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<https://doi.org/10.1038/s41467-020-14773-4>

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A silicate dynamo in the early Earth

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The Earth's magnetic field has operated for at least 3.4 billion years, yet how the ancient field was produced is still unknown. The core in the early Earth was surrounded by a molten silicate layer, a basal magma ocean that may have survived for more than one billion years. Here we use density functional theory-based molecular dynamics simulations to predict the electrical conductivity of silicate liquid at the conditions of the basal magma ocean: 100–140 GPa, and 4000–6000 K. We find that the electrical conductivity exceeds 10,000 S/m, more than 100 times that measured in silicate liquids at low pressure and temperature. The magnetic Reynolds number computed from our results exceeds the threshold for dynamo activity and the magnetic field strength is similar to that observed in the Archean paleomagnetic record. We therefore conclude that the Archean field was produced by the basal magma ocean.

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The Archean magnetic field may have been essential for preserving the early atmosphere and hydrosphere¹. The process by which the field is produced today: a dynamo hosted in the Earth's metallic iron-rich liquid outer core is thought to be difficult to sustain in the early Earth because the core could not cool sufficiently rapidly^{2–4}. Alternative energy sources, including radioactive heat production in the core or exsolution of Mg from the cooling core, may not be sufficient to sustain an early dynamo.

Planetary dynamos in the solar system are hosted in a variety of materials including iron-rich liquid, such as in the Earth and other terrestrial planets, ionically conductive fluid ices, as in Uranus and Neptune, and metallic hydrogen as in Jupiter and Saturn⁵. A silicate dynamo is so far unknown. Magnetohydrodynamic simulations, laboratory experiments, and studies of planetary bodies that host magnetic fields show that dynamo activity requires a sufficiently large magnetic Reynolds number $R_m = \mu_0 \nu L \sigma > 40$, where μ_0 is the magnetic susceptibility, ν is the flow velocity, L is the depth of the layer, and σ is the electrical conductivity^{6,7}. Using illustrative values, $R_m = 40(\nu/1 \text{ cm/s})(L/300 \text{ km})(\sigma/10,000 \text{ S/m})$. Therefore, for a silicate dynamo to operate the electrical conductivity must exceed 10,000 S/m, more than 100 times higher than the highest values measured in silicate liquids at low pressure and temperature^{8,9}, although less than typical metallic conductivity (10^6 S/m for the Earth's outer core).

Here we perform first principles molecular dynamics simulations of a silicate liquid that closely approximates the composition of the bulk silicate Earth and includes the six most abundant oxide components; the size of our simulation is 1129 atoms (see Methods). The simulations and the computation of the electrical conductivity closely follow our previous work on the SiO_2 and $(\text{Mg,Fe})\text{O}$ systems^{10,11} (see Methods). Briefly, we compute the electronic contribution to the electrical conductivity with the Kubo–Greenwood formula¹² and the ionic conductivity from the electric current autocorrelation function¹³. In order to investigate the effect of magnetism on our results, we consider non-spin-polarized and spin-polarized results with the latter characterized by high-spin moments on all the iron atoms. We combine our predictions of electrical conductivity with a model of the thermal evolution of the basal magma ocean to estimate the magnetic Reynolds number and the strength of the magnetic field generated by the silicate dynamo. We find that the magnetic Reynolds number exceeds 40 and that the field strength is in excellent agreement with paleointensity measurements.

Results

Electrical conductivity. Our results show that the electrical conductivity of silicate liquid exceeds 10,000 S/m at the conditions of the basal magma ocean (Fig. 1). The electrical conductivity increases with increasing temperature and decreases with increasing pressure. Magnetism reduces the electrical conductivity by 10%. The primary charge carriers are electrons: the electronic contribution to σ exceeds the ionic contribution by more than an order of magnitude. This behavior contrasts with experimental results at low pressure and temperature where ions are the dominant charge carriers⁸.

We can understand the electrical conductivity of silicate liquid by comparing with simpler systems and by examining the electronic density of states (Fig. 2). The electrical conductivity of the silicate liquid is intermediate to that of SiO_2 liquid^{11,14,15} and $(\text{Mg,Fe})\text{O}$ liquid¹⁰ over the range of temperature and pressure that we have investigated. The conductivity of the silicate liquid is greater than that of SiO_2 because of the role of iron. Iron 3d states contribute to the density of states at the Fermi level and increase the conductivity compared with the iron-free system. The role of

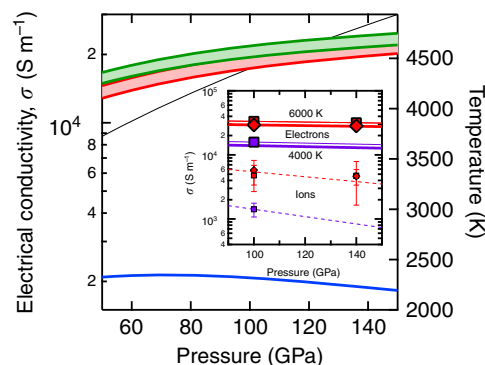


Fig. 1 Electrical conductivity. The electronic σ_{el} (red), ionic σ_{ion} (blue), and total $\sigma_{\text{total}} = \sigma_{\text{el}} + \sigma_{\text{ion}}$ (green) electrical conductivity along the magma ocean isentrope³⁷ (black) for low-spin (top of range shown) and high-spin (bottom of range) results. Along the magma ocean isentrope, the electrical conductivity increases with depth because the effects of increasing temperature outweigh the effects of increasing pressure. Inset. The electrical conductivity of the bulk silicate Earth liquid from our simulations, including the electronic (large symbols) and ionic (small symbols with 1σ uncertainties) contributions at 6000 K (red) and 4000 K (purple) in spin-polarized (diamonds) and non-spin-polarized (squares) calculations. Lines are best fits to the form $\sigma = \sigma_0 T^{-1} \exp[-(E^* + PV^*)/RT]$ for the electronic non-spin-polarized results ($\sigma_0 = 1.994\text{e}9 \text{ S/m}$, $E^* = 108.6 \text{ kJ/mol}$, $V^* = 0.0611 \text{ cm}^3/\text{mol}$, light solid lines) and shifted uniformly downward to account for spin-polarization ($\sigma_0 = 1.754\text{e}9 \text{ S/m}$, bold solid lines), and to the ionic contribution ($\sigma_0 = 1.0811\text{e}9 \text{ S/m}$, $E^* = 131.0 \text{ kJ/mol}$, $V^* = 0.437 \text{ cm}^3/\text{mol}$, dashed lines).

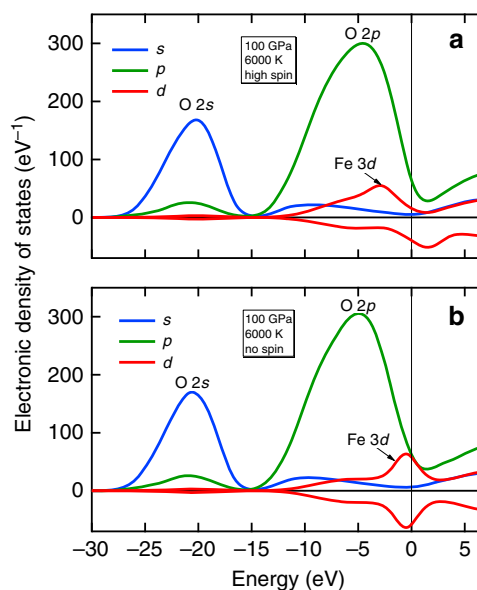


Fig. 2 Electronic density of states in the silicate liquid. At 100 GPa and 6000 K in spin-polarized (a) and non-spin-polarized (b) states. Contributions from s- (blue), p- (green) and d-like (red) states are shown separately and the dominant atomic contributions to each are indicated. The vertical black line is the Fermi level.

iron also explains why the temperature dependence of the electrical conductivity in the silicate liquid is less than that of SiO_2 liquid (the conductivity in silica falls precipitously on cooling and drops ten times from 6000 to 4000 K, whereas in the silicate liquid, it decreases only twofold): the highly localized iron 3d states are less sensitive to their chemical environment than the O

$2p$ states that also contribute to conduction and their contribution to the density of states at the Fermi level is much less sensitive to temperature. The conductivity of the silicate liquid is less than that of $(\text{Mg}_{0.75}\text{Fe}_{0.25})\text{O}$ because the iron concentration is less in the silicate liquid ($\text{Fe}/(\text{Fe} + \text{Mg}) = 0.11$). The electronic density of states also explains why the conductivity of the spin-polarized system is slightly less than that of the non-spin-polarized system: magnetism splits up- and down-spin iron $3d$ states, reducing the density of states at the Fermi level. While there are no experimental measurements of the electrical conductivity of silicate liquids at basal magma ocean conditions, we have shown that our approach yields results that are in good agreement with available experimental data at high pressure including the optical reflectivity of silica liquid and the electrical conductivity of crystalline $(\text{Mg,Fe})\text{O}$ ^{10,11}.

Magnetic field. To quantify magnetic field production, we combine our results for the electrical conductivity with a model of the thermal evolution of the basal magma ocean. The thermal evolution model is identical to that examined previously¹⁶, except that we have replaced the previously assumed value of the entropy of melting with the value determined from first principles molecular dynamics simulations (see Methods). This model yields the thickness of the magma ocean L and heat flux out of the magma ocean q , which we combine with our values of the electrical conductivity to estimate the magnetic Reynolds number $R_m = (Lq/\rho H_T)^{1/3} L \mu_0 \sigma$ where ρ is the mean density of the magma ocean and H_T is the thermal scale height. We have assumed the mixing length scaling for the flow velocity¹⁷. We estimate the magnetic field strength at the top of the basal magma ocean according to the scaling derived from numerical simulations¹⁷ $B_M = 0.63 \rho^{1/3} (Lq/H_T)^{2/3}$, where we have assumed that viscous dissipation is negligible because the ratio of viscous to magnetic diffusivity, the magnetic Prandtl number $P_m = \mu_0 \sigma \eta / \rho = 10^{-7}$ is small, where $\eta = 0.1 \text{ Pa s}$ is the viscosity of the basal magma ocean from previous first principles simulations¹⁸. Finally, we estimate the field strength at the surface $B_S = \frac{1}{7} B_M (r_M/r_E)^3$, where the pre-factor accounts for the proportion of the field strength in the dipole component, and the cubic dependence on radius accounts for the upward continuation of the dipole component to the surface: r_M is the radius at the top of the basal magma ocean and r_E is the radius of the Earth⁶.

Our results show that a basal magma ocean is likely to have produced a magnetic field (Fig. 3). The magnetic field strength is very similar to that observed in the geologic record of the first few billion years of Earth's history. Moreover, the magnetic Reynolds number is sufficiently large to allow for a silicate dynamo in the early Earth. Although the basal magma ocean suppresses core convection, the core is likely to have strong horizontal flows that produce toroidal fields from the poloidal field generated by the basal magma ocean, reinforcing the silicate dynamo. The importance of this effect for the silicate dynamo is uncertain. Ziegler and Stegman¹⁹ suggested as the criterion for magnetic field generation the following dynamo number $D = (R_m R_{\text{mcore}})^{1/2} > 100$, where $R_{\text{mcore}} = 3500$ is the magnetic Reynolds number of the core computed assuming that the horizontal flow velocity is similar to that of the core today. According to the dynamo number criterion, the silicate dynamo may operate throughout the Archean (Fig. 3). Alternative velocity scalings also yield $D > 100$ (see Methods). It is likely that the basal magma ocean became more iron-rich as it crystallized and that this iron enrichment increased the electrical conductivity. Our results for R_m and D may therefore be underestimates. We have

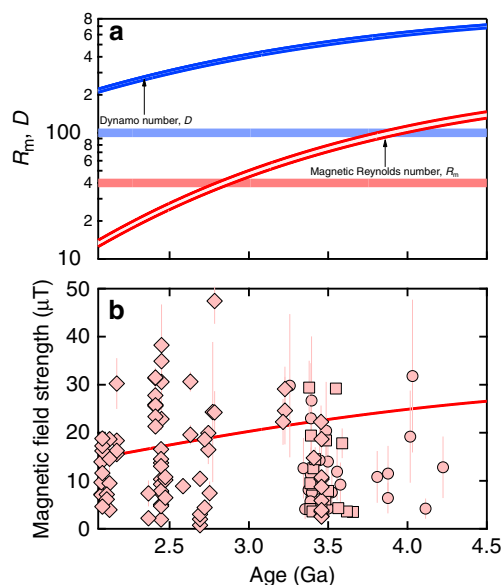


Fig. 3 Magnetic Reynolds number and magnetic field strength. **a** The magnetic Reynolds number (red) and Dynamo number (blue) computed from our electrical conductivity results and thermal evolution model with shading indicating the difference between low-spin (top of range) and high-spin (bottom of range) results compared with the respective critical values of $R_m = 40$ and $D = 100$ (thick horizontal lines). **b** Magnetic field strength computed from our model (red line) compared with paleomagnetic data: diamonds from the PINT database⁴⁰, and circles (Thellier-Coe method) and squares (565C method) from zircons⁴¹. We note that the evidence of a field prior to the oldest whole-rock PINT data at 3.45 Ga relies on the single-crystal zircon results, which have been questioned as not deriving from a primary magnetic carrier⁴².

not attempted a more quantitative treatment of the effects of iron enrichment because liquid-crystal iron partitioning and the magnitude of the effect of iron enrichment on the electrical conductivity of silicate liquid at basal magma ocean conditions are uncertain.

Discussion

The Earth's magnetic field may have transitioned from being produced by the basal magma ocean to being produced by the core near the end of the Archean: as the magma ocean cools, heat flow out of the core increases to the point that core convection, and a core dynamo, is possible (Supplementary Fig. 4b). Mechanisms have been proposed by which the core could produce a field earlier, including the presence of radioactive heat producing elements in the core^{3,20} and the precipitation of Mg^{4,21}. However, recent experimental studies show that the solubility of K and U in the core is too small to power a dynamo^{22,23}. Moreover, a recent reanalysis of experimental data shows that the temperature dependence of Mg precipitation, and thus the power produced, is a factor of six less than originally thought²⁴ and may be less than that required to sustain a magnetic field²⁵. The field produced by the silicate dynamo may have differed in geometry from the present day field and it may be possible to distinguish these unique characteristics in the geologic record. For example, there is some evidence from modeling magnetic field generation in other planetary bodies, including Uranus and Neptune²⁶, that shallow layers, like the basal magma ocean, produce a less dipolar field than the strongly dipolar field of the present Earth. Many super-Earth exoplanets may have extensive magma oceans because of the greater amount of accretional energy stored in larger mass planets²⁷, strong stellar

irradiation, or the insulation of overlying gaseous envelopes²⁸. Silicate dynamos may therefore be common in the universe.

Methods

System. Our system consists of 1129 atoms of seven different elements, with relative proportions chosen to closely match the six most abundant oxide components of the bulk silicate Earth (Supplementary Figs. 1 and 2, Supplementary Table 1).

Molecular dynamics simulations. Our molecular dynamics simulations are based on density functional theory in the PBEsol approximation²⁹, combined with the +*U* method³⁰ with $U-J = 2.5$ eV as in our previous work^{10,31,32}. We use the projector augmented wave method³³, as implemented in VASP³⁴. The core radii and number of electrons treated as valence for each element are listed in Supplementary Table 1. Born-Oppenheimer simulations are performed in the canonical ensemble using the Nosé-Hoover thermostat and run for 6–10 ps with 1 fs time step. We perform spin-polarized simulations in which the difference in the number of up-spin and down-spin electrons is fixed to the high spin value (four times the number of Fe atoms) and also non-spin-polarized calculations. We assume thermal equilibrium between ions and electrons via the Mermin functional³⁵. Sampling the Brillouin zone at the Gamma point and a basis-set energy cutoff of 500 eV were found to be sufficient to converge energy and pressure to within 2 meV/atom and 0.2 GPa, respectively. Our previous studies^{10,11} indicate that our simulations are well converged with respect to the number of atoms: in the case of SiO₂, simulations with 96 and 144 atoms did not differ significantly in the value of σ , while in the case of (Mg,Fe)O, differences in σ between simulations containing 128, 256, and 512 atoms were less than 10%.

Electronic conductivity and electronic density of states. We compute the electronic conductivity via the Kubo-Greenwood formula¹² as implemented in VASP from a series of at least 10 uncorrelated snapshots at each volume-temperature condition (Supplementary Fig. 3). The frequency dependent electronic conductivity is

$$\sigma_{\text{el}}(\omega) = \frac{2\pi e^2 \hbar^2}{3m^2 \omega \Omega} \sum_{\vec{k}} \sum_{ij} [f(\epsilon_j, \vec{k}) - f(\epsilon_i, \vec{k})] \langle \psi_{i,\vec{k}} | \nabla | \psi_{j,\vec{k}} \rangle^2 \delta(\epsilon_i - \epsilon_j - \hbar\omega), \quad (1)$$

where the sums are over the Brillouin zone and pairs of states, respectively, f is the Fermi occupation, ψ is the wavefunction, ϵ is the eigenvalue, ω is the frequency, and Ω is the volume of the simulation cell. In our computations, the δ function is replaced by a Gaussian of width Δ given by the average spacing between eigenvalues weighted by the corresponding change in the Fermi function³⁶. As the behavior of Eq. 1 becomes unphysical for $\hbar\omega < \Delta$, we find the DC conductivity by linearly extrapolating to zero frequency.

We found that a $1 \times 1 \times 1$ k-point mesh and 7200 electronic bands were sufficient to yield converged values of the electronic conductivity and the electronic density of states by performing calculations at doubled Brillouin zone sampling ($2 \times 2 \times 2$ k-point mesh) and a larger number of electronic bands (10,200). We compute the electronic density of states by averaging over 10 snapshots well separated in time from the molecular dynamics trajectories. We use the energy derivative of the Fermi-Dirac function with temperature equal to the ionic temperature to smooth the density of states.

Ionic conductivity. We compute the ionic part of the electrical conductivity in the DC limit from the electric current autocorrelation function¹³

$$J(t) = \sum_{ij} z_i z_j \langle \vec{u}_i(t+t_0) \cdot \vec{u}_j(t_0) \rangle, \quad (2)$$

as the integral

$$\sigma_{\text{ion}} = \frac{e^2}{3kT\Omega} \int J(t) dt. \quad (3)$$

where z_i and $\vec{u}_i$ are the Bader charge and velocity of ion i , respectively, and the angle brackets indicate an average over time origins t_0 . The Bader charges of the ions computed in our simulation are listed in Supplementary Table 1.

Thermal evolution of the basal magma ocean. We solve the coupled system of equations¹⁶:

$$4\pi a^2 k \frac{T_L - T_M}{\delta} = -(M_m c_m + M_c c_c) \frac{dT_L}{dt} + H(t) - 4\pi a^2 \rho \Delta S T_L \frac{da}{dt}, \quad (4)$$

$$T_L = T_A - (T_A - T_B) \xi, \quad (5)$$

$$\frac{d\xi_L}{dt} = -\frac{3a^2 \Delta \xi}{a^3 - b^3} \frac{da}{dt}, \quad (6)$$

where the first equation expresses the relationship between the time evolution of the outer radius of the basal magma ocean a , and its temperature T_L where k is the thermal conductivity, T_M is the temperature of the overlying solid mantle, δ is the thickness of thermal boundary layer at the base of the overlying mantle, M and c are the mass and isobaric specific heat, respectively of the basal magma ocean (subscript m) and core (subscript c), H is the radioactive heat production, ρ is the density of the basal magma ocean, and ΔS is the entropy change on freezing. The inner radius of the basal magma ocean b is assumed to be the core-mantle boundary. The term on the left-hand side is the total heat flux out of the basal magma ocean. On the right-hand side we have contributions from, respectively, cooling of the basal magma ocean and the core, radioactive heat production, and latent heat of freezing. The second equation expresses the idealized phase diagram defined by a linear dependence of the liquidus temperature on the mass fraction of the dense component ξ , where T_A and T_B are the melting temperatures of the end-member light (A) and dense (B) components. The last equation is a statement of mass balance where $\Delta \xi = \xi_L - \xi_S$ is the enrichment of the liquid in the dense component. The model does not include inner core growth, nor radioactive heating, nor Mg-exsolution in the core.

We solve the equations with a fourth-order Runge-Kutta method and adopt values of all parameters identical to those assumed in ref. 16, except for the entropy of melting, which we take from our previous simulations $\Delta S = 652$ J/kg/K³⁷ (Supplementary Table 2). The value of δ is chosen to yield a present day temperature at the core-mantle boundary of 4000 K.

Magnetic Reynolds number. We compute the magnetic Reynolds number of the basal magma ocean as

$$R_m = \mu_0 \nu L \sigma, \quad (7)$$

where μ_0 is the permeability of free space, L is the thickness of the basal magma ocean, ν is the flow velocity, and σ is the electrical conductivity. We take the value of $L = a - b$ from the thermal evolution model (Supplementary Fig. 4). The value of σ is the total electrical conductivity computed at the base of the basal magma ocean and the temperature T_L from the thermal evolution model (Supplementary Fig. 4) and the equations for the temperature dependence of σ_{el} and σ_{ion} given in the caption to Fig. 1 in the main text.

To estimate the flow velocity, we use the scaling recommended by numerical simulations¹⁷ from mixing length theory

$$\nu = \left(\frac{Lq}{\rho H_T} \right)^{1/3}, \quad (8)$$

where q is the total heat flow out of top of the basal magma ocean (Supplementary Fig. 4b), ρ is the density of the magma ocean, and H_T is the thermal scale height, which we find from our previous simulation results³⁷ to be $H_T = 7622$ km. Following¹⁹, we also examine alternative scalings for the velocity, including those based on a balance between Coriolis, inertial, and Archimedean (buoyancy) forces: CIA

$$\nu = \left(\frac{q}{\rho H_T} \right)^{2/5} \left(\frac{L}{\Omega} \right)^{1/5} \quad (9)$$

and from a balance between the buoyancy and Lorentz forces: MAC

$$\nu = \left(\frac{q}{\Omega \rho H_T} \right)^{1/2}, \quad (10)$$

where Ω is the rotation rate.

We also estimate the possible effects of coupling of the magnetic field produced by the basal magma ocean with the underlying, non-convecting core. Although the basal magma ocean suppresses core convection, the core is likely to have strong horizontal flows that generate toroidal fields from the poloidal field produced by the basal magma ocean, reinforcing the silicate dynamo. Ziegler and Stegman¹⁹ suggested as the criterion for magnetic field generation the following dynamo number D : the geometric mean of the magnetic Reynolds numbers of the basal magma ocean and the core

$$D = (R_m R_{\text{mcore}})^{1/2}, \quad (11)$$

where $R_{\text{mcore}} = 3500$ is the magnetic Reynolds number of the core computed assuming that the horizontal flow velocity is similar to that of the core today, and $D > 100$ in order to produce a magnetic field. Following Ziegler and Stegman, we have estimated R_{mcore} by assuming that the horizontal flow velocity is similar to that of the core today ($\nu = 5 \times 10^{-4}$ m/s)³⁸, the conductivity, $\sigma = 1.5 \times 10^6$ S/m³⁹, and $L = 3500$ km.

Data availability

Raw simulation results are available from the corresponding author on request.

Code availability

VASP is widely used proprietary software.

Received: 25 August 2019; Accepted: 29 January 2020;

Published online: 25 February 2020

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Acknowledgements

This project is supported by the European Research Council under Advanced Grant 291432 MoltenEarth (FP7) and by the National Science Foundation (EAR-1853388). Calculations were carried out using the IRIDIS cluster partly owned by University College London, ARCHER of the UK National High-Performance Computing Service, and MARENOSTRUM at the Barcelona Supercomputing Center, Spain of the PRACE Consortium. We thank J. Aurnou for helpful comments on the manuscript.

Author contributions

L.S. and R.S. designed and performed the research, and analyzed the data. M.P.D. provided analytical tools. L.S., R.S., and M.P.D. wrote the paper.

Competing interests

The authors declare no competing interests.

Additional information

Supplementary information is available for this paper at <https://doi.org/10.1038/s41467-020-14773-4>.

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Peer review information *Nature Communications* thanks Ulrich Christensen, Joseph O'Rourke and the other, anonymous, reviewer(s) for their contribution to the peer review of this work.

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**Supplementary Information for
A Silicate Dynamo in the Early Earth**

by

Lars Stixrude, Roberto Scipioni, and Michael P. Desjarlais

Supplementary Tables

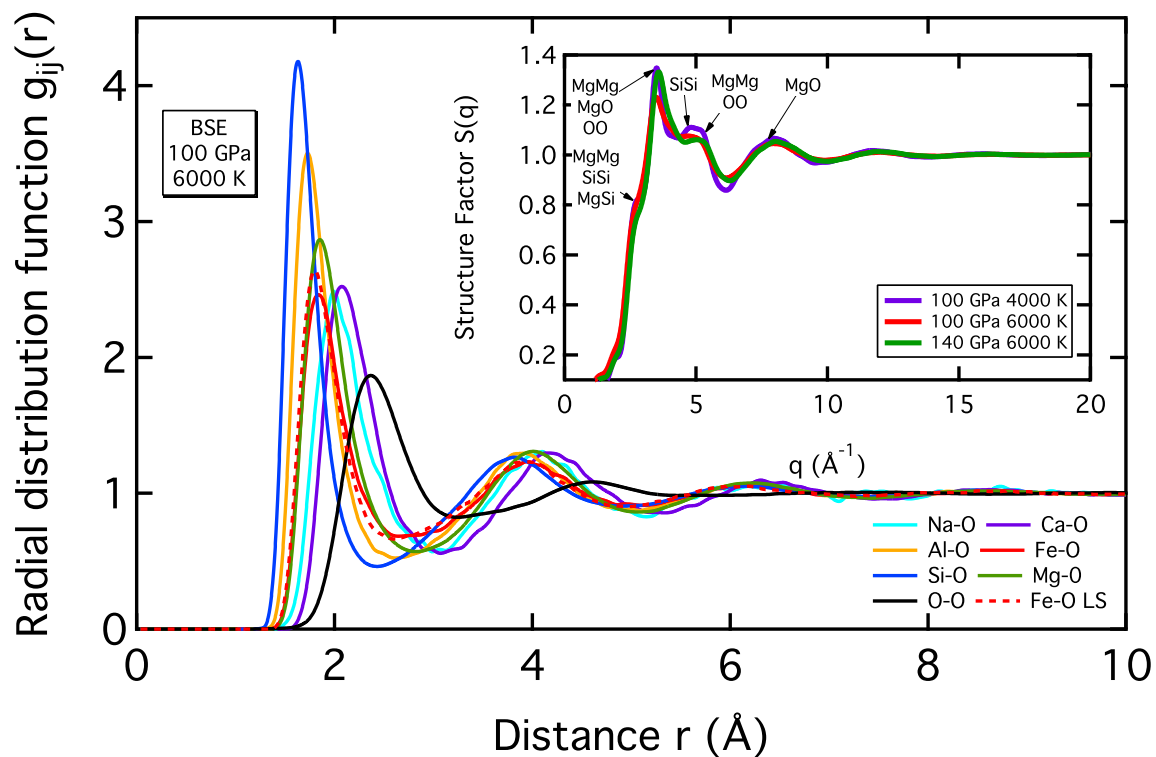
Supplementary Table 1. Composition of the simulated system given as the number of atoms in the periodically repeated simulation cell (Number) and as the mass fraction of conventional oxides (wt. %) compared with the depleted mid-ocean-ridge-basalt mantle (DMM) composition of Workman and Hart ¹. Also shown are the core radii and number of valence electrons of the PAW potentials used for each element, and the Bader charge computed for each ion ².

Element	Number	Oxides wt. %	DMM wt. %	Radius (Bohr)	Valence Electrons	Bader Charge
Si	178	44.93	44.93	1.90	4	2.77
Mg	229	38.78	38.82	2.00	8	1.75
Fe	28	8.45	8.56	2.20	14	0.80
Ca	14	3.30	3.18	3.00	8	1.39
Al	20	4.28	4.37	1.90	3	2.34
Na	2	0.26	0.13	2.20	7	0.81
O	658			1.52	6	-1.48

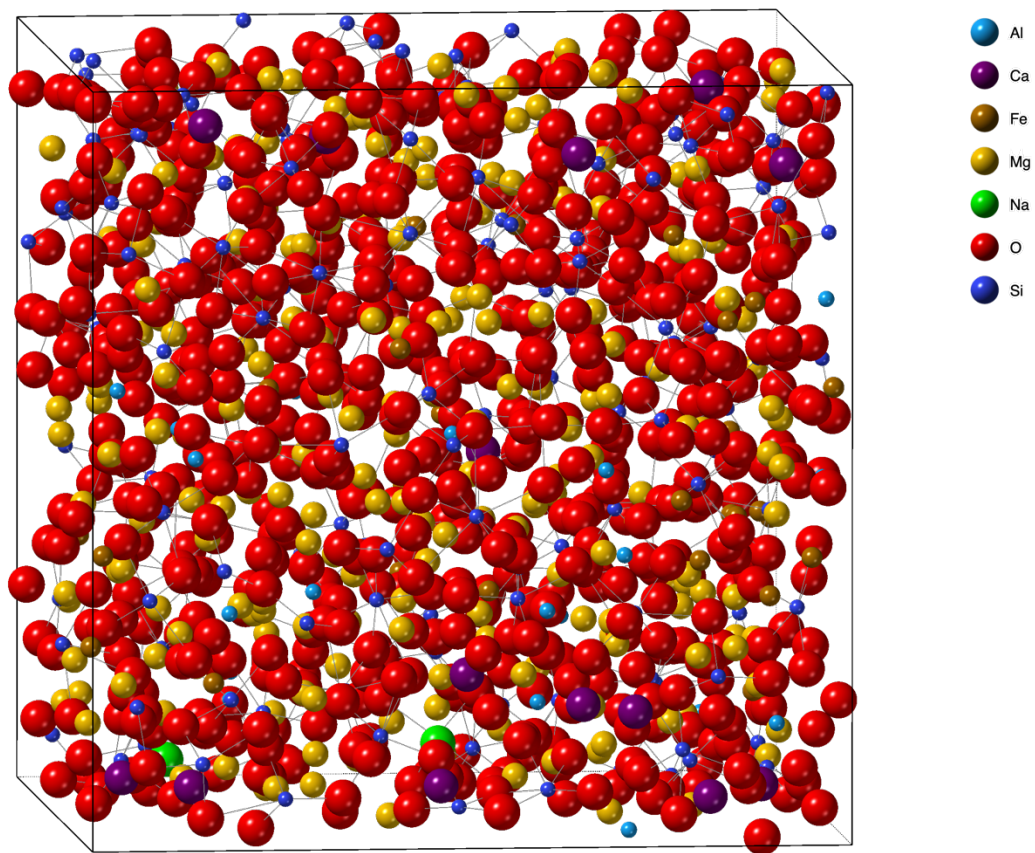
Supplementary Table 2. Values of parameters used in the thermal evolution model.

Parameter		Value
k	Thermal conductivity	$8 \text{ W m}^{-1} \text{ K}^{-1}$
δ	Boundary layer thickness	87 km
T_M	Mantle temperature	2730 K
c_m	Basal Magma ocean specific heat	$1000 \text{ J kg}^{-1} \text{ K}^{-1}$
c_c	Core specific heat	$860 \text{ J kg}^{-1} \text{ K}^{-1}$
M_c	Core mass	$2 \times 10^{24} \text{ kg}$
ρ	Basal magma ocean density	5500 kg m^{-3}
ΔS	Entropy of melting	$652 \text{ J kg}^{-1} \text{ K}^{-1}$
$\Delta \xi$	Mass fraction change on freezing	0.088
T_A	Component A melting temperature	5500 K
T_B	Component B melting temperature	3500 K
b	Core radius	3480 km
Ω	Rotational period	24 hours

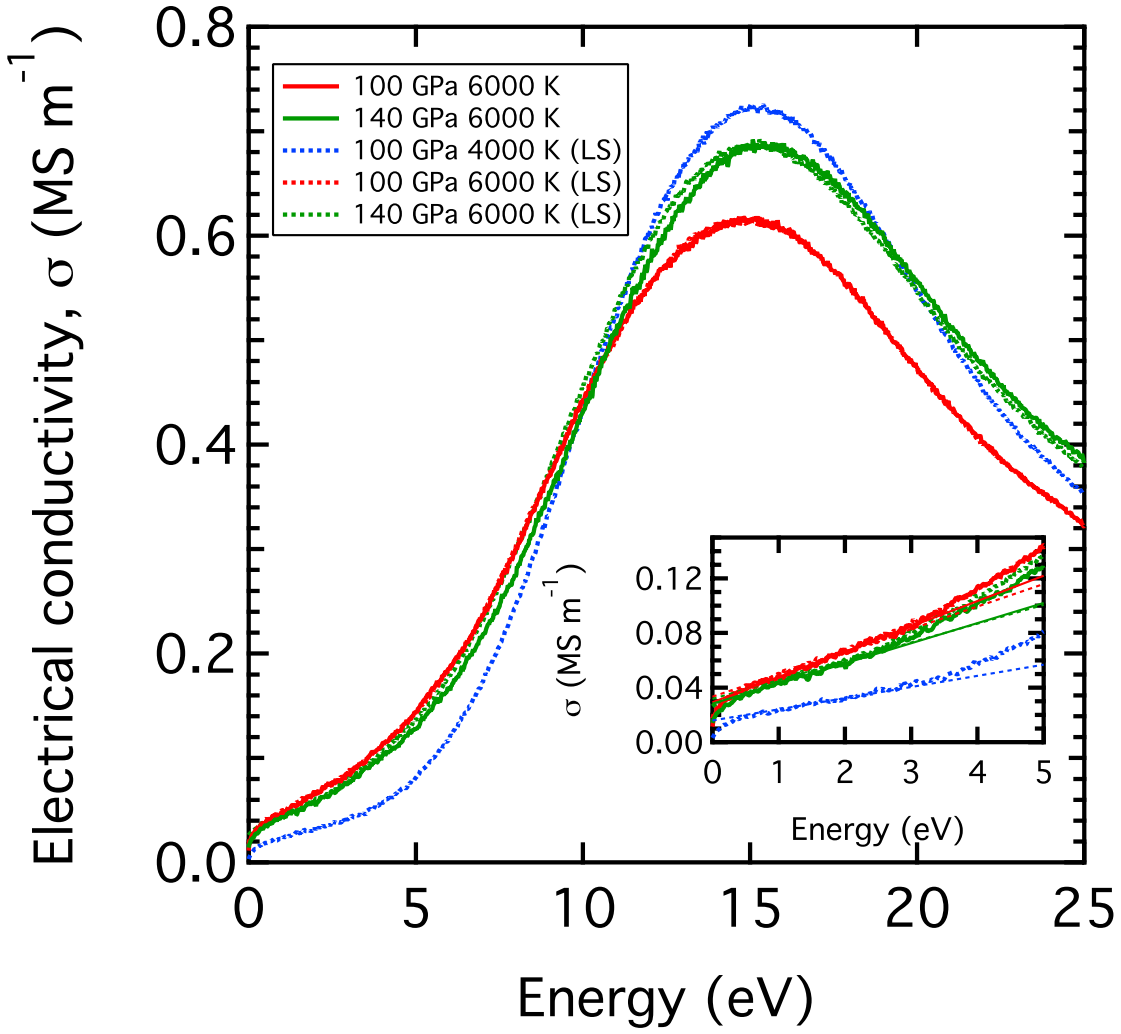
Supplementary Figures



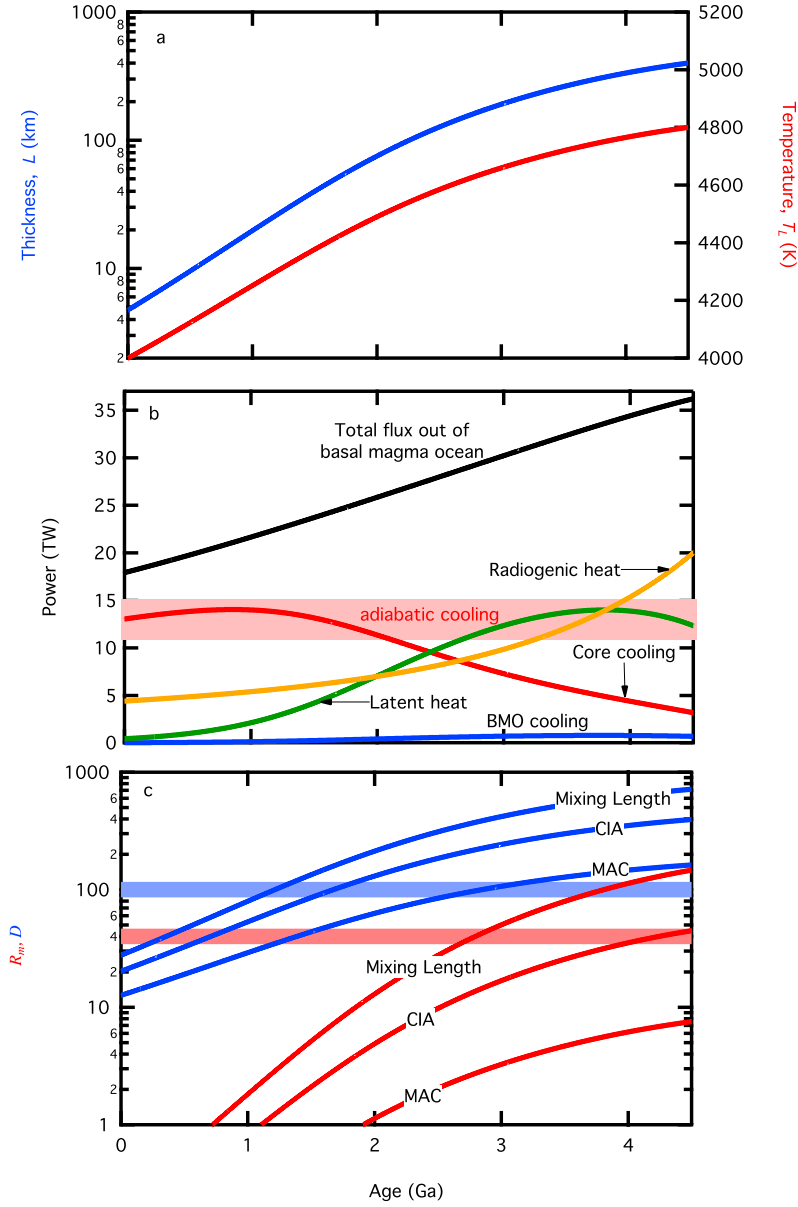
Supplementary Figure 1. Structure of the bulk silicate Earth composition liquid as represented by the oxygen partial radial distributions functions from a fully spin-polarized simulation (solid lines). For comparison, we also show, in the case of Fe-O, the result for a non-spin-polarized (LS) simulation at the same pressure and temperature (dashed line), which produces shorter Fe-O distances. The inset shows the x-ray structure factor computed by convolving the Fourier transform of the radial distribution function with the x-ray scattering factors of the ions. Labels indicate the dominant contributions to the peaks and shoulders.



Supplementary Figure 2. Snapshot from a simulation at 100 GPa and 4000 K.



Supplementary Figure 3. Electronic conductivity as a function of energy at the pressure-temperature conditions indicated from spin polarized (solid) and non-spin polarized (dashed) calculations. We find the zero frequency (DC) value of the electronic conductivity as the intercept of the best fit line to results between 1 and 2 eV as shown in the inset.



Supplementary Figure 4. Thermal evolution of the basal magma ocean. **a** The thickness (blue) and temperature (red) as a function of time. **b** The total heat flux out of the basal magma ocean (black) and the contributions to this total: cooling of the basal magma ocean (blue), cooling of the core (red), radiogenic heat (orange), and latent heat of freezing (green). The pink band shows the heat flow conducted down the core adiabat according to the values of the thermal conductivity of the core predicted by³ (top of band, thermal conductivity at the top of the core $k_{core}=100$ W/m/K) and⁴ (bottom of band, $k_{core}=77$ W/m/K). The pink band indicates the minimum core cooling required for thermal convection of the outer core. **c** Values of the magnetic Reynolds number computed from the thermal evolution model and velocity scaling laws indicated (red lines, Eqs. 0.7-0.10) and the dynamo number (blue lines, Eq. 0.11) as compared with their critical values for dynamo generation (thick horizontal lines).

SUPPLEMENTARY REFERENCES

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