

# New CTEQ Global Analysis with High Precision Data from the LHC

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We present the new CTEQ-TEA global analysis of quantum chromodynamics (QCD). In this analysis, parton distribution functions (PDFs) of the nucleon are determined within the Hessian method at the next-to-next-to leading order (NNLO) in perturbative QCD, based on the most recent measurements from the Large Hadron Collider (LHC) and a variety of world collider data. Because of difficulties in fitting both the ATLAS 7 and 8 TeV  $W$  and  $Z$  vector boson production cross section data, we present two families of PDFs, named CT18 and CT18Z PDFs, respectively, without and with the ATLAS 7 TeV  $W$  and  $Z$  measurements. We study the impact of the CT18 family of PDFs on the theoretical predictions of standard candle cross sections at the LHC.

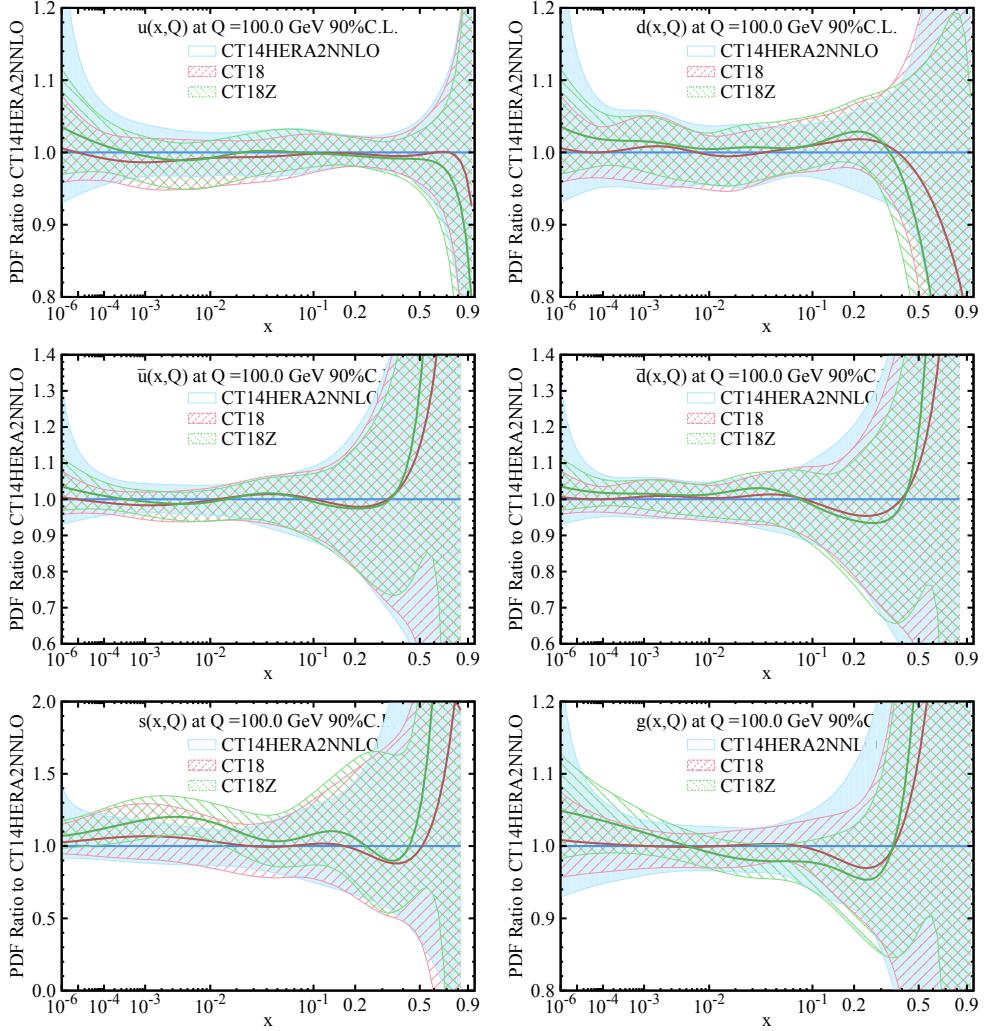
The CT18 parton distribution functions (PDFs) update those of CT14 presented in Ref. [1] with a variety of new LHC data, involving inclusive jet production,  $W$ ,  $Z$  and Drell-Yan production, and the production of top quark pairs, from ATLAS, CMS and LHCb, while retaining crucial *legacy* data, such as measurements from the Tevatron and the HERA Run I and Run II combined data. Measurements of processes in similar kinematic regions, by ATLAS and by CMS, allow crucial cross-checks of the data. Measurements by LHCb often allow extrapolations into new kinematic regions not covered by the other experiments.

The goal of the CT18 analysis is to include as wide a kinematic range for each measurement as allowed by reasonable agreement between data and theory. For the ATLAS 7 TeV jet data [2], for example, all rapidity intervals can not be simultaneously used without the use of systematic error decorrelations provided by the ATLAS experiment. Even with the ATLAS-recommended decorrelations, the resultant  $\chi^2$  is not optimal, resulting in less effective PDF constraints. Inclusive cross section measurements for jet production have been carried out for two different jet radii by both ATLAS and CMS. For both experiments, we have chosen the data with the larger  $R$ -value, as the next-to-next-to-leading order (NNLO) prediction should have a higher accuracy. We evaluate the jet cross section predictions using a scale of  $p_T^{jet}$ , consistent with past usage at the next-to-leading order (NLO). The result is largely consistent with similar evaluations using a scale of  $H_T$  [3].

In an ideal world, all such data sets would perfectly be compatible with each other, but differences are observed that do result in some tension between data sets and pulls in opposite directions. One of the crucial aspects of carrying out a global PDF analysis is dealing with data sets that add some tension to the fits, while preserving the ability of the combined data set to improve on the existing constraints on the PDFs. In some cases, a data set may be in such tension as to require its removal from the global analysis, or its inclusion only in a separate iteration of the new PDF set. Later, we will describe how the high precision ATLAS  $W$  and  $Z$  rapidity distributions [4] require the latter treatment.

Theoretical predictions for comparison to the data used in the global fit have been carried out at NNLO, either indirectly through the use of fast interpolation tables such as NLO APPLGRID [5] and NNLO/NLO  $K$ -factors, or directly (for top-quark related observables) through the use of FASTNNLO grids [6, 7]. New flexible PDF parametrizations have been tested for CT18, to minimize any parametrization bias. In some kinematic regions, there are few constraints from the data on certain PDFs. Lagrange Multiplier constraints are then applied to limit those PDFs to physically reasonable values. A 0.5% uncorrelated error is included to account for numerical uncertainties in the Monte Carlo integration of NNLO cross sections of (i) ATLAS 7 TeV [2] and CMS 7 [8] and 8 TeV [9] jet productions; and (ii) ATLAS 8 TeV high- $p_T$   $Z$  production [10].

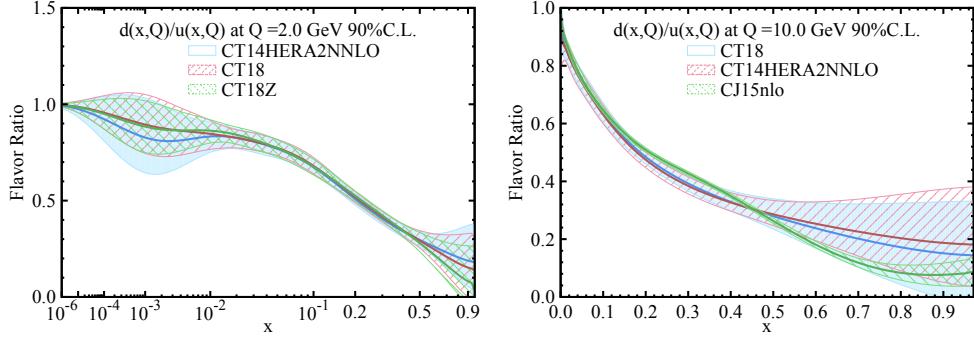
CT18 analysis includes new LHC experiments on  $W$ ,  $Z$ , Drell-Yan, high- $p_T$   $Z$ , jet, and  $t\bar{t}$  pair productions, up to 30 candidate LHC data sets. The alternative CT18Z fit contains the following variations from the CT18 fit: (i) add in the ATLAS 7 TeV  $4.6 \text{ fb}^{-1}$ ,  $W$  and  $Z$  rapidity distribution measurement [4] which is not included in the CT18 fit, (ii) remove the CDHSW data, (iii) take charm pole mass to be 1.4 GeV, instead of the nominal value of 1.3 GeV, (iv) use a saturation scale, instead of the nominal scale of  $Q$ , for all the deep-inelastic scattering (DIS) processes in the fit. The final CT18(Z) data ensemble contains a total of 3681(3493) number of data points and  $\chi^2/N_{pt} = 1.17(1.19)$  at the NNLO.



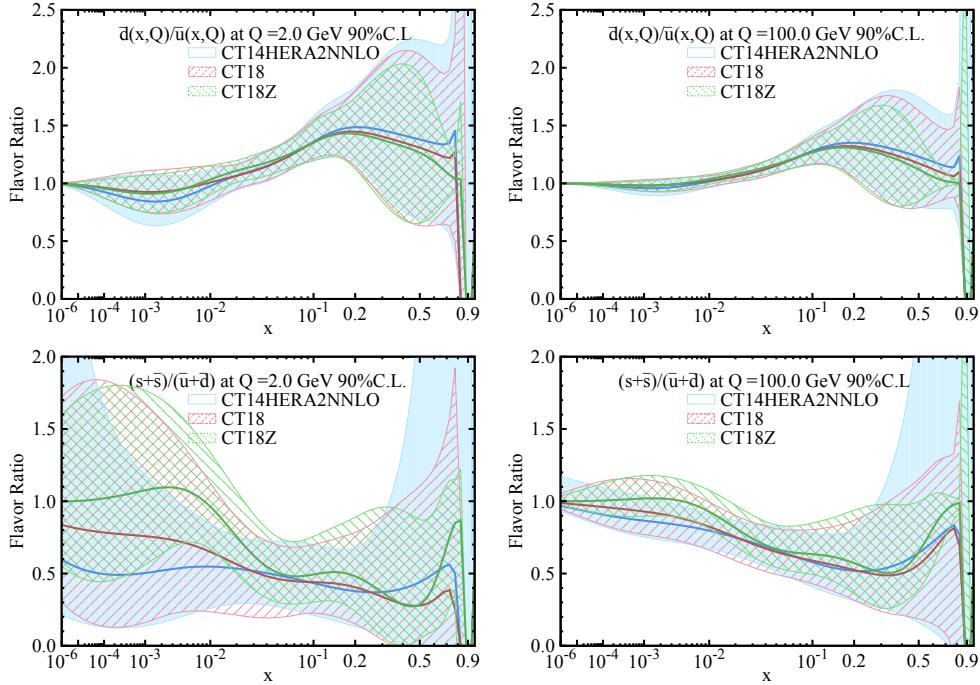
**Figure 1:** A comparison of 90% C.L. PDF uncertainties from CT18 (red curve), CT18Z (green curve) and CT14HERA2 (blue curve) NNLO error ensembles at  $Q = 100$  GeV. The error bands are normalized to the respective central CT14HERA2 NNLO PDFs.

The relative changes between the CT14HERA2 NNLO and CT18 NNLO ensembles are best visualized by comparing their PDF uncertainties. Fig. 1 compares the PDF error bands at 90% confidence level (CL) for the key flavors, with each band normalized to the respective best-fit CT14HERA2 NNLO PDF. The blue and red error bands are obtained for CT14HERA2 NNLO PDFs and CT18 at  $Q = 100$  GeV, respectively.

Fig. 2 shows the different behaviors we find for the  $d/u$  PDF ratio. The changes in  $d/u$  in CT18, as compared to CT14HERA2, can be summarized as a reduction of the central ratio at  $x > 0.5$  and an decreased uncertainty at  $x < 10^{-3}$ . The collider charge asymmetry data constrains  $d/u$  at  $x$  up to about 0.5. At even higher  $x$ , which is not directly constrained by the experiments we fit, the behavior of the CT18 PDFs reflects the parametrization form, which now allows  $d/u$  to approach any constant value as  $x \rightarrow 1$ . As noted earlier, the parametrization form of  $u$ ,  $d$ ,  $\bar{u}$  and  $\bar{d}$  quarks in CT18 are the same as those in CT14HERA2.



**Figure 2:** A comparison of 90% C.L. uncertainties on the ratio  $d(x, Q)/u(x, Q)$  for CT18 (red curve), CT18Z (green curve) and CT14HERA2 (blue curve) NNLO error ensembles at  $Q = 2$  or  $10$  GeV, respectively.

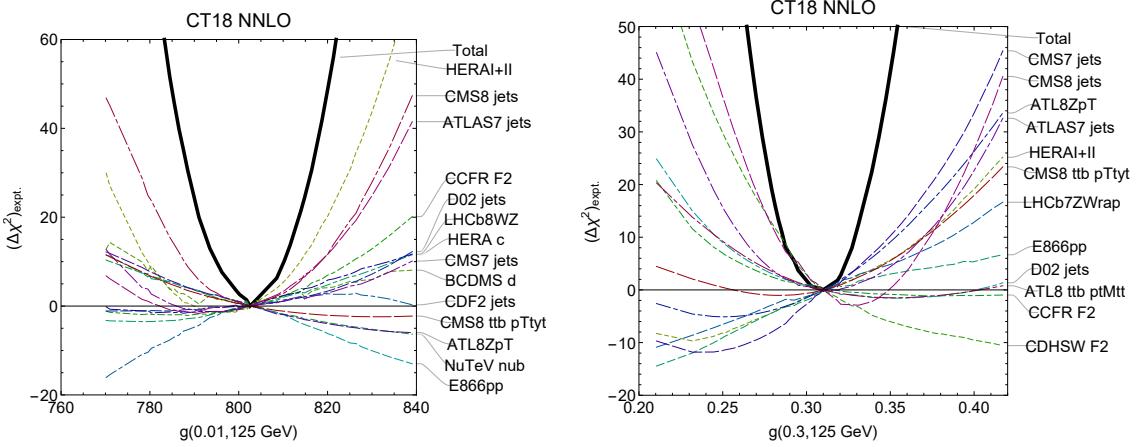


**Figure 3:** A comparison of 90% C.L. uncertainties on the ratios  $\bar{d}(x, Q)/\bar{u}(x, Q)$  and  $(s(x, Q) + \bar{s}(x, Q)) / (\bar{u}(x, Q) + \bar{d}(x, Q))$ , for CT18 (red curve), CT18Z (green curve) and CT14HERA2 (blue curve) NNLO error ensembles at  $Q = 2$  or  $100$  GeV, respectively.

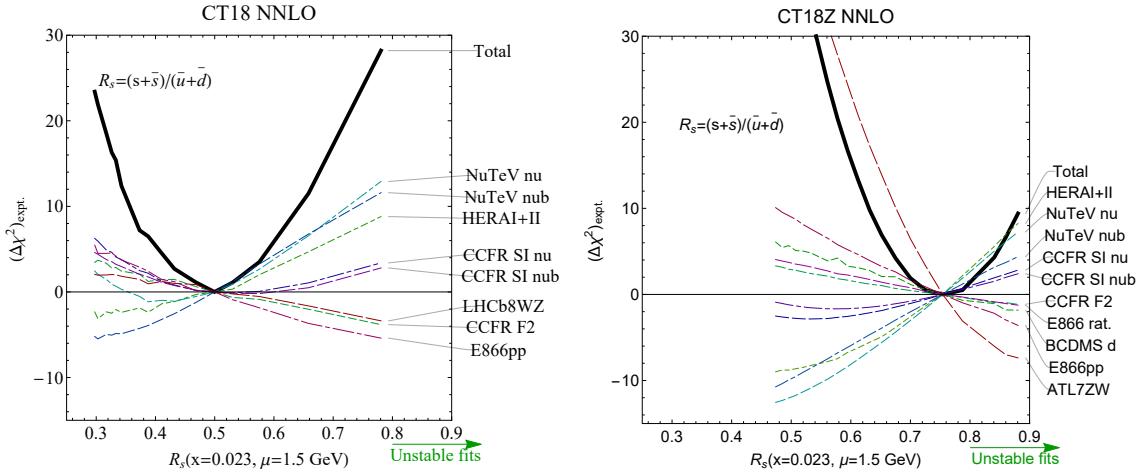
Turning now to the ratios of sea quark PDFs in Fig. 3, we observe that the uncertainty on  $\bar{d}(x, Q)/\bar{u}(x, Q)$  in the left inset has decreased at small  $x$  in CT18. At  $x > 0.1$ , the CT18 non-perturbative parametrization forms for  $\bar{u}$  and  $\bar{d}$  ensure that the ratio  $\bar{d}(x, Q_0)/\bar{u}(x, Q_0)$ , with  $Q_0 = 1.3$  GeV, can approach a constant value that comes out to be close to 1 in the central fit. The uncertainty on  $\bar{d}/\bar{u}$  has also decreased across most of the  $x > 2 \times 10^{-3}$  range, especially around  $x \sim 0.1$ .

The overall increase in the strangeness PDF at  $x < 0.03$  and decrease of  $\bar{u}$  and  $\bar{d}$  PDFs at  $x < 10^{-3}$  lead to a larger ratio of the strange-to-nonstrange sea quark PDFs,  $(s + \bar{s}) / (\bar{u} + \bar{d})$ , presented in Fig. 3. At  $x < 10^{-3}$ , this ratio is determined entirely by parametrization form and was found

in CT10 to be consistent with the exact  $SU(3)$  symmetry of PDF flavors,  $(s + \bar{s}) / (\bar{u} + \bar{d}) \rightarrow 1$  at  $x \rightarrow 0$ , albeit with a large uncertainty. The  $SU(3)$ -symmetric asymptotic solution at  $x \rightarrow 0$  was not enforced in CT14, nor CT14HERA2, so that this ratio at  $Q = 2$  GeV is about 0.6 at  $x = 10^{-6}$ . In CT18, we have taken a different  $s$ -PDF non-perturbative parametrization form and assumed the exact  $SU(3)$  symmetry of PDF flavors so that this ratio asymptotically approaches to 1 as  $x \rightarrow 0$ .



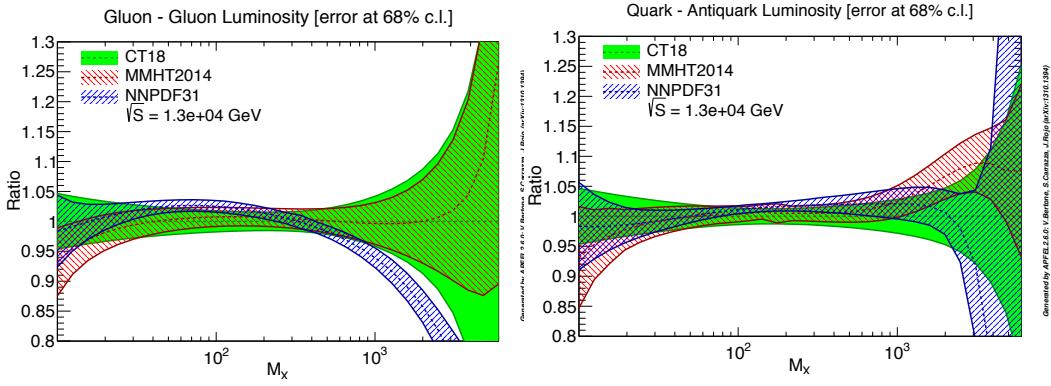
**Figure 4:** The Lagrange Multiplier scan of gluon PDF at  $Q = 125$  GeV and  $x = 0.01$  and  $0.3$ , respectively, for the CT18 NNLO fits.



**Figure 5:** The Lagrange Multiplier scan of  $R_s$  at  $Q = 1.5$  GeV and  $x = 0.023$  for CT18, and CT18Z fits.

One technique that we use to study the parton PDFs is to compute Lagrange Multiplier scans with respect to some feature of  $f(x, Q)$ . Two examples are shown here. First example is to study the constraints on gluon-PDF at  $Q = 125$  GeV and  $x = 0.01$  and  $0.3$ , from various experimental data, cf. Fig. 4. The second example is for the constraints on the  $R_s \equiv (s + \bar{s}) / (\bar{u} + \bar{d})$  ratio at  $Q = 1.5$  GeV,  $x = 0.023$  and  $x = 0.1$ , cf. Fig. 5.

Finally, we compare various PDF luminosities at the 13 TeV LHC, as shown in Fig. 6.



**Figure 6:** Comparison of various PDF luminosities at the 13 TeV LHC.

## Acknowledgments

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