Identification of a Group III CEMP-no Star in the Dwarf Spheroidal Galaxy Canes Venatici I

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Abstract

CEMP-no stars, a subclass of carbon-enhanced metal-poor (CEMP) stars, are one of the most significant stellar populations in galactic archeology, because they dominate the low end of the metallicity distribution function, providing information on the early star formation and chemical-evolution history of the Milky Way and its satellite galaxies. Here we present an analysis of low-resolution ($R \sim 1800$) optical spectroscopy for a CEMP giant, SDSS J132755.56+333521.7, observed with the Large Binocular Telescope (LBT), one of the brightest ($g \sim 20.5$) members of the classical dwarf spheroidal galaxy, Canes Venatici I (CVn I). Many CEMP stars discovered to date have very cool effective temperatures ($T_{\text{eff}} < 4500$ K), resulting in strong veiling by molecular carbon bands over their optical spectra at low/medium spectral resolution. We introduce a technique to mitigate the carbon-veiling problem to obtain reliable stellar parameters, and validate this method with LBT low-resolution optical spectra of the ultra-metal-poor ([Fe/H] $= -4.0$) CEMP-no dwarf, G 77–61, and seven additional very cool CEMP stars, which have published high-resolution spectroscopic parameters. We apply this technique to the LBT spectrum of SDSS J132755.56+333521.7. We find that this star is well described with parameters $T_{\text{eff}} = 4530$ K, log $g = 0.7$, [Fe/H] $= -3.38$, and absolute carbon abundance $A(C) = 7.23$, indicating that it is likely the first Group III CEMP-no star identified in CVn I. The Group III identification of this star suggests that it is a member of the extremely metal-poor population in CVn I, which may have been accreted into its halo.

Unified Astronomy Thesaurus concepts: Metallicity (1031); Carbon stars (199); Chemical abundances (224); Chemically peculiar stars (226); Dwarf galaxies (416); Population II stars (1284); Spectroscopy (1558)

1. Introduction

The nature of the first generation of stars, in particular, the first-star initial mass function (FIMF) and first-star nucleosynthesis pathways, provide crucial information for understanding the first-star-forming environments and early Galactic chemical evolution. While constraining the FIMF remains a challenge, our understanding of first-star nucleosynthesis has been advanced through studies of their likely direct descendants, the so-called CEMP-no stars ([C/Fe] $\geq +0.7$ and [Ba/Fe] $\leq 0.0$), a subclass of carbon-enhanced metal-poor stars (CEMP; Beers & Christlieb 2005; Aoki et al. 2007; Hansen et al. 2016a; Placco et al. 2016; Yoon et al. 2016; Aguado et al. 2018; Ezzeddine et al. 2019; Frebel et al. 2019; Yoon et al. 2019).

CEMP-no stars exhibit overabundances of carbon but subsolar abundance ratios of neutron-capture elements. Based on a variety of studies, (e.g., Yong et al. 2013; Aoki et al. 2018), a substantial fraction of extremely metal-poor (EMP) [Fe/H] $< -3.0$ and more than 50% of ultra-metal-poor (UMP) [Fe/H] $< -4.0$ CEMP-no stars also exhibit overabundances of light elements such as N, O, Na, Mg, Al, and Si, which may be a characteristic signature of first-star nucleosynthesis (Aoki et al. 2002b; Meynet et al. 2010; Nomoto et al. 2013; Choplin et al. 2017; Aoki et al. 2018).

Recently, Yoon et al. (2016) demonstrated that halo CEMP-no stars can be subdivided into at least two groups, based on their morphological distinction in the Yoon–Beers $A(C)^{6}–[\text{Fe/H}]$ diagram. The Group II CEMP-no stars exhibit a strong correlation between $A(C)$ and [Fe/H], indicating formation in environments where progenitor stars simultaneously produced both carbon and iron. In contrast, the progenitors of the Group III CEMP-no stars appear to have produced carbon independently of iron. Similar bifurcated behaviors between Group II and III CEMP-no stars are found in the $A(\text{Na})–A(C)$ and $A(\text{Mg})–A(C)$ spaces, along with the recently explored $A(\text{Ba})–A(C)$ space (Yoon et al. 2019). These chemically distinct behaviors strongly suggest the existence of multiple nucleosynthesis pathways for the formation of CEMP-no stars. Hence, recent theoretical studies have investigated different explanations for the formations of the bifurcated CEMP-no stars, such as different cooling channels (carbon dust grains versus silicate dust grains; Chiaki et al. 2017), different pollution/metall-enrichment pathways (external versus internal enrichments; Chiaki et al. 2018; Chiaki & Wise 2019), or inhomogeneous metal mixing of their birth clouds (Hartwig & Yoshida 2019).

Though some UMP CEMP-no stars are confined close to the Milky Way’s plane, within 3 kpc (Sestito et al. 2019; J. Yoon et al. 2020, in preparation), CEMP-no stars in the halo exhibit kinematics that suggest their dominant association with the outer-halo population of the Milky Way (e.g., Carollo et al. 2014; Lee et al. 2017; Yoon et al. 2018a; Lee et al. 2019). We note that Hansen et al. (2019) reported that their kinematics study of a sample of CEMP-no stars does not necessarily support...
this idea; their inference was based, however, on a rather small sample size (~30). The halo CEMP-no stars are likely to have been accreted from their birthplaces, dark-matter-dominated low-mass mini-halos (e.g., Salvadori et al. 2015; Amorisco 2017; Starkenburg et al. 2017), that are often taken to be the site of first-galaxy formation. The accretion origin of the halo CEMP-no stars has been supported by various studies asserting their association with satellite dwarf galaxies in the Milky Way (e.g., Frebel & Norris 2015; Starkenburg et al. 2017; Spitler et al. 2018). Most recently, Yoon et al. (2019) demonstrated the existence of a similar bifurcated behavior of CEMP-no Groups in the Yoon–Beers diagram among the sample of CEMP-no stars found in the ultra-faint dwarf (UFD) satellite galaxies and classical dwarf spheroidal (dSph) galaxies, providing additional strong evidence for the accretion hypothesis.

The discovery of large numbers of halo CEMP-no stars has been limited by the need for a measurement of [Ba/Fe], which requires time-consuming moderate- to high-resolution spectroscopy. Yoon et al. (2016) devised an alternative approach, based on the absolute carbon abundance, A(C), which is readily measured at low resolution, and capable of effectively (with a success rate of ~90%) distinguishing CEMP-no stars from CEMP-s stars, whose carbon and barium overabundances are thought to originate from mass transfer from their asymptotic giant branch binary companion, which is now a faint white dwarf (Suda et al. 2004; Herwig 2005; Lucatello et al. 2005; Komiya et al. 2007; Bisterzo et al. 2011; Starkenburg et al. 2014; Hansen et al. 2016b; Arensen et al. 2019; Lee et al. 2019). In particular, in the metallicity range where these two CEMP subclasses overlap, −3.5 ≤ [Fe/H] ≤ −2.0, application of this approach opens the opportunity to identify significantly greater numbers of CEMP-no stars.

However, there remains a challenge for the estimation of reliable stellar parameters from low- and medium-resolution spectroscopy, in particular for cooler stars (T_eff < 4500 K), due to the presence of strong molecular carbon bands throughout the optical spectral region of interest. In this work, we develop a technique to mitigate this limitation, both by assigning individual cool CEMP stars into their likely CEMP Groups in the A(C)–[Fe/H] diagram, and performing concurrent determinations of effective temperature, metallicity, and carbon abundance. We validate this method by deriving the stellar parameters of known very cool CEMP stars (T_eff < 4500 K) whose high-resolution spectroscopic parameters are available, including a new low-resolution spectrum of the canonical ultra-metal-poor (Group III CEMP-no) dwarf carbon star, G 77–61.

We employ this method to recently acquired low-resolution optical spectroscopic observations of a carbon giant, SDSS J132755.56+333521.7 (hereafter, SDSS J1327+3335), a member of the satellite dwarf galaxy Canes Venatici I (CV I), to derive its stellar parameters. SDSS J1327+3335 was found in close proximity to the center of CV I, which was originally revealed as a stellar overdensity in the North Galactic Cap using Sloan Digital Sky Survey Data Release 5 (SDSS; York et al. 2000; Yanny et al. 2009). Although the existence of this star was reported in the CV I discovery paper (Zucker et al. 2006), the poor quality of the original SDSS data, due to its faint magnitude (g ~ 20.5), rendered it unusable for reliable stellar-parameter estimates.

In Section 2, we describe the low-resolution (R ~ 1800) spectroscopic follow-up observations of G 77–61 and SDSS J1327+3335 and additional validation stars. We introduce our method for identifying the likely CEMP Group membership and derive their stellar parameters by implementing a Bayesian maximum likelihood estimation (MLE) spectral-matching procedure in Section 3. In Section 4, we validate this method by comparing our derived estimates for G 77–61 and the other seven CEMP stars with high-resolution spectroscopic results. We then apply this method to a low-resolution spectrum of SDSS J1327+3335. In Section 5, we confirm that SDSS J1327+3335 is a likely Group III CEMP-no star, based on its location in the A(C)–[Fe/H] space, and discuss its significance in terms of its host environment and accretion origin. Our conclusions are summarized in Section 6.

2. Data

In this section, we describe the various spectroscopic data made use of in this work.

2.1. Validation Stars

As a validation of the classification and parameter determination methodologies, we select known cool (T_eff < 4500 K) stars, previously studied with high-resolution spectroscopy, for which the metal and carbon abundances are prime examples of their CEMP Group classifications. There is an exception with a warmer Group III star with 4500 K < T_eff ≤ 5000 K. This selection includes several spectra for validation—six stars from the Hamburg/ESO survey (HES; Wisotzki et al. 1996; Christlieb et al. 2001), one spectrum from the HK objective-prism survey (Beers et al. 1985, 1992), and our new low-resolution spectrum of G 77–61, as described in the next subsection. These stars include four CEMP Group I stars (HE 1305+0132, HE 2221–0453, HE 0319–0215, and HE 0017+0055), two Group II stars (HE 1116–0634 and CS 30314–00677), and two Group III stars (HE 1310–0536 and G 77–61).

2.2. Low-resolution Spectroscopic Observations and Data Reduction

While we used existing low-resolution spectra from both the HES survey and HK survey for validation (typical signal-to-noise ratio, S/N, estimates were ~25 at the Ca II K line.), we conducted new low-resolution spectroscopic observations for G 77–61, along with our science target, SDSS J1327+3335. We obtained low-resolution spectroscopy of SDSS J1327+3335 with the Multi-object Double Spectrographs (MODS; Pogge et al. 2010) at the Large Binocular Telescope (LBT) on Mt. Graham, Arizona. For comparison, we also observed the canonical UMP dwarf carbon star G 77–61, with stellar parameters available from previous analysis of high-resolution spectroscopy (Plez & Cohen 2005). Below we provide a description of the observations and data reduction.

The optical spectra of SDSS J1327+3335 were obtained on 2018 May 21 and June 5. We used the blue grating covering the wavelength range 3200–5800 Å, with a dispersion of 0.5 Å pixel^{-1}, which provides a resolving power of R ~ 1800. The 0′′6 segmented long slit was used to obtain eighteen 20-minute exposures for SDSS J1327+3335. The spectra were flat-fielded, bias-subtracted, and bad columns fixed using

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7 There are only two known Group III stars with 4000 K ≤ T_eff ≤ 5000 K: G 77–61 (T_eff = 4000 K) and HE 1310–0536 (T_eff = 5000 K).

8 Yoon et al. (2016) noted that this star is located in the overlapping regions between Group II and Group III.

9 Our method can be implemented for spectra of S/N ~ 20 at 4000 Å and may be extendable to S/N ~ 10, and still produce acceptable results.
Cosmic rays were identified and removed using the L.A. Cosmic IRAF\(^{11}\) task (van Dokkum et al. 2012). The wavelength calibrations were carried out based on observations of Ar lamps taken during the same run with the standard LBT linelists. The sky subtraction, wavelength calibration, and one-dimensional extraction tasks were carried out using IRAF. The MODS 1 and MODS 2 spectra were coadded in the final step.\(^{12}\) Note that three of the 20-minute exposure MODS2 spectra from the June run were not coadded for the final analysis, due to a problem with their flat-field spectra. From the coaddition of 15 spectra (total exposure time 18,000 s), a final S/N of \(\sim 22\) per resolution element at 4000 Å was achieved.

The spectra of G 77–61 were obtained on 2018 February 9, and reduced with the same procedure described above, except that we used HgAr lamp spectra for the MODS2 data for wavelength calibration. The total exposure time was 3200 s. The resulting S/N obtained is \(\sim 160\) per resolution element at 4000 Å.

3. A Novel Method: Archetypal Classification and Spectral Matching

The determination of stellar parameters for cool \((T_{\text{eff}} < 4500\ \text{K})\), strongly carbon-enhanced stars is challenging for two primary reasons. First, large swaths of the optical spectral range

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\(^{11}\) IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.

\(^{12}\) Wavelength shifts of a few tenths of Å were found between the MODS1 and MODS2 spectra, of an unknown origin, hence we decided not to measure radial velocity estimates. These shifts do not influence our abundance results, because the observed spectra were corrected to the rest frame of the Balmer lines prior to all analyses conducted.
can be significantly depressed by the presence of molecular carbon features and metallic lines, including regions commonly used to approximate the continua of these spectra. This issue, referred to as carbon veiling, is exhibited in Figure 1, where continuum depression is seen for cooler atmospheres, causing otherwise carbon-independent features in low-resolution spectra, such as the Ca II H and K lines, to exhibit a dependence on the carbon abundance. This veiling is also sensitive to the surface gravity of the star, and behaves distinctly for each of the three CEMP Groups. Consequently, the effective temperature, metallicity, and carbon abundance of a star need to be considered simultaneously during parameter determination, and should not be regarded as independent procedures. We remind the reader that the low- and medium-resolution spectra of CEMP stars often come from large-scale surveys, which are only approximately flux calibrated, if at all.

The second challenge is the ambiguous nature of spectrum normalization in the presence of significant carbon veiling, especially with regards to spectral matching. It is generally not known to what extent carbon veiling is influencing the pseudo-continuum of an observed spectrum during normalization and subsequent parameter determination. Whereas the normalization of observed spectra with strongly enhanced molecular band features proceeds in a manner that might be oblivious to the degree of carbon veiling, depending on the strength of carbon bands, spectral synthesis does not; the flux is representative of the underlying stellar atmosphere. Parameter determination is therefore only possible if both the observed and synthetic spectra have addressed carbon veiling in an equivalent fashion.

We attempt to resolve these issues in the following manner. First, we employ a normalization technique designed to accommodate both the observed spectra and our library of synthetic spectra, as described below. Then, we employ a two-step procedure to derive reliable estimates of [Fe/H] and A(C): (1) we develop a preliminary CEMP Group classification procedure based on archetypal stellar parameters, and (2) we implement an MLE technique for spectral matching, which takes into account both metal- and carbon-abundance sensitive features during determination of effective temperature, metallicity, and carbon abundance, to derive reliable stellar parameters.

### 3.1. Synthetic Spectra and Normalization

For all synthetic spectral matching, we made use of the synthetic (1D LTE) library described in Whitten et al. (2019); a brief description follows. We implemented a grid of model atmospheres computed with the MARCS code (Gustafsson et al. 2008), taking into account carbon enhancement in the atmosphere. The microturbulence velocities were assigned according to the prescription $\xi = -0.345 \times \log g + 2.225$, derived from a sample of high-resolution spectra. Synthetic spectra were generated from these model atmospheres using the Turbospectrum routine (Alvarez & Plez 1998), covering the wavelength range 3000–5000 Å. We assume the solar abundances of Asplund et al. (2009). Updated linelists and more detailed information about the grids can be found in Whitten et al. (2019). This library was incremented to an appropriate spectral resolution ($R = 2000$), and renormalized along with the observed spectra using the Gaussian Interpolation Spline Interpolation Continuum (GISIC) routine,14 in order to enable matching with the observed spectra. This routine implements a cubic spline interpolation of continuum regions determined from inflection points in the smoothed spectrum. We note that GISIC may be a useful tool for application to other large spectral samples, in particular where automated approaches are employed.

We first interpolate within this library to produce spectra across the range $T_{\text{eff}} = [4000, 5000]$ K, [Fe/H] = $[-4.5, -1.0]$, and [C/Fe] = $[-0.5, +4.5]$. Given the effective temperature range considered in this work, we assume both dwarf and giant classifications. For both classifications, surface gravities are assigned according to the effective temperature and metallicity, using stellar isochrones from the $Y^2$ collaboration (Demarque et al. 2004). An $\alpha$-element enhancement of [α/Fe] = +0.4—consistent with the halo stars (Ishigaki et al. 2013)—is assumed, with an age of 12 Gyr. It is expected that the luminosity class is known prior to classification and parameter determination. In the case that the luminosity class is not known, the methods discussed can be used to determine the most likely classification, by comparing the optimized likelihood functions for both dwarf and giant classifications.

### 3.2. Archetypal Classification

The distinct locations of the CEMP Groups in the A(C)–[Fe/H] space (Yoon et al. 2016) present an opportunity to determine the most likely CEMP Group classification prior to parameter determination, based on comparison with archetypal parameters associated with each group, as listed in Table 1. The archetypal parameters were chosen based on the crude midpoints of the CEMP Group ellipses of the Yoon–Beers diagram. Thus, we referred to the CEMP Group ellipses from Figure 1 of Yoon et al. (2016) for the halo stars and Figure 2 of Yoon et al. (2019) for the dwarf galaxy stars. This preliminary classification is not strictly required for the parameter determination—described in Section 3.3—as the routine is applied over the entire synthetic library range, regardless of the suggested CEMP Group classification. However, the CEMP Group archetype parameters are used to seed the initial values of the parameter determination, and therefore serve as a first guess of the final parameters. We note that because this initial Group classification is derived only based on comparison with the archetypal parameters in Table 1, it may differ from the final assignment, which should be determined based on its final stellar parameters.

When comparing to the CEMP Group archetype parameters, it is important to consider the galactic environment to which a given star belongs. Yoon et al. (2019) showed that, while the characteristic CEMP Groups are seen for stars in

### Table 1

<table>
<thead>
<tr>
<th>Group</th>
<th>[Fe/H]</th>
<th>[C/Fe]</th>
<th>A(C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MW Halo Stars</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Group I</td>
<td>$-2.5$</td>
<td>1.97</td>
<td>7.9</td>
</tr>
<tr>
<td>Group II</td>
<td>$-3.5$</td>
<td>0.97</td>
<td>5.9</td>
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<tr>
<td>Group III</td>
<td>$-4.3$</td>
<td>2.87</td>
<td>7.0</td>
</tr>
<tr>
<td>UFDs/dSphs Stars</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Group I</td>
<td>$-1.5$</td>
<td>1.07</td>
<td>8.0</td>
</tr>
<tr>
<td>Group II</td>
<td>$-3.0$</td>
<td>0.87</td>
<td>6.3</td>
</tr>
<tr>
<td>Group III</td>
<td>$-3.5$</td>
<td>2.37</td>
<td>7.3</td>
</tr>
</tbody>
</table>

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13 See https://www.sdss.org/dr12/spectro/sspp_changes/ for details.

14 https://pypi.org/project/GISIC/
UFD/dSph galaxies, a slight offset exists in the [Fe/H] versus $A(C)$ behavior between the UFD/dSph and halo CEMP-no stars. This offset is likely to be associated with less dilution of the nucleosynthetic products from the progenitor stars in UFDs/dSphs, due to their lower baryonic mass reservoirs compared with the birth mini-halos of the halo stars. We therefore proceed with the UFD/dSph parameters for SDSS J1327+3335, and utilize the halo archetypes for all validation halo stars considered in this work, according to Table 1.

We determine the classification likelihood, on the basis of the chi-squared statistic, for both the Ca II K line and CH G band,

$$\chi^2(f, E|\xi) = \sum_i \frac{(f_i - E_i)^2}{(\xi E_i)^2}. \quad (1)$$

Here, $f_i$ and $E_i$ are the normalized fluxes of the observed and synthetic spectra, respectively, where $i$ represents each data point in the wavelength range considered, as shown in Table 2. The uncertainty used as the denominator in Equation (1) is determined as $\xi E_i$, where $\xi$ is the inverse of the S/N, $\xi = 1/(S/N)$, for each spectral feature, corresponding to a percent uncertainty ($\xi \in (0, 1)$). The reason we introduce the inverse S/N, $\xi$, is to derive an uncertainty on the normalized flux. We discuss the formal estimation of $\xi$ in Section 3.3. For preliminary classification, this value is determined separately for Ca II K and the CH G band, using the average S/N within the sidebands listed in Table 2.

We consider the likelihood of each class as the product of the $\chi^2$-distribution probability density function for each feature:

$$L(\chi^2_{\text{Ca II}}, \chi^2_{\text{CH}}|\nu_{\text{Ca II}}, \nu_{\text{CH}}) = \rho(\chi^2_{\text{Ca II}}; \nu_{\text{Ca II}}) \cdot \rho(\chi^2_{\text{CH}}; \nu_{\text{CH}}). \quad (2)$$

Here, $\rho$ is the $\chi^2$ probability distribution, and $\nu$ is the degrees of freedom, ($n - 1$), for the spectral region of interest. The product of the $\chi^2$ likelihood is used as a means of mitigating the relative difference in wavelength range between the Ca II K and the CH G band features.

It is important to consider the bandwidth over which the $\chi^2$ value is estimated. In general, the greater the absorption line, the larger the bandwidth should be, in order to best evaluate the characteristics of the feature. For the Ca II K line, we therefore implement the band-switching scheme developed by Beers et al. (1990) for the KP equivalent-width estimator:

$$\Delta \lambda_{\text{Ca II}} = \begin{cases} [3930.7, 3936.7] \text{Å} & \text{if } K_6 \leq 2 \text{Å}, \\ [3927.7, 3939.7] \text{Å} & \text{if } K_6 \geq 2, K_{12} \leq 5 \text{Å}, \\ [3924.7, 3942.7] \text{Å} & \text{if } K_{12} > 5 \text{Å} \end{cases}. \quad (3)$$

### Table 2

<table>
<thead>
<tr>
<th>Feature</th>
<th>Blue Sideband (Å)</th>
<th>Line Band (Å)</th>
<th>Red Sideband (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ca II K</td>
<td>[3884, 3923]</td>
<td>[3905, 4045]</td>
<td></td>
</tr>
<tr>
<td>CH G</td>
<td>[4000, 4080]</td>
<td>[4100, 4150]</td>
<td>[4200, 4250]</td>
</tr>
<tr>
<td>C$_2$</td>
<td>(4737 Å)</td>
<td>(4710, 4750)</td>
<td>(4760, 4820)</td>
</tr>
</tbody>
</table>

Figure 2. CEMP Group archetype classification (UFD/dSph) of SDSS J1327+3335. The log-likelihood ($\mathcal{L}$, Equation (2)) is determined across the temperature range $T_{\text{eff}} = [4000, 5000]$ K for each CEMP Group, using the [Fe/H] and $A(C)$ archetype parameters, according to Table 1. GI, GII, and GIII in the legend represent CEMP Groups I, II, and III, respectively. The vertical dashed line represents the photometric temperature estimate, $T_{\text{phot}}$. The gray shaded region shows the uncertainty ($\pm 150$ K) of the temperature estimate.

Here, $K_6$ and $K_{12}$ correspond to pseudo-equivalent widths of the Ca II K line,

$$K_n = \int_{\lambda_0-n/2}^{\lambda_0+n/2} (1 - f(\lambda)) d\lambda, \quad (4)$$

where $\lambda_0$ is the rest-frame wavelength of the Ca II K line, 3933.7 Å.

We compute the likelihood, $\mathcal{L}(\chi^2_{\text{Ca II}}, \chi^2_{\text{CH}})$, for each group archetype across the effective temperature range $T_{\text{eff}} = [4000, 5000]$ K, according to the archetype parameters listed in Table 1. The likelihood of each classification is considered against the photometric temperature estimate, determined using implementations of the Infrared Flux Method (IRFM)\textsuperscript{15} from Berg eject et al. (2001), González Hernández and Bonifacio (2009), and Casagrande et al. (2010). As 2MASS photometry was not available for SDSS J1327+3335, we make use of the IRFM\textsuperscript{16} adopted for the SEGUE Stellar Parameter Pipeline (Lee et al. 2008a, 2008b; Allende Prieto et al. 2008), for which we determine an effective temperature of 4113 K. The resulting log-likelihoods (log $\mathcal{L}$) of SDSS J1327+3335 and the six validation stars are shown in Figure 2 and Figure A1 in the Appendix, respectively. We discuss the detailed results in Section 4.

#### 3.3. MLE Parameter Determination

Here we describe the method developed to produce estimates of $T_{\text{eff}}$, [Fe/H], and [C/Fe]. Best-fit parameters are determined for our low-resolution spectra using maximum likelihood spectral matching, for which we explore our likelihood function by sampling over the $T_{\text{eff}}$, [Fe/H], and [C/Fe] parameter space of our synthetic library using the Python module emcee (Foreman-Mackey et al. 2013). This module is\textsuperscript{15} The final photometric temperature was derived by averaging temperature estimates from these three methods. We note that these methods may not be valid for some EMP/UMP CEMP stars, in particular, those with very strong carbon enhancement. However, we used this estimate only for the preliminary CEMP Group assignment, and as an input parameter for the MCMC method to derive the final value.

\textsuperscript{16} http://www.sdss3.org/dr10/spectro/sspp_irfm.php

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*The Astrophysical Journal, 894(7) (17pp), 2020 May 1*

Yoon et al.
based on Goodman & Weare’s affine invariant Markov Chain Monte Carlo (MCMC) routine (Goodman & Weare 2010). We emphasize that, while the preliminary CEMP Group classification from Section 3.2 motivates the final assignment, the parameter determination is nevertheless conducted over the entire synthetic grid range: \( T_{\text{eff}} = [4000, 5000] \, K, [\text{Fe}/\text{H}] = [-4.5, -1.0], \) and \([\text{C}/\text{Fe}] = [-0.5, +4.5]\). The parameter determination method is essentially independent of the Group classification, with the exception that the initial values for the MCMC are set to the archetype parameters corresponding to the stars’ CEMP Group class.

We utilize three spectral features for parameter determination: the Ca II K line \((\lambda_0 = 3933.7 \, \AA)\), the CH G band, and the C2 Swan band, located at 4737 \( \AA \) (Johnson & Merton 1927; Christlieb et al. 2001; Côté et al. 2019). While the Ca II K and CH G band are sufficient for the preliminary classification, it was found that the CH G band saturates at \( \Delta T(\text{C}) \gtrsim 7.5 \). As this is only problematic for Group I stars, the C2 Swan band\(^{17}\) is utilized—in addition to the CH G band—when the pseudo-equivalent width of the CH G band exceeds 40 \( \AA \), as determined via the line band given in Table 2. Consideration of the relative strengths of these features—integral to our MLE procedure—is reminiscent of the line-depth ratio method shown to be effective for determinations of effective temperature (Kovtyukh 2007), where flux ratios of parameter-sensitive features are analogous to the difference in logarithmic likelihoods corresponding to each feature.

### 3.3.1. \( \chi^2 \) Estimation

We estimate the \( \chi^2(f|E, \xi) \) of the model fit for each feature, using the line bands listed in Table 2 for the Ca II K line, CH G band, and C2 Swan band (4737 \( \AA \)). We consider the following truncated log-\( \chi^2 \) probability distribution function (pdf) for each absorption feature:

\[
\ln p(\chi^2; \nu) = \left( \frac{\nu}{2} - 1 \right) \ln \chi^2 - \frac{\nu}{2} \chi^2.
\]

Here, \( \nu \) is the degrees of freedom associated with each \( \chi^2 \) value. We neglect the additional terms in the \( \chi^2 \) pdf that depend only on \( \nu \), as they are computationally cumbersome and do not influence the resulting posterior likelihood distributions. However, \( \chi^2 \) is a function of the assumed inverse \( S/N, \xi \). We include the estimate of inverse \( S/N \) for each feature as additional parameters to be determined during optimization. For convenience, we denote the set \( \xi = (\xi_{\text{Ca II}}, \xi_{\text{CH}}, \xi_{\text{C2}}) \), \( \chi^2 = (\chi^2_{\text{Ca II}}, \chi^2_{\text{CH}}, \chi^2_{\text{C2}}) \), and \( \nu = (\nu_{\text{Ca II}}, \nu_{\text{CH}}, \nu_{\text{C2}}) \).

We consider the logarithm of the same likelihood used in the classification procedure, Equation (2). However, we include the C2 Swan band likelihood in the event that the pseudo-equivalent width of the CH G band exceeds 40 \( \AA \). For the set of stellar parameters, \( \theta = (T_{\text{eff}}, [\text{Fe}/\text{H}], [\text{C}/\text{Fe}]), \xi \), the log-likelihood function is

\[
\ln L(\theta|\chi^2, \nu) = \ln p(\chi^2_{\text{Ca II}}; \nu_{\text{Ca II}}) + \ln p(\chi^2_{\text{CH}}; \nu_{\text{CH}}) + \ln p(\chi^2_{\text{C2}}; \nu_{\text{C2}}).
\]

This logarithmic likelihood function is then sampled across the parameter space of the synthetic library, \( T_{\text{eff}} = [4000, 5000] \, K, [\text{Fe}/\text{H}] = [-4.5, -1.0], \) and \([\text{C}/\text{Fe}] = [-0.5, +4.5] \).

#### 3.3.2. MLE Priors

For effective temperature, we assume a Gaussian prior about the photometric temperature estimate, \( T_{\text{phot}} \), for which the standard deviation is set to \( \sigma(T_{\text{phot}}) = 250 \, K \). Priors for \( [\text{Fe}/\text{H}] \) and \([\text{C}/\text{Fe}] \) are taken to be uniform, within the range of the synthetic library. The inverse \( S/N \) of each feature—\( \xi_{\text{Ca II}}, \xi_{\text{CH}}, \) and \( \xi_{\text{C2}} \)—corresponds to a percent uncertainty, \( \xi \in (0, 1) \). We therefore implement a beta distribution prior for each, where the mean and variance in each case are motivated by the \( S/N \) estimated from the observed spectrum, using the sidebands in Table 2 and assuming Poisson-dominated noise. This is equivalent to setting the \( \alpha \) and \( \beta \) terms in the beta distribution.

The logarithm of the prior distribution, \( \rho(\theta) \), is as follows:

\[
\ln \rho(\theta|\alpha, \beta) = \text{Uniform}(-4.5 \leq [\text{Fe}/\text{H}] \leq -1.0) + \text{Uniform}(-0.5 \leq [\text{C}/\text{Fe}] \leq +4.5) + \text{Uniform}(4000 \leq T_{\text{eff}}(\text{K}) \leq 5000) - \frac{1}{2} \ln 2\pi\sigma(T_{\text{phot}})^2 - \frac{1}{2} \left( \frac{T_{\text{eff}} - T_{\text{phot}}}{\sigma(T_{\text{phot}})} \right)^2 + \sum_{j=1}^{3} \ln \rho_3(\xi_j, \alpha_j, \beta_j).
\]

Here we use the index \( j \) to denote the three spectral features of Ca II K, CH G band, and C2 Swan band. We remind the reader that the parameters associated with the C2 Swan band, \( \xi_{\text{C2}}, \alpha_{\text{C2}}, \) and \( \beta_{\text{C2}} \), are only included when the pseudo-equivalent width of the CH G band exceeds 40 \( \AA \). Otherwise, only Ca II K and the CH G band are considered.

We determine the parameters \( T_{\text{eff}}, [\text{Fe}/\text{H}], [\text{C}/\text{Fe}], \xi \), which maximize the likelihood, \( \ln L(\theta|\chi^2, \nu) \), by maximizing the posterior distribution of each parameter via kernel density estimation. The width of the Gaussian kernel was determined in each case by the standard deviation of the posterior distribution in question, from which the standard deviation is reported as the uncertainty estimate, \( \sigma(\theta) \), where \( \theta \) represents the set of the stellar parameters \( (T_{\text{eff}}, [\text{Fe}/\text{H}], [\text{C}/\text{Fe}], \xi) \).

As seen in Table 3, the uncertainties reported for estimates of \( A(\text{C}) \) are always larger than the \([\text{Fe}/\text{H}] \) estimates. This is due to the format of the spectral library being in terms of \([\text{Fe}/\text{H}] \) and \([\text{C}/\text{Fe}] \), which requires the \( A(\text{C}) \) to be determined from both. The uncertainty is then the quadrature sum of the \([\text{Fe}/\text{H}] \) and \([\text{C}/\text{Fe}] \) uncertainty. The uncertainties of ourstellar abundance parameters, determined in this manner, are generally on the scale of the synthetic spectral resolution (0.25 dex). In the event that they are significantly smaller, it is advised to consider the grid resolution as the primary uncertainty estimate. Uncertainties are driven largely by correlations in the stellar parameters, for instance the covariance of \( T_{\text{eff}} \) and \([\text{Fe}/\text{H}] \) seen for SDSS J1327+3335 in Figure 3. Additionally, bimodalities in the posterior distributions tend to increase the standard deviations reported as the uncertainties. In such cases, care should be given to the selection of the appropriate mode in the posterior distribution, which maximizes the likelihood.

\(^{17}\)We do not expect the \( G \) band and the Swan band to necessarily yield the same results, due to differences in their molecular line formation. Carbon will be used to form CO, then CH and CN, and finally C2. Thus, the formation of the C2 bands may differ, depending on the presence and abundance of O, N, and H (Ting et al. 2018; Franchini et al. 2020). A full analysis is beyond the scope of our current approach. In our analysis, it is apparent that the abundances from the CH and C2 bands do not agree when the CH line is unsaturated (around \( A(\text{C}) < 7.5 \)). Thus, we included the Swan band as well, only when the CH band is saturated for the Group I stars.
Table 3
CEMP Group Validation Stars

<table>
<thead>
<tr>
<th>Identifier</th>
<th>$T_{\text{eff}}$ (K)</th>
<th>log $g$</th>
<th>$[$Fe/H$]$</th>
<th>$A(C)^a$</th>
<th>$T_{\text{eff}}$ (K)</th>
<th>log $g$</th>
<th>$[$Fe/H$]$</th>
<th>$A(C)^a$</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>This Work</td>
<td></td>
<td>Literature Values from High-resolution Spectroscopy</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Group I</td>
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<td></td>
</tr>
<tr>
<td>HE 1305+0132</td>
<td>4496 ± 130</td>
<td>0.66 ± 0.38</td>
<td>−2.90 ± 0.11</td>
<td>8.28 ± 0.19</td>
<td>4462 ± 100</td>
<td>0.80 ± 0.30</td>
<td>−2.55 ± 0.50</td>
<td>8.57 ± 0.11</td>
<td>Schuler et al. (2007)</td>
</tr>
<tr>
<td>HE 2221–0453</td>
<td>4514 ± 170</td>
<td>0.91 ± 0.42</td>
<td>−2.48 ± 0.11</td>
<td>8.34 ± 0.12</td>
<td>4400$^b$</td>
<td>0.40$^b$</td>
<td>−2.27 ± 0.31</td>
<td>8.00 ± 0.31</td>
<td>Aoki et al. (2007)</td>
</tr>
<tr>
<td>HE 0319–0215</td>
<td>4439 ± 299</td>
<td>0.51 ± 0.60</td>
<td>−2.89 ± 0.25</td>
<td>8.15 ± 0.30</td>
<td>4448$^b$</td>
<td>0.62$^b$</td>
<td>−2.30$^b$</td>
<td>8.13$^b$</td>
<td>Hansen et al. (2016b)$^c$</td>
</tr>
<tr>
<td>HE 0017+0055</td>
<td>4370 ± 48</td>
<td>0.25 ± 0.13</td>
<td>−3.36 ± 0.17</td>
<td>7.45 ± 0.28</td>
<td>4146$^b$</td>
<td>0.41$^b$</td>
<td>−2.80$^b$</td>
<td>7.62$^b$</td>
<td>Hansen et al. (2016b)$^c$</td>
</tr>
<tr>
<td>Group II</td>
<td></td>
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<td></td>
</tr>
<tr>
<td>HE 1116–0634</td>
<td>4722 ± 87</td>
<td>1.24 ± 0.26</td>
<td>−3.32 ± 0.06</td>
<td>5.16 ± 0.09</td>
<td>4400$^{a,d}$</td>
<td>0.1$^b$</td>
<td>−3.73</td>
<td>4.78 ± 0.20</td>
<td>Hollek et al. (2011)</td>
</tr>
<tr>
<td>CS 30314–0067</td>
<td>4141 ± 287</td>
<td>−0.20 ± 0.51$^e$</td>
<td>−2.71 ± 0.04</td>
<td>6.69 ± 0.09</td>
<td>4400 ± 100</td>
<td>0.7 ± 0.3</td>
<td>−2.85 ± 0.18</td>
<td>6.20 ± 0.18</td>
<td>Aoki et al. (2002a)</td>
</tr>
<tr>
<td>CS 30314–0067</td>
<td>4320 ± 12$^d$</td>
<td>0.50 ± 0.10</td>
<td>−3.01 ± 0.06$^e$</td>
<td>6.80$^d$</td>
<td>Roederer et al. (2014)</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Group III</td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>HE 1310–0536</td>
<td>4904 ± 152</td>
<td>1.66 ± 0.36</td>
<td>−4.20 ± 0.22</td>
<td>6.69 ± 0.32</td>
<td>5000±100</td>
<td>1.9±0.30</td>
<td>−4.15±0.30</td>
<td>6.64±0.23</td>
<td>Hansen et al. (2015)</td>
</tr>
<tr>
<td>G 77–61</td>
<td>4174 ± 120</td>
<td>5.07 ± 0.15$^f$</td>
<td>−4.36 ± 0.28</td>
<td>7.17 ± 0.35</td>
<td>4000 ± 200</td>
<td>5.05$^e$</td>
<td>−4.00 ± 0.15</td>
<td>7.0 ± 0.1</td>
<td>Plez &amp; Cohen (2005)</td>
</tr>
</tbody>
</table>

Notes.

$^a$ Reported value from the reference, not evolution corrected.

$^b$ Uncertainty was not reported.

$^c$ Hansen et al. (2016b) observed the star with the FIES spectrograph at the 2.5 m Nordic Optical Telescope. The resolving power of each spectrum is $R \sim 46,000$, and the average $S/N$ is $\sim$10, thus they coadded multiple spectra of a given star to improve the $S/N$.

$^d$ Originally reported spectroscopic temperature estimate.

$^e$ Hansen et al. (2016b) observed the star with the FIES spectrograph at the 2.5 m Nordic Optical Telescope. The resolving power of each spectrum is $R \sim 46,000$, and the average $S/N$ is $\sim$10, thus they coadded multiple spectra of a given star to improve the $S/N$.

$^f$ [M/H], the originally reported metallicity, was derived by using only eight Fe II lines. We note that other typical metal-poor studies adopt metallicity based on Fe I lines. When considering 91 Fe I lines of this star, the metallicity, [Fe/H], is $-3.31 \pm 0.06$.

$^g$ Value derived using the 2017 version of MOOG (I. Roederer 2019, private communication).

$^h$ Represents values determined from $Y^2$ isochrone interpolation; fits were performed within log $g = [0.0, 5.0]$, where values above or below this range were assigned log $g = 5.0$ or log $g = 0.0$, respectively.
Bimodality was seen to be common in the instances where the inverse \( S/N \), \( \xi \), was incorrectly determined for one or more of the spectral features. This can lead to mismanagement and overprioritization of the features with the smallest \( \xi \). For this reason, values of \( \xi \) that are motivated by preliminary knowledge of the spectral \( S/N \) are typically preferred over an automated determination of the optimal \( \xi \) values that maximize the likelihood function.

Surface gravity estimates are assigned via the \( Y^2 \) isochrone interpolation, using the values of \( T_{\text{eff}} \) and \([\text{Fe/H}]\), determined from the maximum likelihood spectral matching, along with the luminosity class. To estimate the uncertainty in the surface gravity, we iteratively sample the posterior distributions of \( T_{\text{eff}} \) and \([\text{Fe/H}]\) to build a distribution of gravity estimates.

4. Results

4.1. Validation of the Methodology

We remind the reader of the two-step methodology—the assignment of likely CEMP Group classification using the archetype parameters and the parameter determination using the MCMC technique. The results of the CEMP Group likelihoods using the archetype parameters for the validation stars are shown in Figure A1 in the Appendix. These likelihood figures include the corresponding photometric temperature estimate (black dashed line) and its uncertainty of \( \pm 150 \text{ K} \) (shaded region). Our classification technique indeed well predicts their original Group classification assigned in Yoon et al. (2016) for all of the validation stars. We note that the Group II likelihood was
exceedingly low for all Group I validation stars, and thus we
excluded them from the figure, in order to prioritize discrimina-
tion between Group I and III classification.

Stellar parameters $T_{\text{eff}}, \text{[Fe/H]}, \text{and } [C/Fe]$ were determined
along with the corresponding $A(C)$ value for each of the
validation stars using the maximum-likelihood-method spectral-
matching procedure, as outlined in Section 3.3. The resulting
parameters, including surface gravity, are listed in Table 3, along
with those determined from previous high-resolution spectro-
scopic studies for comparison. The corresponding model fits are
shown in Figures A2 and A3 in the Appendix.

In general, our estimates from this technique are reasonably
consistent with the high-resolution spectroscopic values for the
validation stars. A few exceptions are explained in more detail
below.

Determinations of effective temperature agree with previous
estimates within $\pm 200 \text{ K}$, which is a typical observational
error, with the exclusion of HE 1116–0634, which differs from
the Hollek et al. (2011) estimate by $+322 \text{ K}$. However, Hollek
et al. (2011) adopted a “pseudo-spectroscopic” temperature for
HE 1116–0634, which was obtained by applying their mean
systematic offset between their spectroscopic and photometric
estimates, $-225 \text{ K}$, from its photometric estimate. Their
photometric temperature, $4625 \text{ K}$, is consistent with our
estimate ($4722 \text{ K}$) within the observational error. Estimates of
metallicity and carbon abundance ratios for most of the
validation stars generally agree within $\pm 0.4 \text{ dex}$. However, two
of the Group I validation stars, HE 0319–0215 and HE 0017
+0015, studied by Hansen et al. (2016b), appear to have
metallicity overestimated by $\sim +0.6 \text{ dex}$, while the $A(C)$ of
these two stars are consistent, which is reasonable, considering
the similar temperature estimates between our results and
theirs. We note that these two stars were observed for radial-
velocity monitoring, thus the average $S/N$ is about 10,
resulting in coaddition of the multiple spectra to improve their
$S/N$. Thus, the Hansen et al. (2016b) values are not necessarily
better estimates than our results. For CS 30314–0067, there are
two high-resolution spectroscopic studies by Aoki et al.
(2002a) and Roederer et al. (2014). While both of the results
are reasonably consistent with ours, the $A(C)$ result of Aoki
et al. (2002a) appears to be underestimated by $\sim -0.5 \text{ dex}$
compared to our result. Since the uncertainty estimate in the
surface gravity is driven entirely by the uncertainty in $T_{\text{eff}}$ and
$[\text{Fe/H}]$, large uncertainties in $T_{\text{eff}}$ can result in correspondingly
large uncertainties in $\log g$. This is seen particularly for
HE 0319–0215 and CS 30314–0067 in Table 3, both of which
have $T_{\text{eff}}$ uncertainties in excess of 250 K and, consequently,$\log g$ uncertainties over 0.5 dex. In the event that the
photometric temperature is better constrained, either by
including additional temperature calibrations or superior
photometric estimates, the effective temperature determined
during spectral matching can be better constrained, and thus the
surface gravity uncertainty is reduced by extension.

4.2. Application to SDSS J1327+3335

We apply the same methodology to our science target,
SDSS J1327+3335, taking UFDs/dSphs archetype parameters
for initial Group classification. There is a clear preference for
CEMP Group III classification across the entire effective
temperature range $T_{\text{eff}} = [4000, 5000] \text{K}$ as seen in Figure 2.
The photometric temperature estimate of $4113 \text{ K}$ for
SDSS J1327+3335 indicates that this star is a Group III star.
We remind that its final CEMP Group classification should be
determined based on the final stellar parameters and its location
in the CEMP A(C)–[Fe/H] morphology, as evidenced in
Section 5.

The posterior distributions for $T_{\text{eff}}, \text{[Fe/H]}, \text{and } [C/Fe]$,
determined from MCMC maximum likelihood spectral match-
ing, are shown in Figure 3. We determine the optimal
parameters to be $T_{\text{eff}} = 4530 \pm 145 \text{ K}$, $\text{[Fe/H]} = -3.38 \pm 0.07$, $\text{[C/Fe]} = +2.18 \pm 0.22$, corresponding to $A(C) = 7.23 \pm 0.23$.
We note that this temperature is higher than the
photometric estimate obtained from $g - i$ color, $4113 \text{ K}$.
However, photometric temperatures for carbon-enhanced stars
—particularly those produced from bluer filters—are quite
often underestimated, due to the strong carbon bands across the
optical spectrum. An effective temperature and metallicity of
$T_{\text{eff}} = 4530 \text{ K} \text{ and } [\text{Fe/H}] = -3.38 \text{ correspond to a surface}
gravity of } \log g = 0.7 \text{, determined by the } Y^2 \text{ isochrone}
interpolation. We estimate the uncertainty in the surface gravity
determination by sampling the posterior distributions of $T_{\text{eff}}$ and
$[\text{Fe/H}]$, the result of which is shown in Figure 4. The scatter in
surface gravity is largely driven by the scatter in the effective
temperature, resulting in an estimate of $\log g = 0.7 \pm 0.4$. The
best-fit normalized synthetic spectrum of SDSS J1327+3335 is
shown in Figure 5.
We can confirm the luminosity class of SDSS J1327+3335 as a giant based on its null parallax ($\pi = -0.3605 \pm 0.4190$ mas) and small proper motion ($\mu_\alpha = -0.567 \pm 0.568$ mas yr$^{-1}$, $\mu_\delta = 0.471 \pm 0.300$ mas yr$^{-1}$) from Gaia Data Release 2 (Gaia Collaboration et al. 2016, 2018; Arenou et al. 2018). We note that this star also possesses a radial velocity of $36 \pm 20$ km s$^{-1}$, commensurate with that of other members of the CVn I dwarf satellite (Zucker et al. 2006).

Since SDSS J1327+3335 is a late-type giant, it is clear that this star has gone through at least one dredge-up episode during its evolution. We attempt to recover the original carbon abundance from application of the carbon evolutionary correction calculator\textsuperscript{18} of Placco et al. (2014), obtaining a change in the carbon of $\Delta[C/Fe] = +0.28$ dex. The final corrected carbon abundance is $A(C) = 7.51$ ([C/Fe]$_c = +2.46$). The rest of our discussion below refers to these corrected abundances.

5. Discussion

CVn I is a distant, faint dwarf galaxy, with a heliocentric distance of $\sim$220 kpc (Zucker et al. 2006). Its absolute magnitude, $M_V \sim -7.9$, makes it a galaxy similar to the Draco and Ursa Minor dwarf spheroidals, but its half-light radius, $\sim$550 pc, is larger than the others. Therefore, various studies have noted that CVn I is likely a dSph, rather than a UFD galaxy (e.g., Simon 2019). The likely CVn I membership of SDSS J1327+3335 is not based on its spatial location, but also on its heliocentric radial velocity (consistent with the galaxy), in addition to the astrometric results noted above. However, since this star is very faint ($g \sim 20.5$) and strongly carbon enhanced, a metallicity determination was not available ($S/N < 2$ at 4000 Å and median $S/N \sim 7$ over the entire wavelength region of its SDSS spectrum). Even though there have been spectroscopic follow-up observations (Ibata et al. 2006; Martin et al. 2007; Simon & Geha 2007; Kirby et al. 2010; François et al. 2016) from which metallicity and [$\alpha$/Fe] abundances for many stars in CVn I (mean metallicity is $-1.98 \pm 0.01$ from Kirby et al. 2011) have been obtained, carbon-abundance estimates of the stars in this galaxy, including SDSS J1327+3335, have not been previously reported.

Figure 5 shows the Yoon–Beers diagram for CEMP stars found in dwarf satellite galaxies. We used the same sample of stars as Yoon et al. (2019), which includes both dSphs (Draco, Sextans, Sculptor, and Ursa Minor) and several UFDs (Bootes I, Reticulum II, Segue I, Tucana II, Pisces II, and Ursa Major II). Note that we did not draw an ellipse for Group I, because there is only one Group I star (from Segue I).

The location of SDSS J1327+3335 in the CEMP Group morphology shown in Figure 6 confirms that it is a CEMP Group III star. Confirmation of its CEMP-no status with a Ba abundance measurement, e.g., from higher-resolution data, is not yet available,\textsuperscript{19} but our classification appears quite likely, based on its A(C) and metallicity according to Yoon et al. (2019).

The Yoon–Beers diagram of the halo CEMP stars reveals a strong correlation between the Group III CEMP stars and CEMP-no stars, and the association of the Group I stars with the CEMP-s stars, with the exception of “anomalous” CEMP-no stars in the Group I region (Yoon et al. 2016). This distinction is also manifested in Figure 3 (the A(Ba)–A(C) diagram) of Yoon et al. (2019), which clearly shows that Group III CEMP-no stars are well separated ($\gtrsim$3.0 dex from the mean A(Ba)) from the CEMP-s stars. Hence, the characteristic CEMP Group morphology in the A(C)–[Fe/H] space can be used for a “first-approximation” diagnostic for identifying the likely nucleosynthetic origin of CEMP stars. There are several known EMP and many very metal-poor ([Fe/H] $< -2.0$) stars

\textsuperscript{18} https://vplacco.pythonanywhere.com/

\textsuperscript{19} The carbon-veiling problem is prevalent over the entire spectrum of SDSS J1327+3335, which is not flux calibrated, resulting in difficulties with the identification of the proper continuum. This prevents reliable spectral synthesis analysis of other important elemental abundances, such as Ba, for confirming this star’s nucleosynthetic origin based on the data in hand. In particular, due to quite strong N enhancement in the CN bands, even the strongest Ba II line at 4554 Å suffers from severe blending with the CN lines. We note that Norfolk et al. (2019) were able to carry out such an analysis for Ba from their approximately flux-calibrated, low-resolution LAMOST data by assuming that deviations in flux at 4554 Å are solely from the Ba enhancement. Since they did not report Ba measurements, it is not clear how to evaluate their synthesis of Ba for very cool stars with strong carbon enhancement such as our stars, which appears to be a minority of their sample.
in the CVn I galaxy (Kirby et al. 2010); thus, we expect to find more CEMP-no stars in this system once measurements of carbon abundance are completed (E. Kirby 2019, private communication).

According to Yoon et al. (2019), the classical dSph galaxies appear to possess only Group II CEMP-no stars, which may result from several causes: (1) The characteristically higher A(C) associated with Group III CEMP-no stars may have been diluted by the larger baryonic masses associated with dSph galaxies compared to UFD galaxies. (2) The additional production of iron associated with prolonged star formation histories in dSphs compared to UFDs (e.g., Tolstoy et al. 2009; Salvadori et al. 2015; de Bennassuti et al. 2017) may even reach levels where individual stars are not recognized as CEMP stars ([C/Fe] \textless 0.7). (3) A different class of nucleosynthetic origins such as spinstars or faint supernovae (Umeda & Nomoto 2003, 2005; Meynet et al. 2006, 2010; Frischknecht et al. 2012, 2016; Chiappini 2013; Nomoto et al. 2013; Tominaga et al. 2014; Maeder & Meynet 2015; Yoon et al. 2016; Choplin et al. 2017). (4) Differences in the original pollution pathways (internal versus external pollution, e.g., Smith et al. 2015; Chiaki et al. 2018; Chiaki & Wise 2019). (5) Differences in the available cooling agents (Group II: silicate-grain cooling versus Group III: carbon-grain cooling; see Chiaki et al. 2017) of the natal clouds could result in predominance of the Group II CEMP-no stars in the dSphs.

Thus, the Group III CEMP-no status of SDSS J1327+3335 is intriguing, and may indicate that CVn I might have had an unusual star formation history compared to other dSphs. Indeed, based on both Keck/DEIMOS spectroscopic and deep LBT photometric observations (Ibata et al. 2006; Martin et al. 2007; Kuehn et al. 2008; Martin et al. 2008), CVn I has been claimed to host two distinct stellar populations—an extended metal-poor population (−2.5 < [Fe/H] < −2.0) with hot kinematics and a more metal-rich population (−2.0 < [Fe/H] < −1.5) with a near-zero velocity dispersion, concentrated on its center, although this dichotomy has been challenged by a kinematic study using more than 200 stars (Simon & Geha 2007). Perhaps SDSS J1327+3335 is a member of the extremely metal-poor population in CVn I, which might have been accreted into its halo. Identification of additional Group II and III CEMP-no stars in this system should enable better understanding of the chemical-evolution and accretion history of the CVn I galaxy.

6. Conclusions

We have presented an analysis of low-resolution optical spectroscopy of SDSS J1327+3335 and G 77−61, taken with the LBT MODS spectrographs, and developed a novel methodology to analyze such challenging cool (T eff < 4500 K) CEMP stars. We identified the star SDSS J1327+3335 as the first likely Group III CEMP-no ([Fe/H] = −3.38, [C/Fe] = +2.46, and A(C) = 7.51) star in the CVn I dwarf satellite galaxy, using our archetypal classification—parameter determination methodology based on maximum likelihood spectral matching. This procedure was validated for each CEMP Group using spectra from the Hamburg/ESO survey, in addition to CS 30314−0067 and G 77−61, a well-known dwarf carbon star, all of which have published high-resolution analyses. The Group III CEMP-no classification for SDSS J1327+3335 appears to be unusual among CEMP-no stars from the dSphs, which are predominantly associated with Group II stars (Yoon et al. 2019). The apparently complex star formation history of this galaxy may be responsible. The association of CEMP-no Groups with a particular nucleosynthetic origin (and/or accretion origin) will provide information on both the chemodynamical assembly histories of individual dwarf galaxies and the halo system of the Milky Way.

We plan to apply our methodology to mitigate the effects of strong molecular carbon veiling, which complicates identification of the continuum around the region of the Ca H and K lines and the CH G band for other cool CEMP EMP/UMP candidates from: (1) our ongoing “Best and Farthest” survey (Yoon et al. 2018b), observing with LBT/MODS and Gemini/GMOS, (2) numerous other cool CEMP stars with strong carbon veiling observed during the course of follow-up spectroscopy over the past few decades of metal-poor candidates from the HK survey (e.g., Beers et al. 1992), (3) the list of CEMP candidates provided by Christlieb et al. (2008), and (4) very cool CEMP...
stars from the low-resolution spectroscopic surveys such as the SDSS, the AAOmega Evolution of Galactic Structure (AEGIS) survey (Yoon et al. 2018a), and the Large Sky Area Multi-Object Fiber Spectroscopic Telescope survey (LAMOST; Cui et al. 2012). These projects will also provide more validation stars and opportunities to improve the accuracy of our approach. This methodology can be widely applicable to numerous data from the future large moderate-resolution spectroscopic surveys such as the Dark Energy Spectroscopic Instrument (DESI; Levi et al. 2019) survey, the William Herschel Telescope Enhanced Area Velocity Explorer (WEAVE; Dalton et al. 2018), and 4MOST (de Jong et al. 2019). These efforts will allow us not only to expedite the discovery process of the most metal-poor stars, but also to calculate frequencies of CEMP Groups separately, and, in turn, provide insights regarding the shape of the FIMF.

We are currently preparing an open source Python package of our new methodology for public use. In the near future, we also plan to extend our synthetic spectral grid to include CEMP stars with even lower effective temperatures (to $T_{\text{eff}} = 3500$ K), in order to better address cooler stars than included in our present grid. Once these grids are available, the versatility of our methodology will extend to probe/constrain the low end of IMF of Population II stars through application to the numerous cool dwarf and giant carbon stars known, and allow us to understand the transition from the FIMF to the current-day IMF.

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Facility: LBT (MODS)

Appendix
Fitting Results for the Validation Stars

Figures A1–A3 present the fitting results for our validation stars, all of which have published high-resolution spectroscopic analyses. Figure A1 shows the fitting results of the CEMP Group likelihoods. Figures A2 and A3 show the MCMC MLE model fits of spectral features for the Group I and Group II/III stars, respectively.
CEMP - Group I

Figure A1. CEMP Group likelihoods ($\ln L$, Equation 2) for the validation stars. Likelihoods are based on the CEMP Group archetype parameters in Table 1. The symbols and color scales are the same as in Figure 2. Note that the vertical dashed line of G 77-61 is slightly hidden, as its temperature estimate is 4000 K.
Figure A2. MCMC MLE model fits (purple) of the Ca II K (left column), CH G band (center column), and C2 Swan band (right column), for the Group I validation stars: HE 1305+0132, HE 2221-0453, HE 0319-0215, and HE 0017+0055. The gray lines present the observed spectra. The gray shaded regions correspond to the wavelength range considered in each absorption feature. Purple shading about the model fit represents the inverse S/N for each feature ($\xi$), determined from maximum likelihood estimation.
Figure A3. MCMC MLE model fits of the Ca II K (left column) and CH G band (right column), for the Group II (HE 1116-0034, CS 30314–0067) and Group III (HE 1310-0536 and G 77–61) validation stars. The symbols and color scales are the same as in Figure A2.