS

Assume that the MBS covers the area with size of 1 km \( \times \) 1 km, which is discretized into 100 \( \times \) 100 locations. Each location has the same size of 10 m \( \times \) 10 m. The MBS is located on the 2D coordinates of (500 m, 500 m), and the altitude of the MBS is 10 m. A hotspot \( \mathcal{A} \) is identified as a rectangular area at the 2D coordinates of (300 m–900 m, 300 m–700 m), as shown in Fig. 2(a), and the locations in the hotspot \( \mathcal{A} \) have the same weight, i.e., \( \forall i \in \mathcal{A}, w_i = 1 \). Other simulation parameters are listed in Table I.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f_c )</td>
<td>Carrier Frequency</td>
<td>2 GHz</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>Environmental parameter</td>
<td>11.9</td>
</tr>
<tr>
<td>( \beta )</td>
<td>Environmental parameter</td>
<td>0.13</td>
</tr>
<tr>
<td>( \epsilon_{\text{LOS}} )</td>
<td>Excessive pathloss in LOS</td>
<td>6 dB</td>
</tr>
<tr>
<td>( \epsilon_{\text{NLOS}} )</td>
<td>Excessive pathloss in NLOS</td>
<td>26 dB</td>
</tr>
<tr>
<td>( P_{\text{مب}} )</td>
<td>Transmission power of the MBS</td>
<td>46 dBm</td>
</tr>
<tr>
<td>( P_{\text{dBm}} )</td>
<td>Transmission power of the DBS</td>
<td>30 dBm</td>
</tr>
<tr>
<td>( \sigma^2 )</td>
<td>Noise</td>
<td>-104 dBm</td>
</tr>
<tr>
<td>( h_{\text{max}} )</td>
<td>Maximum altitude of the DBS</td>
<td>1000 m</td>
</tr>
<tr>
<td>( h_{\text{min}} )</td>
<td>Minimum altitude of the DBS</td>
<td>10 m</td>
</tr>
<tr>
<td>( r )</td>
<td>Predefined threshold in PGD</td>
<td>0.0001</td>
</tr>
</tbody>
</table>

We evaluate the performance of STAR by comparing it with other four methods, i.e., Single MBS (SMBS), Coverage maximization DBS placement (CDBS) [22], Simultaneous user Association and DBS Placement (SOAP) [32], and Spectral efficiency Aware DBS Placement and usEr association (STABLE) [31]. In SMBS, no DBS is deployed in the hotspot area, and so the MBS has to deliver traffic to the UEs by itself. In CDBS and STABLE, the DBS is placed at the center of the hotspot area with the horizontal coordination of (600 m, 500 m). However, CDBS optimizes the altitude of the DBS in order to maximize the coverage area of the DBS. In SOAP, initially, the DBS is randomly deployed in a valid 3D location. Then, in each iteration, the associated area of the DBS is updated based on the current 3D location of the DBS. The 3D location of the DBS is then recalculated based on the updated associated area, where the new horizontal location of the DBS is at the weighted center of gravity of its associated area, and the new altitude of the DBS is optimized to maximize the SE of its worst location, which is associated with the DBS and has the farthest distance to the DBS. The iteration terminates once the SE of the worst location no longer increases. STABLE jointly optimizes the DBS's altitude and the user association in order to maximize the overall SE of the hotspot area. Here, the DBS's altitude is calculated based on the optimal altitudes for the DBS's coverage area. The coverage area of the DBS is defined as the sum of the locations, whose pathloss to the DBS is no larger than a predefined threshold. In the simulations, the predefined threshold is set to be 105 dB.
associated locations, i.e., \( h^* = \frac{1}{\mathcal{L}} \sum_{i \in \mathcal{L}} \tilde{h}_i \), where \( \tilde{h}_i \) is the critical point of function \( \eta_i^d \) in Eq. (3), i.e., \( \nabla \eta_i^d(\tilde{h}_i) = 0 \). Here, \( \eta_i^d \) is the average pathloss between the BSs and location \( i \) (i.e., Eq. (3)) and \( \nabla \eta_i^d(h) = \frac{d\eta_i^d}{dh} \). In the simulations, we will consider SMBS as the baseline method, and calculate the SE improvement incurred by other three methods (i.e., comparing the SE of the hotspot area incurred by the SMBS to that incurred by STAR, SOAP, STABLE, and CDBS, respectively). Also, to analyze the optimality of STAR, we conduct a brute-force search to find the optimal solution of \( P_0 \). In the brute force search, the DBS is iteratively placed over a location in a hot spot. For each location, the altitude of the DBS is iteratively selected from \( h_{\text{min}} \) to \( h_{\text{max}} \) with 2 m increment. For each 3D DBS placement, we calculate the user association and the total SE of the hotspot. The optimal 3D placement of the DBS is the one that incurs the highest SE of the hotspot.

Fig. 2 shows the 3D position of the DBS, the user association, and the SEs of the locations in the hotspot area incurred by SMBS, STAR, SOAP, OPT (i.e., brute-force search), STABLE, and CDBS. STABLE and CDBS assume that the DBS is placed at the center of the hotspot area, but with different altitudes. Since the DBS is placed very close to the MBS and the transmission power of the MBS is much higher than that of the DBS, STABLE and CDBS do not improve the spectral efficiency significantly. As shown in Fig. 2(c), by applying STABLE, only a small number of locations are associated with the DBS. Note that a location is associated with the DBS only if the SE is improved as compared to the location associated with the MBS (i.e., SMBS). Thus, the more locations are associated with the DBS, the more improved the SE of the area can be as compared to SMBS. As shown in Fig. 2(f), no location is associated with the DBS by applying CDBS, and thus the spectral efficiency of the hotspot area is not improved as compared to SMBS. On the other hand, STAR, OPT, and SOAP generate similar DBS locations, which are far away from the MBS to improve the SEs of the locations that are at the edge of the hotspot area. The number of locations associated with the DBS by applying STAR is more than by applying SOAP, but less than by applying OPT. Fig. 3, which shows the total SE improvement (as compared to SMBS) of the whole hotspot area as well as the execution time of different methods, provides more straightforward results to demonstrate the performance. We can see that the total SE improvement incurred by STAR is very close to OPT and much higher than other methods. Meanwhile, the execution time of STAR is much less than OPT (which takes more than 21 days). Although the execution time of STAR is more than SOAP, STABLE, and CDBS, it is feasible to implement STAR in real application scenarios, where the location of a DBS is not frequently updated owing to the slow hotspot movement.

Next, we analyze how the position of the hotspot area affects the performance of different methods. We move the hotspot area from west to east without changing its size, i.e., (100~700 m, 300~700 m), (125~725 m, 300~700 m) . . . , where the range of the hotspot area in the Y coordinates does not change, but the range of the hotspot area in the X coordinates moves 25 m to the east in each iteration. Fig. 4 shows the total SE improvement incurred by the different methods by varying the position of the hotspot area. Here, the values of the X axis in Fig. 4 refers to the range of the hotspot area in the X coordinates. Fig. 5 shows the 3D DBS position incurred by different methods when the hotspot area is moved from west.
to east. Different dots with the same color indicate different 3D DBS positions corresponding to different hotspot positions for the same method. For example, the 1st black dot (i.e., the black dot with the smallest value in the X axis) indicates the 3D DBS position when STAR is applied and the hotspot position is (100~700 m, 300~700 m); the 2nd black dot indicates the 3D DBS position when STAR is applied and the hotspot position is (125~725 m, 300~700 m), and so on.

Based on Fig. 4, we can find that the total SE improvement incurred by STAR is always higher than others. Here, STABLE and CDBS do not optimize the horizontal position of the DBS by simply placing it at the center of the hotspot area. Thus, as the center of the hotspot area is closer to the MBS’s location, the SE improvement is reduced significantly. For example, when the position of the hotspot area is (200~800 m, 300~700 m), as shown in Fig. 5, both STABLE and CDBS place the DBS over the horizontal location (500 m, 500 m), which is overlapped with the MBS. As a result, STABLE and CDBS do not improve the total SE since all the locations are associated with the MBS. Note that CDBS does not improve the SE of the hotspot area in any scenario as its goal is to maximize the coverage area of the DBS, which results in a very high altitude of the DBS (~680 m as shown in Fig. 5), thus significantly reducing the SE of the DBS’s surrounding area (i.e., the hotspot area). As compared to STABLE and CDBS, STAR and SOAP can dynamically adjust the 3D locations once the hotspot area moves. However, STAR always achieves higher SE improvement than SOAP because SOAP is to maximize the SE of the worst location among its associated locations, that results in DBS being deployed at a higher altitude, thus reducing the overall SE.

VI. CONCLUSION

In this paper, we have formulated the problem of jointly optimizing 3D DBS placement and the user association in the context of drone assisted mobile access networks. We have designed the STAR algorithm to efficiently solve the problem and validated its performance via extensive simulations. However, STAR does not consider the capacity limitation of the backhaul link, which may become the bottleneck of transmitting traffic from an MBS to UEs via a DBS. In the future, we will investigate on how the 3D DBS placement affects the throughput of the FSO-based backhaul link between the DBS and the MBS, and design a backhaul-aware DBS placement method to maximize the overall network throughput.

REFERENCES

Xiang Sun (S’13–M’18) received the B.E. and M.E. degrees from the Hefei University of Engineering, Hefei, China, in 2008 and 2011, respectively, and the Ph.D. degree in electrical engineering from the New Jersey Institute of Technology, Newark, NJ, USA, in 2018. He is currently an Assistant Professor with the Department of Electrical and Computer Engineering, University of New Mexico, Albuquerque, NM, USA. His research interests include wireless networks, free space optics, Internet of Things, mobile edge computing and networking, big data-driven networking, and green communications and computing. He was an Associate Editor for Digital Communications and Networks.

Nirwan Ansari (S’78–M’83–SM’94–F’09) received the Ph.D. degree from Purdue University, West Lafayette, IN, USA, the M.S.E.E. degree from the University of Michigan, Ann Arbor, MI, USA, and the B.S.E.E. degree (summa cum laude with a perfect GPA) from the New Jersey Institute of Technology (NJIT), Newark, NJ, USA. He is currently a Distinguished Professor of electrical and computer engineering with NJIT. He authored Green Mobile Networks: A Networking Perspective (IEEE, 2017) with T. Han, and coauthored two other books. He has also authored or coauthored more than 600 technical publications, more than 300 published in widely cited journals/magazines. He has guest-edited a number of special issues covering various topics in communications and networking. He has served on the editorial/advisory board of more than 30 prestigious IEEE journals including Associate Editor of IEEE WIRELESS COMMUNICATIONS MAGAZINE. His current research focuses on green communications and networking, cloud computing, drone-assisted networking, and various aspects of broadband networks. He was elected to serve in the IEEE Communications Society (ComSoc) Board of Governors as a Member-at-Large, has chaired some ComSoc technical and steering committees, and has been serving in many committees such as the IEEE Fellow Committee, and has been actively organizing numerous IEEE International Symposia/Workshops. He is frequently invited to deliver keynote addresses, distinguished lectures, tutorials, and invited talks. Some of his recognitions include several excellence in teaching awards, a few best paper awards, the NCE Excellence in Research Award, several ComSoc TCC Technical Recognition awards, the NJ Inventors Hall of Fame Inventor of the Year Award, the Thomas Alva Edison Patent Award, Purdue University Outstanding Electrical and Computer Engineering Award, the NCE 100 Medal, NAII Fellow, and designation as a COMSOC Distinguished Lecturer. He has also been granted more than 40 U.S. patents.

Rafael Fierro (S’95–M’08–SM’13) received the M.Sc. degree in control engineering from the University of Bradford, England, U.K. and the Ph.D. degree in electrical engineering from the University of Texas at Arlington. Since 2007, he has been a Professor with the Department of Electrical and Computer Engineering, University of New Mexico, the director of Heterogeneous Systems (MARHES) Laboratory. Dr. Fierro was the recipient of a Fulbright Scholarship, National Science Foundation CAREER Award, and the 2008 International Society of Automation (ISA) Transaction Best Paper Award. He is an Associate Editor for the IEEE TRANSACTIONS ON AUTOMATION SCIENCE AND ENGINEERING.

Authorized licensed use limited to: UNIVERSITY OF NEW MEXICO. Downloaded on March 11, 2020 at 18:11:51 UTC from IEEE Xplore. Restrictions apply.