



JCMT BISTRO Survey Observations of the Ophiuchus Molecular Cloud: Dust Grain Alignment Properties Inferred Using a Ricean Noise Model

Kate Pattle^{1,2}, Shih-Ping Lai^{1,3}, Tetsuo Hasegawa², Jia-Wei Wang¹, Ray S. Furuya⁴, Derek Ward-Thompson⁵, Pierre Bastien⁶, Simon Coudé⁷, Chakali Eswaraiah^{8,9}, Lapo Fanciullo³, James di Francesco^{10,11}, Thiem Hoang^{12,13}, Gwanjeong Kim¹⁴, Woojin Kwon^{12,13}, Chang Won Lee^{12,13}, Sheng-Yuan Liu³, Tie Liu^{12,15}, Masafumi Matsumura¹⁶, Takashi Onaka^{17,18}, Sarah Sadavoy¹⁹, and Archana Soam⁷

¹ Institute for Astronomy and Department of Physics, National Tsing Hua University, Hsinchu 30013, Taiwan; kpattle@gapp.nthu.edu.tw

² National Astronomical Observatory of Japan, National Institutes of Natural Sciences, Osawa, Mitaka, Tokyo 181-8588, Japan

³ Academia Sinica Institute of Astronomy and Astrophysics, P.O. Box 23-141, Taipei 10617, Taiwan

⁴ Institute of Liberal Arts and Sciences, Tokushima University, Minami Jousanajima-machi 1-1, Tokushima 770-8502, Japan

⁵ Jeremiah Horrocks Institute, University of Central Lancashire, Preston PR1 2HE, UK

⁶ Centre de recherche en astrophysique du Québec & département de physique, Université de Montréal, C.P. 6128 Succ. Centre-ville, Montréal, QC, H3C 3J7, Canada

⁷ SOFIA Science Center, Universities Space Research Association, NASA Ames Research Center, Moffett Field, CA 94035, USA

⁸ CAS Key Laboratory of FAST, National Astronomical Observatories, Chinese Academy of Sciences, People's Republic of China

⁹ National Astronomical Observatories, Chinese Academy of Sciences, Datun Road, Chaoyang District, Beijing 100101, People's Republic of China

¹⁰ NRC Herzberg Astronomy and Astrophysics, 5071 West Saanich Road, Victoria, BC V9E 2E7, Canada

¹¹ Department of Physics and Astronomy, University of Victoria, Victoria, BC V8W 2Y2, Canada

¹² Korea Astronomy and Space Science Institute (KASI), 776 Daedeokdae-ro, Yuseong-gu, Daejeon 34055, Republic of Korea

¹³ University of Science and Technology, Korea (UST), 217 Gajeong-ro, Yuseong-gu, Daejeon 34113, Republic of Korea

¹⁴ Nobeyama Radio Observatory, National Astronomical Observatory of Japan, National Institutes of Natural Sciences, Nobeyama, Minamimaki, Minamisaku, Nagano 384-1305, Japan

¹⁵ East Asian Observatory, 660 North A'ohōkū Place, University Park, Hilo, HI 96720, USA

¹⁶ Faculty of Education and Center for Educational Development and Support, Kagawa University, Saiwai-cho 1-1, Takamatsu, Kagawa, 760-8522, Japan

¹⁷ Department of Astronomy, Graduate School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan

¹⁸ Faculty of Science and Engineering, Meisei University, 2-1-1 Hodokubo, Hino, Tokyo 191-856, Japan

¹⁹ Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA

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Abstract

The dependence of the polarization fraction p on total intensity I in polarized submillimeter emission measurements is typically parameterized as $p \propto I^{-\alpha}$ ($\alpha \leq 1$) and used to infer dust grain alignment efficiency in star-forming regions, with an index $\alpha = 1$ indicating near-total lack of alignment of grains with the magnetic field. In this work, we demonstrate that the non-Gaussian noise characteristics of the polarization fraction may produce apparent measurements of $\alpha \sim 1$ even in data with significant signal-to-noise in Stokes Q , U , and I emission, and so with robust measurements of polarization angle. We present a simple model demonstrating this behavior and propose a criterion by which well-characterized measurements of the polarization fraction may be identified. We demonstrate that where our model is applicable, α can be recovered by fitting the p - I relationship with the mean of the Rice distribution without statistical debiasing of the polarization fraction. We apply our model to JCMT BISTRO Survey POL-2 850 μm observations of three clumps in the Ophiuchus molecular cloud, finding that in the externally illuminated Oph A region, $\alpha \approx 0.34$, while in the more isolated Oph B and C, despite their differing star formation histories, $\alpha \approx 0.6$ – 0.7 . Our results thus suggest that dust grain alignment in dense gas is more strongly influenced by the incident interstellar radiation field than by star formation history. We further find that grains may remain aligned with the magnetic field at significantly higher gas densities than has previously been believed, thus allowing investigation of magnetic field properties within star-forming clumps and cores.

Key words: dust, extinction – ISM: magnetic fields – submillimeter: ISM – stars: formation – techniques: polarimetric

1. Introduction

The role of magnetic fields in the star formation process is not well understood (e.g., Crutcher 2012). Observations of magnetic field morphologies in the densest parts of molecular clouds are typically performed indirectly through submillimeter dust polarization observations (e.g., Matthews et al. 2009). In low-density, well-illuminated environments in the interstellar medium (ISM), dust grains are expected to be aligned with their minor axes parallel to the local magnetic field direction (Davis & Greenstein 1951). However, at sufficiently high optical depths, grains are expected to become less efficiently aligned with the magnetic field (Andersson et al. 2015). Recent results have suggested that this occurs at a visual extinction

$A_V \sim 20$ – 30 mag (Whittet et al. 2008; Alves et al. 2014; Jones et al. 2015). This inferred break in behavior is, in each case so far reported, coincident with a change in tracer from optical/near-infrared extinction polarimetry to submillimeter dust emission polarimetry (Andersson et al. 2015; Jones et al. 2015). Submillimeter emission polarimetry is the only effective wide-area tracer of ISM polarization in dense molecular clouds ($A_V \gtrsim 30$ mag) where stars are forming. It is thus vital to studies of the role of magnetic fields in star formation to know which gas densities are being traced by dust polarization observations.

A commonly used method of assessing the alignment of grains is to determine the relationship between polarization efficiency and visual extinction (Whittet et al. 2008; Alves et al. 2014;

Jones et al. 2015, 2016). In submillimeter studies, this is generally treated as a relationship between the polarization fraction p and total submillimeter intensity I , as polarization efficiency is identical to the polarization fraction for optically thin emission (Alves et al. 2015), and the optically thin submillimeter total intensity is proportional to the visual extinction A_V for a given temperature (see Jones et al. 2015; Santos et al. 2017). Recent comparisons between p and submillimeter dust opacity measurements (an alternative proxy for A_V) suggest that the standard assumption in polarization studies of $I \propto A_V$ is likely to be too simplistic (Juvela et al. 2018). However, regardless of the exact nature of the relationship between I and A_V , an accurate measurement of the p - I relationship is required in order to interpret dust grain alignment properties.

It is expected that observations of dense material within molecular clouds will show a power-law dependence of p on I , $p \propto I^{-\alpha}$ (Whittet et al. 2008). This index is expected to steepen as grains become increasingly poorly aligned with the magnetic field: an index of $\alpha = 0$ would indicate equal grain alignment at all optical depths, an index of $\alpha = 0.5$ is predicted for a cloud in which grain alignment decreases linearly with increasing optical depth, while an index of $\alpha = 1$ is predicted for an environment in which all observed polarized emission is produced in a thin layer at the surface of the cloud, and grains at higher densities have no preferred alignment relative to the magnetic field (see Whittet et al. 2008; Jones et al. 2015).

Several recent studies of molecular clouds and starless cores have found power-law indices α in the range 0.5–1, for example, $\alpha = 0.7$ in OMC-3 and 0.8 in Barnard 1 (Matthews & Wilson 2000), 0.64 ± 0.01 in CB 54 and 0.55 ± 0.22 in DC 253-1.6 (Henning et al. 2001), 0.83 ± 0.01 in NGC 2024 FIR 5 (Lai et al. 2002), 0.92 ± 0.17 in Pipe 109 (Alves et al. 2014, 2015), 0.84 – 1.02 in W51 (Koch et al. 2018), 1.0 in FeSt 1-457 (Kandori et al. 2018), 0.7 or 0.8 in Oph A (Kwon et al. 2018), 0.9 in Oph B (Soam et al. 2018), and 1.0 in Oph C (Liu et al. 2019). (Note that a larger value of α indicates a steeper negative slope.) In most of these cases, the data used have been selected to have a signal-to-noise ratio (S/N) ≥ 3 in some combination of polarization fraction, polarized intensity, and total intensity. Recent improvements in instrumental sensitivity have allowed more stringent selection criteria: some recent observations have employed an S/N cut of 20 in total intensity (Kwon et al. 2018; Soam et al. 2018). These results have generally been taken to suggest poor grain alignment within the densest parts of molecular clouds.

Polarized intensity and polarization fraction are both constrained to be positive quantities and so are characterized by Ricean statistics (Rice 1945; Serkowski 1958), albeit approximately so in the case of the polarization fraction, as discussed below. This results in a strong positive bias in the measured polarization fraction at low total intensities. Several methods of correcting for this bias have been proposed, of varying levels of sophistication (Wardle & Kronberg 1974; Simmons & Stewart 1985; Vaillancourt 2006; Quinn 2012; Montier et al. 2015a, 2015b; Vidal et al. 2016; Müller et al. 2017). These methods are collectively known as (statistical) debiasing. An alternative approach is to bypass the problem of characterizing the polarization fraction by working with the Stokes parameters of the observed polarized emission directly (e.g., Herron et al. 2018). The Rice distribution is discussed extensively in the electrical engineering literature due to its relevance to signal processing (e.g., Lindsey 1964; Sijbers et al. 1998; Abdi et al. 2001).

In this work, we investigate the extent to which measurements of the p - I index are biased by the statistical behavior of the polarization fraction and choice of selection criteria. We demonstrate a method by which the relationship between p and I can be accurately characterized using the full observed data set without recourse to statistical debiasing.

The L1688 region of the Ophiuchus molecular cloud is a nearby (138.4 ± 2.6 pc; Ortiz-León et al. 2018) site of low-to-intermediate-mass star formation (Wilking et al. 2008). The region contains a number of dense clumps, Oph A–F, notable for their differing properties and star formation histories (Motte et al. 1998; Pattle et al. 2015). The Oph A, B, and C clumps have been observed with the James Clerk Maxwell Telescope (JCMT) POL-2 polarimeter as part of the JCMT B-fields in Star-forming Region Observations (BISTRO) survey (Ward-Thompson et al. 2017; Kwon et al. 2018; Soam et al. 2018; Liu et al. 2019). We apply the methods developed in this paper to the JCMT BISTRO survey observations of L1688.

This paper is structured as follows. In Section 2 we present the key equations governing the behavior of the polarization fractions. In Section 3, we present a simple model for the behavior of the polarization fraction as a function of S/N. In Section 4 we present Monte Carlo simulations demonstrating the behavior of our model and testing various fitting methods to recover the underlying relationship between polarization fraction and total intensity. In Section 5, we apply our model to recent JCMT POL-2 observations of the Ophiuchus molecular cloud. Section 6 summarizes our results.

2. Mathematical Properties of the Polarization Fraction

Linearly polarized intensity is given by

$$P = \sqrt{Q^2 + U^2}, \quad (1)$$

where Q is the Stokes Q intensity and U is the Stokes U intensity. We do not consider circular polarization here, and so we assume the Stokes V intensity to be zero throughout. The polarization fraction, the ratio of polarized intensity P to total intensity I , is given by

$$p = \frac{\sqrt{Q^2 + U^2}}{I}. \quad (2)$$

We take measurements of Stokes I , Q , and U to have measurement errors of δI , δQ , and δU , respectively. We assume that these measurement uncertainties are drawn from Gaussian distributions of width σ_I , σ_Q , and σ_U .

Note that all symbols defined and used in this work are summarized in Table 3 in the Appendix.

2.1. The Rice Distribution

Polarized intensity—the result of the addition in quadrature of real numbers, as shown in Equation (1)—must be a positive quantity. The addition in quadrature of small values of Q and U , with measurement uncertainties δQ and δU will produce spurious measurements of polarized intensity where $\delta Q \gtrsim |Q|$ and $\delta U \gtrsim |U|$ produce spurious measurements of polarized intensity. The results of such an addition in quadrature are described mathematically by the Rice distribution (Rice 1945), where the quantities under addition have noise properties that are Gaussian and uncorrelated. In principle, we can expect the uncertainties on Stokes Q and U to be independent, as Q and U

are orthogonal components of the Stokes polarization vector (see, e.g., Herron et al. 2018). We discuss the validity of this assumption in the specific case of JCMT POL-2 observations in Section 5.

The Rice distribution has positive skewness at low S/N, while at high S/N, it tends toward a Gaussian distribution (Rice 1945). Assuming that the Stokes Q and U data have independent Gaussian measurement uncertainties, polarized intensities derived using Equation (1) will be Rice-distributed (Wardle & Kronberg 1974; Simmons & Stewart 1985).

As the distributions of the observed values of the polarized intensity, and so of the polarization fraction, are different from the underlying distributions that would be seen in the absence of measurement error, we henceforth denote the observed values of the polarized intensity and polarization fraction as P' and p' , respectively.

The division $p' = P'/I$ (see Equation (2)) can, at low S/N (where I is small and P' may be artificially large), produce artificially high values of p' . If $P'/\delta P \ll I/\delta I$, as is generally the case, as $p \ll 1$ in physically realistic situations, the effect of the measurement error on I on the distribution of p' will be minimal, so p' will also be approximately Rice-distributed (see Simmons & Stewart 1985).

If the polarization fractions that we measure can be treated as being Rice-distributed, the probability of measuring a polarization fraction p' given a true polarization fraction p and an rms uncertainty in polarization fraction σ_p (the probability density function) is

$$\text{PDF}_{\text{Rice}}(p'|p) = \frac{p'}{\sigma_p^2} \exp\left(-\frac{p'^2 + p^2}{2\sigma_p^2}\right) \mathcal{I}_0\left(\frac{p'p}{\sigma_p^2}\right), \quad (3)$$

where \mathcal{I}_0 is the zeroth-order modified Bessel function (Simmons & Stewart 1985). See Montier et al. (2015a) for a derivation of this result (see also Bastien et al. 2007; Hull & Plambeck 2015).

The mean of the Rice distribution is given by

$$\mu_p = \sqrt{\frac{\pi}{2}} \sigma_p \mathcal{L}_{\frac{1}{2}}\left(-\frac{p^2}{2\sigma_p^2}\right), \quad (4)$$

where $\mathcal{L}_{\frac{1}{2}}$ is a Laguerre polynomial of order $\frac{1}{2}$,

$$\begin{aligned} \mathcal{L}_{\frac{1}{2}}\left(-\frac{p^2}{2\sigma_p^2}\right) &= e^{-\frac{p^2}{4\sigma_p^2}} \left[\left(1 + \frac{p^2}{2\sigma_p^2}\right) \mathcal{I}_0\left(\frac{p^2}{4\sigma_p^2}\right) \right. \\ &\quad \left. + \frac{p^2}{2\sigma_p^2} \mathcal{I}_1\left(\frac{p^2}{4\sigma_p^2}\right) \right], \end{aligned} \quad (5)$$

and \mathcal{I}_0 and \mathcal{I}_1 are modified Bessel functions of order zero and 1, respectively.

We note that approximating p' as Rice-distributed is a statement that I is perfectly known, and so is equivalent to setting its rms uncertainty $\sigma_I = 0$. We will demonstrate in Section 4 that Equation (3) describes synthetic data with realistic noise properties sufficiently well to justify making this assumption.

Having chosen to treat I as perfectly known, if the measurement uncertainties on Q and U are equivalent, i.e., $\sigma_Q = \sigma_U$, then σ_p will be given by

$$\sigma_p = \frac{\sigma_Q}{I} = \frac{\sigma_U}{I} \quad (6)$$

(see Equation (2)). This approximation is discussed by Montier et al. (2015a).

2.2. Debiasing

The correction of the observed polarization fraction p' for the bias described above is known as “debiasing.” A commonly used method for debiasing polarization fractions is the Wardle & Kronberg (1974) estimator (see also Serkowski 1962), under which the debiased observed polarized intensity is given by

$$P'_{\text{db}} = \sqrt{Q^2 + U^2 - \frac{1}{2}(\delta Q^2 + \delta U^2)}. \quad (7)$$

Similarly, the debiased observed polarization fraction is given by

$$p'_{\text{db}} = \frac{\sqrt{Q^2 + U^2 - \frac{1}{2}(\delta Q^2 + \delta U^2)}}{I}. \quad (8)$$

As this is the default debiasing method for POL-2 data (e.g., Kwon et al. 2018), we compare the results of fitting non-debiased data and data debiased using the Wardle & Kronberg (1974) estimator in Section 4. For a detailed comparison of debiasing methods, see Montier et al. (2015b).

2.3. An Aside on Polarization Angle

The polarization angle θ_p is given by

$$\theta_p = \frac{1}{2} \arctan(U, Q). \quad (9)$$

We note that measurements of the polarization angle follow a different probability distribution than those of the polarization fraction (Naghizadeh-Khouei & Clarke 1993). We expect measurements of the polarization angle to be significantly more robust than those of the polarization fraction, as the Q and U distributions have the same statistical properties and thus their ratio is not affected by the issues discussed above. Note also that the polarization angle is not constrained to be positive.

Inference of grain alignment properties from the polarization angle distribution would require at minimum a model of the plane-of-sky magnetic field morphology and an estimate of the fluctuations in magnetic field direction induced by Alfvénic turbulence (Chandrasekhar & Fermi 1953). We therefore do not consider polarization angles in this work.

3. A Simple Model for the Polarization Fraction

We construct a simple model in which the polarization fraction is fully described by

$$p(I) = p_0 \left(\frac{I}{I_0} \right)^{-\alpha}, \quad (10)$$

where p_0 is the polarization fraction at the reference intensity, I_0 . We expect $0 < \alpha \leq 1$ (e.g., Whittet et al. 2008).

The reference intensity, or normalization, I_0 , can be treated as a free parameter of the model. However, we choose to specify $I_0 = \sigma_{QU}$, where σ_{QU} is a single value, with units of intensity, representative of the rms noise in both Stokes Q and U measurements. We thus assume that the Stokes Q and U data sets have identical statistical properties and can be adequately characterized by a single rms noise value. This is a reasonable assumption for recent submillimeter emission polarization measurements, as described in Section 5 below.

By taking $I_0 = \sigma_{QU}$, we assume that the power-law relationship between I and p applies to all measurements above the noise level of the data. Choosing $I_0 = \sigma_{QU}$ allows us to discuss the behavior of our model in terms of a simple S/N criterion, I/σ_{QU} , as demonstrated below. The reference polarization fraction p_0 thus depends on σ_{QU} . In order to emphasize this, we define the polarization fraction at the noise level of the data, $p(I = \sigma_{QU}) = p_{\sigma_{QU}}$; i.e., if $I_0 = \sigma_{QU}$, $p_0 = p_{\sigma_{QU}}$.

In order to meaningfully compare polarization fractions in data sets with different rms noise levels, we must convert $p_{\sigma_{QU}}$ to the polarization fraction at a common reference intensity level. In this work, we choose a reference intensity of $I = 100 \text{ mJy beam}^{-1}$ and so define

$$p_{100 \text{ mJy beam}^{-1}} = p_{\sigma_{QU}} \left(\frac{100 \text{ mJy beam}^{-1}}{\sigma_{QU}} \right)^{-\alpha}. \quad (11)$$

The choice to reference to $100 \text{ mJy beam}^{-1}$ is largely arbitrary but suitable for the JCMT POL-2 data that we consider in Section 5 below, in which $I = 100 \text{ mJy beam}^{-1}$ is both significantly above the rms noise level of the data and below the maximum intensities observed. Note that the JCMT has an effective beam size of $14''.1$ at $850 \mu\text{m}$ (Dempsey et al. 2013).

Equation (10) becomes unphysical where $p(I) > 1$. Moreover, in physically realistic scenarios, we expect $p \lesssim 0.2$ in data with good S/N, as the maximum percentage of polarization observed in the diffuse ISM is $\sim 20\%$ (Planck Collaboration et al. 2015). We thus require that $p < 1$ and expect that $p \lesssim 0.2$ wherever we believe our observed Stokes Q , U , and I values to be reliable.

3.1. Physical Implications of α

If $\alpha = 0$, this implies that the polarized intensity $P = \sqrt{Q^2 + U^2} \propto I$, so $p = p_{\sigma_{QU}}$ everywhere. If polarized intensity is directly proportional to total intensity, this indicates that all emission along each sight line is polarized to the same degree, so there is no variation in polarization efficiency anywhere within the observed cloud.

If $\alpha = 1$, this implies that P does not vary with I ; i.e., a constant amount of polarized emission is observed at all locations in the cloud. This indicates that only a small portion of the total line of sight is contributing polarized emission. This is usually interpreted as a thin layer of polarized emission overlaying an otherwise unpolarized optically thin sight line. This polarized emission is implicitly from low-density material; so, if the higher-density material along the sight line is also polarized, that polarized emission ought to also be detectable. Thus, claiming a physical index of $\alpha = 1$ is essentially a statement that one has observed statistical noise in Stokes Q and U around a constant level of polarized intensity, and that this indicates a genuine absence of polarized emission at high total intensities, rather than insufficient S/N to achieve a detection.

Intermediate values of $0 < \alpha < 1$ indicate a positive relationship, $P \propto I^{1-\alpha}$, in which the total amount of polarized emission increases with, but slower than, total emission. This implies that as the amount of material along the sight line increases, the ability of that material to produce polarized emission decreases (under the assumption of isothermal, optically thin emission). Thus, an index of $0 < \alpha < 1$ indicates that depolarization increases with depth into the cloud.

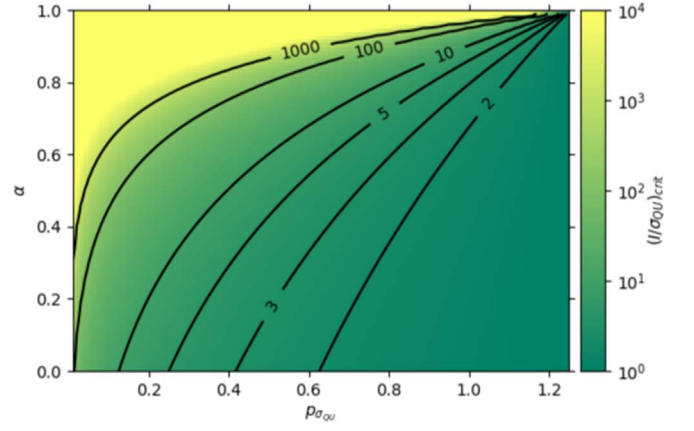


Figure 1. The S/N value $(I/\sigma_{QU})_{\text{crit}}$ at which our model predicts a break in the power-law index as a function of α and $p_{\sigma_{QU}}$, derived using Equation (14). In order to detect and accurately characterize a power-law behavior shallower than $\alpha = 1$, a reasonable number of data points with $(I/\sigma_{QU}) > (I/\sigma_{QU})_{\text{crit}}$ are required. The contours show lines of constant S/N. The color table saturates at $I/\sigma_{QU} = 10^4$. Note that not all combinations of α and $p_{\sigma_{QU}}$ will produce physically plausible results.

3.2. Low-S/N Limit

In the low-S/N limit, the distribution of p' tends to the Rice distribution regardless of the value of α (or p_0 or I_0). In the limit where $p \ll \sigma_p$, $\mathcal{L}_2(-p^2/2\sigma_p) \rightarrow 1$, and therefore $\mu_p \rightarrow \sigma_p \sqrt{\pi/2}$. Taking $\sigma_p = \sigma_{QU}/I$, the behavior of the distribution is well approximated by

$$p' = \sqrt{\frac{\pi}{2}} \left(\frac{I}{\sigma_{QU}} \right)^{-1} \quad (12)$$

at small I . Thus, at low S/N, $p' \propto I^{-1}$, regardless of the true value of α .

In the no-signal case ($p_{\sigma_{QU}} = 0$; $Q = U = 0$), Equation (12) characterizes the observed signal at all values of I . Thus, in the absence of a true measurement, $p' \propto I^{-1}$ behavior will be observed.

3.3. High-S/N Limit

In the high-S/N limit, the distribution of p' tends toward a Gaussian distribution around the true value,

$$p' = p_{\sigma_{QU}} \left(\frac{I}{\sigma_{QU}} \right)^{-\alpha}. \quad (13)$$

3.4. S/N Criterion

Equations (12) and (13) suggest that, for $\alpha < 1$, the underlying power-law dependence of p on I will be observable when

$$\frac{I}{\sigma_{QU}} > \left(\frac{I}{\sigma_{QU}} \right)_{\text{crit}} = \left(\frac{1}{p_{\sigma_{QU}} \sqrt{\pi/2}} \right)^{\frac{1}{1-\alpha}}. \quad (14)$$

At S/Ns below this critical value, the artificial $p' \propto I^{-1}$ behavior will dominate, and the true value of α will not be recoverable.

Figure 1 shows solutions of Equation (14) for the critical S/N value $(I/\sigma_{QU})_{\text{crit}}$ above which the true power-law behavior

(i.e., the true value of α) would be recoverable. It is apparent that significant S/N is required to distinguish a power-law behavior with a steep value of α from instrumental noise.

4. Monte Carlo Simulations

In order to test the accuracy of our interpretation of the model described above, we performed a set of Monte Carlo simulations.

We investigated values of α in the range $0 \leq \alpha \leq 1$. In each case, we took $p_{100 \text{ mJy beam}^{-1}} = 0.025$ (i.e., emission is intrinsically 2.5% polarized at $I = 100.0$; intensity units are arbitrary but chosen to mimic POL-2 data, which are calibrated in mJy beam $^{-1}$). This value of $p_{100 \text{ mJy beam}^{-1}}$ was chosen for its similarity to the POL-2 observations. We then calculated the appropriate value of $p_{\sigma_{QU}}$ for our chosen α and $p_{100 \text{ mJy beam}^{-1}}$ using Equation (11).

As we are not concerned with polarization angles in this work, we choose for simplicity that Stokes $U = 0$ ($\theta_p = 0^\circ$, implying that the underlying magnetic field is uniform and oriented 90° east of north), and so Equation (10) is equivalent to

$$Q(I) = p(I) \times I = p_{\sigma_{QU}} \sigma_{QU}^\alpha I^{1-\alpha}. \quad (15)$$

We drew a set of 10^3 randomly distributed $\log_{10}(I/\sigma_{QU})$ values in the range $0 < \log_{10}(I/\sigma_{QU}) < 3$ (thus assuming that low-S/N values of I are more probable). We drew measurement errors ΔQ and ΔU on Stokes Q and U from Gaussian distributions of equal (fixed) width, σ_{QU} , and ΔI on Stokes I from a Gaussian distribution of (fixed) width σ_I . We here chose $\sigma_{QU} = \sigma_I = 5.0$ (arbitrary units). Equations (3) and (4) assume that the effect of σ_I on the distribution of p is negligible. We wished to test whether that approximation is valid in observations where the noise on Stokes I is comparable to that on Stokes Q and U .

The “observed” values Q_{obs} , U_{obs} , and I_{obs} were then, for the i th value,

$$Q_{\text{obs},i} = Q_i + \Delta Q_i, \quad (16)$$

$$U_{\text{obs},i} = \Delta U_i, \quad (17)$$

and

$$I_{\text{obs},i} = I_i + \Delta I_i. \quad (18)$$

“Observed” values of p' and p'_{db} were calculated using Equations (2) and (8), respectively, for a given value of $p_{\sigma_{QU}}$. We repeated this process 10^4 times.

Figure 2 shows a single realization of our Monte Carlo simulations for three cases: $\alpha = 1$, 0.5, and 0 (constant polarization fraction). In all cases, $p_{100 \text{ mJy beam}^{-1}} = 0.025$. The results are shown without any debiasing of the polarization fraction and colored according to their S/N in I and p' .

Figure 2 shows that where $I/\sigma_{QU} < (I/\sigma_{QU})_{\text{crit}}$, the distribution shows an identical $p' \propto I^{-1}$ behavior in all cases, and that the underlying power-law behavior does not dominate over the I^{-1} dependence until $I/\sigma_{QU} \gg (I/\sigma_{QU})_{\text{crit}}$. Thus, unless a reasonable number of data points have S/Ns significantly greater than the critical value, the true power-law behavior is not recoverable. The overall behavior of the recovered polarization fraction is well described by the mean of the Rice distribution.

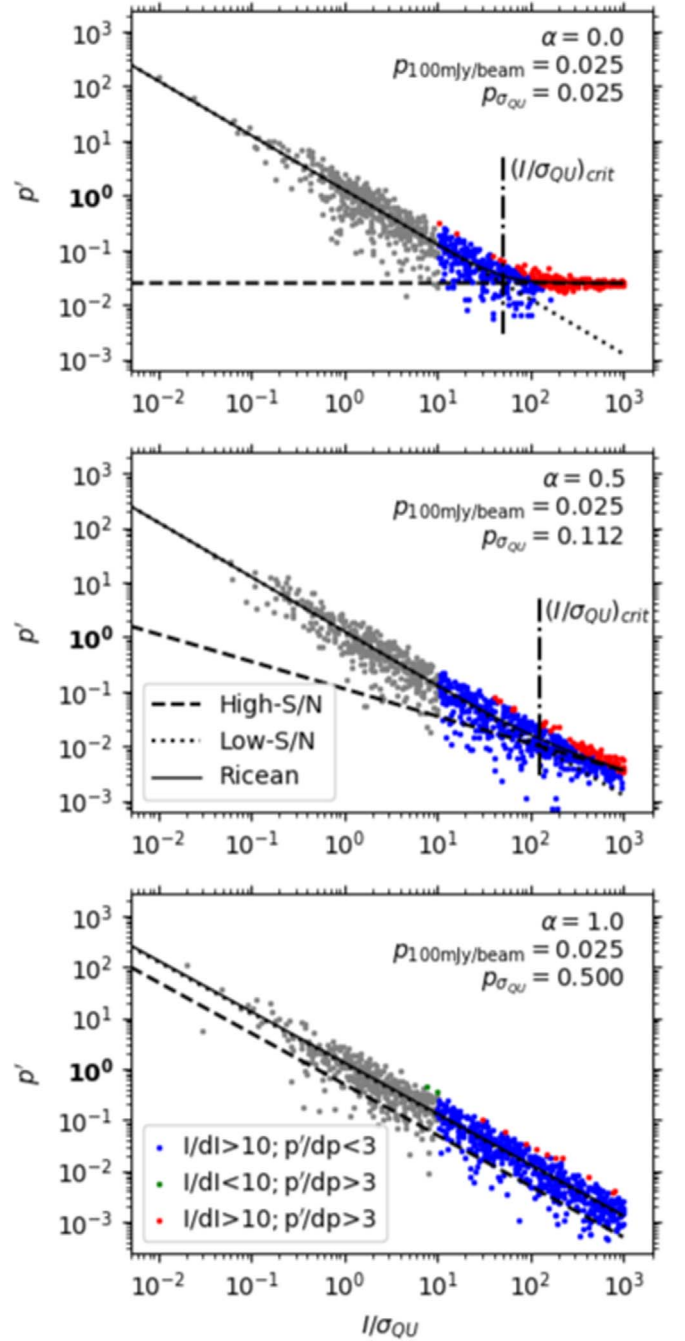


Figure 2. Monte Carlo simulations of the observed polarization fraction p' as a function of S/N I/σ_{QU} for three cases: $\alpha = 0$ (top), 0.5 (middle), and 1 (bottom). In all cases, $p_{100 \text{ mJy beam}^{-1}} = 0.025$. Results are shown without debiasing. The polarization fraction p' is given as an absolute value (not as a percentage), so any value $p' > 1$ (marked in bold on plot axes) is unphysical. Points are colored according to their S/N in I and p' ; gray points meet none of the criteria shown in the legend. The solid black line shows $p' = \mu_p$, the mean of the Rice distribution, for the given values of α and $p_{\sigma_{QU}}$. The dashed black line shows the true polarization fraction $p = p_{\sigma_{QU}}(I/\sigma_{QU})^{-\alpha}$. The dotted line shows the null-hypothesis/low-S/N relation $p' = \sqrt{\pi/2}(I/\sigma_{QU})^{-1}$. In the cases where $\alpha < 1$, the dotted-dashed line marks the critical value $(I/\sigma_{QU})_{\text{crit}} = (p_{\sigma_{QU}}^{-1} \sqrt{\pi/2})^{1/(1-\alpha)}$.

4.1. Uncertainty on Polarization Fraction

In keeping with standard practice in observational polarimetry and the default behavior of the POL-2 pipeline (e.g., Kwon et al. 2018), we estimated the uncertainty on the

polarization fraction using the relation

$$\delta p = \left(\frac{Q^2 \delta Q^2 + U^2 \delta U^2}{I^2(Q^2 + U^2)} + \frac{\delta I^2(Q^2 + U^2)}{I^4} \right)^{\frac{1}{2}} \quad (19)$$

(e.g., Wardle & Kronberg 1974). We note that this result is derived using classical error propagation and so assumes that δQ , δU , and δI are small and uncorrelated. We here take $\delta Q = \delta U = \sigma_{QU}$ and $\delta I = \sigma_I$. As discussed above, measurement errors δp calculated using Equation (19) can only be treated as representative of a Gaussian distribution around p' when $p'/\delta p$ is large.

4.2. Fitting Methods

We investigated the results of fitting two models to our Monte Carlo simulations. Fitting was performed using the *scipy* routine *curve_fit*. In all cases, we attempted to recover the input values of $p_{\sigma_{QU}}$ and α , assuming that σ_{QU} is a fixed and directly measurable property of the data set. We supplied our calculated δp values to *curve_fit* as 1σ uncertainties on p' . Although this is technically valid only at high S/N, the default behavior of this fitting routine is to consider only the relative magnitudes of the input uncertainties. The uncertainties provided thus down-weight the contribution of low-S/N points to the fitting process.

Single power-law—In keeping with standard practice, we fitted a single power-law model, Equation (13), to the high-S/N data. This model assumes that $p' \approx p$ and so is usually applied to data that have been statistically debiased. Applying this model to data that have not been debiased would inherently lead to artificially high values of α being recovered. In order to fairly test this model, we thus applied it to the debiased polarization fractions p'_{db} returned by our Monte Carlo simulations; i.e., we fitted

$$p'_{db} = p_{\sigma_{QU}} \left(\frac{I}{\sigma_{QU}} \right)^{-\alpha} \quad (20)$$

to a high-S/N subset of the debiased data. We tested two commonly used S/N criteria: $I/\delta I > 10$ and $p'_{db}/\delta p > 3$. As we are here selecting higher-S/N data points, the δp values we use should be somewhat representative of 1σ Gaussian uncertainties on p'_{db} . However, this model will provide accurate values of $p_{\sigma_{QU}}$ and α only if the p'_{db} values selected are well within the high-S/N limit described in Section 3.3.

Mean of Rice distribution—We fitted the mean of the Rice distribution (Equation (4)), assuming that p is given by Equation (13), and that $\sigma_p \approx \sigma_{QU}/I$, i.e.,

$$p' = \sqrt{\frac{\pi}{2}} \left(\frac{I}{\sigma_{QU}} \right)^{-1} \mathcal{L}_{\frac{1}{2}} \left[-\frac{p_{\sigma_{QU}}^2}{2} \left(\frac{I}{\sigma_{QU}} \right)^{2(1-\alpha)} \right]. \quad (21)$$

We hereafter refer to this model as the “Ricean-mean model.” This model is applied to the entire data set without any selection by S/N and to data that have not been statistically debiased. The Ricean-mean model is predicated on the Ricean probability density function (Equation (3)) being applicable to the data, which will not be the case if any attempt has been made to correct the data for observational bias. We note that although the δp values used in the fitting process do not strictly represent 1σ Gaussian uncertainties, they do have the effect of

significantly down-weighting the contribution of low-S/N data to the best-fit model. Fitting this model thus requires a good measurement of σ_{QU} with which to constrain the low-S/N behavior.

We fitted these models to non-debiased (Ricean-mean) and debiased (power-law) values of p' for each realization of our Monte Carlo simulations. We tested values of α in the range $0 \leq \alpha \leq 1$. Our results are shown in Figure 3. We find that, of the fitting models we tested, only the Ricean-mean model can accurately recover both α and $p_{\sigma_{QU}}$ when α is large.

For data with a maximum I/σ_{QU} value of 1000 and $p_{100 \text{ mJy beam}^{-1}} = 0.025$, α and $p_{\sigma_{QU}}$ can be approximately recovered with the single power-law model only while $\alpha < 0.3$. For the single power-law model, the recovered value of α is systematically larger than the input value, tending toward 1 as α increases (thus, an input value $\alpha = 1$ can be accurately recovered). The recovered value of $p_{\sigma_{QU}}$ is also larger than the input value for steep values of α . Selecting $p/\delta p > 3$ systematically increases the recovered value of $p_{\sigma_{QU}}$, as would be expected from examination of Figure 2. Thus, we expect fitting a single power-law model to, in general, systematically return larger-than-input values of α and $p_{\sigma_{QU}}$ and so over-estimate the extent to which depolarization is occurring. This is shown in Figure 3.

We find that the Ricean-mean model performs well for most values of α . As expected, the Ricean-mean model cannot accurately recover the input model parameters without a significant number of data points above $(I/\sigma_{QU})_{\text{crit}}$. If the data set under consideration has a maximum S/N $(I/\sigma_{QU})_{\text{max}}$, a necessary condition for the input model parameters to be recoverable will be

$$\left(\frac{I}{\sigma_{QU}} \right)_{\text{max}} > \left(\frac{I}{\sigma_{QU}} \right)_{\text{crit}}, \quad (22)$$

because if the break from $p' \propto I^{-1}$ to $p' \propto I^{-\alpha}$ occurs above the maximum S/N in the data set, α will perforce not be recoverable. Thus, for a given value of $p_{\sigma_{QU}}$, there will be some theoretical maximum (i.e., steepest) recoverable value of α , which we define as α_{max} , associated with $(I/\sigma_{QU})_{\text{max}} = (I/\sigma_{QU})_{\text{crit}}$. Combining this equality with Equation (14) (substituting α_{max} for α in the latter), we find

$$\alpha_{\text{max}} = 1 - \frac{\log \left(\frac{1}{p_{\sigma_{QU}}} \sqrt{\frac{\pi}{2}} \right)}{\log \left(\left[\frac{I}{\sigma_{QU}} \right]_{\text{max}} \right)}. \quad (23)$$

In practice, a reasonable number of data points must have S/Ns greater than $(I/\sigma_{QU})_{\text{crit}}$ in order to accurately recover the input model values. Figure 3 shows that, for our chosen values of $p_{100 \text{ mJy beam}^{-1}} = 0.025$, $\sigma_{QU} = 5.0$, and $(I/\sigma_{QU})_{\text{max}} = 1000$, the Ricean-mean model can accurately recover values up to $\alpha \approx 0.6$ and approximately recover $\alpha \approx 0.7$, but values steeper than this cannot be recovered accurately. The $\alpha = 0.9$ and 1.0 cases have no data points above $(I/\sigma_{QU})_{\text{crit}}$. Our results suggest that in order to accurately recover the input parameters, $\gtrsim 40\%$ of the data points must be above $(I/\sigma_{QU})_{\text{crit}}$.

When performing these Monte Carlo simulations, we set $\sigma_I = \sigma_{QU}$. We find that the Ricean-mean model can accurately recover the input model values despite the approximation $\sigma_I = 0$ in Equation (3). This supports our assumption that the

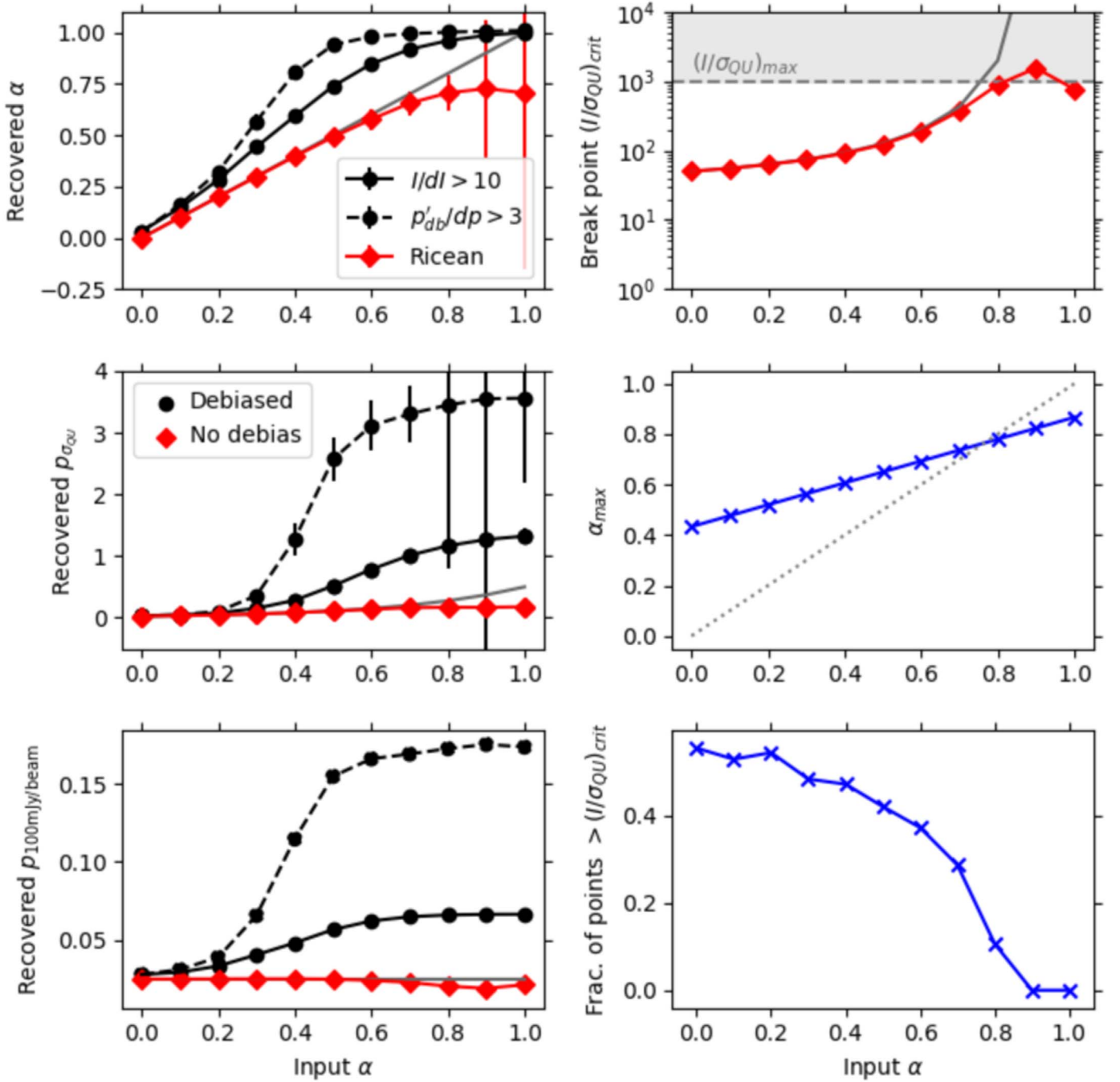


Figure 3. Results of fitting to Monte Carlo simulations for $p_{100 \text{ mJy beam}^{-1}} = 0.025$ and $0 \leq \alpha \leq 1$. Left column: The black data points show single power-law fitting to debiased data where $p/\delta p > 3$ (dashed line) and $I/\delta I > 10$ (solid line). The red data points show fitting of the Ricean-mean model to non-debiased data. Top row: recovered values of α ; middle row: recovered values of $p_{\sigma_{QU}}$; bottom row: recovered values of $p_{100 \text{ mJy beam}^{-1}}$. All rows: The solid gray line shows the input values. Right column (relevant to Ricean-mean model only): The top row shows the critical S/N value $(I/\sigma_{QU})_{\text{crit}}$ inferred from the best-fit α and $p_{\sigma_{QU}}$ for the Ricean-mean model. The solid gray line shows the input values. The horizontal dashed line shows the maximum S/N value in the simulations, $(I/\sigma_{QU})_{\text{max}} = 1000$, and the values $(I/\sigma_{QU})_{\text{crit}} > (I/\sigma_{QU})_{\text{max}}$ (indicating the range in which input model values are not recoverable) are shaded in gray. The dotted gray line shows the 1:1 relation; values near or to the right of this line will not be accurately recoverable. Bottom row: fraction of data points above the critical S/N $(I/\sigma_{QU})_{\text{crit}}$.

effect of uncertainty on the total intensity on the observed polarization fraction is negligible compared to that on the polarized intensity.

We find that the Ricean-mean model consistently performs better than single power-law fitting in accurately recovering α and $p_{\sigma_{QU}}$. We therefore choose to apply this model to our observational data.

5. An Example: JCMT POL-2 Observations of the L1688 Region of the Ophiuchus Molecular Cloud

In order to test our model on real data, we used JCMT BISTRO survey (Ward-Thompson et al. 2017) 850 μm POL-2 observations of three dense clumps within the Ophiuchus L1688 molecular cloud: Oph A, Oph B, and Oph C. These data sets were originally presented by Kwon et al. (2018),

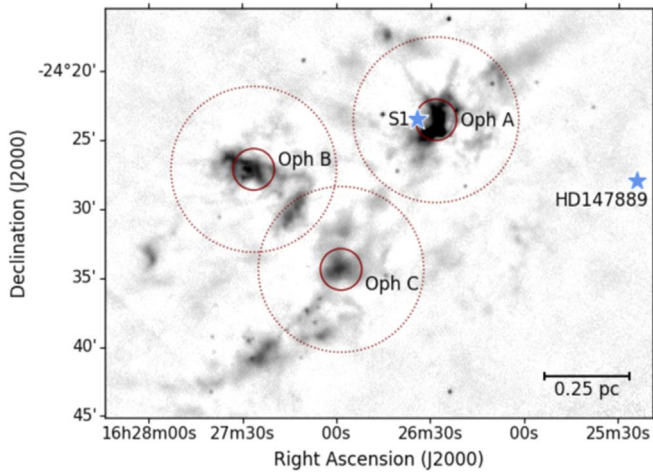


Figure 4. Finding chart for the L1688 region. The gray-scale image shows the JCMT Gould Belt Survey SCUBA-2 850 μm map of the region (Pattle et al. 2015). The three BISTRO fields are marked in red: solid lines show the central 3' diameter regions with uniform noise characteristics used in this work, and dotted lines show the full extent of the observations. The locations of the B stars HD 147889 and S1 are marked with blue stars. A plane-of-sky distance of 0.25 pc at our assumed distance to L1688 of 138 pc is shown in the lower right corner.

Soam et al. (2018), and Liu et al. (2019), respectively, and were taken under JCMT project code M16AL004.

The Oph A and B clumps are active star formation sites containing outflow-driving protostellar sources and gravitationally bound prestellar cores, while Oph C has little or no ongoing star formation and contains only pressure-bound cores (Pattle et al. 2015). Oph B and C are cold (~ 10 K) clumps showing little sign of external influence. Oph A is warmer, ~ 20 K, and is in the vicinity of two B stars, HD 147889 (spectral type B2V, Wilking et al. 2008; effective temperature $T_{\text{eff}} \sim 20,800$ K, Silaj et al. 2010) and S1 (B4V, $T_{\text{eff}} \sim 17,000$ K; Mookerjee et al. 2018). The immediate proximity of the latter of these significantly increases the ionizing photon flux on Oph A over that on other clumps in L1688 (Pattle et al. 2015). The geometry and radiation field of L1688 is discussed in detail by Liseau et al. (1999) and Stamatellos et al. (2007). A finding chart for the L1688 region is shown in Figure 4.

5.1. Observations and Data Reduction

We reduced each set of observations²⁰ (20 observations of Oph A and C; 19 observations of Oph B) using the *pol2map*²¹ routine recently added to SMURF (Berry et al. 2005; Chapin et al. 2013) and the “2018 January” instrumental polarization model (Friberg et al. 2018). The data reduction process is as described by Soam et al. (2018), with the following modifications: (1) in the second stage of the data reduction process, the *skyloop*²² routine was used, in which each iteration of the mapmaker is performed on each of the observations in the set in turn, rather than each observation being reduced consecutively, as is the standard method; (2) variances in the final coadded maps were calculated according to the standard deviation of the measured values in each pixel across the 20

observations, rather than as the mean of the rms of the bolometer counts in that pixel in each observation; and (3) in the final coadded maps, each observation was weighted according to the mean of its associated variance values. The net effect of these alterations is to improve homogeneity between observations and reduce noise in the final coadded maps. Based on the outcomes of fitting our Monte Carlo simulations, we did not attempt to debias the measured polarization fractions.

As discussed in Section 3, the Ricean model assumes that Stokes Q and U have uncorrelated uncertainties. This is a reasonable assumption for POL-2 data. The first step of the POL-2 data reduction process is to separate each bolometer time stream into Q , U , and I time streams by fitting a sinusoidal function to the data using the *calcqu*²³ routine. So long as the phase of the polarized emission (twice the position angle of the POL-2 half-wave plate) is accurately known at each point in the bolometer time stream, the Q and U time streams should be correctly separated. The Q , U , and I data are thereafter reduced independently of one another.

In our model, we assume that the observed data can be accurately characterized by a single rms noise value, σ_{QU} . The JCMT POL-2 observations use an observing mode wherein the central 3' diameter region of each 12' diameter observation has constant exposure time and so approximately constant rms noise (Friberg et al. 2016). We thus considered only this central region of each field. (In Oph B, this corresponds to the Oph B2 clump.) The three fields, along with their polarization vectors, are shown in Figure 5.

Each pixel in the output Stokes Q and U maps has associated variance values V_Q and V_U , determined as described above. These variance maps can be converted into maps of 1σ rms noise by taking their square roots. We thus estimated a single rms noise value for our data,

$$\langle\sigma_{QU}\rangle = \frac{1}{2N} \sum_{i=1}^N (\sqrt{V_{Q,i}} + \sqrt{V_{U,i}}), \quad (24)$$

where N is the number of pixels in the data set. We set $\sigma_{QU} = \langle\sigma_{QU}\rangle$ when performing model fitting. We retain the notation $\langle\sigma_{QU}\rangle$ while fitting real data in order to emphasize that this is a measured property of the data set. The $\langle\sigma_{QU}\rangle$ values measured in each field are listed in Table 1. We also calculated the uncertainties on the polarization fraction for each pixel from the variance values V_Q , V_U , and V_I using Equation (19).

The JCMT POL-2 data are by default reduced onto 4'' pixels. In order to investigate the dependence of the observed polarization fraction on rms noise, we also gridded the data to $4n''$ pixels, where $n = 1-8$, thereby generally reducing the rms noise, as shown in Table 1. We note that binning to larger pixel sizes increases the chance of beam-averaging-related depolarization. However, for the 8'' and 12'' cases, as we grid from a pixel size of $\sim 1/3$ of the 850 μm JCMT primary beam to slightly smaller than beam-sized pixels (the JCMT has an effective beam size of $14''.1$ at 850 μm ; Dempsey et al. 2013), we do not expect this to be an issue in at least these cases. We did not grid to larger pixel sizes than 32'', as at larger pixel sizes, the rms noise values ceased to improve, and the number of data points became prohibitively small.

²⁰ A single JCMT BISTRO POL-2 observation consists of 40 minutes of observing time using the POL-2-DAISY scan pattern described by Friberg et al. (2016).

²¹ <http://starlink.eao.hawaii.edu/docs/sc22.pdf>

²² <http://starlink.eao.hawaii.edu/docs/sc21.htx/sc21.html>

²³ <http://starlink.eao.hawaii.edu/docs/sun258.htx/sun258ss5.html>

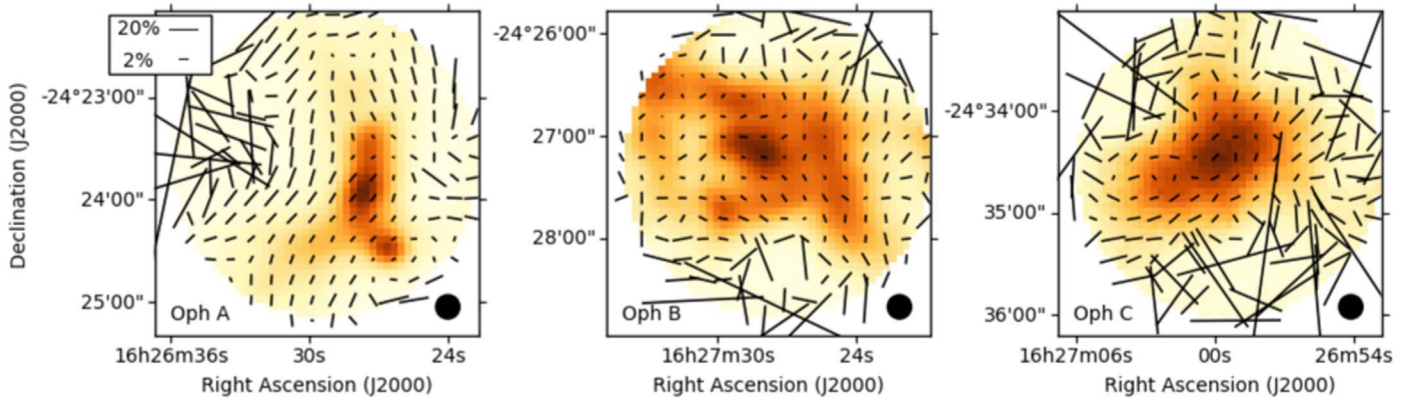


Figure 5. The POL-2 850 μm total intensity maps of the central 3' of the BISTRO Oph A, B, and C fields, with polarization vectors overlaid. Vectors are sampled to a 12'' grid and scaled according to $\sqrt{p'}$. The polarization fractions have not been debiased. The 20% and 2% polarization vectors are shown in the upper left corner of the left panel, demonstrating the nonlinearity of the vector scale. The JCMT 850 μm beam size is shown in the lower right corner of each plot.

5.2. Fitting

We fitted each data set with the mean of the Rice distribution (Equation (4)) using all data points and uncertainties calculated using Equation (19). Fitting was performed as described in Section 4.2. The models were normalized to the mean uncertainty in Q and U , $\langle\sigma_{QU}\rangle$, and the data were fitted for $p_{\sigma_{QU}}$ and α .

The results of our fitting are listed in Table 1 and plotted in Figures 6 and 7. It can be seen that in all cases, the data are well characterized by $\langle\sigma_{QU}\rangle$ and well described by the Rice distribution, following Equation (4).

Table 1 lists the reduced χ^2 values for each model and the null hypothesis. Under the null hypothesis, $p_{\sigma_{QU}} = 0$, so $p' = (I/\langle\sigma_{QU}\rangle)^{-1}\sqrt{\pi/2}$ for all I . As in Section 4.2, we note that the uncertainties on δp can be treated as Gaussian only at high S/N. The reduced- χ^2 statistic is thus not strictly a direct comparison between the difference between the data and the model and the variance in the data. We therefore compare only the relative size of the reduced- χ^2 statistics for the best-fit and null-hypothesis models, treating a smaller value of the reduced χ^2 as being broadly representative of better agreement between the data and the model.

5.3. Oph A

Oph A shows clear evidence for a power-law behavior shallower than $\alpha = 1$. Examination of Figure 6 shows significant deviation from $\alpha = 1$ on 12'' pixels. This is confirmed by the fitted models producing a reduced- χ^2 statistic approximately three to four times smaller than that of the null hypothesis on all pixel sizes.

When fitting the mean of the Rice distribution to the Oph A data, we consistently recovered $p_{100 \text{ mJy beam}^{-1}} \approx 0.047$ and $\alpha \approx 0.34$. The results returned from 4''–28'' pixel data are consistent within the fitting uncertainties, with no obvious signs of depolarization due to beam averaging, although the fitting results become more uncertain as the pixel size increases, as shown in Figure 8. Fitting of the Oph A data fails for 32'' pixels; this is likely due to the relatively small number of remaining data points and the significant intrinsic scatter in the data around the best-fit model. In all cases, the best-fitting models produce reduced- χ^2 statistics significantly greater than

unity, suggesting more variation in the data than can be explained by our simple model alone.

We thus interpret our results as indicating that the Oph A data can be represented by the model $p_{100 \text{ mJy beam}^{-1}} = 0.047$ and $\alpha = 0.34$. Equations (11) and (14) suggest that, when $\sigma_{QU} \approx 1 \text{ mJy beam}^{-1}$, this behavior will be recoverable only when a significant number of data points fall above $(I/\sigma_{QU})_{\text{crit}} \sim 18$.

5.4. Oph B

In Oph B, the incompatibility of the data with the null hypothesis becomes more apparent with increasing pixel size. In the 4'' case, the Oph B data do not clearly support a power-law index distinct from $\alpha = 1$ being observed, with the Ricean-mean model and the null hypothesis producing similar reduced- χ^2 values.

In the 12'' case, the data appear to be skewed above the null-hypothesis line in Figure 6. The Ricean-mean fitting results produce reduced- χ^2 values a factor of ~ 2 smaller than that of the null hypothesis. Gridding the data to larger pixel sizes results in progressively smaller values of $p_{\sigma_{QU}}$ and α being recovered, as shown in Figure 8. The 32'' case is shown in Figure 7 and clearly shows that the data are not consistent with an index of $\alpha = 1$.

The most representative values of α and $p_{100 \text{ mJy beam}^{-1}}$ in Oph B are not very well constrained. To a certain extent, Figure 8 shows a stabilization in the fitted values of α and $p_{100 \text{ mJy beam}^{-1}}$ in Oph B at lower rms noise values. On the larger pixel sizes considered, $\alpha \sim 0.6$ –0.7. On 20'' pixels and larger, $p_{100 \text{ mJy beam}^{-1}}$ becomes consistent with a value of ~ 0.02 . It is also possible that gridding to larger pixel sizes alters the observed average grain properties in Oph B, although, as discussed above, this does not appear to be the case in Oph A. Equations (11) and (14) suggest that $\alpha = 0.65$ and $p_{100 \text{ mJy beam}^{-1}} = 0.02$ would, for $\sigma_{QU} \approx 1 \text{ mJy beam}^{-1}$, be recoverable only when a significant number of data points fall above $(I/\sigma_{QU})_{\text{crit}} \sim 26$.

5.5. Oph C

We find that Oph C behaves similarly to Oph B. Due to its lower peak brightness than Oph B, the Oph C data show little evidence for deviation from an I^{-1} behavior on beam-sized or smaller pixels. In the 4'' and 8'' data, the null hypothesis

Table 1Mean rms Noise in Stokes Q and U , $\langle\sigma_{QU}\rangle$; Number of Pixels, N ; and Fitting Results for the Ricean-mean Model for L1688 Oph A, B, and C Data on Pixel Sizes of $4''$ – $32''$

Pixel Size (arcsec)	$\langle\sigma_{QU}\rangle$ (mJy beam ⁻¹)	N	Null $\frac{\chi^2}{N}$	Ricean-mean Model			$\frac{\chi^2}{N-2}$
				α	$P_{\sigma_{QU}}$	$P_{100 \text{ mJy beam}^{-1}}$	
Oph A							
4	3.29 ± 0.55	1456	33.3	0.34 ± 0.02	0.15 ± 0.02	0.047 ± 0.009	9.2
8	1.88 ± 0.36	400	101.0	0.34 ± 0.03	0.18 ± 0.04	0.047 ± 0.016	24.9
12	1.45 ± 0.50	192	189.4	0.33 ± 0.05	0.19 ± 0.06	0.047 ± 0.025	45.1
16	1.15 ± 0.44	114	291.9	0.34 ± 0.06	0.21 ± 0.09	0.046 ± 0.032	73.0
20	1.07 ± 0.66	79	397.2	0.39 ± 0.08	0.31 ± 0.18	0.053 ± 0.050	110.6
24	0.95 ± 0.66	56	437.1	0.38 ± 0.10	0.30 ± 0.20	0.051 ± 0.058	98.9
28	1.02 ± 0.77	47	480.4	0.31 ± 0.12	0.18 ± 0.16	0.043 ± 0.062	115.5
32	0.60 ± 0.16	31	832.0	0.00 ± 0.16	0.02 ± 0.03	0.020 ± 0.046	172.1
Oph B							
4	3.37 ± 0.57	1404	1.4	0.86 ± 0.03	0.89 ± 0.11	0.048 ± 0.011	1.0
8	1.93 ± 0.41	390	2.5	0.78 ± 0.05	0.73 ± 0.18	0.034 ± 0.015	1.4
12	1.49 ± 0.54	191	3.7	0.76 ± 0.07	0.68 ± 0.25	0.028 ± 0.018	2.0
16	1.18 ± 0.49	115	4.7	0.70 ± 0.09	0.53 ± 0.26	0.024 ± 0.021	2.2
20	1.12 ± 0.76	78	6.6	0.66 ± 0.12	0.44 ± 0.29	0.023 ± 0.027	3.2
24	0.99 ± 0.73	58	7.7	0.71 ± 0.12	0.58 ± 0.38	0.022 ± 0.026	3.5
28	1.03 ± 0.77	47	6.4	0.57 ± 0.18	0.22 ± 0.22	0.016 ± 0.030	3.2
32	0.61 ± 0.16	32	12.2	0.59 ± 0.16	0.34 ± 0.34	0.017 ± 0.030	4.2
Oph C							
4	3.70 ± 0.65	1239	0.9	0.83 ± 0.03	0.75 ± 0.09	0.049 ± 0.011	0.7
8	2.12 ± 0.45	359	1.4	0.84 ± 0.04	0.93 ± 0.16	0.037 ± 0.012	1.0
12	1.64 ± 0.63	177	2.1	0.76 ± 0.07	0.70 ± 0.20	0.031 ± 0.018	1.3
16	1.30 ± 0.54	109	2.3	0.75 ± 0.07	0.72 ± 0.24	0.027 ± 0.018	1.3
20	1.22 ± 0.80	75	2.6	0.69 ± 0.09	0.52 ± 0.22	0.025 ± 0.020	1.3
24	1.10 ± 0.87	55	2.9	0.71 ± 0.12	0.52 ± 0.29	0.021 ± 0.023	1.7
28	1.15 ± 0.88	45	4.0	0.58 ± 0.14	0.30 ± 0.21	0.023 ± 0.030	2.0
32	0.67 ± 0.18	32	6.0	0.63 ± 0.11	0.52 ± 0.30	0.022 ± 0.025	2.0

Note. Note that the results for Oph A on $32''$ pixels are not reliable.

produces a reduced- χ^2 value comparable to that of the Ricean-mean model, and there is no clear evidence that the Ricean-mean model provides a better description of the data. In the $12''$ case, shown in Figure 6, there is only a marginal improvement in goodness of fit over the null-hypothesis case.

As in Oph B, gridding to larger pixels produces smaller values of both α and $p_{100 \text{ mJy beam}^{-1}}$ and makes the deviation of the data from the null-hypothesis behavior more apparent. Figure 7 qualitatively shows the similarity between the Oph B and C data, while Figure 8 shows that the fitting results of Oph B and C agree very closely in all cases.

5.6. Discussion

Our results suggest that grains in Oph A are intrinsically better aligned with the magnetic field than those in Oph B and C. Grains in Oph B and C appear to lose what alignment they have with the magnetic field more precipitously with increasing density (or extinction) than is the case in Oph A. Oph B and C appear to have indistinguishable grain properties despite their differing star formation histories, while Oph A and B behave significantly differently despite having comparable mass and both being active sites of star formation.

We estimated the upper-limit ionizing fluxes on Oph A, B, and C from the B stars HD 147889 and S1 as a qualitative

indicator of the differences in interstellar radiation field (ISRF) on the three clumps. We took the flux of Lyman continuum photons to be $\sim 10^{20.4} \text{ cm}^{-2} \text{ s}^{-1}$ from the surface of HD 147889 and $\sim 10^{18.5} \text{ cm}^{-2} \text{ s}^{-1}$ from the surface of S1 (Pattle et al. 2015, and references therein). We determined plane-of-sky distances from HD 147889 and S1 to the centers of Oph A, B, and C, assuming a distance to L1688 of 138 pc (Ortiz-León et al. 2018), and so estimated upper-limit ionizing fluxes from the stars on each region.²⁴ These fluxes are listed in Table 2. We assume that the global ISRF on the three regions is comparable (a reasonable assumption, given the clumps' proximity to one another). It can be seen that the ionizing flux on Oph A is an order of magnitude larger than that on Oph B and C, and that this difference is primarily caused by the proximity of S1 to Oph A. It is likely that HD 147889 will affect the three clumps similarly, while S1's influence is dominant in Oph A but negligible elsewhere.

²⁴ We note that if we adopted the three-dimensional model of L1688 proposed by Liseau et al. (1999), the distance from HD 147889 to the three clumps would be 0.86 pc to Oph A, 1.33 pc to Oph B, and 1.03 pc to Oph C (distances scaled to account for their assumed distance to L1688 of 150 pc). This would alter our inferred fluxes from HD 147889 by factors of ~ 0.5 , ~ 0.6 , and ~ 0.8 in Oph A, B, and C respectively. This would not change the conclusions of our analysis.

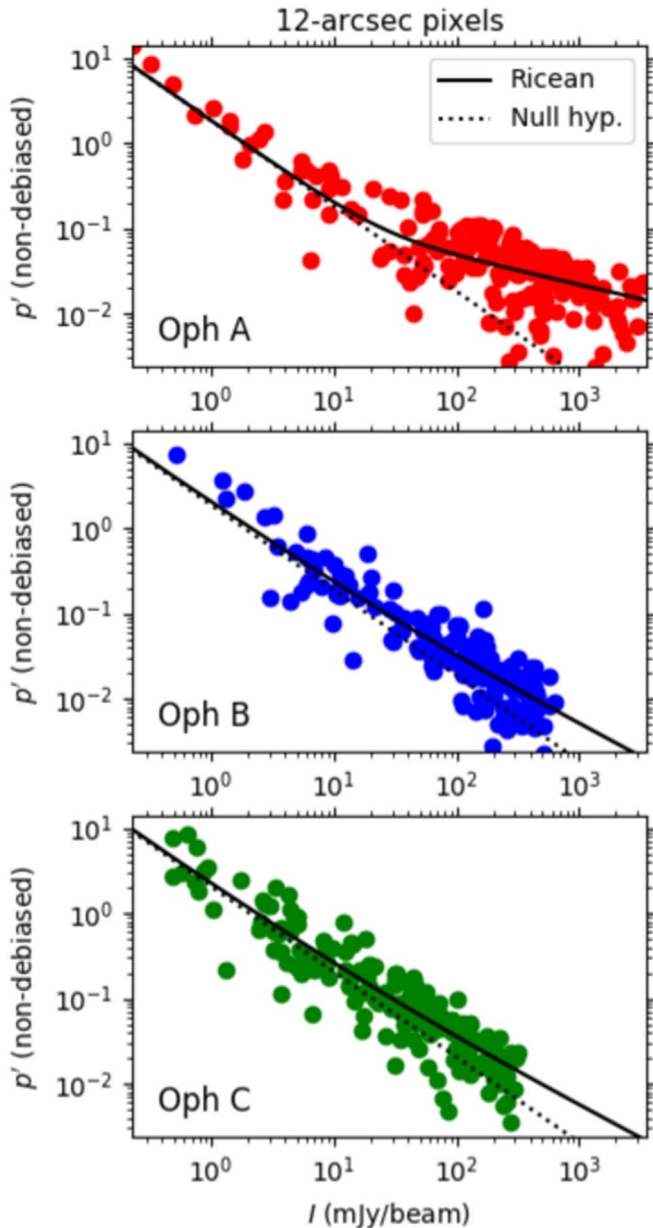


Figure 6. Plot of observed polarization fraction p' vs. total intensity I for the Oph A, B, and C data, gridded onto $12''$ pixels. Top row: Oph A; middle row: Oph B; bottom row: Oph C. The solid black line shows the best-fitting Ricean model. The dotted black line shows the expected behavior under the null hypothesis. Note that the polarization fractions have not been debiased.

The most likely explanation for the better grain alignment in Oph A is thus the elevated photon flux on that region, primarily resulting from the proximity of the star S1. Under the radiative torque alignment (RAT) paradigm of grain alignment (Lazarian & Hoang 2007; Andersson et al. 2015), this stronger and bluer radiation field on Oph A would allow grain alignment to persist to a higher optical depth. The strongly anisotropic radiation field on Oph A might also favor better grain alignment in this region (Dolginov & Mitrofanov 1976; Onaka 2000; Weingartner & Draine 2003). We note that the difference in behavior between Oph A and Oph B, both of which are actively forming stars, suggests that the better grain alignment in Oph A is primarily driven by external influence, not by short-wavelength flux from protostellar sources within the clump.

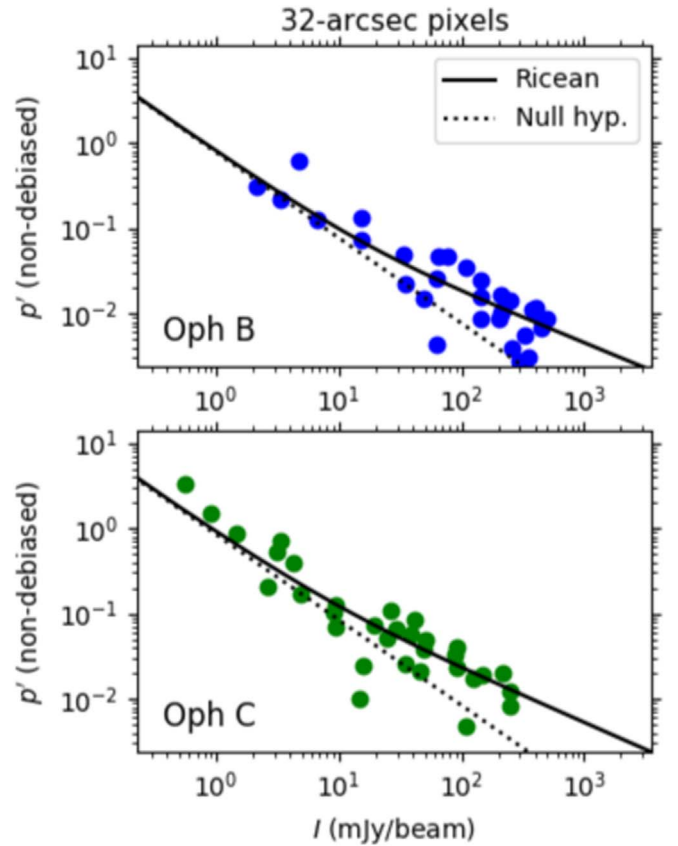


Figure 7. Observed polarization fraction p' vs. total intensity I for the B and C data, with data gridded to $32''$ pixels. The polarization fractions have not been debiased. Best-fitting models are shown as in Figure 6. Note that both data sets show significant deviation from the null-hypothesis behavior.

We note that the ionizing flux from these stars will not itself directly contribute to grain alignment within the clumps. In order to drive RAT grain alignment, the wavelength of the incident radiation must be shorter than twice the size of the largest grains, i.e., $\lesssim 1\text{--}2\ \mu\text{m}$ (Andersson et al. 2015). The short-wavelength photons considered here will undergo multiple scatterings before they can contribute significantly to grain alignment, while longer-wavelength emission from the stars may contribute more directly, particularly in Oph A, thanks to its proximity to S1. We emphasize that the calculations above only qualitatively demonstrate the global elevation of photon flux on Oph A over the other two clumps. Modeling of the detailed radiation field in L1688 is beyond the scope of this work.

The magnetic field in Oph A may also be intrinsically more ordered in Oph A than in Oph B and C, as the clump's location between HD 147889 and S1 could result in its molecular gas, and thus its magnetic field, being compressed by the HD 147889 photon-dominated region (PDR) and the S1 reflection nebula. In contrast, Oph B and C are evolving in relative isolation from the two B stars and are not undergoing significant compression. In this case, the lower value of α in Oph A might in part result from its more ordered internal magnetic field, with less vector cancellation of the observed polarization fraction along the line of sight occurring in Oph A than in the other two regions.

Another possible cause of better grain alignment in Oph A than in the other two clumps is grain growth in the dense

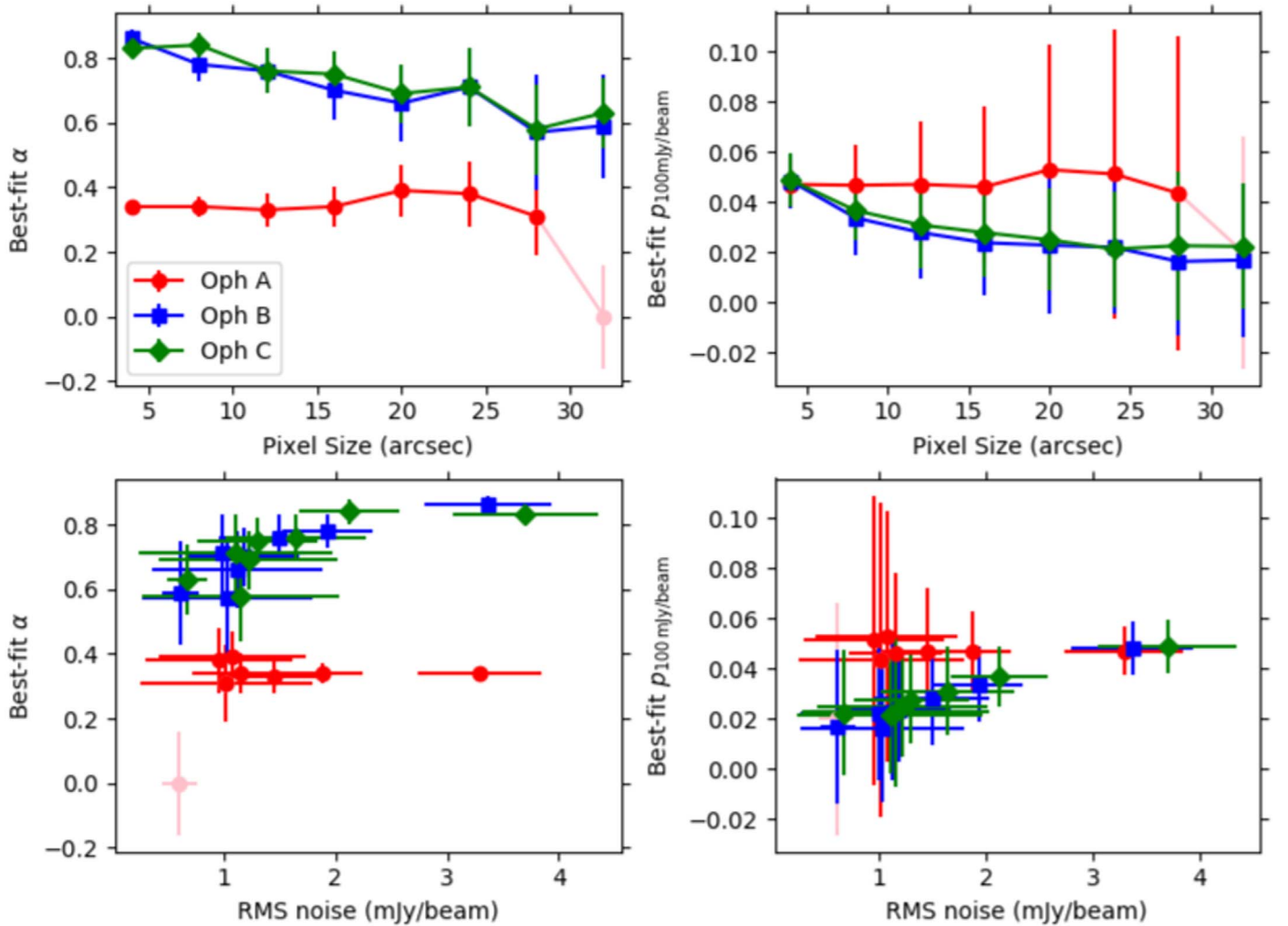


Figure 8. Best-fit values of α (left) and $p_{100 \text{ mJy beam}^{-1}}$ (right) for the Oph A, B, and C data, as determined from fitting the Ricean-mean model, as a function of pixel size (top) and rms noise $\langle\sigma_{QU}\rangle$ (bottom). Fitting results for Oph A on 32'' pixels are shown in pink, as this result is not reliable.

Table 2

Ionizing Flux on Oph A, B, and C from the Stars HD 147889 and S1

Region	Plane-of-sky Distance (pc)		Upper-limit Ionizing Photon Flux ($\text{s}^{-1} \text{m}^{-2}$)		
	HD 147889	S1	HD 147889	S1	Total
Oph A	0.62	0.05	7.0×10^{10}	1.5×10^{11}	2.2×10^{11}
Oph B	1.13	0.51	2.1×10^{10}	1.2×10^9	2.2×10^{10}
Oph C	0.91	0.50	3.2×10^{10}	1.2×10^9	3.4×10^{10}

regions of Oph A. The peak gas density of Oph A is approximately 1 order of magnitude higher than in Oph B and C (Motte et al. 1998). Such high densities might provide the necessary conditions for the formation of large dust grains (e.g., Hirashita & Li 2013). In the RAT paradigm, larger dust grains can be aligned by longer-wavelength photons, as described above; thus, the presence of large grains would allow grain alignment to persist to a higher optical depth.

While our results support better grain alignment in Oph A than in the other clumps, they do not suggest that grains in Oph B and C have no alignment with the magnetic field. Our modeling suggests that an index $\alpha \sim 0.6\text{--}0.7$ is plausible for both Oph B and C, suggesting that some degree of grain

alignment may persist to high optical depths within these clumps.

These results suggest that grain alignment could persist to significantly higher densities within starless clumps and cores than has previously been believed to be the case (e.g., Jones et al. 2015; Kwon et al. 2018; Soam et al. 2018), even in the absence of a short-wavelength illuminating source. This is consistent with recent modeling results, which suggest that grains remain well aligned with the magnetic field at gas densities $>10^3 \text{ cm}^{-3}$ (Seifried et al. 2019).

5.7. Limitations of the Fitting Process

The simple model we consider in this work is subject to a number of limitations.

We emphasize that in this work, we selected our data such that they can be well characterized by a single rms noise value in both Stokes Q and U . Data sets containing significant variation in rms noise would produce additional vertical spread in the p' - I plane, further complicating the recovery of an accurate value of α .

Our data show scatter about the best-fit line greater than can be explained by instrumental uncertainty alone, particularly in Oph A, which in all cases shows reduced- χ^2 values significantly larger than those in Oph B and C, and where

fitting fails for the largest pixel size considered here, likely due to significant intrinsic scatter in the data and the small number of data points to which the model can be fitted. In order to demonstrate the statistical properties of the data, we have chosen a very simple model in which the data are characterized by a single power law. More complex relationships between the polarization fraction and intensity could be investigated in future studies, as well as accounting for intrinsic variation in $p_{\sigma_{QU}}$ and α within a given region.

Our model is unphysical in that it suggests that the polarization fraction can increase indefinitely at small I . We are implicitly assuming first that there is a turnover in behavior at a density below which the polarization fraction becomes a shallower function of intensity, tending to the value in the low-density ISM. Second, we assume that this turnover occurs at densities lower than we can probe with POL-2. (In approximately isothermal environments, the SCUBA-2 camera is effectively volume-density-limited in its detections; see Ward-Thompson et al. 2016.)

Our results suggest that an observed index of $\alpha \simeq 1$ in the submillimeter data (e.g., Alves et al. 2014; Jones et al. 2015; Liu et al. 2019) is not sufficient to claim that nonaligned grains have been observed. However, if a break or turnover in behavior from a shallow power law ($\alpha < 1$) to an index of $\alpha = 1$ with increasing intensity were observed within a single polarized submillimeter emission data set, this would be strong evidence for the loss of grain alignment at high intensities. This is because if an index $\alpha < 1$ were recoverable at intermediate intensities, then an $\alpha = 1$ index seen at high intensities in the same data set could not simply result from having insufficient S/N to measure a shallower index and would thus be indicative of a genuine change in behavior with intensity. We do not see any evidence of such a break in behavior in Ophiuchus.

5.8. Relation between I and Visual Extinction A_V

In this paper, we consider only the relationship between p and I , with the goal of accurately determining their underlying relationship in the presence of Ricean noise. However, it is important to emphasize that the true physical relationship under investigation is not between p and I but between p and A_V .

Recent POL-2 studies (Juvela et al. 2018; Coudé et al. 2019; Wang et al. 2019) show a shallower relationship between p' and *Herschel Space Observatory*-derived dust opacity/optical depth measurements (a proxy for A_V , as discussed below) than between p' and I . We here present a simple argument for why we expect the p - A_V relationship to be intrinsically shallower than the p - I relationship.

The submillimeter intensity I_ν of thermal dust emission at a frequency ν is given by

$$I_\nu = B_\nu(T) \tau_\nu \Omega, \quad (25)$$

where $B_\nu(T)$ is the Planck function at temperature T , τ_ν is the submillimeter optical depth, and Ω is the solid angle (e.g., Hildebrand 1983). We henceforth assume that we are observing over a constant area, so

$$I_\nu \propto B_\nu(T) \tau_\nu. \quad (26)$$

Assuming $\tau_\nu \propto A_V$, i.e., optically thin submillimeter emission (e.g., Jones et al. 2015) and constant dust optical properties along the line of sight,

$$I_\nu \propto B_\nu(T) A_V. \quad (27)$$

Thus, I is a direct tracer of A_V only where T is constant. However, in most environments in molecular clouds, $B_\nu(T)$ and I are observed to be anticorrelated (e.g., Kirk et al. 2013; Könyves et al. 2015). This is a physical effect, with cooling being caused by self-shielding in dense environments (e.g., Glover & Clark 2012). Such cooling is expected in regions that do not contain embedded massive stars causing internal heating, such as the dense clumps of L1688 (Stamatellos et al. 2007). We parameterize the relationship between $B_\nu(T)$ and I_ν as

$$B_\nu(T) \propto I_\nu^\gamma, \quad (28)$$

initially placing no constraint on γ (note that here $B_\nu(T)$ is the source function of the dust emission; see Equation (26)). Combining Equations (10), (27), and (28),

$$p \propto A_V^{-\frac{\alpha}{1-\gamma}}. \quad (29)$$

If $\gamma < 0$ ($B_\nu(T)$, and so T , decreases with increasing I_ν), then

$$\frac{1}{1-\gamma} < 1. \quad (30)$$

Thus, in most physical environments in molecular clouds, any power-law relationship between A_V and p must be shallower (and likely more weakly correlated) than that between I and p . We note that $\gamma < 0$ would not hold in the presence of significant heating by sources located at high A_V , but in that case, we might expect these heating sources to also be driving grain alignment in their vicinity.

This analysis further suggests that grains could be better aligned at higher extinction than has previously been believed.

The exact nature of the relationship between I , T , and τ is not obtainable from single-wavelength observations such as those considered here. However, forthcoming multiwavelength studies will allow more direct investigation of the I - A_V relationship.

6. Summary

The dependence of the polarization fraction on total intensity in polarized submillimeter emission measurements is typically parameterized as a power law and used to infer the efficiency of dust grain alignment with the magnetic field in star-forming clouds and cores. In this work, we have demonstrated that significant S/N and well-characterized noise properties are required to recover a genuine power-law relationship between the polarization fraction and total intensity.

We presented a simple model for the dependence of the polarization fraction on total intensity in molecular clouds and so demonstrated that below an S/N threshold of $I/\sigma_{QU} = (p_{\sigma_{QU}}^{-1} \sqrt{\pi/2})^{\frac{1}{1-\alpha}}$, a power-law index of -1 will always be observed, as a result of the addition in quadrature of Stokes Q and U components and the approximate $1/I$ dependence of the error in the polarization fraction. For power-law indices $\alpha < 1$, the intrinsic dependence of the polarization fraction on intensity will be recoverable at high S/N. However, a genuine measurement of $p \propto I^{-1}$ —indicating unaligned grains—will be indistinguishable from statistical noise in most, if not all, physically realistic scenarios without additional information. We demonstrated that fitting a single power law is likely to result in overestimation of α and so of the degree of depolarization occurring. We further found that fitting the

mean of the Rice distribution to non-debiased data will accurately recover both $p_{\sigma_{QU}}$ and α , provided a reasonable number of data points fall above the required S/N threshold.

We used JCMT POL-2 observations of three clumps in the L1688 region of the Ophiuchus molecular cloud to demonstrate the statistical behavior described above. We found that the Oph A region, which is illuminated by two B stars, shows significantly better grain alignment than the neighboring Oph B and C. We found a power-law index of $\alpha \approx 0.34$ in Oph A, significantly shallower than that found by previous works. The power-law indices in Oph B and C are less well constrained but steeper than that of Oph A, and they are likely to be in the range $\alpha \sim 0.6$ – 0.7 . Oph B and C have intrinsically lower polarization fractions than Oph A at a total intensity of 100 mJy beam⁻¹, with emission from Oph A being 4.7% polarized, while emission from Oph B and C is $\sim 2\%$ polarized. Oph C, a quiescent cloud, appears to behave comparably to the actively star-forming Oph B. Our results thus suggest that grain alignment in Ophiuchus is driven by the external radiation field on the clumps, not by internal radiation sources.

These results suggest that grain alignment could persist to significantly higher densities within starless clumps and cores than has previously been believed to be the case. Submillimeter polarization measurements could thus potentially trace the magnetic field morphology in dense, star-forming gas.

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Facility: James Clerk Maxwell Telescope (JCMT).

Software: Starlink (Currie et al. 2014), Astropy (Astropy Collaboration et al. 2013, 2018).

Appendix

Appendix: List of Symbols Used in This Work

Table 3 lists the symbols used in this work, along with their units and the section of the paper in which they are defined.

Table 3
Symbols Used in This Work

Symbol	Definition	Units	Section Defined in
α	Power-law index, $p \propto I^{-\alpha}$	Dimensionless	1, 3
α_{\max}	Steepest recoverable α for given $p_{\sigma_{QU}}$ and $(I/\sigma_{QU})_{\max}$	Dimensionless	4.2
I	Stokes I intensity	Intensity	2
σ_I	rms noise in Stokes I	Intensity	2
δI	Measurement uncertainty on Stokes I	Intensity	2
I_{obs}	Stokes I intensity in Monte Carlo model	Intensity	4
ΔI	Measurement error on Stokes I in Monte Carlo model	Intensity	4
\mathcal{I}_0	Modified Bessel function of order zero	...	2.1
\mathcal{I}_1	Modified Bessel function of order 1	...	2.1
$\mathcal{L}_{\frac{1}{2}}$	Laguerre polynomial of order $\frac{1}{2}$...	2.1
N	Number of pixels in a given data set	Dimensionless	5.1
p	Intrinsic polarization fraction	Dimensionless	2
p'	Measured polarization fraction	Dimensionless	2.1; see also 4.2
p'_{db}	Debiased measured polarization fraction	Dimensionless	2.2
p_0	Polarization fraction at reference intensity I_0	Dimensionless	3
$p_{\sigma_{QU}}$	Polarization fraction at reference intensity σ_{QU}	Dimensionless	3
$p_{100 \text{ mJy beam}^{-1}}$	Polarization fraction at $I = 100 \text{ mJy beam}^{-1}$	Dimensionless	3
σ_p	rms noise in polarization fraction	Dimensionless	2.1
δp	Measurement uncertainty on polarization fraction	Dimensionless	4.1
μ_p	Mean of Rice-distributed polarization fraction	Dimensionless	2.1
P	Intrinsic polarized intensity	Intensity	2
P'	Measured polarized intensity	Intensity	2.1
P'_{db}	Debiased measured polarized intensity	Intensity	2.2
Q	Stokes Q intensity	Intensity	2
σ_Q	rms noise in Stokes Q	Intensity	2
δQ	Measurement uncertainty on Stokes Q	Intensity	2

Table 3
(Continued)

Symbol	Definition	Units	Section Defined in
V_Q	Variance on Stokes Q intensity	(Intensity) ²	5.1
Q_{obs}	Stokes Q intensity in Monte Carlo model	Intensity	4
ΔQ	Measurement error on Stokes Q in Monte Carlo model	Intensity	4
U	Stokes U intensity	Intensity	2
σ_U	rms noise in Stokes U	Intensity	2
δU	Measurement uncertainty on Stokes U	Intensity	2
V_U	Variance on Stokes U intensity	(Intensity) ²	5.1
U_{obs}	Stokes U intensity in Monte Carlo model	Intensity	4
ΔU	Measurement error on Stokes U in Monte Carlo model	Intensity	4
σ_{QU}	$\left\{ \begin{array}{l} (1) \text{ Representative rms noise in Stokes } Q \text{ and } U \\ (2) \text{ Reference intensity for fitted model} \end{array} \right.$	Intensity	3
$\langle \sigma_{QU} \rangle$	σ_{QU} inferred from real data	Intensity	5.1
θ_p	Polarization angle	Angle	2.3
V	Stokes V intensity	Intensity	2
$(I/\sigma_{QU})_{\text{crit}}$	Critical S/N below which $p' \propto I^{-1}$ dominates	Dimensionless	3.4
$(I/\sigma_{QU})_{\text{max}}$	Maximum S/N in a given data set	Dimensionless	4.2
A_V	Visual extinction	mag	5.8
B_ν	Planck function	$\text{W m}^{-2} \text{Hz}^{-1} \text{sr}^{-1}$	5.8
γ	Power-law index, $I \propto T^{-\gamma}$	Dimensionless	5.8
Ω	Solid angle	sr	5.8
ν	Frequency	Hz	5.8
T	Dust temperature	K	5.8
τ	Submillimeter optical depth/dust opacity	Dimensionless	5.8

ORCID iDs

Kate Pattle  <https://orcid.org/0000-0002-8557-3582>
 Shih-Ping Lai  <https://orcid.org/0000-0001-5522-486X>
 Tetsuo Hasegawa  <https://orcid.org/0000-0003-1853-0184>
 Jia-Wei Wang  <https://orcid.org/0000-0002-6668-974X>
 Ray S. Furuya  <https://orcid.org/0000-0003-0646-8782>
 Derek Ward-Thompson  <https://orcid.org/0000-0003-1140-2761>
 Pierre Bastien  <https://orcid.org/0000-0002-0794-3859>
 Simon Coudé  <https://orcid.org/0000-0002-0859-0805>
 Chakali Eswaraiah  <https://orcid.org/0000-0003-4761-6139>
 Lapo Fanciullo  <https://orcid.org/0000-0001-9930-9240>
 James di Francesco  <https://orcid.org/0000-0002-9289-2450>
 Thiem Hoang  <https://orcid.org/0000-0003-2017-0982>
 Gwanjeong Kim  <https://orcid.org/0000-0003-2011-8172>
 Woojin Kwon  <https://orcid.org/0000-0003-4022-4132>
 Chang Won Lee  <https://orcid.org/0000-0002-3179-6334>
 Sheng-Yuan Liu  <https://orcid.org/0000-0003-4603-7119>
 Tie Liu  <https://orcid.org/0000-0002-5286-2564>
 Masafumi Matsumura  <https://orcid.org/0000-0002-6906-0103>
 Takashi Onaka  <https://orcid.org/0000-0002-8234-6747>
 Sarah Sadavoy  <https://orcid.org/0000-0001-7474-6874>
 Archana Soam  <https://orcid.org/0000-0002-6386-2906>

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