

Capacity and Outage of Terahertz Communications with User Micro-mobility and Beam Misalignment

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Abstract—User equipment mobility is one of the primary challenges for the design of reliable and efficient wireless links over millimeter-wave and terahertz bands. These high-rate communication systems use directional antennas and therefore have to constantly maintain alignment between transmitter and receiver beams. For terahertz links, envisioned to employ radiation patterns of no more than few degrees wide, not only the macro-scale user mobility (human walking, car driving, etc.) but also the micro-scale mobility – spontaneous shakes and rotations of the device – becomes a severe issue. In this paper, we propose a mathematical framework for the first-order analysis of the effects caused by micro-mobility on the capacity and outage in terahertz communications. The performance of terahertz communications is compared with and without micro-mobility illustrating the difference of up to 1 Tbit/s or 75%. In response to this gap, it is finally shown how the negative effects of the micro-mobility can be partially addressed by a proper adjustment of the terahertz antenna arrays and the period of beam realignment procedure.

I. INTRODUCTION

While the commercial fifth-generation (5G) mobile networks exploiting millimeter wave (mmWave) band are expected to appear within the next few years [1], the researchers started targeting Terahertz (THz, 300 GHz–3 THz) band communications as a technology enabler for novel 6G and beyond applications [2], [3]. The sub-millimeter wavelength of THz frequencies promises ultra-large antenna arrays featuring thousands of elements at both transmitter and receiver sides [4]. These arrays will be capable of creating extremely directional steerable antenna radiation patterns with the beamwidth of just a few degrees or even less. The later feature allows to overcome severe path loss and atmospheric absorption at THz frequencies and maintain adequate levels of signal-to-noise ratio (SNR) at the distances of up to a few tens of meters [5].

On the negative side, the use of very narrow THz radiation patterns in mobile communications challenges the accuracy and speed of the employed beam steering procedures to follow the nodes mobility. For handheld and wearable THz devices, not only the conventional macro-mobility (human walking, car driving, etc.) but also the much less predictable micro-mobility (small-scale shakes and rotations) have to be considered [6], [7]. These fast displacements of the mobile THz user equipment (THz-UE) may cause frequent misalignments of the highly-directional THz beams, consequently leading to possible outages and degradation of the link capacity [8].

The topic has been partially studied to date. The capacity of a THz link with a fixed beam misalignment was evaluated in [9]. Then, Priebe et al. [10] performed ray-based simulations to explore the impact of typical human mobility on indoor THz

systems. Approaches to analytically model the effect have been proposed, among others, in [11] and [12]. Both works study a snapshot of the network, where the current misalignment is modeled as a random variable. An indoor network with a THz access point (THz-AP) and walking human users has been simulated in [8] and [13]. An enhanced solution to maintain the mmWave beam alignment in the presence of micro-mobility has been presented in [14]. The joint beam alignment and rate control algorithm for mmWave networks has been delivered in [15]. Finally, Hur et al. [6] modeled the mmWave backhaul links with 2D mobility caused by the wind, however, no rotations have been considered.

Summarizing, no mathematical framework quantifying the effect of the THz-UE micro-mobility (both displacements and rotations) on the mobile THz communications has been reported to date. We address this gap in the present article. The main contributions of this work are:

- To estimate the achieved capacity and fraction of time in outage of a THz link as a function of THz-UE micro-mobility parameters and antenna array characteristics, a unified mathematical framework is proposed based on probability and random walk theories.
- To numerically characterize the system performance when accounting for the THz-UE micro-mobility, a mathematical methodology is employed. It is particularly shown that the capacity of the THz link can decrease by up to 75% in the presence of THz-UE micro-mobility. It is also demonstrated that a proper adjustment of the antenna array sizes using our framework results in up to 500 Gbit/s capacity improvement.

II. SYSTEM MODEL

1) Deployment and Propagation Model: We consider a single link between a stationary THz-AP and a handheld THz-UE separated by d meters (see Fig. 1). To model the narrow THz beams, we assume that both THz-AP and THz-UE are equipped with 2D antenna arrays of $N_A \times N_A$ and $N_U \times N_U$ ($N_A \gg N_U$) elements generating 3D sectorized antenna radiation patterns with the gains of $G_A = N_A^2$, $G_U = N_U^2$. The corresponding antenna radiation pattern angles for THz-AP and THz-UE are approximated as $\alpha = \frac{102\pi}{180N_A}$ and $\beta = \frac{102\pi}{180N_U}$ [16].

We employ a THz-specific propagation model from [5]. According to it, the SNR at the THz-UE, S_U , is written as

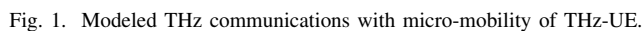
$$S_U = P_A G_A G_U \frac{c^2}{16\pi^2 f^2 N_0(B)} d^{-2} e^{-Kd}, \quad (1)$$

where f is the carrier frequency, B is the bandwidth, K is an absorption coefficient for the band, $N_0(B)$ is the noise level.

2) Micro-mobility Model: The micro-mobility of the THz-UE is modeled as a combination of random displacements processes over OX and OY axis in Fig. 1, $x(t)$ and $y(t)$, together with the random rotation processes $\phi(t)$ and $\theta(t)$.

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In the following section, we present our mathematical framework to analyze and compare the characteristics of these schemes in the presence of THz-UE micro-mobility. For simplicity, we assume that the detection of outage (beam misalignment) is instantaneous. However, the framework can be further extended to account for non-zero time to detect an outage by introducing an additional component in T_B .

3) *Micro-mobility $\phi(t)$ and $\theta(t)$* : We now include angular mobility in our analysis. The misalignment caused by rotations happens when THz-AP appears outside of the turning THz-UE beam. In general, the particular angle that THz-UE has to turn over ϕ and θ to cause misalignment depends on the current location of the THz-UE, $x(t)$ and $y(t)$. At the same time, for any current Δx and Δy , the bounding angle $M_{\phi\theta}$ is $M_{\phi\theta} \in [\frac{\beta}{2} - \frac{\alpha}{2}, \frac{\beta}{2} + \frac{\alpha}{2}]$, $\alpha = \frac{102\pi}{180\Omega_A}$, $\beta = \frac{102\pi}{180\Omega_U}$ (see Fig. 1).

$$f_{T_A}(t) = \frac{\frac{e^{-\frac{(\log(t)-\mu_x)^2}{2\sigma_x^2}}}{\sigma_x} \left[2 - \operatorname{erfc}\left(\frac{\mu_x - \log(t)}{\sqrt{2}\sigma_x}\right)\right] + \frac{e^{-\frac{(\log(t)-\mu_y)^2}{2\sigma_y^2}}}{\sigma_y} \left[2 - \operatorname{erfc}\left(\frac{\mu_y - \log(t)}{\sqrt{2}\sigma_y}\right)\right]}{2\sqrt{2\pi} \left[1 - \frac{1}{2}\operatorname{erfc}\left(\frac{\mu_x - \log(t)}{\sqrt{2}\sigma_x}\right) + \frac{1}{2}\operatorname{erfc}\left(\frac{\mu_y - \log(t)}{\sqrt{2}\sigma_y}\right)\right]} + \frac{\frac{e^{-\frac{(\log(t)-\mu_\phi)^2}{2\sigma_\phi^2}}}{\sigma_\phi} \left[2 - \operatorname{erfc}\left(\frac{\mu_\phi - \log(t)}{\sqrt{2}\sigma_\phi}\right)\right] + \frac{e^{-\frac{(\log(t)-\mu_\theta)^2}{2\sigma_\theta^2}}}{\sigma_\theta} \left[2 - \operatorname{erfc}\left(\frac{\mu_\theta - \log(t)}{\sqrt{2}\sigma_\theta}\right)\right]}{2\sqrt{2\pi} \left[1 - \frac{1}{2}\operatorname{erfc}\left(\frac{\mu_x - \log(t)}{\sqrt{2}\sigma_x}\right) + \frac{1}{2}\operatorname{erfc}\left(\frac{\mu_y - \log(t)}{\sqrt{2}\sigma_y}\right)\right]} \quad (8)$$

As $N_A \gg N_U$, the first term dominates, and the range is relatively small. For clarity, we use an upper bound on $M_{\phi\theta}$, $M_{\phi\theta} = \frac{102\pi}{360}(1/N_U + 1/N_A)$, so when either $\phi(t)$ or $\theta(t)$ reaches $\pm M_{\phi\theta}$, the alignment is lost. We can, finally, characterize the FPT pdfs for $\phi(t)$ and $\theta(t)$ – $f_\phi(t)$ and $f_\theta(t)$ – using (3), while $f_{T_{\phi,\theta}}(t)$ is obtained as a minimum of these two RVs.

4) *Aggregated micro-mobility*: Let us define T_A as an RV representing the FPT for reaching any of the boundary conditions $\pm M_{XY}$ or $\pm M_{\phi\theta}$. Now, we characterize $f_{T_A}(t)$ – the pdf of this FPT – as the minimum of two RVs, i.e.,

$$f_{T_A}(t) = f_{T_{X,Y}}(t)[1 - F_{T_{\phi,\theta}}(t)] + f_{T_{\phi,\theta}}(t)[1 - F_{T_{X,Y}}(t)]. \quad (6)$$

While the sought pdf can be precisely calculated, the resulting equation involves *quadruple infinite sums* over n resulting in high computational complexity. At the same time, despite the fact that the pdf $f_X(t)$ has a complex expression, the mean and variance of the FPT are finite and equal to $M_{XY}^2/2D_X$ and $M_{XY}^4/6D_X^2$, respectively [19]. Therefore, recalling that the FPT to $\pm M_{XY}$ with individual micro-mobility component can be well approximated with Lognormal distribution featured by the same first moments [19], [20]¹, with the use of (5) we have

$$f_{T_{X,Y}}(t) = \frac{1}{2\sqrt{2\pi}\sigma_x\sigma_y t} \left[\sigma_x e^{-\frac{(\mu_x - \log(t))^2}{2\sigma_x^2}} \left[\operatorname{erf}\left(\frac{\mu_x - \log(t)}{\sqrt{2}\sigma_x}\right) + 1 \right] + \sigma_y e^{-\frac{(\mu_y - \log(t))^2}{2\sigma_y^2}} \left[\operatorname{erf}\left(\frac{\mu_y - \log(t)}{\sqrt{2}\sigma_y}\right) + 1 \right] \right], \quad t > 0, \quad (7)$$

where $\mu_x = \log(\frac{2M_{XY}}{\Delta x}) - \frac{1}{2}\log(\frac{5}{3})$, $\mu_y = \log(\frac{2M_{XY}}{\Delta y}) - \frac{1}{2}\log(\frac{5}{3})$, $\sigma_x = \sigma_y = \sqrt{\log(5/3)}$, and also $\mu_\phi = \log(\frac{2M_{\phi\theta}}{\Delta\phi}) - \frac{1}{2}\log(\frac{5}{3})$, $\mu_\theta = \log(\frac{2M_{\phi\theta}}{\Delta\theta}) - \frac{1}{2}\log(\frac{5}{3})$, $\sigma_\phi = \sigma_\theta = \sqrt{\log(5/3)}$.

Now, to determine the PFT for the aggregated mobility we apply (6) to arrive at (8), where $\operatorname{erfc}(\cdot)$ is the complementary error function, while cdfs $F_{T_{X,Y}}(t)$ and $F_{T_{\phi,\theta}}(t)$ are obtained by integrating the corresponding pdfs.

B. THz Link Metrics with Micro-Mobility

Once the random time the aggregated micro-mobility of THz-UE leads to beam misalignment, T_A , is characterized, we proceed with deriving the THz link metrics of interest. We particularly obtain: (i) the fraction of time THz-UE is in outage, including the time spent for the beam realignment; (ii) the mean spectral efficiency (SE) and capacity of the THz link; and (iii) the mean time to the first beam misalignment caused by the micro-mobility of THz-UE.

1) *Scheme 1*: Consider first the scheme, where the beam alignment procedure is only invoked when THz-UE gets to an

outage condition. The fraction of link outage time is $p_{O,1} = T_B/(T_A + T_B)$, where T_B is the duration of the beam alignment procedure. Using law of the unconscious statistician we have

$$p_{O,1} = \int_0^\infty \frac{T_B}{t + T_B} f_{T_A}(t) dt. \quad (8)$$

To obtain mean spectral efficiency (SE) and capacity of the THz link, $E[L_1]$ and $E[C_1]$ ², we recall that both are zero for $p_{O,1}$ and determined by S_U from (1) for the rest of the time as

$$L_{\max} = \log_2(1 + S_U), \quad C_{\max} = B \log_2(1 + S_U), \quad (9)$$

where L_{\max} and C_{\max} represent the SE and link capacity, respectively, when the beams are aligned.

The mean SE and capacity with *Scheme 1* thus are

$$E[L_1] = (1 - p_{O,1})L_{\max}, \quad E[C_1] = (1 - p_{O,1})C_{\max}. \quad (10)$$

Finally, the mean time to the first beam misalignment is

$$E[T_1] = \int_0^\infty f_{T_A}(t) dt. \quad (11)$$

2) *Scheme 2*: We now study the second scheme, where beam alignment is invoked after a fixed interval T_U . Here, $T_{O,2}$ – the outage duration in a period $T_U + T_B$ – depends on whether the time to misalignment is greater or smaller than T_U :

$$T_{O,2} = \begin{cases} \frac{T_B}{T_U + T_B}, & T_A \geq T_U, \\ \frac{T_U + T_B - T_A}{T_U + T_B}, & T_A < T_U. \end{cases} \quad (12)$$

The probability $\Pr\{T_A < T_U\}$ is directly obtained as

$$\Pr\{T_A < T_U\} = \int_0^{T_U} f_{T_A}(t) dt = F_{T_A}(T_U). \quad (13)$$

The conditional pdf of the time to misalignment provided that it is less than T_U is $f_{T_A}(t)/F_{T_A}(T_U)$. Now, the fraction of time in outage, $p_{O,2}$, can be obtained by weighting the means of two fractions in (12) as

$$p_{O,2} = \frac{T_B[1 - F_{T_A}(T_U)]}{T_U + T_B} + \int_0^{T_U} \frac{T_U + T_B - t}{T_U + T_B} f_{T_A}(t) dt. \quad (14)$$

The SE and capacity of the THz link with *Scheme 2* are

$$E[L_2] = (1 - p_{O,2})L_{\max}, \quad E[C_2] = (1 - p_{O,2})C_{\max}, \quad (15)$$

where L_{\max} and C_{\max} are given in (9).

In contrast to *Scheme 1*, the mean time to the first beam misalignment, $E[T_2]$ in this case can be longer than T_A . Observing that T_2 consist of several consecutive intervals of duration $T_U + T_B$ plus a fraction of the last interval where the actual misalignment will happen, we arrive at

$$E[T_2] = \frac{1 - F_{T_A}(T_U)}{F_{T_A}(T_U)} (T_U + T_B) + \frac{1}{F_{T_A}(T_U)} \int_0^{T_U} t f_{T_A}(t) dt. \quad (16)$$

IV. NUMERICAL RESULTS

In this section, our derived results are numerically elaborated. Following the recent IEEE standard for wireless communications over low-THz band [21], we assume $f = 0.3$ THz, $B = 50$ GHz, and $P_A = 20$ dBm. The THz beam steering delay,

² $E[X]$ stands for the mean value of X .

¹To check the proposed approximation, we have utilized the original distribution specified in (3) and the approximating Lognormal distribution to generate samples of equal size and then performed statistical chi-square test. The hypothesis H_0 was that both samples belong to the same distribution against an alternative hypothesis, H_1 , that the distributions differ. With the level of significance set to $\alpha = 0.05$ the test shows that for the ranges of input parameters considered in the paper samples drawn from original distribution and the approximating one belong to the same distribution.

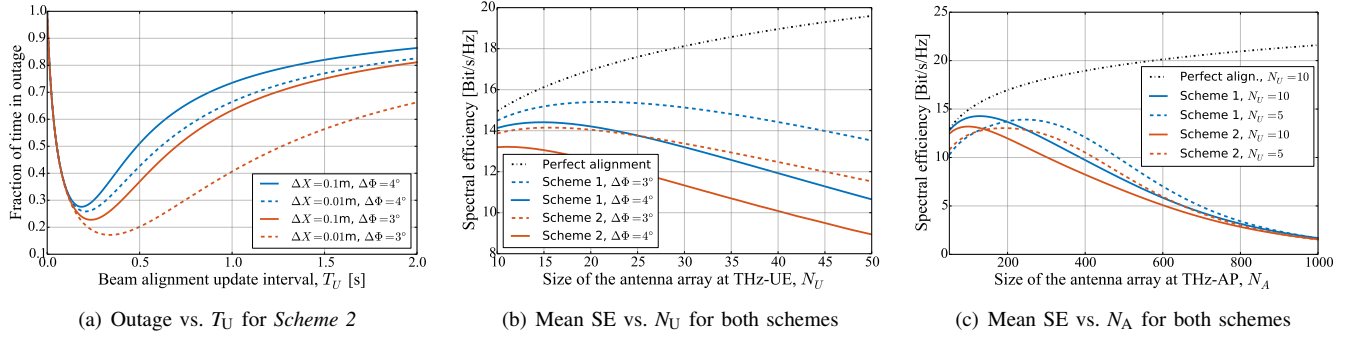


Fig. 2. Adjustment of T_U , N_U , and N_A for the considered levels of THz-UE micro-mobility.

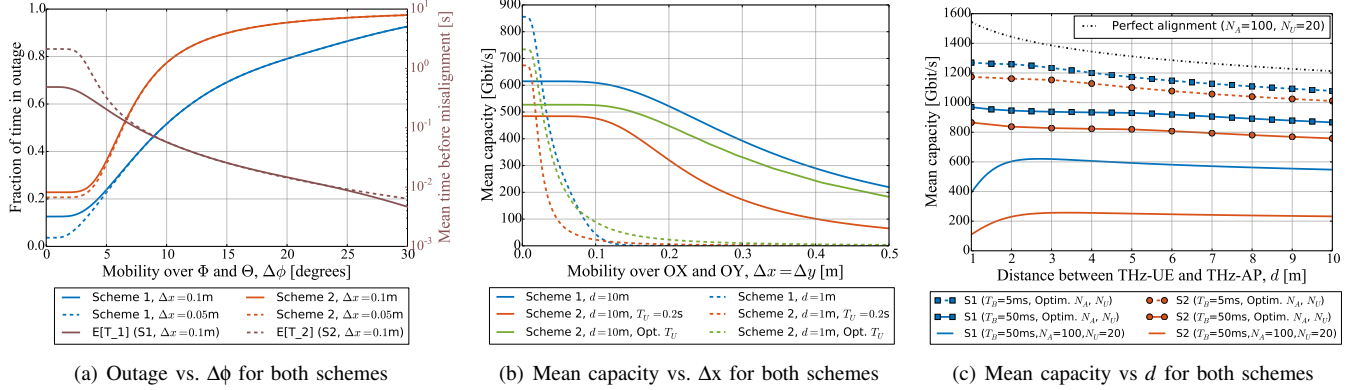


Fig. 3. The impact of THz-UE micro-mobility on the outage- and capacity-centric characteristics.

δ , is set to 5 mcs. To better contrast the impact of Cartesian and angular micro-mobility, we assume $\Delta x = \Delta y$ and $\Delta\phi = \Delta\theta$. For illustrative purposes, we also take certain representative values for Δx and $\Delta\phi$ from the measurement campaign reported in [7]. Specifically, $\Delta x = 0.1\text{ m}$ and $\Delta\phi = 4^\circ$ is typical for playing a dynamic game on a smartphone, while $\Delta x = 0.01\text{ m}$; $\Delta\phi = 3^\circ$ correspond to the video watching scenario.

1) *The effect of the beam realignment period, T_U :* We start with Fig. 2(a) presenting the fraction of time in outage versus T_U for Scheme 2. Here, we observe that too low value of T_U results in the system spending most of its time performing beam realignment, while too rare updates ($T_U > 1\text{ s}$) also lead to degraded performance. There is an “optimal” T_U for each of the configurations and its typical value lies within ≈ 200 – 300 ms and decreases with the level of micro-mobility.

2) *The effect of the antenna array size at THz-UE, N_U :* We now proceed with Fig. 2(b) illustrating the impact of N_U on the SE of the THz link when $N_A = 100$ and $\Delta x = 0.1\text{ m}$. For Scheme 2, the “optimal” values of T_U derived from Fig. 2(a) are employed. In this figure, we notice that even relatively low levels of angular micro-mobility, $\Delta\phi = 3^\circ$, lead to up to 70% reduction in SE versus the theoretical limit for $N_U = 50$.

One may also identify an optimization problem since greater N_U improves the SE during the actual data transmission, but simultaneously challenges the beam alignment. Particularly, Scheme 1 achieves the highest performance with $N_U = 21$ for $\Delta\phi = 3^\circ$ and with $N_U = 15$ for $\Delta\phi = 4^\circ$. The greater level of angular mobility makes the lower N_U preferable and decreases the maximum SE: 15.4 bit/s/Hz vs. 14.4 bit/s/Hz . Similar trends are observed for Scheme 2. We finally notice that Scheme 1 slightly outperforms Scheme 2 maintaining a maximum SE of approximately 1 bit/s/Hz higher.

3) *The effect of the antenna array size at THz-AP, N_A :* We continue our investigations with Fig. 2(c) presenting the mean SE as a function of N_A . Similar observations to those from Fig. 2(b) are made. We also notice that the chosen N_U affects the “optimal” value of N_A (and vice versa). Particularly, for Scheme 2, SE maximizes at $N_A = 190$ with $N_U = 5$ and at $N_A = 100$ with $N_U = 10$. Therefore, in order to maximize the SE N_A and N_U have to be optimized jointly for every set of micro-mobility characteristics. The figure also illustrates that ultra-massive antenna arrays ($N_A \approx 1024$, as in [4]) are currently irrelevant for mobile systems as they invoke both low active time, T_A , and high overheads on T_B .

4) *The effect of angular micro-mobility, $\Delta\phi$:* Fig. 3(a) illustrates the fraction of time in outage (left axis) and the mean time to the first misalignment (right axis) as functions of $\Delta\phi$. N_A is set to 100 and N_U – to 20. We start with the fraction of time in outage. For both schemes, there is a regime, $\Delta\phi < 3^\circ$, where the curves are flat as with low $\Delta\phi$ the system performance is mainly limited by the cartesian micro-mobility, so the minor changes in $\Delta\phi$ do not have any notable impact.

In contrast, when $\Delta\phi > 10^\circ$, the impact of angular mobility dominates. Consequently, the curves for $\Delta x = 0.1\text{ m}$ and $\Delta x = 0.01\text{ m}$ are similar for both schemes. We also note that Scheme 1 outperforms Scheme 2 in terms of the fraction of time in outage. The opposite trend is observed for the right axis, where $E[T_2] > E[T_1]$ for all the values of $\Delta\phi$. The gain is the most visible for $\Delta\phi < 4^\circ$.

5) *The effect of Cartesian mobility, Δx :* We continue studying the implications of micro-mobility on THz link with Fig. 3(b) presenting the mean link capacity as a function of Δx when $N_A = 100$ and $N_U = 20$. Here, for $d = 10\text{ m}$ we observe similar effect as in Fig. 3(a): the small values of Δx (e.g., $\Delta x < 0.1\text{ m}$) do not have immediate implications on the metric,

as the system is primarily limited by a relatively high $\Delta\phi = 6^\circ$.

At the same time, for $d = 1$ m this effect is no longer present as the beam generated by THz-AP at 1 m distance is less than 2 cm wide. Consequently, even very small drifts caused by cartesian micro-mobility lead to immediate degradation in capacity (e.g., from 850 Gbit/s at $\Delta x = 0.02$ m to 50 Gbit/s at $\Delta x = 0.1$ m for Scheme 1). So, it is especially important to account for cartesian micro-mobility at short distances.

We, finally, bring the attention to comparing Scheme 2 when $T_U = 0.2$ with Scheme 2 when T_U is numerically optimized for each of the Δx values following the approach from Fig. 2(a). We observe the second system notably outperforming the first one for the entire range of Δx and for both considered separation distances, d . With this comparison, we emphasize the importance of accounting for micro-mobility in THz communications and optimizing the system parameters for an envisioned pattern of micro-mobility, whenever feasible.

6) *The effect of beam realignment time, T_B* : We continue our discussion on the necessity of system optimization accounting for the micro-mobility pattern with Fig. 3(c). This figure demonstrates the maximum achievable capacity of a THz link when all the flexible parameters – N_A , N_U , and T_U – are jointly optimized following the effects in Fig. 2.

Two major observations are made from this figure. First, the curves for $T_B = 50$ ms are ≈ 350 Gbit/s lower than the ones for $T_B = 5$ ms. So, the design of reliable and efficient procedure for beam realignment is of crucial importance for mobile THz communications. Secondly, there is a 0.6–1.1 Tbit/s difference between the theoretical curve and those for practical $T_B = 50$ ms (corresponds to $N_A = 100$, $N_U = 20$, and $\delta = 5$ ms). Thus, it is important to account for micro-mobility in performance evaluation of mobile THz systems. Ignoring this factor results in severe overestimation of the achievable data rates.

Finally, we compare the performance of Schemes 1 and 2 with $T_B = 50$ ms and optimized N_A , N_U when $T_B = 50$ ms, $N_A = 100$, and $N_U = 20$. As seen from Fig. 3(c), the former one provides up to *half of a Tbit/s* greater capacity. The gain is especially visible at $d < 2$ m, where cartesian micro-mobility results in worse SE for smaller distances despite the lower pathloss. The latter observation confirms the need to account for THz-UE micro-mobility not only in performance studies, but also in the design of the transceivers for prospective THz mobile communications.

V. CONCLUSIONS

In this paper, we proposed a mathematical framework to estimate the performance of THz communications in the presence of both Cartesian and angular micro-mobility of the THz-UE. Our study revealed that: (i) the micro-mobility of THz-UE may decrease the capacity of the THz link by hundreds of Gbit/s; (ii) the Cartesian micro-mobility is more harmful at shorter distances, when d is around few meters, while the impact of angular one is more visible at longer ones; (iii) on-demand beam alignment procedure leads to 10–15% higher spectral efficiency than periodic beam alignment. The framework can be tuned for other micro-mobility patterns (autonomous driving, UAV networks, etc.) by replacing $f_{T_A}(t)$ in (8) without any modifications in the further analysis. It can

also be further extended to analyze the enhanced beam management procedures, e.g., those reported in [14], [15]. We plan to rely on this framework in the future when developing our end-to-end THz communication system with micro-mobility.

There are several important practical outcomes of our study. First of all, it is shown that the periodic beam realignment procedure (Scheme 2) must be performed every 100 ms–300 ms depending on the system parameters to maximize the link capacity. It is also revealed that optimizing T_U using our framework allows for up to 200% lower fraction of time in an outage. Secondly, it is illustrated that a too high number of antenna elements on either THz-AP or THz-UE decreases the link performance. In contrast, when one selects the number of antenna elements using the contributed framework, it becomes possible to improve the capacity of the THz link by as high as 500 Gbit/s. Finally, the framework also enables determining the specific numerical requirements for the beam realignment time and THz beam steering delay, thus providing the necessary insights for the design of the prospective hardware for future mobile THz systems.

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