



Three-dimensional tomography reveals distinct morphological and optical properties of soot aggregates from coal-fired residential stoves in China

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ABSTRACT

Electron tomography (ET) is used to reconstruct the exact 3-dimensional morphologies of fractal-like soot aggregates sampled from a household heating stove commonly used in China. Conventional ET techniques suffer from “the missing wedge” problem caused by unreachable tilt angles, leading to noisy reconstructed tomograms. We overcame this problem by implementing a high-resolution object-edge identification method coupled with a novel voxel-filling algorithm to improve the reconstruction quality. Our reconstructed micron-length aggregates highlight the local non-idealities present throughout a particle's surface; these characteristics are almost impossible to account for in existing computational simulation exercises. Q-space analysis predicts the fractal dimension of our ET reconstructed aggregates to be in the range between 2.2 and 2.6, which deviates significantly from the universal value of 1.8 obtained using the widely adopted diffusion limited cluster-cluster aggregation (DLCA) model. The optical properties of our ET reconstructed aggregates are compared with those built with a DLCA model and equivalent spheres. The most striking optical characteristics of the ET reconstructed aggregates are their wavelength invariant mass absorption cross-sections of $\sim 3.5 \text{ m}^2/\text{g}$ and single scattering albedo of ~ 0.5 . The sample size investigated in this work is constrained by the extremely time-consuming object-edge identification process of electron tomography. This issue necessitates the development of more efficient computer vision algorithms for future research.

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1. Introduction

Residential coal combustion is a primary source of heating and cooking in rural areas of developing countries such as China and India [1–3]. Incomplete coal combustion in household stoves produces soot, which accounts for a large fraction of the regional carbonaceous aerosol emissions [4,5]. Soot particles strongly scatter and absorb solar radiation and are consequentially recognized as an important climate forcer [6,7]. The optical properties of soot, which are crucial to radiative forcing estimations, depend highly on the complex fractal-like morphology of soot aggregates [8,9].

Thus, an accurate parameterization of soot morphology is a prerequisite to constraining the uncertainties in the estimates of Earth's energy balance and thereby advancing the currently adopted climate model.

The morphology of soot aggregates is most commonly characterized with *ex situ* electron microscopy (EM) and subsequent digital image analysis [10,11]. This technique requires experimentalists to extract the unknown three-dimensional (3-d) geometric characteristics of soot aggregates from their two-dimensional (2-d) projected images, according to certain shape approximation assumptions or experimentally-determined correction factors [10,12,13]. Since soot aggregates possess anisotropic shapes [14,15], an inference of their 3-d morphology (from 2-d projected images) is inevitably subject to the random orientations by which aggregates reside on the EM grids. Previous studies [16,17] show that the

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key morphological parameters of a soot particle (such as monomer number, projected area, and fractal dimension D_f) inferred from EM images taken from multiple angles deviate significantly with each other [18,19].

Alternatively, the 3-d morphology of aggregates can be studied with computer simulations based on Monte Carlo method, for example, the diffusion limited cluster-cluster aggregation (DLCA) model, which mimics the dynamic process of soot aggregates growth in stochastic Brownian systems [15,20,21]. Such a model generates 3-d “virtual aggregates” taking fractal shape, which are regarded as an approximation to the geometry of real-world soot. Subsequent analyses can be performed on the virtual aggregates to acquire their 3-d morphological parameters [22]. The use of computer simulation circumvents the projection artefacts in traditional EM analysis, but the idealized aggregate geometry, which is commonly assumed in simulation models, fails to capture the diversity in the minor structures of real-world soot [23]. For example, a DLCA model commonly treats soot monomers as equally sized and point-contacting spheres [20,21,24,25]. Only a few studies to our knowledge have considered the sintering induced intermonomer necking [26,27], the lognormal distribution of monomer radii [28], and the possible deviation of monomers from perfect spheres [23,29]. Furthermore, it is commonly assumed in simulations that the relative position of monomers in an aggregate remains unchanged once the monomers are joined together [21,24,25]. This is again not always true in real world scenarios. Recent experiments [18] provide evidence suggesting that the restructuring of soot aggregates (i.e. rotation per monomer contacting points) could occur simultaneously during their growth. Such a non-ideal overall structure of soot aggregates may also affect their optical properties in an unanticipated manner, which remains unaddressed in contemporary models.

The limitations of traditional EM techniques and computer simulations can be overcome with the advent of electron tomography (ET), by which experimentalists could characterize the 3-d morphology accurately. As a development of the transmission electron microscopy (TEM) method, ET is a powerful technique that captures 3-d nanoscale structures through multiple viewing-angle projections [18,30,31]. Doing so, the non-ideal structures of soot aggregates can be faithfully preserved in 3-d reconstruction from projection artefacts. In this study, we apply ET to reconstruct the complete 3-d geometry of soot aggregates sampled from residential heating stove, and subsequently we compute their optical properties based on the reconstructed geometries. This paper is organized as follows: First we briefly recap the theoretical foundation of the q-space analysis [32] and discrete dipole approximation (DDA) [32–34], which are respectively adopted here to compute the aggregates’ morphological and optical parameters. Next, we describe the experimental methods involved in soot sampling and ET reconstruction. This is followed by section detailing a novel object-edge identification method (along with a voxel filling algorithm), which is designed to overcome the “the missing wedge [35,36]” problem inherent to ET, thereby improving the accuracy of final 3-d reconstruction. Next, we present the reconstructed 3-d geometry of soot aggregates, along with their morphological and optical parameters, which are respectively determined with q-space analysis and DDA. This paper concludes with a side-by-side comparison between the ET reconstructed soot and idealized DLCA aggregates, regarding their morphology and optical properties.

2. Theory

2.1. Q-space analysis of aggregate morphology

Q-space analysis has been widely adopted to study the morphology of aggregates [32,37]. This technique, which originates

from light scattering experiments, involves plotting the structure factor (S , normalized scattering intensity) of the aggregate versus the magnitude of scattering wave vector q in a log-log space. The magnitude of $S(q)$ scales with q by a power-law exponent taking values of $-2D_m + D_s$ (where D_m and D_s respectively denote mass and surface dimension of the object). For fractal aggregates, $D_f = D_m = D_s$, the power-law scaling relationship is reduced to $S(q) \propto q^{-D_f}$. Thus, the size delimited fractal morphology along with the corresponding D_f values can be readily determined with $S(q)$ trends in the log-log space. In theoretical studies, one could calculate $S(q)$ according to the discrete form of the orientational averaged scattering intensity:

$$S(q) = \left| \frac{1}{N} \sum_{j=1}^N \exp[i(\vec{r}_j \cdot \vec{q})] \right|^2, \quad (1)$$

with $q = \frac{4\pi}{\lambda} \sin\left(\frac{\theta}{2}\right)$

Here, N represents the number of point scatterers constituting the aggregates, $\vec{r}_j$ is the location of scatterer j relative to the origin, λ is the wavelength of the incident light, and θ is the scattering angle.

2.2. Discrete dipole approximation

The exact solution to electromagnetism equations are available only for objects with a symmetric geometry. For asymmetric objects, numerical approximation models are widely used to simulate the related optical properties. DDA is one of such model. DDA assumes the particle of interest is assembled by numerous dipoles. Each dipole, j , located at r_j from the coordinate origin, is illuminated by both the electric field, E_{incj} , due to the incident wave, and the radiation scattered by all the other oscillating dipoles, $E_{rad, k \neq j}$. The moment of dipole j , P_j , can be expressed as the product of the dipole polarizability, α_j , and the total external radiations:

$$P_j = \alpha_j (E_{inc,j} - E_{rad,k \neq j}) \quad (j = 1, 2, \dots, N). \quad (2)$$

The monochromatic incident plane wave, E_0 , polarized in two mutually orthogonal directions, propagates along vector k . The induced electric field, $E_{inc,j}$, can be written in a complex expression:

$$E_{inc,k} = E_0 \exp(ik \cdot r_k - i\omega t). \quad (3)$$

Meanwhile, for any dipole j , $E_{rad,j}$ is a linear combination of all the other dipole moments $P_{l \neq j}$. Therefore Eq. (2) can be compactly formulated as a set of N inhomogeneous linear complex vector equations of the form P_j ($j = 1, 2, \dots, N$) [33,38].

3. Methods

3.1. Soot sampling

Particle samples were collected from a widely used traditional heating stove (NS18-17, 18 kW, Beijing Laowan Bioenergy Technology Co., Ltd, China) in a rural Chinese household (see Fig. 1 for the schematic of sampling experiment). The stove with a dimension of $460 \times 410 \times 985$ mm was placed at the center of a sealed room (about 10 m^3) maintained at a slightly positive pressure with filtered air. The flue gas from the stove was drawn out at a fixed flow rate of $0.56 \text{ m}^3/\text{s}$ through a circular hood connected to a dilution tunnel. Locally available bituminous coal chunks were crushed into pieces of approximately 3 inches in diameter before being fed into the upper region of the stove combustion chamber, where they are ignited with a mixture of air and propane gas applied at a fixed

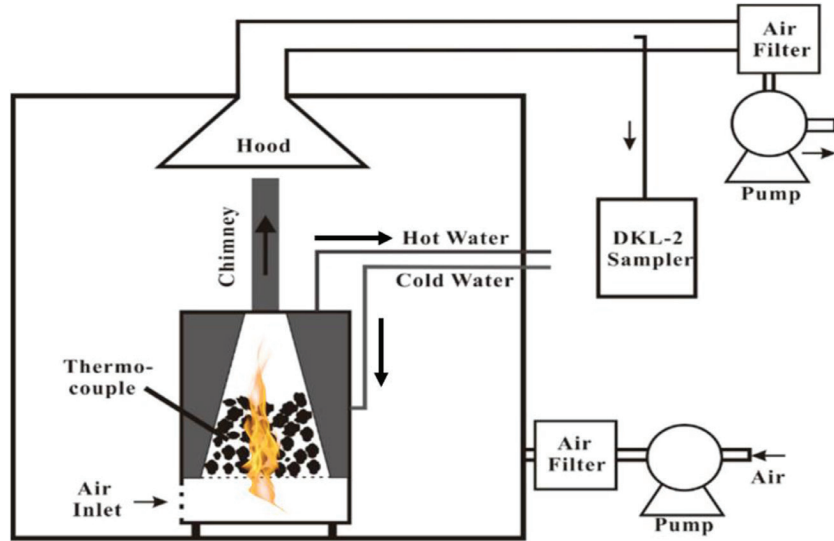


Fig. 1. Schematic diagram of the experimental setup for soot particle sampling from a coal-combustion stove.

flow rate of 3 lpm. The stove design and its operation during the experiment are detailed in a previous publication [39].

Soot aggregates emitted from the stove were collected 4 meters downstream of the exhaust on carbon-coated copper TEM grids (300-mesh, Beijing XXBR Technology Co., Ltd, China) mounted on a DKL-2 type single-stage cascade impactor (0.5-mm-diameter jet nozzle). The flow rate of the impactor was set to 1 lpm. A sampling time of 20 seconds (determined in a trial-and-error manner) was used to ensure sufficient but not overcrowded loading of particles onto the grids [40]. We started TEM sampling about 30 min after ignition, at which a steady flaming condition was reached. Such a condition ensured that the sampled particles were produced from the combustion of coal, but not the propane pilot flame.

3.2. Electron tomography

We used a FEI Tecnai F20 TEM D545 microscope to acquire 2-d tilt-series of TEM images for four soot particles (hereafter sample A, B, C, and D). The ranges of title angles used for sample A, B, C, and D are respectively $[-60^\circ, +60^\circ]$, $[-60^\circ, +70^\circ]$, $[-60^\circ, +60^\circ]$, and $[-65^\circ, +60^\circ]$. The title angle was incremented by one degree during the imaging. ET reconstruction was implemented through the weighted back projection algorithm in IMOD 4.9 coupled with the RAPTOR alignment module [41,42]. The reconstructed results are stacks of what we call “tomograms”. Since 3-d ET reconstruction suffers from “the missing wedge” caused by unreachable tilt angles, the tomograms of the soot aggregate are normally noisy. In this study, we identified the boundary of soot particle from the reconstructed slices at the pixel locations where sharp contrast (between particle and background) is observed. These boundaries were determined in each slice, and when stacked together, constitute the closed surface of soot aggregate.

3.3. Voxel filling

Tomograms are made up of volumetric pixels (hereafter voxels) that represent the elementary geometric unit of a 3-d objects. An accurate voxel filling process (voxelization) is therefore fundamental to every subsequent analysis. In this work, we developed a layer-by-layer voxelization method to fill the space encapsulated by the aggregate surface.

Given the irregular fractal-like shape of soot aggregates, the most straightforward and effective voxelization procedure is to allocate voxels along successive horizontal lines in each tomogram

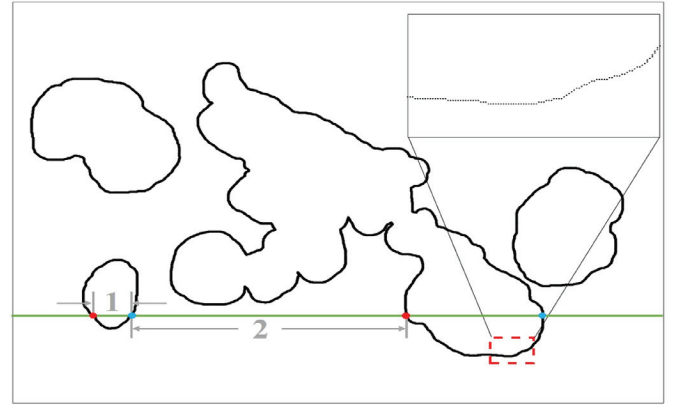


Fig. 2. An example of voxel filling in one tomogram slice. The inset shows the zoomed in view corresponding to the red-dashed square area. It highlights the continuous black points constituting the object boundaries. The green line is one of the horizontal voxel filling lines (the filling direction in each horizontal line is from left to right). It has four intersection points (IPs). Voxel filling starts from the red points (voxel-filling starting points) and ends at the closest blue points (voxel-filling ending points). If the blue point on the left is the current IP, the number of pixels of “gap 1” is defined as the intra-prior distance (IPrD), and the number of pixels of “gap 2” is defined as the intra-posterior distance (IPoD).

slice. But this poses another challenge: the intersection points (hereafter IPs) between closed surface contours and the horizontal lines must be correctly identified as either starting or ending points for voxelization. Please refer to Fig. 2 for examples of IPs on a horizontal line in one tomogram slice.

We applied an intra-line and inter-line method to categorize IPs. We define the number of voxels between the current IP and the previous IP in each horizontal line as the intra-prior distance (IPrD), and the number of voxels between the next IP and the current IP as the intra-posterior distance (IPoD). For intra-line analysis, different value combinations of IPrD and IPoD help us to confirm the basic type of a given IP. In this study, basic types include boundary starting points (IPrD > 1 meanwhile IPoD = 1), boundary ending points (IPrD = 1 meanwhile IPoD > 1), singular boundary points (IPrD > 1 meanwhile IPoD > 1), and normal boundary points (IPrD = IPoD = 1). The first three types of boundary points are all possible starting or ending IPs for voxel filling.

Note that an intra-line analysis does not provide us a sufficient condition to determine whether the gap between two successive

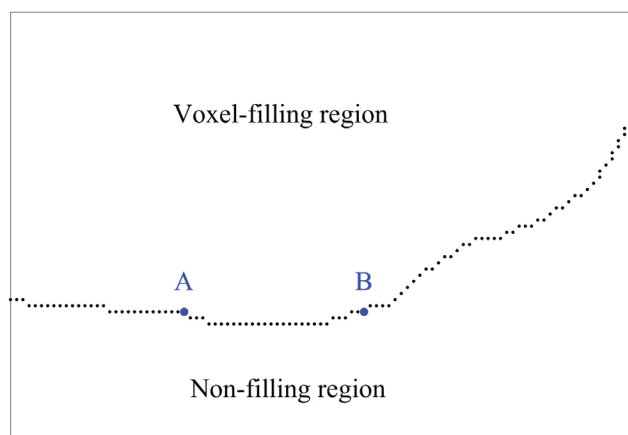


Fig. 3. The same figure as the inset of Figure 2. Here we highlight an example of an ambiguous case after intra-line categorization. The area above the black dots is the object region, which should be filled with voxels. The area below the black dots is the background region, which should be left blank. Both point A and point B are categorized as boundary ending points by intra-line analysis as introduced above. But point A is a voxel-filling starting point at the same time, while point B acts only as a voxel-filling ending point.

IPs should be voxelized. Curvatures of aggregate boundaries cause ambiguities to IPs categorizations. For example, a boundary ending point (Point A in Fig. 3) also represents a starting point for the subsequent voxel filling process. However, this is not the case for another boundary ending point (B in Fig. 3). Intra-line categorization thus cannot inform us whether we should start the voxel filling procedure at these points.

Here inter-line analysis aids in for finer categorization. We incorporate prior knowledge to distinguish, for example, whether a boundary ending point is a filling starting point or not. The principle we follow is that natural objects, e.g., soot aggregates in this study, should have continuous surfaces. In the voxel filling process, this principle can be interpreted as that successive horizontal lines (in either the bottom up or top down direction) should contain similar numbers of voxels after voxelization. Besides, a pair of starting and ending points for voxelization should locate in the region adjacent to their counterparts in the previous horizontal line. Given that the first horizontal filling line of each slice is always tangential to the object boundaries, intra-line analysis can categorize all the necessary filling starting and ending pairs accurately. Subsequently IP pairs in next horizontal lines can be accurately identified according to a combination of intra- and inter-line analysis.

3.4. Q-space analysis

Q-space analysis was next performed on the 3-d reconstructions of aggregates. We calculated of $S(q)$ according to Eq. (1), wherein the $\bar{r}$ was determined with the 3-d coordinates of voxels. In this treatment, the voxels making up the reconstructed aggregates are regarded as the point scatterers in q-space analysis [43,44].

3.5. Computation of optical properties

The optical properties of the ET reconstructed and DLCA aggregates are calculated with DDA. We compiled and ran DDSCAT 7.3.2 on a research computing cluster at Washington University in St. Louis equipped with a gfortran compiler. Isotropic polarizability was assigned to all voxels of the reconstructed aggregates. Related optical properties were simulated through appropriate numbers of dipole representations of each aggregate model. A convergence test

of the DDA simulation is detailed in supplementary information (Figure S2).

4. Results and discussion

4.1. Reconstruction of aggregate geometry in 3-d

Fig. 4 shows snapshots of the ET reconstructed aggregates. One could observe that the detailed non-ideal morphologies of soot monomers, such as the intermonomer necking and the deviation of monomers from spherical shape, are faithfully preserved in the 3-d reconstruction. Furthermore, the non-ideal overall structure of the aggregate backbone can be observed in the reconstruction of aggregate C, for example, the internal ring structure due to the possible restructuring of the aggregate during its growth [45]. We also notice that, except for aggregate D wherein two extremely large monomers are observed, the other three aggregates are comprised of monomers of similar size. This monodisperse distribution of monomer radii implies that the nascent soot particles experience similar combustion and transport conditions. For aggregate D, the two extremely large monomers have similar pixel values as the other smaller monomers in the projection images. It is reasonable to recognize them as consisting of identical black carbon components with those smaller counterparts.

4.2. Q-space analysis

Here, we compare the morphological parameters of ET reconstructed aggregates to that of idealized DLCA aggregates. The number of constituent monomers in the DLCA aggregates ranges between 50 and 150, ensuring that the DLCA are of the comparable size relative to the ET reconstructed ones. Fig. 5 shows the q-space analysis of all four ET reconstructed aggregates and a typical DLCA aggregate. Here we plot the normalized structure factor $S(q)$ versus the product of q and aggregate radius of gyration R_g , representing a dimensionless form of the probing length. Fig. 5 shows that size-delimited power-law regimes exist in the $S(q)$ trend. First, a fractal regime, with a slope ($-D_f$) taking value between -2.2 and -2.6 , can be observed within the length scale $1 < qR_g < 10$. As qR_g further increases, a kink point is reached, beyond which $S(q)$ takes up a steeper trend with a slope ($-2D_m + D_s$) of -4 . This second power-law regime ($qR_g > 10$) is also known as Porod regime, wherein the probing length is below average monomer radius and consequentially the aggregates are seen as 3-d Euclidian objects (i.e. $D_m = 3$ and $D_s = 2$) [44].

One could observe that the reconstructed soot aggregates have $2.2 < D_f < 2.6$, which are noticeably larger than the $D_f \approx 1.8$ of the DLCA aggregates. Qualitatively speaking, this is in good agreement with the visual appearances of our ET reconstructed aggregates, which manifest more compact morphology than that of the idealized DLCA aggregates. Specifically, significant degrees of inter-monomer necking can be observed in the ET reconstructions, which obfuscate the point-contacting arrangement of monomers typically assumed in DLCA. Furthermore, the possible restructuring of aggregate backbone (as indicated by the internal ring structure in aggregate C), could also lead to a more compact packing arrangement for monomers.

4.3. Optical properties

Since spherical particles are widely used in regional climate models, in this section, we calculate the optical properties of spherical particles using Mie theory with reference to the two aggregate models mentioned in previous sections. The material of soot aggregates considered in this study is isotropic black carbon, so the polarizability tensor α_j degrades to a scalar quantity [46].

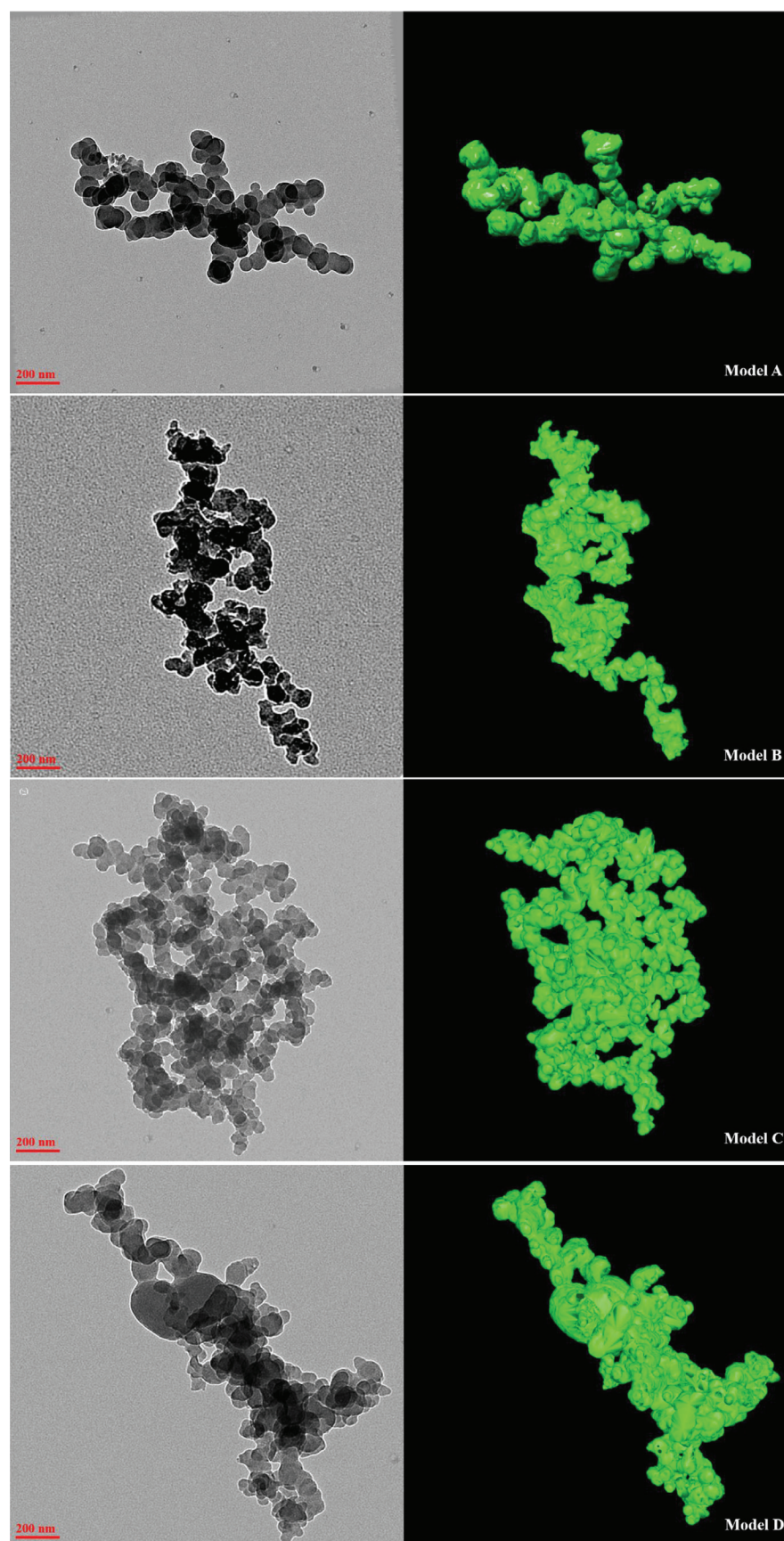


Fig. 4. Electron Tomography reconstruction of aggregates A, B, C, and D. The left panels show the transmission EM images of the soot aggregates. The right panels show the 3-d reconstructed geometries of the corresponding aggregates.

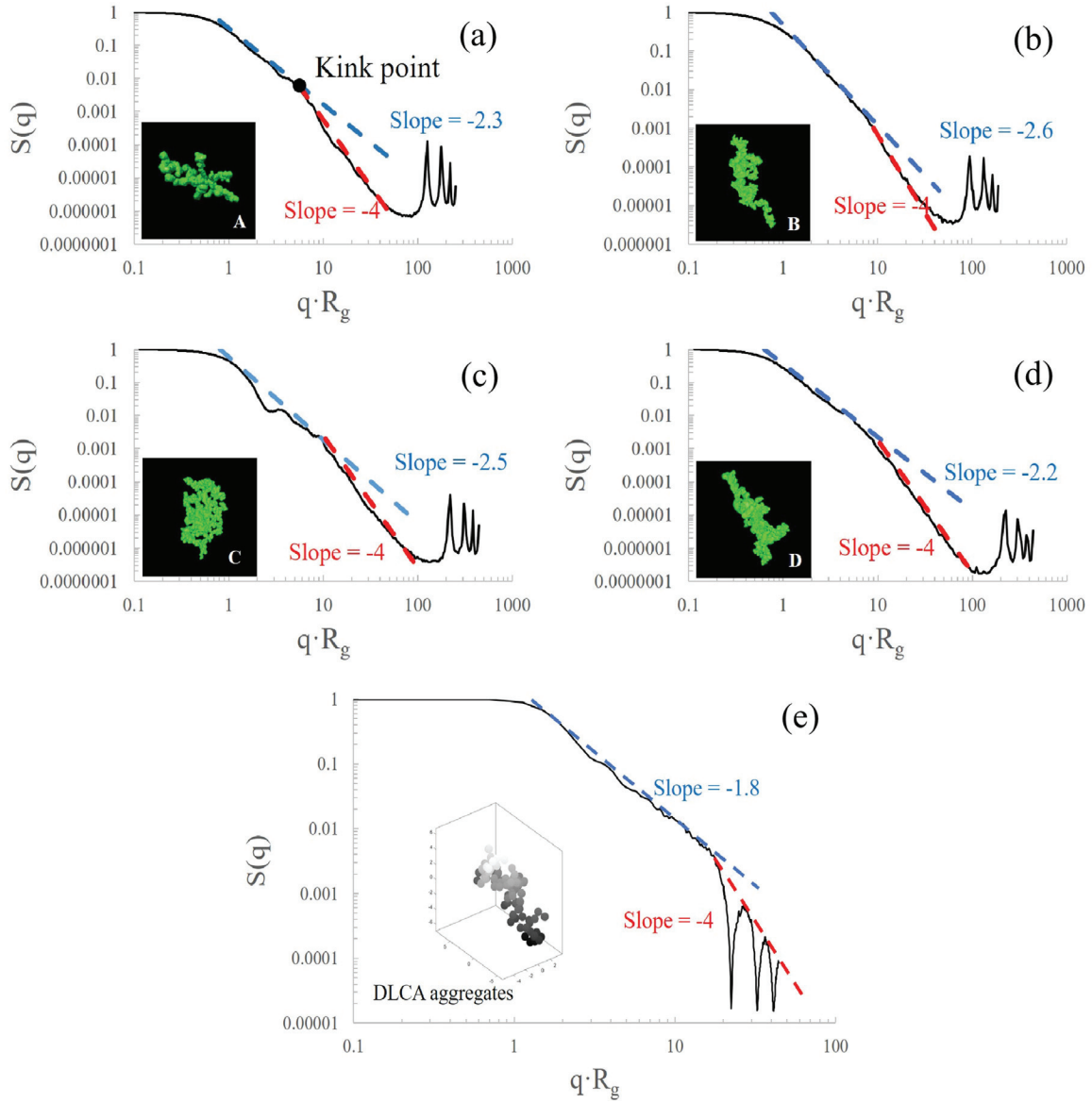


Fig. 5. Panels (a) - (d) Q-space analysis of four ET aggregates, Panel (e) Q-space analysis of a typical DLCA aggregate

First, we choose a moderate refractive index, $1.95-0.79i$ [47], as the typical refractive index of black carbon to study the effects of different particle morphologies to their optical properties. At the end of this section, we will provide a sensitivity analysis of aggregates' optical properties to different refractive indices.

Fig. 6 (a) and (b) respectively show the single scattering albedo (SSA) and asymmetric factor of ET reconstructed aggregates as functions of incident light wavelength. Also plotted here are the SSA and asymmetric factor determined from DLCA model and the volumetrically equivalent spheres. In Fig. 6 (a), the black cross symbols represent the mean value of SSA calculated using the four ET reconstructed aggregates. (Detailed optical properties of ET reconstructed aggregates are shown in Table S1). Blue circle symbols represent the statistical SSA of DLCA aggregates with different number of primary particles, which have volumetrically equivalent radii between $0.27 \mu\text{m}$ to $0.40 \mu\text{m}$. The red circle symbols represent the SSA calculated for volumetrically equivalent spheres with Mie theory. The styles of symbol in Fig. 6 (b) follows that in (a).

The values of SSA and the asymmetry parameter are observed to decrease with an increase in the incident wavelength. This ob-

servation holds true for both the ET reconstructed aggregates and the idealized models (i.e. DLCA and spherical particles). Specifically, the use of DLCA model results in a systematic underestimation of SSA; whereas overestimated SSA values are observed in the case of equivalent spherical model. This observation implies that when the aggregate morphology becomes less compact, the contribution of scattering to total extinction tends to decrease. Meanwhile, both DLCA and the equivalent spherical particle model systematically underestimate the values of asymmetry parameter. This observation indicates that the underestimated asymmetry parameter cannot be deterministically related with the compactness of aggregate morphology. Future studies should focus on elucidating the sensitivity of asymmetry parameters on other non-ideal minor structures of aggregates.

Fig. 7 shows the mass absorption cross section (MAC), along with the absorption angstrom exponent (AAE) values, calculated from the ET reconstructed aggregates, DLCA aggregates, and equivalent spherical model. MAC in this study is defined as:

$$MAC = \frac{Q_{abs} \cdot \pi r_{equ}^2}{\frac{4}{3} \rho \pi r_{equ}^3}, \quad (4)$$

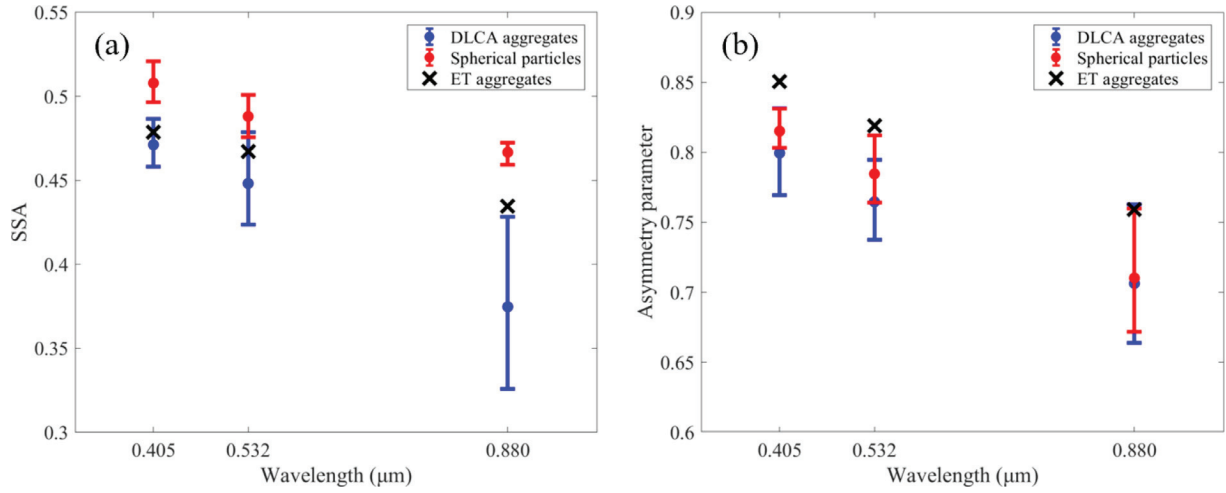


Fig. 6. Single scattering albedos (a) and asymmetry parameter (b) of ET reconstructed aggregates, DLCA aggregates, and volumetrically equivalent sphere with radii ranging from 0.27 μm to 0.40 μm .

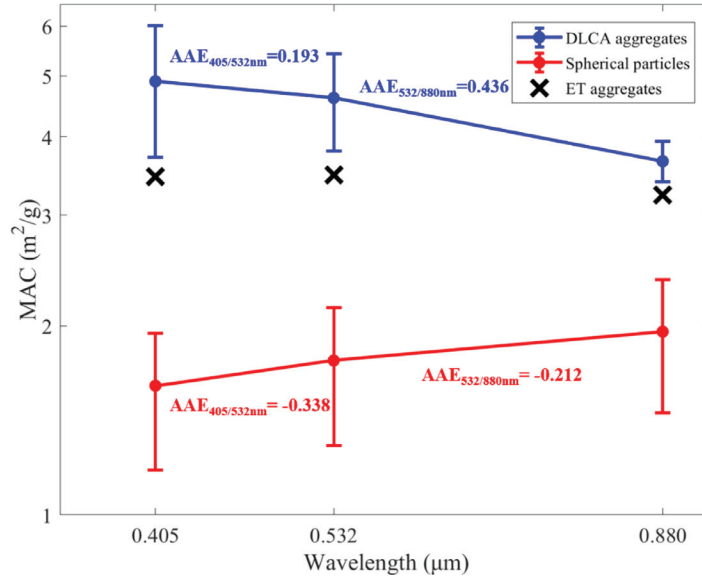


Fig. 7. Wavelength dependence of Mass Absorption Cross-sections (MAC) for ET soot aggregates, and comparison with equivalent DLCA soot aggregates and volumetrically equivalent soot spheres. As is apparent, MAC values of ET aggregates are spectrally invariant.

Here, Q_{abs} is the orientational averaged absorption efficiency of an aggregate, r_{equ} is the volumetrically equivalent radius of the aggregate, and ρ is its density. The average MAC of ET aggregates is 35.6%, 27.8%, and 9.7% lower than the DLCA counterparts with comparable size and monomer numbers, and is 54.2%, 50.1%, and 40.6% higher than their volumetrically equivalent spheres at 405 nm, 532 nm, and 880 nm, respectively. We estimate the average MAC of ET aggregates, based on an assumption of black carbon's density of 1.8 g/cm³, to be $\sim 3.43 \text{ m}^2/\text{g}$ at 532 nm. Our observation of three different particle models implies that aggregates with less compact morphologies are greater light absorbers, even without any coating. No significant wavelength dependency is observed for the MAC of the ET reconstructed aggregates; whereas a slightly positive AAE is observed for comparable DLCA aggregates, and a negative value is observed for that of the equivalent spherical models. According to Rayleigh-Debye-Gans (RDG) theory, particles with diameters smaller than the wavelength and with a moderate refractive index have an absorption efficiency written as:

$$Q_{abs} = -\frac{4x}{3} \text{Im}(m^2 - 1), \quad (5)$$

Here, x is the size parameter (product of particle radius and the wavenumber of incident light), and m is the complex refractive index. Since m is assumed to be wavelength independent, $AAE = -\ln(MAC_{\lambda_1}/MAC_{\lambda_2})/\ln(\lambda_1/\lambda_2)$ by its definition is close to a constant value of unity [48,49]. Figure S3 plots AAE values as functions of volumetrically equivalent radii for spherical particles derived from Mie theory. As particle radii increase, AAE values of both wavelength pairs rise above constant one and dramatically decrease below zero. In our study, the volumetrically equivalent radii of all aggregate models are larger than 0.27 μm . If we define the spherical particles sharing comparable AAE values to the aggregated particles as “AAE-equivalent spheres”, the size of AAE equivalent spheres (shaded in grey in Figure S3) of the ET reconstructed aggregate is smaller than that of the volumetrically equivalent spheres (shaded in red in Figure S3).

Previous studies quantified the influence of fractal morphologies on absorption using the concept of phase-shift parameter [44,50]. The “optical effective radius” significantly decreases after it is corrected to account for the small packing fraction of fractal aggregates. Our results (in Fig. 7 and Figure S3) validate the fractal

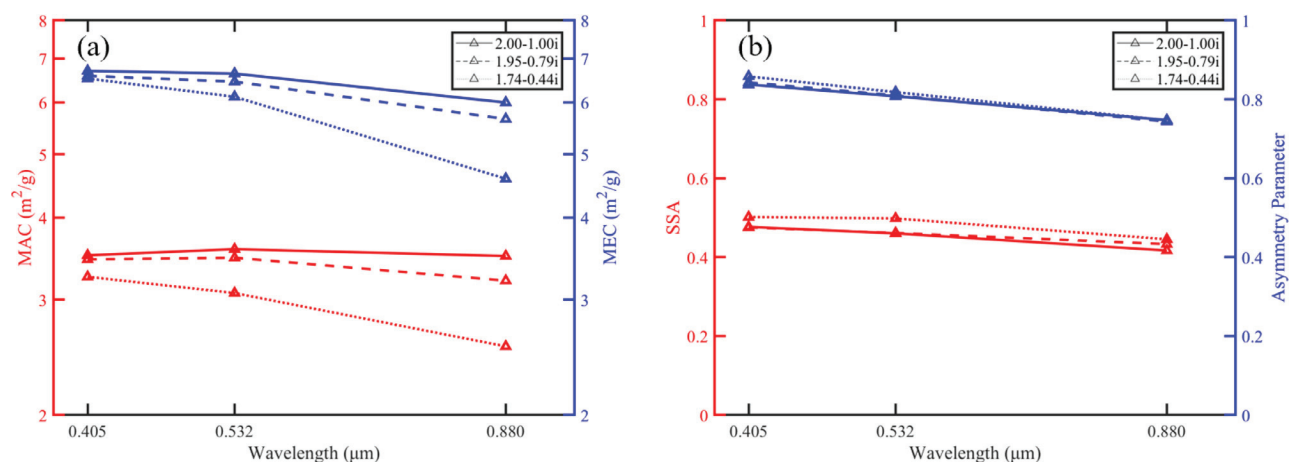


Fig. 8. Variation in mass absorption (MAC) and extinction cross sections (MEC), single scattering albedo (SSA) and asymmetry parameter of ET aggregates as a function of varying refractive indices. The plots show the sensitivity of optical properties to varying values of complex refractive index.

morphologies lead to a deviation between geometric and optical equivalent size.

In Fig. 8, we evaluate how different refractive indices affect ET aggregate optical properties. Besides $m = 1.95 - 0.79i$, two published values, $2.00 - 1.00i$ [51] and $1.74 - 0.44i$ [52] are applied to show the sensitivities of previously mentioned optical properties. MEC in Fig. 8 (a) represents the mass extinction cross section. It is similarly defined as MAC in Eq. (4) but substitutes extinction efficiency Q_{ext} for Q_{abs} . We found higher m values amplify particle extinction and absorption cross-sections. Meanwhile, the characteristic of wavelength independent AAE has been preserved under two high m value assumptions. For $m = 1.74 - 0.44i$, a weak inverse wavelength dependence of MAC is observed. Fig. 8 (b) shows that SSA and asymmetry parameters are less sensitive to variations in refractive indices.

5. Conclusion

We apply electron tomography coupled with a slice-by-slice voxel filling algorithm to reconstruct the 3-d morphology of soot aggregates sampled from a coal combustion system. The non-ideal structure of soot aggregates (i.e. non-spherical monomers, necking structures between monomers, and the internal rings structures), which are rarely considered in computer simulation, have been accurately preserved in the ET reconstruction. The morphology and optical properties of the soot aggregates are respectively studied with DDA and q-space analysis, which are directly applied to the ET reconstruction. Structure factor obtained from q-space analysis proves to be effective in quantitating the size delimited aggregate morphology. The D_f of the ET reconstructed aggregates takes values in the range between 2.2 and 2.6, indicating more compact morphologies than that of the idealized DLCA aggregates. The optical properties of ET reconstructed aggregates are compared with that of the idealized DLCA aggregates and volumetrically equivalent spheres. Our results show that the fractal-like morphology leads to enhancements in both the magnitude of MAC and the fraction of absorption in total extinction. The MAC of spherical particles is observed to have a weak dependency on incident wavelength, parameterized with a negative AAE value, when their size parameters slightly exceed unity; Whereas the MAC of ET aggregates remains constant with changing incident wavelengths, this wavelength independence holds for high refractive index values. Moreover, no deterministic relationship has been observed between the asymmetric parameter and the compactness of the aggregate morphology. Future works should be directed towards understanding the influence of the non-ideal structure of real-world

aggregates on their asymmetric parameter. We should emphasize that our findings here are based on single particle analysis, which therefore could deviate from the ensemble qualities of soot particles suspended in atmosphere.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:[10.1016/j.jqsrt.2020.107184](https://doi.org/10.1016/j.jqsrt.2020.107184).

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