

Influence Function based Data Poisoning Attacks to Top- N Recommender Systems

Minghong Fang
Iowa State University
myfang@iastate.edu

Neil Zhenqiang Gong
Duke University
neil.gong@duke.edu

Jia Liu
Iowa State University
jiali@iastate.edu

ABSTRACT

Recommender system is an essential component of web services to engage users. Popular recommender systems model user preferences and item properties using a large amount of crowdsourced user-item interaction data, e.g., rating scores; then top- N items that match the best with a user's preference are recommended to the user. In this work, we show that an attacker can launch a *data poisoning attack* to a recommender system to make recommendations as the attacker desires via injecting fake users with carefully crafted user-item interaction data. Specifically, an attacker can trick a recommender system to recommend a target item to as many normal users as possible. We focus on matrix factorization based recommender systems because they have been widely deployed in industry. Given the number of fake users the attacker can inject, we formulate the crafting of rating scores for the fake users as an optimization problem. However, this optimization problem is challenging to solve as it is a non-convex integer programming problem. To address the challenge, we develop several techniques to approximately solve the optimization problem. For instance, we leverage *influence function* to select a subset of normal users who are influential to the recommendations and solve our formulated optimization problem based on these influential users. Our results show that our attacks are effective and outperform existing methods.

CCS CONCEPTS

• Security and privacy → Web application security.

KEYWORDS

Adversarial recommender systems, data poisoning attacks, adversarial machine learning.

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1 INTRODUCTION

Recommender system is a key component of many web services to help users locate items they are interested in. Many recommender systems are based on collaborative filtering. For instance, given a large amount of user-item interaction data (we consider rating scores in this work) provided by users, a recommender system

learns to model latent users' preferences and items' features, and then the system recommends top- N items to each user, where the features of the top- N items best match with the user's preference.

As a recommender system is driven by user-item interaction data, an attacker can manipulate a recommender system via injecting fake users with fake user-item interaction data to the system. Such attacks are known as *data poisoning attacks* [9, 10, 17, 19, 23, 34, 38]. Several recent studies designed recommender-system-specific data poisoning attacks to association-rule-based [38], graph-based [10] and matrix-factorization-based recommender systems [19]. However, how to design customized attacks to matrix-factorization-based top- N recommender systems remains an open question even though such recommender systems have been widely deployed in the industry. In this work, we aim to bridge the gap. In particular, we aim to design an optimized data poisoning attack to *matrix-factorization-based top- N recommender systems*. Suppose that an attacker can inject m fake users into the recommender system and each fake user can rate at most n items, which we call *filler items*. Then, the key question is: *how to select the filler items and assign rating scores to them such that an attacker-chosen target item is recommended to as many normal users as possible?* To answer this question, we formulate an optimization problem for selecting filler items and assigning rating scores for the fake users, with an objective to maximize the number of normal users to whom the target item is recommended.

However, it is challenging to solve this optimization problem because it is a non-convex integer programming problem. To address the challenge, we propose a series of techniques to approximately solve the optimization problem. First, we propose to use a loss function to approximate the number of normal users to whom the target item is recommended. We relax the integer rating scores to continuous variables and convert them back to integer rating scores after solving the reformulated optimization problem. Second, to enhance the effectiveness of our attack, we leverage the *influence function approach* inspired by the interpretable machine learning literature [14, 15, 33] to account for the reality that the top- N recommendations may be only affected by a subset S of influential users. For convenience, throughout the rest of this paper, we refer to our attack as S -attack. We show that the influential user selection subproblem enjoys the *submodular* property, which guarantees a $(1 - 1/e)$ approximation ratio with a simple greedy selection algorithm. Lastly, given S , we develop a gradient-based optimization algorithm to determine rating scores for the fake users.

We evaluate our S -attack and compare it with multiple baseline attacks on two benchmark datasets, including Yelp and Amazon Digital Music (Music). Our results show that our attacks can effectively promote a target item. For instance, on the Yelp dataset,

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when injecting only 0.5% of fake users, our attack can make a randomly selected target item appear in the top- N recommendation lists of 150 times more normal users. Our \mathcal{S} -attack outperforms the baseline attacks and continues to be effective even if the attacker does not know the parameters of the target recommender system. We also investigate the effects of our attacks on recommender systems that are equipped with fake users detection capabilities. For this purpose, we train a binary classifier to distinguish between fake users and normal ones. Our results show that this classifier is effective against traditional attack schemes, e.g., PGA attack [19], etc. Remarkably, we find that our influence-function-based attack continues to be effective. The reason is that our proposed attack is designed with stealth in mind, and the detection method can detect some fake users but miss a large fraction of them. In summary, our contributions are as follows:

- We propose the first data poisoning attack to matrix-factorization-based Top- N recommender systems, which we formulate as a non-convex integer optimization problem.
- We propose a series of techniques to approximately solve the optimization problem with provable performance guarantee.
- We evaluate our \mathcal{S} -attack and compare it with state-of-the-art using two benchmark datasets. Our results show that our attack is effective and outperforms existing ones.

2 RELATED WORK

Data poisoning attacks to recommender systems: The security and privacy issues in machine learning models have been studied in many scenarios [24, 29–31, 39, 41, 42]. The importance of data poisoning attacks has also been recognized in recommender systems [7, 21–23, 28, 37]. Earlier work on poisoning attacks against recommender systems are mostly agnostic to recommender systems and do not achieve satisfactory attack performance, e.g., random attack [17] and average attack [17]. Recently, there is a line of work focusing on attacking specific types of recommender systems [10, 19, 38]. For example, Fang *et al.* [10] proposed efficient poisoning attacks to graph-based recommender systems. They injected fake users with carefully crafted rating scores to the recommender systems in order to promote a target item. They modeled the attack as an optimization problem to decide the rating scores for the fake users. Li *et al.* [19] proposed poisoning attacks to matrix-factorization-based recommender systems. Instead of attacking the top- N recommendation lists, their goal was to manipulate the predictions for all missing entries of the rating matrix. As a result, the effectiveness of their attacks is unsatisfactory in matrix-factorization-based top- N recommender systems.

Data poisoning attacks to other systems: Data poisoning attacks generally refer to attacks that manipulate the training data of a machine learning or data mining system such that the learnt model makes predictions as an attacker desires. Other than recommender systems, data poisoning attacks were also studied for other systems. For instance, existing studies have demonstrated effective data poisoning attacks can be launched to anomaly detectors [27], spam filters [25], SVMs [4, 36], regression methods [12, 35], graph-based methods [32, 43], neural networks [5, 11, 20], and federated learning [9], which significantly affect their performance.

3 PROBLEM FORMULATION

3.1 Matrix-Factorization-Based Recommender Systems: A Primer

A matrix-factorization-based recommender system [16] maps users and items into latent factor vectors. Let \mathcal{U} , \mathcal{I} and \mathcal{E} denote the user, item and rating sets, respectively. We also let $|\mathcal{U}|$, $|\mathcal{I}|$ and $|\mathcal{E}|$ denote the numbers of users, items and ratings, respectively. Let $\mathbf{R} \in \mathbb{R}^{|\mathcal{U}| \times |\mathcal{I}|}$ represent the user-item rating matrix, where each entry r_{ui} denotes the score that user u rates the item i . Let $\mathbf{x}_u \in \mathbb{R}^d$ and $\mathbf{y}_i \in \mathbb{R}^d$ denote the latent factor vector for user u and item i , respectively, where d is the dimension of latent factor vector. For convenience, we use matrices $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_{|\mathcal{U}|}]$ and $\mathbf{Y} = [\mathbf{y}_1, \dots, \mathbf{y}_{|\mathcal{I}|}]$ to group all \mathbf{x} - and \mathbf{y} -vectors. In matrix-factorization-based recommender systems, we aim to learn \mathbf{X} and \mathbf{Y} via solving the following optimization problem:

$$\arg \min_{\mathbf{X}, \mathbf{Y}} \sum_{(u, i) \in \mathcal{E}} (r_{ui} - \mathbf{x}_u^\top \mathbf{y}_i)^2 + \lambda \left(\sum_u \|\mathbf{x}_u\|_2^2 + \sum_i \|\mathbf{y}_i\|_2^2 \right), \quad (1)$$

where $\|\cdot\|_2$ is the ℓ_2 norm and λ is the regularization parameter. Then, the rating score that a user u gives to an unseen item i is predicted as $\hat{r}_{ui} = \mathbf{x}_u^\top \mathbf{y}_i$, where \mathbf{x}_u^\top denotes the transpose of vector \mathbf{x}_u . Lastly, the N unseen items with the highest predicted rating scores are recommended to each user.

3.2 Threat Model

Given a target item t , the goal of the attacker is to promote item t to as many normal users as possible and maximize the hit ratio $h(t)$, which is defined as the fraction of normal users whose top- N recommendation lists include the target item t . We assume that the attacker is able to inject some fake users into the recommender system, each fake user will rate the target item t with high rating score and give carefully crafted rating scores to other well-selected items. The attacker may have full knowledge of the target recommender system (e.g., all the rating data, the recommendation algorithm). The attacker may also only have partial knowledge of the target recommender system, e.g., the attacker only has access to some ratings. We will show that our attacks are still effective when the attacker has partial knowledge of the target recommender system.

3.3 Attack Strategy

We assume that the rating scores of the target recommender system are integer-valued and can only be selected from the set $\{0, 1, \dots, r_{\max}\}$, where r_{\max} is the maximum rating score. We assume that the attacker can inject m fake users into the recommender system. We denote by \mathcal{M} the set of m fake users. Each fake user will rate the target item t and at most n other carefully selected items (called *filler items*). We consider each fake user rates at most n filler items to avoid being easily detected. We let \mathbf{r}_v and Ω_v denote the rating score vector of fake user v and the set of items rated by v , respectively, where $v \in \mathcal{M}$ and $|\Omega_v| \leq n + 1$. Then, r_{vi} is the score that user v rates the item i , $i \in \Omega_v$. Clearly, Ω_v satisfies $|\Omega_v| = \|\mathbf{r}_v\|_0$, where $\|\cdot\|_0$ is the ℓ_0 norm (i.e., the number of non-zero entries in a vector). The attacker's goal is to find an optimal rating score vector for each fake user v to maximize the hit ratio $h(t)$. We formulate

this hit ratio maximization problem (HRM) as follows:

$$\text{HRM: } \max h(t) \quad (2)$$

$$\text{s.t. } |\Omega_v| \leq n + 1, \quad \forall v \in \mathcal{M}, \quad (3)$$

$$r_{vi} \in \{0, 1, \dots, r_{max}\}, \quad \forall v \in \mathcal{M}, \forall i \in \Omega_v. \quad (4)$$

Problem HRM is an integer programming problem and is NP-hard in general. Thus, finding an optimal solution is challenging. In the next section, we will propose techniques to approximately solve the problem.

4 OUR SOLUTION

We optimize the rating scores for fake users one by one instead of optimizing for all the m fake users simultaneously. In particular, we repeatedly optimize the rating scores of one fake user and add the fake user to the recommender system until we have m fake users. However, it is still challenging to solve the HRM problem even if we consider only one fake user. To address the challenge, we design several techniques to approximately solve the HRM problem for one fake user. First, we relax the discrete ratings to continuous data and convert them back to discrete ratings after solving the problem. Second, we use a differentiable loss function to approximate the hit ratio. Third, instead of using all normal users, we use a selected subset of influential users to solve the HRM problem, which makes our attack more effective. Fourth, we develop a gradient-based method to solve the HRM problem to determine the rating scores for the fake user.

4.1 Relaxing Rating Scores

We let vector $\mathbf{w}_v = [w_{vi}, i \in \Omega_v]^\top$ be the relaxed continuous rating score vector of fake user v , where w_{vi} is the rating score that user v gives to the item i . Since $r_{vi} \in \{0, 1, \dots, r_{max}\}$ is discrete, which makes it difficult to solve the optimization problem defined in (2), we relax the discrete rating score r_{vi} to continuous variables w_{vi} that satisfy $w_{vi} \in [0, r_{max}]$. Then, we can use gradient-based methods to compute \mathbf{w}_v . After we solve the optimization problem, we convert each w_{vi} back to a discrete integer value in the set $\{0, 1, \dots, r_{max}\}$.

4.2 Approximating the Hit Ratio

We let Γ_u be the set of top- N recommended items for a user u , i.e., Γ_u consists of the N items that u has not rated before and have the largest predicted rating scores. To approximate the optimization problem defined in (2), we define a loss function that is subject to the following rules: 1) for each item $i \in \Gamma_u$, if $\hat{r}_{ui} < \hat{r}_{ut}$, then the loss is small, where \hat{r}_{ui} and \hat{r}_{ut} are the predicted rating scores that user u gives to item i and target item t , respectively; 2) the higher target item t ranks in Γ_u , the smaller the loss. Based on these rules, we reformulate the HRM problem as the following problem:

$$\begin{aligned} \min_{\mathbf{w}_v} \mathcal{L}_{\mathcal{U}}(\mathbf{w}_v) &= \sum_{u \in \mathcal{U}} \sum_{i \in \Gamma_u} g(\hat{r}_{ui} - \hat{r}_{ut}) + \eta \|\mathbf{w}_v\|_1 \\ \text{s.t. } w_{vi} &\in [0, r_{max}], \end{aligned} \quad (5)$$

where $g(x) = \frac{1}{1+\exp(-x/b)}$ is the Wilcoxon-Mann-Whitney loss function [2], b is the *width* parameter, η is the regularization parameter, and $\|\cdot\|_1$ is the ℓ_1 norm. Note that $g(\cdot)$ guarantees that

$\mathcal{L}_{\mathcal{U}}(\mathbf{w}_v) \geq 0$ and is differentiable. The ℓ_1 regularizer $\|\mathbf{w}_v\|_1$ aims to model the constraint that each fake user rates at most n filler items. In particular, the ℓ_1 regularizer makes a fake user's ratings small to many items and we can select the n items with the largest ratings as the filler items.

4.3 Determining the Set of Influential Users

It has been observed in [18, 33] that different training samples have different contributions to the solution quality of an optimization problem, and the performance of the model training could be improved if we drop some training samples with low contributions. Motivated by this observation, instead of optimizing the ratings of a fake user over all normal users, we solve the problem in (5) using a subset of *influential users*, who are the most responsible for the prediction of the target item before attack. We let $\mathcal{S} \subseteq \mathcal{U}$ represent the set of influential users for the target item t . For convenience, in what follows, we refer to our attack as \mathcal{S} -attack. Under the \mathcal{S} -attack, we further reformulate (5) as the following problem:

$$\begin{aligned} \min_{\mathbf{w}_v} \mathcal{L}_{\mathcal{S}}(\mathbf{w}_v) &= \sum_{u \in \mathcal{S}} \sum_{i \in \Gamma_u} g(\hat{r}_{ui} - \hat{r}_{ut}) + \eta \|\mathbf{w}_v\|_1 \\ \text{s.t. } w_{vi} &\in [0, r_{max}]. \end{aligned} \quad (6)$$

Next, we propose an influence function approach to determine \mathcal{S} and then solve the optimization problem defined in (6). We let $F(\mathcal{S}, t)$ denote the influence of removing all users in the set \mathcal{S} on the prediction at the target item t , where influence here is defined as the change of the predicted rating score. We want to find a set of influential users that have the largest influence on the target item t . Formally, the influence maximization problem can be defined as:

$$\max F(\mathcal{S}, t), \quad \text{s.t. } |\mathcal{S}| = \Delta, \quad (7)$$

where Δ is the desired set size (i.e., the number of users in set \mathcal{S}). However, it can be shown that the problem is NP-hard [13]. In order to solve the above influence maximization problem of (7), we first show how to measure the influence of one user, then we show how to approximately find a set of Δ users with the maximum influence.

We define $\pi(k, t)$ as the influence of removing user k on the prediction at the target item t :

$$\pi(k, t) \stackrel{\text{def}}{=} \sum_{j \in \Omega_k} \varphi((k, j), t), \quad (8)$$

where $\varphi((k, j), t)$ is the influence of removing edge (k, j) in the user-item bipartite on the prediction at the target item t , Ω_k is the set of items rated by user k . Then, the influence of removing user set \mathcal{S} on the prediction at the target item t can be defined as:

$$F(\mathcal{S}, t) \stackrel{\text{def}}{=} \sum_{k \in \mathcal{S}} \pi(k, t). \quad (9)$$

Since the influence of user and user set can be computed based on the edge influence $\varphi((k, j), t)$, the key challenge boils down to how to evaluate $\varphi((k, j), t)$ efficiently. Next, we will propose an appropriate influence function to efficiently compute $\varphi((k, j), t)$.

4.3.1 Influence Function for Matrix-factorization-based Recommender Systems. For a given matrix-factorization-based recommender system, we can rewrite (1) as follows:

$$\theta^* = \arg \min_{\theta} \frac{1}{|\mathcal{E}|} \sum_{(u, i) \in \mathcal{E}} \ell((u, i), \theta), \quad (10)$$

where $\theta \triangleq (X, Y)$. We let $\hat{r}_{ui}(\theta)$ denote the predicted rating score user u gives to item i under parameter θ , and $\hat{r}_{ui}(\theta) \triangleq \mathbf{x}_u^\top(\theta)\mathbf{y}_i(\theta)$.

If we increase the weight of the edge $(k, j) \in \mathcal{E}$ by some ζ , then the perturbed optimal parameter $\theta_{\zeta, (k, j)}^*$ can be written as:

$$\theta_{\zeta, (k, j)}^* = \arg \min_{\theta} \frac{1}{|\mathcal{E}|} \sum_{(u, i) \in \mathcal{E}} \ell((u, i), \theta) + \zeta \ell((k, j), \theta). \quad (11)$$

Since removing the edge (k, j) is equivalent to increasing its weight by $\zeta = -\frac{1}{|\mathcal{E}|}$, the influence of removing edge (k, j) on the prediction at edge (o, t) can be approximated as follows [8, 15]:

$$\begin{aligned} \Phi((k, j), (o, t)) &\stackrel{\text{def}}{=} \hat{r}_{ot}(\theta_{\zeta, (k, j)}^*) - \hat{r}_{ot}(\theta^*) \approx -\frac{1}{|\mathcal{E}|} \cdot \frac{\partial \hat{r}_{ot}(\theta_{\zeta, (k, j)}^*)}{\partial \zeta} \Big|_{\zeta=0} \\ &= \frac{1}{|\mathcal{E}|} \nabla_{\theta} \hat{r}_{ot}(\theta^*) H_{\theta^*}^{-1} \nabla_{\theta} \ell((k, j), \theta^*), \end{aligned} \quad (12)$$

where $\theta_{\zeta, (k, j)}^*$ is the optimal model parameter after removing edge (k, j) and H_{θ^*} represents the Hessian matrix of the objective function defined in (10). Therefore, the influence of removing edge (k, j) on the prediction at the target item t can be computed as:

$$\varphi((k, j), t) \stackrel{\text{def}}{=} \sum_{o \in \mathcal{U}} |\Phi((k, j), (o, t))|, \quad (13)$$

where $|\cdot|$ is the absolute value.

4.3.2 Approximation Algorithm for Determining \mathcal{S} . Due to the combinatorial complexity, solving the optimization problem defined in (7) remains an NP-hard problem. Fortunately, based on the observation that the influence of set \mathcal{S} (e.g., $F(\mathcal{S}, t)$) exhibits a diminishing returns property, we propose a greedy selection algorithm to find a solution to (7) with an approximation ratio guarantee. The approximation algorithm is a direct consequence of the following result, which says that the influence $F(\mathcal{S}, t)$ is monotone and submodular.

THEOREM 1 (SUBMODULARITY). *The influence $F(\mathcal{S}, t)$ is normalized, monotonically non-decreasing and submodular.*

PROOF. Define three sets \mathcal{A} , \mathcal{B} and \mathcal{C} , where $\mathcal{A} \subseteq \mathcal{B}$ and $\mathcal{C} = \mathcal{B} \setminus \mathcal{A}$. To simplify the notation, we use $F(\mathcal{A})$ to denote $F(\mathcal{A}, t)$. It is clear that the influence function is normalized since $F(\emptyset) = 0$. Since $F(\mathcal{B}) - F(\mathcal{A}) = \sum_{u \in \mathcal{B}} F(u) - \sum_{u \in \mathcal{A}} F(u) = \sum_{u \in \mathcal{B} \setminus \mathcal{A}} F(u) = F(\mathcal{C}) \geq 0$, which implies that the influence $F(\mathcal{S}, t)$ is monotonically non-decreasing. To show the submodular property, we let $\bar{\mathcal{S}}$ denote the complement of a set \mathcal{S} . Now, consider an arbitrary set \mathcal{D} , for which we have: $F(\mathcal{B} \cup \mathcal{D}) - F(\mathcal{A} \cup \mathcal{D}) = F((\mathcal{B} \cup \mathcal{D}) \setminus (\mathcal{A} \cup \mathcal{D})) \stackrel{(a)}{=} F(\mathcal{C} \setminus (\mathcal{C} \cap \mathcal{D})) \leq F(\mathcal{C}) = F(\mathcal{B}) - F(\mathcal{A})$, where (a) follows from $(\mathcal{B} \cup \mathcal{D}) \setminus (\mathcal{A} \cup \mathcal{D}) = (\mathcal{B} \cup \mathcal{D}) \cap \overline{(\mathcal{A} \cup \mathcal{D})} = \mathcal{C} \setminus (\mathcal{C} \cap \mathcal{D})$. Hence, the influence $F(\mathcal{S}, t)$ is submodular and the proof is completed. \square

Based on the submodular property of $F(\mathcal{S}, t)$, we propose Algorithm 1, a greedy-based selection method to select an influential user set \mathcal{S} with Δ users. More specifically, we first compute the influence of each user, and add the user with the largest influence to the candidate set \mathcal{S} (breaking ties randomly). Then, we recompute the influence of the remaining users in the set $\mathcal{U} \setminus \mathcal{S}$, and find the user with the largest influence within the remaining users, so on and so forth. We repeat this process until we find Δ users.

Algorithm 1 Greedy Influential User Selection.

Input: Rating matrix R , budget Δ .

Output: Influential user set \mathcal{S} .

```

1: Initialize  $\mathcal{S} = \emptyset$ .
2: while  $|\mathcal{S}| < \Delta$  do
3:   Select  $u = \arg \max_{k \in \mathcal{U} \setminus \mathcal{S}} \pi(k, t)$ .
4:    $\mathcal{S} \leftarrow \mathcal{S} \cup \{u\}$ .
5: end while
6: return  $\mathcal{S}$ .
```

Clearly, the running time of Algorithm 1 is linear. The following result states that Algorithm 1 achieves a $(1 - 1/e)$ approximation ratio, and its proof follows immediately from standard results in submodular optimization [26] and is omitted here for brevity.

THEOREM 2. *Let \mathcal{S} be the influential user set returned by Algorithm 1 and let \mathcal{S}^* be the optimal influential user set, respectively. It then holds that $F(\mathcal{S}, t) \geq \left(1 - \frac{1}{e}\right) F(\mathcal{S}^*, t)$.*

4.4 Solving Rating Scores for a Fake User

Given \mathcal{S} , we design a gradient-based method to solve the problem in (6). Recall that we let $\mathbf{w}_v = [w_{vi}, i \in \Omega_v]^\top$ be the rating vector for the current injected fake user v . We first determine his/her latent factors by solving Eq. (1), which can be restated as:

$$\begin{aligned} \arg \min_{\mathbf{X}, \mathbf{Y}, \mathbf{z}} \sum_{(u, i) \in \mathcal{E}'} (r_{ui} - \mathbf{x}_u^\top \mathbf{y}_i)^2 + \sum_{i \in \mathcal{I}} (w_{vi} - \mathbf{z}^\top \mathbf{y}_i)^2 \\ + \lambda \left(\sum_u \|\mathbf{x}_u\|_2^2 + \sum_i \|\mathbf{y}_i\|_2^2 + \|\mathbf{z}\|_2^2 \right), \end{aligned} \quad (14)$$

where $\mathbf{z} \in \mathbb{R}^d$ is the latent factor vector for fake user v , and \mathcal{E}' is the current rating set (rating set \mathcal{E} without attack plus injected ratings of fake users added before user v).

Toward this end, note that a subgradient of loss $\mathcal{L}_{\mathcal{S}}(\mathbf{w}_v)$ in (6) can be computed as:

$$\begin{aligned} G(\mathbf{w}_v) &= \sum_{u \in \mathcal{S}} \sum_{i \in \Omega_u} \nabla_{\mathbf{w}_v} g(\hat{r}_{ui} - \hat{r}_{ut}) + \eta \partial \|\mathbf{w}_v\|_1 \\ &= \sum_{u \in \mathcal{S}} \sum_{i \in \Omega_u} \frac{\partial g(\delta_{u, it})}{\partial \delta_{u, it}} (\nabla_{\mathbf{w}_v} \hat{r}_{ui} - \nabla_{\mathbf{w}_v} \hat{r}_{ut}) + \eta \partial \|\mathbf{w}_v\|_1, \end{aligned} \quad (15)$$

where $\delta_{u, it} = \hat{r}_{ui} - \hat{r}_{ut}$ and $\frac{\partial g(\delta_{u, it})}{\partial \delta_{u, it}} = \frac{g(\delta_{u, it})(1-g(\delta_{u, it}))}{b}$. The subgradient $\partial \|\mathbf{w}_v\|_1$ can be computed as $\frac{\partial}{\partial w_{vi}} \|\mathbf{w}_v\|_1 = \frac{w_{vi}}{\|w_{vi}\|}$. To compute $\nabla_{\mathbf{w}_v} \hat{r}_{ui}$, noting that $\hat{r}_{ui} = \mathbf{x}_u^\top \mathbf{y}_i$, then the gradient $\frac{\partial \hat{r}_{ui}}{\partial \mathbf{w}_v}$ can be computed as:

$$\frac{\partial \hat{r}_{ui}}{\partial \mathbf{w}_v} = \mathbf{J}_{\mathbf{w}_v}(\mathbf{x}_u)^\top \mathbf{y}_i + \mathbf{J}_{\mathbf{w}_v}(\mathbf{y}_i)^\top \mathbf{x}_u, \quad (16)$$

where $\mathbf{J}_{\mathbf{w}_v}(\mathbf{x}_u)$ and $\mathbf{J}_{\mathbf{w}_v}(\mathbf{y}_i)$ are the Jacobian matrices of \mathbf{x}_u and \mathbf{y}_i taken with respect to \mathbf{w}_v , respectively. Next, we leverage first-order stationary condition to approximately compute $\mathbf{J}_{\mathbf{w}_v}(\mathbf{x}_u)$ and $\mathbf{J}_{\mathbf{w}_v}(\mathbf{y}_i)$. Note that the optimal solution of problem in (14) satisfies the following first-order stationary condition:

$$\lambda \mathbf{x}_u = \sum_{i \in \Omega_u} (r_{ui} - \mathbf{x}_u^\top \mathbf{y}_i) \mathbf{y}_i, \quad (17)$$

$$\lambda \mathbf{y}_i = \sum_{u \in \Omega_i} (r_{ui} - \mathbf{x}_u^\top \mathbf{y}_i) \mathbf{x}_u + (w_{vi} - \mathbf{z}^\top \mathbf{y}_i) \mathbf{z}, \quad (18)$$

$$\lambda \mathbf{z} = \sum_{i \in \mathcal{I}} (w_{vi} - \mathbf{z}^\top \mathbf{y}_i) \mathbf{y}_i, \quad (19)$$

Algorithm 2 Our \mathcal{S} -Attack.

Input: Rating matrix R , target item t , parameters $m, n, d, \eta, \lambda, \Delta, b$.
Output: Fake user set \mathcal{M} .

- 1: Find influential user set \mathcal{S} according to Algorithm 1 for item t .
- 2: Let $\mathcal{M} = \emptyset$.
- 3: **for** $v = 1, \dots, m$ **do**
- 4: Solve the optimization problem defined in Eq. (6) to get \mathbf{w}_v .
- 5: Select n items with the largest values of w_{vi} as filler items.
- 6: Set $r_{vt} = r_{max}$.
- 7: Let μ_i and σ_i^2 be item i 's mean and variance of the scores rated by all normal users. Let $r_{vi} \sim \mathcal{N}(\mu_i, \sigma_i^2)$ be the random rating for each filler item i given by fake user v .
- 8: Let $R \leftarrow R \cup \{r_v\}$ and $\mathcal{M} \leftarrow \mathcal{M} \cup \{v\}$.
- 9: **end for**
- 10: **return** $\{r_v\}_{v=1}^m$ and \mathcal{M} .

where Ω_u is the set of items rated by user u and Ω^i is the set of users who rate the item i . Inspired by [19, 35], we assume that the optimality conditions given by (17)–(19) remain valid under an infinitesimal change of \mathbf{w}_v . Thus, setting the derivatives of (17)–(19) with respect to \mathbf{w}_v to zero and with some algebraic computations, we can derive that:

$$\frac{\partial \mathbf{x}_u}{\partial w_{vi}} = \mathbf{0}, \quad (20)$$

$$\frac{\partial \mathbf{y}_i}{\partial w_{vi}} = \left(\lambda \mathbf{I} + \sum_{u \in \Omega^i} \mathbf{x}_u \mathbf{x}_u^\top + \mathbf{z} \mathbf{z}^\top \right)^{-1} \mathbf{z}, \quad (21)$$

where \mathbf{I} is the identity matrix and (21) follows from $(\mathbf{x}_u^\top \mathbf{y}_i) \mathbf{x}_u = (\mathbf{x}_u \mathbf{x}_u^\top) \mathbf{y}_i$. Lastly, computing (20) and (21) for all $i \in \Gamma_u$ yields $\mathbf{J}_{\mathbf{w}_v}(\mathbf{x}_u)$ and $\mathbf{J}_{\mathbf{w}_v}(\mathbf{y}_i)$. Note that $\nabla_{\mathbf{w}_v} \hat{r}_{ut}$ can be computed in exactly the same procedure. Finally, after obtaining $G(\mathbf{w}_v)$, we can use the projected subgradient method [3] to solve \mathbf{w}_v for fake user v . With \mathbf{w}_v , we select the top n items with largest values of w_{vi} as the filler items. However, the values of \mathbf{w}_v obtained from solving (6) may not mimic the rating behaviors of normal users. To make our \mathcal{S} -attack more “stealthy,” we will show how to generate rating scores to disguise fake user v . We first set $r_{vt} = r_{max}$ to promote the target item t . Then, we generate rating scores for the filler items by rating each filler item with a normal distribution around the mean rating for this item by legitimate users, where $\mathcal{N}(\mu_i, \sigma_i^2)$ is the normal distribution with mean μ_i and variance σ_i^2 of item i . Our \mathcal{S} -attack algorithm is summarized in Algorithm 2.

5 EXPERIMENTS

5.1 Experimental Setup

5.1.1 Datasets. We evaluate our attack on two real-world datasets. The first dataset is **Amazon Digital Music (Music)** [1]. This dataset consists of 88,639 ratings on 15,442 music by 8,844 users. The second dataset is **Yelp** [40], which contains 504,713 ratings of 11,534 users on 25,229 items.

5.1.2 \mathcal{S} -Attack Variants. With different ways of choosing the influential user set \mathcal{S} , we compare three variants of our \mathcal{S} -attack.

\mathcal{U} -Top- N attack (\mathcal{U} -TNA): This variant uses all normal users as the influential user set \mathcal{S} , i.e., $\mathcal{S} = \mathcal{U}$, then solve Problem (6).

Table 1: HR@10 for different attacks.

Dataset	Attack size	None	PGA	SGLD	\mathcal{U} -TNA	\mathcal{S} -TNA-Rand	\mathcal{S} -TNA-Inf
Music	0.3%	0.0017	0.0107	0.0138	0.0498	0.0141	0.0543
	0.5%	0.0017	0.0945	0.1021	0.1355	0.0942	0.1521
	1%	0.0017	0.1803	0.1985	0.2492	0.2054	0.2567
	3%	0.0017	0.3681	0.3587	0.4015	0.3511	0.4172
	5%	0.0017	0.5702	0.5731	0.5832	0.5653	0.6021
Yelp	0.3%	0.0015	0.0224	0.0261	0.0619	0.0258	0.0643
	0.5%	0.0015	0.1623	0.1757	0.2304	0.1647	0.2262
	1%	0.0015	0.4162	0.4101	0.4323	0.4173	0.4415
	3%	0.0015	0.4924	0.5131	0.5316	0.4923	0.5429
	5%	0.0015	0.6442	0.6431	0.6806	0.6532	0.6813

\mathcal{S} -Top- N attack+Random (\mathcal{S} -TNA-Rand): This variant randomly selects Δ users as the influential user set \mathcal{S} , then solve Problem (6).

\mathcal{S} -Top- N attack+Influence (\mathcal{S} -TNA-Inf): This variant finds the influential user set \mathcal{S} by Algorithm 1, then solve Problem (6).

5.1.3 Baseline Attacks. We compare our \mathcal{S} -attack variants with the following baseline attacks.

Projected gradient ascent attack (PGA) [19]: PGA attack aims to assign high rating scores to the target items and generates filler items randomly for the fake users to rate.

Stochastic gradient Langevin dynamics attack (SGLD) [19]: This attack also aims to assign high rating scores to the target items, but it mimics the rating behavior of normal users. Each fake user will select n items with the largest absolute ratings as filler items.

5.1.4 Parameter Setting. Unless otherwise stated, we use the following default parameter setting: $d = 64$, $\Delta = 400$, $\eta = 0.01$, $b = 0.01$, and $N = 10$. Moreover, we set the attack size to be 3% (i.e., the number of fake users is 3% of the number of normal users) and the number of filler items is set to $n = 20$. We randomly select 10 items as our target items and the hit ratio (HR@ N) is averaged over the 10 target items, where HR@ N of a target item is the fraction of normal users whose top- N recommendation lists contain the target item. Note that our \mathcal{S} -attack is \mathcal{S} -TNA-Inf attack.

5.2 Full-Knowledge Attack

In this section, we consider the worst-case attack scenario, where the attacker has full knowledge of the recommender system, e.g., the type of the target recommender system (matrix-factorization-based), all rating data, and the parameters of the recommender system (e.g., the dimension d and the tradeoff parameter λ in use).

Table 1 summarizes the results of different attacks. “None” means the hit ratios without any attacks. First, we observe that the variants of our \mathcal{S} -attack can effectively promote the target items using only a small number of fake users. For instance, in the Yelp dataset, when injecting only 0.5% of fake users, \mathcal{S} -TNA-Inf attack improves the hit ratio by 150 times for a random target item compared to that of the non-attack setting. Second, the variants of our \mathcal{S} -attack outperform the baseline attacks in most cases. This is because the baseline attacks aim to manipulate all the missing entries of the rating matrix, while our attack aims to manipulate the top- N recommendation lists. Third, it is somewhat surprising to see that the \mathcal{S} -TNA-Inf attack outperforms the \mathcal{U} -TNA attack. Our observation shows that by dropping the users that are not influential to the recommendation of the target items when optimizing the rating scores for the fake users, we can improve the effectiveness of our attack.

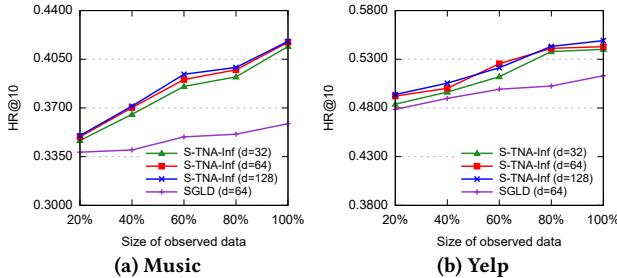


Figure 1: The attacker knows a subset of ratings for the normal users and does not know d .

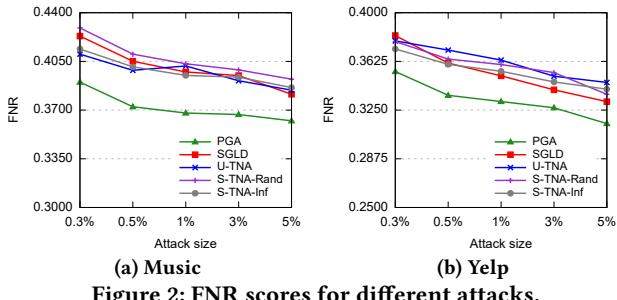


Figure 2: FNR scores for different attacks.

5.3 Partial-Knowledge Attack

In this section, we consider partial-knowledge attack. In particular, we consider the case where the attacker knows the type of the target recommender system (matrix-factorization-based), but the attacker has access to a subset of the ratings for the normal users and does not know the dimension d . In particular, we view the user-item rating matrix as a bipartite graph. Given a size of observed data, we construct the subset of ratings by selecting nodes (users and items) with increasing distance from the target item (e.g., one-hop distance to the target item, then two-hop distance and so on) on the bipartite graph until we reach the size of observed data.

Figure 1 shows the attack results when the attacker observes different amounts of normal users ratings and our attack uses different d , where the target recommender system uses $d = 64$. The attack size is set to be 3%. Note that in the partial-knowledge attack, the attacker selects the influential user set and generates fake users based only on the observed data. Naturally, we observe that as the attacker has access to more ratings of the normal users, the attack performance improves. We find that our attack also outperforms SGLD attack (which performs better than PGA attack) in the partial-knowledge setting. Moreover, our attack is still effective even if the attacker does not know d . In particular, the curves corresponding to different d are close to each other for our attack in Figure 1.

6 DETECTING FAKE USERS

To minimize the impact of potential attacks on recommender systems, a service provider may arm the recommender systems with certain fake-user detection capability. In this section, we investigate whether our attack is still effective in attacking the fake-user-aware recommender systems. Specifically, we extract six features—namely, RDMA [6], WDMA [23], WDA [23], TMF [23], FMTD [23], and MeanVar [23]—for each user from its ratings. Then, for each attack,

Table 2: HR@10 for different attacks when attacking the fake-user-aware recommender systems.

Dataset	Attack size	None	PGA	SGLD	\mathcal{U} -TNA	S -TNA-Rand	S -TNA-Inf
Music	0.3%	0.0011	0.0028	0.0064	0.0127	0.0068	0.0199
	0.5%	0.0011	0.0043	0.0145	0.0298	0.0139	0.0342
	1%	0.0011	0.0311	0.0916	0.1282	0.0934	0.1215
	3%	0.0011	0.2282	0.2631	0.2846	0.2679	0.2994
	5%	0.0011	0.3243	0.3516	0.3652	0.3531	0.3704
Yelp	0.3%	0.0010	0.0018	0.0097	0.0231	0.0093	0.0242
	0.5%	0.0010	0.0062	0.0278	0.0431	0.0265	0.0474
	1%	0.0010	0.1143	0.1585	0.1774	0.1612	0.1831
	3%	0.0010	0.3301	0.3674	0.3951	0.3665	0.3968
	5%	0.0010	0.4081	0.4223	0.4486	0.4269	0.4501

we construct a training dataset consisting of 800 fake users generated by the attack and 800 randomly sampled normal users. We use the training dataset to learn a SVM classifier. Note that the classifier may be different for different attacks.

Fake-user detection results: We deploy the trained SVM classifiers to detect the fake users under different attacks settings. Figure 2 reports the fake users detection results of different attacks, where False Negative Rate (FNR) represents the fraction of fake users that are predicted to be normal. From Figure 2, we find that PGA attack is most likely to be detected. The reason is that the fake users generated by PGA attack do not rate the filler items according to normal users’ behavior, thus the generated fake users are easily detected. We also observe that a large fraction of fake users are not detected.

Attacking fake-user-aware recommender systems: We now test the performance of attacks on fake-user-aware recommender systems. Suppose that the service provider removes the predicted fake users from the system detected by the trained SVM classifiers. We recompute the hit ratio after the service provider excludes the predicted fake users from the systems. Note that a large portion of fake users and a small number of normal users will be deleted. The results are shown in Table 2. We observe that PGA attack achieves the worst attack performance when the service provider removes the predicted fake users from the systems. The reason is that the PGA attack is most likely to be detected. Comparing Table 1 and Table 2, we can see that when the target recommender system is equipped with fake-user detectors, our attacks remain effective in promoting the target items and outperform the baseline attacks. This is because the detectors miss a large portion of the fake users.

7 CONCLUSION

In this paper, we proposed the first data poisoning attack to matrix-factorization-based top- N recommender systems. Our key idea is that, instead of optimizing the ratings of a fake user using all normal users, we use a subset of influential users. Moreover, we proposed an efficient influence function based method to determine the influential user set for a specific target item. We also performed extensive experimental studies to demonstrate the efficacy of our proposed attacks. Our results showed that our proposed attacks outperform existing ones.

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