

1 *Review*

## 2 Energy and Charge Transport in 2D Atomic Layer 3 Materials: Raman-based Characterization

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13 **Abstract:** As holding extraordinary mechanical and physical properties, two-dimensional (2D)  
14 atomic layer materials, including graphene, transition metal dichalcogenides, and MXenes, have  
15 attracted a great deal of attention. The characterization of energy and charge transport in these  
16 materials is particularly crucial for their applications. As noncontact methods, Raman-based  
17 techniques are widely used in exploring the energy and charge transport in 2D materials. In this  
18 review, we **explain the principle** of Raman-based thermometry in detail. We critically review  
19 different Raman-based techniques, which include steady state Raman, time-domain differential  
20 Raman, frequency-resolved Raman, and energy transport state-resolved Raman techniques  
21 constructed in frequency domain, space domain, and time domain. Detailed outlooks are provided  
22 about Raman-based energy and charge transport in 2D materials and issues that need special  
23 attention.

24 **Keywords:** 2D materials, energy transport, charge transport, Raman spectroscopy

25

### 26 1. Introduction

27 Owing to their extraordinary electrical, optical and mechanical properties, two-dimensional (2D)  
28 materials, for instance, graphene, black phosphorus, hexagonal boron nitride, transition metal  
29 dichalcogenides (TMDs), and MXenes, can be used in many different areas, for instance,  
30 optoelectronic devices, biosensing, energy storage, etc. [1-7]. And the thermal transport, interface  
31 thermal transport, electronic structures, physical structures, and hot carrier transport properties of  
32 these 2D materials are of great importance in fundamental research, as well as in engineering  
33 applications [8]. From the perspective of fundamental research, it is of great importance to explore  
34 the physics behind thermal dissipation and thermal management at the micro/nanoscale. For the  
35 application, with rapid increase in power density in modern electronics, the heat accumulation  
36 becomes a bottleneck for further miniaturization. As the heat accumulation in electronic and  
37 optoelectronic devices raises the operating temperature, the device performance and lifetime can be  
38 influenced. Thus, it is in high demand to improve the heat conductance and reduce the interface  
39 thermal resistance [8, 9].

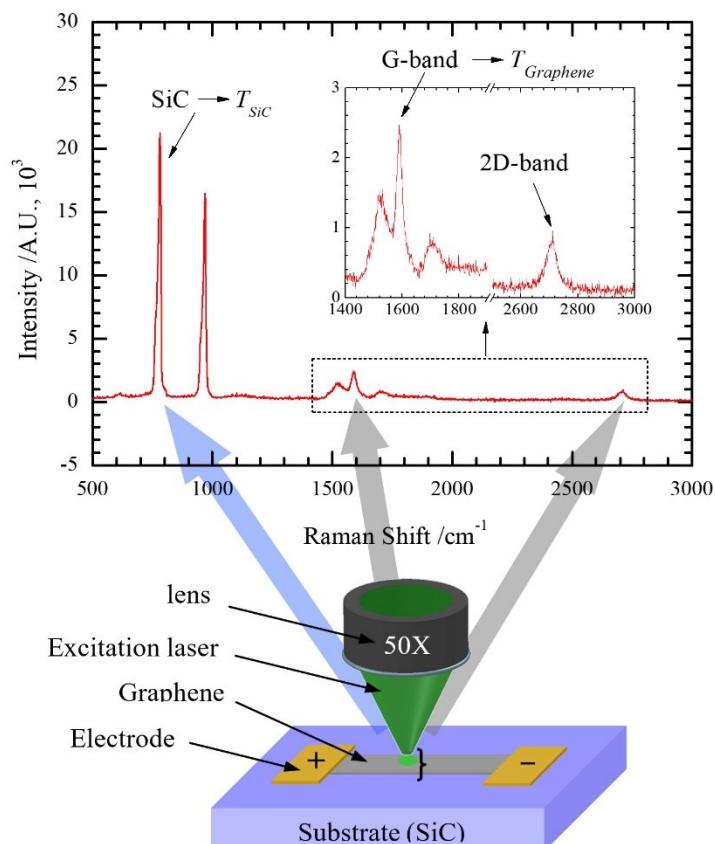
40 Over the last few years, many simulation-based methods have been reported to characterize the  
41 thermal transport in 2D materials, such as molecular dynamics simulation, non-equilibrium Green  
42 function method, Boltzmann transport equation, and first-principles-based multi-temperature model  
43 [10-13]. Many experimental methods, like time-domain thermoreflectance (TDTR), microbridge  
44 method,  $3\omega$  method, laser flash technique, and Raman spectroscopy, are employed to explore the

45 thermal properties of 2D materials [14-17]. For TDTR, it requires complicated setups and careful  
 46 operation. The accuracy of microbridge method is affected by the thermal contact resistance between  
 47 the sample and contact, and by the difficulty in evaluating the tiny heat flow sustained by very thin  
 48 samples. The  $3\omega$  method is vulnerable to the harmonic noises in the current source. The laser flash  
 49 technique will become extremely difficult to use for measuring very thin samples (a few  $\mu\text{m}$ ) and for  
 50 measurement at cryogenic temperatures. Raman spectroscopy, which carries signature information  
 51 about materials regardless of their distance and size, provides a unique way to looking into the  
 52 energy transport, hot carrier diffusion, and physical structure of 2D materials. As a noncontact optical  
 53 method, Raman-based thermometry is able to realize precise (material specific) and specific thermal  
 54 properties characterization of 2D materials with sub-micron size by focusing the excitation laser to a  
 55 very small spot.

56 Currently, many novel and new Raman-based techniques have been developed to meet different  
 57 requirements of 2D materials measurement. For instance, different energy transport states are  
 58 constructed to study the thermal conductivity, hot carrier diffusion, and interface thermal resistance  
 59 of suspended or supported 2D materials. In the following sections, a comprehensive critical review  
 60 about various Raman-based techniques developed for energy and charge transport in 2D materials  
 61 is presented to give a clear picture of the progress in this field. In addition, potential research  
 62 perspectives in the field of 2D materials using these Raman-based techniques are also discussed.

## 63 2. Steady State Raman

64 For steady state Raman, an electrical current or a continuous-wave laser is applied to the 2D  
 65 materials to realize steady state heating. Meanwhile, the sample is irradiated by an excitation laser  
 66 and the corresponding Raman signal is collected. Based on the temperature-dependence  
 67 characteristic Raman signal, the interface resistance between the sample and the substrate or the  
 68 thermal conductivity of the sample can be determined.

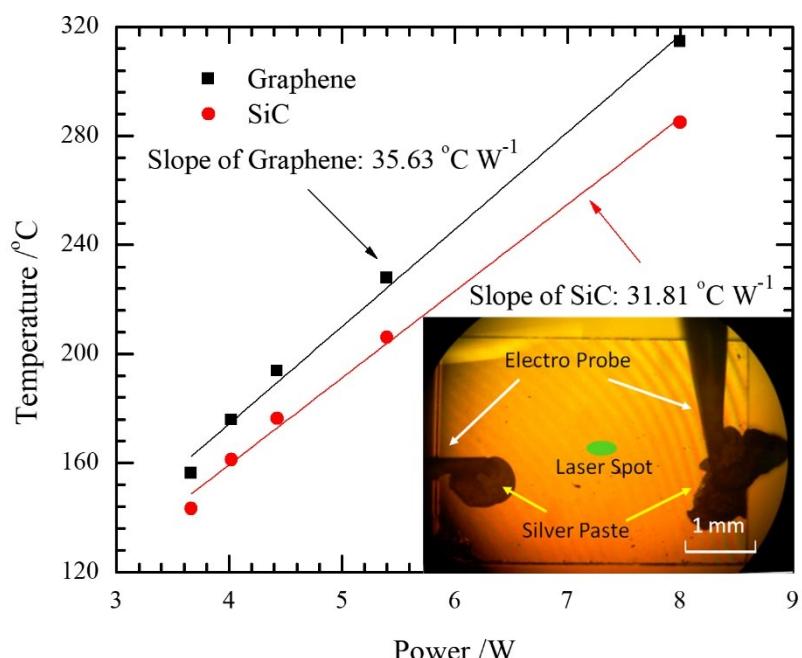


69  
 70 **Figure 1.** Illustration of the sample under electrical heating for measuring interface thermal  
 71 resistance. The top figure depicts the Raman spectrum of epitaxial graphene on 4H-SiC [18].

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73 Yue *et al.* developed an electrical heating method for the interfacial thermal resistance  
 74 **measurement** of epitaxial graphene on 4H-SiC [18]. As shown in Figure 1, the steady state heating of  
 75 the sample is achieved with an electrical current passing through. And a confocal Raman system is  
 76 used to obtain the Raman signal with an excitation laser irradiating the graphene. Then, the  
 77 temperature of graphene and SiC can be differentiated based on the corresponding Raman signals.  
 78 Finally, the interfacial thermal resistance between these two materials can be derived based on  
 79  $R_{tc} = (T_{graphene} - T_{SiC}) \cdot A / (I^2 \cdot R)$ , where  $A$  is the graphene area,  $R$  is the electrical resistance of graphene,  
 80 and  $I$  is the applied current. Due to the large uncertainty originated from a single temperature point,  
 81 a linear fitting of the relation between the temperature and input power of Joule heating is conducted.  
 82 The equation for determining thermal resistance can be rewritten as  $R_{tc} = (T'_{graphene} - T'_{SiC}) \cdot A$ , where  
 83  $T'_{graphene}$  and  $T'_{SiC}$  are the temperature against input power slopes shown in Figure 2.

84 Though the heating level can be controlled accurately by adjusting the electrical current, the  
 85 results can be affected by the contact resistance between the electrode and the sample. **Additionally**,  
 86 precise positioning of the laser is also important for Raman-based temperature measurement. To  
 87 overcome these drawbacks, Tang *et al.* developed a dual laser Raman-based thermal probing method  
 88 with a superior spatial resolution [19, 20]. In this method, two lasers are used, one is for thermal  
 89 probing, and the other one is for heating. In this work, the interfacial energy coupling across  
 90 graphene/substrate interfaces is characterized, and the experimental setup is shown in Figure 3. The  
 91 sample is placed on a nanostage, which is controlled by a piezoelectric actuator. As the stability is  
 92 improved dramatically and the positioning resolution could be down to as small as 5 nm, the noise  
 93 level in Raman spectra is greatly reduced.

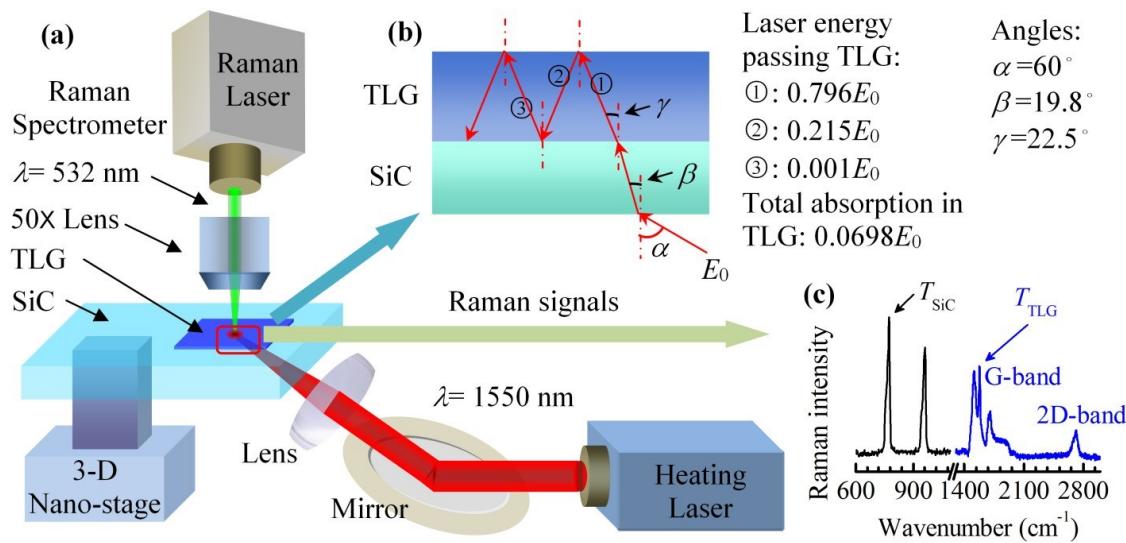


94

95 **Figure 2.** The relationship between temperature and heating power [18]. Figure reproduced  
 96 with permission from John Wiley and Sons.

97 During calibration and real interface measurement, 2D materials experience different stress  
 98 effect. In calibration, **the temperatures of the 2D material and the substrate are the same. However**,  
 99 **the temperature of the 2D material is higher than the substrate in actual experiment**. Additionally,  
 100 the 2D material has different thermal expansion coefficient from the substrate. Therefore, it does not  
 101 mean the temperature is determined precisely in experiment even with high quality calibration. Also  
 102 during experiment, the local spacing at the interface will significantly affect the laser absorption,

103 which could probably lead to very high error in laser absorption calculation. All these need to be  
 104 resolved in order to obtain high-level understanding of the energy transport in 2D materials interface.  
 105 Raman shift, which is related to temperature and stress, has a higher sensitivity to temperature than  
 106 Raman linewidth. Based on this, for the first time, Tang *et al.* decoupled the thermal and mechanical  
 107 behavior by looking into the difference in temperature determined by using Raman shift and  
 108 linewidth [20]. That is, the local stress effect is extracted, and the interface spacing effect is also  
 109 evaluated based on the corrugation-induced Raman enhancement.



111 **Figure 3.** Experimental system used for characterizing the tri-layered graphene/SiC  
 112 interface. An infrared laser is used to heat the sample and a 532 nm laser is used to excite  
 113 Raman signals. Reproduced from [20] with permission from The Royal Society of  
 114 Chemistry.

115 Furthermore, Yuan *et al.* also studied the interface thermal conductance between few to tens-  
 116 layered molybdenum disulfide (MoS<sub>2</sub>) and crystalline silicon (c-Si) [21]. In this work, only one laser,  
 117 which is for both thermal probing and heating, is used. And it is proved that there is a spacing  
 118 between MoS<sub>2</sub> and c-Si, which can lead to a much lower interfacial thermal conductance. As the  
 119 thermal expansion coefficients of MoS<sub>2</sub> and c-Si are different, the imperfect contact between MoS<sub>2</sub>  
 120 and c-Si could become much smoother after laser heating. In addition, with the increased sample  
 121 thickness, the mechanical stiffness is improved and a better interface contact between MoS<sub>2</sub> and c-Si  
 122 is obtained. Thus, the interface thermal conductance increases. In a short word, the interface spacing  
 123 effect is a very crucial factor in studying the interfacial thermal conductance, and it is necessary to  
 124 further investigate thermal expansion coefficients of the sample and substrate. Zobeiri *et al.* studied  
 125 the thermal expansion coefficient of WS<sub>2</sub> in detail [22]. In this work, the in-plane and cross-plane  
 126 linear thermal expansion coefficients of WS<sub>2</sub> were considered separately. And the in-plane linear  
 127 thermal expansion coefficient, which plays a very important role in calculating the theoretical air gap  
 128 thickness between WS<sub>2</sub> and Si substrate, was determined. The range is about  $5 \times 10^{-6}$  to  $8 \times 10^{-6}$  K<sup>-1</sup> with  
 129 temperatures varying from 300 to 700 K, and agrees well with reference values.

### 130 3. Time-domain Differential and Frequency-resolved Raman

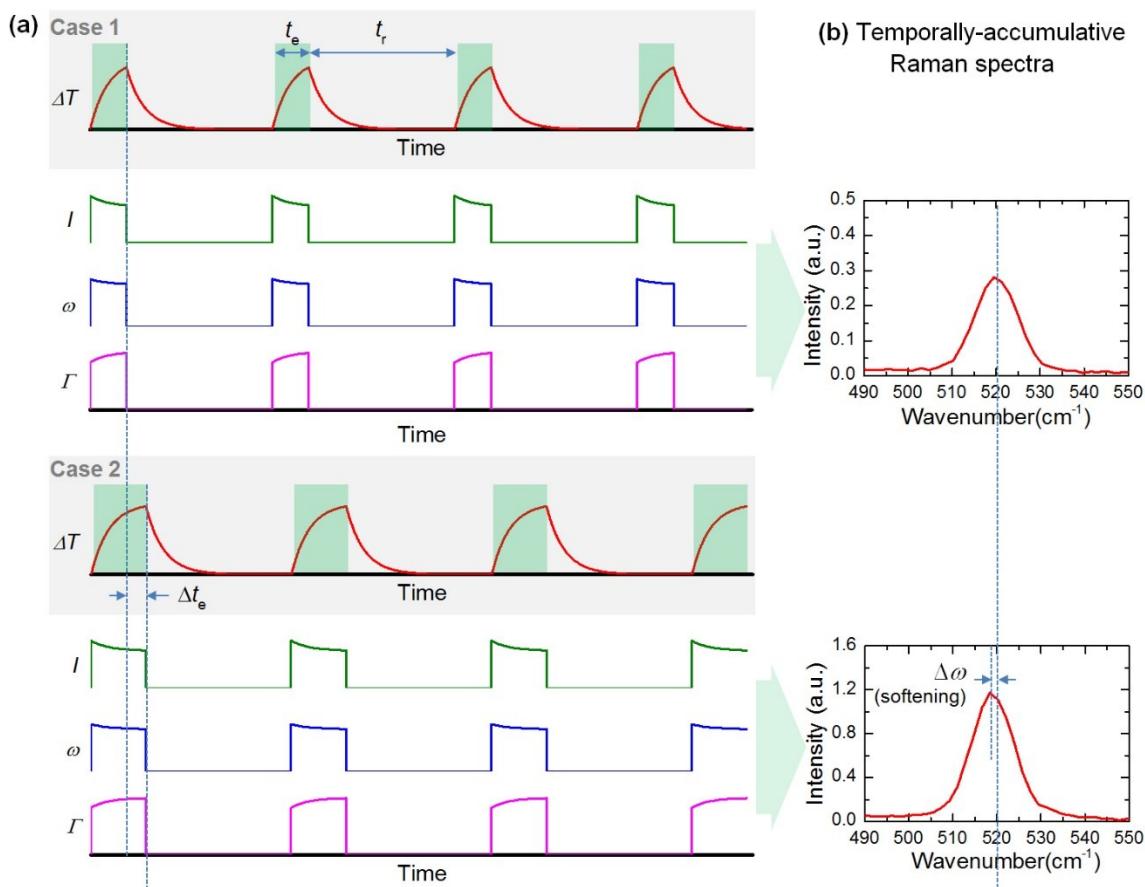
131 For steady-state Raman spectroscopy, a relationship between temperature and Raman signal is  
 132 needed. Both temperature calibration and laser absorption measurement are required to ensure the  
 133 accuracy of the measurement. However, the temperature calibration is really time-consuming and  
 134 could bring in large errors. Due to unknown optical property variation of different samples, the laser  
 135 absorption measurement can also introduce very large errors. To overcome these critical physics  
 136 problems faced in steady-state Raman spectroscopy, techniques involving time resolving will be

137 more appreciated.

138 *3.1. Time-domain Differential Raman (TD-Raman)*

139 The TD-Raman technique is inspired by the transient electro-thermal (TET) technique, which is  
 140 developed for effective thermal characterization of one-dimensional (1D) materials [23, 24]. In this  
 141 technique, a single modulated laser beam is used for both sample heating and thermal probing. The  
 142 concept of this technique is shown in Figure 4(a). Both transient and steady-state measurements are  
 143 conducted for this technique. The transient measurement consisted of an excitation period ( $t_e$ ) and a  
 144 thermal relaxation period ( $t_r$ ). And  $t_r$  is required to be long enough for the sample to completely cool  
 145 down upon coming of next laser cycle. Multiple cycles are used to collect sufficient Raman signal.

146 As shown in Figure 4(a), during the excitation period, there is a temperature rise and Raman  
 147 signal is also collected. With the increase of sample temperature, the Raman intensity decreases, the  
 148 peak is redshifted and the linewidth broadens. During  $t_r$ , as the laser is turned off, no Raman signal  
 149 is collected in this period. Comparing the two cases, the excitation period in Case 2 is a bit longer  
 150 than Case 1, while the thermal relaxation periods are the same. Due to the longer excitation time, the  
 151 temperature increases further, and the corresponding Raman spectrum also varies. Figure 4(b) shows  
 152 the temporally accumulative Raman spectra in the two cases. It can be seen that the Raman intensity  
 153 in Case 2 is higher than that in Case 1, and a Raman peak position softening is observed. By combining  
 154 the above Raman signal variation and further physical data analysis, the temperature evolution of  
 155 the sample can be obtained to determine the thermal diffusivity of the sample [23].



156  
 157 **Figure 4.** (a) The temperature evolution of the sample, and corresponding variations of  
 158 Raman peak intensity ( $I$ ), peak shift ( $\omega$ ) and linewidth ( $\Gamma$ ). (b) Temporally accumulative  
 159 Raman spectra of one laser pulse cycle in Case 1 and Case 2. Reprinted with permission  
 160 from [23] © The Optical Society.

161 In the work of TD-Raman development, the thermal diffusivity of a Si cantilever is measured. In

162 the experimental setup, one end is connected to bulk base and the other end is heated by a modulated  
 163 laser. As the length of the sample is much larger than the diameter or thickness of the sample, a one-  
 164 dimensional (1D) model is used for the heat conduction with the governing equation as:

165 
$$\rho c_p \frac{\partial \Delta T}{\partial t} = \kappa \frac{\partial^2 \Delta T}{\partial x^2} + q_0, \quad (1)$$

166 where  $\rho$  is the density,  $c_p$  is the specific heat of the sample,  $\Delta T$  is the temperature rise,  $\kappa$  is the  
 167 thermal conductivity,  $x$  is the distance away from the heat sink, and  $q_0$  is the heat generation per unit  
 168 volume induced by the laser heating. The spatially averaged temperature rise can be obtained based  
 169 on the following equation:

170 
$$\overline{\Delta T}(t) = \frac{2q_0 L^3}{\kappa(x_2 - x_1)} \sum_{m=1}^{\infty} \frac{1}{m^4 \pi^4} \left[ 1 - \exp\left(-\frac{m^2 \pi^2 \alpha t}{L^2}\right) \right] \left( \cos \frac{m\pi}{L} x_1 - \cos \frac{m\pi}{L} x_2 \right)^2, \quad (2)$$

171 where  $\alpha$  is the thermal diffusivity, and  $L$  is the sample length. The normalized temperature rise is  
 172 then obtained as:

173 
$$\overline{\Delta T}^* = \frac{\overline{\Delta T}(t)}{\overline{\Delta T}(t \rightarrow \infty)} = \frac{\sum_{m=1}^{\infty} \frac{1}{m^4 \pi^4} \left[ 1 - \exp\left(-\frac{m^2 \pi^2 \alpha t}{L^2}\right) \right] \left( \cos \frac{m\pi}{L} x_1 - \cos \frac{m\pi}{L} x_2 \right)^2}{\sum_{m=1}^{\infty} \frac{1}{m^4 \pi^4} \left( \cos \frac{m\pi}{L} x_1 - \cos \frac{m\pi}{L} x_2 \right)^2}. \quad (3)$$

174 As the variations of Raman signal are linearly related to temperature rise, the Raman spectra  
 175 obtained in experiment are employed to determine the average temperature rise of the sample in the  
 176 heated area. And the accumulative Raman emission for one excitation cycle (from 0 to  $t_e$ ) is calculated  
 177 based on the equation below:

178 
$$E_{\omega}(\omega, t_e) = I_0 \int_0^{t_e} (1 - A \overline{\Delta T}^*) \exp \left[ -\frac{4 \ln 2 \cdot (\omega - \omega_0 + B \overline{\Delta T}^*)^2}{(\Gamma_0 + C \overline{\Delta T}^*)^2} \right] dt, \quad (4)$$

179 where  $I_0$ ,  $\omega_0$ ,  $\Gamma_0$  are the corresponding Raman properties at the beginning of laser heating,  $A$ ,  $B$ ,  $C$  are  
 180 the changing rate of Raman intensity, Raman shift, and linewidth against the normalized  
 181 temperature. Then, a parameter named Fourier number  $Fo$  ( $Fo = \alpha t_e / L^2$ ) is substituted into Equation (4)  
 182 to get the following equation:

183 
$$E_{\omega}(\omega, Fo_e) = I_0 \int_0^{Fo_e} (1 - A \overline{\Delta T}^*) \exp \left[ -\frac{4 \ln 2 \cdot (\omega - \omega_0 + B \overline{\Delta T}^*)^2}{(\Gamma_0 + C \overline{\Delta T}^*)^2} \right] dFo, \quad (5)$$

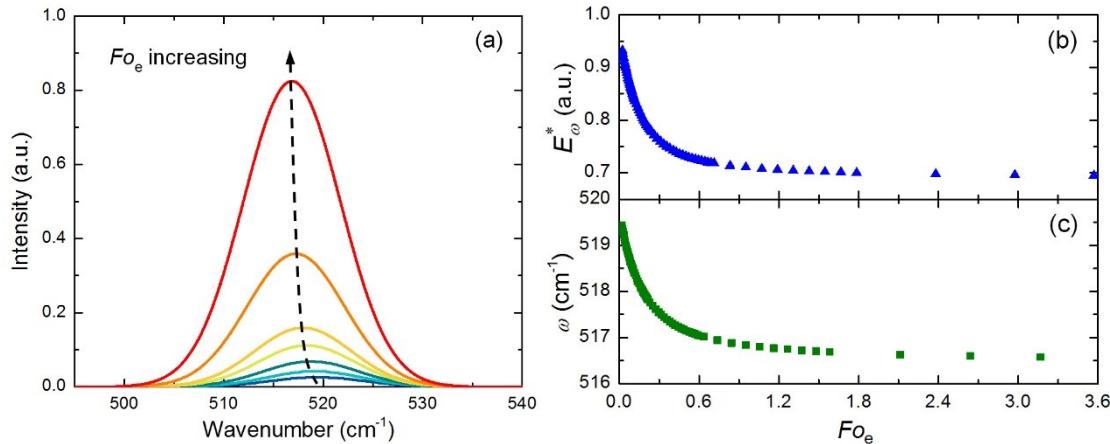
184 where  $Fo_e = \alpha t_e / L^2$ . In order to eliminate the integration time's effect, a normalized intensity is used and  
 185 the expression is:

186 
$$E_{\omega}^*(\omega, Fo_e) = \frac{I_0}{Fo_e} \int_0^{Fo_e} (1 - A \overline{\Delta T}^*) \exp \left[ -\frac{4 \ln 2 \cdot (\omega - \omega_0 + B \overline{\Delta T}^*)^2}{(\Gamma_0 + C \overline{\Delta T}^*)^2} \right] dFo. \quad (6)$$

187 Based on Equation (5), the reconstructed Raman spectra per cycle at different  $Fo_e$  is shown in  
 188 Figure 5(a). With the increase of  $Fo_e$ , the Raman peak is redshifted (softening), the linewidth becomes  
 189 slightly broader, and the Raman intensity increases significantly. The variations of normalized  
 190 Raman intensity and Raman shift against  $Fo_e$  are shown in Figure 5(b) and 5(c). As the temperature  
 191 increases rapidly at the beginning of laser heating, the normalized Raman intensity and Raman shift  
 192 decrease quickly correspondingly. With the increase of heating time, these two parameters will reach  
 193 a constant when the sample reaches steady state. Based on Equation (6), different trial values of  
 194 thermal diffusivity are used to find the best fitting curve for the experimental data. The thermal  
 195 diffusivity of the silicon cantilever is determined at  $9.17 \times 10^{-5} \text{ m}^2/\text{s}$ , which is very close to the reference  
 196 value of  $8.66 \times 10^{-5} \text{ m}^2/\text{s}$  [23]. Similarly, the thermal diffusivity of carbon nanotube fiber is also  
 197 determined, which is around  $1.74 \times 10^{-5} \text{ m}^2/\text{s}$  [24]. Although this technique has only been used in 1D  
 198 materials for concept design and testing, it can also be used to characterize the thermal diffusivity of

199 **2D materials, either supported and suspended.**

200 For the TD-Raman technique, both temperature rise and laser absorption information are not  
 201 needed. Therefore, it provides higher level physics understanding. However, a technical issue faced  
 202 in experiment is that: when the heating time is too short, the overall laser on time is very small, and  
 203 it takes extremely long time to collect the Raman signal. Thus, stage shift or environment noise will  
 204 increase the uncertainty, which indicates that it is extremely challenging to study very fast thermal  
 205 transport phenomena. This issue can be resolved using the frequency-resolved Raman (FR-Raman)  
 206 technique without sacrificing the measurement accuracy.



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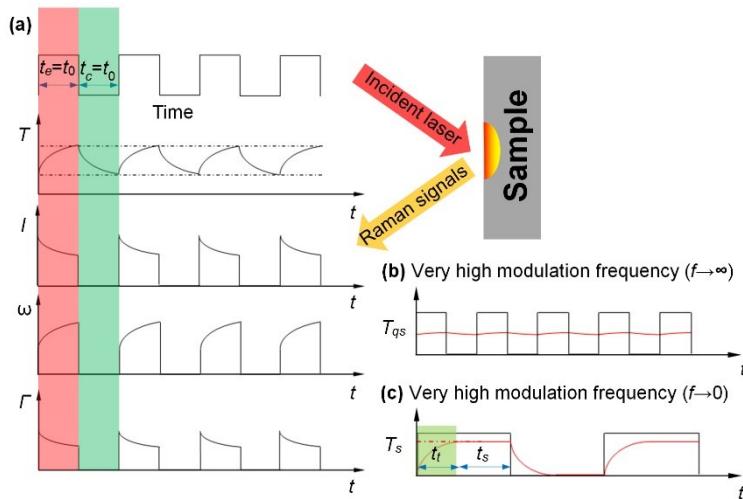
208 **Figure 5.** (a) The relationship between the reconstructed silicon Raman spectrum per cycle  
 209 and the Fourier number. (b) The decreasing trend of the normalized Raman intensity  
 210 against the Fourier number. (c) The decreasing trend of the Raman shift against the Fourier  
 211 number. Reprinted with permission from [23] © The Optical Society.

### 212 3.2. Frequency-resolved Raman (FR-Raman)

213 For the FR-Raman technique, as shown in Figure 6, an amplitude-modulated square-wave laser  
 214 with different frequencies is used for both sample heating and Raman signals collecting [25]. **Figure**  
 215 **6(a) shows that durations of the laser excitation time and the thermal relaxation time are the same.**  
 216 The temperatures at the beginning and end of the laser excitation time are frequency-dependent. At  
 217 very high frequencies, shown in Figure 6(b), the temperature rise in the laser excitation time and the  
 218 temperature fall in the thermal relaxation time are almost negligible. That is, the temperature of the  
 219 sample can be assumed to be constant in the whole process. And this state is named as “quasi-steady  
 220 state”. At very low frequencies, shown in Figure 6(c), the laser excitation time is long enough for the  
 221 temperature rising to a steady-state temperature. Also, the rising period, which was much smaller  
 222 than the heating period, can be neglected. As a result, the sample temperature can be seen as a  
 223 constant during the excitation time. And this state is termed “steady state”. The temperature rise  
 224 values at these two states are then taken as  $\Delta T_{qs}$  and  $\Delta T_s$ , where  $\Delta T_{qs} = \Delta T_s/2$ . As the heating effect  
 225 increases with the decrease of frequency, Raman intensity decreases and Raman peak redshifts. The  
 226 Gaussian distribution function is used to fit the Raman peaks to obtain precise Raman properties:  
 227 intensity, Raman shift, and linewidth. The variation of these properties against the modulation  
 228 frequency can be fitted to determine the thermal diffusivity of a sample. The determined thermal  
 229 diffusivities of Si based on Raman intensity and Raman shift are  $9.57 \times 10^{-5} \text{ m}^2/\text{s}$  and  $11.00 \times 10^{-5} \text{ m}^2/\text{s}$ ,  
 230 respectively, which agree well with literature value.

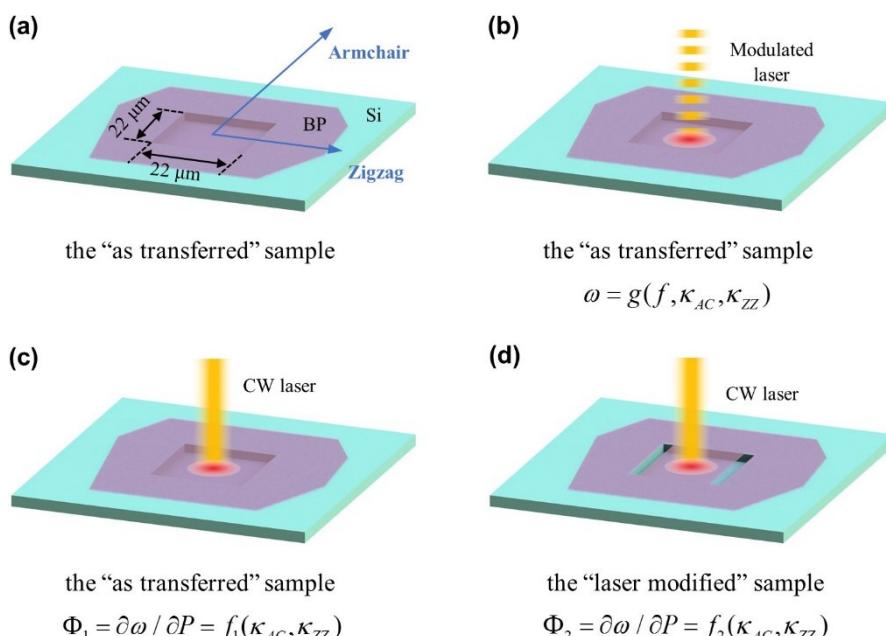
231 The FR-Raman technique not only provides a novel way to probe transient thermal transport  
 232 with very high temporal resolution, but also can be used to characterize the anisotropic thermal  
 233 conductivities of materials without the need of optical absorption and temperature coefficient [26].  
 234 The example given here is for the measurement of black phosphorus (BP). As shown in Figure 7(a),  
 235 the armchair and zigzag directions of the suspended BP are aligned along an edge of a square dent.  
 236 Figure 7(b) shows that the sample is irradiated by a modulated laser beam and the corresponding  
 237 Raman spectra are collected. Then, as shown in Figure 7(c) and 7(d), Raman spectra of the sample

238 before and after cutting are collected upon continuous wave (CW) laser irradiation with different  
 239 laser powers. The power differential of the Raman shift  $\Phi_1$  and  $\Phi_2$  are determined. For these two  
 240 parameters,  $\Phi_1$  depends on the armchair thermal conductivity  $\kappa_{AC}$  and the zigzag thermal  
 241 conductivity  $\kappa_{ZZ}$ , while  $\Phi_2$  mainly depends on  $\kappa_{AC}$ . These two values are linearly related to the average  
 242 temperature rise in the heating region  $\Delta T_1$  and  $\Delta T_2$ , which are obtained from the ANSYS simulation  
 243 results shown in Figure 8(a) and 8(b). Afterwards, as shown in Figure 8(c),  $\eta$  ( $\kappa_{ZZ}/\kappa_{AC}$ ) can be  
 244 determined by interpolating  $\Phi_2/\Phi_1$  to the simulated curve of  $\Delta_2/\Delta T_1$  and  $\eta$ .



245  
 246  
 247  
 248

**Figure 6.** (a) Mechanism of FR-Raman. (b) Temperature variation at quasi-steady state. (c)  
 Temperature variation at very low frequency (close to steady-state). Reprinted with  
 permission from [25] © The Optical Society.



249

**Figure 7.** (a) Schematic of a suspended BP sample. (b) Sample irradiated by a modulated  
 laser beam. (c) Sample irradiated by a CW laser beam before cutting. (d) Sample irradiated  
 by a CW laser beam after cutting at two parallel boundaries. Reprinted from [26], with the  
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 253

The determination of  $\kappa_{AC}$  is realized by comparing the experimental normalized average temperature rise  $\Delta \bar{T}_{nor\_e}$  with its simulated counterpart  $\Delta \bar{T}_{nor\_s}$ . In the simulation,  $\kappa_{AC}$  is adjusted to

256 reach a minimum standard deviation between  $\Delta\bar{T}_{nor\_e}$  and  $\Delta\bar{T}_{nor\_s}$ . And  $\Delta\bar{T}_{nor\_e}$  is calculated from  $\omega(f)$   
 257 using the equation below:

258

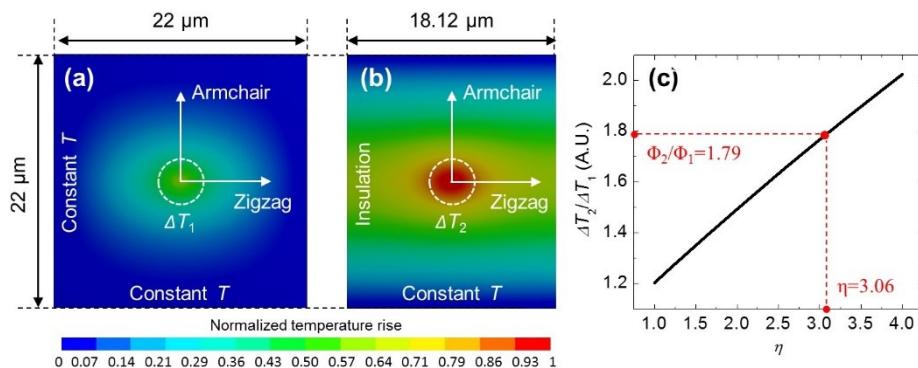
$$\Delta\bar{T}_{nor\_e} = 1 + C \cdot [\omega(f) - \omega_s] / \Delta\omega, \quad (7)$$

259 where  $\Delta\omega$  and  $\omega_s$  are obtained from steady state,  $C$  is a correction coefficient. Theoretically,  $\Delta\bar{T}_{nor\_e}$   
 260 decreases from 1 (steady state) to 0.5 (quasi-steady state), and the experimental data are shown in  
 261 Figure 9(a). ANSYS is also used to simulate the thermal response to determine  $\Delta\bar{T}_{nor\_e}$ , which is equal  
 262 to:

263

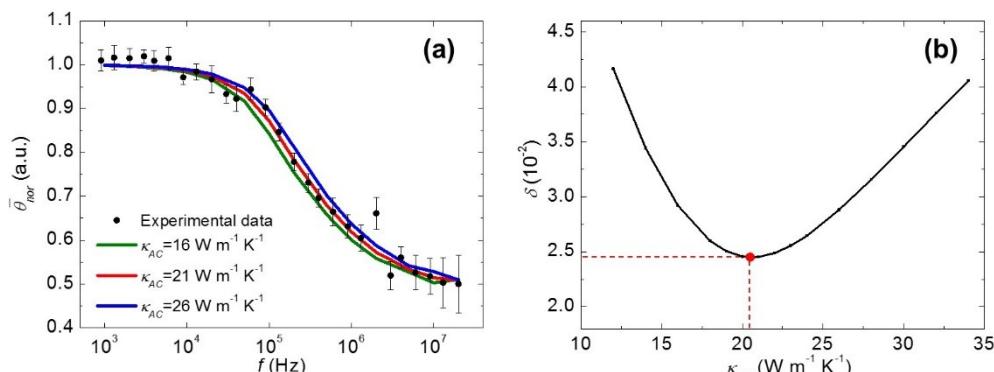
$$\Delta\bar{T}_{nor\_s} = \frac{\int_0^{1/2f} \sum_{n=0}^{\infty} (-1)^n \cdot \Delta T_s(t_p + n/(2f)) dt}{(1/2f) \cdot \Delta\bar{T}_{\infty}}, \quad (8)$$

264 where  $\Delta T_s(t)$  represents the temperature rise as a function of time,  $\Delta\bar{T}_{\infty}$  is the average temperature  
 265 rise in the steady state. Since  $\eta$  is already known,  $\Delta\bar{T}_{nor\_s}$  is a function of  $f$  and  $\kappa_{AC}$ . Thus, the variation  
 266 of  $\Delta\bar{T}_{nor\_s}$  against  $f$  is only determined by  $\kappa_{AC}$ . Figure 9(a) shows three fitting curves by adjusting the  
 267  $\kappa_{AC}$  values. Based on the curve between  $\kappa_{AC}$  and standard deviation  $\delta$ , shown in Fig. 9(b), the best  
 268 fitting value is obtained.



269

270 **Figure 8.** (a) and (b) Simulated normalized temperature rise distribution in the 157.6-nm  
 271 thick sample before cutting and after cutting. (c) The theoretical curve of  $\Delta T_2 / \Delta T_1$  as a  
 272 function of  $\eta$ . Reprinted from [26], with the permission of AIP Publishing.



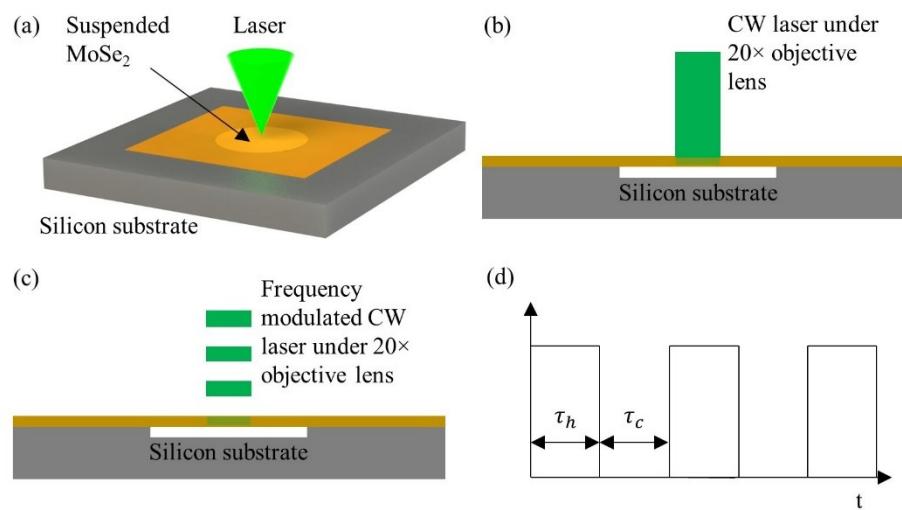
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274 **Figure 9.** (a) The various theoretical fitting curves of experimental data. (b) The standard  
 275 deviation  $\delta$  of experimental data to theoretical curves as a function of  $\kappa_{AC}$ . Reprinted from  
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277 **3.3. Frequency-domain Energy Transport State-resolved Raman (FET-Raman)**

278 For FR-Raman, the data fitting is for the Raman shift against the modulation frequency, and it

takes quite tremendous measurements. An alternative, named FET-Raman, is to fix the frequency, but vary the laser power and study the Raman shift change against laser power [27, 28]. Here we take the work on MoSe<sub>2</sub> to introduce this technique. The physical principle of this technique is shown in Figure 10. During each heating period, since the thermal diffusion length of MoSe<sub>2</sub> in the cross-plane direction is much longer than the sample thickness, the thermal transport in the cross-plane direction can be neglected. The first energy transport state is the steady state heating constructed by a CW laser, shown in Figure 10(b). By using different laser powers ( $P$ ), a parameter named Raman shift power coefficient (RSC) is obtained:  $\psi_{\text{CW}} = \partial\omega/\partial P = \alpha \cdot (\partial\omega/\partial T) \cdot f_1(\kappa)$ , where  $\alpha$  is laser absorption coefficient,  $\partial\omega/\partial T$  is Raman shift temperature coefficient, and  $\kappa$  is in-plane thermal conductivity of MoSe<sub>2</sub>. The second energy transport state is a transient state heating constructed by a square wave modulated CW laser, shown in Figure 10(c) and 10(d). After a sufficient number of heating cycles, the sample temperature will vary periodically with time. As illustrated in Section 3.2, the energy transport state changes from quasi-steady state to steady state with the decrease of frequency. Therefore, an appropriate frequency should be selected to construct a transient state with good sensitivity. Based on the curves shown in Figure 9(a), this frequency should be around the middle of quasi-steady state to steady state range. Then, a similar RSC value is also obtained:  $\psi_{\text{FR}} = \partial\omega/\partial P = \alpha \cdot (\partial\omega/\partial T) \cdot f_2(\kappa, \rho c_p)$ , where  $\rho c_p$  is volumetric heat capacity of the sample.

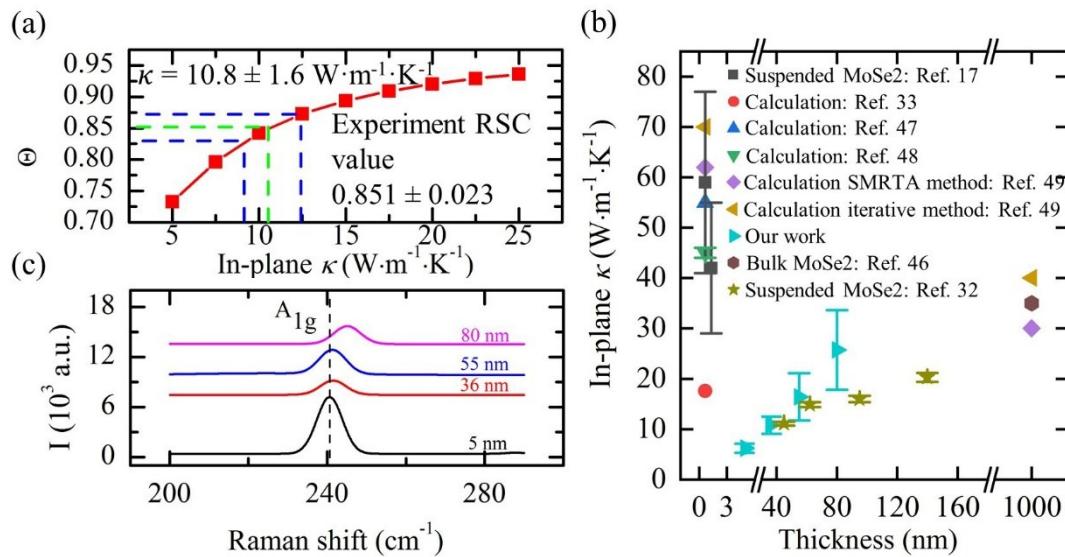


296

297 **Figure 10.** (a) Schematic of suspended MoSe<sub>2</sub> nanosheet. (b) Suspended MoSe<sub>2</sub> sample  
298 under CW laser and (c) under frequency-modulated CW laser heating and Raman  
299 excitation. (d) Square wave used to modulate the CW laser. Reprinted from [27], Copyright  
300 (2019), with permission from Elsevier.

301 As the thermal diffusion lengths in the two states are different, a dimensionless normalized RSC  
302  $\Theta = \psi_{\text{FR}} / \psi_{\text{CW}} = f_3(\kappa, \rho c_p)$  is used to completely eliminate the effects of  $\alpha$  and  $\partial\omega/\partial T$ . In the  
303 experiment, very low laser powers are employed to ensure a moderate temperature rise of the  
304 sample. This ensures the effect of volumetric heat capacity change with temperature can also be  
305 ignored. That is, the normalized RSC is only related to the in-plane thermal conductivity of MoSe<sub>2</sub>. A  
306 3D numerical modeling is then conducted to characterize the temperature profile under these two  
307 states. A theoretical relation between the ratio of temperature rises in the two states and in-plane  
308 thermal conductivity is obtained. The in-plane thermal conductivity of the sample can be determined  
309 by interpolating the experimental data into the curve. As shown in Figure 11(a),  $\kappa$  of a 36 nm-thick  
310 MoSe<sub>2</sub> is determined as  $10.8 \pm 1.6 \text{ W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ . Figure 11(b) shows the  $\kappa$  values of MoSe<sub>2</sub> with different  
311 thickness from different studies, and the feasibility of FET-Raman technique firmly verified. **Figure**  
312 **11(c) shows the blue shift of Raman spectra with the increased thickness, which means the interlayer**  
313 **Van der Waals force in MoSe<sub>2</sub> is increasing.** Additionally, combining with the TET technique, the  
314 FET-Raman can also be used to characterize the anisotropic thermal conductivity of carbon fibers

315 [28].



316

317 **Figure 11.** (a) 3D numerical simulation of a 36 nm-thick MoSe<sub>2</sub> sample. (b) Comparison of  
 318 in-plane  $\kappa$  values of MoSe<sub>2</sub> nanosheets from different studies. (c) The blue shift of Raman  
 319 peak with the increase of sample thickness. Reprinted from [27], Copyright (2019), with  
 320 permission from Elsevier.

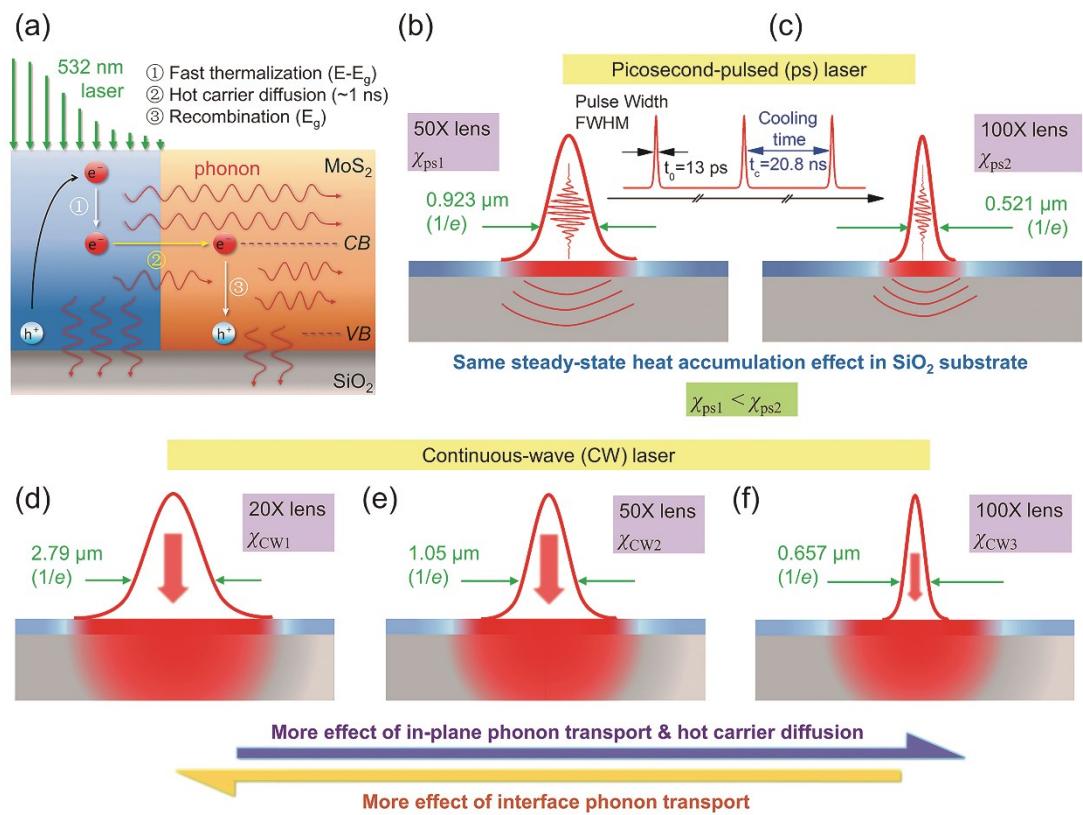
#### 321 4. Energy Transport State-resolved Raman

322 Similar to the modulation of laser in TD-Raman technique, the CW laser used in FET-Raman  
 323 technique is also modulated with a square wave. In addition to the modulation in time domain, this  
 324 energy transport design can also be extended to spatial domain to control the energy transport states.  
 325 Yuan *et al.* reports a novel technique for non-contact simultaneous determination of interface thermal  
 326 resistance ( $R$ ) and hot carrier diffusion coefficient ( $D$ ) of MoS<sub>2</sub> nanosheets on c-Si by varying the laser  
 327 heating area [29]. In this work, the constructed two energy transport states are in spatial domain. **To**  
 328 **be fully free from the large errors of laser absorption evaluation and temperature coefficient**  
 329 **calibration, a further developed technique named energy transport state-resolved Raman (ET-**  
 330 **Raman) is developed to determine  $R$  and  $D$**  [30, 31]. In this technique, three distinct energy transport  
 331 states in both spatial and time domains are constructed to probe materials' thermal response.  
 332 Furthermore, a five-state ET-Raman technique is proposed to measure  $\kappa$  of MoS<sub>2</sub>, and the effects of  
 333  $R$  and  $D$  are taken into consideration, and all these properties are determined simultaneously [32].

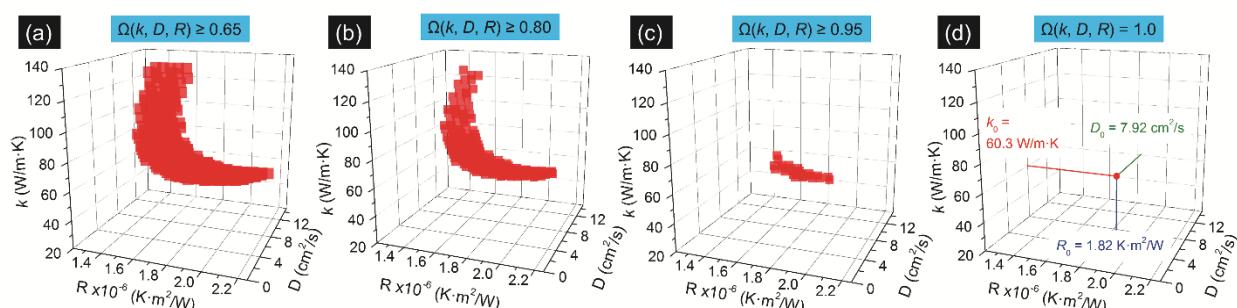
334 Figure 12 (a) shows the physical principles of this technique. A laser with 532 nm wavelength is  
 335 used to irradiate the sample for both laser heating and Raman probing. As the excitation energy is  
 336 higher than the band gap of MoS<sub>2</sub>, three physical processes take place. First, hot carriers are  
 337 generated, and then diffuse in space before the electron-hole recombination. Subsequently, phonons,  
 338 which receive energy from the hot carriers or electron-hole recombination, transports the energy by  
 339 heat conduction. This process mainly depends on  $\kappa$  of the sample. The third process, which is  
 340 determined by  $R$ , is the heat conduction from MoS<sub>2</sub> to the substrate. As shown in Figure 12 (d) - (f),  
 341 combined with three different objective lenses (20 $\times$ , 50 $\times$ , and 100 $\times$ ), a CW laser is used to construct  
 342 three steady states. Similar to FET-Raman, three RSCs ( $\chi_{\text{CW}_1}$ ,  $\chi_{\text{CW}_2}$ ,  $\chi_{\text{CW}_3}$ ) can be obtained, and we  
 343 have  $\chi_{\text{CW}_3} > \chi_{\text{CW}_2} > \chi_{\text{CW}_1}$ . With the decrease of laser spot size,  $D$  and  $\kappa$  play a much more important  
 344 role in determining the temperature of the sample. Based on this, the effects of  $R$ ,  $\kappa$ , and  $D$  can be  
 345 differentiated.

346 In this technique, two transient states are designed by using a picosecond-pulsed laser with two  
 347 objective lenses (50 $\times$  and 100 $\times$ ), shown in Figure 12 (b) and (c), to rule out the large errors introduced  
 348 by laser absorption evaluation and temperature coefficient calibration. Similarly, two RSCs under the

349 two lenses are obtained as  $\chi_{ps_1}$  and  $\chi_{ps_2}$ , respectively. And the heat accumulation effect can be  
 350 ruled out by taking the difference of these two RSCs as  $\chi_{ps_2} - \chi_{ps_1}$ . Based on the five measured RSCs,  
 351 three dimensionless normalized RSCs  $\Theta_1 = \chi_{CW_1}/(\chi_{ps_2} - \chi_{ps_1})$ ,  $\Theta_2 = \chi_{CW_2}/(\chi_{ps_2} - \chi_{ps_1})$ , and  
 352  $\Theta_3 = \chi_{CW_3}/(\chi_{ps_2} - \chi_{ps_1})$  are obtained. And all these coefficients, which are related to the temperature  
 353 rise of the sample, are functions of  $\rho c_p$ ,  $R$ ,  $D$ , and  $\kappa$ .



354  
 355 **Figure 12.** The mechanism of five-state ET-Raman technique. (a) Physical processes  
 356 happening in MoS<sub>2</sub> upon laser irradiating. (b) and (c) Two transient states in picosecond  
 357 laser heating under 50 $\times$  and 100 $\times$  objective lenses. (d) – (f) Three steady states under a CW  
 358 laser with 20 $\times$ , 50 $\times$ , and 100 $\times$  objective lenses [32]. Reproduced by permission of the PCCP  
 359 Owner Societies.

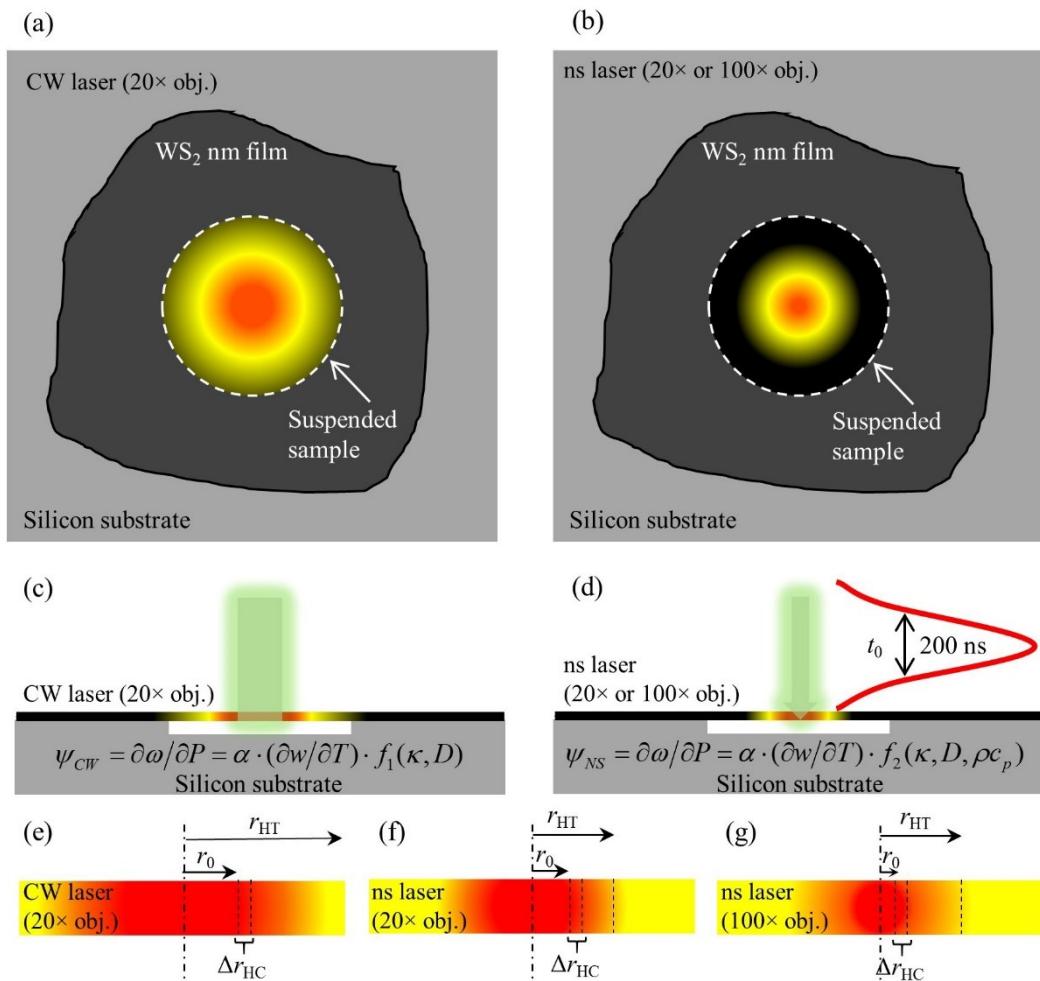


360  
 361 **Figure 13.** The normalized probability distribution function  $\Omega(\kappa, D, R)$  with the  
 362 probability of 0.65 in (a), 0.80 in (b), 0.95 in (c), and 1.0 in (d) [32]. Reproduced by permission  
 363 of the PCCP Owner Societies.

364 A 3D numerical modeling is employed to calculate the temperature rise to determine  $R$ ,  $D$ , and  
 365  $\kappa$  simultaneously. To normalize the  $(\kappa, D, R)$  space data, a normalized probability distribution

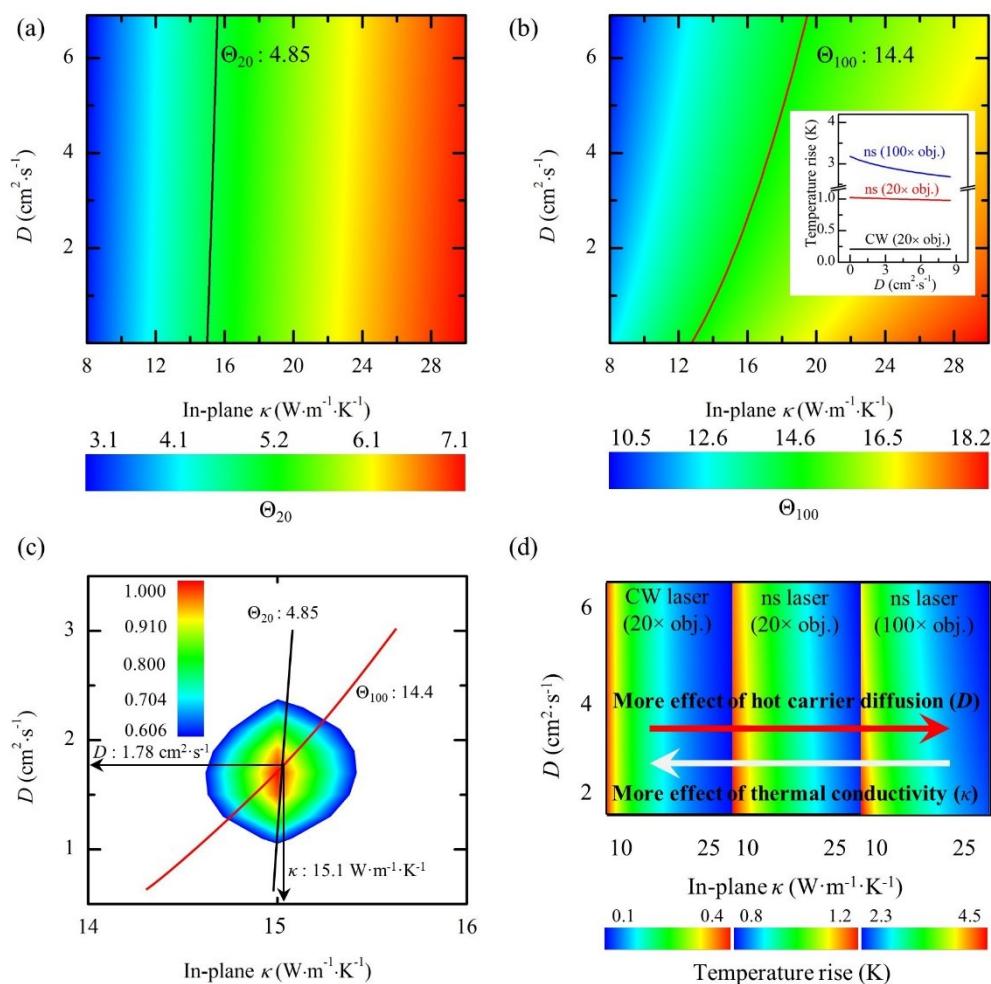
366 function  $\Omega_i = \exp\left[-(\Theta_i - \Theta_{\exp_i})^2 / (2\sigma_i^2)\right]$  ( $i = 1, 2$ , and  $3$ ) is employed.  $\Theta_i$  and  $\Theta_{\exp_i}$  are  
 367 normalized RSCs from 3D modeling and experiment, respectively.  $\sigma_i$  is the experimental  
 368 uncertainty. Then,  $(\kappa, D, R)$  of the sample can be determined when a composite probability  
 369 distribution function  $\Omega(\kappa, D, R) = \Omega_1 \cdot \Omega_2 \cdot \Omega_3$  is equal to 1. Figure 13 shows the determination of the  
 370 three parameters for 2.4 nm-thick MoS<sub>2</sub>. With the increase of probability level from 0.65 to 1.0, the  $(\kappa, D, R)$   
 371 space range is decreased to have only one point in the space that could give  $\Omega(\kappa, D, R) = 1$ . Based on this,  
 372 there three parameters can be obtained as  $\kappa_0 = 60.3 \text{ W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ ,  $D_0 = 7.92 \text{ cm}^2 \cdot \text{s}^{-1}$ ,  
 373 and  $R_0 = 1.82 \times 10^{-6} \text{ K} \cdot \text{m}^2 \cdot \text{K}^{-1}$ , respectively.

374 In addition to supported 2D materials, the ET-Raman technique can also be used for suspended  
 375 2D materials. However, a strong heat accumulation will happen in suspended samples because of  
 376 the very short pulse interval for the picosecond laser, a nanosecond laser is used instead [33, 34].  
 377 Wang *et al.* used one CW laser and one nanosecond laser with the same wavelength to construct the  
 378 steady state heating and transient state heating [33]. The in-plane thermal conductivities of  
 379 suspended MoS<sub>2</sub> and MoSe<sub>2</sub> with different thickness are measured. However, the hot carrier effect  
 380 is not considered in this work. Zobeiri *et al.* developed a 3-state nanosecond ET-Raman technique to  
 381 measure  $\kappa$  and  $D$  of nm-thick suspended WS<sub>2</sub> films [34].



382  
 383 **Figure 14.** (a) and (b) Heat conduction of suspended WS<sub>2</sub> nanosheets irradiated by a CW  
 384 and a nanosecond laser. (c) and (d) Steady state and transient state constructed using the  
 385 two lasers. (e-g) Heat diffusion length, laser spot radius, and hot carrier diffusion length  
 386 under the three states. Reprinted from [34], Copyright (2019), with permission from  
 387 Elsevier.

388 In the 3-state nanosecond ET-Raman technique, the three heat transport states are constructed  
 389 with two lasers and two objective lenses. As shown in Figure 14 (a), a CW laser with a  $20\times$  objective  
 390 lens is used to construct the steady state. Figure 14 (b) shows that two transient states are constructed  
 391 using a nanosecond pulsed laser and two different objective lenses ( $20\times$  and  $100\times$ ). Since the  
 392 thickness is very thin, the temperature distribution in the thickness direction is assumed to be  
 393 uniform. Similarly, three RSCs under the three states are obtained as  $\psi_{CW}$ ,  $\psi_{ns20}$ ,  $\psi_{ns100}$ . As shown in  
 394 Figure 14 (c),  $\psi_{CW}$  is a function of  $\alpha$ ,  $\kappa$ ,  $D$ , and Raman temperature coefficient ( $\partial\omega/\partial T$ ). While, both  
 395  $\psi_{ns20}$  and  $\psi_{ns100}$  are a function of  $\alpha$ ,  $\kappa$ ,  $D$ ,  $\rho c_p$ , and  $\partial\omega/\partial T$ , shown in Figure 14 (d). And the effects of  
 396  $\kappa$  and  $D$  can be distinguished by using the two objective lenses to vary the local heating size.  
 397 Considering the moderate temperature rise in the experiment,  $\rho c_p$  can be taken as a constant.



398  
 399 **Figure 15.** (a) and (b)  $\Theta$  for different  $\kappa$  and  $D$  values obtained from simulation and  
 400 experiments of the 13 nm-thick sample under (a)  $20\times$  and (b)  $100\times$  objective lenses. (c) Measured  $\kappa$  and  $D$ . (d) The sensitivity variation of temperature rise to  $\kappa$  and  $D$  under different energy transport states. Reprinted from [34], Copyright (2019), with permission from Elsevier.

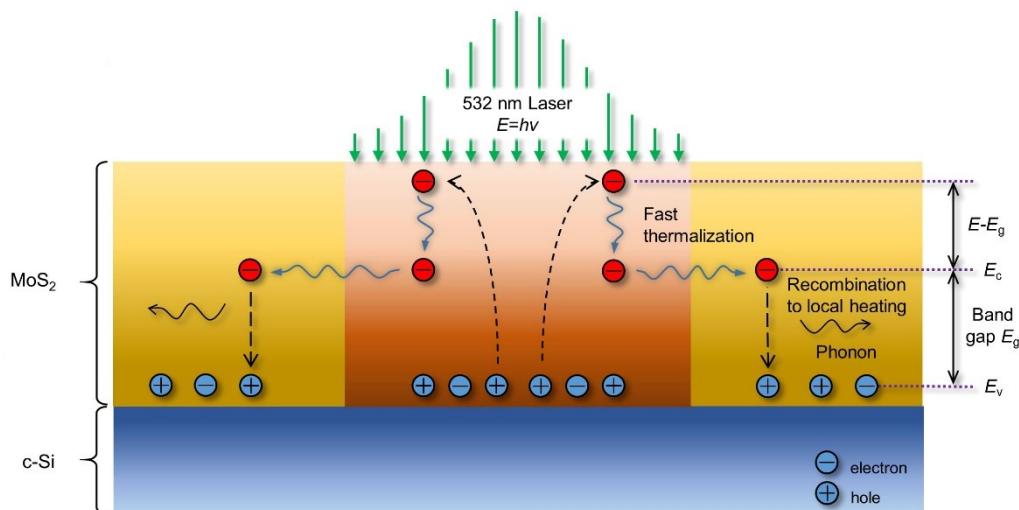
404 Based on the three RSCs, two normalized RSCs are defined as  $\Theta_{20} = \psi_{ns20}/\psi_{CW}$  and  
 405  $\Theta_{100} = \psi_{ns100}/\psi_{CW}$ . Then, the effects of  $\alpha$  and  $\partial\omega/\partial T$  are ruled out. Figure 14 (e-g) shows the heat and  
 406 hot carrier diffusion lengths in the in-plane direction of suspended sample. Under steady state, the  
 407 heat can transfer to the boundaries of the sample. While under the two transient states, the thermal  
 408 transport is nearly confined in the laser spot area. That is, the effect of  $\kappa$  on thermal transport is more  
 409 significant under steady state. As shown in Figure 15 (d), the effect of  $\kappa$  becomes less significant with  
 410 the decrease of local heating size, while the effect of  $D$  becomes more prominent with the decrease of

411 local heating size. The temperature rise under the three states are simulated to obtain the theoretical  
 412  $\Theta$  values under different  $\kappa$  and  $D$  trial values, shown in Figure 15 (a) and (b). The solid lines indicate  
 413 that several  $(\kappa, D)$  combinations can match the experimental values. As shown in Figure 15 (c), by  
 414 using the two solid lines to locate the cross-point,  $\kappa$  and  $D$  values are determined as  $15.1 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$   
 415 and  $1.78 \text{ cm}^2\cdot\text{s}^{-1}$ , respectively.

416 In summary, different energy transport states are constructed in both time and space domains  
 417 to characterize the thermal properties of supported or suspended samples. Either a picosecond or a  
 418 nanosecond laser is used to realize the differential in time domain. Similarly, TDTR technique  
 419 measures thermal properties by heating the surface of the sample with a train of laser pulses and  
 420 detecting the resulting temperature variation through the reflectivity of the surface with a time-  
 421 delayed laser. This technique is able to detect temperature evolution at micrometer-scale and  
 422 picosecond-scale resolutions, which indicates that it can be used to explore non-equilibrium thermal  
 423 phenomena [14]. The ET-Raman technique in fact measures a material's thermal response within a  
 424 pulse in an integral way. It gives an average temperature within a very short time domain (ns or ps),  
 425 and provides a completely new way to characterize nanoscale energy transport.

## 426 5. Probing of Conjugated Hot Carrier Transport

427 In most of the work on Raman study of energy transport in 2D materials, hot carrier diffusion is  
 428 not considered, although this effect could be critically important, especially for tightly focused laser  
 429 spot ( $<0.5 \mu\text{m}$  diameter). Figure 16 shows the physics of hot carrier diffusion. The sample is irradiated  
 430 by a laser, the energy of which is higher than the bandgap of  $\text{MoS}_2$ . Thus, electrons are excited to the  
 431 conduction band while leaving holes in the valence band. Then a fast thermalization process (about  
 432  $10^{-12} \text{ s}$ ) happens, and hot carriers dissipate part of the energy to other electrons and lattice. This  
 433 process is neglected due to the very short time. The second process is hot carrier diffusion, in which  
 434 the remaining photon energy carried by electrons is diffused out of the laser spot area before  
 435 recombining with holes. As this process is typically in nanoseconds, it should be taken into  
 436 consideration. Afterwards, electrons and holes recombine because of Coulomb attraction, the energy  
 437 is released by exciting phonons at the same time. The phonons then dissipate the energy with the  
 438 sample and through layers down to the substrate.



439  
 440 **Figure 16.** The physical process of hot carrier diffusion. Reproduced from [29] with  
 441 permission from The Royal Society of Chemistry.

442 For steady state, the generation and diffusion of heat and hot carriers are governed by two partial  
 443 differential equations. The first one is the carrier diffusion equation to determine the hot carrier  
 444 concentration  $\Delta N(r, t)$  ( $\text{cm}^{-3}$ ):

445  $D\nabla^2\Delta N - \frac{\Delta N}{\tau} + \frac{\partial n_0}{\partial T_{\text{CW}}} \frac{\Delta T_{\text{CW}}}{\tau} + \Phi\alpha = 0, \quad (9)$

446 where  $D$  ( $\text{cm}^2\cdot\text{s}^{-1}$ ) is carrier diffusion coefficient,  $\tau$  (s) is electron-hole recombination time of the  
 447 sample,  $\Phi$  (photons per  $\text{cm}^3$  per s) is incident photon flux of the laser source,  $n_0$  ( $\text{cm}^{-3}$ ) is the  
 448 equilibrium free-carrier density at temperature  $T$ . The second equation is the thermal diffusion  
 449 equation which involves the free carrier density:

450  $\kappa\nabla^2\Delta T_{\text{CW}} + (h\nu - E_g)\Phi\alpha + \frac{E_g\Delta N}{\tau} = 0, \quad (10)$

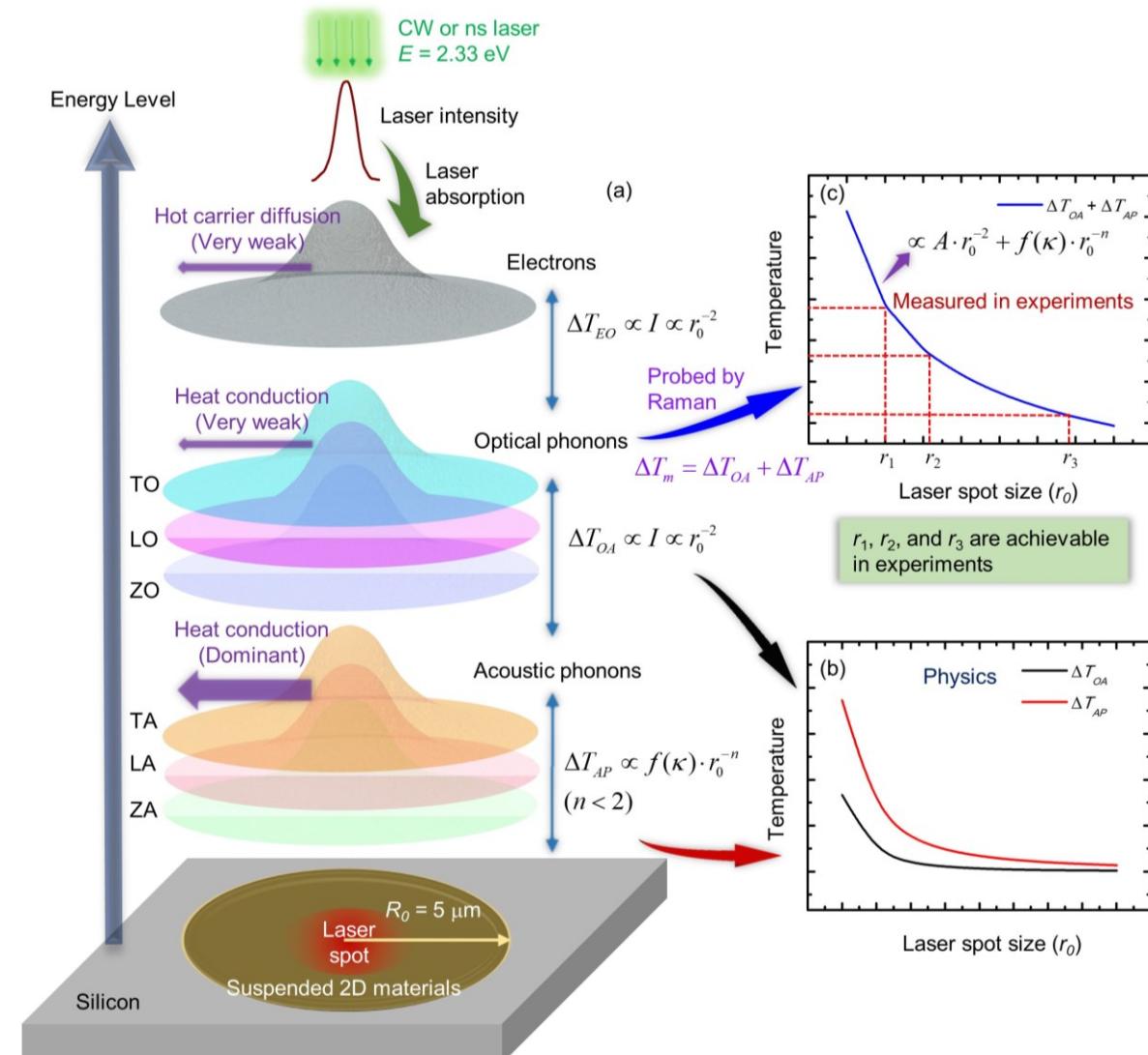
451 where  $\Delta T(r,t)$  (K) and  $E_g$  (eV) are temperature rise and bandgap energy of the sample,  $h\nu$  is photon  
 452 energy of the laser source. Due to the hot carrier diffusion effect, the real heating area will be larger  
 453 than the laser irradiating area, and is highly related to the hot carrier diffusion length ( $L_D = \sqrt{\tau D}$ ).  
 454 As a result, when the laser spot size is large enough, the hot carrier diffusion will have negligible  
 455 effect on the heating area.

456 For transient state, Yuan *et al.* used a picosecond laser to characterize the thermal transport for  
 457 supported samples [32]. The laser pulse (13 ps) is so short that the heat conduction becomes very  
 458 weak. Then, five transport states in both time and space domains are constructed.  $\kappa$  and  $R$  values are  
 459 determined by taking  $D$  into consideration. Zobeiri *et al.* used a nanosecond laser to study the thermal  
 460 transport for suspended samples [34]. Three transport states in both time and space domains are  
 461 constructed.  $\kappa$  of the suspended sample is determined by taking  $D$  into consideration. As shown in  
 462 Figure 15 (a), due to the large laser spot size under  $20\times$  objective lens, the effect of  $D$  on  $\kappa$  of the  
 463 sample is very tiny. While under  $100\times$  objective lens, shown in Figure 15 (b), due to the relative small  
 464 laser spot size, the effect of  $D$  cannot be neglected.

## 465 6. Probing of Thermal Nonequilibrium among Phonon Branches

466 The physical process happening inside different Raman-based methods consists of energy  
 467 transfer among photons, electrons, and phonons. For phonons, three optical branches, which are  
 468 longitudinal optical (LO), transverse optical (TO), and flexural optical (ZO) branches, are included.  
 469 Similarly, there are also three acoustic branches (LA, TA, and ZA). And the temperatures of these  
 470 branches are at nonequilibrium under laser excitation. ZA phonons are the main heat carriers in the  
 471 heat conduction process, while optical phonons are the ones probed by Raman spectroscopy. Thus,  
 472 neglect of nonequilibrium between ZA phonons and optical phonons can induce significant  
 473 underestimation of thermal conductivity. Wang *et al.* designed and employed a nanosecond ET-  
 474 Raman technique to explore the temperature nonequilibrium among different phonon branches [35].

475 Figure 17(a) shows the energy transfer process among different energy carriers. Optical phonons  
 476 (OP) receive energy from hot carriers, and will have a prominent temperature rise. Then, OP will  
 477 transfer majority of the energy to acoustic phonons (AP) through energy coupling. For the  
 478 temperature difference between OP and AP, we have  $\Delta T_{\text{OA}} \propto I \propto r_0^{-2}$ , where  $I$  and  $r_0$  are the laser  
 479 energy and radius of laser spot. And the temperature rise of AP ( $\Delta T_{\text{AP}}$ ) is related to both  $r_0$  and  $\kappa$ , we  
 480 have  $\Delta T_{\text{AP}} \propto f(\kappa) \cdot r_0^{-n}$  with  $n < 2$ . As shown in Figure 17(b), with the increase of laser spot size,  $\Delta T_{\text{OA}}$   
 481 decreases to zero faster than  $\Delta T_{\text{AP}}$ , which indicates that the effect of energy coupling between OP  
 482 and AP is negligible under very large laser spot. In Raman-based techniques, as shown in Figure 17  
 483 (c) the temperature rise of OP, which can be expressed as  $\Delta T_m = \Delta T_{\text{OA}} + \Delta T_{\text{AP}} \propto Ar_0^{-2} + f(\kappa) \cdot r_0^{-n}$ , is  
 484 probed under different laser spot size. Afterwards, the percentages of  $\Delta T_{\text{OA}}$  and  $\Delta T_{\text{AP}}$  in  $\Delta T_m$  are  
 485 determined.



486

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491

**Figure 17.** (a) The energy transfer process among different energy carriers in 2D materials under laser irradiation. (b) The temperature difference between optical phonons and acoustic phonons against laser spot size. (c) The determination of thermal conductivity and energy coupling coefficient between optical phonons and acoustic phonons [35]. Figure reproduced with permission from John Wiley and Sons.

492

493

494

In nanosecond ET-Raman experiments, the measured  $\psi$  values are linearly related to Raman intensity weighted temperature rise of the sample. The Raman intensity weighted temperature rise measured under steady state can be written as:

495

$$\Delta \bar{T}_{\text{m}} \Big|_{\text{CW}} = \Delta \bar{T}_{\text{AP}} \Big|_{\text{CW}} + \frac{1}{3} \cdot \frac{I_0}{\tau_L} \cdot \frac{\delta}{G_{\text{pp}} \Big|_{\text{CW}}}, \quad (11)$$

496

497

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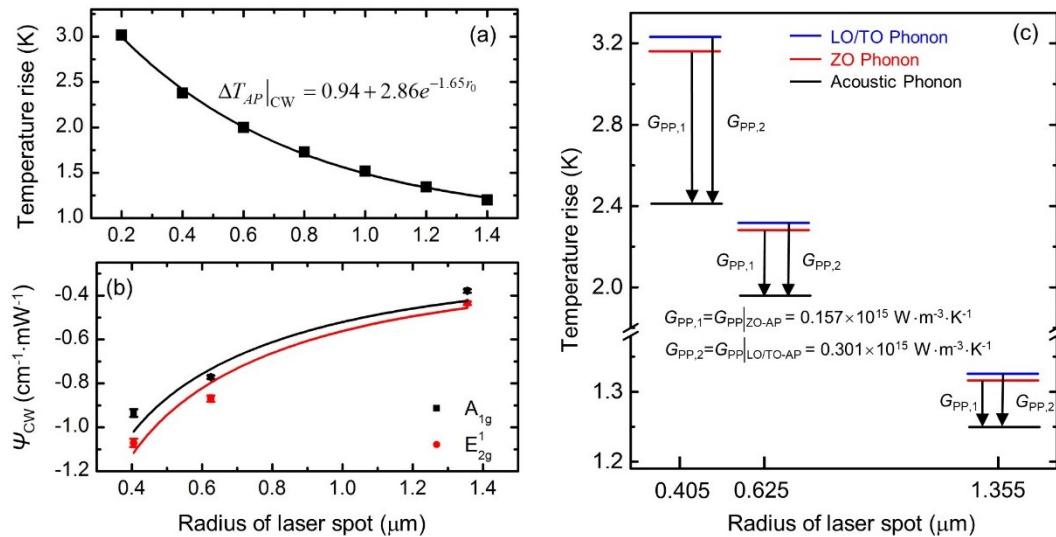
500

where  $G_{\text{pp}} \Big|_{\text{CW}}$  is the energy coupling factor between OP and AP,  $I_0$  is the absorbed laser power per unit area at the center of laser spot,  $\tau_L$  is the laser absorption depth, and  $\delta$  ( $0 < \delta < 1$ ) is portion of laser energy transferred from the measured Raman mode optical phonons to acoustic phonons. Figure 18 (a) shows the variation of  $\Delta \bar{T}_{\text{AP}} \Big|_{\text{CW}}$  against laser spot size using a 3D numerical modeling for the 55 nm thick MoS<sub>2</sub>. Based on this, the relation between  $\psi_{\text{CW}}$  and  $\Delta \bar{T}_{\text{m}} \Big|_{\text{CW}}$  can be expressed as:

501

$$\psi_{\text{CW}} = A \cdot \left[ (0.94 + 2.86e^{-1.65r_0}) + \frac{1}{3} \cdot \frac{P}{\pi r_0^2 \tau_L} \cdot \frac{\delta}{G_{\text{pp}} \Big|_{\text{CW}}} \right] / P, \quad (12)$$

502 where  $A$  is determined by Raman shift temperature coefficient and laser absorption,  $P$  is the laser  
 503 power,  $r_0$  is the radius of laser spot. Figure 18 (b) shows the  $\psi_{CW}$  values under three objective lenses,  
 504 and Equation (12) is used to obtain  $\psi_{CW} \sim r_0$  fitting curve. Then, the energy coupling factors between  
 505 OP and AP for the two Raman modes under steady state are determined as  $0.301 \times 10^{15} \text{ W} \cdot \text{m}^{-3} \cdot \text{K}^{-1}$  for  
 506  $E_{2g}^1$  mode and  $0.157 \times 10^{15} \text{ W} \cdot \text{m}^{-3} \cdot \text{K}^{-1}$  for  $A_{1g}$  mode. Afterwards, the percentages of  $\Delta T_{OA}$  and  $\Delta T_{AP}$   
 507 can be distinguished, and the temperatures of LO/TO phonon, ZO phonon, and AP are obtained,  
 508 shown in Figure 18 (c). Specifically, the temperature difference between OP and AP takes more than  
 509 25% of the measured temperature rise under a small laser spot size. Thus,  $\Delta T_{OA}$  cannot be neglected  
 510 when a small laser spot is used.



511  
 512 **Figure 18.** Determination of coupling factor of  $\text{MoS}_2$  under steady state. (a) Temperature  
 513 rise of acoustic phonons obtained from simulation. (b) Experimental values and fitting  
 514 curves of  $\psi_{CW}$  against laser spot size. (c) Distinct temperatures of different phonon branches  
 515 [35]. Figure reproduced with permission from John Wiley and Sons.

516 However, for the FR-Raman and TD-Raman, this effect is ruled out since they only use the  
 517 Raman shift change versus modulation frequency. The phonon branch temperature difference is a  
 518 constant and has no effect in the physical data processing. Also in other techniques, like the TET  
 519 technique, the phonon branch temperature difference is negligible. In TET, we fit the trend of the  
 520 temperature change against time to determine the thermal diffusivity, then determine the thermal  
 521 conductivity. The electrons-OP and OP-AP temperature difference will only add a constant value on  
 522 the AP temperature, and does not affect the fitting results. Note in the TET technique, since the  
 523 heating is over the whole sample and the inter-phonon branch heat current is significantly lower than  
 524 the laser intensity in this work, the electron temperature is very close to that of the AP and their  
 525 temperature difference is negligible compared with the measured temperature rise. The temperature  
 526 difference between electron and AP can be calculated by  $T_e - T_{AP} = I^2 RV^{-1} \left[ \left( \sum G_{ep} \right)^{-1} + \left( \sum G_{pp} \right)^{-1} \right]$

527 , where  $I$  is the current flowing through the sample,  $R$  is its resistance at steady state,  $V$  is the volume  
 528 of the sample,  $G_{ep}$  is the coupling factor between electrons and OP. As there are three phonon  
 529 branches for both OP and AP, here the sums of all the corresponding coupling factors are used in the  
 530 calculation. For instance, the in-plane thermal conductivity of graphene paper is obtained as  $634 \text{ W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$  using the TET technique. The length, width, and thickness of the sample are around 17 mm, 0.28  
 531 mm, and 28.6  $\mu\text{m}$ , respectively [36]. Then, based on the coupling factors, the temperature difference  
 532 between electrons and AP is calculated to be around  $2.8 \times 10^{-8} \text{ K}$ , which is negligible compared with a  
 533 measured temperature rise of 2 K [35, 37].

535 

## 7. Concluding Remarks and Outlooks

536 As Raman spectroscopy can be used to characterize the energy and charge transport in 2D  
 537 materials, many different Raman-based techniques have been developed over the last decade. Steady  
 538 state Raman can be used to measure the thermal conductivity and interface thermal resistance.  
 539 However, both temperature calibration and laser absorption measurement, which induce large  
 540 errors, are needed. To overcome this drawback, techniques involving time resolving, which include  
 541 TD-Raman and FR-Raman, are proposed. For TD-Raman, it is not appropriate for studying very fast  
 542 thermal transport phenomena. Though FR-Raman can be used for fast thermal transport, a large  
 543 number of measurements under different frequencies are required for the data fitting process. Then,  
 544 FET-Raman technique, with a fixed frequency, was developed to characterize the thermal properties  
 545 by studying the Raman shift change against laser power.

546 For all the Raman-based techniques mentioned above, the hot carrier diffusion effect is not  
 547 considered. By constructing different energy transport states in both time and space domains, ET-  
 548 Raman techniques are proposed. For supported samples, a picosecond laser and a CW laser are  
 549 combined to realize the simultaneous measurement of  $\kappa$ ,  $D$ , and  $R$ . To reduce the heat accumulation  
 550 effects in suspended samples, a nanosecond laser and a CW laser are used together to measure  $\kappa$  and  
 551  $D$ . As all Raman-based techniques share the similar energy transport process, the neglect of  
 552 temperature nonequilibrium among different energy carriers can also introduce errors in the thermal  
 553 property characterization. The nanosecond ET-Raman technique is further developed to study the  
 554 energy coupling between OP and AP. The corresponding coupling factors are determined, and a  
 555 much more accurate thermal conductivity is also obtained. This breakthrough is expected to move  
 556 the Raman-based energy transport probing to an unprecedented level.

557 In summary, Raman-based techniques show excellent suitability and performance in  
 558 characterizing the energy and charge transport of 2D materials. Additionally, since 2D materials are  
 559 extremely thin, the beam scattering techniques (e.g. XRD) cannot obtain sound diffraction signal and  
 560 determine the in-plane lattice size. On the other hand, using thermal diffusivity ( $\alpha$ ) measured by  
 561 Raman spectroscopy, we can measure the thermal diffusivity at different temperatures. Then by  
 562 using the thermal reffusivity theory, we can extend to obtain the thermal reffusivity at the 0 K limit,  
 563 and obtain the structure domain size. The thermal reffusivity model of phonons is expressed as:

$$564 \quad \Theta = \frac{1}{\alpha} = \frac{3}{v^2} \left( \frac{1}{\tau_{\text{phonon}}} + \frac{1}{\tau_{\text{defect}}} \right) = \Theta_0 + C \cdot e^{-B/T}, \quad (13)$$

565 where  $v$  is the average group velocity,  $\tau_{\text{phonon}}$  and  $\tau_{\text{defect}}$  are the electron-phonon scattering time and  
 566 defect scattering time, respectively.  $\Theta_0$  is the thermal reffusivity at the 0 K limit, and is entitled as  
 567 residual thermal reffusivity,  $B$  is a constant proportional to the material's Debye temperature. Based  
 568 on Equation (13),  $\Theta$  decreases with the decrease of temperature and reaches  $\Theta_0$  at the 0 K limit. **And**  
 569 **the defect scattering intensity from grain boundary, lattice imperfections, chemical impurities, rough**  
 570 **edges, and amorphous structures, etc. can be reflected by  $\Theta_0$ .** In addition, the lattice vibration also  
 571 weakens and the phonon population decreases as temperature goes down. From Equation (13),  $\Theta_0$   
 572 can be written as  $\Theta_0 = 3 / (v l_0)$ , where  $l_0$  is the mean free path limited by defect scattering.  $l_0$  is called  
 573 structure thermal domain size, which is actually an effective domain size combining the effect from  
 574 three-dimensional crystallite [38-40].

575 During Raman scattering of 2D materials, the intensity in fact reflects some critical properties of  
 576 the 2D materials, like electron excitation energy and interface spacing [22]. In TMDs, based on the  
 577 light scattering theory and time-dependent perturbation theory, the Raman intensity can be written  
 578 as:

$$579 \quad I \propto \left| \frac{1}{[E(T) - E_i - i\Gamma(T)][E(T) - E_s - i\Gamma(T)]} \right|^2, \quad (14)$$

580 where  $E(T)$  and  $\Gamma(T)$  are exciton's temperature dependent transition energies and damping constants,  
 581 respectively.  $E_i$  and  $E_s$  are the energy of incident and scattered lights. Based on this equation, the  
 582 sample temperature will affect electronic band structure, and the corresponding Raman intensity will

583 then be influenced. In addition, the optical properties of the sample and their variation with  
584 temperature also affect the Raman intensity. For supported samples, there is an interface spacing  
585 between the sample and the substrate. The Raman intensity is altered due to the multi-reflections in  
586 this spacing air gap layer. Thus, the interpretation of temperature dependent Raman intensity should  
587 take all the factors above into consideration, and it is a critical direction that needs to be explored.

588 Raman-based techniques are also widely used for exploring the thermal properties of monolayer  
589 2D materials. Guo *et al.* measured the thermal conductivity of strained monolayer graphene by using  
590 optothermal Raman method [41]. Cai *et al.* measured the thermal conductivity and thermal expansion  
591 coefficient of suspended monolayer boron nitride by using optothermal Raman method [42]. Yalon  
592 *et al.* measured the temperature-dependent thermal boundary conductance of monolayer MoS<sub>2</sub> with  
593 AlN and SiO<sub>2</sub> using Raman thermometry technique [43]. However, the radiative electron-hole  
594 recombination effect, which significantly affects the measurement accuracy, is not considered in  
595 current Raman-based techniques. Further work should consider this effect and significantly advance  
596 the understanding.

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598 searches and studies; D.L. and X.W. conceived and revised the paper. All authors have read and agreed to the  
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