

Target Language-Aware Constrained Inference for Cross-lingual Dependency Parsing

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Abstract

Prior work on cross-lingual dependency parsing often focuses on capturing the commonalities between source and target languages and overlooks the potential of leveraging linguistic properties of the languages to facilitate the transfer. In this paper, we show that weak supervisions of linguistic knowledge for the target languages can improve a cross-lingual graph-based dependency parser substantially. Specifically, we explore several types of *corpus linguistic statistics* and compile them into *corpus-wise constraints* to guide the inference process during the test time. We adapt two techniques, Lagrangian relaxation and posterior regularization, to conduct inference with corpus-statistics constraints. Experiments show that the Lagrangian relaxation and posterior regularization inference improve the performances on 15 and 17 out of 19 target languages, respectively. The improvements are especially significant for target languages that have different word order features from the source language.

1 Introduction

Natural language processing (NLP) techniques have achieved remarkable performance in a variety of tasks when sufficient training data is available. However, obtaining high-quality annotations for low-resource language tasks is challenging, and this poses great challenges to process low-resource languages. To bridge the gap, cross-lingual transfer has been proposed to transfer models trained on high-resource languages (e.g., English) to low-resource languages (e.g., Tamil) to combat the resource scarcity problem. Recent studies have demonstrated successes of transferring models across languages without retraining for NLP tasks, such as named entity recognition (Xie et al., 2018), dependency parsing (Tiedemann, 2015; Agić et al., 2014), and question

answering (Joty et al., 2017), using a shared multi-lingual word embedding space (Smith et al., 2017) or delexicalization approaches (Zeman and Resnik, 2008; McDonald et al., 2013).

One key challenge for cross-lingual transfer is the *differences* among languages; for example, languages may have different word orders. When transferring a model learned from a source language to target languages, the performance may drop significantly due to the differences. To tackle this problem, various approaches have been proposed to better capture the *commonalities* between the source and the target languages (McDonald et al., 2011; Guo et al., 2016; Täckström et al., 2013; Agić, 2017; Ahmad et al., 2019); however, they overlook the potential to leverage linguistic knowledge about the target language to account for the *differences* between the source and the target languages to facilitate the transfer.

In this paper, we propose a complementary approach that studies how to leverage the linguistic knowledge about the target languages to help the transfer. Specifically, we use corpus linguistic statistics of the target languages as weak supervision signals to guide the test-time *inference* process when parsing with a graph-based parser. This approach is effective as the model only need to be trained *once* on the source language and applied to many target languages using different constraints *without retraining* the model.

We argue that certain corpus linguistic statistics such as the word order (e.g., how often an adjective appears before or after a noun) can be easily obtained from available resources such as World Atlas of Language Structures (WALS) (Dryer and Haspelmath, 2013). To incorporate the corpus linguistic statistics to a cross-lingual parser, we compile them into corpus-wise constraints and adopt two families of methods: 1) Lagrangian relaxation (LR) and 2) posterior regularization (PR) to

Algorithm 1 Lagrangian Relaxation for Constraint Inference

Input: Constraints $\mathcal{C} = \{C_i\}_{i=1}^N$, corresponding ratio $\mathbf{r} = \{r_i\}_{i=1}^N$, tolerance margin $\theta = \{\theta_i\}_{i=1}^N$, learning rate decay η , initial learning rate α_0

Output: parse trees \hat{Y}

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1:  $\alpha \leftarrow \alpha_0$ 
2:  $\lambda_i \leftarrow 0, i \in [N]$ 
3: repeat
4:    $\hat{Y} \leftarrow \arg \max_{Y \in \mathcal{Y}} L(Y, \lambda; \mathcal{C})$ 
5:    $\hat{r}_i \leftarrow R(C_i, \hat{Y}), i \in [N]$ 
6:   if  $\forall i, \text{abs}(r_i - \hat{r}_i) \leq \theta$  then
7:     return  $\hat{Y}$ 
8:    $\lambda_i \leftarrow \alpha(\hat{r}_i - r_i), i \in [N]$ 
9:    $\alpha \leftarrow \eta\alpha$ 
10: until MAX_ITER times
11: return  $\hat{Y}$ 

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where λ_i is called Lagrangian multiplier. It is well-known that we can solve the dual form of the constrained inference problem:

$$\max_{Y \in \mathcal{Y}} \min_{\lambda \geq 0} L(Y, \lambda; \mathcal{C}).$$

To solve the dual form, we initialize λ_i to be 0. At iteration t , we firstly conduct an constraint-augmented inference with a fixed $\lambda^{(t)}$:

$$\hat{Y}^{(t)} = \max_{Y \in \mathcal{Y}} L(Y, \lambda^{(t)}; \mathcal{C}). \quad (6)$$

As $F(C)$ is a linear function w.r.t y_k , we combine it with $S_{ij}^{(k)} y_k(i, j)$. In this way, the inference problem Eq. (6) can be treated as a special case of Eq. (1) with a different scoring matrix $S^{(k)}$. In this way, we can treat the inference on every sentence independently and leverage existing inference techniques.

After solving the constraint-augmented inference, we compute the ratio of every constraint $\hat{r}_i^{(t)} = R(C_i, \hat{Y}^{(t)})$, and use gradient ascent algorithm to update the Lagrangian multipliers

$$\lambda_i^{(t+1)} = \lambda_i^{(t)} + \alpha^{(t)}(r_i - \hat{r}_i).$$

Here $\alpha^{(t)}$ denote the step size at iteration t . The algorithm is shown in Algorithm 1.

3.2 Posterior Regularization

From a probabilistic point of view, the parser model learns parameters θ to realize Eq. (2). During the inference, the model predict a probability distribution $p_\theta(\mathbf{Y}|\mathbf{W})$ over possible parse trees

given a sentence. The posterior regularization algorithm first defines a feasible set of the probability distributions w.r.t the given constraints, and looks for the closest feasible distribution $q^*(\mathbf{Y})$ to the model distribution $p_\theta(\mathbf{Y}|\mathbf{W})$. The best parse tree is given by $\arg \max_{\mathbf{Y}} q^*(\mathbf{Y})$. Specifically, we define the feasible set as:

$$Q = \{q(\mathbf{Y}) | r_i - \theta_i \leq R(C_i, q(\mathbf{Y})) \leq r_i + \theta_i, i \in [N]\},$$

where $R(C, q) = \frac{\sum_k \sum_{(i,j): (k,i,j) \in C^+} q_k(i,j)}{\sum_k \sum_{(i,j): (k,i,j) \in C^+ \cup C^-} q_k(i,j)}$, with $q_k(i, j) = E_{Y \sim q(\mathbf{Y})}[y_k(i, j)]$.

To measure the distance between two distribution, we use the KL-divergence, and find the best feasible distribution $q^*(\mathbf{Y})$:

$$q^*(\mathbf{Y}) = \arg \min_{q \in Q} KL(q(\mathbf{Y}) || p_\theta(\mathbf{Y}|\mathbf{W})). \quad (7)$$

If the feasible set has the expectation form:

$$\{q | \mathbb{E}_{Y \sim q}[\phi(\mathbf{Y})] \leq \mathbf{b}\}, \quad (8)$$

Eq. (7) has a simple close form solution (Ganchev et al., 2010):

$$q^*(\mathbf{Y}) = \frac{p_\theta(\mathbf{Y}|\mathbf{W}) \exp(-\lambda^* \cdot \phi(\mathbf{Y}))}{Z(\lambda^*)}, \quad (9)$$

where λ^* is the solution of

$$\lambda^* = \arg \max_{\lambda \geq 0} -\mathbf{b} \cdot \lambda - \log Z(\lambda), \quad (10)$$

$$Z(\lambda) = \sum_{Y'} p_\theta(Y'|\mathbf{W}) \exp(-\lambda^* \cdot \phi(Y')).$$

In the rest of this section, we first show that the feasible set Q we considered above can be reformulated in the form of Eq. (8), and then we discuss how to solve Eq. (10). To show that the inequality $R(C, q(\mathbf{Y})) \leq r$, in Q can be formulated in the form of Eq. (8), we set

$$\phi_C(\mathbf{Y}) = \sum_{k,i,j} y_k(i, j) \phi_C(k, i, j),$$

and

$$\phi_C(k, i, j) = \begin{cases} 1 - r & (k, i, j) \in C^+ \\ -r & (k, i, j) \in C^- \\ 0 & (k, i, j) \notin C^+ \cup C^- \end{cases} \quad (11)$$

Similarly, we can derive $R(C, q(\mathbf{Y})) \geq r$, into the same form and rewrite Q as

$$Q = \{q(\mathbf{Y}) | \mathbb{E}_{Y \sim q} \phi(\mathbf{Y}) \leq \mathbf{0}\},$$

Algorithm 2 Posterior Regularization

Input: Constraints $\mathcal{C} = \{C_i\}_{i=1}^N$, corresponding ratio $r = \{r_i\}_{i=1}^N$, tolerance margin $\theta = \{\theta_i\}_{i=1}^N$

Output: parse trees \hat{Y}

- 1: $p_\theta(y_k(i, j) = 1) \leftarrow \text{normalize}\left(\exp\left(S_{ij}^{(k)}\right)\right)$
 - 2: $\phi \leftarrow$ defined by Eq. (11)
 - 3: $\lambda_i \leftarrow 0, i \in [N]$
 - 4: **repeat**
 - 5: estimate $\mathbf{g} \leftarrow \partial \log Z(\lambda) / \partial \lambda$ in a batch
 - 6: update λ based on \mathbf{g}
 - 7: **until** MAX_ITER times
 - 8: **for** each (k, i, j) **do**
 - 9: $q_k(i, j) \leftarrow$ defined by Eq. (12)
 - 10: $\hat{Y} \leftarrow$ MAP inference based on q
 - 11: **return** \hat{Y}
-

where $\phi = (\phi_{C_1}, \phi_{C_2}, \dots, \phi_{C_N})$ is a collection of the constraints. The detailed derivations can be found in Appendix A.

We solve Eq. (10) by sub-gradient descent³. Noting that there can be exponential number of terms in $Z(\lambda)$, we firstly need to factorize $Z(\lambda)$ from corpus level to instance level and arc level, and compute the gradient. The technical details are in Appendix A. With the optimal λ^* , we can compute the feasible distribution $q^*(\mathbf{Y})$ given p_θ and \mathbf{W} . Noting that the solution Eq. (9) can also be factorized to arc-level:

$$q_k^*(i, j) \propto p_\theta(y_k(i, j) | \mathbf{w}_k) \exp(-\lambda^* \cdot \phi(k, i, j)), \quad (12)$$

here $q_k^*(i, j)$ denote the arc-level distribution $q^*(y_k(i, j) = 1)$ satisfying Eq. (3). We then do MAP inference based on q , which is actually a minimal spanning tree problem same as before. Algorithm 2 summarizes the process.

4 Experiments

In this section, we evaluate the proposed algorithms by transferring an English dependency parser to 19 target languages covering 13 language families of real low-resource languages. We first introduce the experimental setup including data selection and constraint details and then discuss the results as well as in-depth analysis.

4.1 Setup

Model and Data We train the best performing Att-Graph parser proposed in Ahmad et al. (2019)

³In implementation, we use stochastic gradient descent with Adam optimizer (Kingma and Ba, 2015)

on English and transfer it to 19 target languages in UD Tree Bank v2.2 (Nivre et al., 2018).⁴ The model takes words and predicted POS tags⁵ as input, and achieve transfer by leveraging pre-trained multi-lingual FastText (Bojanowski et al., 2017) embeddings that project the word embeddings from different languages into the same space using an offline transformation method (Smith et al., 2017; Conneau et al., 2018). The SelfAtt-Graph model uses a Transformer (Vaswani et al., 2017) with relative position embedding as the encoder and a deep biaffine scorer (Dozat and Manning, 2017) as the decoder. We follow the setting in Ahmad et al. (2019) to train and tune only on the source language (English) and directly transfer to all the target languages. We modify their decoder to incorporate constraints with the proposed constrained inference algorithms during the transfer phase without retraining the model. All the hyper-parameters are specified in Appendix Table 4 together with hyper-parameters for the inference algorithms in Appendix Table 5.

Constraints We consider two types of constraints: 1) instance-level projective constraints for avoiding creating crossing arcs in the dependency trees, 2) corpus-statistics constraints constructed by the process described in Section 2.2. We consider the following three corpus-statistics constraints: $C1 = (NOUN)$, $C2 = (NOUN, ADP)$, $C3 = (NOUN, ADJ)$; intuitively, $C1$ concerns about the ratio of nouns being on the right of their heads; $C2$ concerns about the ratio of nouns being on the left of adpositions among all noun-adposition arcs; $C3$ concerns about the ratio of nouns being on the left of adjectives among all noun-adjective arcs.

For binary constraints, $C2$ and $C3$ can be directly compiled from WALS feature 85A and 87A respectively. We encode “dominant order” specified in WALS as the ratio being always greater than 0.75 (i.e., $r = 0.875$ and $\theta = 0.125$). If there is no dominant order or the feature is missing, we set $r = 0.5$ and $\theta = 0.25$. Some WALS features like 82A, 83A are also about word order, but we need to specify the arc types to utilize them. For simplicity, we only consider forming constraints from the POS tags in this paper. To estimate the

⁴We make the selection to prioritize the coverage of language families and low resource languages. The language family information can be found in Table 1.

⁵We use predicted POS tags provided in UD v2.2.

Family	Lang.	Features	Baseline	Lagrangian Relaxation			Posterior Regularization		
				Oracle	WALS	Δ WALS	Oracle	WALS	Δ WALS
IE.Germanic	en	1,1,1	90.5	90.3	90.4	-0.1	90.4	90.6	+0.1
IE.Indic	ur	-1,-1,1	18.3	35.2	34.0	+15.7	35.0	33.7	+15.4
IE.Indic	hi	-1,-1,1	34.3	52.4	53.4	+19.1	51.3	49.1	+14.8
Dravidian	ta	-1,-1,1	36.1	42.8	43.4	+7.3	43.1	43.0	+6.9
Turkic	tr	-1,-1,1	31.2	35.2	37.1	+5.9	35.1	36.3	+5.1
Afro-Asiatic	ar	1, 1, -1	38.5	47.3	45.3	+6.8	45.8	43.7	+5.2
Afro-Asiatic	he	1, 1, -1	55.7	58.8	57.6	+1.9	58.3	57.6	+1.9
Austronesian	id	1, 1, -1	49.3	53.1	52.3	+3.0	52.3	51.9	+2.6
Korean	ko	-1,-1,1	34.0	37.1	37.2	+3.2	36.3	36.4	+2.4
IE.Celtic	cy	1, 1, -1	47.3	54.2	51.7	+4.4	53.8	50.0	+2.7
IE.Romance	ca	1, 1, -1	73.9	74.9	73.8	-0.1	74.9	74.7	+0.8
IE.Romance	fr	1, 1, -1	77.8	79.1	78.7	+0.9	79.0	79.0	+1.2
Uralic	et	1, -1,1	65.3	65.5	65.8	+0.5	65.7	66.0	+0.7
Uralic	fi	1, -1,1	66.7	67.1	67.0	+0.3	66.9	67.1	+0.4
IE.Slavic	hr	1, 1, 1	62.2	63.7	63.2	+1.0	63.6	63.4	+1.2
IE.Slavic	bg	1, 1, 1	79.6	79.7	79.2	+0.0	79.7	79.7	+0.1
IE.Baltic	lv	1, 1, 1	70.3	70.7	69.5	-0.8	70.5	69.9	-0.4
IE.Latin	la	?, ?, ?	47.4	48.0	45.6	-1.8	48.1	47.3	-0.1
IE.Germanic	da	1, 1, 1	76.6	76.6	76.5	-0.1	76.6	76.6	+0.0
IE.Germanic	nl	0, 1, 1	67.5	67.6	67.5	+0.0	67.9	67.9	+0.4
Average Performance			54.3	58.4	57.8	+3.5	58.1	57.5	+3.1

Table 1: Cross-lingual transfer performances for dependency parsing on 19 languages from 13 different families, with the performance on the source language (English) as a reference. Performances are reported per UAS (we observe similar trends for LAS and details can be found in the appendix Table 7). We compare the baseline model (Ahmad et al., 2019) with our two algorithms (Lagrangian relaxation and posterior regularization) considering the oracle constraints, and the corpus-statistics constraints compiled from WALS. Columns Δ WALS denote the improvements bring by leveraging WALS feature as constraints. We also create a Features column to show three WALS features [83A,85A,87A] for each language. The values {1, -1, 0, ?} stand for the same as English, opposite to English, no dominant order, and feature missing, respectively.

ratio for unary constraint $C1$, we use the WALS features 82A, 83A, 85A, 86A, 87A, 88A, 89A that are related to *NOUN* to form feature vectors, and do regression on languages in the test set except the target language to predict the constraint ratio. The process guarantees the target language remain unseen during the ratio estimation process. The ratios on the regression training languages are estimated by sampling 100 sentences in the training set per language.

We also consider an oracle setting where we collect a “ground-truth” ratio of each constraint for the target language to estimate an upper bound of our inference algorithms. In the oracle setting, we estimate the ratio on the whole training corpus of the target language and set the margin to $\theta = 0.01$.

4.2 Parsing Performances

We first compare the performances of the cross-lingual dependency parser with or without con-

straints. Table 1 illustrates the results for the 19 target languages we selected,⁶ along with the performance on the source language (English). The performance on English is not as high as the dependency parsers specialized for English, because to achieve transfer, we have to freeze the pre-trained multi-lingual word embeddings. Yet this parser achieved the best single-source transfer performances according to Ahmad et al. (2019).

As is shown in Table 1, the improvements by our constrained inference algorithms are dramatic in a few languages that have very distinct word order features from the source language. For example, the parsing performance of Hindi (hi) improves about 15% in UAS with WALS features via both Lagrangian relaxation and posterior regularization inference. The improvements are less

⁶We also run on all languages in Ahmad et al. (2019) for completeness and observe similar trends. The results can be found in Appendix Table 7.

obvious for languages that are in the same family as English such as Danish(da) and Dutch(nl). This is expected as the corpus linguistic statistics of these languages are similar to English thus the constraints are mostly satisfied with the baseline parser. Comparing Lagrangian relaxation and posterior regularization, we find posterior regularization being more robust and less sensitive to the errors in the corpus-statistics estimation, while Lagrangian relaxation gives a higher improvement on average. Overall, the two proposed constrained inference algorithms improved the transfer performance by 3.5% and 3.1% per UAS on average on 19 target languages.

For languages like Finnish (fi) and Estonian (et), the WALs setting works even better than the oracle. We suspect the reason being the large margin we set in the WALs setting. When the estimated corpus-statistics is different from the real ratio in the test set, the large margin relaxes the constraints, thus could result in better performances.

Discussion. Despite the major experiments and analysis are conducted using English as the only source language, our approach is general and does not have restriction on the choice of the source language(s). To verify this claim, we run experiments with Hebrew as the source language. Under the oracle setting, Lagrangian relaxation and posterior regularization improve the baseline by 4.4% and 4.1%, respectively.

We observed that if we compile WALs features into hard constraints (i.e., set $r = 0$ or 1), the constraint inference framework only improves performance on half of the languages. For example, in Estonian (et), the performance *drops* about 3%. This is because WALs only provides the dominant order. Therefore, treating WALs as hard constraints introduces error to the inference.

Finally, we assume if we can access to native speakers, the corpus-statistics can be estimated by a few partial annotations of parse trees. In our simulation, using less than 300 arcs, we can achieve the same performance as using the oracle.

4.3 Contributions of Individual Constraints

We analyze the contribution of each constraint demonstrated in Table 2. Here we use the oracle setting to reduce the noise introduced by corpus-statistics estimation errors. The results are based on Lagrangian relaxation inference. As shown in Table 2, Despite some languages have

Model	UAS	coverage	Δ
baseline	54.3	N/A	N/A
+Proj.	54.6	N/A	+0.3
+Proj.+C1	57.0	0.24	+2.4
+Proj.+C2	55.7	0.08	+1.1
+Proj.+C3	55.0	0.07	+0.4
oracle	58.4	N/A	+4.1

Table 2: Ablation study: average UAS of baseline model with different sets of constraints. Proj. represent projective constraints. C1-C3 and oracle are introduced in 4.1. The improvements for projective constraint and oracle are compared to baseline. For the other three constraint sets the improvement is compared to model with projective constraint.

Const.	statistics	improvement
+Proj.	N/A	+0.1
C1	0.30/0.36/0.94	+6.9
C2	0.00/0.06/1.00	+11.3
C3	0.14/0.27/0.12	+0.5
All	N/A	+18.1

Table 3: Contribution of individual constraints and their statistics in Hindi. The second column lists the ratios estimated from oracle in English/ baseline in Hindi/ oracle in Hindi, respectively. The improvement is measured in UAS. The improvement of constraints is computed same as Table 2

non-projective dependencies, we observed performance improvements on almost all the languages when the projective constraint is enforced. All the constraints we formulated have positive contributions to the performance improvements. C1 = (NOUN) brings the largest gain probably because its widest coverage.

Table 1 shows that the performance of Hindi improves from 34% to over 51% per UAS for both inference algorithms. To better understand where the improvements come from, we conduct an analysis to breakdown the contribution of each individual constraint for Hindi. Table 3 shows the results. We can see that since the corpus linguistic statistics between Hindi and English are distinct, the baseline model only achieves low performance. With the constrained inference, especially the postposition constraint (C2), the proposed inference algorithm bring significant improvement.

To verify the effectiveness of the constraints, we analyze the relation between the performance improvements and corpus statistics ratio gaps between the source and the target languages. To quantify the ratio gap, we weight constraints by

their coverage rate and compute the weighted average of the ratio difference between source and target languages. Results show that the performance improvement is highly related to the ratio gap. The Pearson Correlation Coefficient is 0.938. The figure showing the correlation between performance gap (as per UAS) and the corpus statistics ratio gap is in the Appendix Figure 3.

5 Related Work

Cross-Lingual Transfer for Parsing Many approaches have been developed to transfer a dependency parser. However, they mainly focus on better capture information from the source language(s). McDonald et al. (2011); Guo et al. (2016); Täckström et al. (2013); Chen et al. (2019) consider transferring a parser trained on multiple source languages. Agić (2017); Lin et al. (2019) selects good source languages by comparing part-of-speech tags sequences. Søgaard (2011); Täckström et al. (2013) chooses suitable data points from the source language. Pires et al. (2019) uses multilingual BERT to leverage language features from multiple languages. Ahmad et al. (2019) design an order-free model to take out the order features from the source language. Xiao and Guo (2014); Guo et al. (2015) learn an alignment from source words to target words. Ponti et al. (2018) learn an anisomorphism from the source parsing tree to target. Rasooli and Collins (2019) reorder the source data before training. In contrast, we focus on incorporating linguistic properties in the target languages.

Constrained Inference for Parsing Several previous studies show that adding constraints in inference time improves the performance of models. Grave and Elhadad (2015) consider incorporating constraints to promote popular types of arcs in an unsupervised setting. Naseem et al. (2010); Li et al. (2019) train a parser with constraints compiled from the frequency of particular arcs. Compared with the previous work, we focus on cross-lingual transfer with word order constraints.

Finally, prior studies have noticed that the word order information is significant for parsing and use it as features (Ammar et al., 2016; Naseem et al., 2012; Rasooli and Collins, 2017; Zhang and Barzilay, 2015; Dryer, 2007). Täckström et al. (2013) further propose to decompose these features from models for adapting target languages. Wang and Eisner (2018a) use the statistics of sur-

face part-of-speech (POS) tags of target languages to learn the word order. Wang and Eisner (2018b) use POS tags of target languages together with a similar language, and design a stochastic permutation process to synthetic the word order. However, none of them consider using the word order features as constraints.

Incorporating Constraints In NLP Tasks

Constraints are widely incorporated in variety of NLP tasks. To name a few, Roth and Yih (2004) propose to formulate constrained inferences in NLP as integer linear programming problems. To solve the intractable structure, Rush and Collins (2012) decompose the structure and incorporate constraints on some composite tasks. To improve the performance of a model, Chang and Collins (2011); Peng et al. (2015) incorporate constraints on exact decoding tasks and inference tasks on graphical models, and Chang et al. (2013); Dalvi (2015); Martins (2015) incorporate corpus-level constraints on semi-supervised multilabel classification and coreference resolution. Zhao et al. (2017) incorporate corpus-level constraints to avoid amplifying gender bias on visual semantic role labeling and multilabel classification. In contrast to previous work, we incorporate corpus-level constraints to facilitate dependency parser in the cross-lingual transfer setting.

6 Conclusion

We propose to leverage corpus-linguistic statistics to guide the inference of cross-lingual dependency parsing. We compile these statistics into corpus-statistic constraints and design two inference algorithms on top of a graph-based parser based on Lagrangian relaxation and posterior regularization. Experiments on 19 languages show that our approach improves the performance of the cross-lingual parser substantially. In the future, we plan to study the design and incorporation of fine-grained constraints considering multiple languages for cross-lingual transfer. We also plan to adapt this constrained inference framework to other cross-lingual structured prediction problems, such as semantic role labeling.

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