

# Stability of H<sub>3</sub>O at extreme conditions and implications for the magnetic fields of Uranus and Neptune

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The anomalous nondipolar and nonaxisymmetric magnetic fields of Uranus and Neptune have long challenged conventional views of planetary dynamos. A thin-shell dynamo conjecture captures the observed phenomena but leaves unexplained the fundamental material basis and underlying mechanism. Here we report extensive quantum-mechanical calculations of polymorphism in the hydrogen-oxygen system at the pressures and temperatures of the deep interiors of these ice giant planets (to >600 GPa and 7,000 K). The results reveal the surprising stability of solid and fluid trihydrogen oxide (H<sub>3</sub>O) at these extreme conditions. Fluid H<sub>3</sub>O is metallic and calculated to be stable near the cores of Uranus and Neptune. As a convecting fluid, the material could give rise to the magnetic field consistent with the thin-shell dynamo model proposed for these planets. H<sub>3</sub>O could also be a major component in both solid and superionic forms in other (e.g., nonconvecting) layers. The results thus provide a materials basis for understanding the enigmatic magnetic-field anomalies and other aspects of the interiors of Uranus and Neptune. These findings have direct implications for the internal structure, composition, and dynamos of related exoplanets.

planetary science | high-pressure physics | magnetic fields | water

Danetary magnetic fields arise from magnetohydrodynamic processes (1). Earth's geomagnetic field is generated in its outer core, which consists largely of molten iron, whereas the magnetic fields of Jupiter and Saturn are produced within thick layers consisting predominantly of metallic fluid hydrogen. The magnetic fields of most planets in the Solar System are axial-dipole dominated; the exceptions are Uranus and Neptune, which exhibit anomalous nondipolar and nonaxisymmetric fields (2, 3). Interior models of these planets developed over the years generally identify three constituent regions, namely a gaseous hydrogen-helium outer envelope, a thick intermediate layer of "hot ices," and a core consisting of heavier elements (4). The pressure-temperature (P-T) conditions of the outer region are insufficient to produce fluid metallic hydrogen, and the proposed cores are thought to be solid or nonconvecting, which would preclude the existence of a dynamo in either region needed to produce the observed magnetic fields. The middle so-called "ice layer" has therefore been proposed as the region most likely to be responsible for the anomalous magnetic fields, specifically in a "thin" shell above the core (5, 6). Dynamo models have been proposed that are able to reproduce the anomalous nondipolar and nonaxisymmetric fields of Uranus and Neptune (7, 8), but a number of questions remain (9–11).

A fundamental question concerns their origin and physical mechanism of these intriguing planetary magnetic fields in terms of the component materials, an issue which in turn requires constraints on composition. The dearth of information about materials behavior at the relevant conditions has been cited as problematic for the thin-shell dynamo model in particular (11). A compositional reference model developed for these planets constrains the ice layer composition to have mole fractions of 56% H<sub>2</sub>O, 36% CH<sub>4</sub>, and 8% NH<sub>3</sub> (12), later refined as "synthetic Uranus" (13), with *P*-*T* conditions spanning 20–600 GPa and 2,000–7,000 K. CH<sub>4</sub> becomes unstable and dissociates into C and H<sub>2</sub> above 10 GPa and 2,000 K (14–18), and NH<sub>3</sub> is predicted to react with water to produce molecular mixtures in the form of (H<sub>2</sub>O)(NH<sub>3</sub>)<sub>2</sub> from 80 to 540 GPa (19). Assuming full dissociation of CH<sub>4</sub> and complete mixing of NH<sub>3</sub> with H<sub>2</sub>O, the ice layers are expected to have H<sub>2</sub>O:H<sub>2</sub> ratios reaching 13:18.

Given the large H<sub>2</sub>O component, there has been a great deal of focus on the role of phases of H<sub>2</sub>O in generating the magnetic fields within these planets. It has been suggested that H<sub>2</sub>O in the form of superionic ice constitutes a large fraction of the ice layer with ionic fluid water in the outer portions (20–23). This proposal has led to a number of subsequent computational studies of the behavior of H<sub>2</sub>O at high *P*-*T* conditions (24–27). The results found electrical conductivities of 2–20 ( $\Omega$  cm)<sup>-1</sup> in ionic H<sub>2</sub>O ice and near 100 ( $\Omega$  cm)<sup>-1</sup> in superionic ice (3, 9). Although these species may contribute to magnetic field generation, it is important

# Significance

Understanding the interior structure and dynamics of outer Solar System planets in terms of their component materials is a major scientific challenge. A highly intriguing case concerns the anomalous nondipolar and nonaxisymmetric magnetic fields of Uranus and Neptune. A thin-shell dynamo model has been shown to capture observed phenomena but leaves unexplained its origin and materials basis. We report extensive theoretical calculations that indicate the stability of trihydrogen oxide (H<sub>3</sub>O) in solid, superionic, and fluid metallic states at the deep interior conditions of these planets. The fluid metallic phase is stable in a thin-shell zone near their cores and exhibits the properties required to produce the observed enigmatic magnetic fields. These findings have implications for other planets, including related exoplanets.

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to consider the role of other high *P*-*T* phases in the H–O binary system.

There have been limited studies of the broader O-H binary system along the full range of P-T conditions of the deep interiors of Uranus and Neptune. High-pressure experiments on hydrogen and water have uncovered new phases, including the existence of H<sub>4</sub>O which consists of the expected molecular components (i.e., H<sub>2</sub> and H<sub>2</sub>O) in a novel clathrate structure (28). Additional work was done to constrain the full P-T-X phase diagram, but this was limited to below 30 GPa and 450 K (29). Computational studies have examined higher P-T conditions but have focused on the familiar H<sub>2</sub>O composition as mentioned above (24-27). The miscibility of H<sub>2</sub> and H<sub>2</sub>O at 2-70 GPa and 1,000-6,000 K has also been studied theoretically (30), but these do not correspond to the deepest regions within Uranus and Neptune. The extent to which hydrogen molecules dissociate and/or react (e.g., with H<sub>2</sub>O) to form new stable solid and fluid phases at the deep interior conditions of Uranus and Neptune thus remains an open question. This study was conducted to identify phases in the H-O system, including their structures and physical properties, in order to provide a materials basis for understanding the anomalous magnetic fields of these planets.

## Results

We began by examining H2-H2O mixtures to the deep interior pressures of Uranus and Neptune using an in-house quantum-mechanical material structure search CALYPSO method (31, 32). Our search uncovered the surprising stability of trihydrogen oxide  $(H_3O)$  at these compressions (Fig. 1A). The unit cell of the  $H_3O$ structure (space group Cmca) found here contains 64 atoms; its hydrogen-oxygen covalent framework has a H:O ratio of 2:1, with remaining hydrogen in the voids in the form of H<sub>2</sub> molecules. This clathratelike framework structure differs from those previously found experimentally or predicted theoretically at high pressures for  $H_2O$  (28, 34, 35). The basic structural unit hosts six distinct bond lengths and three different bond angles (Fig. 1C). Adjacent basic units are nested, four of which form the unit cell. The structure contains unusual H<sub>2</sub> dimers separated by 1.09 Å with a nearest-neighbor H-H distance of 0.65 Å at 500 GPa, which is significantly shorter than that of molecular hydrogen at ambient conditions (0.74 Å). Calculations of the enthalpy of formation



**Fig. 1.** Formation enthalpy and crystal structure of H<sub>3</sub>O. (*A*) Formation enthalpy of H–O compounds with respect to decomposition into H<sub>2</sub>O and H<sub>2</sub> at 400 and 600 GPa. (*B*) Enthalpy including the effect of zero-point energy versus pressure for H<sub>3</sub>O relative to the results for decomposed H<sub>2</sub>O and H<sub>2</sub>. (*C*) Crystal structure (space group *Cmca*) and basic structural units of H<sub>3</sub>O. Lattice parameters at 500 GPa are a = 3.35 Å, b = 5.84 Å, and c = 5.80 Å. There are two inequivalent atomic positions for O and four for H: O1 at 8f (0.00, 0.16, 0.00) and O2 at 8f (0.50, 0.49, 0.34), H1 at 8f (0.00, 0.33, 0.07), H2 at 8f (0.00, 0.43, 0.34), H3 at 16g (0.76, 0.09, 0.09), and H4 at 16g (0.33, 0.24, 0.23). Six distinct bonds in the basic unit labeled 1 through 6 have lengths 1.16, 1.02, 1.08, 1.06, 1.06, and 1.10 Å, respectively, and three bond angles  $\theta_1 = 174.6^\circ$ ,  $\theta_2 = 174.7^\circ$ , and  $\theta_3 = 171.3^\circ$ . Adjacent basic units are nested to form the unit cell of the H<sub>3</sub>O structure, which is controlled by the persistence both covalent bonding and repulsive interactions at these extreme conditions. The evolution of the O–H distances with pressure and temperature is shown in *SI Appendix*, Fig. S10. The *Pbcm* structure (38) at 600 GPa are used.



Fig. 2. Simulations of crystalline solid, superionic solid, and fluid phases of H<sub>3</sub>O. (A-C) MSD of oxygen and hydrogen in H<sub>3</sub>O at (A) 1,000 K, (B) 3,000 K, and (C) 6,000 K at a density of 4.30 g/cm<sup>3</sup>, in three phases. (D-F) Trajectory snapshots of the corresponding phases, where the purple and green spheres represent instantaneous positions of oxygen and hydrogen atoms, respectively.

show that Cmca-H<sub>3</sub>O is stable against decomposition to H<sub>2</sub>O and H<sub>2</sub> above 450 GPa (Fig. 1B). The stability of an H<sub>3</sub>O phase having this composition was previously reported (33, 36), but its structure is different and is stable at much higher pressure of 4.2 terapascals (TPa) (SI Appendix, Figs. S1–S3), which is far above the pressure range (0.4-0.6 TPa) considered in our study and not relevant to Uranus and Neptune. Our simulations are thus not in contradiction with the previous results obtained for the system at higher pressures (33, 36).

The onset of stability of H<sub>3</sub>O lies within the pressures of 20-600 GPa estimated for the ice layers of Uranus and Neptune. Because of the high temperatures that also prevail within these planetary interiors, we examined the P-T phase stability and behavior using ab initio molecular dynamics (AIMD) simulations. Fig. 2 shows simulated mean-square displacement (MSD) and trajectory of H<sub>3</sub>O at a density of 4.30 g/cm<sup>3</sup>. At 1,000 K, MSD values of the hydrogen and oxygen atoms remain nearly constant (Fig. 24), showing that the system is stable in the solid with all atoms near their equilibrium positions (Fig. 2D). At 3,000 K, the hydrogen atom MSD values begin to increase, whereas those of the oxygen atoms remain nearly constant (Fig. 2B), which signals a transition into a superionic state. This observation of a transition in the solid is corroborated by trajectory data, which also show that the oxygen atoms remain near their equilibrium positions while hydrogen atoms diffuse (Fig. 2E). On further increase in temperature (6,000 K), the oxygen atoms then diffuse, indicative of melting (Fig. 2 C and F). These calculations thus show that  $H_3O$  transforms from a crystalline solid to superionic solid at 1,250 K at 4.30 g/cm<sup>3</sup>, then to a fluid near 5,250 K (Fig. 3).

We also carried out AIMD simulations of H<sub>2</sub>O at comparable densities and temperatures to compare with the behavior of  $H_3O$ . The  $H_2O$  calculations were carried out at 4.93 g/cm<sup>3</sup> and 5,000-8,000 K. We find that solid H<sub>2</sub>O remains in a superionic state up to 7,000 K, where H<sub>3</sub>O is a fluid under these conditions (e.g., Fig. 3). In addition, we performed AIMD simulations using a supercell initially containing 48 H<sub>2</sub>O molecules (144 atoms) in the *Pbcm* structure (37) and 48 atoms of hydrogen in the  $I4_1/amd$ structure (38) at 4.30 g/cm<sup>3</sup> and 7,000 K (SI Appendix, Fig. S4A).

The results show that hydrogen atoms readily penetrate into the H<sub>2</sub>O lattice (SI Appendix, Fig. S4B), giving a radial distribution function for the H–H<sub>2</sub>O system that matches that of H<sub>3</sub>O (SIAppendix, Fig. S4C). These results validate a scenario in which H<sub>2</sub>O reacts with hydrogen to form H<sub>3</sub>O at these and even more extreme planetary interior conditions (SI Appendix, Fig. S5).

The above results enable us to construct a  $\vec{P}$ -T phase diagram of H<sub>3</sub>O covering the conditions corresponding to the interiors of Uranus and Neptune (Fig. 3A). The phase boundaries separating the solid, superionic, and fluid states were determined by AIMD simulations. The boundary separating H<sub>3</sub>O and its decomposition products ( $H_2O$  and  $H_2$ ) at low temperatures was determined by the difference in Gibbs free energy calculated using the quasiharmonic approximation (39). The isentropes of Uranus and Neptune pass through the stability field of the fluid phase of H<sub>3</sub>O (i.e., above  $\sim$ 500 and  $\sim$ 510 GPa), indicating that fluid H<sub>3</sub>O is viable deep inside these ice giants in a shell surrounding their proposed cores. From the estimated pressure-radius relationship for these planets (40), these calculations predict that fluid H<sub>3</sub>O stably exists in a thin-shell zone of 0.32-0.39 R (Fig. 3B), where R is the total radius of the planet. The density of fluid H<sub>3</sub>O at 0.32 Ris close to  $4.30 \text{ g/cm}^3$ , which is similar to the density of Uranus at the same radius  $(4.12 \text{ g/cm}^3)$  (40).

Electrical conductivity is crucial to understanding planetary magnetic fields generated by the planetary dynamo. To that end, we also calculated the electronic structure and electrical transport properties of these materials. Calculations of the electronic band gap show that H<sub>3</sub>O has a lower metallization temperature (~5,000 K at 540 GPa) than H<sub>2</sub>O (~6,000 K at 590 GPa) (SI Appendix, Fig. S6A). These results indicate that  $H_3O$  becomes a metallic fluid in the deep mantle conditions of Uranus and Neptune. In contrast, H<sub>2</sub>O remains in a superionic state and does not become a metallic fluid at these  $P - \hat{T}$  conditions (up to 7,000 K and 600 GPa); rather, in the presence of hydrogen it reacts to produce H<sub>3</sub>O. Further, the calculated electrical conductivity of H<sub>3</sub>O shows an abrupt increase between 5,000 and 6,000 K, i.e., from 19 to 164  $(\Omega \text{ cm})^{-1}$  (SI Appendix, Fig. S6B), which is consistent with the band-gap results. In contrast, the

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**Fig. 3.** The pressure–temperature phase diagram of  $H_3O$  in relation to the interiors of Uranus and Neptune. (A) Stability fields separating  $H_2O + H_2$  and solid, superionic, and metallic liquid phases of  $H_3O$ , obtained from AIMD simulations. The blue and red solid lines indicate proposed isentropes of Neptune and Uranus (25), with the depth axis referring to the former. The filled circle, filled square, and filled triangle data points are AIMD simulation results at 4.14, 4.30, and 4.52 g/cm<sup>3</sup>, respectively. (B) Possible schematic interior structure of Neptune. The gray and white regions represent the core and outer gas layers, respectively. The purple, blue, and orange areas represent regions dominated by ionic  $H_2O$ , superionic  $H_2O$ , and liquid  $H_3O$ , respectively. We emphasize that the boundaries shown are schematic and could be diffuse, and additional stratification cannot be ruled out (41). The pressure–radius relation was extracted from the estimate in ref. 40.

electrical conductivity of  $H_2O$  is found to be an order of magnitude lower than that of  $H_3O$  above 6,000 K, and no sudden changes in electrical conductivity are found for  $H_2O$  (*SI Appendix*, Fig. S6*B*). This metallization of  $H_3O$  on melting thus parallels that found for other materials such as silicon (42), diamond (43), and nitrogen (44).

# Discussion

The principal result of this study is the unexpected finding of the high degree of stability of  $H_3O$  at *P*-*T* conditions that correspond

to the deep interiors of Uranus and Neptune. The results are based on accurate and well-tested quantum simulations that have been validated for a variety of materials, in particular for low-Z materials, at extreme *P*-*T* conditions (e.g., refs. 19, 31, 32, and 45–48). Our AIMD simulations have not taken into account nuclear quantum effects for the hydrogens, the accurate determination of which requires substantial additional simulations. Although this is beyond the scope of the present work, the main conclusions regarding the predicted high degree of stability for H<sub>3</sub>O at the conditions explored are not expected to change since the simulated temperatures are higher than its Debye temperature (2,700 K at 500 GPa). This assessment is consistent with our previous studies of quantum effects in pure hydrogen and other hydrogen-rich systems at extreme conditions (48, 49).

The calculated *P*-*T* stability of H<sub>3</sub>O, together with its density and electrical conductivity under conditions at the base of the mantles of these planets, provide a materials basis for the underlying mechanism of their corresponding dynamos, specifically, for the thin-shell structure model conjectured for their planetary dynamos (5–8). Fluids with high electrical conductivity are essential to generating planetary magnetic fields (11). Our calculations reveal that the electrical conductivity of H<sub>3</sub>O reaches 164 ( $\Omega$  cm)<sup>-1</sup> at 6,000 K, an order of magnitude larger than the value of ~20 ( $\Omega$  cm)<sup>-1</sup> for ionic ice that has been proposed to be responsible for the magnetic field of Uranus (13). Given that fluid H<sub>3</sub>O is also more capable of convection than superionic solid ice, whose viscosity is expected to be several orders of magnitude larger than that of typical fluids, H<sub>3</sub>O is also more conducive to producing magnetic fields.

Another consideration concerns the effects of element partitioning and fluid miscibility. Ice layer compositional models for Uranus and Neptune mentioned above correspond to  $H_{35}O_7N$  (12) and  $H_{28}O_7N$ (41), or a hydrogen–oxygen composition of  $H_5O$  and  $H_4O$ , respectively. It has been suggested that  $H_2O$  and  $H_2$  can mix in all proportions in the fluid or plasma state at extreme conditions (30). On the other hand, the stability of  $H_3O$  in both solid and fluid phases predicted here and its similar density compared to that of the deep mantles inferred for Uranus and Neptune suggest a fluid metal with a composition close to that of  $H_3O$ . Indeed, the difference in densities (4.30 g/cm<sup>3</sup> calculated for  $H_3O$ versus 4.12 g/cm<sup>3</sup> inferred for the planets at the base of their mantles) can be explained by partitioning of other elemental components, including light elements C and N as well as heavier elements due to reactions with the proposed core.

Other materials models have been suggested for these planetary magnetic fields, including those arising from other complex metallic mixtures in their interiors as well as fluid hydrogen metallization (11, 41, 50, 51). The finding that H<sub>3</sub>O is stable over a broad range of the deep interiors of Uranus and Neptune indicates that any of these proposed models needs to take into account this species, even as a possible core component. We note that our proposal of a dominant H<sub>3</sub>O component at depth in ice giant planets is independent of whether the core is discrete (7), stably stratified (41), or diffuse as proposed for gas giants (52); the component could also be present at shallower depths in combination with other elements. These questions as well as the effects on melting and subsolidus phase relations for this multicomponent system at these extreme conditions remain to be studied. Moreover, the present predictions are within the range of current dynamic compression techniques (23, 53), and are thus expected to guide the design of experiments to test the theoretical results. The experiments should lead to improved understanding of the detailed structure of these unusual magnetic fields in terms of the component materials, specifically the geometry of the field represented as a strong displaced dipole.

There are also implications for other planets given that  $H_3O$  is found to be stable at more extreme *P*-*T* conditions than those found within Uranus and Neptune, including the variety of Neptune-like objects and for "water worlds" being discovered in exoplanet searches (54, 55). For example, OGLE-2008-BLG-092L (56), a planet with four times the mass of Uranus, would support an even thicker region of metallic  $H_3O$  within its interior. Fluid metallic  $H_3O$  would also be expected to be a component of gas giant interiors but detailed consideration of this possibility requires further study of its thermodynamic and transport properties at more extreme conditions.

#### Conclusions

Given that hydrogen and oxygen are the first and third most abundant elements in the solar system, a consideration of their chemical interactions over a broad range of P-T conditions is required to understand the interior composition, structure, and processes of large planetary bodies. Extensive detailed quantum-mechanical simulations reveal the stability of H<sub>3</sub>O at conditions corresponding to the deep interiors of Uranus and Neptune and indicate the importance of considering this chemical component for interior models of these planets. The stability, density, and electrical conductivity of fluid metallic H<sub>3</sub>O are an order of magnitude larger than those of H<sub>2</sub>O ice phases that have been proposed to be responsible for these magnetic fields. The results for the fluid metallic phase, in particular, provide a materials basis for the thin-shell dynamo model proposed to explain the magnetic field anomalies of Uranus and Neptune. Moreover, the theoretical results correspond to a P-T range that is accessible by current experimental techniques, and thus should guide future laboratory studies. The chemistry predicted at these extreme conditions will also be useful for developing accurate materials-based models for exoplanets, including the variety of Neptune-like objects that are being discovered.

### Methods

Extensive structure searches were conducted using a swarm-intelligencebased CALYPSO method and code, which enables global structure searching in conjunction with ab initio energetic calculations. This method has been benchmarked on various known systems (45–47, 57). Density-functional (DF) theory calculations were performed using the Vienna Ab initio Simulation Package (VASP) plane-wave code (58, 59), where the Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation DF (60) and frozencore all-electron projector-augmented wave potentials (61) are adopted. The cutoff radius of the pseudopotentials for oxygen and hydrogen were 0.58 and 0.42 Å, respectively. To ensure validity of the adopted pseudopotentials, we also performed full-potential all-electron calculations for the equation of state for  $H_3O$  over the pressure range studied here using the WIEN2K code (62). The VASP calculation results were nearly identical to those obtained from all-electron calculations (*S1 Appendix*, Fig. S7), validating the use of the pseudopotentials up to 600 GPa. The electronic wave functions

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were expanded in a plane-wave basis set with a kinetic energy cutoff of 1,200 eV, and the Brillouin zone (BZ) sampling was on *k* meshes with a reciprocal space resolution of  $2\pi \times 0.032$  Å<sup>-1</sup> to ensure that energies were converged to 1 meV/atom. The phonon calculations were performed with the Phonopy code (63) using a finite-displacement approach (64).

The AIMD simulations were performed in the canonical (NVT) ensemble applying a Nosé thermostat. A system containing 128 atoms was used for H<sub>3</sub>O. Simulations reach 15 ps, with the first 2-5 ps for equilibrating the system. The time step was chosen to be 0.5 fs, and a  $2 \times 2 \times 2$  k-mesh grid is used for the BZ sampling. To check for size effects, a larger system with 576 atoms was adopted. The transition temperature of this larger system was the same as for the smaller system, confirming convergence regarding system size. The simulated temperatures ranged from 1,000 to 7,000 K with a temperature step of 500 K, and we chose the temperature step in the regions of interest (1,000-1,500 K and 5,000-6,000 K) to be 250 K to investigate the temperatures for phase transitions from the crystalline solid to the superionic phase, and then to the fluid. The simulation cell for H<sub>2</sub>O contained 144 atoms. The Gibbs free energy (G) was calculated using the quasiharmonic approximation by the Phonopy code. G is defined at a constant T and P by the formula:  $G(T, P) = \min_{V} [U(V) + PV + F_{phonon}(T, V)]$ , where U is the internal lattice energy, V is volume, and  $F_{phonon}$  is the phonon free

energy.  $F_{phonon}(T, V) = k_B T \int_{0}^{\infty} g(\omega, V) \ln \left[ 2 \sinh \left( \frac{\hbar \omega}{2k_B T} \right) \right] d\omega$ , where  $g(\omega, V)$  is the phonon density of states at frequency  $\omega$  and volume V. The minimal value of

G was found at the equilibrium volume for a given T and P. The time-averaged valence-conduction electronic band gap was calculated using the PBE functional (50 configurations for averaging) and cross-checked using the GW method (65) (10 configurations for averaging). For GW calculations, a  $2 \times 2 \times 2$  k-mesh grid was used for balancing accuracy and efficiency (SI Appendix, Fig. S6). The PBE and GW calculations were in good agreement, and gave consistent results for H<sub>3</sub>O reaching the metallic state under the same P-T conditions (SI Appendix, Fig. S9). The time-averaged direct current electrical conductivity was calculated via the Kubo-Greenwood formula (66, 67). using the KGEC code (68), which is a postprocessor

module for use with the Quantum Espresso package (69). To obtain converged conductivity results, 576 atoms for H<sub>3</sub>O and 540 atoms for H<sub>2</sub>O were used in the simulation. A  $3 \times 3 \times 3 k$  mesh was used for BZ sampling. The conductivity values were determined from averaging over 10 configurations.

Data Availability Statement. All data discussed in the paper are available upon request.

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