

Observation of 9-Fold Coordinated Amorphous TiO₂ at High Pressure

Yu Shu,[†] Yoshio Kono,^{*,‡,⊥} Itaru Ohira,[‡] Qianjun Li,[§] Rostislav Hrubíak,[†] Changyong Park,[†] Curtis Kenney-Benson,[†] Yanbin Wang,^{||} and Guoyin Shen^{*,†}

[†]High Pressure Collaborative Access Team, X-ray Science Division, Argonne National Laboratory, Argonne, Illinois 60439, United States

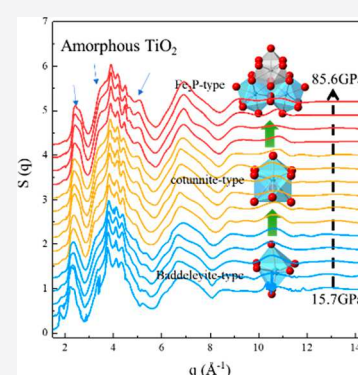
[‡]Geophysical Laboratory, Carnegie Institution of Washington, Argonne, Illinois 60439, United States

[§]State Key Laboratory of Superhard Materials, Jilin University, Changchun 130012, China

^{||}Center for Advanced Radiation Sources, The University of Chicago, Chicago, Illinois 60637, United States

Supporting Information

ABSTRACT: Knowledge of the structure in amorphous dioxides is important in many fields of science and engineering. Here we report new experimental results of high-pressure polyamorphism in amorphous TiO₂ (a-TiO₂). Our data show that the Ti coordination number (CN) increases from 7.2 ± 0.3 at ~ 16 GPa to 8.8 ± 0.3 at ~ 70 GPa and finally reaches a plateau at 8.9 ± 0.3 at $\lesssim 86$ GPa. The evolution of the structural changes under pressure is rationalized by the ratio (γ) of the ionic radius of Ti to that of O. It appears that the CN ≈ 9 plateau correlates with the two 9-fold coordinated polymorphs (cotunnite, Fe₂P) with different γ values. This CN– γ relationship is compared with those of a-SiO₂ and a-GeO₂, displaying remarkably consistent behavior between CN and γ . The unified CN– γ relationship may be generally used to predict the compression behavior of amorphous AO₂ compounds under extreme conditions.



Information about pressure-induced structural changes in amorphous dioxides (a-AO₂) is critical for understanding macroscopic properties (e.g., refractive index, density, elasticity, strength, etc.) under extreme compression. As prototype network-forming glasses, pressure-induced structural changes of amorphous SiO₂ (a-SiO₂) and GeO₂ (a-GeO₂) have been extensively studied.^{1–15} At ambient pressure, both a-SiO₂ and a-GeO₂ are characterized by 4-fold coordinated Si and Ge, respectively, forming corner-linked AO₄ tetrahedral networks.³ Upon compression, the coordination number (CN) of the A cation in a-SiO₂ and a-GeO₂ gradually increases from 4 to 6 at pressures of 18–40 GPa^{4–6} and 5–15 GPa,^{7–10} respectively. A CN = 6 plateau is reached at ~ 40 – 100 GPa⁵ and ~ 15 – 50 GPa^{9,11} for a-SiO₂ and a-GeO₂, respectively. Whether additional transformations with CN > 6 can occur under further compression is controversial. X-ray spectroscopy studies show that CNs in a-SiO₂¹³ and a-GeO₂¹⁴ remain at ~ 6 over wide pressure ranges of 65–120 and 15–100 GPa, respectively. X-ray diffraction (XRD) experiments, however, show continuous and nearly linear increases in CN, with the CNs of a-SiO₂ and a-GeO₂ increasing to ~ 7 at 172 GPa¹² and ~ 7.4 at 92 GPa,¹¹ respectively. So far, no CN > 6 plateau has been found in any amorphous dioxides.

TiO₂ is a low-pressure analogue of SiO₂ in studying its high-pressure structural polymorphs.¹⁶ Investigation of amorphous TiO₂ (a-TiO₂) should provide new insight into further CN changes. It is reported that nanograined TiO₂ undergoes

pressure-induced amorphization at ~ 13 – 16 GPa,^{17,18} with the characteristic structural motifs similar to that of 7-fold coordinated crystalline baddeleyite TiO₂.¹⁷ An *ab initio* simulation study¹⁹ predicts that the CN of Ti in a-TiO₂ gradually increases from 6 to 7 with an increase in pressure up to 55 GPa. Experimentally, however, the pressure corresponding to the change in CN from 6 to 7 is significantly lower^{17,18} than those in the simulation.¹⁹ The simulation study also predicts a further change in CN to 8 at 60 GPa, above which CN stays unchanged up to 75 GPa, implying that the next energetically favored structure of a-TiO₂ may have CN = 8.

We compressed TiO₂-B nanoribbons that display amorphization at a pressure range of ~ 13.4 – 16.3 GPa¹⁷ and measured the structure *in situ* using a double-stage large-volume Paris–Edinburgh cell¹¹ combined with the multiangle energy dispersive X-ray diffraction technique.²⁰ We found that the CN of Ti of a-TiO₂ continuously increases from 7.2 ± 0.3 at 15.7 GPa to 8.8 ± 0.3 at 70.2 GPa. Over a wide pressure range of 70.2–85.7 GPa, CN remains constant at 8.9 ± 0.3 . These results shed new light on pressure-induced polyamorphism in a-AO₂, suggesting that the CN plateau above 6 is 9 for dioxide glasses under extreme compression.

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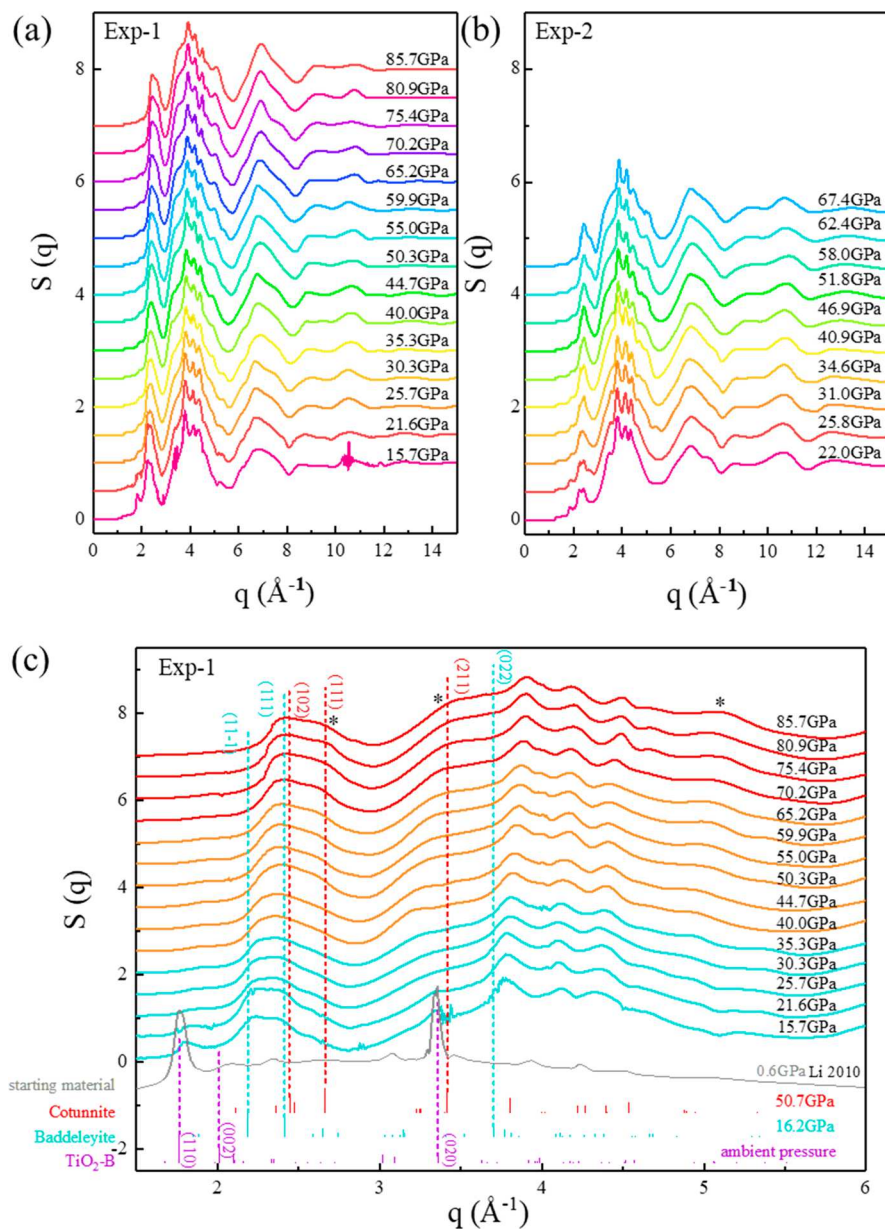


Figure 1. Obtained structure factors $S(q)$ of a- TiO_2 from (a) Exp-1 and (b) Exp-2. (c) $S(q)$ data from Exp-1 (from $q = 1.5$ to 6 \AA^{-1}) are compared with those of the starting material (gray line)¹⁷ and the diffraction peaks of various crystalline polymorphs of TiO_2 . Ticks at the bottom indicate peak positions of the crystalline polymorphs: $\text{TiO}_2\text{-B}$ (purple), baddeleyite (blue), and cotunnite (red). Main peak positions are indicated by long dashed vertical lines. The asterisks indicate the newly formed amorphous peaks under high pressure.

Structure factors, $S(q)$, of a- TiO_2 were determined at pressures of ≤ 85.7 GPa (Exp-1) and ≤ 67.4 GPa (Exp-2) in two experimental runs (panels a and b, respectively, of Figure 1). Over the entire pressure ranges, $S(q)$ exhibits five peaks centered around 2.4, 4, 7, 8.5, and 11 \AA^{-1} . All of these peak positions are close to the $S(q)$ peaks from a simulation study at ambient pressure,²¹ except a small one located around 8.5 \AA^{-1} . Three weak nanocrystalline peaks are superimposed on the second amorphous peak at $\sim 4 \text{ \AA}^{-1}$, which persists over the entire pressure range. These peaks correspond to the (023), (-222), and (313) planes of the $\text{TiO}_2\text{-B}$ phase.¹⁷ As shown in the Supporting Information, the presence of these remaining crystalline peaks does not significantly affect the structural analysis of the a- TiO_2 sample.

At 15.7 GPa, two characteristic peaks near 1.8 and 3.35 \AA^{-1} , corresponding to the (110) and (020) planes of the $\text{TiO}_2\text{-B}$

structure, respectively, were visible (Figure 1c). With an increase in pressure, these two peaks completely disappeared above 30.3 GPa, which is consistent with the result reported previously.¹⁷ The first amorphous peak displays a broad top from ~ 2.2 to 2.4 \AA^{-1} at 15.7 GPa. This q range corresponds to the interplane distances of (11-1) ($q \approx 2.19 \text{ \AA}^{-1}$) and (111) ($q \approx 2.42 \text{ \AA}^{-1}$) of baddeleyite TiO_2 at 16.2 GPa.²² With an increase in pressure, the shape of the first peak gradually changed to be asymmetrical. Above 50.3 GPa, a new shoulder appeared at the high q side ($\sim 2.65 \text{ \AA}^{-1}$) with its intensity increasing as pressure was further increased. Eventually, above 70.2 GPa, the first peak developed a new broad top from ~ 2.4 to 2.65 \AA^{-1} corresponding to the (102) ($q \approx 2.45 \text{ \AA}^{-1}$) and (111) ($q \approx 2.66 \text{ \AA}^{-1}$) planes of the 9-fold coordinated cotunnite TiO_2 at 50.7 GPa.²² Meanwhile, above 40.0 GPa, two peaks emerged at ~ 3.25 and $\sim 4.95 \text{ \AA}^{-1}$ with their

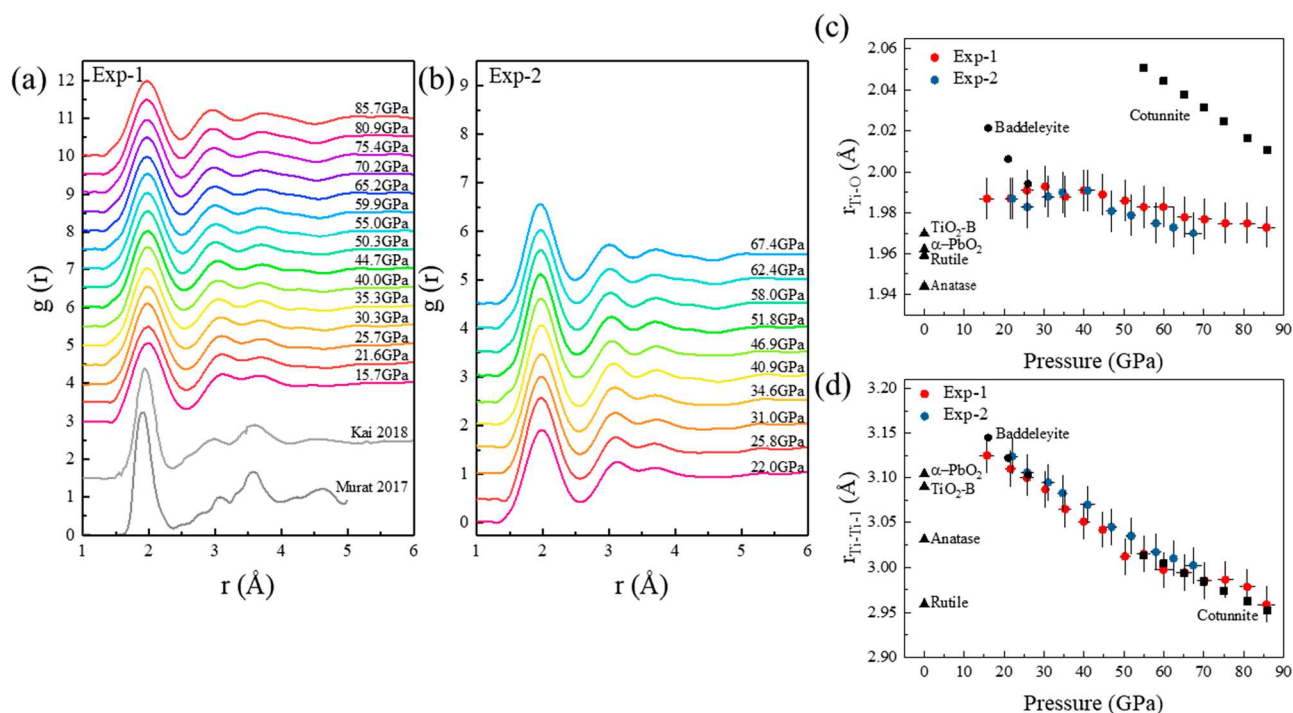


Figure 2. (a) Pair distribution functions $g(r)$ from Exp-1 (colored lines) together with that from simulation at ambient pressure (gray line).^{19,21} (b) $g(r)$ from Exp-2. (c and d) Colored circles are $r_{\text{Ti-O}}$ and $r_{\text{Ti-Ti-1}}$ obtained from the first and second peak positions of $g(r)$, respectively. Black symbols are the calculated average $r_{\text{Ti-O}}$ and $r_{\text{Ti-Ti-1}}$ of TiO_2 crystalline polymorphs.²²

positions shifting to high q as the pressure was increased to 70.2 GPa. These changes in $S(q)$ indicate a gradual structural change from 15.7 to 70.2 GPa. At higher pressures from 70.2 to 85.7 GPa, no clear changes in $S(q)$ were observed (Figure 1(c)).

Pair distribution functions, $g(r)$, were derived for a- TiO_2 as shown in Figure 2. The first three $g(r)$ peaks near 1.99, 3.1, and 3.7 Å are assigned to represent Ti–O ($r_{\text{Ti-O}}$), Ti–Ti-1 ($r_{\text{Ti-Ti-1}}$), and Ti–Ti-2 ($r_{\text{Ti-Ti-2}}$) distances, respectively. The O–O distance ($r_{\text{O-O}}$) expected to be centered roughly around 2.4 Å¹⁹ is barely recognizable. This may be due to (1) the relative weak scattering power of oxygen and (2) the $r_{\text{O-O}}$ peak, which decreases rapidly with an increase in pressure, overlapping with the intense $r_{\text{Ti-O}}$ peak.¹⁹ All peaks in the obtained $g(r)$ are broader than those from simulations,^{19,21} partly because the Lorch modification function was applied in our Fourier transformation process. $r_{\text{Ti-Ti-1}}$ and $r_{\text{Ti-Ti-2}}$ are attributed to the distances of two Ti atoms with edge-sharing (or face-sharing) and corner-sharing polytopes, respectively.²¹ The intensity ratios of the Ti–Ti-1 versus Ti–Ti-2 peaks are reversed when compared to the ambient-pressure simulation $g(r)$ (Figure 2a,b). This suggests that the fractions of edge-sharing and face-sharing interpolytope connections in compressed a- TiO_2 are higher than the 6-fold-coordinated a- TiO_2 at ambient pressure.

Major factors affecting the A–O distance in a- AO_2 under high pressure include compression and local structural changes. Compression tends to decrease the A–O distance, while structural changes, often involving an increase in CN, tend to increase the A–O distance with an increase in pressure. In the latter case, the increased distance is commonly expressed as the increased (apparent) ionic radius for the A cation.²³ Figure 2c shows clearly that the $r_{\text{Ti-O}}$ values of a- TiO_2 above 10 GPa are greater than the average ambient-pressure

Ti–O distances in 6-fold crystalline structures (TiO_2 -B, rutile, α - PbO_2 , and anatase),²² suggesting that the CN of Ti is likely higher than 6. Figure 2c also shows that $r_{\text{Ti-O}}$ is more or less constant at ~ 1.99 Å between 15.7 and 40.0 GPa, suggesting that the competing effects of compression and structural change nearly cancel each other. Because the effect of compression on Ti–O distance is generally a gradual and smooth process,¹⁷ the CN in a- TiO_2 likely increases gradually with an increase in pressure from 15.7 to 40 GPa. Above 40 GPa, $r_{\text{Ti-O}}$ becomes negatively dependent on pressure, from 1.99 Å at 40.0 GPa to 1.97 Å at 85.7 GPa, with a slope much smaller than those of crystalline TiO_2 phases (Figure 2c). The decrease in $r_{\text{Ti-O}}$ with pressure suggests that the effect of compression becomes greater than that of the CN change between 40 and 85.7 GPa.

Figure 2d shows that $r_{\text{Ti-Ti-1}}$ in a- TiO_2 decreases almost linearly with an increase in pressure. Interestingly, the compression behavior of $r_{\text{Ti-Ti-1}}$ in a- TiO_2 is similar to the average edge-sharing Ti–Ti distance of baddeleyite TiO_2 and the average face-sharing Ti–Ti distance of cotunnite TiO_2 . Because $r_{\text{Ti-Ti-1}}$ represents how closely each TiO_x polyhedron is connected to its neighbors, the compression behavior of $r_{\text{Ti-Ti-1}}$ in a- TiO_2 suggests that the interpolyhedron connection in a- TiO_2 may be close to those in the 7- and 9-fold coordinated crystalline structures.

We determined the CN of Ti in a- TiO_2 by fitting the first peak of $g(r)$ with the pair function method²⁴ (more details in the Supporting Information). The CN was determined to be 7.2 ± 0.3 at 15.7 GPa, and then it quickly increased to 8.4 ± 0.3 at 40.0 GPa (Figure 3a). Upon further compression, the CN increased to 8.8 ± 0.3 at 70.2 GPa and then remained constant around 8.8–8.9 up to the highest pressure of 85.7 GPa. With all of the results from the $S(q)$, $g(r)$, atomic distances, and CNs (Figures 1–3), structural evolution of a-

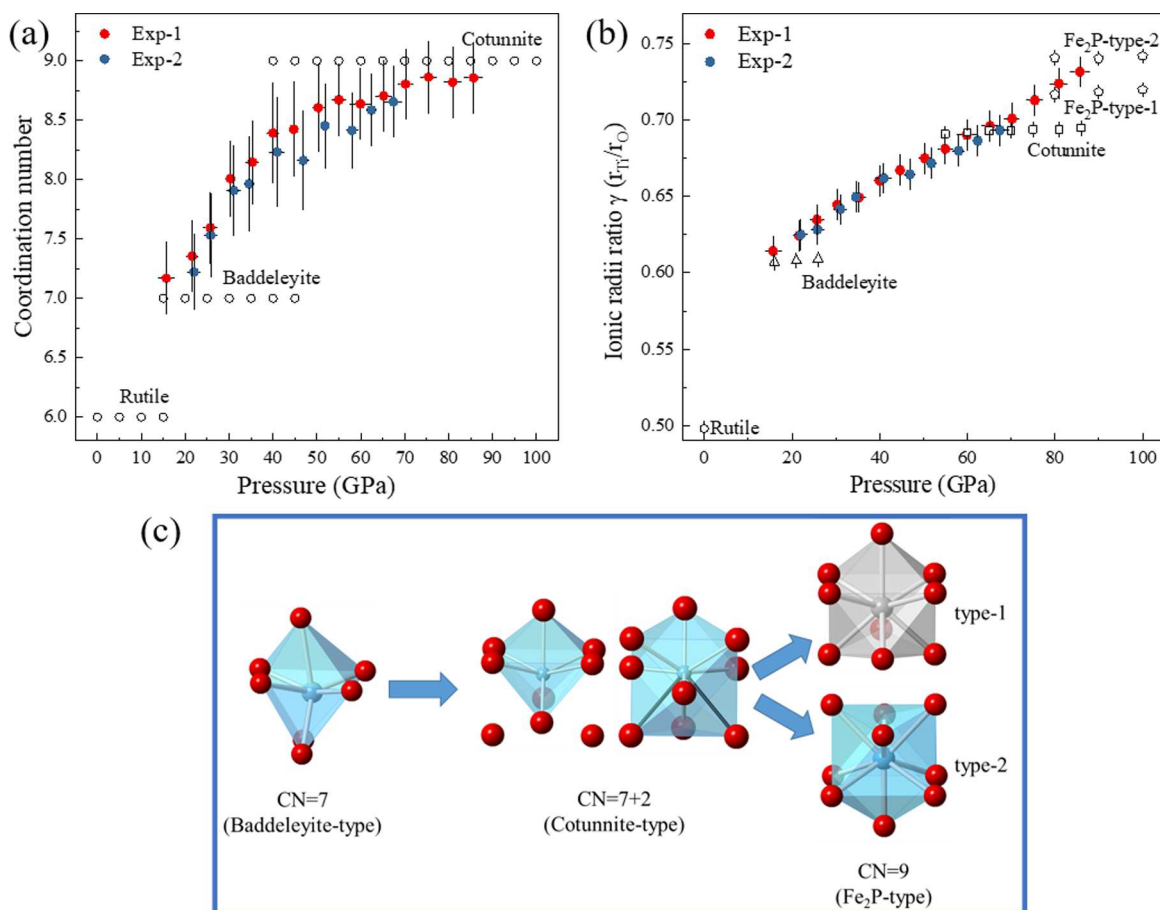


Figure 3. (a) Coordination number (CN) of Ti in a-TiO₂ as a function of pressure. Numerical values of the CN are summarized in the Supporting Information. (b) Ionic radius ratio ($\gamma = r_{\text{Ti}}/r_{\text{O}}$) as a function of pressure. Here, a-TiO₂ data (filled circles) are compared with those of TiO₂ crystalline polymorphs (empty black symbols). (c) Schematics showing geometric features of different coordination motifs in crystalline TiO₂. Red and blue spheres represent oxygen and titanium atoms, respectively.

TiO₂ may be divided into three stages over the pressure range. From 15.7 to 40.0 GPa, a-TiO₂ is dominated by 7-fold coordinated baddeleyite-like motifs. Above 40.0 GPa, the fraction of 9-fold coordinated cotunnite-like motifs increases with pressure to become the dominant component at 70.2 GPa. Above 70.2 GPa, it is dominantly in 9-fold coordinated up to the highest pressure of 85.7 GPa in this study, displaying a plateau.

To understand the plateau at CN \approx 9 above 70.2 GPa, we examine both crystalline and amorphous structures of TiO₂. We note that, unlike the 7-fold coordinated baddeleyite, there are two 9-fold coordinated polymorphs (cotunnite and Fe₂P) that have similar calculated enthalpies (the difference is <0.1 eV/f.u. at 0 K)^{25,26} and are stable over a very wide range of pressure (35–636 GPa).²⁶ It has been proposed in AB binary compounds²⁷ that the dense packing configuration strongly depends on the ratio (γ) of the ionic radii of the A (r_{A}) and B (r_{B}) atoms. We also note that the structural features of local maxima of densely packed binary hard spheres with varying γ depend on the CN of the A atoms. Kummerfeld's study²⁷ provides an inspiration for correlating pressure-induced CN changes of both crystalline and amorphous materials. To investigate the relationship between CN and $\gamma = r_{\text{A}}/r_{\text{O}}$ in TiO₂, we use simulation results of known TiO₂ polymorphs, namely, rutile (CN = 6), baddeleyite (CN = 7), cotunnite (CN = 9), and Fe₂P (CN = 9),^{22,25} under different pressures, and then

calculate the γ values of these polymorphs by using the mean fictive ionic radius (MEFIR) method,²⁸ which weighs shorter bond distances more than longer bond distances. As shown in Figure 3b, within any given crystalline polymorph, γ only exhibits a slight increase ($\sim 0.0002 \text{ GPa}^{-1}$) upon compression. However, across different polymorphs, γ changes rapidly: ~ 0.61 for baddeleyite, ~ 0.69 for cotunnite, ~ 0.72 for Fe₂P type 1, and ~ 0.74 for Fe₂P type 2. Thus, the ratio γ may provide a key to understanding the CN \approx 9 plateau of a-TiO₂.

We assume that the r_{O} in a-TiO₂ is the same as that of crystalline polymorphs in the corresponding pressure ranges.²² The r_{O} values for the baddeleyite TiO₂ at 15.7–25.8 GPa and cotunnite TiO₂ at 55.0–85.7 GPa may be expressed by a linear relation (Figure S2). This linear relation is also consistent with a simulation study that shows that the O–O distance of a-TiO₂ exhibits a nearly linear shift.¹⁹ By applying this r_{O} relation to a-TiO₂, we calculate $r_{\text{Ti}} = r_{\text{Ti-O}} - r_{\text{O}}$ based on our $g(r)$ results. The obtained γ value is 0.614 at 15.7 GPa, which is similar to that of baddeleyite TiO₂ (Figure 3b). At 70.2 GPa, γ is 0.701, similar to that of cotunnite TiO₂. In the pressure range of 15.7–70.2 GPa, the increase in γ is mainly due to the increase in CN, which results in a significant increase in r_{Ti} . At pressures of >70.2 GPa, γ of a-TiO₂ increases continuously from 0.701 to 0.732, a value between that of Fe₂P type 1 ($\gamma \approx 0.72$) and Fe₂P type 2 ($\gamma \approx 0.74$).

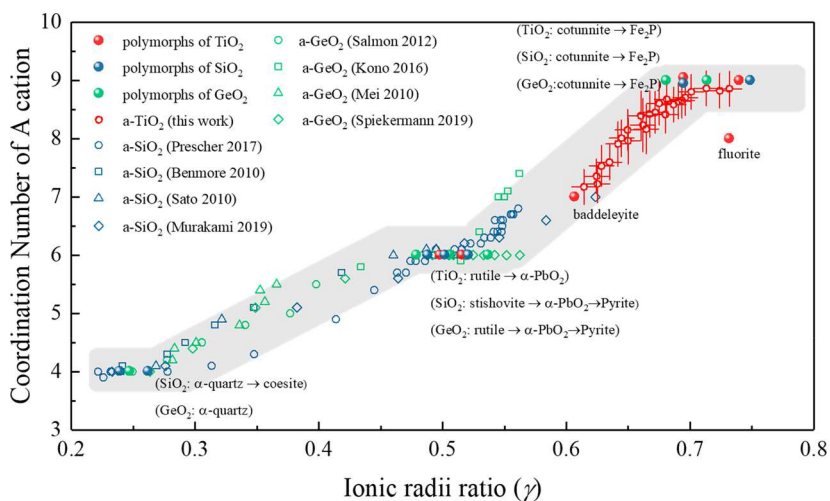


Figure 4. Relationship between the ionic radius ratio and the coordination number of cations. The data of a-AO₂ (empty symbols) are compared with those of crystalline polymorphs (filled circles) with different coordinated structures.

If the structural motifs of a-TiO₂ are assumed to be similar to those of crystalline polymorphs at the corresponding pressures, the above comparisons of γ values provide a hint about the origin of the CN \approx 9 plateau. The geometric features of different coordination motifs are shown in Figure 3c. For a cotunnite-type polyhedron, the two longest bonds (colored black) are \sim 18% longer than the mean Ti–O distance. Thus, cotunnite may be viewed as a (7+2) coordinated structure with a TiO₇ polyhedron modified from baddeleyite-type and two other secondary oxygen ions. Under compression, a cotunnite-type polyhedron may undergo continuous modifications from (7+2) coordination to a more uniform TiO₉ Fe₂P-type polyhedron. As shown in Figure 3b, even though γ continues to increase with pressure above 70.2 GPa, the basic coordination motifs in a-TiO₂ remain a configuration with CN \sim 9, thus forming a coordination plateau. With further compression, a-TiO₂ may transform to a higher CN with other structural motifs (such as one similar to the *I4/mmm* phase with CN = 10).²⁶

Finally, to examine the applicability of the relationship mentioned above to a-AO₂ (A = Ti, Si, or Ge), we calculate γ values for them^{4,5,8,10–12,14,15} and associated crystalline polymorphs [α -quartz, coesite (CN = 4), rutile/stishovite, α -PbO₂, pyrite (CN = 6), cotunnite, and Fe₂P (CN = 9)] of SiO₂^{29–32} and GeO₂^{25,29,33} by the MEFIR method. All three compounds, regardless of whether they are crystalline and amorphous, show remarkably consistent behavior (Figure 4). CNs of the A cations exhibit plateaus at CN values of 4, 6, and 9 over wide ranges of γ . For crystalline materials, each of these plateaus is associated with at least two polymorphs over the γ range. The CN of amorphous materials follows closely these plateaus. Between the plateaus, the CN of amorphous materials increases gradually and almost linearly. This CN– γ relationship for a-AO₂ shows that the local structure change in a-AO₂ is closely related to the pressure-induced AO₂ crystalline polymorphs. These data imply a unified relationship between CN and γ in a-AO₂. The existence of 9-fold coordinated a-TiO₂ and the plateau at CN \approx 9 strongly suggests that similar amorphous structures and plateau may exist in a-SiO₂ and a-GeO₂ at higher pressures. Furthermore, the CN of many forms of a-AO₂ under high pressure is often difficult to determine experimentally, but values of r_{A-O} can be directly obtained

from the first peak position in $g(r)$. Thus, the CN in a-AO₂ may be inferred by using the CN– γ relationship.

■ ASSOCIATED CONTENT

📄 Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcllett.9b03378>.

Details of the experimental and analytical methods (PDF)

■ AUTHOR INFORMATION

Corresponding Authors

*E-mail: kono.yoshio.rj@ehime-u.ac.jp.

*E-mail: gyshen@anl.gov.

ORCID

Yu Shu: 0000-0002-0903-435X

Quanjun Li: 0000-0002-4718-4156

Changyong Park: 0000-0002-3363-5788

Guoyin Shen: 0000-0001-5146-1147

Present Address

[†]Y.K.: Geodynamics Research Center, Ehime University, Ehime 790-8577, Japan.

Notes

The authors declare no competing financial interest.

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