Electromagnetic precursors to gravitational wave events:

Numerical simulations of flaring in pre-merger binary neutron star magnetospheres

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ABSTRACT

The detection of gravitational waves from neutron star merger events has opened up a new field of multi-messenger astronomy linking gravitional waves events to short-gamma ray bursts and kilonova afterglows. A further - yet to be discovered - electromagnetic counterpart is precursor emission produced by the non-trivial interaction of the magnetospheres of the two neutron stars prior to merger. By performing special-relativistic force-free simulations of orbiting neutron stars we discuss the effect of different magnetic field orientations and show how the emission can be significantly enhanced by differential motion present in the binary, either due to stellar spins or misaligned stellar magnetospheres. We find that the build-up of twist in the magnetic flux tube connecting the two stars can lead to the repeated emission of powerful flares for a variety of orbital configurations. We also discuss potential coherent radio emission mechanisms in the flaring process.

Keywords: gravitational waves — gamma-ray burst: general — stars: neutron

1. INTRODUCTION

Possessing some of the highest densities and strongest magnetic fields in the universe neutron stars are an ideal tool to study strong gravity, nuclear physics and high-energy plasma physics alike. multi-messenger observation of the neutron star merger GW170817 has demonstrated how the different observational channels (gravitational waves, kilonova afterglow and short gamma-ray burst) can be used to constrain the properties of neutron stars, e.g. their masses, radii and, in turn, nuclear physics beyond saturation (Abbott et al. 2018; Most et al. 2018b; De et al. 2018; Raithel 2019). While the observed electromagnetic counterparts have all been emitted following the merger, the presence of strong magnetic field configurations in radio pulsars indicates that the magnetospheres of the two stars might interact non-trivially prior to the merger. Even if the two neutron stars themselves would have inactive magnetospheres due to the spin-down over their long lifetime, the interaction of the two stars can reignite pair creation and establish a nearly force-free (Goldreich

& Julian 1969) magnetosphere filled with pair plasma at the time of merger (Lyutikov 2019b). This scenario has been shown analytically to dissipate electromagnetic energy either in terms of a unipolar inductor scenario (Lai 2012; Piro 2012), where one of the stars has a higher magnetic field than its companion and also in the case of comparable magnetization (Hansen & Lyutikov 2001; Lyutikov 2019b). In addition this scenario has also been invoked to drive powerful fireballs (Metzger & Zivancev 2016) and Fast Radio Bursts (FRBs) (Wang et al. 2016). Since the highly dynamical electromagnetic field configurations present in the inspiraling binary are too involved to be studied using purely analytical approaches a few numerical studies have been performed in order to study force-free magnetospheric interactions, either in binary black hole mergers (Alic et al. 2012; Palenzuela et al. 2010), in neutron star binaries (Palenzuela et al. 2013b,a; Ponce et al. 2014), in mixed binaries (Paschalidis et al. 2013) and in collapsing neutron stars (Lehner et al. 2012; Palenzuela 2013) (see also Most et al. (2018a); Nathanail et al. (2017) for electrovacuum simulations). While these studies have been performed self-consistently in full general relativity they have not studied the main source of energy dissipation in current sheets, which are important sources of broad-band electromagnetic emission. In this Letter we show that if all of the magnetic field dynamics is fully resolved the interaction of the magnetic fields in the binary can lead to the launching of powerful magnetic flares similar to magnetars (Kaspi & Beloborodov 2017) and coronal mass ejection in the Sun (Forbes 2000), where magnetic energy dissipation occurs in the main current sheet trailing the flare.

2. METHODS

This work studies the emission of electromagnetic precursor prior to the merger of a double neutron star system. We model the neutron stars as spherical conductors with a circumferential radius of 13 km and a spin axis aligned with the orbital angular momentum. The neutron stars are equipped with dipole magnetic fields having a magnetic field strength B_0 at the surface. We solve the covariant equations of general-relativistic forcefree electrodynamics (Palenzuela 2013) using the newly developed GReX code (Most et al. 2020). We decompose the four-dimensional metric $g_{\mu\nu}$ within a 3+1 split into $ds^2 = (-\alpha^2 + \beta_k \beta^k) dt^2 + 2\beta_k dx^k dt + \gamma_{ij} dx^i dx^j$. Since, for simplicity, we only incorporate special relativistic effects we adopt a co-rotating Minkowski frame $\alpha = 1$, $\gamma_{ij} = \delta_{ij}$ and $\beta_i = -\varepsilon_{ijk}\Omega^j x^k$, where $\Omega = (0, 0, 0, \omega)$ is the orbial angular momentum vector, (see also Schiff 1939; Carrasco & Shibata 2020). The interior of the neutron star obeys the ideal MHD condition

$$E^{i} = -\varepsilon^{ijk} v_{i} B_{k}, \tag{1}$$

where $v_i = \varepsilon_{ijk} \Omega_s^j x_s^k$, Ω_s being the spin vector of the neutron star and x_s being the coordinate vector centered on the neutron star. We emphasize that adopting a co-rotating frame allows us to cleanly separate the orbital motion from the spin of the individual neutron stars so that only the spin velocity enters in (1). While simulations of pulsar magnetospheres typically do not adopt a fully general-relativistic framework to solve the Maxwell equations in the corotating frame (see e.g. Bai & Spitkovsky 2010), it would be straightforward and interesting to also implement this approach within relativisitc particle-in-cell codes for magnetospheric modeling (Parfrey et al. 2019; Crinquand et al. 2020). More details can be found in the Appendix. The exterior is evolved according to the force-free conditions $E_i B^i = 0$ and $E^2 < B^2$ (Komissarov 2004). These are then imposed using a stiff constraint relaxation scheme (Alic et al. 2012) for the evolution of the electric and magnetic fields E^i and B^i (Baumgarte & Shapiro 2003). To handle the stiff current in the Ohm's law we use the third order accurate implicit-explicit (IMEX) Runge-Kutta(RK) SSP3(4.3.3) scheme (Pareschi & Russo 2005) and compute the explicit fluxes using a fourth order accurate finite volume scheme (McCorquodale & Colella

2011), combining a fifth-order WENO-Z reconstruction (Borges et al. 2008) with a Rusanov Riemann solver (Rusanov 1961) similar to the approach in (Most et al. 2019). We similarly enforce the ideal-MHD condition inside the star by computing a stiff instantaneous correction current that exactly enforces (1) at every substep of the IMEX-RK scheme.

The computational grid is provided by a set of nested boxes using the AMReX (the AMReX Development Team et al. 2019) highly parallel adaptive mesh-refinement framework, on which GReX is built. The outer-most box extends up to $\simeq 1200\,\mathrm{km}$ whereas the inner-most box spans $\simeq 40\,\mathrm{km}$ in all directions with a highest resolution of $\simeq 400\,\mathrm{m}$ and a total number of 6 refinement levels. Since the angular component of the shift $\beta_\phi = -\omega R$ diverges at large distances R from the origin, we damp the shift $\beta_\phi \simeq R^{-2}$ close to the boundary and impose simple third order extrapolation boundary conditions on the electromagnetic fields.

3. RESULTS

We investigate the evolution of the common magnetosphere of a neutron star binary in close orbit to demonstrate under which conditions powerful electromagnetic flares can be expected shortly before merger. We will first study a fiducial system in which both stars are in a synchronised orbit, with one star having an additional spin Ω_s , and the energy for the flare is extracted from the rotational energy of the spinning neutron star. In

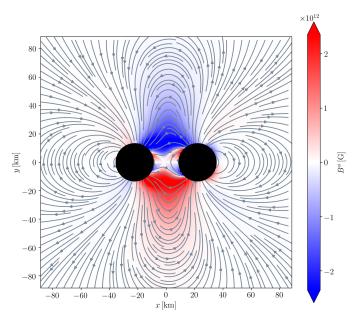


Figure 1. Intermediate force-free magnetic field configuration of a binary in close orbit, in which the right star is spinning. The color qualitatively indicates the twist, i.e. the out-of-plane component B^{ϕ} of the magnetic field.

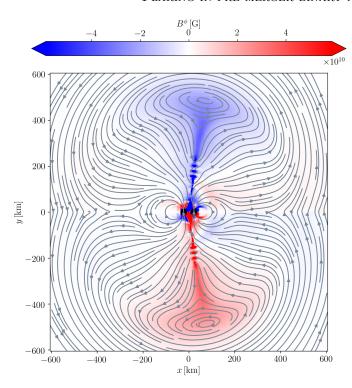


Figure 2. Electromagnetic flare launched from an orbiting neutron star binary in close contact after a significant twist has built up due to the rotation of the right star. Shown in color is the out-of-plane magnetic field B^{ϕ} in a co-rotating frame indicating the twist in the flux tubes connecting the stars. The current sheet trailing the flare is shown to form magnetic islands as a result of the plasmoid instability.

order to establish that this flaring effect is also present in binaries endowed with different field configurations we in addition consider binaries where the magnetic moment of one of the stars is misaligned with the orbital angular momentum. Finally, we also establish the robustness of our results by studying the fiducial binary at various separations ranging up to 100 km. As we show below, for the case of the misaligned binary the flaring occurs even in the case of non-spinning neutron stars. Moreover, the flaring luminosity depends only on the separation between the two stars, not on the actual values of the stellar spin. This proves that flaring events are driven by the energy stored in the twisted magnetic field loop, and not by the Poynting flux driven by the orbital or rotational motion (Carrasco et al. 2019; Carrasco & Shibata 2020).

We consider two stars endowed with strong dipole magnetic fields having a field strength $B_0 \simeq 10^{12}\,\mathrm{G}$ at the surface. In particular, we focus on anti-aligned field line configurations with their magnetic moments pointing in opposite directions, which result in a closed loop magnetic field configuration. Since the field strengths of

the interacting dipoles become strongest at close separation shortly before merger, we study a fiducial binary at 45 km separation, which corresponds to an orbital light cylinder $R_{LC}^{\rm orbit} \simeq 170\,{\rm km}$. The light cylinder here denotes the distance from the origin of the binary beyond which its no longer possible for the field to co-rotate as this would have to happen at speeds larger than the light speed (Goldreich & Julian 1969). We include differential motion in the fiducial binary by adding spin to one of the stars, corresponding to a stellar light cylinder $R_{LC}^{\rm star} \simeq 470\,{\rm km}$. As outlined in the previous section we then proceed and perform a fully special relativistic force-free simulation of this orbiting binary to illustrate how powerful electromagnetic flares can be launched in a binary system in close contact prior to merger.

After an initial transient necessary for the force-free constraint relaxation scheme to establish an initial forcefree magnetic field configuration, the spinning star in the fiducial binary continuously twists the magnetic flux tube connecting the two stars. This is illustrated in Fig. 1 which shows the out-of-plane magnetic field component B^{ϕ} in a co-rotating frame. The twist causes the magnetic field lines to inflate transferring energy from the rotation of the neutron star into the magnetic field. It is important that for this process to work the stars need to be in sufficiently close contact since the twist is established by an Alfven wave propagating between the two stars along the flux tube, which requires that the separation a of the binary is smaller than the stellar light cylinder $R_{LC}^{\rm star}$. Assuming realistic dimensionless spins $\chi \leq 0.05^{-1}$, i.e. $R_{LC}^{\rm star} \simeq 350 {\rm km}$, in the binary (Zhu et al. 2018), this will always happen during the last orbits before the merger.

As can already be anticipated in Fig. 1, at some point the built-up pressure of the toroidal magnetic field B^{ϕ} will be so strong that the twisted magnetic flux tube that connects the two stars, blue and red region in Fig. 1, has to open up. This is shown in Fig. 2 which presents the flare at the time when a magnetic bubble gets ejected together with a reconnecting current sheet trailing it, similar to magnetar flares (for example, in 2D force-free simulations of Parfrey et al. 2012). Looking at the out-of-plane magnetic field component it can easily be seen that magnetic islands are formed in the current sheet, suggesting that magnetic reconnection and the plasmoid instability are taking place (Loureiro et al. 2007; Bhattacharjee et al. 2009). In order to better quantify the energy contained in the out-going bubble

 $^{^1}$ The dimensionless spin is defined as $\chi=J/M^2,$ where J and M are the angular momentum and mass of the neutron star, respectively.

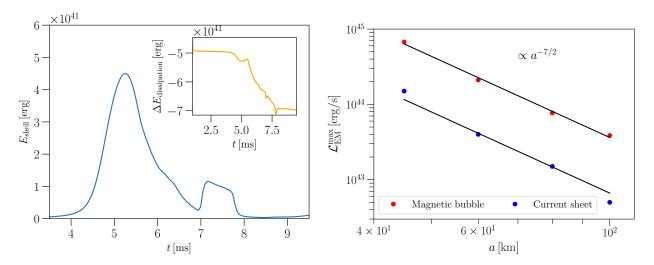


Figure 3. (Left): Energy E_{shell} contained in the shell enclosing the flare. The inset is showing the energy $\Delta E_{\text{dissipation}}$ dissipated in the current sheet. (Right): Peak luminosity $\mathcal{L}_{\text{EM}}^{\text{max}}$ of the out-going magnetic bubble (red dots) and dissipation in the current sheet (blue dots) as a function of the separation a between the stars in the binary.

as well as understand the angular distribution of the emission on large scales we extract the Poynting flux $4\pi \mathbf{S}_{\mathrm{EM}} = \mathbf{E} \times \mathbf{B} - \frac{1}{2} \left(E^2 + B^2 \right) \boldsymbol{\beta}$ on a spherical shell placed at a radius of $450\,\mathrm{km}$ from the origin. We then integrate the out-going energy flux over one burst and show its angular distribution in Fig. 4. We can see that the bubble begins to widen at large scales from the binary indicating its quasi-isotropic structure at infinity. Further, the energy in the bubble is about $10^{41}\,\mathrm{erg}$ per surface angle. In order to quantify the amount of energy dissipated in the current sheet we consider Poynting's theorem of electromagnetic energy conservation in the simulation domain

$$\partial_t \left(\frac{1}{8\pi} \left(E^2 + B^2 \right) \right) + \nabla \cdot \mathbf{S}_{EM} = \mathcal{L}_{dissipation}, \quad (2)$$

where $\mathcal{L}_{\text{dissipation}}$ is the dissipative luminosity, driven by the resistive terms in the Ohms law. Eq. (2) states the the electromagnetic energy $E_{\text{EM}} = \int \mathrm{d}^3 x \frac{1}{8\pi} \left(E^2 + B^2 \right)$ can only change either by a transport of energy via a Poynting flux \mathbf{S}_{EM} or via dissipation $\mathcal{L}_{\text{dissipation}}$. In order to estimate the amount of dissipation we consider

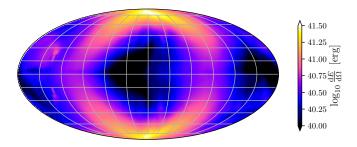


Figure 4. Time integrated electromagnetic energy $dE/d\Omega$ per surface angle extracted on a radial shell at 450 km radius.

two spherical surfaces centered on the origin of the binary. The inner surface encloses just the two stars while the outer shell is placed at a large distance from the origin. We can then estimate the amount of dissipation by computing the energy balance in the shell between the two surfaces according to Eq. (2). This is shown in the left panel of Fig. 3 which shows the evolution of the energy E_{shell} contained in the shell during one flaring event and the amount of energy dissipation $\Delta E_{\text{dissipation}}$ in the current sheet. We anticipate these results not to depend strongly on numerical resolution as it has been shown that the non-linear development of the plasmoid instability causes the magnetic reconnection rate to become independent of the physical resistivity η at high Lundquist number $S_L \geq \eta^{-1} \simeq 10^4$ (Loureiro et al. 2007; Bhattacharjee et al. 2009).

Finally we highlight how the peak luminosity $\mathcal{L}_{\rm EM}^{\rm max}$ of the precursor flare for the fiducial binary scales with the orbital separation a. This is shown in Fig. 3 for both the Poynting flux contained in the outgoing magnetic bubble as well as for the dissipative luminosity in the current sheet. We find a clean scaling of $\mathcal{L}_{\rm EM} \propto a^{-7/2}$ in both cases. In order to better understand the scaling we estimate the free energy $\Delta E_{\rm twist}$ in the twisted flux tube in the limit of small twist, ψ , following Parfrey et al. (2013),

$$\Delta E_{\text{twist}} \approx \frac{1}{8} \psi^2 u^3 E_0 = \psi^2 \frac{R^3}{a^3} E_0,$$
 (3)

$$\approx 1.4 \times 10^{41} B_{12}^2 R_{13}^3 \psi^2 \,\text{erg},$$
 (4)

where u characterizes the fraction of twisted field lines, u = 2R/a, and E_0 is the energy of the unperturbed dipole configuration. In addition we have introduced

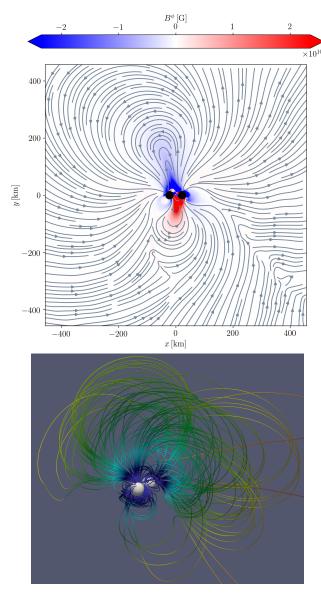


Figure 5. Some as in Fig. 2 but with 45° misaligned magnetic fields. The flaring is induced by the orbital motion. (Top) Out-of-plane magnetic field B^{ϕ} in the meridional plane. (Bottom) Three-dimensional visualisation of the field line configuration at the flare onset time.

 $B_{12}=B/10^{12}\,\mathrm{G}$ and $R_{13}=R/13\,\mathrm{km}$. If further we assume that reconnection in the flaring sheet happens during the time $\Delta t\simeq 2a/v_{\mathrm{rec}}$ (Parfrey et al. 2013), where $v_{\mathrm{rec}}\sim 0.1c$ is the reconnection speed, we find that

$$\mathcal{L}_{\rm EM}^{\rm max} = \frac{\Delta E_{\rm twist}}{\Delta t} \approx \eta \frac{\psi^2}{2} v_{\rm rec} \frac{R^3}{a^4} E_0$$

$$\approx 4.6 \times 10^{44} \eta B_{12}^2 R_{13}^3 \psi_{\pi}^2, \qquad (6)$$

where the pre-factor $\eta \leq 1$ quantifies the fraction of the free energy in the twisted flux tube that is available for reconnection, and flaring happens at twist value $\sim \pi$, i.e. $\psi_{\pi} = \psi/\pi$. Although not exact, this scaling is very

similar to the one obtained from the simulations, and the differences might be associated with the assumption of small twist in Eq. (6). We further find that the energy dissipated in the current sheet is always and order of magnitude below the energy carried away by the flare. Although the scaling found in our simulations seems very clean we caution that we have not included any form of orbital decay caused by the inspiral. Since this will be subdominant at larger separations we still believe our results to be applicable to most binaries.

While our analysis has so far been focused on studying a single system with equal magnetization and a non-zero stellar spin of one of the neutron stars we now show that the flaring effect is quite general and will occur for a variety of orbital configurations. In Fig. 5 we show the flaring process for an equally magnetized binary, where both stars are non-spinning but the left star has a magnetic moment that is misaligned by 45° with the direction of the orbital angular momentum. Whereas in the fiducial case the differential motion was caused by a relative difference in spin between the two stars. A non-spinning binary with a misaligned magnetic field will twist its common magnetosphere because of the orbital motion itself. In other words, while the energy that drives the flare in the fiducial case was provided by the rotational motion of the star, it is in this case provided purely by the orbital motion. Since we expect pulsar magnetic fields to be generally misaligned with their spin axis, this proves that magnetic flaring on the timescale of the orbital period is the most generic result of the interaction of magnetospheres with the comparable field strength of both stars.

4. DISCUSSION

We have presented the first force-free electrodynamics simulations demonstrating how powerful electromagnetic flares can be launched as precursors to the neutron star merger events. We have found that these are produced by a built-up of twist in the common force-free magnetosphere of the binary system, caused by differential motion. We have shown that this can be either caused by a relative spin difference of the two stars or misalignment of the magnetosphere, which are common for pulsars.

While predicting both high-energy and coherent radio emission signatures of the magnetic flare requires first-principles kinetic plasma simulations, lessons learned in the pulsar magnetosphere research allow us to describe potential outcomes. For example, we expect most of the dissipated power in the current sheet to go into accelerated particles and, at typical magnetic field strengths $\geq 10^6 {\rm G}$ at the sheet location, to be quickly radiated

away as high-energy synchrotron radiation. Kinetic simulations of relativistic radiative reconnection (similar to ones done for pulsar current sheets in Hakobyan et al. 2019) that take into account synchrotron cooling of emitting particles and pair production due to collisions of high-energy photons are needed to calculate the expected high-energy signature. While this study adopts a simplified resistive force-free prescription for the dissipation in the current sheets, the $\approx 10\%$ efficiency of converting the outgoing Poynting flux into the dissipated power, $\mathcal{L}_{dissipation}$, in magnetic reconnection is not uncommon in full kinetic plasma simulations of magnetospheres (Philippov & Spitkovsky 2014; Cerutti et al. 2015; Brambilla et al. 2018). Future kinetic studies of flaring events in binary magnetospheres will be able to verify this conclusion (Crinquand et al. 2019).

Given relatively low expected luminosities in the highenergy band, coherent radio emission is a best bet for a potential precursor signal Lyutikov (2019a). We anticipate two potential mechanisms: the first channel is a radio afterglow of the magnetic reconnection in the current sheet trailing the outgoing bubble, and the second channel is the synchrotron maser emission model of the outgoing magnetized bubble shocking the ambient plasma. Lyubarsky (2019) and Philippov et al. (2019) have shown that merging plasmoids in the pulsar current sheet beyond the light cylinder can produce coherent radio emission if the magnetic field strength in the upstream of the sheet is $\simeq 10^6 - 10^8 \text{G}^2$. Rescaling the results shown in Figs. 2 and 5 we find that in our simulation this corresponds to fields strengths of $B_0 \simeq 10^8 - 10^{10} \text{G}$ at the surface of the star. For such a field strength the outgoing Poynting luminosity would, hence, be $\mathcal{L}_{\rm EM}^{\rm max} \simeq 10^{39}-10^{41}\,{\rm erg s^{-1}}$. Given typically very low efficiency, $\leq 10^{-4}$, of converting reconnecting magnetic flux into escaping coherent electromagnetic waves it makes it unlikely to expect an FRBstrength radio signal from the current sheet trailing the flare. As noted by Lyubarsky (2020) in a similar context of magnetar flares, reconnection in the collision of the escaping magnetic bubble with the large-scale magnetospheric current sheet is more likely to produce a powerful radio signal. Another coherent radio emission channel is linked to the escaping magnetic bubble. Since the ambient of the binary is not empty but filled with a highly conducting electron-positron plasma with insignificant baryon pollution, the bubble can produce a magnetized shock at some distance from the binary, which may drive a synchrotron maser instability and associated electromagnetic emission (Gallant et al. 1992). The quasi-isotropic structure of the escaping magnetized bubble that we find in this work should help with the detectability of these events. This scenario has been studied in the case of flares of young magnetars, which is one possibility to explain Fast Radio Bursts (Lyubarsky 2014; Beloborodov 2017; Metzger et al. 2019). We plan to explore these possibilities in the future.

One caveat of our study is that for now we have neglected effects of the inspiral motion and general relativistic corrections, such as red shifts. These will be particularly important to understand potential transients from the last orbits before the merger, and we plan to incorporate those effects in an upcoming work. In order to better illustrate the observational prospect it will be important to cover the vast parameter space of magnetic field configurations, e.g. to explore unequal magnetization and inclination effects. This investigation will be reported in a follow-up paper.

During the final preparation of this work we became aware of Carrasco & Shibata (2020), who study the case of a single orbiting neutron star with a force-free magnetosphere using a setup very similar to the one described in this work. Their results focus on a continuous electromagnetic emission from a large-scale magnetospheric current sheet resulting from orbital motion, similar to the one that occurs in the magnetosphere of a usual rotating pulsar. While they are well applicable to systems with large orbital separations, i.e. greater than the stellar and orbital light cylinders, this work discusses the non-trivial magnetospheric interaction of two neutron stars prior to merger. It leads to the emission of powerful electromagnetic flares, which are more likely to be detectable as electromagnetic precursors of neutron star mergers (Callister et al. 2019).

ACKNOWLEDGEMENTS

ERM and AP would like to thank Federico Carrasco, William East, Hayk Hakobyan, Luis Lehner, Yuri Levin, Maxim Lyutikov, Brian Metzger, Kohta Murase, Eliot Quataert, Luciano Rezzolla, Masaru Shibata, Lorenzo Sironi, Anatoly Spitkovsky and James Stone for valuable and insightful discussions. ERM gratefully acknowledges support and hospitality from the Simons Foundation through the pre-doctoral program at the Center for Computational Astrophysics, Flatiron Institute. This research was supported by the National Science Foundation under Grant No. AST-1909458. Research at the Flatiron Institute is supported by the Simons Foundation.

REFERENCES

- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2018, Physical Review Letters, 121, 161101
- Alic, D., Moesta, P., Rezzolla, L., Zanotti, O., & Jaramillo, J. L. 2012, Astrophys. J., 754, 36
- Bai, X.-N., & Spitkovsky, A. 2010, Astrophys. J., 715, 1282 Baumgarte, T. W., & Shapiro, S. L. 2003, Astrophys.

Journal, 585, 921

- Beloborodov, A. M. 2017, Astrophys. J. Lett., 843, L26
- Bhattacharjee, A., Huang, Y.-M., Yang, H., & Rogers, B. 2009, Physics of Plasmas, 16, 112102
- Borges, R., Carmona, M., Costa, B., & Don, W. 2008, Journal of Computational Physics, 227, 3191
- Brambilla, G., Kalapotharakos, C., Timokhin, A. N., Harding, A. K., & Kazanas, D. 2018, Astrophys. J., 858, 81
- Callister, T. A., Anderson, M. M., Hallinan, G., et al. 2019, Astrophys. J. Lett., 877, L39
- Carrasco, F., & Shibata, M. 2020, arXiv e-prints, arXiv:2001.04210
- Carrasco, F., Viganò, D., Palenzuela, C., & Pons, J. A. 2019, MNRAS, 484, L124
- Cerutti, B., Philippov, A., Parfrey, K., & Spitkovsky, A. 2015, Mon. Not. R. Astron. Soc., 448, 606
- Crinquand, B., Cerutti, B., & Dubus, G. 2019, Astron. & Astrophys., 622, A161
- Crinquand, B., Cerutti, B., Philippov, A. e., Parfrey, K., & Dubus, G. 2020, arXiv e-prints, arXiv:2003.03548
- De, S., Finstad, D., Lattimer, J. M., et al. 2018, Physical Review Letters, 121, 091102
- Forbes, T. 2000, Journal of Geophysical Research: Space Physics, 105, 23153
- Gallant, Y. A., Hoshino, M., Langdon, A. B., Arons, J., & Max, C. E. 1992, Astrophys. J., 391, 73
- Goldreich, P., & Julian, W. H. 1969, Astrophys. J., 157, 869Hakobyan, H., Philippov, A., & Spitkovsky, A. 2019,Astrophys. J., 877, 53
- Hansen, B. M. S., & Lyutikov, M. 2001, Mon. Not. R. Astron. Soc., 322, 695
- Kaspi, V. M., & Beloborodov, A. M. 2017, Annual Review of Astronomy and Astrophysics, 55, 261
- Komissarov, S. S. 2004, Mon. Not. R. Astron. Soc., 350, 427Lai, D. 2012, Astrophys. J. Lett., 757, L3
- Lehner, L., Palenzuela, C., Liebling, S. L., Thompson, C., & Hanna, C. 2012, Phys. Rev. D, 86, 104035
- 2 For higher field strength the sheet width shrinks as $\propto B^{-3/2}$ (Uzdensky & Spitkovsky 2014), and the radiation will be emitted at frequencies higher than radio.

- Loureiro, N. F., Schekochihin, A. A., & Cowley, S. C. 2007, Physics of Plasmas, 14, 100703
- Lyubarsky, Y. 2014, Mon. Not. R. Astron. Soc., 442, L9
- —. 2019, Mon. Not. R. Astron. Soc., 483, 1731
- —. 2020, arXiv e-prints, arXiv:2001.02007
- Lyutikov, M. 2019a, arXiv e-prints, arXiv:1901.03260
- —. 2019b, Mon. Not. R. Astron. Soc., 483, 2766
- McCorquodale, P., & Colella, P. 2011, Communications in Applied Mathematics and Computational Science, 6, 1
- Metzger, B. D., Margalit, B., & Sironi, L. 2019, MNRAS, 485, 4091
- Metzger, B. D., & Zivancev, C. 2016, Mon. Not. R. Astron. Soc., 461, 4435
- Most, E. R., Nathanail, A., & Rezzolla, L. 2018a, Astrophys. J, 864, 117
- Most, E. R., Papenfort, L. J., & Rezzolla, L. 2019, arXiv e-prints, arXiv:1907.10328
- —. 2020, in preparation, arXiv:in preparation
- Most, E. R., Weih, L. R., Rezzolla, L., & Schaffner-Bielich, J. 2018b, Phys. Rev. Lett., 120, 261103
- Nathanail, A., Most, E. R., & Rezzolla, L. 2017, Mon. Not.
 R. Astron. Soc., 469, L31
- Palenzuela, C. 2013, Mon. Not. R. Astron. Soc., 431, 1853
- Palenzuela, C., Lehner, L., & Liebling, S. L. 2010, Science, 329, 927
- Palenzuela, C., Lehner, L., Liebling, S. L., et al. 2013a, Phys. Rev. D, 88, 043011
- Palenzuela, C., Lehner, L., Ponce, M., et al. 2013b, Phys. Rev. Lett., 111, 061105
- Pareschi, L., & Russo, G. 2005, Journal of Scientific Computing, 25, 129
- Parfrey, K., Beloborodov, A. M., & Hui, L. 2012, Astrophys. J. Lett., 754, L12
- —. 2013, Astrophys. J., 774, 92
- Parfrey, K., Philippov, A., & Cerutti, B. 2019, Phys. Rev. Lett., 122, 035101
- Paschalidis, V., Etienne, Z. B., & Shapiro, S. L. 2013, Phys. Rev. D, 88, 021504
- Philippov, A., Uzdensky, D. A., Spitkovsky, A., & Cerutti, B. 2019, Astrophys. J. Lett., 876, L6
- Philippov, A. A., & Spitkovsky, A. 2014, Astrophys. J., 785, L33
- Piro, A. L. 2012, Astrophys. J., 755, 80
- Ponce, M., Palenzuela, C., Lehner, L., & Liebling, S. L. 2014, Phys. Rev. D, 90, 044007
- Raithel, C. A. 2019, European Physical Journal A, 55, 80
- Rusanov, V. V. 1961, J. Comput. Math. Phys. USSR, 1, 267
- Schiff, L. I. 1939, Proceedings of the National Academy of Sciences, 25, 391

the AMReX Development Team, Almgren, A., Beckner, V., et al. 2019

Uzdensky, D. A., & Spitkovsky, A. 2014, Astrophys. J., 780, 3

Wang, J.-S., Yang, Y.-P., Wu, X.-F., Dai, Z.-G., & Wang,
F.-Y. 2016, Astrophys. J. Lett., 822, L7
Zhu, X., Thrane, E., Osłowski, Stefan and Levin, Y., &
Lasky, P. D. 2018, Phys. Rev. D, 98, 043002

APPENDIX

In this appendix we briefly state the equations of general relativistic electrodynamics augmented with divergence cleaning in order to maintain the $D_i B^i = 0$ and $D_i E^i = 4\pi q$ constraints. Written in covariant form using the field strength tensor $F^{\mu\nu}$ the augmented Maxwell equations read (Palenzuela 2013),

$$\nabla_{\mu} \left(F^{\mu\nu} + \psi g^{\mu\nu} \right) = -4\pi \mathcal{J}^{\nu} + \kappa_{\psi} \psi n^{\nu}, \tag{7}$$

$$\nabla_{\mu} \left(*F^{\mu\nu} + \phi g^{\mu\nu} \right) = \kappa_{\phi} \phi n^{\nu}, \tag{8}$$

where ϕ, ψ are generalized Lagrange multipliers and $\kappa_{\phi}, \kappa_{\psi}$ are their damping constants and the 4-current $\mathcal{J}^{\mu} = qn^{\mu} + J^{\mu}$, where J^{μ} is the spatial part of the current, q is the charge density and $\mathbf{n} = \alpha^{-1} (1, -\beta^{i})$ is the normal vector of the 3-dimensional hypersurface of the space-time foliation.

Within the 3+1 split of the metric introduced earlier in the text,

$$ds^{2} = \left(-\alpha^{2} + \beta_{k}\beta^{k}\right)dt^{2} + 2\beta_{k}dx^{k}dt + \gamma_{ij}dx^{i}dx^{j}, \tag{9}$$

the Maxwell equations (7) and (8) become (Palenzuela 2013),

$$\partial_t \left(\sqrt{\gamma} q \right) + \partial_i \left(\alpha J^i - \beta^i q \right) = 0, \tag{10}$$

$$\partial_t \left(\sqrt{\gamma} B^i \right) + \partial_k \left(-\sqrt{\gamma} \beta^k B^i + \alpha \sqrt{\gamma} \varepsilon^{ikj} E_j + \alpha \sqrt{\gamma} \phi \right) = -\sqrt{\gamma} B^k \partial_k \beta^i + \sqrt{\gamma} \phi \left(\gamma^{ij} \partial_j \alpha - \alpha \gamma^{jk} \Gamma^i_{jk} \right), \tag{11}$$

$$\partial_t \left(\sqrt{\gamma} \phi \right) + \partial_k \left(-\beta^k \sqrt{\gamma} \phi + \alpha \sqrt{\gamma} B^k \right) = -\alpha \sqrt{\gamma} \phi K + \sqrt{\gamma} B^k \partial_k \alpha - \alpha \kappa_\phi \sqrt{\gamma} \phi, \tag{12}$$

$$\partial_t \left(\sqrt{\gamma} E^i \right) + \partial_k \left(-\sqrt{\gamma} \beta^k E^i - \alpha \sqrt{\gamma} \varepsilon^{ikj} B_j + \alpha \sqrt{\gamma} \psi \right) = -\sqrt{\gamma} E^k \partial_k \beta^i + \sqrt{\gamma} \psi \left(\gamma^{ij} \partial_j \alpha - \alpha \gamma^{jk} \Gamma^i_{jk} \right) - 4\pi \alpha \sqrt{\gamma} J^i, \quad (13)$$

$$\partial_t \left(\sqrt{\gamma} \psi \right) + \partial_k \left(-\beta^k \sqrt{\gamma} \psi + \alpha \sqrt{\gamma} E^k \right) = -\alpha \sqrt{\gamma} \psi K + 4\pi \alpha \sqrt{\gamma} q + \sqrt{\gamma} E^k \partial_k \alpha - \alpha \kappa_\psi \sqrt{\gamma} \psi. \tag{14}$$

Here Γ_{ij}^k is the metric compatible Christoffel symbol of the 3-metric γ_{ij} , $\gamma = \det \gamma_{ij}$ and K is the trace of the extrinsic curvature. These equations are covariant and are valid in any frame, in particular also in the corotating frame (Schiff 1939). In order to clarify the implications of this approach and similar (but not identically) to Carrasco & Shibata (2020), we adopt a co-rotating Minkowski frame (Schiff 1939) $\alpha = 1$, $\gamma_{ij} = \delta_{ij}$ and $\beta_i = -\varepsilon_{ijk}\Omega^j x^k$, where $\Omega = (0,0,0,\omega)$ is the orbital angular momentum vector. In order to understand the meaning of this construction we consider the advection velocity u^{μ} of a fluid element inside the stars.

$$\frac{u^i}{u^0} = \alpha v^i - \beta^i = \varepsilon^{ijk} \Omega_{sj} x_{sk} + \varepsilon^{ijk} \Omega_j x_k, \tag{15}$$

where v^i is the 3-velocity seen by the corotating observer. In simple words, since the observer corotates with the star, the local velocity he sees does not contain the $\mathbf{\Omega} \times \mathbf{x}$ part of the orbital motion and, hence, does not enter the electric field

$$E^{i} = -\varepsilon^{ijk} v_{j} B_{k}, \tag{16}$$

seen by the corotating observer. Nonetheless, because we are solving the covariant form of the Maxwell equations, we can see that the actual field that enters the induction equation is $E - \beta \times B$, and hence the rotational contribution does enter into the magnetic field evolution consistently. Since Ω and Ω_s are aligned we can express this as

$$\frac{u^{i}}{u^{0}} = \varepsilon^{ijk} \left(\Omega_{s} + \Omega\right) z_{j} x_{sk} + \varepsilon^{ijk} \Omega_{j} x_{\text{star k}}, \tag{17}$$

where \mathbf{z} is the z-coordinate vector and $\mathbf{x}_{\text{star}} = \mathbf{x} - \mathbf{x}_{\mathbf{s}}$ is the coordinate vector of the stellar center hence. Hence, a fluid element inside the star would spin with $(\Omega_s + \Omega)$ around the spin axis of the star and at the same time co-move with the orbital motion of the star. If we would in addition subtract $\varepsilon_{ijk}\Omega^j x_{\text{star}}^k$ from the 3-velocity v^i , which enters the electric field inside the star via Eq. (16), we would indeed adopt a truly corotating frame in which the star no longer moves since then

$$\frac{u^i}{u^0} = \alpha v^i - \beta^i = \varepsilon^{ijk} \left(\Omega_s + \Omega\right) z_j x_{sk},\tag{18}$$

which corresponds to the purely rotational motion of the star. We can also see from this expression that $\Omega_s = 0$ implies a residual rotation in the true comoving frame, corresponding to the case of synchronised orbital motion of the stars.